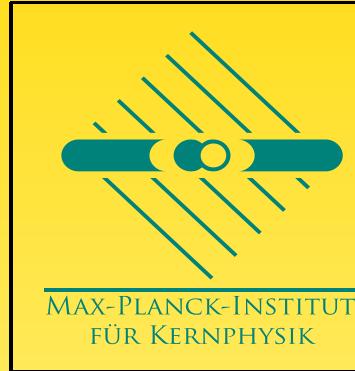


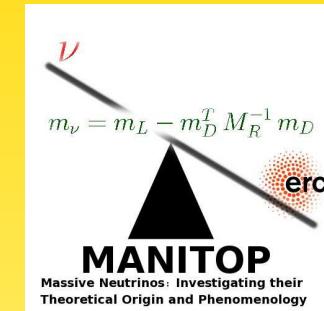
# Neutrinoless Double Beta Decay and Particle Physics



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WHEPP12

12/01/12



## Outline

$(A, Z) \rightarrow (A, Z + 2) + 2 e^- \quad (0\nu\beta\beta) \Rightarrow \text{Lepton Number Violation}$

- Introduction
- **Standard Interpretation** (neutrino physics)
- **Non-Standard Interpretations** (BSM  $\neq$  neutrino physics)

review on  $0\nu\beta\beta$  and particle physics:

W.R., Int. J. Mod. Phys. E20, 1833-1930 (2011)

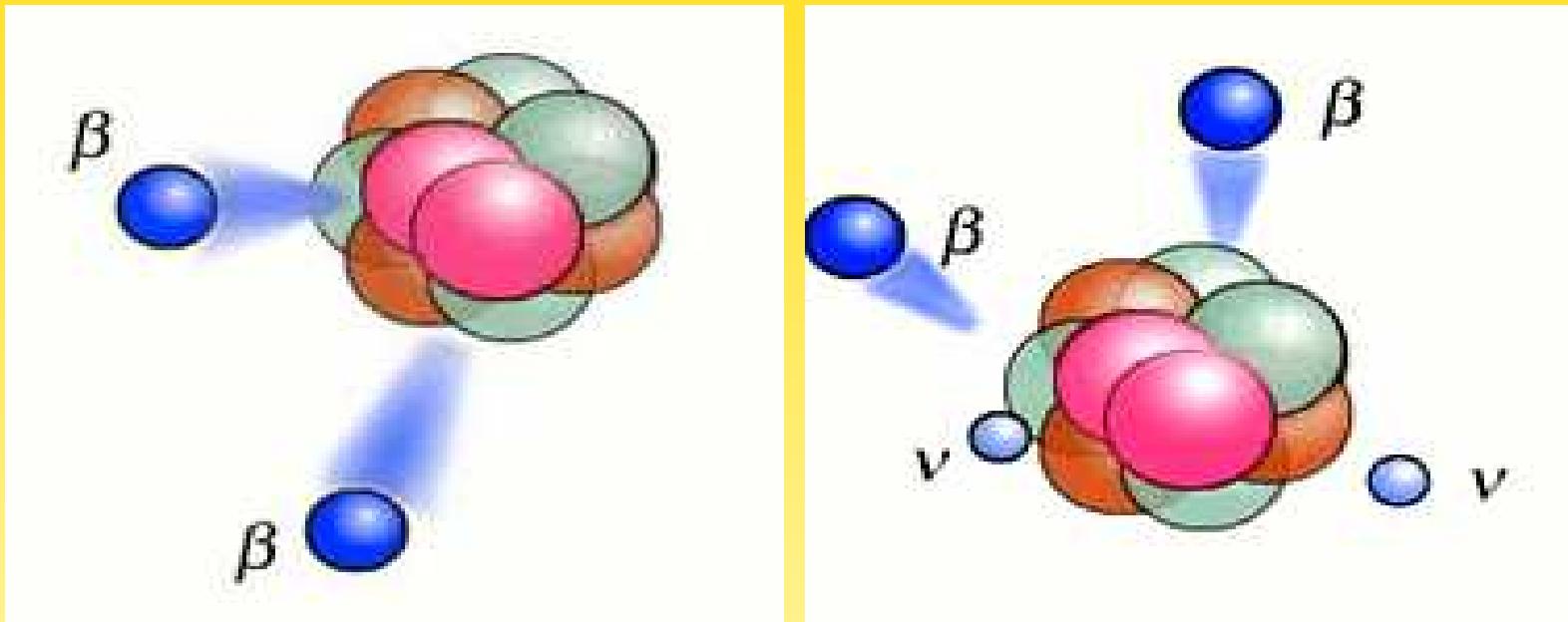
## Why should we probe Lepton Number Violation (LNV)?

- $L$  and  $B$  accidentally conserved in SM
- effective theory:  $\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}_{\text{LNV}} + \frac{1}{\Lambda^2} \mathcal{L}_{\text{LFV, BNV, LNV}} + \dots$
- baryogenesis:  $B$  is violated
- $B, L$  often connected in GUTs
- GUTs have seesaw and Majorana neutrinos
- (chiral anomalies:  $\partial_\mu J_{B,L}^\mu = c G_{\mu\nu} \tilde{G}^{\mu\nu} \neq 0$  with  $J_\mu^B = \sum \bar{q}_i \gamma_\mu q_i$  and  $J_\mu^L = \sum \bar{\ell}_i \gamma_\mu \ell_i$ )

⇒ Lepton Number Violation as important as Baryon Number Violation  
( $0\nu\beta\beta$  is much more than a neutrino mass experiment)

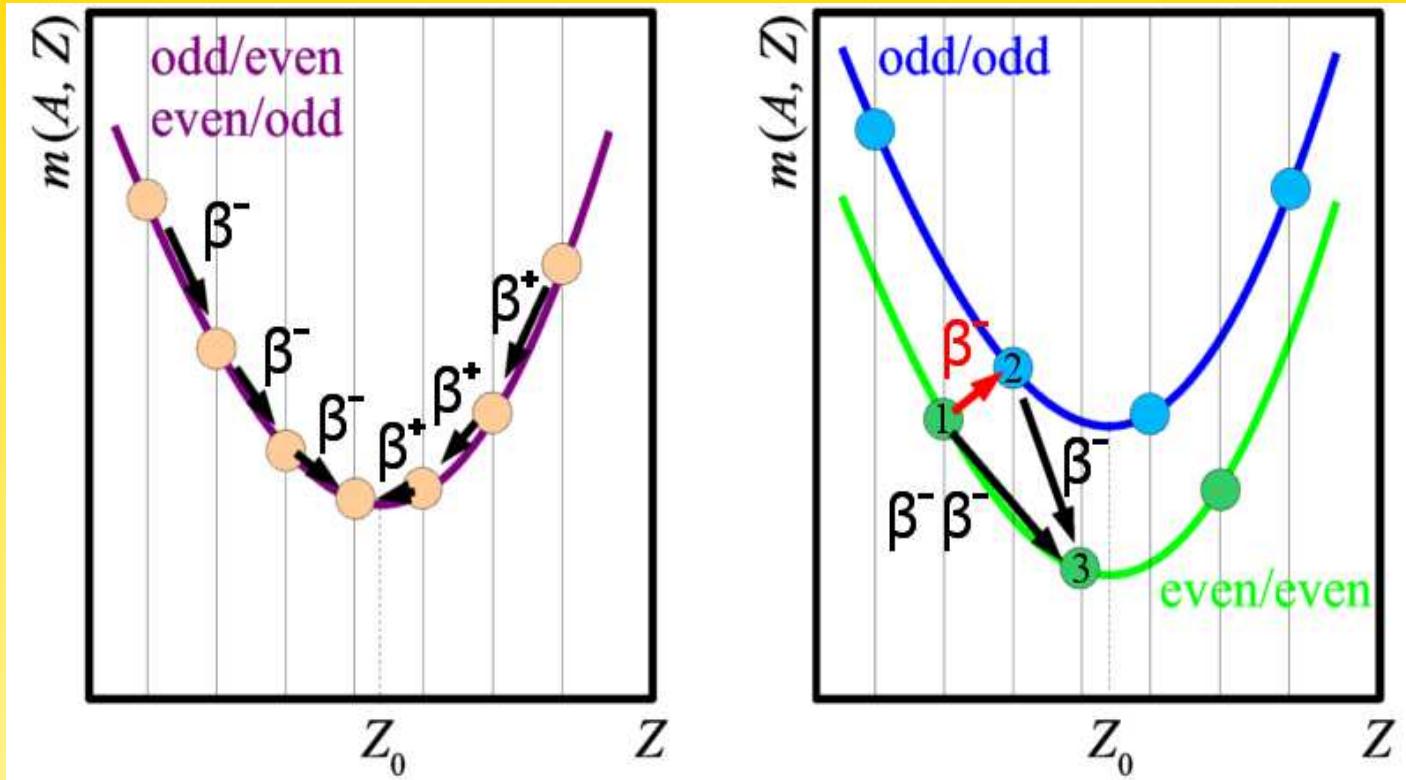
## What is Neutrinoless Double Beta Decay?

$$(A, Z) \rightarrow (A, Z + 2) + 2 e^- \quad (0\nu\beta\beta)$$



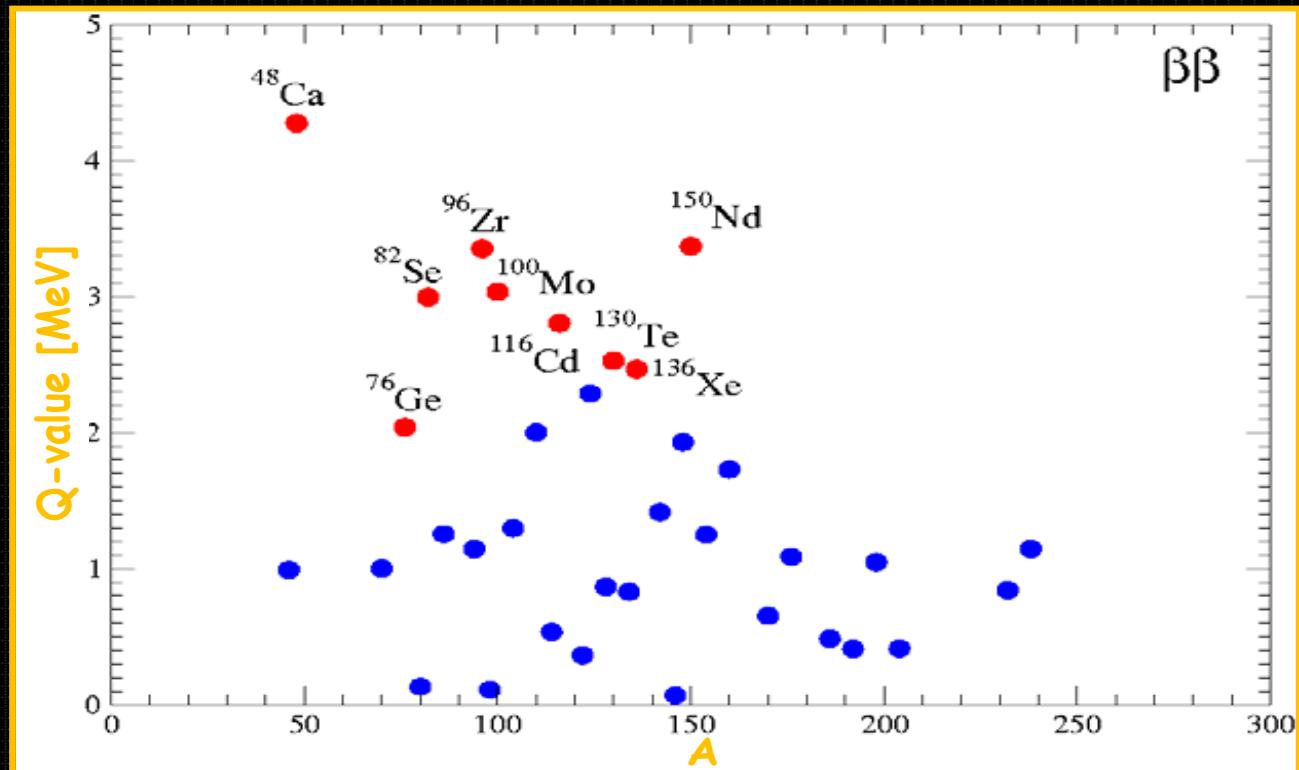
- second order in weak interaction:  $\Gamma \propto G_F^4 \Rightarrow$  rare!
- not to be confused with  $(A, Z) \rightarrow (A, Z + 2) + 2 e^- + 2 \bar{\nu}_e \quad (2\nu\beta\beta)$   
(which occurs more often but is still rare)

Need to forbid single  $\beta$  decay:



- $E_{\text{Bindung}} = E_{\text{Volumen}} - E_{\text{Oberfläche}} - E_{\text{Coulomb}} - E_{\text{Symmetrie}} \pm E_{\text{Paarbildung}}$
- $\Rightarrow \text{even/even} \rightarrow \text{even/even}$
- either direct ( $0\nu\beta\beta$ ) or two simultaneous decays with virtual (energetically forbidden) intermediate state ( $2\nu\beta\beta$ )

# How many nuclei in this condition?



Slide by A. Giuliani

## Upcoming experiments: exciting time!!

current best limit is from 2001...

Name	Isotope	source = detector; calorimetric with			source $\neq$ detector event topology
		high energy res.	low energy res.	event topology	
CANDLES	$^{48}\text{Ca}$	–	✓	–	–
COBRA	$^{116}\text{Cd}$ (and $^{130}\text{Te}$ )	–	–	✓	–
CUORE	$^{130}\text{Te}$	✓	–	–	–
DCBA	$^{82}\text{Se}$ or $^{150}\text{Nd}$	–	–	–	✓
EXO	$^{136}\text{Xe}$	–	–	✓	–
GERDA	$^{76}\text{Ge}$	✓	–	–	–
KamLAND-Zen	$^{136}\text{Xe}$	–	✓	–	–
LUCIFER	$^{82}\text{Se}$ or $^{100}\text{Mo}$ or $^{116}\text{Cd}$	✓	–	–	–
MAJORANA	$^{76}\text{Ge}$	✓	–	–	–
MOON	$^{82}\text{Se}$ or $^{100}\text{Mo}$ or $^{150}\text{Nd}$	–	–	–	✓
NEXT	$^{136}\text{Xe}$	–	–	✓	–
SNO+	$^{150}\text{Nd}$	–	✓	–	–
SuperNEMO	$^{82}\text{Se}$ or $^{150}\text{Nd}$	–	–	–	✓
XMASS	$^{136}\text{Xe}$	–	✓	–	–

multi-isotope determination good for 3 reasons

Experiment	Isotope	Mass of Isotope [kg]	Sensitivity $T_{1/2}^{0\nu}$ [yrs]	Status	Start of data-taking
GERDA	$^{76}\text{Ge}$	18	$3 \times 10^{25}$	running	$\sim 2011$
		40	$2 \times 10^{26}$	in progress	$\sim 2012$
		1000	$6 \times 10^{27}$	R&D	$\sim 2015$
CUORE	$^{130}\text{Te}$	200	$6.5 \times 10^{26*}$	in progress	$\sim 2013$
			$2.1 \times 10^{26}^{**}$		
MAJORANA	$^{76}\text{Ge}$	30-60	$(1 - 2) \times 10^{26}$	in progress	$\sim 2013$
		1000	$6 \times 10^{27}$	R&D	$\sim 2015$
EXO	$^{136}\text{Xe}$	200	$6.4 \times 10^{25}$	in progress	$\sim 2011$
		1000	$8 \times 10^{26}$	R&D	$\sim 2015$
SuperNEMO	$^{82}\text{Se}$	100-200	$(1 - 2) \times 10^{26}$	R&D	$\sim 2013\text{-}15$
KamLAND-Zen	$^{136}\text{Xe}$	400	$4 \times 10^{26}$	in progress	$\sim 2011$
		1000	$10^{27}$	R&D	$\sim 2013\text{-}15$
SNO+	$^{150}\text{Nd}$	56	$4.5 \times 10^{24}$	in progress	$\sim 2012$
		500	$3 \times 10^{25}$	R&D	$\sim 2015$

## Interpretation of Experiments

Master formula:

$$\Gamma^{0\nu} = G_x(Q, Z) |\mathcal{M}_x(A, Z) \eta_x|^2$$

- $G_x(Q, Z)$ : phase space factor
- $\mathcal{M}_x(A, Z)$ : nuclear physics
- $\eta_x$ : particle physics

## Interpretation of Experiments

Master formula:

$$\Gamma^{0\nu} = G_x(Q, Z) |\mathcal{M}_x(A, Z) \eta_x|^2$$

- $G_x(Q, Z)$ : phase space factor; **calculable**
- $\mathcal{M}_x(A, Z)$ : nuclear physics; **problematic**
- $\eta_x$ : particle physics; **interesting**

### 3 Reasons for Multi-isotope determination

- 1.) credibility
- 2.) test NME calculation

$$\frac{T_{1/2}^{0\nu}(A_1, Z_1)}{T_{1/2}^{0\nu}(A_2, Z_2)} = \frac{G(Q_2, Z_2)}{G(Q_1, Z_1)} \frac{|\mathcal{M}(A_2, Z_2)|^2}{|\mathcal{M}(A_1, Z_1)|^2}$$

systematic errors drop out, ratio sensitive to NME model

- 3.) test mechanism

$$\frac{T_{1/2}^{0\nu}(A_1, Z_1)}{T_{1/2}^{0\nu}(A_2, Z_2)} = \frac{G_x(Q_2, Z_2)}{G_x(Q_1, Z_1)} \frac{|\mathcal{M}_x(A_2, Z_2)|^2}{|\mathcal{M}_x(A_1, Z_1)|^2}$$

particle physics drops out, ratio of NMEs sensitive to mechanism

## Experimental Aspects

particle theory:

$$(T_{1/2}^{0\nu})^{-1} \propto (\text{particle physics})^2$$

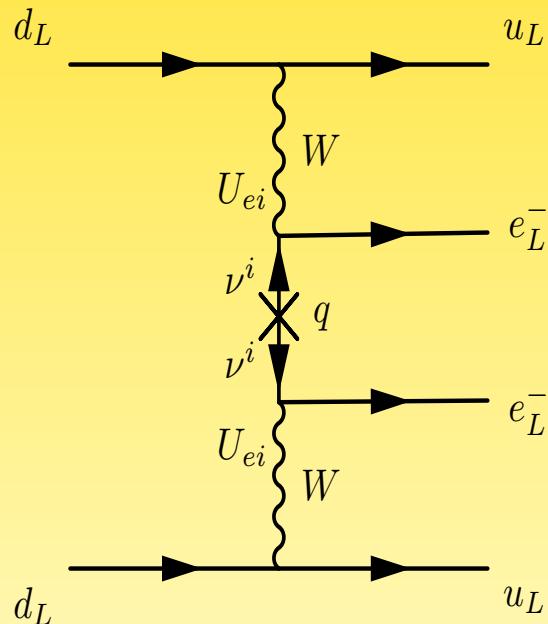
experimentally:

$$(T_{1/2}^{0\nu})^{-1} \propto \begin{cases} a M \varepsilon t & \text{without background} \\ a \varepsilon \sqrt{\frac{M t}{B \Delta E}} & \text{background-dominated} \end{cases}$$

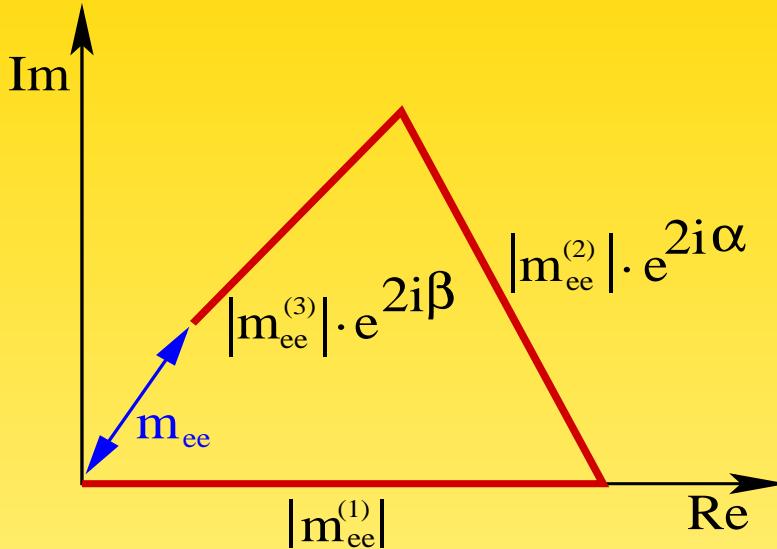
*Note: factor 2 in particle physics is combined factor of 16 in  $M \times t \times B \times \Delta E$*

## Standard Interpretation

Neutrinoless Double Beta Decay is mediated by light and massive Majorana neutrinos (the ones which oscillate) and all other mechanisms potentially leading to  $0\nu\beta\beta$  give negligible or no contribution



## $\Delta L \neq 0$ : Neutrinoless Double Beta Decay

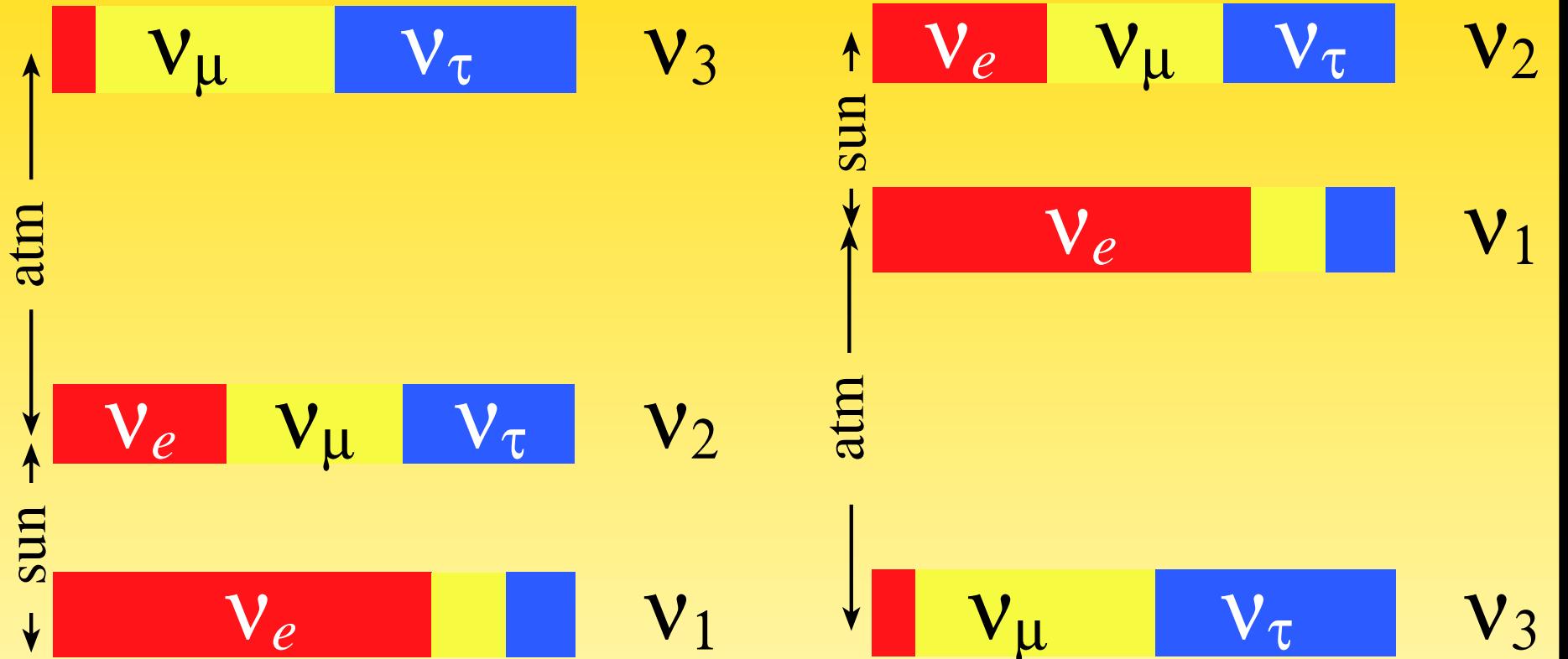


Amplitude proportional to coherent sum ("effective mass"):

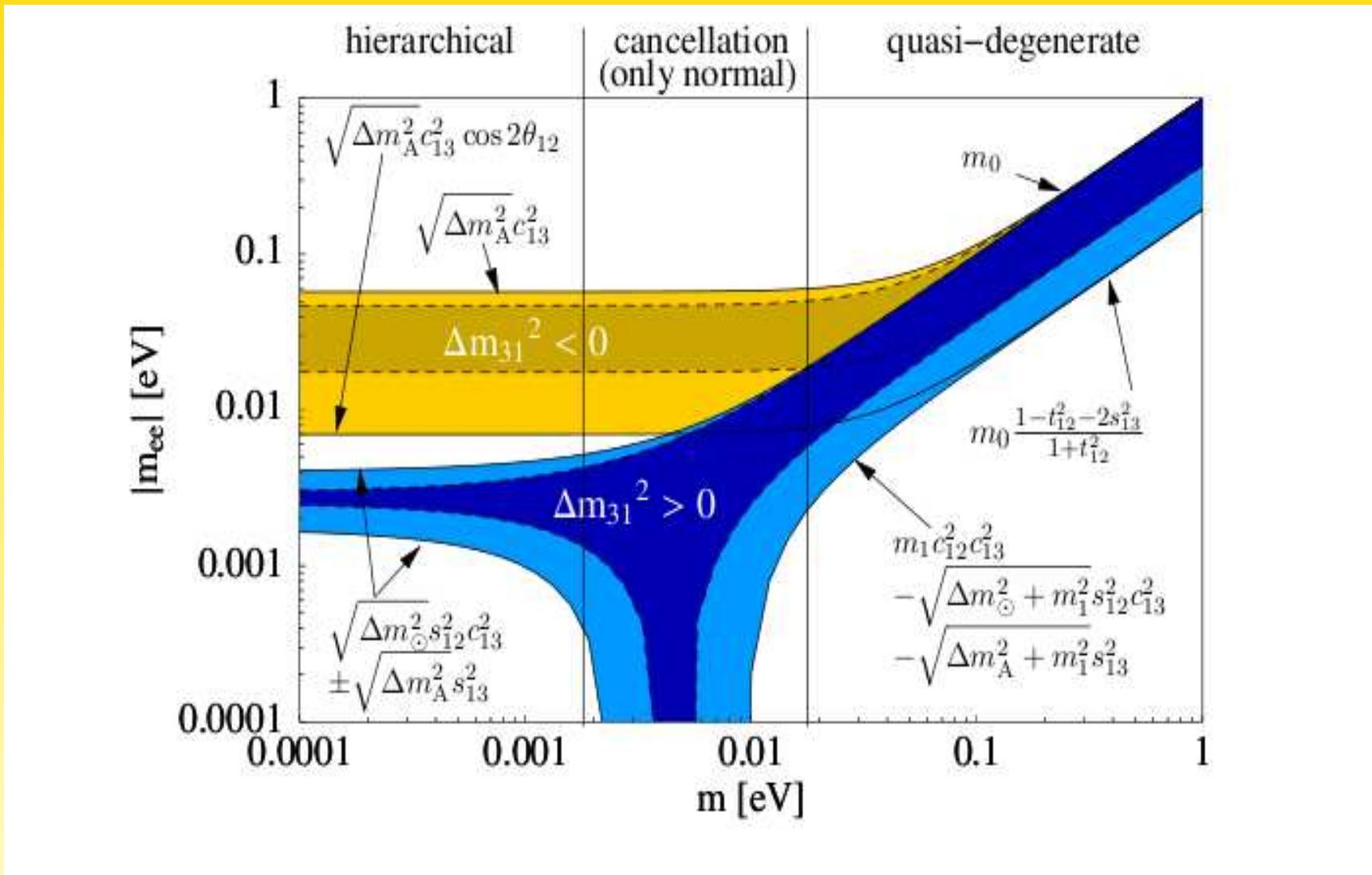
$$|m_{ee}| \equiv \left| \sum U_{ei}^2 m_i \right| = \left| |U_{e1}|^2 m_1 + |U_{e2}|^2 m_2 e^{2i\alpha} + |U_{e3}|^2 m_3 e^{2i\beta} \right|$$

$$= f(\theta_{12}, m_i, |U_{e3}|, \text{sgn}(\Delta m_A^2), \alpha, \beta)$$

7 out of 9 parameters of  $m_\nu$ !



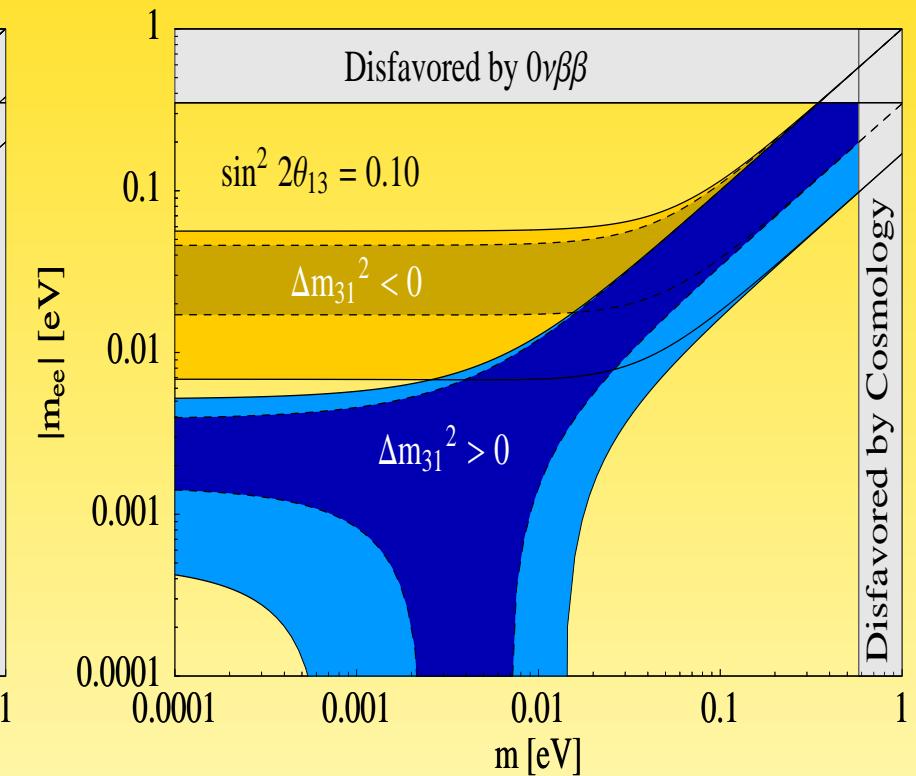
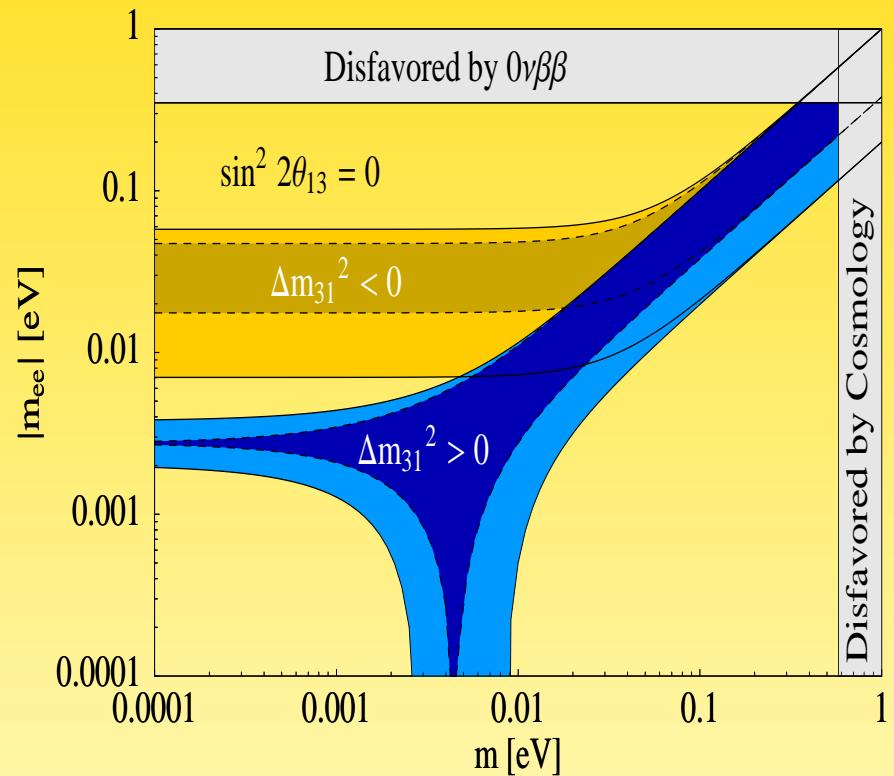
## The usual plot



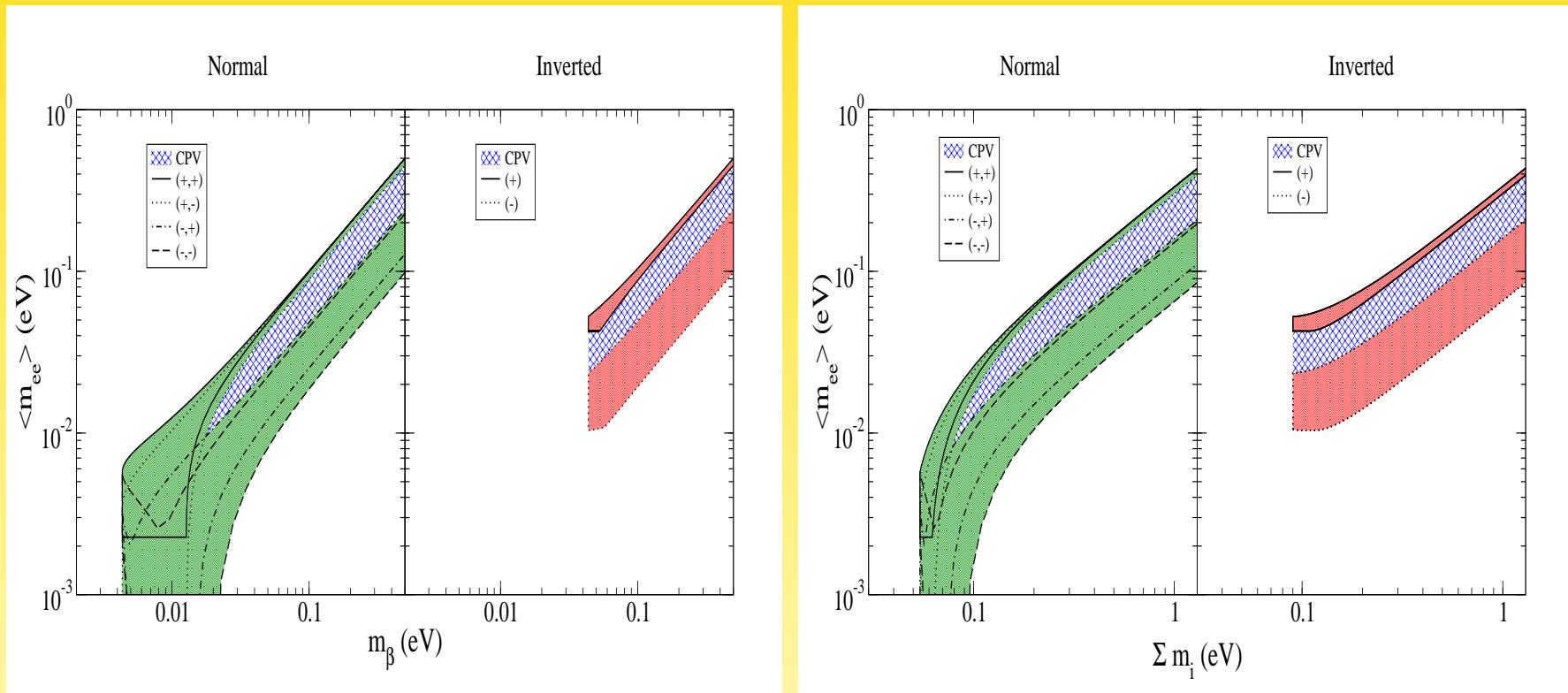
## Crucial points

- NH: can be zero!
- IH: cannot be zero!  $|m_{ee}|_{\min}^{\text{inh}} = \sqrt{\Delta m_A^2} c_{13}^2 \cos 2\theta_{12}$
- gap between  $|m_{ee}|_{\min}^{\text{inh}}$  and  $|m_{ee}|_{\max}^{\text{nor}}$
- QD: cannot be zero!  $|m_{ee}|_{\min}^{\text{QD}} = m_0 c_{13}^2 \cos 2\theta_{12}$
- QD: cannot distinguish between normal and inverted ordering

## $0\nu\beta\beta$ and $U_{e3}$



## Plot against other observables



Complementarity of  $|m_{ee}| = U_{ei}^2 m_i$ ,  $m_\beta = \sqrt{|U_{ei}|^2 m_i^2}$  and  $\Sigma = \sum m_i$

## Neutrino Mass Matrix

KATRIN			$0\nu\beta\beta$		cosmology		
	yes	no	yes	no	yes	no	
KATRIN	yes	-	-	QD + Majorana	QD + Dirac	QD	N-SC
	no	-	-	N-SI	low IH or NH or Dirac	$m_\nu \lesssim 0.1 \text{ eV}$ or N-SC	NH
$0\nu\beta\beta$	yes	+	+	-	-	(IH or QD) + Majorana	N-SC or N-SI
	no	+	+	-	-	low IH or (QD + Dirac)	NH
cosmology	yes	+	+	+	+	-	-
	no	+	+	+	+	-	-

## Which mass ordering with which life-time?

	$\Sigma$	$m_\beta$	$ m_{ee} $
NH	$\sqrt{\Delta m_A^2}$ $\simeq 0.05 \text{ eV}$	$\sqrt{\Delta m_\odot^2 +  U_{e3} ^2 \Delta m_A^2}$ $\simeq 0.01 \text{ eV}$	$\left  \sqrt{\Delta m_\odot^2 +  U_{e3} ^2 \sqrt{\Delta m_A^2} e^{2i(\alpha-\beta)}} \right $ $\sim 0.003 \text{ eV} \Rightarrow T_{1/2}^{0\nu} \gtrsim 10^{28-29} \text{ yrs}$
IH	$2\sqrt{\Delta m_A^2}$ $\simeq 0.1 \text{ eV}$	$\sqrt{\Delta m_A^2}$ $\simeq 0.05 \text{ eV}$	$\sqrt{\Delta m_A^2} \sqrt{1 - \sin^2 2\theta_{12} \sin^2 \alpha}$ $\sim 0.03 \text{ eV} \Rightarrow T_{1/2}^{0\nu} \gtrsim 10^{26-27} \text{ yrs}$
QD	$3m_0$	$m_0$	$m_0 \sqrt{1 - \sin^2 2\theta_{12} \sin^2 \alpha}$ $\gtrsim 0.1 \text{ eV} \Rightarrow T_{1/2}^{0\nu} \gtrsim 10^{25-26} \text{ yrs}$

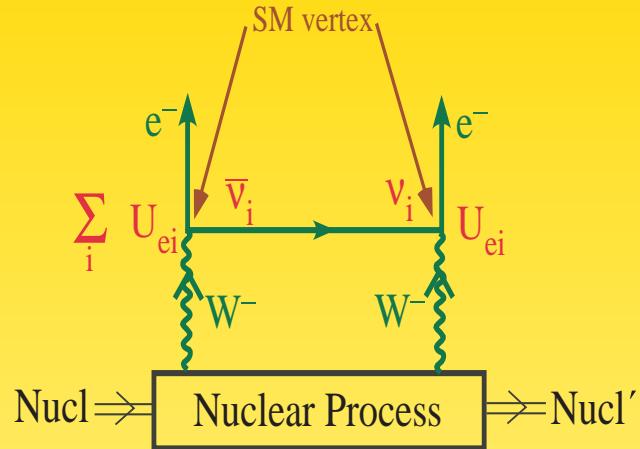
(for  $10^{26}$  yrs you need  $10^{26}$  atoms, which are  $10^3$  mols, which are 100 kg)

## From life-time to particle physics: Nuclear Matrix Elements



*Dark Lord Of The Sith b5* © 88, 1999 Star Wars: Ord Mantell, [www.starwars.priv.pl](http://www.starwars.priv.pl)

## From life-time to particle physics: Nuclear Matrix Elements



- 2 point-like Fermi vertices; “long-range” neutrino exchange; momentum exchange  $q \simeq 1/r \simeq 0.1$  GeV
- NME  $\leftrightarrow$  overlap of decaying nucleons...
- different approaches (QRPA, NSM, IBM, GCM, pHFB) imply uncertainty
- plus uncertainty due to model details
- plus convention issues (Cowell, PRC 73; Smolnikov, Grabmayr, PRC 81; Dueck, W.R., Zuber, PRD 83)

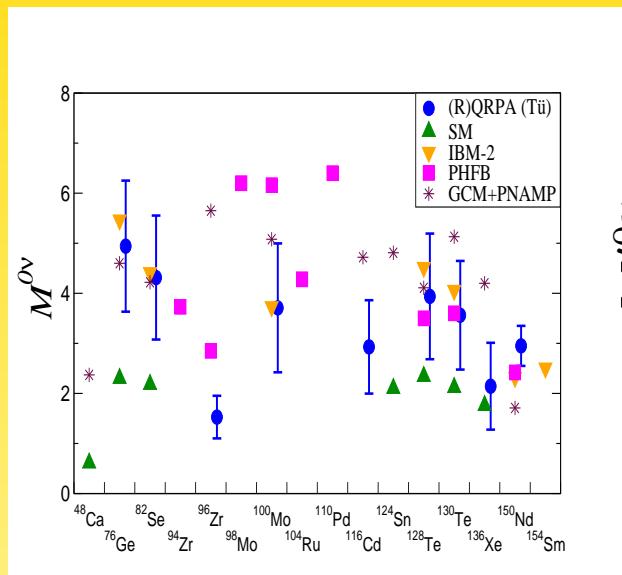
typical model for NME: set of single particle states with a number of possible wave function configurations; solve  $\mathcal{H}$  in a mean background field

- Quasi-particle Random Phase Approximation (QRPA) (many single particle states, few configurations)
- Nuclear Shell Model (NSM) (many configurations, few single particle states)
- Interacting Boson Model (IBM) (many single particle states, few configurations) (many single particle states, few configurations)
- Generating Coordinate Method (GCM) (many single particle states, few configurations)
- projected Hartree-Fock-Bogoliubov model (pHFB)

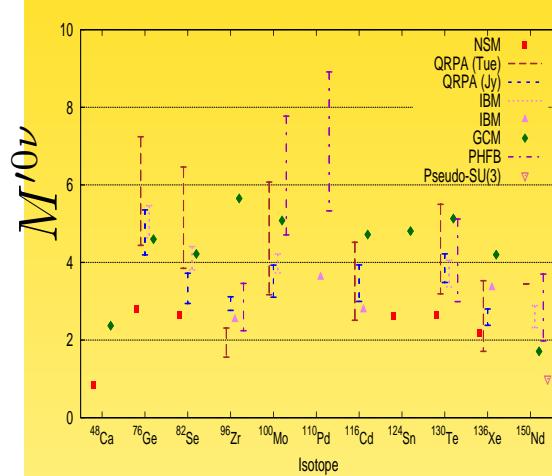
tends to overestimate NMEs

tends to underestimate NMEs

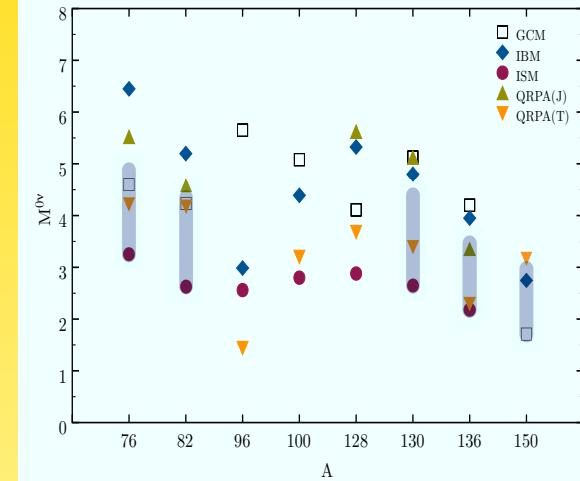
# From life-time to particle physics: Nuclear Matrix Elements



Faessler, 1104.3700

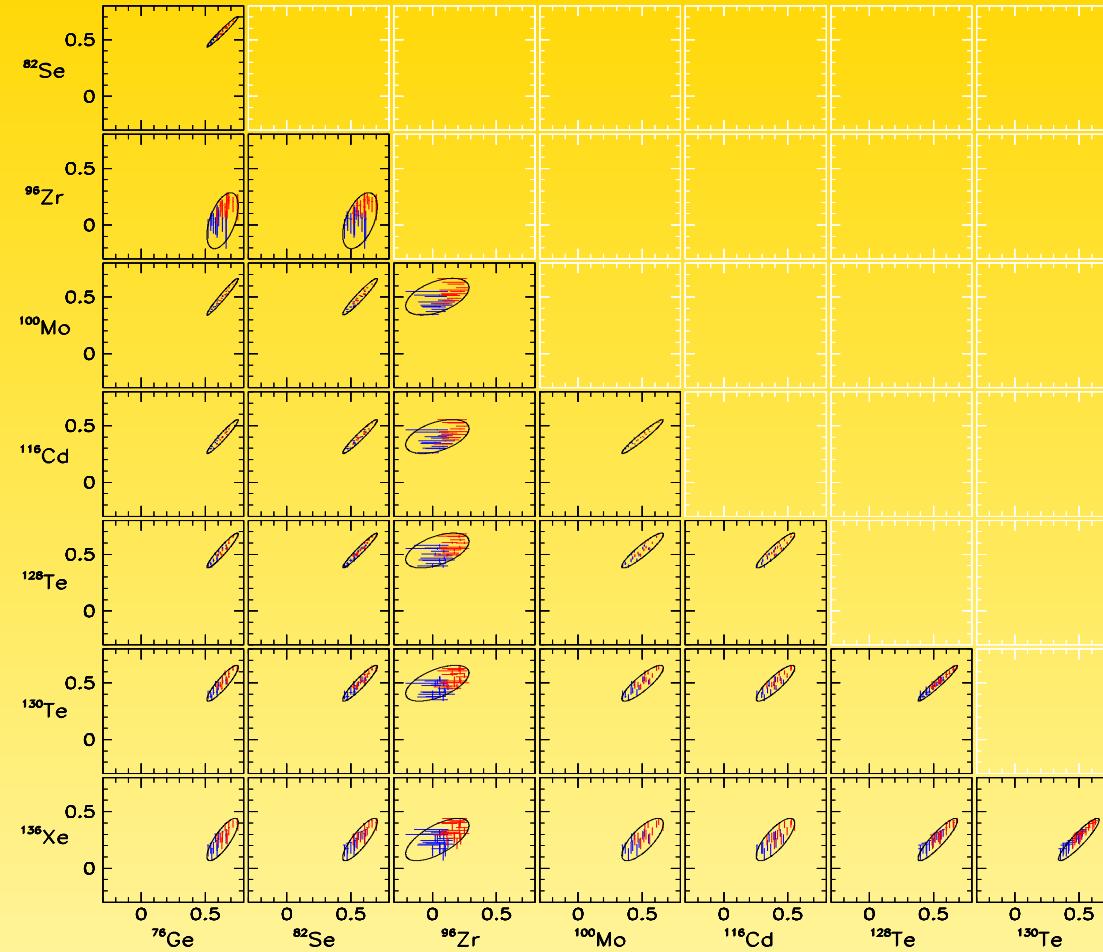


Dueck, W.R., Zuber, PRD 83



Gomez-Cadenas et al., 1109.5515

to better estimate error range: correlations need to be understood



Faessler, Fogli *et al.*, PRD 79

ellipse major axis: SRC (blue, red) and  $g_A$

ellipse minor axis:  $g_{pp}$

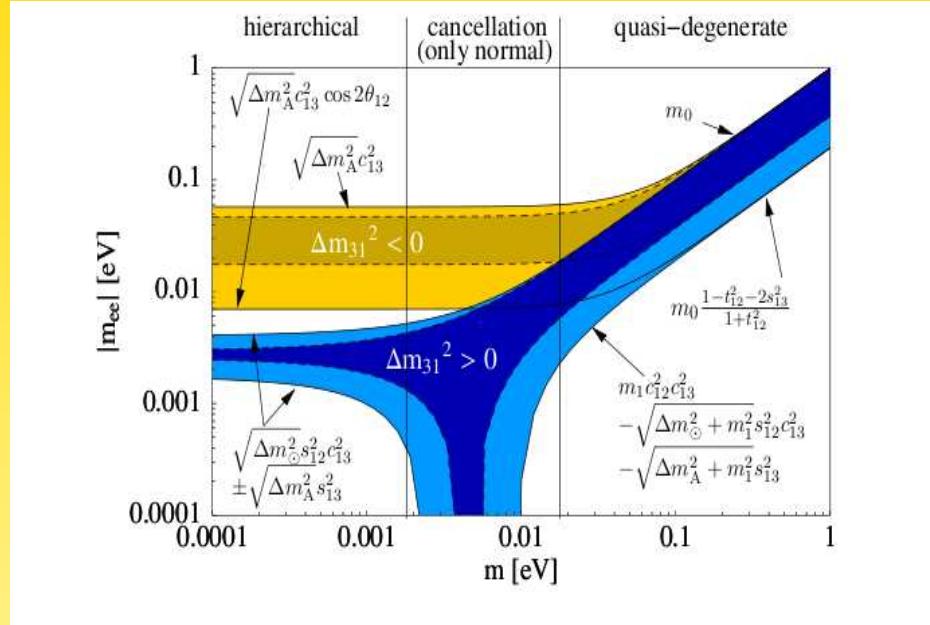
## $0\nu\beta\beta$ and Neutrino physics

Isotope	$T_{1/2}^{0\nu}$ [yrs]	Experiment	$ m_{ee} _{\min}^{\lim}$ [eV]	$ m_{ee} _{\max}^{\lim}$ [eV]
$^{48}\text{Ca}$	$5.8 \times 10^{22}$	CANDLES	3.55	9.91
$^{76}\text{Ge}$	$1.9 \times 10^{25}$	HDM	0.21	<b>0.53</b>
	$1.6 \times 10^{25}$	IGEX	0.25	0.63
$^{82}\text{Se}$	$3.2 \times 10^{23}$	NEMO-3	0.85	2.08
$^{96}\text{Zr}$	$9.2 \times 10^{21}$	NEMO-3	3.97	14.39
$^{100}\text{Mo}$	$1.0 \times 10^{24}$	NEMO-3	0.31	0.79
$^{116}\text{Cd}$	$1.7 \times 10^{23}$	SOLOTVINO	1.22	2.30
$^{130}\text{Te}$	$2.8 \times 10^{24}$	CUORICINO	0.27	0.57
$^{136}\text{Xe}$	$5.0 \times 10^{23}$	DAMA	0.83	2.04
$^{150}\text{Nd}$	$1.8 \times 10^{22}$	NEMO-3	2.35	5.08

Experiment	Isotope	Mass of Isotope [kg]	Sensitivity $T_{1/2}^{0\nu}$ [yrs]	Status	Start of data-taking	Sensitivity $\langle m_\nu \rangle$ [eV]
GERDA	$^{76}\text{Ge}$	18	$3 \times 10^{25}$	running	$\sim 2011$	0.17-0.42
		40	$2 \times 10^{26}$			0.06-0.16
		1000	$6 \times 10^{27}$	R&D	$\sim 2015$	0.012-0.030
CUORE	$^{130}\text{Te}$	200	$6.5 \times 10^{26}^*$	in progress	$\sim 2013$	0.018-0.037
			$2.1 \times 10^{26}^{**}$			0.03-0.066
MAJORANA	$^{76}\text{Ge}$	30-60	$(1 - 2) \times 10^{26}$	in progress	$\sim 2013$	0.06-0.16
		1000	$6 \times 10^{27}$			0.012-0.030
EXO	$^{136}\text{Xe}$	200	$6.4 \times 10^{25}$	in progress	$\sim 2011$	0.073-0.18
		1000	$8 \times 10^{26}$			0.02-0.05
SuperNEMO	$^{82}\text{Se}$	100-200	$(1 - 2) \times 10^{26}$	R&D	$\sim 2013\text{-}15$	0.04-0.096
KamLAND-Zen	$^{136}\text{Xe}$	400	$4 \times 10^{26}$	in progress	$\sim 2011$	0.03-0.07
		1000	$10^{27}$			0.02-0.046
SNO+	$^{150}\text{Nd}$	56	$4.5 \times 10^{24}$	in progress	$\sim 2012$	0.15-0.32
		500	$3 \times 10^{25}$			0.06-0.12

Note: with *same* lifetime:  $^{150}\text{Nd}$  and  $^{100}\text{Mo}$  do best...

## Inverted Ordering

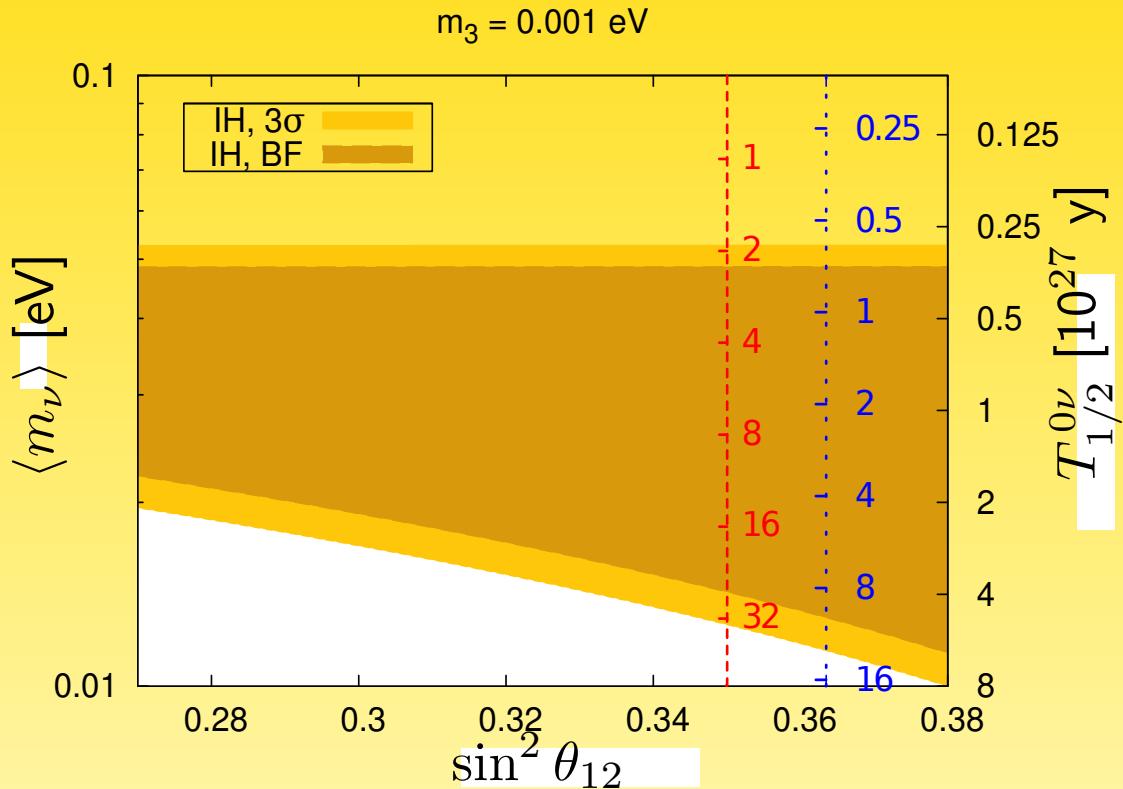


Nature provides 2 scales:

$$\langle m_\nu \rangle_{\max}^{\text{IH}} \simeq c_{13}^2 \sqrt{\Delta m_A^2} \quad \text{and} \quad \langle m_\nu \rangle_{\min}^{\text{IH}} \simeq c_{13}^2 \sqrt{\Delta m_A^2} \cos 2\theta_{12}$$

requires  $\mathcal{O}(10^{26} \dots 10^{27})$  yrs

## Ruling out Inverted Hierarchy



Dueck, W.R., Zuber, PRD **83**

## Ruling out Inverted Hierarchy

$$|m_{ee}|_{\min}^{\text{IH}} = (1 - |U_{e3}|^2) \sqrt{|\Delta m_A^2|} (1 - 2 \sin^2 \theta_{12}) = \begin{cases} (0.015 \dots 0.020) \text{ eV} & 1\sigma \\ (0.010 \dots 0.024) \text{ eV} & 3\sigma \end{cases}$$

- small  $|U_{e3}|$
- large  $|\Delta m_A^2|$
- small  $\sin^2 \theta_{12}$

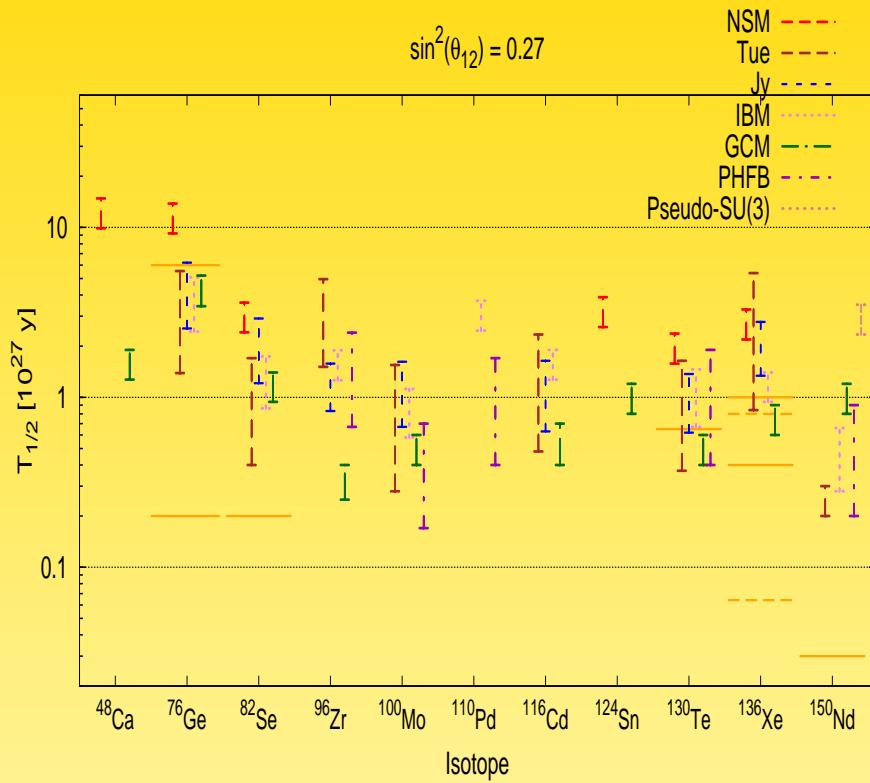
Current  $3\sigma$  range of  $\sin^2 \theta_{12}$  gives factor of 2 uncertainty for  $|m_{ee}|_{\min}^{\text{IH}}$

$\Rightarrow$  combined factor of 16 in  $M \times t \times B \times \Delta E$

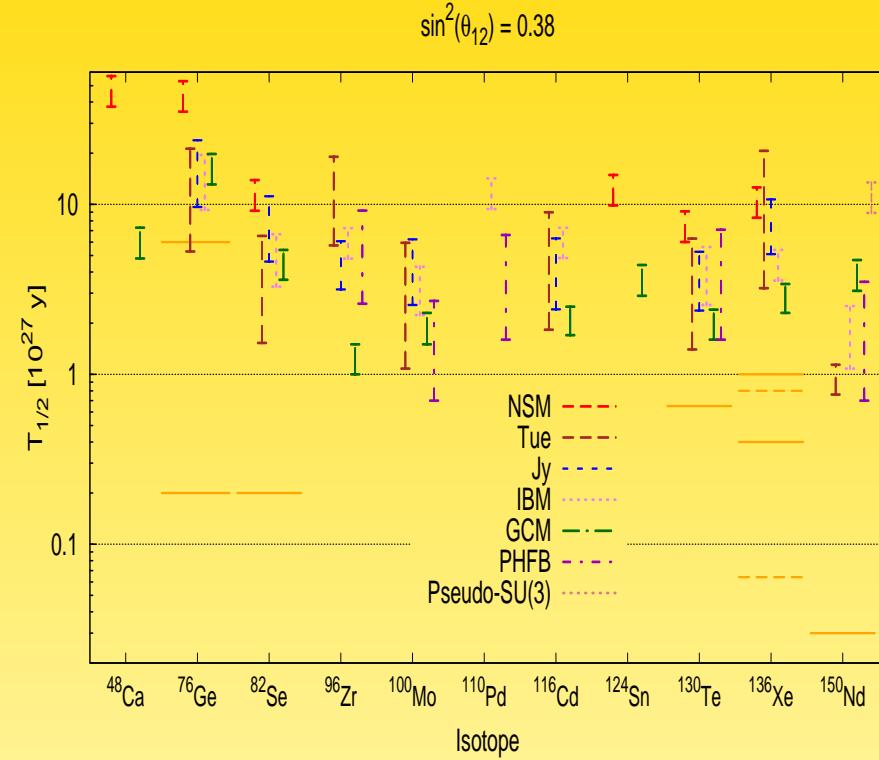
$\Rightarrow$  need precision determination of  $\theta_{12}$

Dueck, W.R., Zuber, PRD 83

## Ruling out Inverted Hierarchy



$$\sin^2 \theta_{12} = 0.27$$



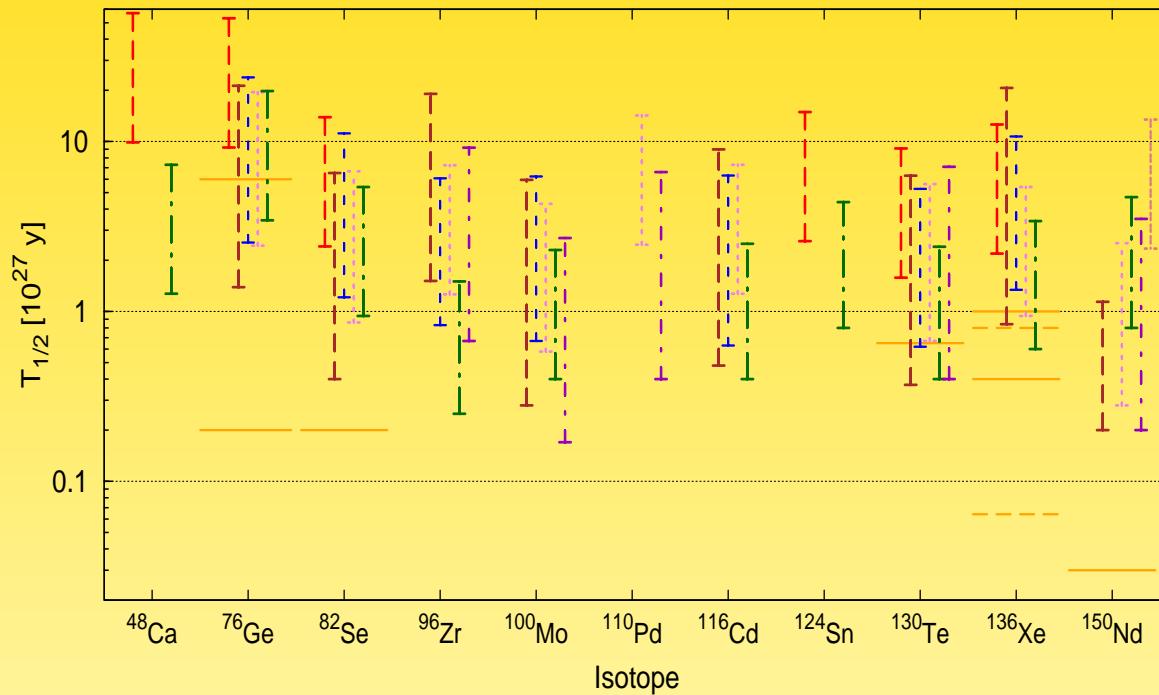
$$\sin^2 \theta_{12} = 0.38$$

spread due to NMEs **and due to  $\theta_{12}$ !!**

Note:  $^{100}\text{Mo}$  and  $^{150}\text{Nd}$  do best...

## Ruling out Inverted Hierarchy

$$0.27 < \sin^2(\theta_{12}) < 0.38$$

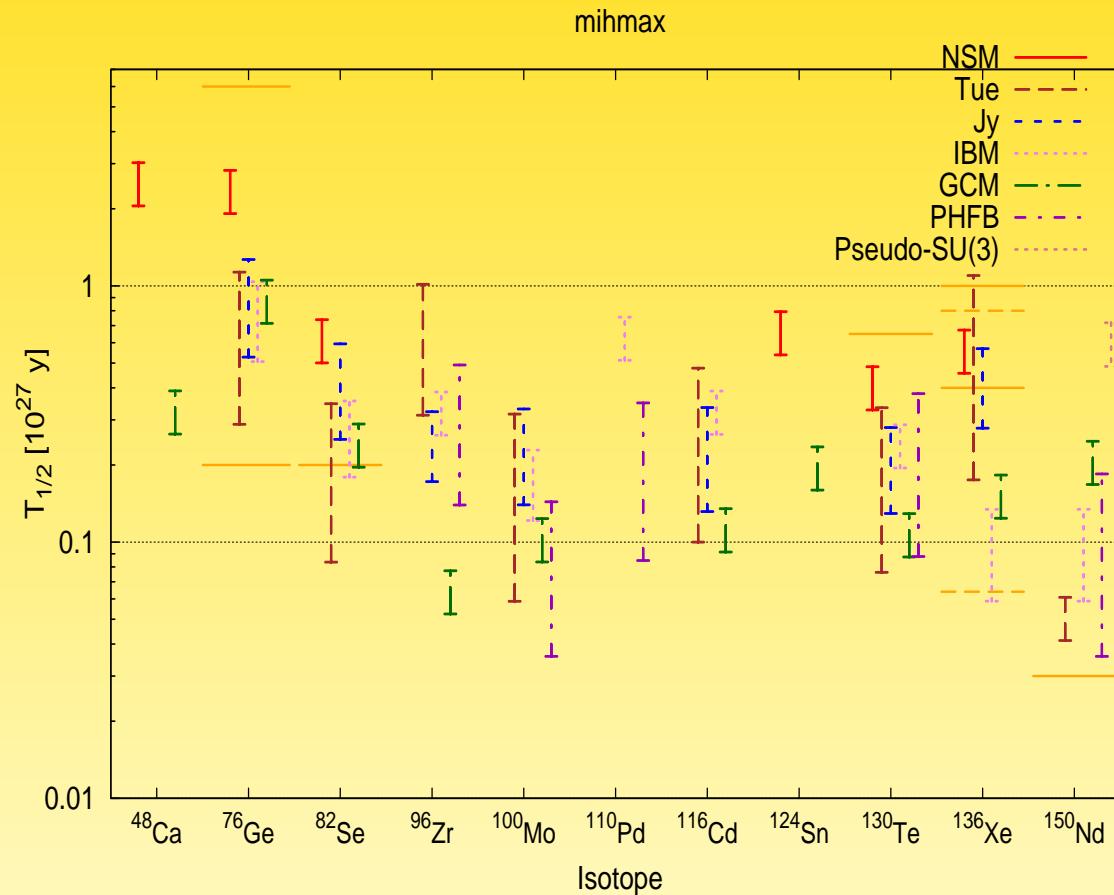


spread due to NMEs **and due to  $\theta_{12}$ !!**

Note:  $^{100}\text{Mo}$  and  $^{150}\text{Nd}$  do best...

# Testing Inverted Hierarchy

## lifetime to enter the IH regime



## Tri-bimaximal Mixing

$$U_{\text{TBM}} = \begin{pmatrix} \sqrt{\frac{2}{3}} & \sqrt{\frac{1}{3}} & 0 \\ -\sqrt{\frac{1}{6}} & \sqrt{\frac{1}{3}} & -\sqrt{\frac{1}{2}} \\ -\sqrt{\frac{1}{6}} & \sqrt{\frac{1}{3}} & \sqrt{\frac{1}{2}} \end{pmatrix}$$

Harrison, Perkins, Scott (2002)

with mass matrix

$$(m_\nu)_{\text{TBM}} = U_{\text{TBM}}^* m_\nu^{\text{diag}} U_{\text{TBM}}^\dagger = \begin{pmatrix} A & B & B \\ \cdot & \frac{1}{2}(A + B + D) & \frac{1}{2}(A + B - D) \\ \cdot & \cdot & \frac{1}{2}(A + B + D) \end{pmatrix}$$

$$A = \frac{1}{3} (2m_1 + m_2 e^{-2i\alpha}) , \quad B = \frac{1}{3} (m_2 e^{-2i\alpha} - m_1) , \quad D = m_3 e^{-2i\beta}$$

$\Rightarrow$  Flavor symmetries...

## Flavor Symmetry Models

suppose your model predicts TBM:

$$(m_\nu)_{\text{TBM}} = \begin{pmatrix} x & y & y \\ \cdot & z+x & y-z \\ \cdot & \cdot & z+x \end{pmatrix}$$

$$m_1 = x - y , \quad m_2 = x + 2y , \quad m_3 = x - y + 2z$$

if  $z = y + x/2$ :

$$m_1 = x - y , \quad m_2 = x + 2y , \quad m_3 = 2x + y$$

and one has a neutrino mass sum-rule

$$m_1 + m_2 = m_3$$

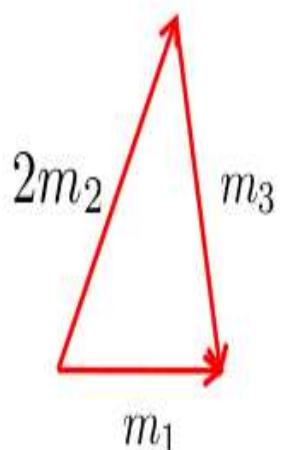
# The Zoo (of $A_4$ models)

Type	$L_i$	$\ell_i^c$	$\nu_i^c$	$\Delta$	References
A1				-	[1–14] [15] <sup>#</sup>
A2	$\underline{3}$	$\underline{1}, \underline{1}', \underline{1}''$	-	$\underline{1}, \underline{1}', \underline{1}'', \underline{3}$	[16–18]
A3				$\underline{1}, \underline{3}$	[19]
B1	$\underline{3}$	$\underline{1}, \underline{1}', \underline{1}''$	$\underline{3}$	-	[4, 20–27] <sup>#</sup> [28–30]* [31–45]
B2				$\underline{1}, \underline{3}$	[46] <sup>#</sup>
C1				-	[2, 47, 48]
C2	$\underline{3}$	$\underline{3}$	-	$\underline{1}$	[49, 50] [51] <sup>#</sup>
C3				$\underline{1}, \underline{3}$	[52]
C4				$\underline{1}, \underline{1}', \underline{1}'', \underline{3}$	[53]
D1				-	[54, 55] <sup>#</sup> [56, 57]* [58]
D2	$\underline{3}$	$\underline{3}$	$\underline{3}$	$\underline{1}$	[59] [60]*
D3				$\underline{1}'$	[61]*
D4				$\underline{1}', \underline{3}$	[62]*
E	$\underline{3}$	$\underline{3}$	$\underline{1}, \underline{1}', \underline{1}''$	-	[63, 64]
F	$\underline{1}, \underline{1}', \underline{1}''$	$\underline{3}$	$\underline{3}$	$\underline{1}$ or $\underline{1}'$	[65]
G	$\underline{3}$	$\underline{1}, \underline{1}', \underline{1}''$	$\underline{1}, \underline{1}', \underline{1}''$	-	[66]
H	$\underline{3}$	$\underline{1}, \underline{1}, \underline{1}$	-	-	[67]
I	$\underline{3}$	$\underline{1}, \underline{1}, \underline{1}$	$\underline{1}, \underline{1}, \underline{1}$	-	[68]*
J	$\underline{3}$	$\underline{1}, \underline{1}, \underline{1}$	$\underline{3}$	-	[12, 39, 69, 70]
K	$\underline{3}$	$\underline{1}, \underline{1}, \underline{1}$	$\underline{1}, \underline{1}$	$\underline{1}$	[71]*
L	$\underline{3}$	$\underline{1}, \underline{1}, \underline{1}$	$\underline{1}$	-	[72]*
M	$\underline{1}, \underline{1}', \underline{1}''$	$\underline{1}, \underline{1}'', \underline{1}'$	$\underline{3}, \underline{1}$	-	[73, 74]
N	$\underline{1}, \underline{1}', \underline{1}''$	$\underline{1}, \underline{1}'', \underline{1}'$	$\underline{3}, \underline{1}', \underline{1}''$	-	[75]

Barry, W.R., PRD **81**, updated regularly on

[http://www.mpi-hd.mpg.de/personalhomes/jamesb/Table\\_A4.pdf](http://www.mpi-hd.mpg.de/personalhomes/jamesb/Table_A4.pdf)

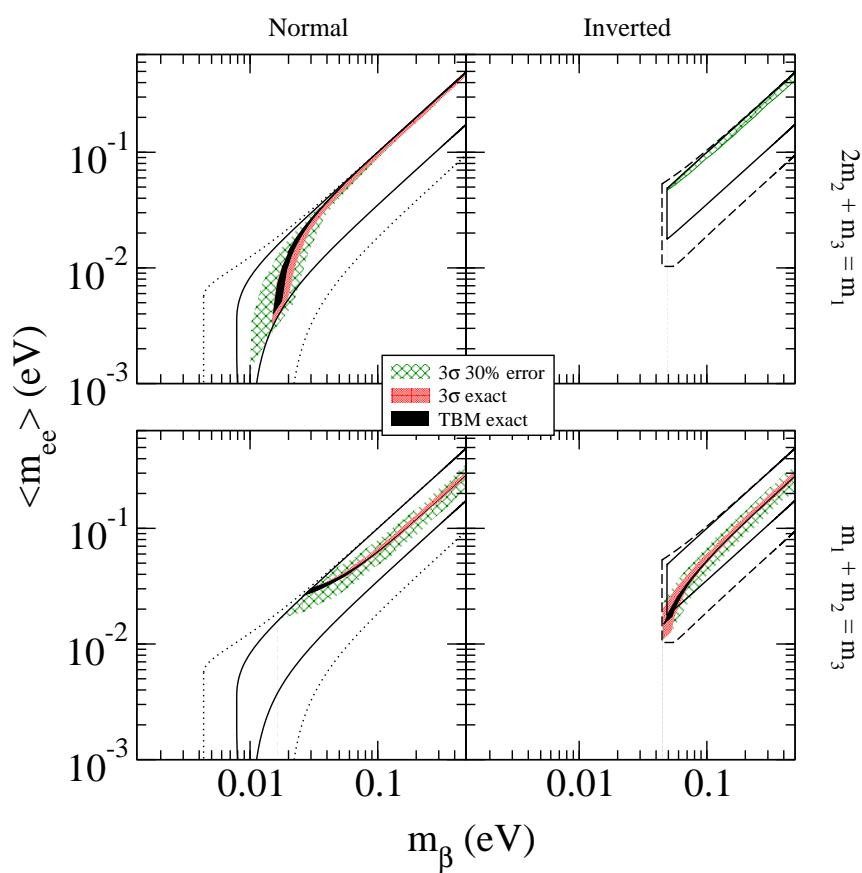
## Sum-rules in Models and $0\nu\beta\beta$



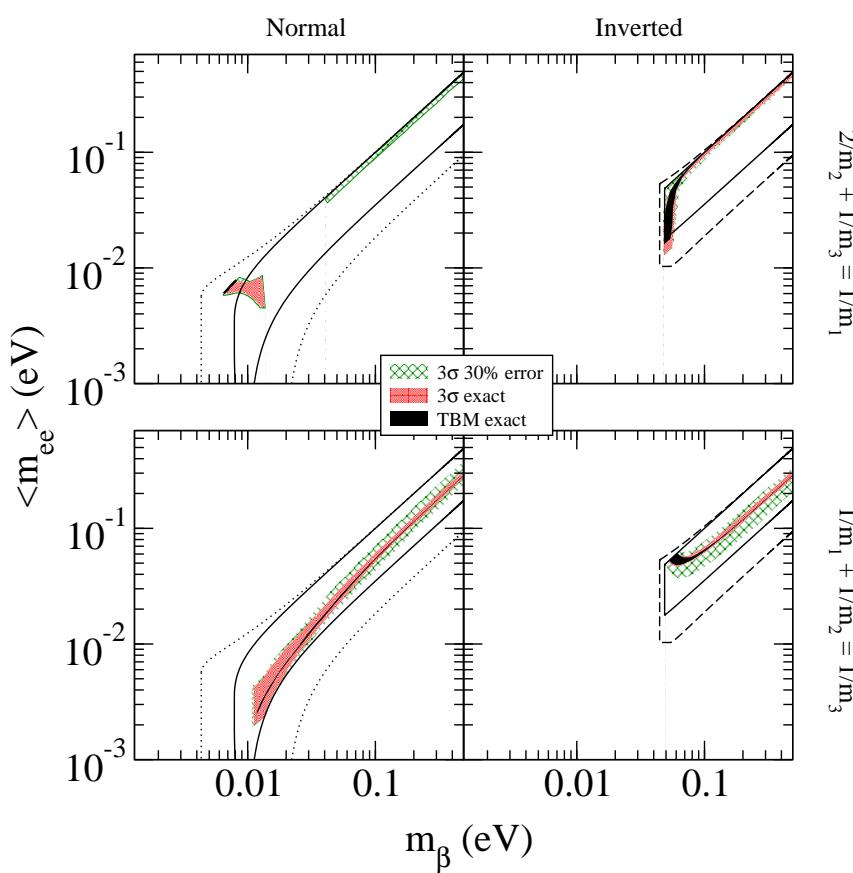
Sum-rule	Flavour symmetry
$2m_2 + m_3 = m_1$	$A_4, T', (S_4)$
$m_1 + m_2 = m_3$	$S_4, (A_4)$
$\frac{2}{m_2} + \frac{1}{m_3} = \frac{1}{m_1}$	$A_4, T'$
$\frac{1}{m_1} + \frac{1}{m_2} = \frac{1}{m_3}$	$S_4$

constrains masses and Majorana phases

Barry, W.R., NPB **842**



$$2m_2 + m_3 = m_1 \quad m_1 + m_2 = m_3$$



$$2/m_2 + 1/m_3 = 1/m_1$$

$$1/m_1 + 1/m_2 = 1/m_3$$

$$m_1 + m_2 - m_3 = \epsilon m_{\max}$$

stable: new solutions not before  $\epsilon \simeq 0.2$

## Sterile Neutrinos??

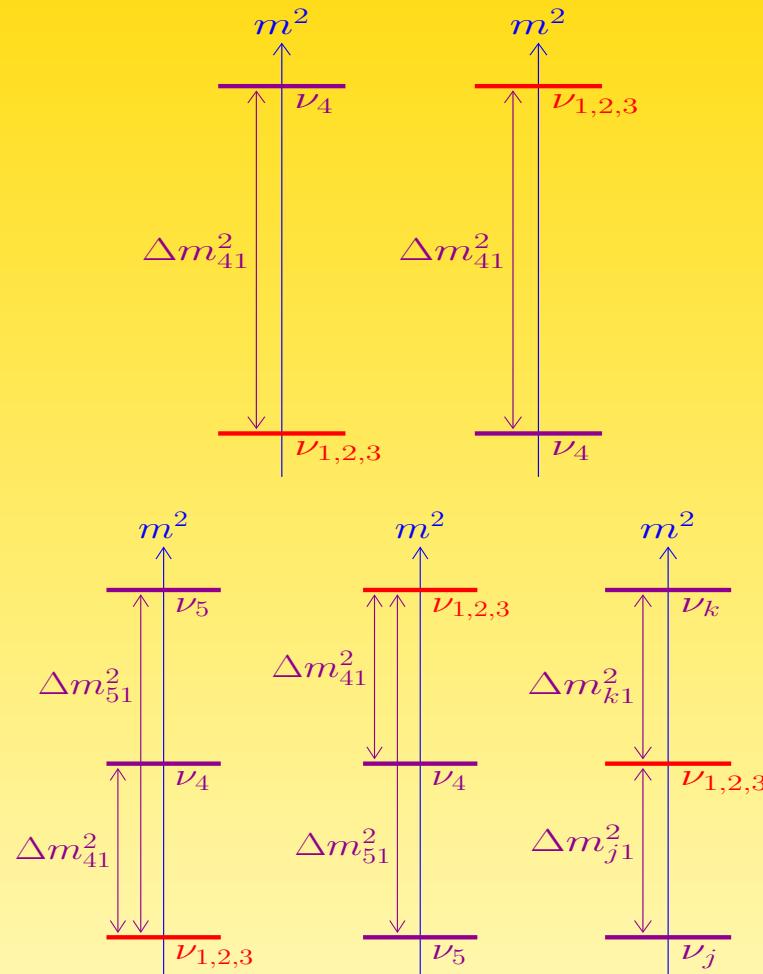
- LSND/MiniBooNE
- cosmology
- BBN
- $r$ -process nucleosynthesis in Supernovae
- reactor anomaly ([Mention et al., PRD 83](#))

	$\Delta m_{41}^2$ [eV $^2$ ]	$ U_{e4} $	$ U_{\mu 4} $	$\Delta m_{51}^2$ [eV $^2$ ]	$ U_{e5} $	$ U_{\mu 5} $
3+2/2+3	0.47	0.128	0.165	0.87	0.138	0.148
1+3+1	0.47	0.129	0.154	0.87	0.142	0.163

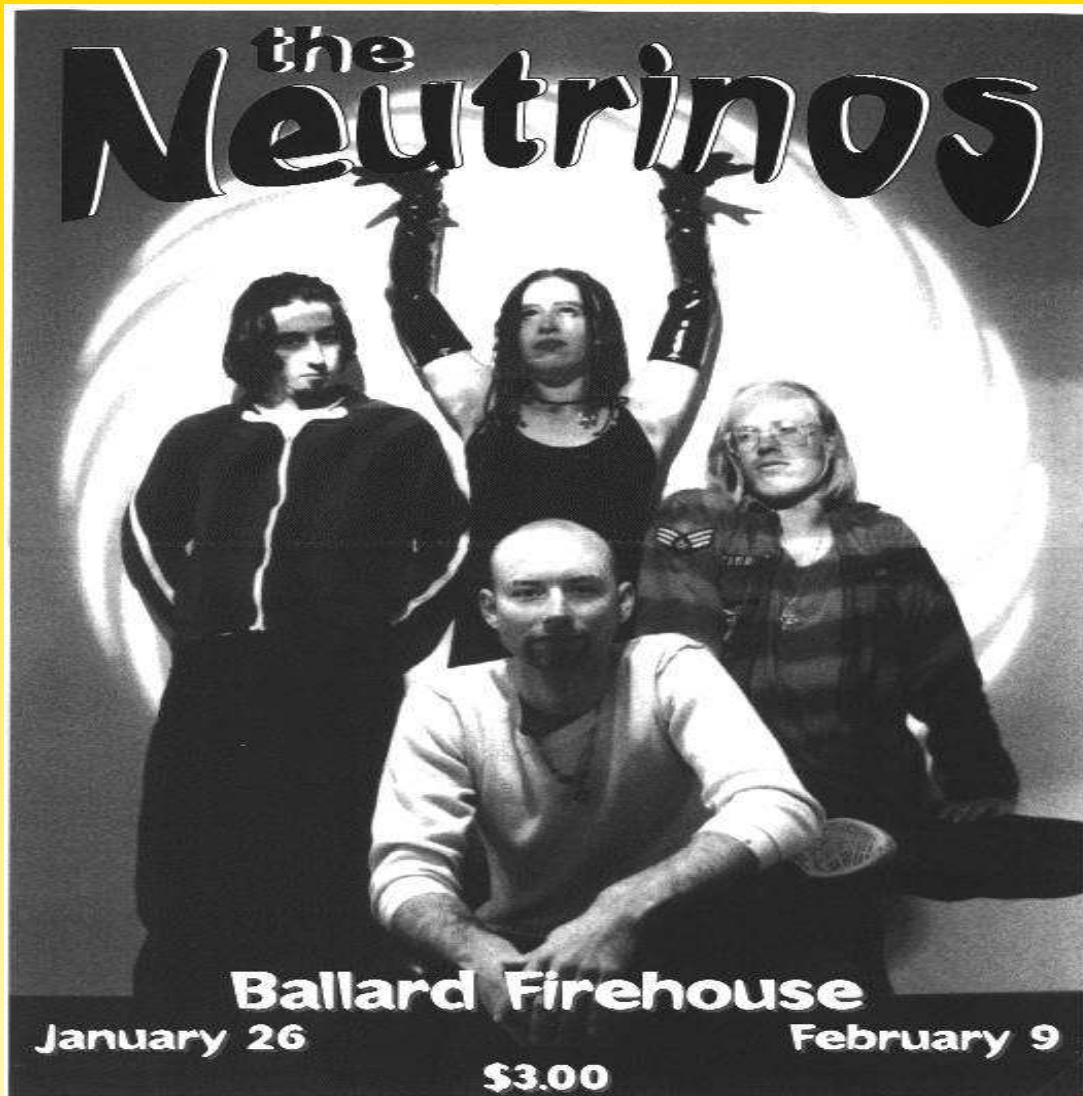
or  $\Delta m_{41}^2 = 1.78$  eV $^2$  and  $|U_{e4}|^2 = 0.151$

[Kopp, Maltoni, Schwetz, 1103.4570](#)

## Mass Orderings



3 active neutrinos can be normally or inversely ordered



Which one is sterile?

## Sterile Neutrinos and $0\nu\beta\beta$

- recall  $|m_{ee}|_{\text{NH}}^{\text{act}}$  can vanish and  $|m_{ee}|_{\text{IH}}^{\text{act}} \sim 0.02$  eV cannot vanish
- $|m_{ee}| = |\underbrace{|U_{e1}|^2 m_1 + |U_{e2}|^2 m_2 e^{2i\alpha} + |U_{e3}|^2 m_3 e^{2i\beta}}_{m_{ee}^{\text{act}}} + \underbrace{|U_{e4}|^2 m_4 e^{2i\Phi_1}}_{m_{ee}^{\text{st}}} |$
- $\Delta m_{\text{st}}^2 \simeq 1$  eV<sup>2</sup> and  $|U_{e4}| \simeq 0.15$
- sterile contribution to  $0\nu\beta\beta$ :

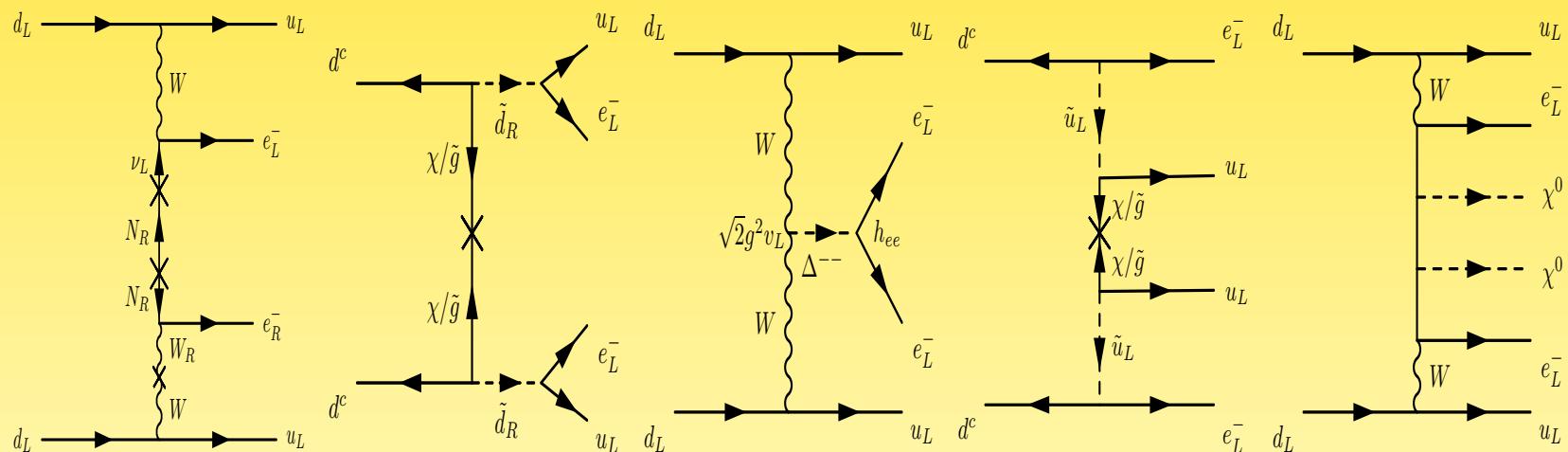
$$|m_{ee}|^{\text{st}} \simeq \sqrt{\Delta m_{\text{st}}^2} |U_{e4}|^2 \simeq 0.02 \text{ eV} \left\{ \begin{array}{l} \gg |m_{ee}|_{\text{NH}}^{\text{act}} \\ \simeq |m_{ee}|_{\text{IH}}^{\text{act}} \end{array} \right.$$

- $\Rightarrow |m_{ee}|_{\text{NH}}$  cannot vanish and  $|m_{ee}|_{\text{IH}}$  can vanish!

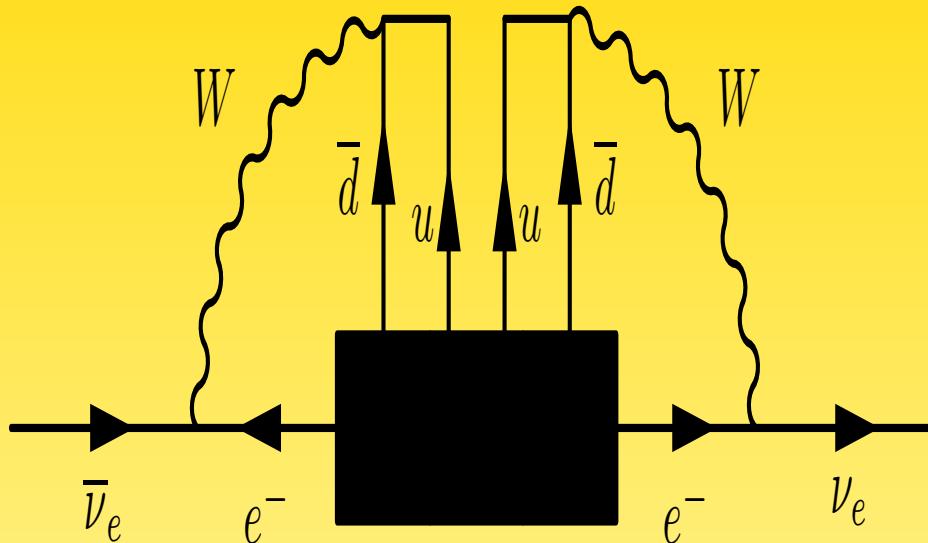
Barry, W.R., Zhang, JHEP 1107

## Non-Standard Interpretations:

There is at least one other mechanism leading to Neutrinoless Double Beta Decay and its contribution is at least of the same order as the light neutrino exchange mechanism



Schechter-Valle theorem: no matter what process, neutrinos are Majorana:



Blackbox diagram is 4 loop:

$$m_\nu \sim \frac{1}{(16\pi^2)^4} \frac{\text{MeV}^5}{m_W^4} \lesssim 10^{-23} \text{ eV}$$

explicit calculation: Duerr, Lindner, Merle, 1105.0901

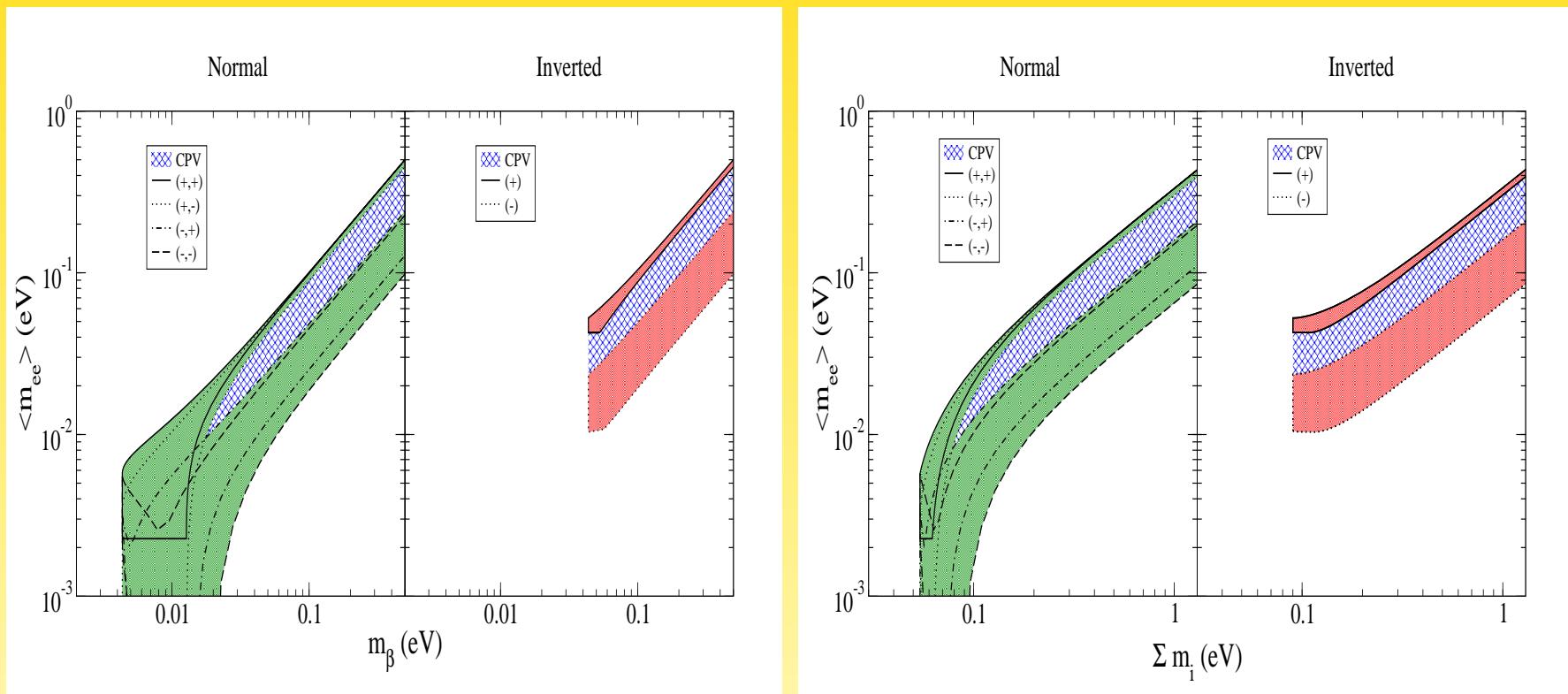
mechanism	physics parameter	current limit	test
<b>light neutrino exchange</b>	$ U_{ei}^2 m_i $	0.5 eV	oscillations, cosmology, neutrino mass
<b>heavy neutrino exchange</b>	$\left  \frac{S_{ei}^2}{M_i} \right $	$2 \times 10^{-8} \text{ GeV}^{-1}$	LFV, collider
<b>heavy neutrino and RHC</b>	$\left  \frac{V_{ei}^2}{M_i M_W^4} \right $	$4 \times 10^{-16} \text{ GeV}^{-5}$	flavor, collider
<b>Higgs triplet and RHC</b>	$\left  \frac{(M_R)_{ee}}{m_{\Delta_R}^2 M_W^4} \right $	$10^{-15} \text{ GeV}^{-1}$	flavor, collider $e^-$ distribution
<b><math>\lambda</math>-mechanism with RHC</b>	$\left  \frac{U_{ei} \tilde{S}_{ei}}{M_W^2} \right $	$1.4 \times 10^{-10} \text{ GeV}^{-2}$	flavor, collider, $e^-$ distribution
<b><math>\eta</math>-mechanism with RHC</b>	$\tan \zeta  U_{ei} \tilde{S}_{ei} $	$6 \times 10^{-9}$	flavor, collider, $e^-$ distribution
<b>short-range <math>\mathcal{R}</math></b>	$\frac{ \lambda'_{111} }{\Lambda_{\text{SUSY}}^5}$ $\Lambda_{\text{SUSY}} = f(m_{\tilde{g}}, m_{\tilde{u}_L}, m_{\tilde{d}_R}, m_{\chi_i})$	$7 \times 10^{-18} \text{ GeV}^{-5}$	collider, flavor
<b>long-range <math>\mathcal{R}</math></b>	$\left  \sin 2\theta^b \lambda'_{131} \lambda'_{113} \left( \frac{1}{m_{\tilde{b}_1}^2} - \frac{1}{m_{\tilde{b}_2}^2} \right) \right $ $\sim \frac{G_F}{q} m_b \frac{ \lambda'_{131} \lambda'_{113} }{\Lambda_{\text{SUSY}}^3}$	$2 \times 10^{-13} \text{ GeV}^{-2}$ $1 \times 10^{-14} \text{ GeV}^{-3}$	flavor, collider
<b>Majorons</b>	$ \langle g_\chi \rangle  \text{ or }  \langle g_\chi \rangle ^2$	$10^{-4} \dots 1$	spectrum, cosmology

## Distinguishing Mechanisms

### The inverse problem of $0\nu\beta\beta$

- 1.) Other observables (LHC, LFV, KATRIN, cosmology,...)
- 2.) Decay products (individual  $e^-$  energies, angular correlations, spectrum,...)
- 3.) Nuclear physics (multi-isotope,  $0\nu\text{ECEC}$ ,  $0\nu\beta^+\beta^+$ ,...)

## 1.) Distinguishing via other Observables



standard mechanism: KATRIN, cosmology

## Energy Scale:

Note: *standard amplitude* for light Majorana neutrino exchange:

$$\mathcal{A}_l \simeq G_F^2 \frac{|m_{ee}|}{q^2} \simeq 7 \times 10^{-18} \left( \frac{|m_{ee}|}{0.5 \text{ eV}} \right) \text{ GeV}^{-5} \simeq 2.7 \text{ TeV}^{-5}$$

⇒ for  $0\nu\beta\beta$  holds:

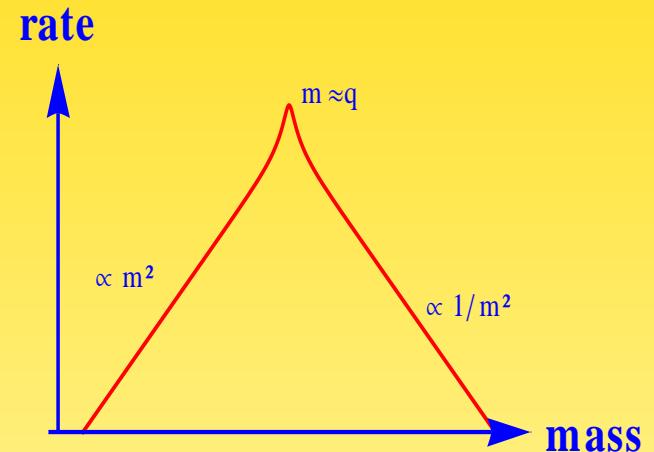
$$1 \text{ eV} = 1 \text{ TeV}$$

⇒ Phenomenology in colliders, LFV

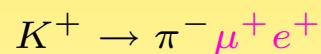
## Examples

- Fermions and no RHC:

$$\mathcal{A} \propto \frac{m}{q^2 - m^2} \rightarrow \begin{cases} m & \text{for } q^2 \gg m^2 \\ \frac{1}{m} & \text{for } q^2 \ll m^2 \end{cases}$$



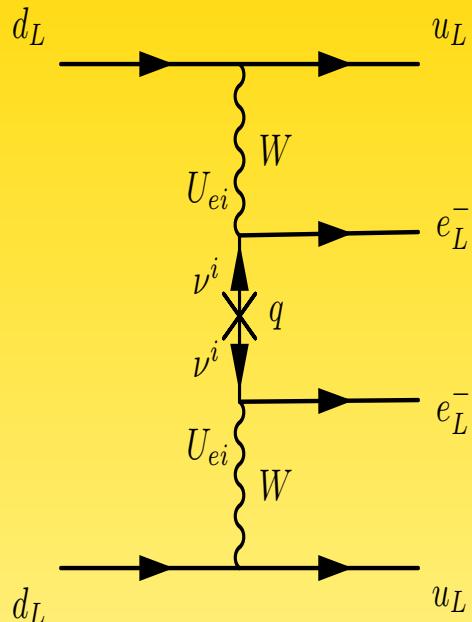
Note: maximum  $\mathcal{A}$  corresponds to  $m \simeq \langle q \rangle$ : limits on  $\mathcal{O}(m_K)$  Majorana neutrinos from



- heavy scalar:

$$\mathcal{A} \propto \frac{1}{q^2 - m^2} \rightarrow \frac{1}{m^2}$$

## Heavy neutrinos



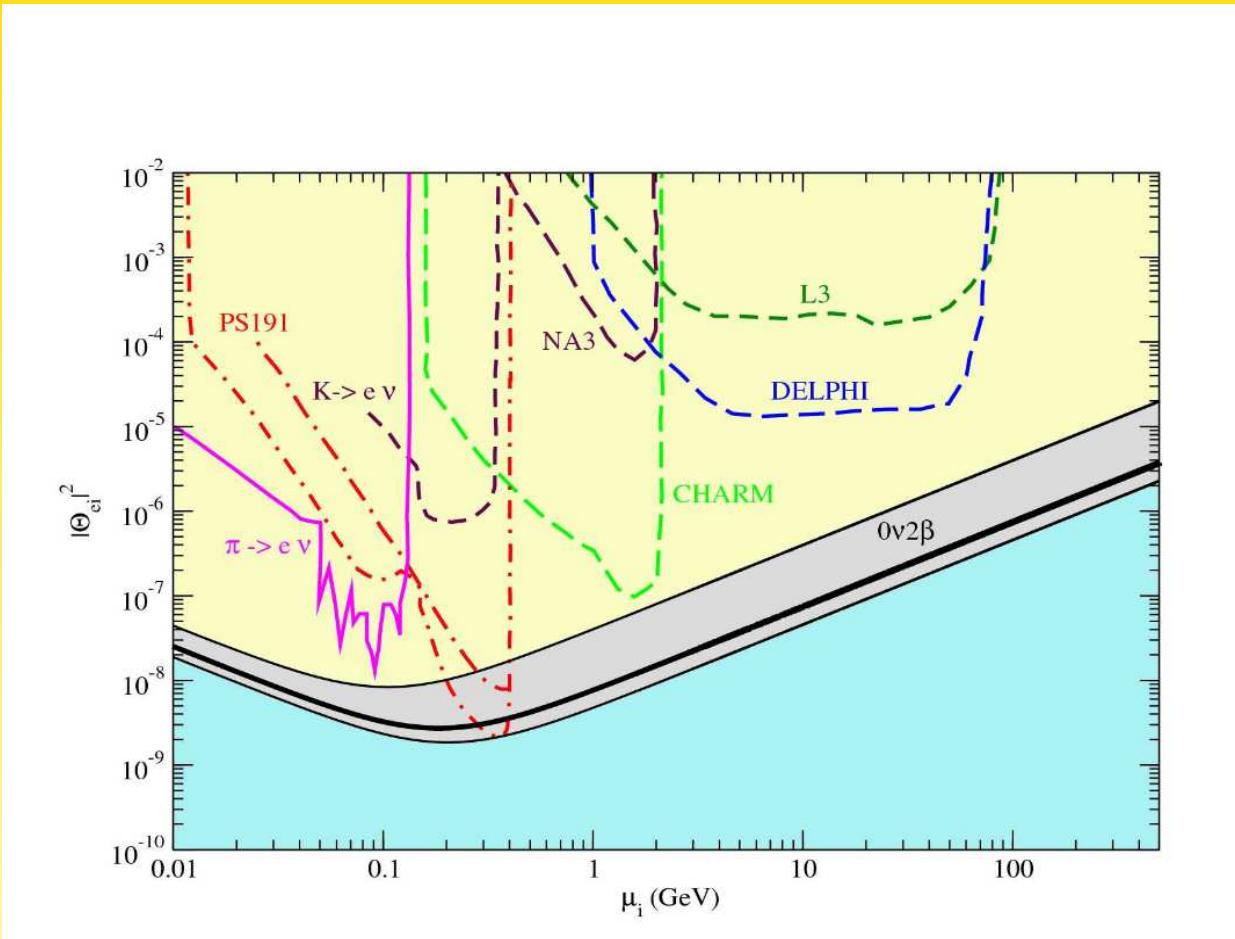
same diagram with  $U \rightarrow S$

$$\mathcal{A}_h = G_F^2 \frac{S_{ei}^2}{M_i} \equiv G_F^2 \langle \frac{1}{m} \rangle \Rightarrow \langle \frac{1}{m} \rangle \leq 5 \times 10^{-8} \text{ GeV}^{-1}$$

literature value:  $2 \times 10^{-8} \text{ GeV}^{-1} \dots$

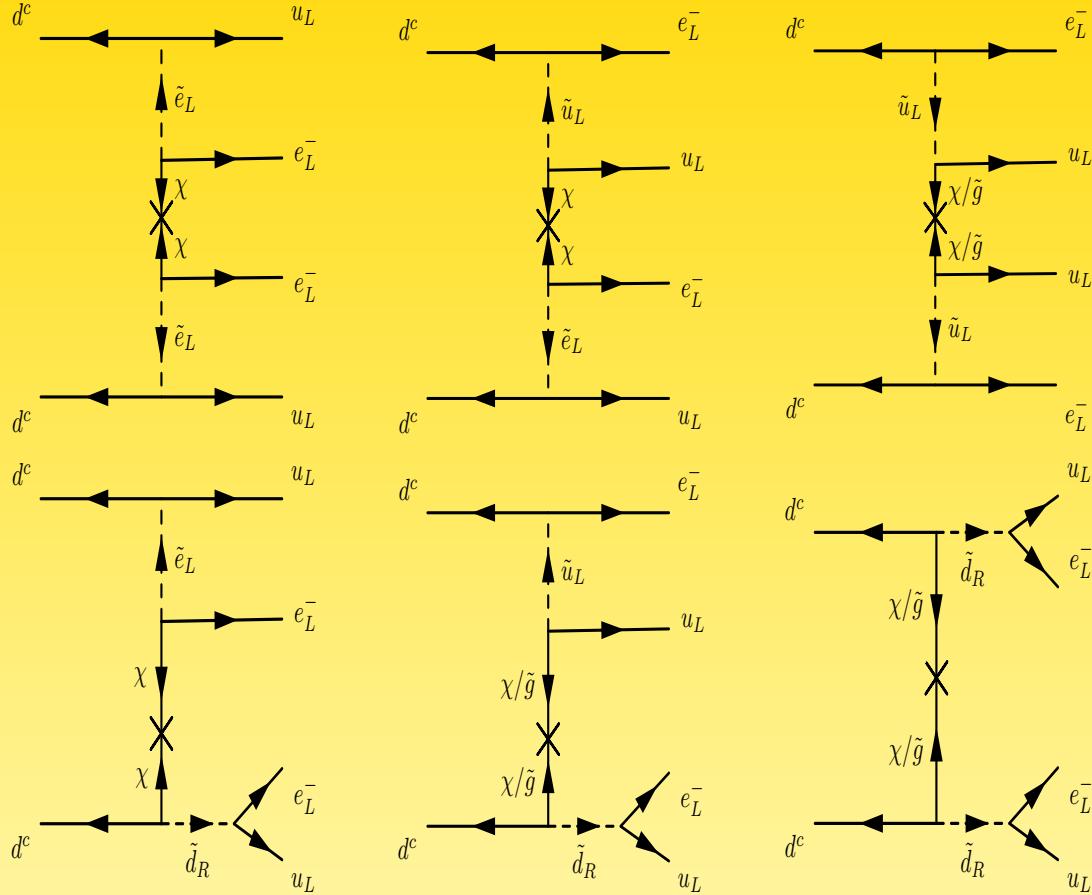
$\Rightarrow$  comparison on amplitude level is fine

## Heavy neutrinos



Mitra, Senjanovic, Vissani, 1108.0004

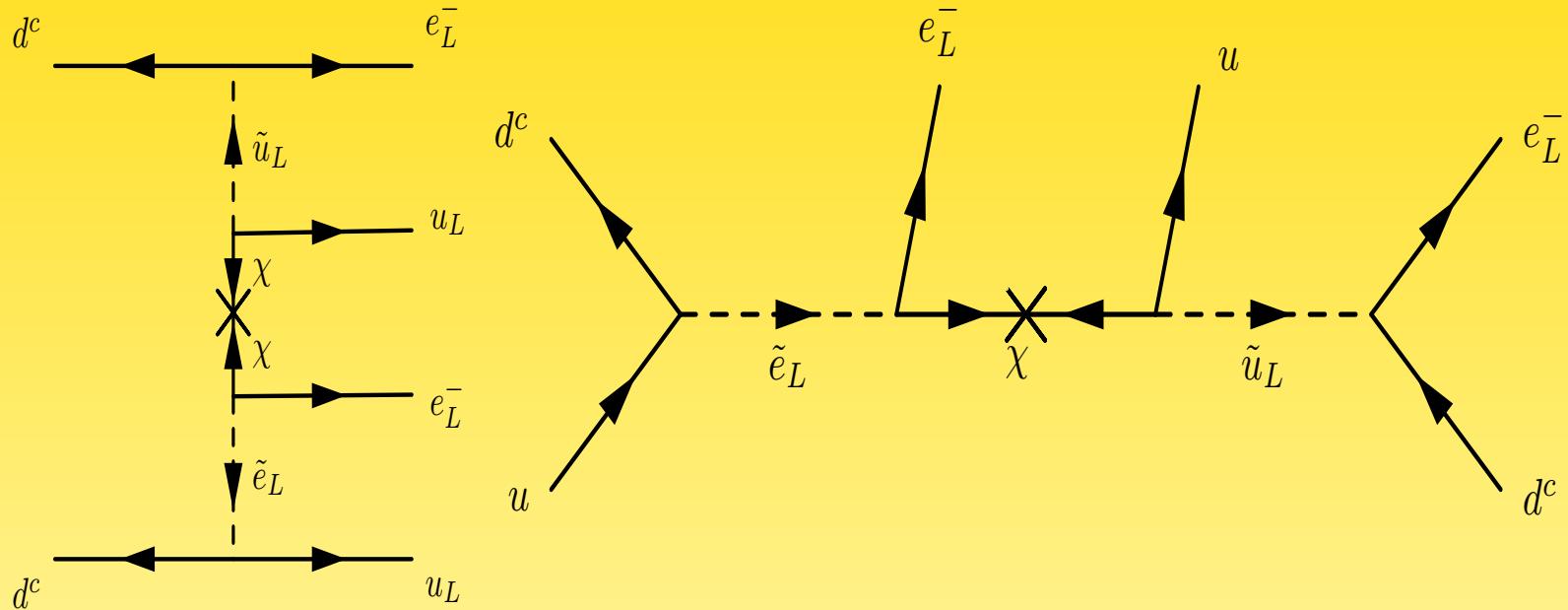
## Supersymmetry: short range



$$\mathcal{A}_{R_1} \simeq \frac{\lambda'^2_{111}}{\Lambda_{\text{SUSY}}^5}$$

## Supersymmetry: short range

interplay with LHC:

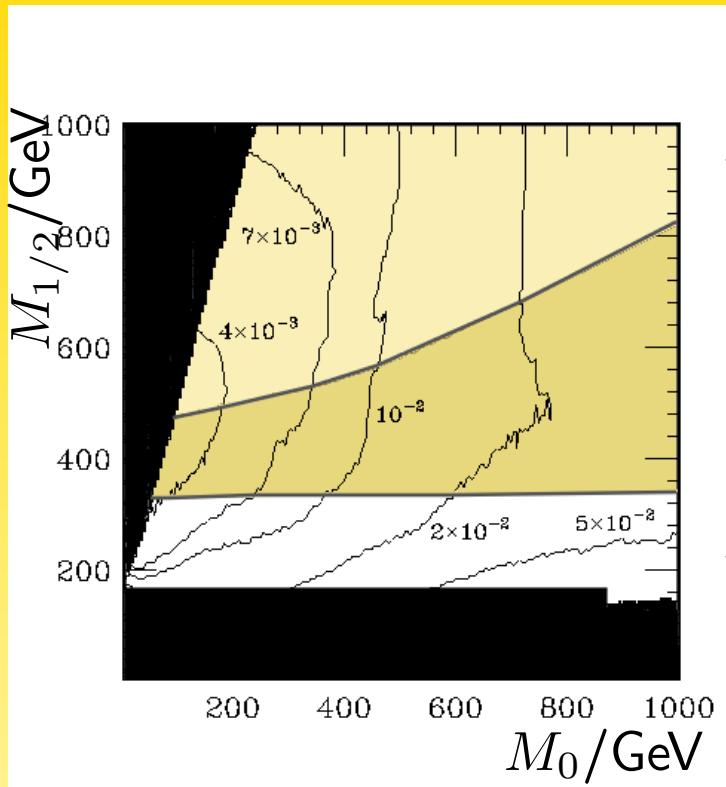


“resonant selectron production”

$$\hat{\sigma} \propto \frac{\lambda'^2_{111}}{\hat{s}}$$

Allanach, Kom, Paes, 0903.0347

$$\tan \beta = 10, A_0 = 0, 10 \text{ fb}^{-1}$$



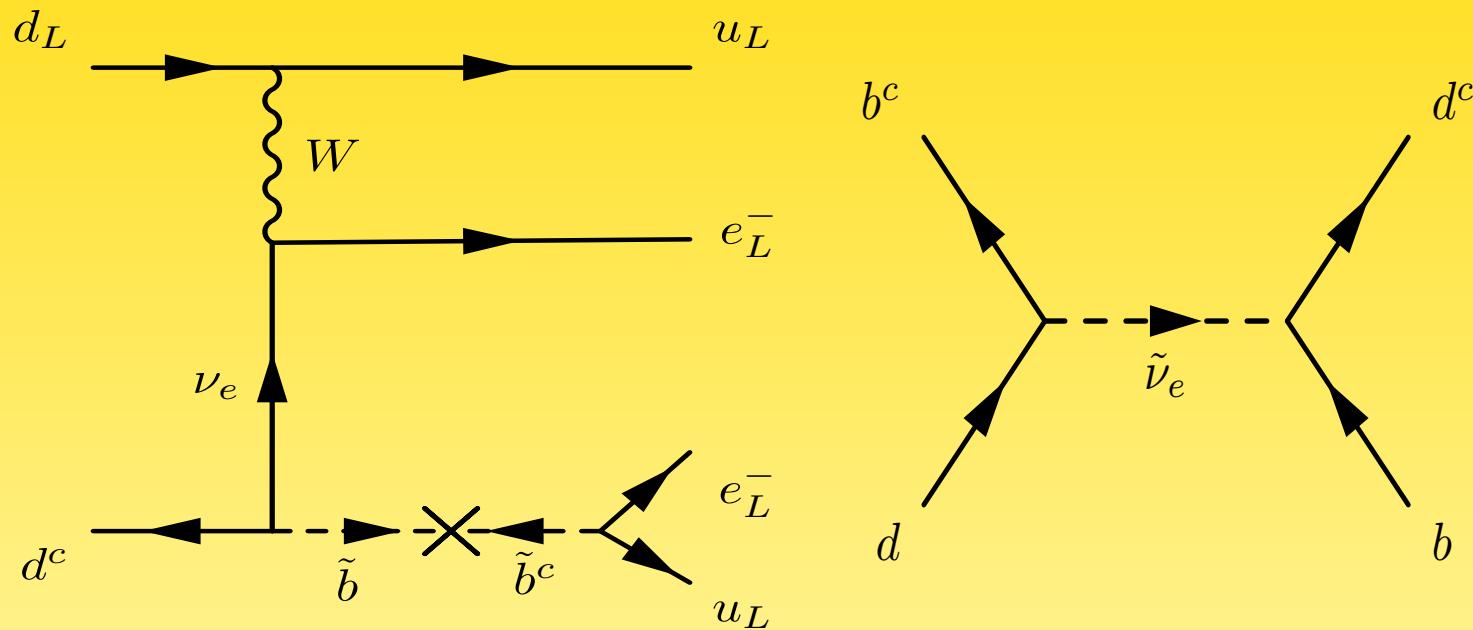
$$T_{1/2}^{0\nu\beta\beta}(\text{Ge}) > 1 \times 10^{27} \text{ yrs}$$

$$100 > T_{1/2}^{0\nu\beta\beta}(\text{Ge})/10^{25} \text{ yrs} > 1.9$$

$$T_{1/2}^{0\nu\beta\beta}(\text{Ge}) < 1.9 \times 10^{25} \text{ yrs}$$

- observation in white region in conflict with  $0\nu\beta\beta$
- if  $0\nu\beta\beta$  observed: dark yellow region tests  $R$  SUSY mechanism
- light yellow region: no significant  $R$  contribution to  $0\nu\beta\beta$

## Supersymmetry: long range



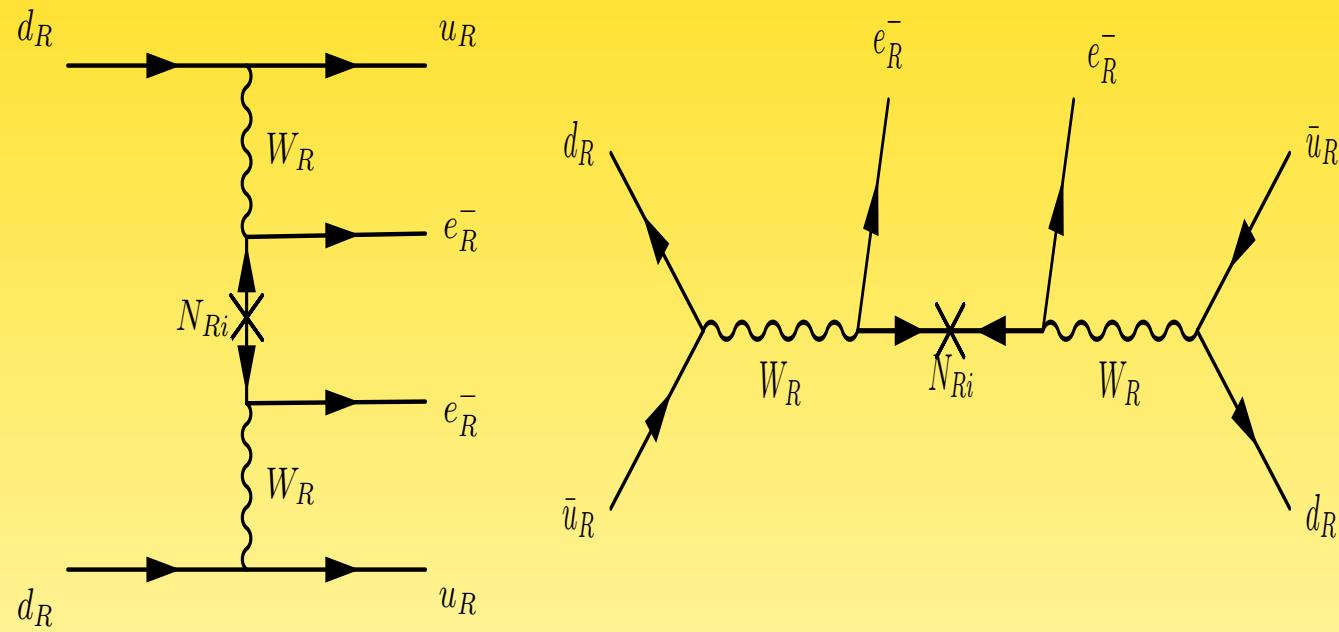
$$\mathcal{A}_{R_2}^b \simeq G_F \frac{1}{q} U_{ei} m_b \frac{\lambda'_{131} \lambda'_{113}}{\Lambda_{\text{SUSY}}^3}$$

$0\nu\beta\beta$

$$\frac{\lambda'_{131} \lambda'_{113}}{\Lambda_{\text{SUSY}}^2}$$

$B^0 - \bar{B}^0$  mixing

## Left-right symmetry



Tello et al., 1011.3522

## “Inverse $0\nu\beta\beta$ ”

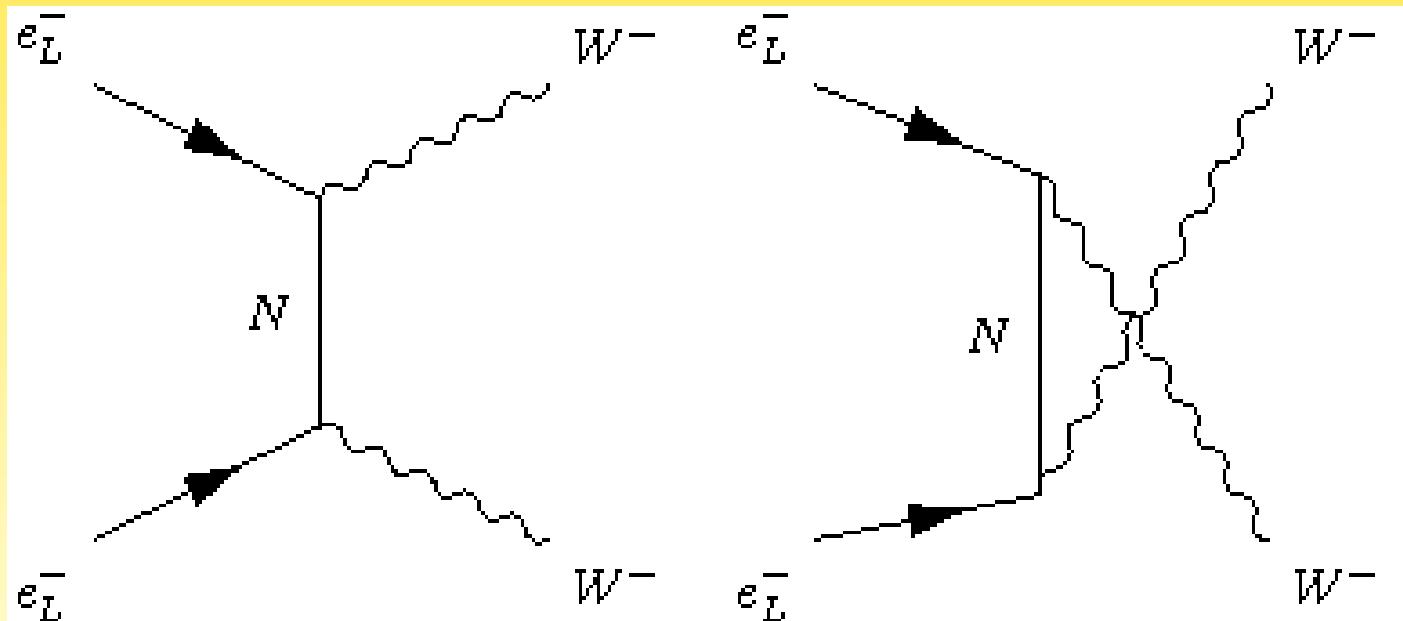
this is not



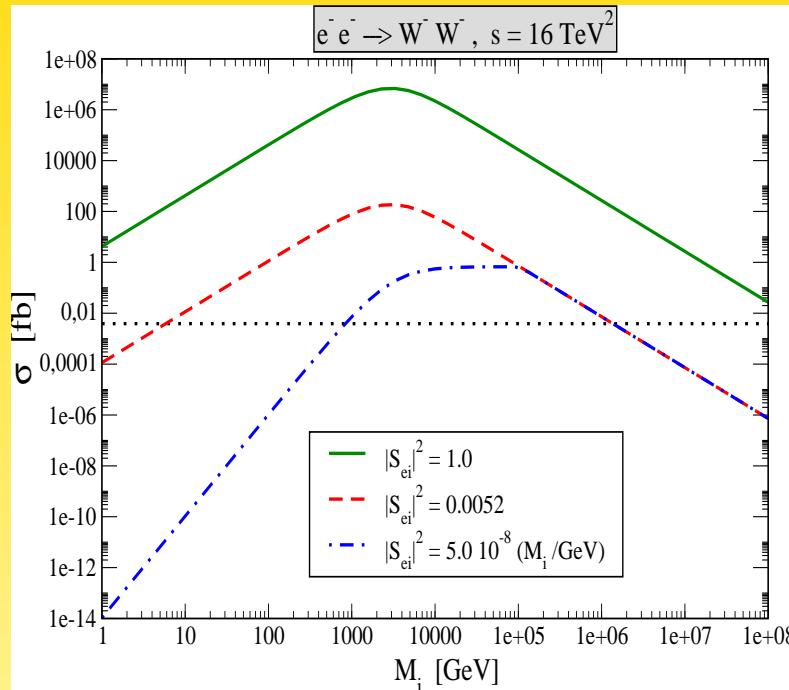
but rather



Rizzo; Heusch, Minkowski; Gluza, Zralek; Cuypers, Raidal;...



## Inverse Neutrinoless Double Beta Decay



W.R., PRD **81**

$$\frac{d\sigma}{d \cos \theta} = \frac{G_F^2}{32 \pi} \left\{ \sum (m_\nu)_i \mathcal{U}_{ei}^2 \left( \frac{t}{t - (m_\nu)_i} + \frac{u}{u - (m_\nu)_i} \right) \right\}^2$$

## Inverse Neutrinoless Double Beta Decay

Extreme limits:

- light neutrinos:

$$\sigma(e^- e^- \rightarrow W^- W^-) = \frac{G_F^2}{4\pi} |m_{ee}|^2 \leq 4.2 \cdot 10^{-18} \left( \frac{|m_{ee}|}{1 \text{ eV}} \right)^2 \text{ fb}$$

⇒ way too small

- heavy neutrinos:

$$\sigma(e^- e^- \rightarrow W^- W^-) = 2.6 \cdot 10^{-3} \left( \frac{\sqrt{s}}{\text{TeV}} \right)^4 \left( \frac{S_{ei}^2/M_i}{5 \cdot 10^{-8} \text{ GeV}^{-1}} \right)^2 \text{ fb}$$

⇒ too small

- $\sqrt{s} \rightarrow \infty$ :

$$\sigma(e^- e^- \rightarrow W^- W^-) = \frac{G_F^2}{4\pi} \left( \sum \mathcal{U}_{ei}^2 (m_\nu)_i \right)^2$$

⇒ amplitude grows with  $\sqrt{s}$ ? Unitarity??

## Unitarity

high energy limit  $\sqrt{s} \rightarrow \infty$ :

$$\sigma(e^- e^- \rightarrow W^- W^-) = \frac{G_F^2}{4\pi} \left( \sum \mathcal{U}_{ei}^2 (m_\nu)_i \right)^2$$

$\leftrightarrow$  amplitude grows with  $\sqrt{s}$ ?

Answer: exact see-saw relation  $\mathcal{U}_{ei}^2 (m_\nu)_i = 0$

$$\mathcal{M} = \begin{pmatrix} 0 & m_D \\ m_D^T & M_R \end{pmatrix} = \mathcal{U} \begin{pmatrix} m_\nu^{\text{diag}} & 0 \\ 0 & M_R^{\text{diag}} \end{pmatrix} \mathcal{U}^T$$

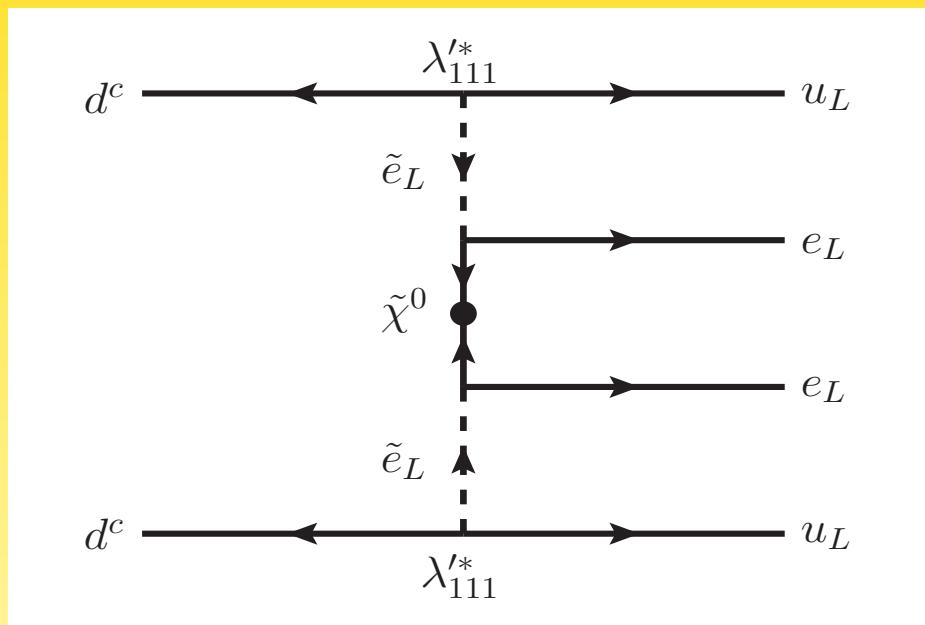
if Higgs triplet is present: unitarity also conserved

$$\sigma(e^- e^- \rightarrow W^- W^-) = \frac{G_F^2}{4\pi} \left( (\mathcal{U}_{ei}^2 (m_\nu)_i - (m_L)_{ee})^2 \right) = 0$$

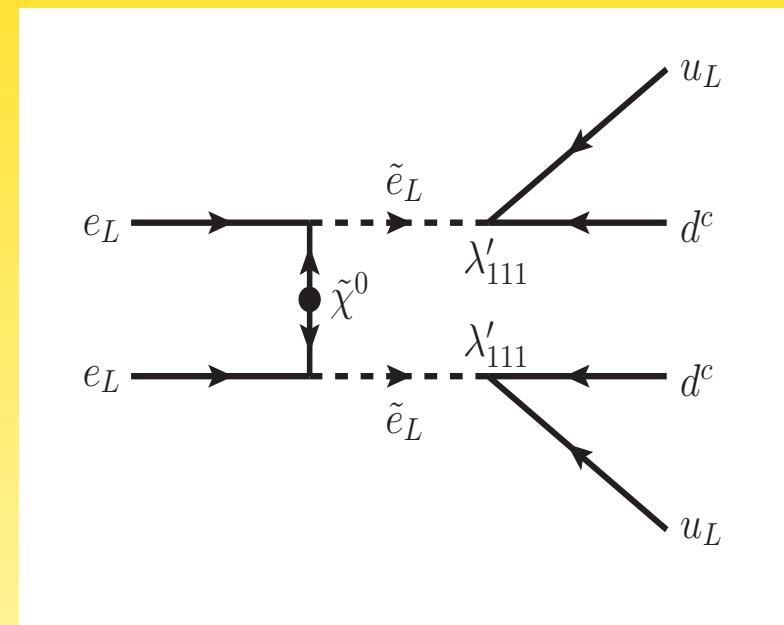
W.R., PRD **81**

## Inverse $0\nu\beta\beta$ and RPV SUSY

$$\mathcal{W} = \lambda'_{111} L_1 Q_1 D_1^c \Rightarrow e^- e^- \rightarrow 4 \text{ jets}$$



$0\nu\beta\beta$



resonant selectron production  
via gauge interactions

## Cross section

$$\sigma(e_L^- e_L^- \rightarrow \tilde{e}_L^- \tilde{e}_L^-) = \frac{\pi \alpha^2 |g_L|^4}{s} \frac{2m_{\tilde{\chi}^0}^2}{s + 2m_{\tilde{\chi}^0}^2 - 2m_{\tilde{e}_L}^2} \left[ L + \frac{2\lambda}{(s + 2m_{\tilde{\chi}^0}^2 - 2m_{\tilde{e}_L}^2)^2 - \lambda^2} \right]$$

where

$$L = \ln \frac{s + 2m_{\tilde{\chi}^0}^2 - 2m_{\tilde{e}_L}^2 + \lambda}{s + 2m_{\tilde{\chi}^0}^2 - 2m_{\tilde{e}_L}^2 - \lambda}$$

$$\lambda = \lambda(s, m_{\tilde{e}_L}^2, m_{\tilde{e}_L}^2) = \sqrt{s^2 - 4sm_{\tilde{e}_L}^2}$$

Keung, Littenberg, 1983

adjustable parameters

$$m_{\tilde{\chi}^0}, \quad m_{\tilde{g}}, \quad m_{\tilde{e}_L}, \quad m_{\tilde{u}_L}, \quad m_{\tilde{d}_R}, \quad \lambda'_{111}$$

squarks and gluinos decoupled;

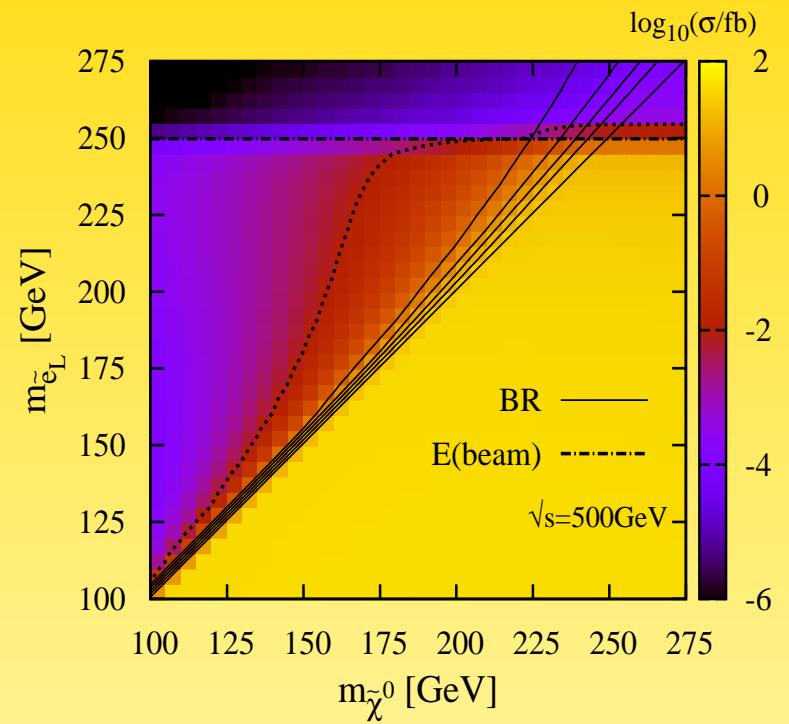
competing decays  $\tilde{e}_L \rightarrow e \tilde{\chi}^0$  and  $\tilde{e}_L \rightarrow jj$

competing decays  $\tilde{e}_L \rightarrow e \tilde{\chi}^0$  and  $\tilde{e}_L \rightarrow jj$ :

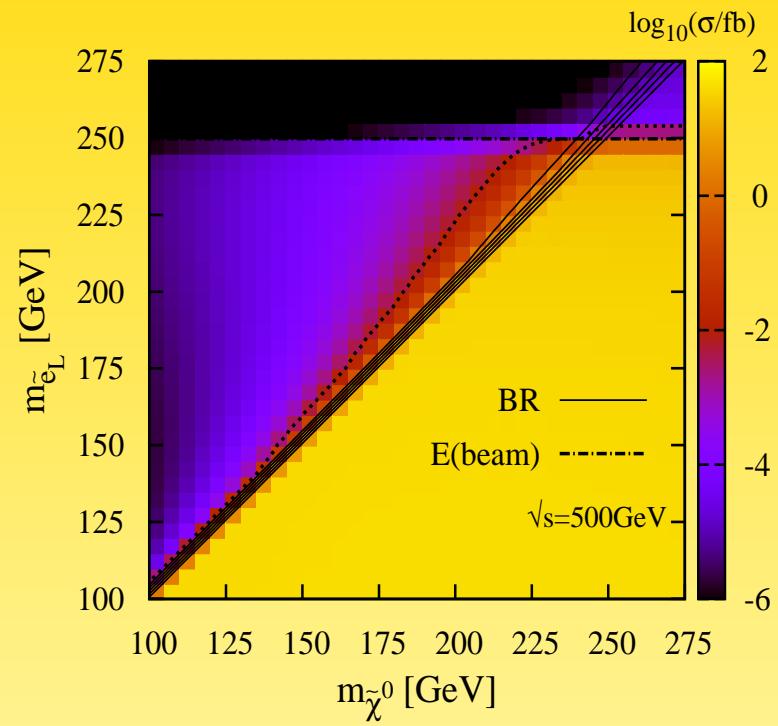
- $0\nu\beta\beta$ -limit goes with  $\Lambda_{\text{SUSY}}^5 \Rightarrow \lambda'_{111}$  can be  $\mathcal{O}(1)$  and thus  $\text{BR}(\tilde{e}_L \rightarrow jj) > \text{BR}(\tilde{e}_L \rightarrow e \tilde{\chi}^0)$
- even for low masses, large  $\text{BR}(\tilde{e}_L \rightarrow jj)$  possible for narrow band around  $m_{\tilde{e}_L} - m_{\tilde{\chi}^0} \ll m_{\tilde{e}_L}$

reconstruction:

- mass and width of  $\tilde{e}_L$ : dijet invariant mass distribution
- $\text{BR}(\tilde{e}_L \rightarrow jj)$  and thus  $\lambda'_{111}$ :  $\tilde{e}_L$  decays
- mass of  $\tilde{\chi}^0$ : rate of  $e_L^- e_L^- \rightarrow \tilde{e}_L^- \tilde{e}_L^-$



$1.9 \times 10^{25}\text{yrs}$

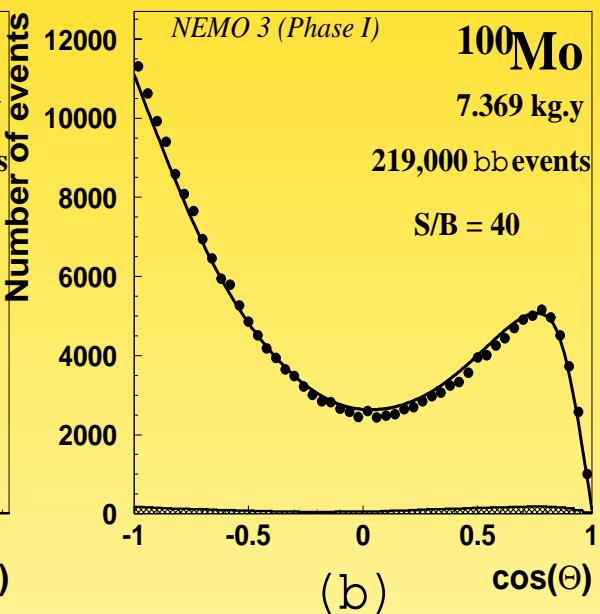
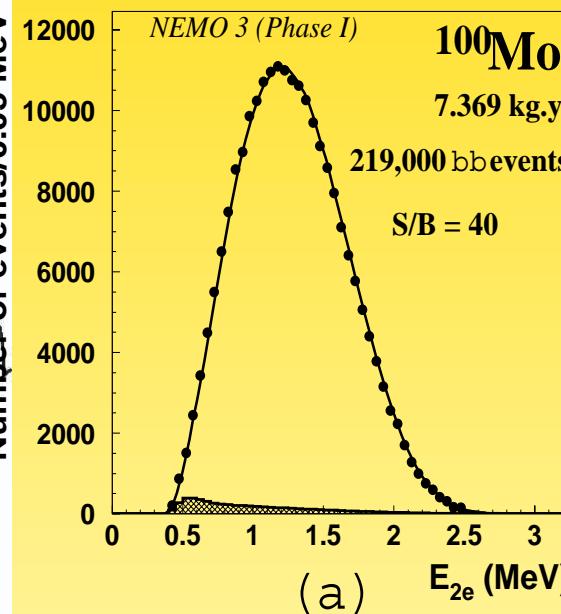
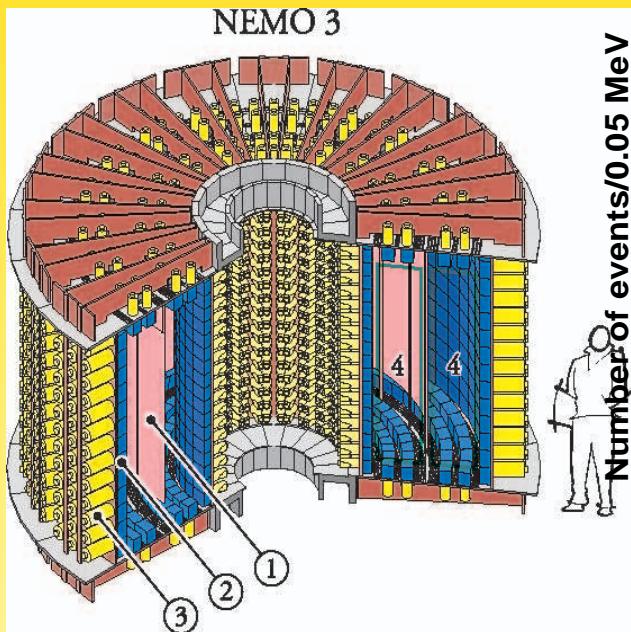


$1.0 \times 10^{27}\text{yrs}$

Kom, W.R., 1110.3220

## 2.) Distinguishing via decay products

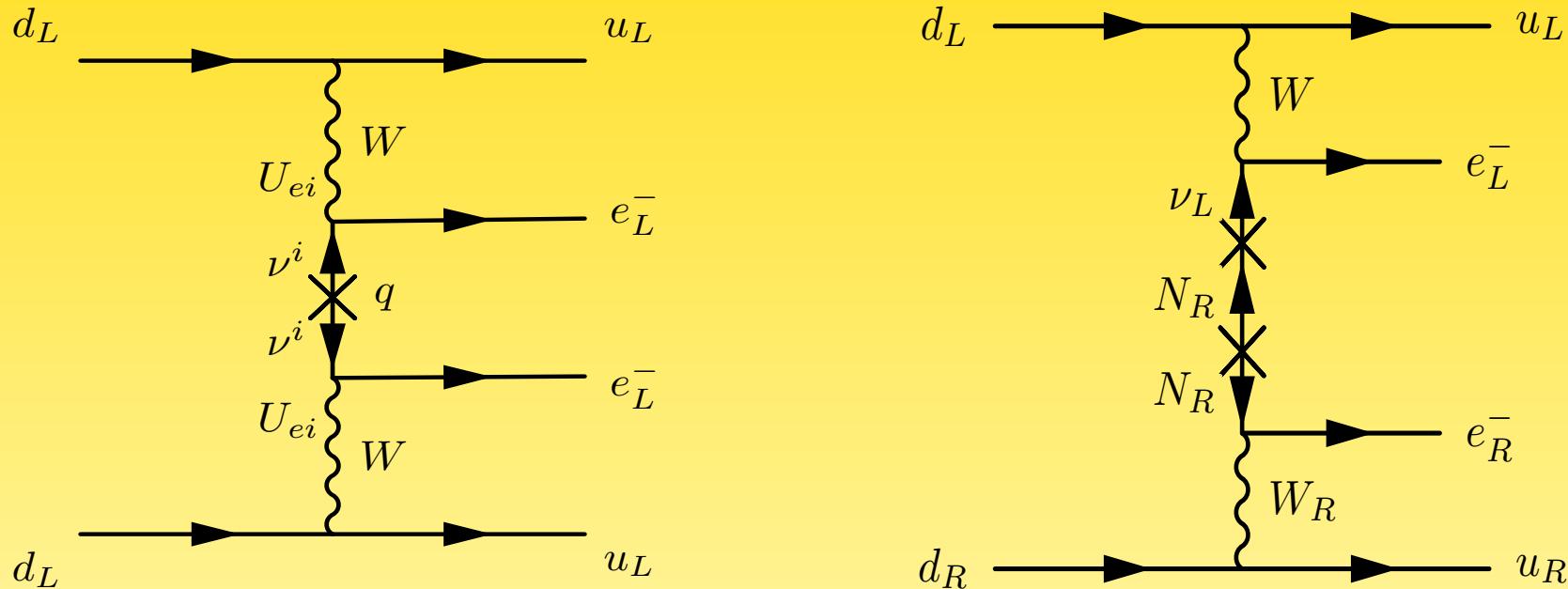
### SuperNEMO



- source foils in between plastic scintillators
- individual electron energy, and their relative angle!

## Distinguishing via decay products

Consider standard plus  $\lambda$ -mechanism



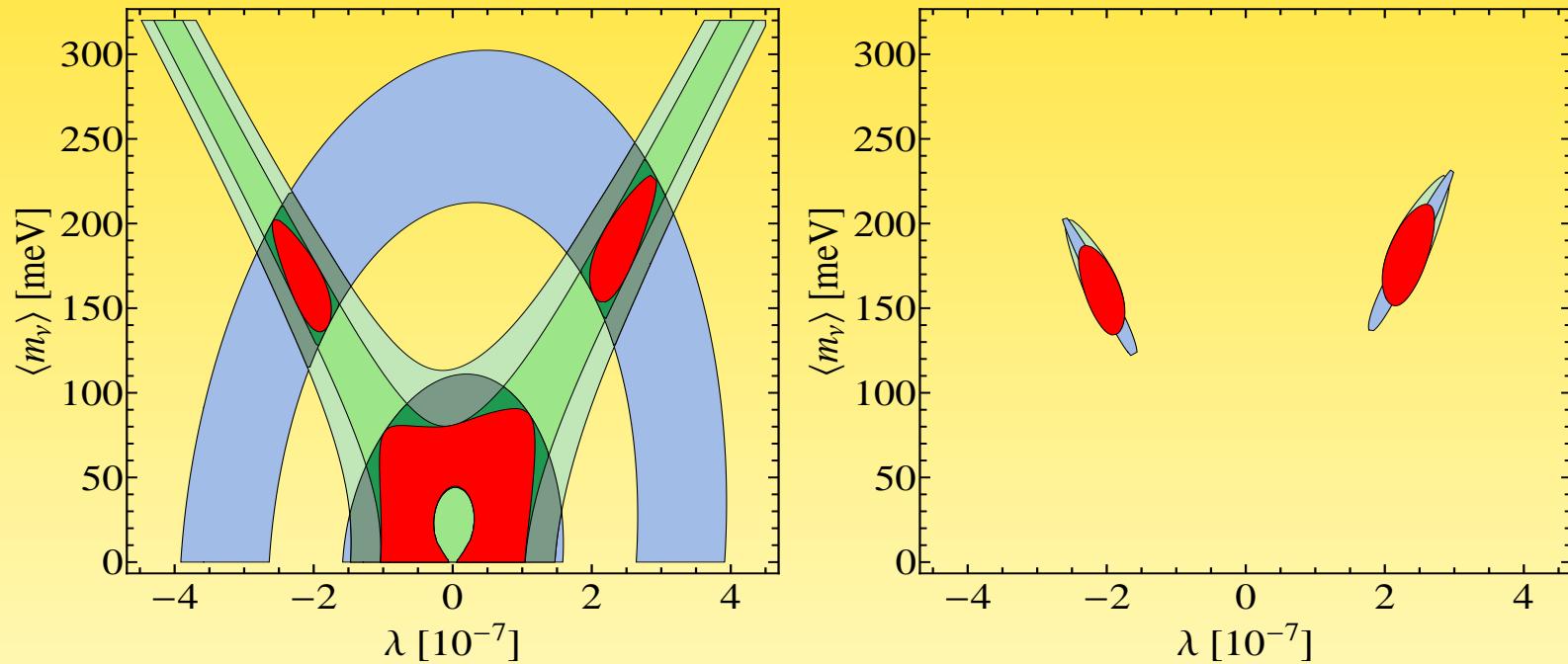
$$\frac{d\Gamma}{dE_1 dE_2 d\cos\theta} \propto (1 - \beta_1 \beta_2 \cos\theta) \quad \frac{d\Gamma}{dE_1 dE_2 d\cos\theta} \propto (E_1 - E_2)^2 (1 + \beta_1 \beta_2 \cos\theta)$$

Arnold et al., 1005.1241

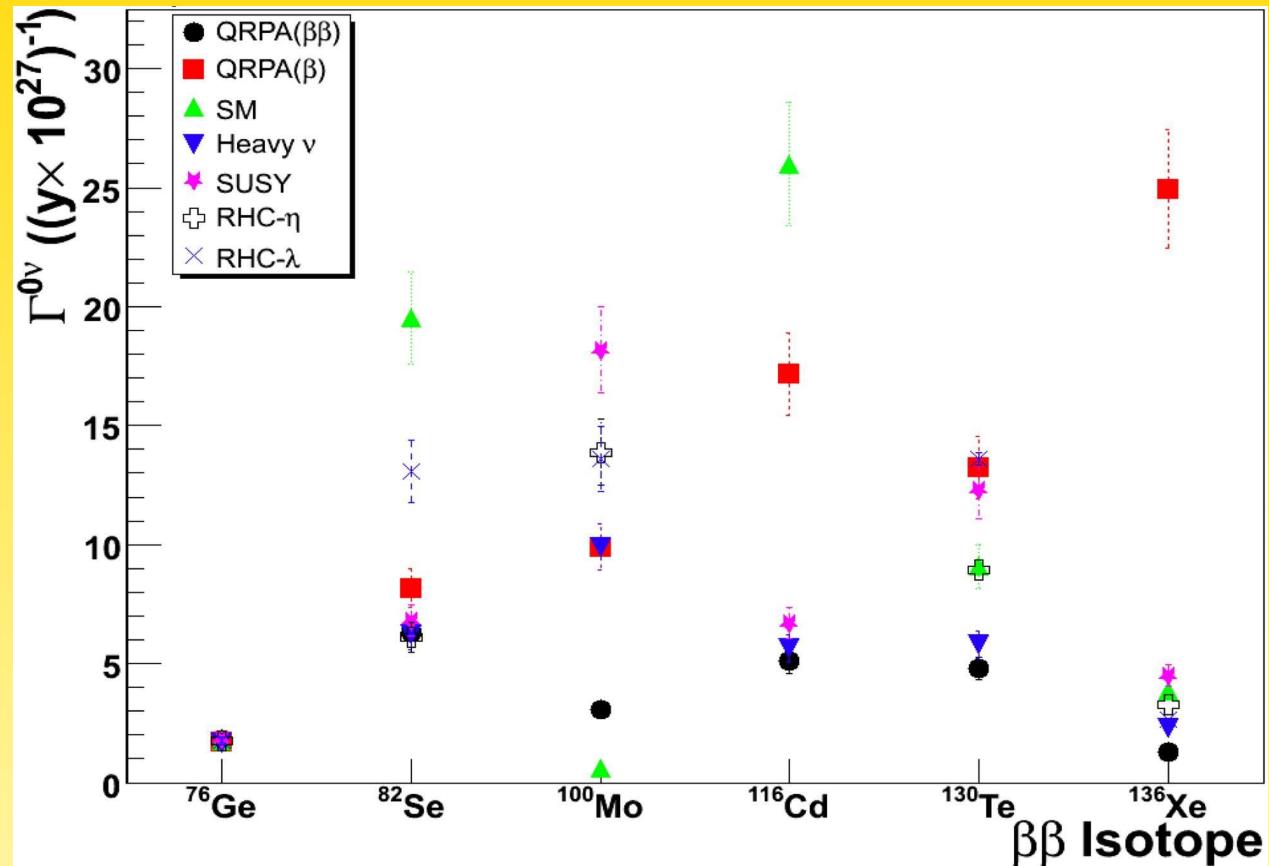
## Distinguishing via decay products

Defining asymmetries

$$A_\theta = (N_+ - N_-)/(N_+ + N_-) \text{ and } A_E = (N_> - N_<)/(N_> + N_<)$$



### 3.) Distinguishing via nuclear physics



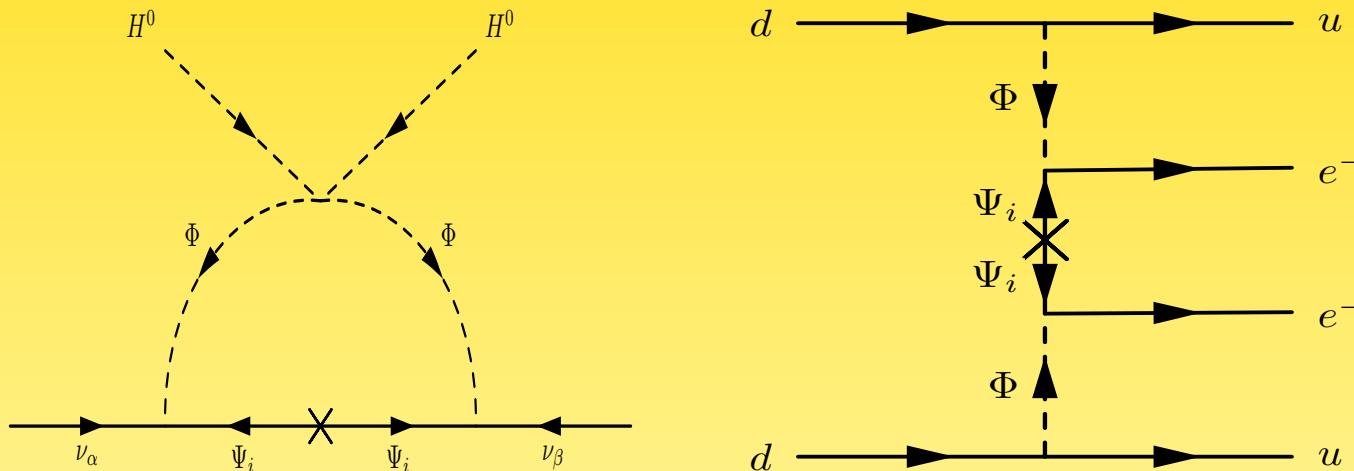
Gehman, Elliott, hep-ph/0701099

3 to 4 isotopes necessary to disentangle mechanism

## Direct vs. Indirect Contribution

Example: Color Octet Mechanism (Perez, Wise, PRD 80)

introduce  $\rho_\alpha = (8, 1, 0)$  and  $S = (8, 2, \frac{1}{2})$



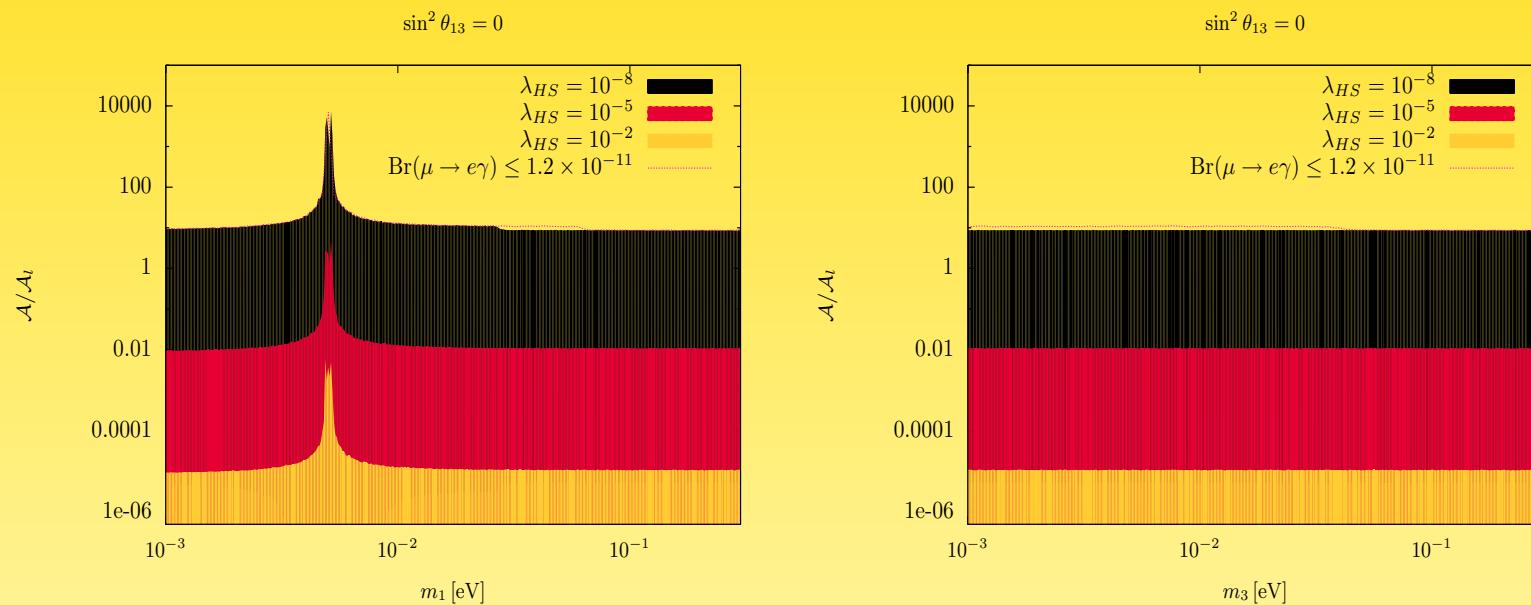
1-loop  $m_\nu$

indirect contribution to  $0\nu\beta\beta$ : direct contribution to  $0\nu\beta\beta$ :

$$\mathcal{A}_l \simeq G_F^2 \frac{|m_{ee}|}{q^2}$$

$$\mathcal{A} \simeq c_{ud}^2 \frac{y_{e\alpha}^2}{M_{\rho_\alpha} M_S^4}$$

## Direct vs. Indirect Contribution



Choubey, Dürr, Mitra, W.R., in preparation

## Summary

***Chi l'ha visto ?***



Ettore Majorana ordinario di fisica teorica all' Università di Napoli, è misteriosamente scomparso dagli ultimi di marzo. Di anni 31, alto metri 1,70, snello, con capelli neri, occhi scuri, una lunga cicatrice sul dorso di una mano. Chi ne sapesse qualcosa è pregato di scrivere al R. P. E. Maria- necci, Viale Regina Margherita 66 - Roma.