

Recap : local thermodynamical equilibrium :



Universe expands: $\Gamma \downarrow$ faster than $H \downarrow$ (e.g. $\rho \sim G \rho^2 T^5$ vs. $H \propto T g_*^{1/2}$) : $\Rightarrow T \propto \sqrt[3]{t}$

freeze-out at $\Gamma = H$: e.g. neutrinos freeze-out at $T \approx 0.75$ ReV (80+!)

$$T_{\text{frozen}} = \sqrt[3]{\frac{4}{3}} T_{\text{f}}^{\text{new}} = 1.09 \text{ K} ; m_{\text{SD}} = 2.3 \sqrt{\frac{d^3 \rho}{127}} \Phi_F(\tilde{p}, T_{\text{f}}^{\text{new}}) = 336 \text{ cm}^{-3}$$

note: E, T scale with z identically $\Rightarrow \Phi_F = e^{-\frac{1}{zT} + 1}$ stars

For non-relativistic ~~particles~~ particles : $S = m \cdot m$

$$\Rightarrow S_3 = \frac{g_3}{g_{\text{cr}}} = \frac{\sum m_i^2 m_i}{g_{\text{cr}}} = \frac{\sum m_i^2 m_i}{3H^2 / 8\pi^6 N} \Rightarrow S_3 g_*^2 \approx \frac{\sum m_i^2}{94 \text{ eV}}$$

if neutrinos non-relativistic: $E \approx 3m_\nu c^2 \Rightarrow \Omega_\nu h^2 = \frac{\sum m_\nu^2}{94 \text{ eV}}$ 9-6-27

$$\psi = \frac{1}{2^{E_T+1}} \rightarrow 2^{-m_T}$$

if $\nu = DM$: $\Omega_\nu \approx 0.25 \Rightarrow \sum m_\nu \approx 25 \text{ eV}$ (BUT: ν would be hot dark matter, relativistic when freezing out)

$$m_3 \approx \sqrt{\Delta m_A^2} ; m_2 = \sqrt{\Delta m_\theta^2} ; m_1 = 0 \quad \sum m_\nu \approx 0.06 \text{ eV}$$

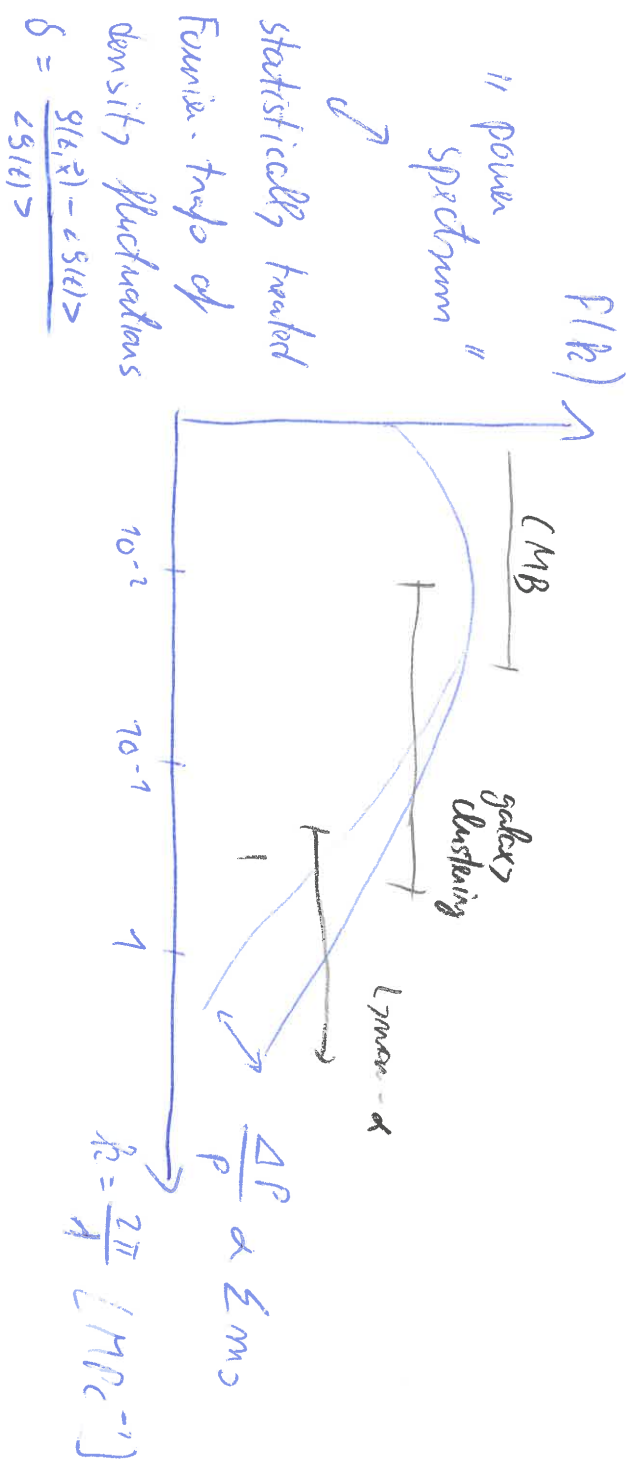
$$m_2 \approx m_1 = \sqrt{\Delta m_A^2} ; m_3 = 0 \quad \sum m_\nu = 0.1 \text{ eV}$$

typical limits on $\sum m_\nu$ nowadays $\lesssim 0.2 \text{ eV}$

cf. to KATRIN: $m_\nu = \sqrt{\sum |U_{\nu i}|^2 m_i^2} \lesssim 0.8 \text{ eV}$
 2105.08533 ☺
 corresponds to $\sum m_\nu \approx 2.4 \text{ eV}$

→ Cosmological limits related to structure formation and Cosmic Microwave Background
 initial perturbations (overdensities) as seeds of structure (galaxies, clusters, ...)
 Abundances are not (= relativistic) "escape potential wells, level energy over/under-densities
 Slow down growth of gravitational potential wells on scales $\lambda \ll \lambda_{FS}$

$\lambda_{FS} \sim \left(\frac{2V}{m_s} \right) \text{Mpc} \iff$ the closer scale to λ_{MB} Mpc, the larger the effect



"Cosmological SM": Λ CDM: 6 parameters: H_0 , Ω_{Baryon} , Ω_{matter} , τ , $P_{\text{lin}}(k) = A k^m$
($n_s = 0$, $w_{\text{DE}} = -1$)

optical depth for scattering of CMB
with ionized e⁻

add Σm_s to fits of mean (mean!) observables.

#) CMB: relativistic, not a good probe; shift in matter-radiation equality, degenerates to many other effects

#) CMB lensing
#) galaxy clustering
#) cluster counts
#) Lyman- α

} distribution of matter along line-of-sight at different times
the smaller the scales, the larger effect of m_s ; but the more systematics (\rightarrow isotropy + homogeneity...)

strongest limits: $\Sigma m_s \lesssim 0.1 \text{ eV}$

BUT: degeneracies, problems, not a lab measurement (\rightarrow complementarity)

simplest models: by next 10 years; see effect of Σm_s in upcoming surveys!

Also important: $N_{eff} \rightarrow$ BBN Big Bang Nucleosynthesis (1s - 3 min, production of D, ^3He , ^4He , ^7Li)

① $T \approx 620 \dots 70^2 \text{ KeV}$ $n, d, \dots, g \rightarrow p, n$

② $\bar{\nu}_e p \leftrightarrow e^+ n$
 $\nu_e n \leftrightarrow e^- p$
 $n \leftrightarrow p e^- \nu_e$

freeze out at $T_f \approx 0.75 \text{ KeV}$
 $\left(\frac{n}{p} \right)_0 = \exp \left\{ -\frac{\Delta m}{T_f} \right\} \approx \frac{1}{6}$ $\Delta m = m_n - m_p$

neutrons decay: $\left(\frac{n}{p} \right) = \left(\frac{n}{p} \right)_0 \exp \left\{ -\frac{t}{\tau} \right\} \approx \frac{1}{7}$ after 3 min (6.2 KeV)

③ $T \approx 0.1 \text{ KeV}$: BBN starts $p(n, d) D \equiv n + p \rightarrow d + D$ $E_B = 2.2 \text{ KeV}$
 (not earlier, because $\frac{m_B}{m_p} \approx 10^{-10}$) (less than T , but too many photons...)
 (not of distribution)

then complicated nuclear chain starts, producing ^3He , ^4He , ^7Li

most goes in $D + D \rightarrow ^4\text{He} + \gamma$ stops at $A = 5, 8$, too large \rightarrow condenses being /

mass fraction of ${}^4\text{He}$: $Y = \frac{m({}^4\text{He})}{m_{\text{Baryon}}} = \frac{4m_p M_{{}^4\text{He}}}{m_p(p+m)} = \frac{4m_2}{p+m} = \frac{2m_p}{1+m_p} \approx \frac{2 \cdot 1/2}{1} = \frac{1}{2}$

$T_{\text{fn}} \propto (\sqrt{g_{\text{eff}}})^{1/3}$; $g_4 = 2 + \frac{7}{8}(4 + 2 \cdot (3 + \Delta N_{\text{eff}}))$

$\Delta N_{\text{eff}} \nearrow : T_{\text{fn}} \nearrow \Rightarrow \left(\frac{m}{p}\right) = e^{-\Delta m / T_{\text{fn}}} \nearrow \Rightarrow \frac{m}{p} \nearrow$
 $\Rightarrow Y \nearrow$

$\Rightarrow \Delta N_{\text{eff}} \leq 0.5$

Why would N_{eff} be $\neq 3$?
 \rightarrow one hot particle (BSM) would contribute
 \rightarrow right strand neutrinos...

Light sterile neutrinos

Various longstanding hints ...

LSND: 800 keV p-beam on H_2O target $L = 30$ m, $E_{\nu} \approx 30$ keV

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \approx 3 \times 10^{-3} \neq 0 \text{ at } \approx 4\sigma \Rightarrow \frac{\Delta m^2}{eV^2} \frac{L}{m} \frac{keV}{E} \sim 1$$

$$\Rightarrow \Delta m^2 = eV^2 \Rightarrow \Delta m_{21, \text{sol}}^2, \Delta m_{31, \text{atm}}^2$$

$$\sin^2 2\theta \approx 10^{-2} \Rightarrow$$

Also: MiniBoone similar parameters.

Reactor Anomaly:

Re-analysis of reactor neutrino flux (new data, $T_{reactor}$, ...)
flux 6% ^{more} than previously thought

\Rightarrow all experiments measured less neutrinos than they should
have $\Rightarrow P(\nu_e \rightarrow \nu_3)$ compatible with LSND values!

+ GALEX

We know from LEP that $z \rightarrow \nu\nu$ (invisible z -width) implies $N_s = 3$

\Rightarrow only 3 active neutrinos (with mass $< m_{z/2}$)

\Rightarrow the fourth state must be sterile (no isospin, or accompanying charged lepton)

$$\Rightarrow \mathcal{U} = \begin{pmatrix} \mathcal{U}_{e1} & \mathcal{U}_{e2} & \mathcal{U}_{e3} & \mathcal{U}_{e4} \\ \mathcal{U}_{\mu 1} & \mathcal{U}_{\mu 2} & \mathcal{U}_{\mu 3} & \mathcal{U}_{\mu 4} \\ \mathcal{U}_{\tau 1} & \mathcal{U}_{\tau 2} & \mathcal{U}_{\tau 3} & \mathcal{U}_{\tau 4} \\ \mathcal{U}_{s1} & \mathcal{U}_{s2} & \mathcal{U}_{s3} & \mathcal{U}_{s4} \end{pmatrix} \quad \begin{array}{l} \text{would contain 6 mixing angles} \\ \text{3 CP phases (+ 3 } \theta_{MNSM}) \end{array}$$

should show up everywhere \Rightarrow many tests in dedicated experiments, plus in other experiments that look for other things

In general, not consistent with cosmology $\left(\begin{array}{l} 1) N_{eff} = 4 \\ 2) \sum m_\nu \approx \sqrt{\Delta m_{41}^2} \sim eV \end{array} \right)$
 need extra new physics to address this