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Thermal relics
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Multiflavor FIMP
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Multiflavor leptophilic
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Self-interacting DM
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Conclusion
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Thermal relics beyond minimal dark sectors

Johannes Herms

Max-Planck-Institut für Kernphysik, Heidelberg

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The Dark Matter Production Mechanism Program

What is dark matter?



The Dark Matter Production Mechanism Program

What is dark matter?

Starting point:

$$\rho_{\text{DM},0} \simeq 1.26 \cdot 10^{-6} \text{ GeV cm}^{-3}$$

→ *Where did it come from?*



The Dark Matter Production Mechanism Program

What is dark matter?

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$$\rho_{\text{DM},0} \simeq 1.26 \cdot 10^{-6} \text{ GeV cm}^{-3}$$

→ *Where did it come from?*

Thermal relic particle dark matter

- stable neutral particles are automatically dark matter candidates
- thermal bath of the early Universe accounts for production

→ *relate production to signatures*



Thermal history of the visible sector

- All we know about early Universe is from *relic particles*
- *Relic abundances* calculable from GR + known particle and atomic physics
 - $T_\gamma \sim \text{MeV}$: neutrinos decouple $\rightarrow \rho_\nu$
 - $T_\gamma \sim \text{MeV}$: neutrons decouple $\rightarrow {}^4\text{He}/\text{H}$
 - $T_\gamma \sim 0.1 \text{ MeV}$: nuclear reactions decouple $\rightarrow \text{D}/\text{H}, {}^3\text{He}/\text{H}, {}^7\text{Li}/\text{H}$
 - $T_\gamma \sim \text{eV}$: atoms form, photons decouple $\rightarrow \text{CMB}$
 - *however*: proton relic abundance instead determined by baryon asymmetry



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- can *extrapolate* cosmology to earlier times
 - assuming SM particle physics



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 - *however*: proton relic abundance instead determined by baryon asymmetry
- $t \geq 1 \text{ s}$, Universe is dominated by SM radiation bath of temperature T
- can *extrapolate* cosmology to earlier times
 - assuming SM particle physics
- introducing (meta-)stable particles that interact with the SM, we can relate their properties to their relic abundance

maybe dark matter is a thermal relic, too?



This talk

① thermal relics

- textbook basics
- WIMP successes
- simple model failures

② details in the dark: multiple DM candidates

③ details in the dark: self-interactions



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Early Universe thermodynamics

Boltzmann Equation

std. treatment [GondoloGelmini'91]

$$E \frac{\partial f_\chi}{\partial t} - \textcolor{blue}{H} |\vec{p}|^2 \frac{\partial f_\chi}{\partial E} = -\frac{1}{2g_\chi} \int d\Pi_b d\Pi_i d\Pi_j (2\pi)^4 \delta^4 (p_\chi + p_b - p_i - p_j) \\ \times |\mathcal{M}|_{\chi+b \leftrightarrow i+j}^2 [f_\chi \textcolor{blue}{f}_b (1 \pm \textcolor{blue}{f}_i) (1 \pm \textcolor{blue}{f}_j) - f_i f_j (1 \pm f_\chi) (1 \pm \textcolor{blue}{f}_b)] + \dots$$

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- assume SM bath dominates Universe

$$\textcolor{blue}{H}^2 = \frac{8\pi G}{3} \rho_R \quad \text{with} \quad \rho_R = \frac{\pi^2}{30} g_{\text{eff}}(T) T^4, \quad \textcolor{blue}{f}_{\text{SM}}(\vec{p}) = \frac{1}{e^{(E-\mu)/T} \pm 1}$$

- assume *kinetic equilibrium*, MB, $f_\chi(E) \rightarrow e^{\mu/T} e^{-E/T}$

$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle \sigma v \rangle_{\chi+b \rightarrow i+j} \left(n_\chi n_b - n_\chi^{\text{eq}} n_b^{\text{eq}} \frac{n_i n_j}{n_i^{\text{eq}} n_j^{\text{eq}}} \right) + \dots,$$

$$\langle \sigma v \rangle = \frac{1}{n_\chi^{\text{eq}} n_b^{\text{eq}}} \int d^3 p_\chi d^3 p_b \sigma v_{\text{Mol}} e^{-(E_\chi + E_b)/T}$$

for absence of kin.eq., see eg. [1706.07433]



Thermal dark matter production

WIMP freeze-out: the standard paradigm

- The WIMP paradigm:

- DM stabilised by a dark parity
- freeze-out of $2 \rightarrow 2$ interactions determines the relic density

$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle\sigma v\rangle_{\chi\chi \rightarrow \text{SM}} \left(n_\chi^2 - n_\chi^{\text{eq}2} \right)$$



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Thermal dark matter production

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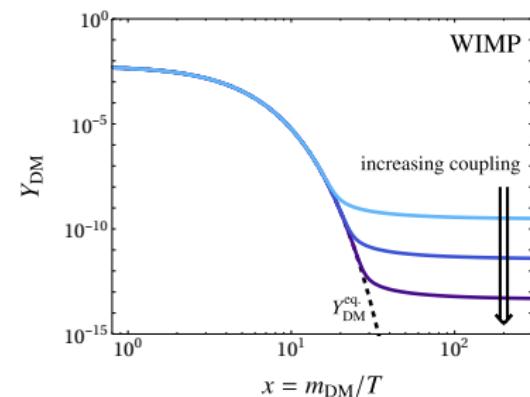
- DM stabilised by a dark parity
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$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle\sigma v\rangle_{\chi\chi \rightarrow \text{SM}} \left(n_\chi^2 - n_\chi^{\text{eq},2} \right)$$

- introduce evolution parameter
 $x = m/T$ and abundance $Y \equiv n/s$

$$\frac{dY_\chi}{dx} = -\frac{s\langle\sigma v\rangle_{\chi\chi \rightarrow \text{SM}}}{xH} \left(Y_\chi^2 - Y_\chi^{\text{eq},2} \right)$$

$$Y_{\text{DM}}^{\text{observed}} = 4.35 \cdot 10^{-10} \left(\frac{m_{\text{DM}}}{\text{GeV}} \right)^{-1}$$



- quick estimate: $n_\chi(x_{\text{fo}})\langle\sigma v\rangle(x_{\text{fo}}) \simeq H(x_{\text{fo}})$, $Y_\chi|_{\text{today}} \simeq Y_\chi^{\text{eq}}(x_{\text{fo}})$

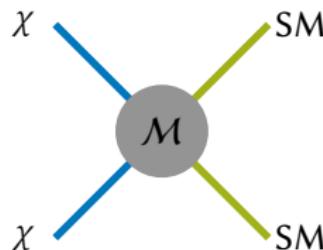
$$\langle\sigma v\rangle_{\chi\chi \rightarrow \text{SM}} \simeq (2 \sim 3) \times 10^{-26} \text{ cm}^3/\text{s}$$



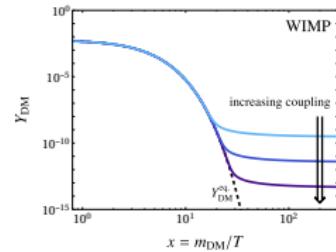
Thermal dark matter production

WIMP freeze-out: the search

The WIMP paradigm is very predictive and has inspired a large experimental program.



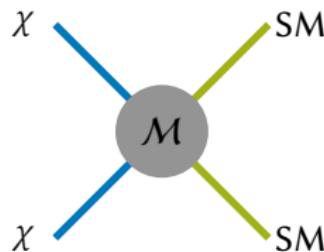
$\langle\sigma v\rangle_{T \sim m/20}$ determines relic abundance



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$\langle\sigma v\rangle_{T \sim m/20}$ determines relic abundance



$\langle\sigma v\rangle_{v \sim v_{gal}}$ dark matter indirect detection

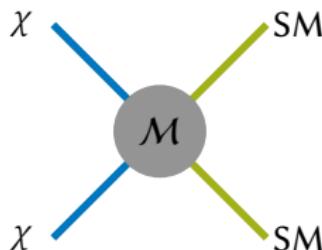


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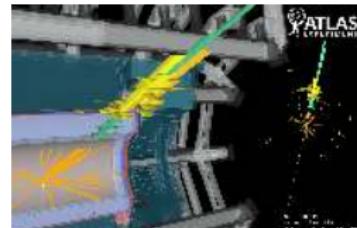
Thermal dark matter production

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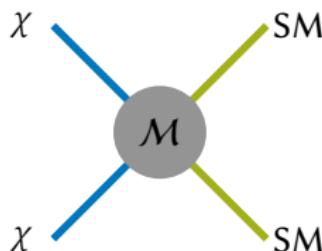
-  $\langle\sigma v\rangle_{T \sim m/20}$ determines relic abundance
-  $\langle\sigma v\rangle_{v \sim v_{\text{gal}}}$ dark matter indirect detection
-  $\sigma_{pp \rightarrow \chi\chi + X}$ collider signatures



Thermal dark matter production

WIMP freeze-out: the search

The WIMP paradigm is very predictive and has inspired a large experimental program.



-  $\langle\sigma v\rangle_{T \sim m/20}$ determines relic abundance
-  $\langle\sigma v\rangle_{v \sim v_{\text{gal}}}$ dark matter indirect detection
-  $\sigma_{pp \rightarrow \chi\chi + X}$ collider signatures
-  $\sigma_{\chi n}$ dark matter direct detection



Thermal dark matter production

Freeze-out: variations on a theme

there may be multiple particles odd under the stabilising symmetry
 \Rightarrow *dark sector*

- *co-annihilation*: other particles in the dark sector may aid DM depletion [Griest,Seckel'91]
 - *chemical equilibrium* within the dark sector \rightarrow effective WIMP

$$n_i = n_{\text{dark}} \left(\frac{n_i^{\text{eq}}}{n_{\text{dark}}^{\text{eq}}} \right) \quad \Rightarrow \quad \frac{dn_{\text{dark}}}{dt} + 3Hn_{\text{dark}} = -\langle \sigma v \rangle_{\text{eff}} \left(n_{\text{dark}}^2 - n_{\text{dark}}^{\text{eq}2} \right)$$

- different processes can deplete the dark sector, e.g.
 - $2 \rightarrow 2$ may be “forbidden” [1505.07107,2012.11766] $\Rightarrow 3 \rightarrow 2$ [1702.07716]
 - “secluded” dark matter, annihilation into unstable dark sector particles [0711.4866]
 - dark matter number changing interactions $\phi\phi\phi \rightarrow \phi\phi$, $\chi\chi\chi\chi \rightarrow \chi\chi$
 - ...
- same motivation, different signatures possible

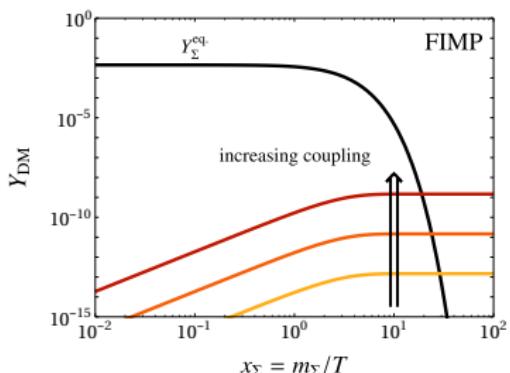


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Thermal dark matter production

Freeze-in: FIMPs

example: from heavy particle decay



$$\frac{dn_\chi}{dt} + 3Hn_\chi = \langle \Gamma_{\Sigma \rightarrow \chi X} \rangle \left(n_\Sigma - n_\Sigma^{\text{eq}} \frac{n_\chi}{n_\chi^{\text{eq}}} \right) - \langle \sigma v \rangle_{\chi\chi \rightarrow \text{SM}} \left(n_\chi^2 - n_\chi^{\text{eq}2} \right)$$

- for FIMP from heavy particle Σ decay

$$c\tau_\Sigma \simeq 1.6 \text{ m} \times g_\Sigma \left(\frac{m_\Sigma}{100 \text{ GeV}} \right)^{-2} \left(\frac{m_\chi}{10 \text{ keV}} \right) \left(\frac{\Omega_\chi}{\Omega_{\text{DM}}} \right)^{-1}$$

- lack of thermalisation → cosmological history relevant!



Let's look at an example!

A simple example...

Singlet scalar dark matter

The simplest model, arguably

- add one dof. to the SM, real scalar singlet ϕ , stabilised by a \mathbb{Z}_2

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - \frac{1}{2} m^2 \phi^2 - \frac{1}{4!} \lambda_\phi \phi^4 - \frac{1}{2} \lambda_{\phi h} (H^\dagger H) \phi \phi$$

- production in SM thermal bath

$$\frac{dn_\phi}{dt} + 3Hn_\phi = - \langle \sigma v \rangle_{\phi\phi \rightarrow \text{SM}} \left(n_\phi^2 - n_\phi^{\text{eq2}} \right) \quad \leftarrow \text{WIMP}$$

$$- \langle \sigma v \rangle_{\phi\phi\phi\phi \rightarrow \phi\phi} \left(n_\phi^4 - n_\phi^2 n_\phi^{\text{eq2}} \right) \quad \leftarrow \text{SIMP}$$

$$+ \langle \Gamma_{h \rightarrow \phi\phi} \rangle \left(n_h - n_h^{\text{eq}} n_\phi^2 / n_\phi^{\text{eq2}} \right) \quad \leftarrow \text{FIMP}$$

- different mechanisms can determine the relic abundance

- standard WIMP
- self-interactions → SIMP [eg. 1906.07659]
- freeze-in [eg. 1908.05491]



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- different mechanisms can determine the relic abundance
 - standard WIMP ✓
 - self-interactions → SIMP [eg. 1906.07659] ?
 - freeze-in [eg. 1908.05491] ✗ $\lambda_{\phi h} \lesssim 10^{-10}$; no signatures!
 - signatures?



I like minimal models – why?

- laziness.
- Occam's razor?

I like minimal models – why?

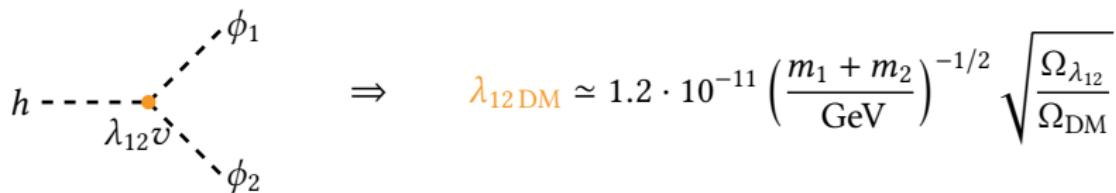
- laziness.
- Occam's razor?
 - dark matter identification is not a beauty pageant → not really...
- simple = generic?
 - simple model → expect to find common signatures
 - what do we do if we find *no* signatures?
→ take more detail into account!

Multi-flavour singlet scalars

Add two real scalars $\phi_{1,2}$ to the SM, stabilised by a \mathbb{Z}_2

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2} \partial_\mu \phi_i \partial^\mu \phi_i - \frac{1}{2} m_{ij} \phi_i \phi_j - \frac{1}{4!} \lambda'_{ijkl} \phi_i \phi_j \phi_k \phi_l - \frac{1}{2} \lambda'_{ij} \left(H^\dagger H \right) \phi_i \phi_j,$$

FIMP production is governed by the decay


$$\Rightarrow \lambda_{12 \text{ DM}} \simeq 1.2 \cdot 10^{-11} \left(\frac{m_1 + m_2}{\text{GeV}} \right)^{-1/2} \sqrt{\frac{\Omega_{\lambda_{12}}}{\Omega_{\text{DM}}}}$$

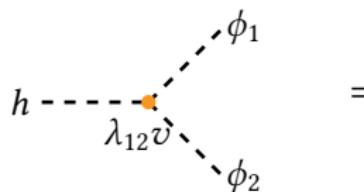


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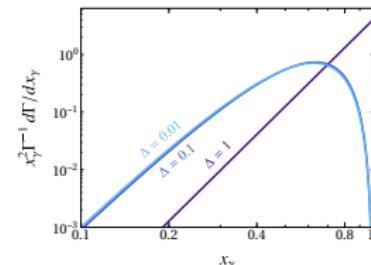
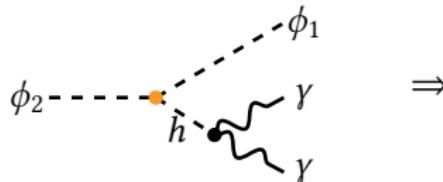
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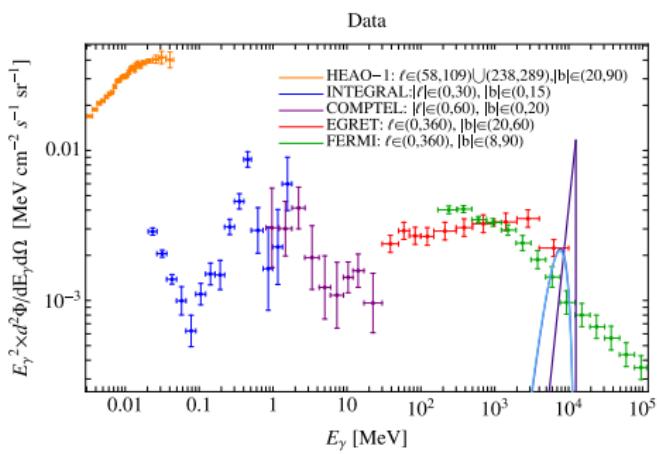
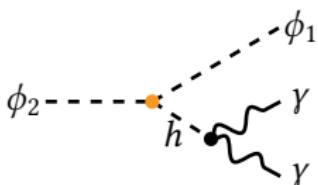


$\Rightarrow \lambda_{12 \text{ DM}} \simeq 1.2 \cdot 10^{-11} \left(\frac{m_1 + m_2}{\text{GeV}} \right)^{-1/2} \sqrt{\frac{\Omega_{\lambda_{12}}}{\Omega_{\text{DM}}}}$

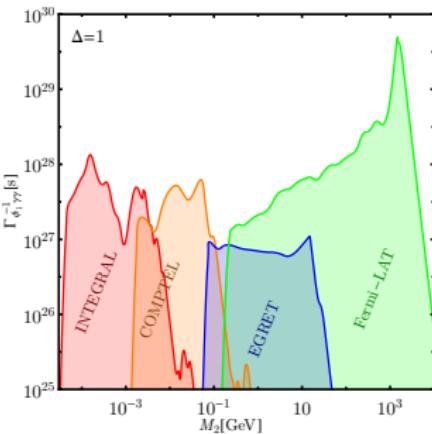
λ_{12} induces dark matter decay into γ -rays [Ghosh et.al. 1909.13292]



Gamma ray spectral features



adapted from Essig et.al. [1309.4091]



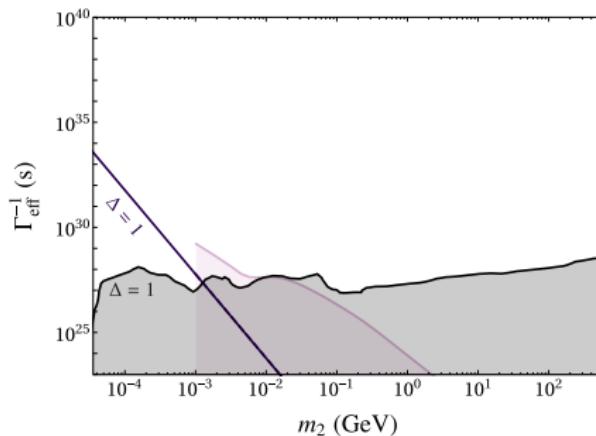
Ghosh et.al. [1909.13292]



Probing multiflavour FIMP dark matter

1912.09458 w. Alejandro Ibarra

⇒ can relate production mechanism to signature!



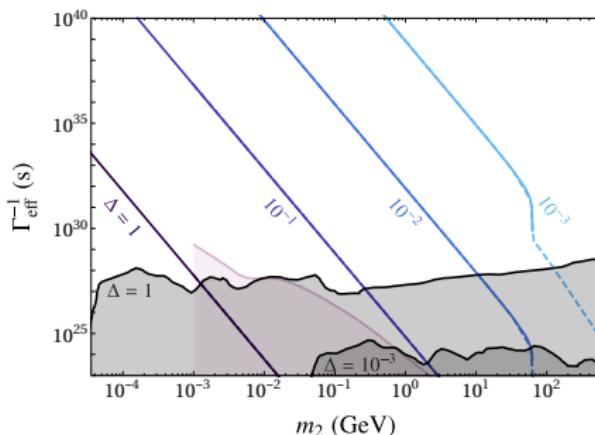
- Lines show expected signal strength for $\Omega_{\lambda_{12}} = \Omega_{\text{DM}}$
- small mass splitting $\Delta \equiv 1 - m_1^2/m_2^2$ suppresses signal
- $\delta m_{ij}^2 \sim \lambda'_{ij} v^2 / 2 \sim \text{MeV}$



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- $\delta m_{ij}^2 \sim \lambda'_{ij} v^2 / 2 \sim \text{MeV}$



Generally: What about DM-“flavour”?

- SM fermions come in 3 generations, 1st generation dominates cosmology and astrophysics
- DM fermions?

however...

- “Flavour physics” relies on complex, chiral nature of SM
- Flavour violation limits put strong constraints on non-trivial flavoured interactions of DM [eg. Kopp+’1401.6457]

\Rightarrow as first step: look at 2 DM candidates w. same gauge QNs



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Fermionic multi-flavour Dark Matter

DM fermion $\psi_{1,2}$, odd under \mathbb{Z}_2 → need mediator Σ to couple to SM

$$\begin{aligned}\mathcal{L} \supset & (\mathcal{D}_\mu \Sigma)^\dagger (\mathcal{D}^\mu \Sigma) - m_\Sigma \Sigma^\dagger \Sigma - \lambda_{H\Sigma} |H|^2 |\Sigma|^2 \\ & + \left(\frac{1}{2} \bar{\psi}_i i \not{\partial} \psi_i - \frac{1}{2} m_i \bar{\psi}_i^c \psi_i - g_i \bar{f}_{R,L} \psi_i \Sigma + \text{h.c.} \right)\end{aligned}$$



Fermionic multi-flavour Dark Matter

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- choose *leptophilic* scenario

$$\mathcal{L} \supset -g_i \bar{l}_R \psi_i \Sigma$$

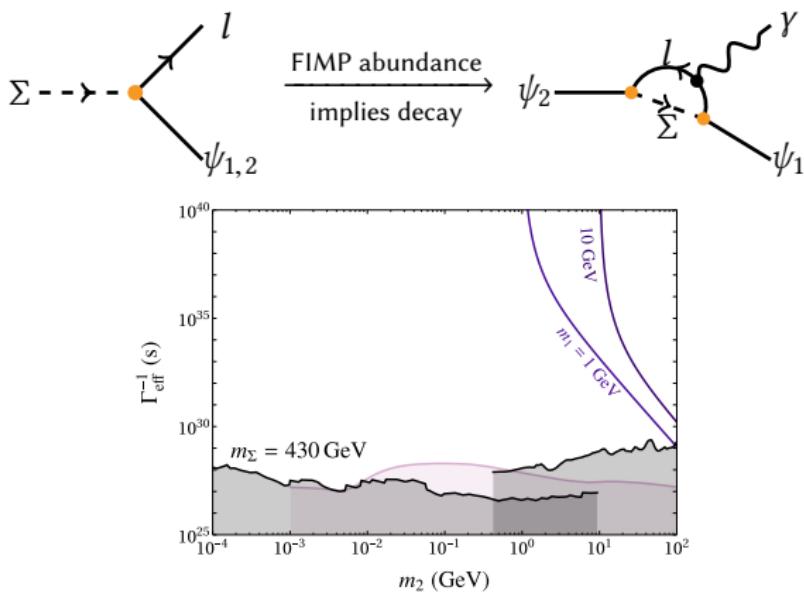
- single component scenario popular model: m_Σ, m_1, g_1
- multi-flavour scenario:

$$m_\Sigma, m_2, m_1, g_2, g_1$$

→ *qualitatively different signatures?*



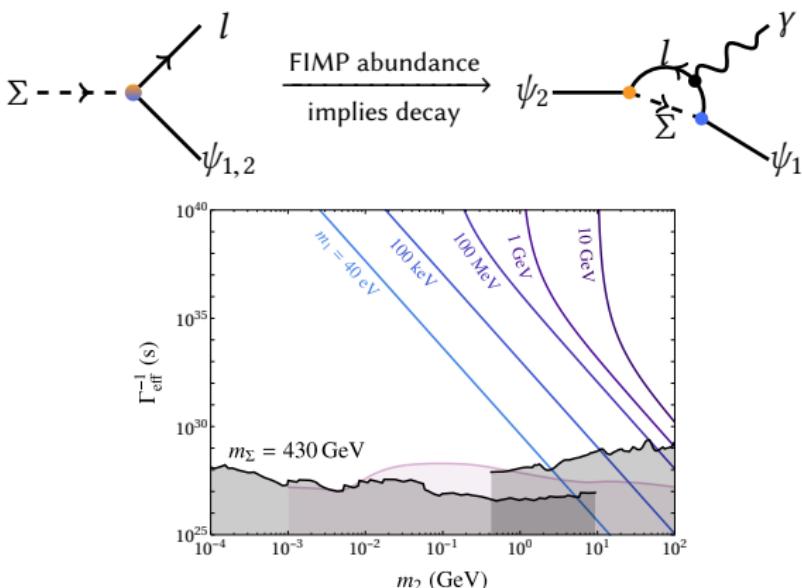
Decaying fermion FIMP DM



- Decay signal suppressed by two small couplings
- γ -ray line limits from [FermiLAT'1506.00013] and [Essig+'1309.4091], CMB limits from [Slatyer+'1610.06933]



Decaying fermion FIMP DM



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- γ -ray line limits from [FermiLAT'1506.00013] and [Essig+'1309.4091], CMB limits from [Slatyer+'1610.06933]
- large coupling possible for small $m_1 \Rightarrow$ how small?



Lower limits to the DM mass

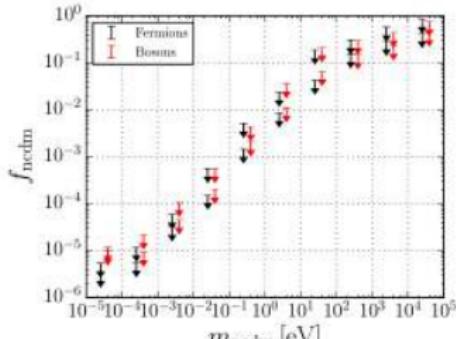
- general: DM free-streaming erases primordial inhomogeneities

$$\lambda_{\text{FS}} = \int_{t_i}^{t_{\text{EQ}}} \frac{\langle v \rangle(t')}{R(t')} dt'$$

- limits on DM mass [Irsic+, 1702.01764]

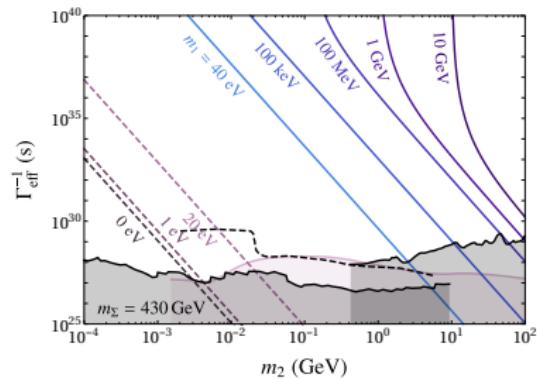
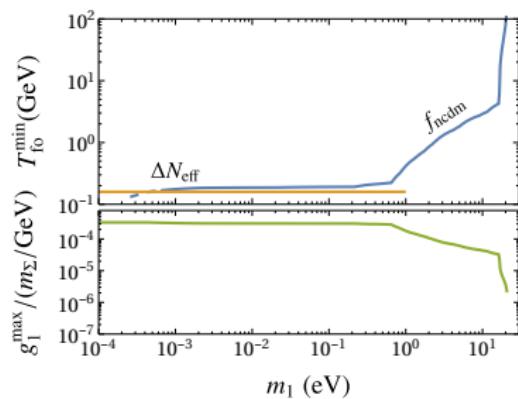
$$m_{\text{WDM}} > 5.3 \text{ keV} \xrightarrow[\text{[Kamada+ 1907.04558]}]{\text{recast to}} m_{\text{FIMP}} > 15.6 \text{ keV} \cdot \left(\frac{106.75}{g_{s,\text{eff}}(T_{\text{prod}})} \right)^{1/3}$$

- WDM actually rather cool: $\Omega_{\text{DM}}^{\text{obs}} \equiv (T_{\text{WDM}}/T_V)^3 (m_{\text{WDM}}/94 \text{ eV})$
- subdominant non-cold component [eg. Diamanti+ 1701.03128]



Mixed FIMP - HDM

- for very light m_1 : g_1 allowed to thermalise ψ_1
- abundance set by $T_{\text{fo},1}$
- coupling g_1 constrained by f_{ncdm}



- signals possible in proposed MeV-range γ -ray instruments [eg. eASTROGAM, 1711.01265]



Full range of couplings

General 2-flavour leptophilic DM thermal relics

solve Boltzmann eqn. to obtain relic abundance ($i = \psi_1, \psi_2, \Sigma$)

$$\begin{aligned} \frac{dn_i}{dt} + 3Hn_i = & - \sum_j \langle \sigma v \rangle_{ij \rightarrow AB}^{\text{ann}} \left(n_i n_j - n_i^{\text{eq}} n_j^{\text{eq}} \right) \\ & - \sum_j \langle \sigma v \rangle_{iA \rightarrow jB}^{\text{sca}} \left(n_i n_A^{\text{eq}} - n_j n_B^{\text{eq}} \frac{n_i^{\text{eq}}}{n_j^{\text{eq}}} \right) \\ & - \sum_j \tilde{\Gamma}_{i \rightarrow j} \left(n_i - n_j \frac{n_i^{\text{eq}}}{n_j^{\text{eq}}} \right), \end{aligned}$$

fast conversions can ensure chemical equilibrium $n_i = n_{\text{dark}} \frac{n_i^{\text{eq}}(T)}{n_{\text{dark}}^{\text{eq}}(T)}$,

$$\frac{dn_{\text{dark}}}{dt} + 3Hn_i = -\langle \sigma v \rangle_{\text{eff}}^{\text{ann}} \left(n_{\text{dark}}^2 - n_{\text{dark}}^{\text{eq}}{}^2 \right)$$

[Griest,Seckel'91], ...



Numerical solution to the Boltzmann Eqn

- no chemical equilibrium → no MICROMEGRAs etc.
- cast BE into numerics-friendly form

$$\frac{d \ln Y_i}{dx} = - \sum_j \left[\frac{\langle \sigma v \rangle_{ij \rightarrow AB}^{\text{ann}} s Y_i \frac{Y_j^{\text{eq}}}{Y_i^{\text{eq}}} }{x \tilde{H}} \right] \left(\frac{Y_j}{Y_i} \frac{Y_i^{\text{eq}}}{Y_j^{\text{eq}}} - \frac{Y_i^{\text{eq}}{}^2}{Y_i^2} \right) - \sum_j \left[\frac{\langle \sigma v \rangle_{iA \rightarrow jB}^{\text{sca}} s Y_A^{\text{eq}} }{x \tilde{H}} + \frac{\tilde{\Gamma}_{i \rightarrow j}}{x \tilde{H}} \right] \left(1 - \frac{Y_j}{Y_i} \frac{Y_i^{\text{eq}}}{Y_j^{\text{eq}}} \right).$$

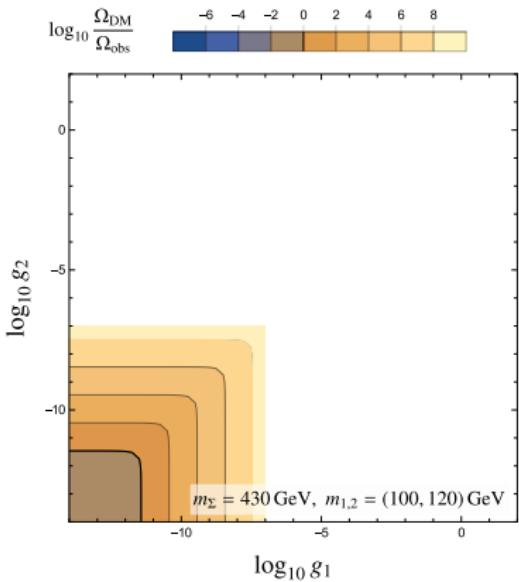
- if $\Gamma_{\text{aa} \leftrightarrow \text{bb}} \gg H$: stiff equation!
- physics to the rescue: consider summed equation, imposing equilibrium relations



Full range of couplings

The full range of couplings

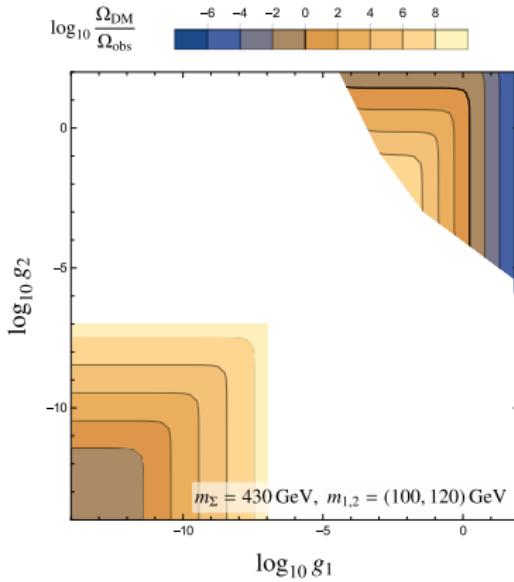
- Numerically solve Boltzmann system for particles $i = \Sigma, \psi_2, \psi_1$ in complete coupling parameter space



Full range of couplings

The full range of couplings

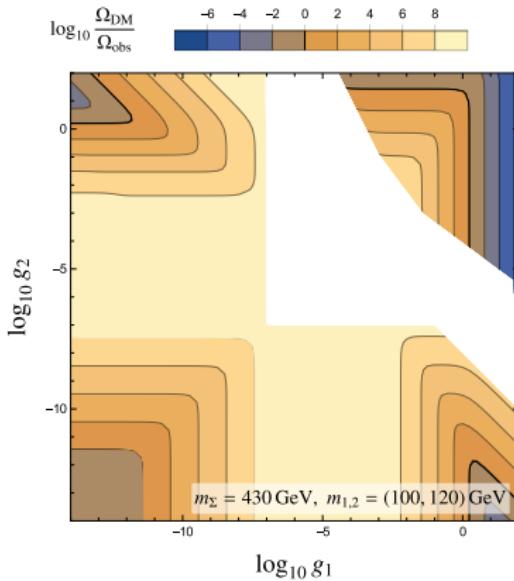
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Full range of couplings

The full range of couplings

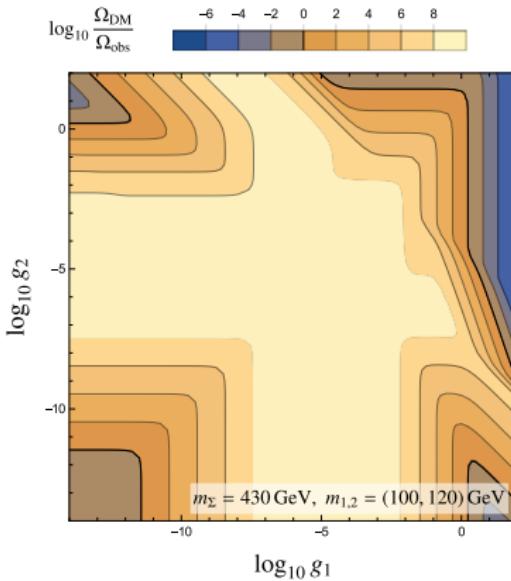
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Full range of couplings

The full range of couplings

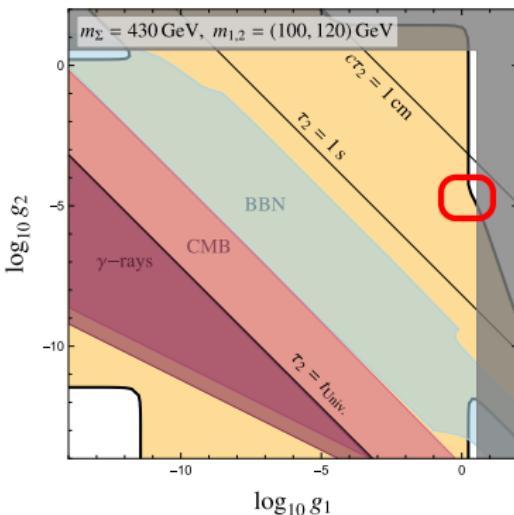
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Full range of couplings

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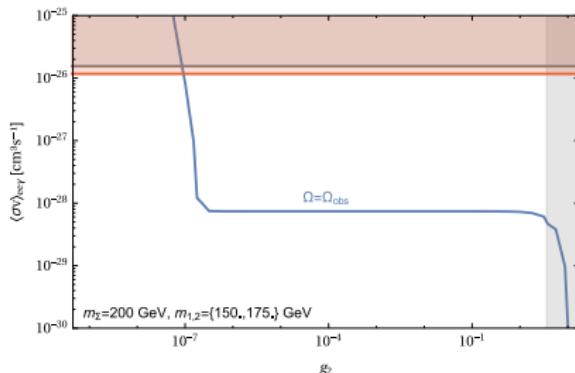
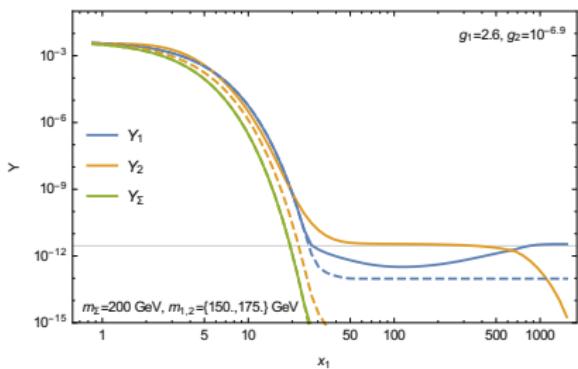


- most of parameter space ruled out by overabundance
- complex interplay of reactions in WIMP-WIMP region



2nd component effects on WIMP signatures

- even if ψ_2 not around today, can modify expectations for WIMP signals



- commonplace: reduction of signals due to *coannihilation*
- here: can have *enhancement of $\langle\sigma v\rangle$* over canonical WIMP value
 - surprises possible also for instruments that don't reach canonical benchmark



Falsifying WIMP Dark Matter?

- direct/indirect/collider WIMP identification inconclusive so far
- WIMP CDM scenario has other predictions
 - cuspy halos following Navarro-Frenk-White profile [NFW'97]
 - subhalos form down to $M_{\text{halo}} \ll M_{\odot}$ [eg. Bringmann'09]
- small scale issues of Λ CDM
 - cored halos, diverse halos [eg. 1504.01437]
 - missing satellites, missing small-but-“too-big-to-fail” galaxies [eg. 1111.2048]
- dark matter *self-interactions*? [review eg. 1705.02358] [1904.10539]
 - thermalised cores
 - host halo effects amplified
 - gravothermal collapse possible



Self interacting dark matter

Singlet fermions for concreteness, “sterile neutrino”

$$\mathcal{L}_{\text{DM}} = \frac{1}{2} \overline{\chi^c} i\not{\partial} \chi - \frac{1}{2} m_\chi \overline{\chi^c} \chi - y_\chi \overline{L} \widetilde{H} \chi + \frac{1}{4! \Lambda^2} (\overline{\chi^c} \chi)(\overline{\chi^c} \chi) + \text{h.c.}$$

- self-scattering

$$\sigma_{2 \rightarrow 2} = \frac{1}{72\pi} \frac{m_\chi^2}{\Lambda^4}$$

- constraints

$$\sigma_{2 \rightarrow 2}/m_{\text{DM}} \lesssim 1 \text{ cm}^2/\text{g}$$



[0704.0261]



Self interacting dark matter

Singlet fermions for concreteness, “sterile neutrino”

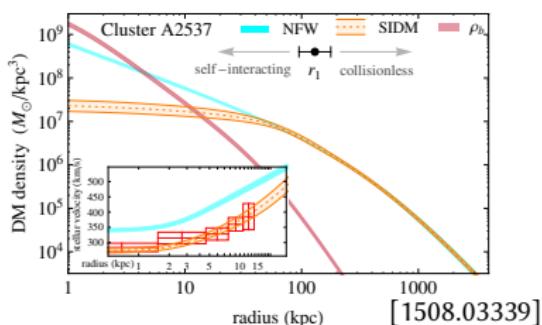
$$\mathcal{L}_{\text{DM}} = \frac{1}{2} \overline{\chi^c} i\not{\partial} \chi - \frac{1}{2} m_\chi \overline{\chi^c} \chi - y_\chi \overline{L} \widetilde{H} \chi + \frac{1}{4! \Lambda^2} (\overline{\chi^c} \chi)(\overline{\chi^c} \chi) + \text{h.c.}$$

- self-scattering

$$\sigma_{2 \rightarrow 2} = \frac{1}{72\pi} \frac{m_\chi^2}{\Lambda^4}$$

- constraints and possible evidence?

$$0.1 \text{ cm}^2/\text{g} \lesssim \sigma_{2 \rightarrow 2}/m_{\text{DM}} \lesssim 1 \text{ cm}^2/\text{g}$$



[0704.0261]



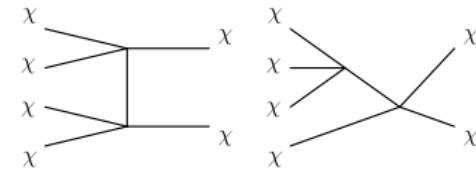
Majorana SIMPs

connecting self-interactions to DM production

- number-changing interactions can deplete n_χ

$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle\sigma v^3\rangle_{4 \rightarrow 2} \left(n_\chi^4 - n_\chi^2 n_\chi^{\text{eq}2} \right)$$

→ Strongly Interacting Massive Particle (SIMP) DM

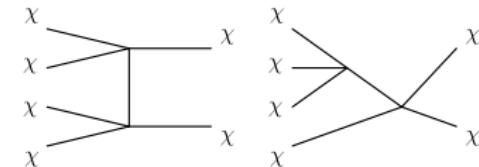


Majorana SIMPs

connecting self-interactions to DM production

- number-changing interactions can deplete n_χ

$$\frac{dn_\chi}{dt} + 3H(\textcolor{blue}{T})n_\chi = -\langle \sigma v^3 \rangle_{4 \rightarrow 2} \left(n_\chi^4 - n_\chi^2 n_\chi^{\text{eq}2}(\textcolor{orange}{T'}) \right)$$



→ Strongly Interacting Massive Particle (SIMP) DM

- what about T' ?

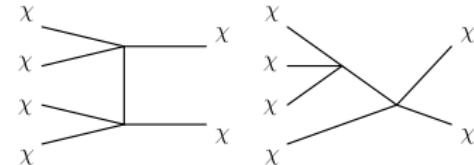


Majorana SIMPs

connecting self-interactions to DM production

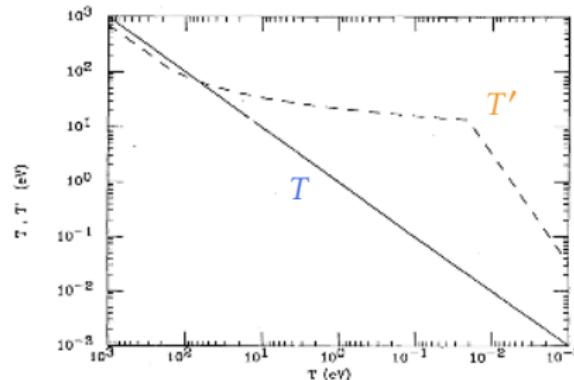
- number-changing interactions can deplete n_χ

$$\frac{dn_\chi}{dt} + 3H(T)n_\chi = -\langle\sigma v^3\rangle_{4 \rightarrow 2} \left(n_\chi^4 - n_\chi^2 n_\chi^{\text{eq}}(T') \right)$$



→ Strongly Interacting Massive Particle (SIMP) DM

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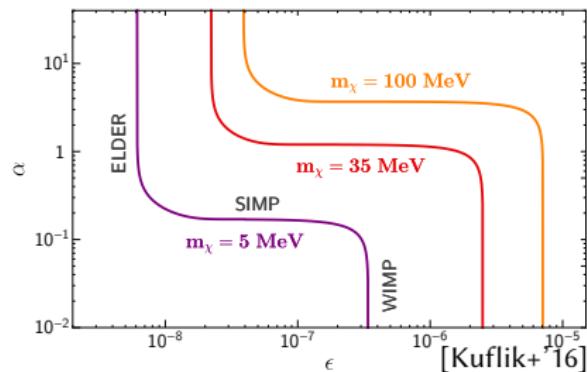
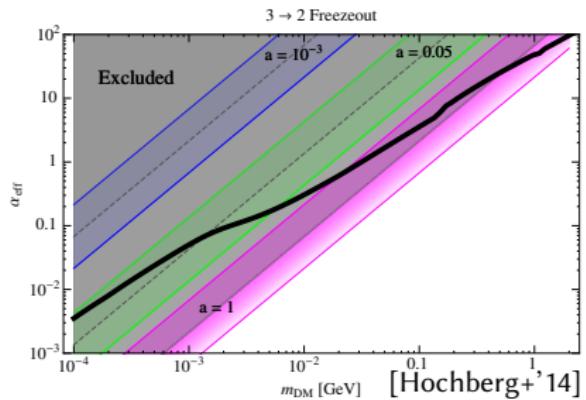
[Carlson+’92]

Johannes Herms



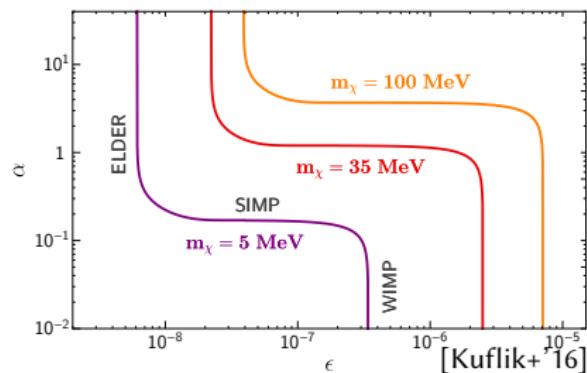
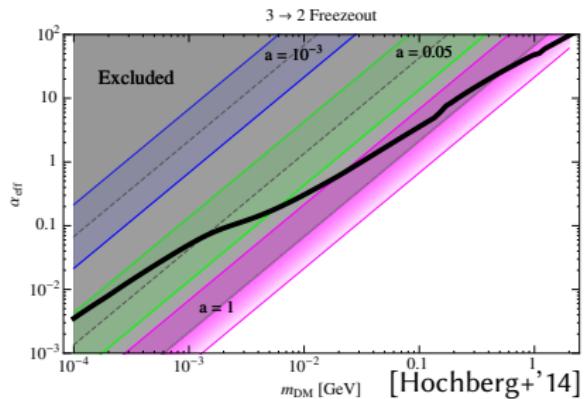
Solutions to the SIMP heat problem

- couple DM to SM kinetically, $T' \equiv T$ [Hochberg+ '14]
 - dump entropy to SM → need sizable couplings!



Solutions to the SIMP heat problem

- couple DM to SM kinetically, $T' \equiv T$ [Hochberg+ '14]
 - dump entropy to SM → need sizable couplings!



- start out colder, $T'(0) < T(0)$ [e.g. Bernal, Chu '15]
 - both 3 → 2, 4 → 2 possible
 - less predictive, depends on initial condition



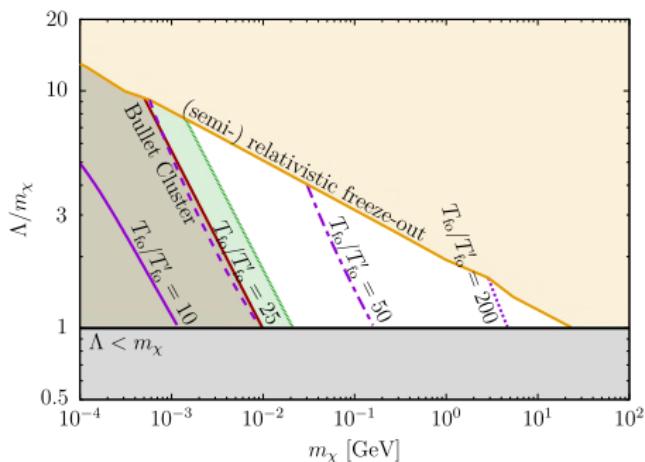
Self-interacting Majorana singlets

1802.02973 w. Takashi Toma, Alejandro Ibarra

$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle \sigma v^3 \rangle_{4 \rightarrow 2} \left(n_\chi^4 - n_\chi^2 n_\chi^{\text{eq}2} \right)$$

- instantaneous freeze-out approx

$$H(T_{\text{fo}}) = \langle \sigma v^3 \rangle(T'_{\text{fo}}) n_\chi^3(T'_{\text{fo}})$$



Populating the dark sector in a UV-complete model

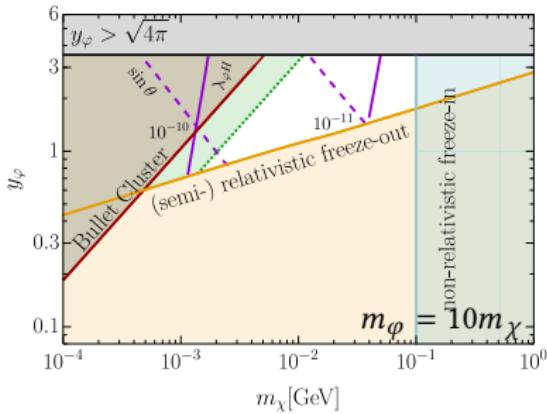
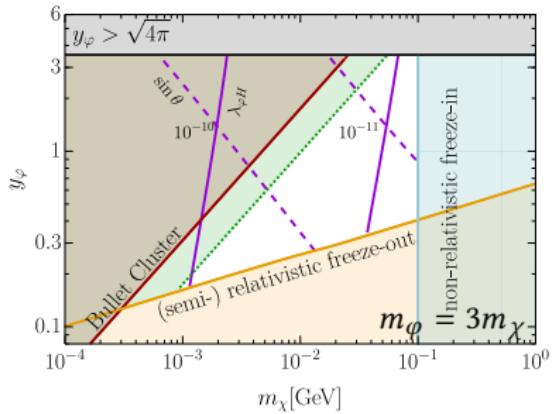
add a real scalar!

$$\mathcal{L}_{\varphi, \text{int}} = -\frac{y_\varphi}{2} \varphi \overline{\chi^c} \chi - \mu_{\varphi H} \varphi |H|^2 - \frac{1}{2} \lambda_{\varphi H} \varphi^2 |H|^2$$

- Higgs portal as possible source of dark entropy

$$\frac{d(\rho'/\rho)}{dT} = -\frac{1}{HT\rho} \Gamma_{h \rightarrow \text{dark}} m_h n_h(T)$$

- relate ρ'/ρ to entropy ratio $S/S' = s/s' \equiv \zeta \in [10^5, 10^{10}]$



- recently: methods to extend to relativistic regions [1906.07659]



Conclusions

- Thermal relic scenario attractive and plausible
 - implications for particle physics
 - implications for astrophysical DM properties
- production modelling to find range of expectable signatures
- multi-flavour dark matter
 - predicts signals in otherwise untestable FIMP regime
 - can amplify/reduce WIMP signals
- self-interacting dark matter
 - interesting astrophysical hints
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Conclusions

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Future directions

- *self-thermalisation* of decoupled dark sectors?
- *tests of decoupled dark sectors?*
- can we get any mileage out of dark sector entropy?
- where else do we need to model harder to arrive at signatures?



Backup

Gamma ray signals from dark matter

- Gamma ray flux measured by telescopes

$$\frac{d\Phi}{dE_\gamma}(E_\gamma, \psi) = \frac{1}{4\pi} \int_{\text{l.o.s.}} ds Q(E_\gamma, \vec{r}(s, \psi))$$

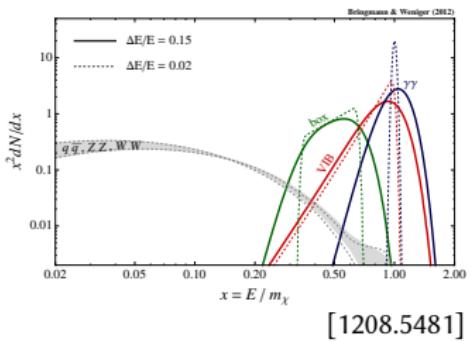
- source terms

$$Q_{\text{dec}}(E, \vec{r}) = \Gamma_{\text{dec}} \left(\frac{\rho_{\text{DM}}(\vec{r})}{m_{\text{DM}}} \right) \frac{dN_\gamma}{dE}$$

$$Q_{\text{ann}}(E, \vec{r}) = \langle \sigma v \rangle_{\text{ann}} \left(\frac{\rho_{\text{DM}}(\vec{r})}{m_{\text{DM}}} \right)^2 \frac{dN_\gamma}{dE}$$

- extragalactic contribution

$$\frac{d\Phi_{\text{extragalactic}}^{\text{dec}}}{dE_\gamma}(E_\gamma) = \frac{1}{4\pi} \frac{\Omega_{\text{DM}} \rho c}{m_{\text{DM}}} \int_0^\infty dz \frac{1}{H(z)} \frac{d\Gamma}{dE_\gamma}(E_\gamma(1+z)) e^{-\tau(E_\gamma, z)}$$



[1208.5481]



Numerical solution of the Boltzmann equation

- Boltzmann system for particles $i = \Sigma, \psi_2, \psi_1$

$$\begin{aligned} \frac{dn_i}{dt} + 3Hn_i &= - \sum_j \langle \sigma v \rangle_{ij \rightarrow AB}^{\text{ann}} \left(n_i n_j - n_i^{\text{eq}} n_j^{\text{eq}} \right) \\ &\quad - \sum_j \langle \sigma v \rangle_{iA \rightarrow jB}^{\text{sca}} \left(n_i n_A^{\text{eq}} - n_j n_B^{\text{eq}} \frac{n_i^{\text{eq}}}{n_j^{\text{eq}}} \right) \\ &\quad - \sum_j \tilde{\Gamma}_{i \rightarrow j} \left(n_i - n_j \frac{n_i^{\text{eq}}}{n_j^{\text{eq}}} \right) \\ \frac{d \ln Y_i}{dx} &= - \sum_j \left[\frac{\langle \sigma v \rangle_{ij \rightarrow AB}^{\text{ann}} s Y_i \frac{Y_j^{\text{eq}}}{Y_i^{\text{eq}}}}{x \tilde{H}} \right] \left(\frac{Y_j}{Y_i} \frac{Y_i^{\text{eq}}}{Y_j^{\text{eq}}} - \frac{Y_i^{\text{eq}}{}^2}{Y_i^2} \right) \\ &\quad - \sum_j \left[\frac{\langle \sigma v \rangle_{iA \rightarrow jB}^{\text{sca}} s Y_A^{\text{eq}}}{x \tilde{H}} + \frac{\tilde{\Gamma}_{i \rightarrow j}}{x \tilde{H}} \right] \left(1 - \frac{Y_j}{Y_i} \frac{Y_i^{\text{eq}}}{Y_j^{\text{eq}}} \right). \end{aligned}$$

- fast rates give stiff equation → use summed equations if chemical equilibrium



Evolution of a decoupled dark sector

- Boltzmann equations

$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle\sigma v^3\rangle \left(n_\chi^4 - n_\chi^2 n_\chi^{\text{eq}2} \right),$$

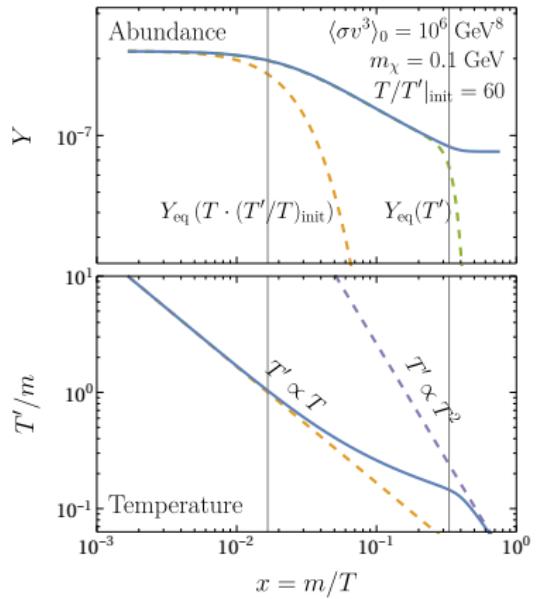
$$\frac{d\rho_\chi}{dt} + CH\rho_\chi = 0$$

with

$$C(x) = \frac{1}{\rho}(3\rho + 3\mathcal{P})$$

- T' from

$$\frac{\rho}{n} = m \left(\frac{K_1(x')}{K_2(x')} + \frac{3}{x'} \right)$$



Populating the dark sector

- energy transfer from SM through Higgs decay

$$\frac{d\rho'}{dt} + CH\rho' = \frac{g_i}{(2\pi)^3} \int f_h(p) E_h(p) \Gamma_h(E_h(p)) d^3p = \Gamma_{h \rightarrow \text{dark}} m_h n_h(T)$$

$$\frac{d(\rho'/\rho)}{dT} = -\frac{1}{HT\rho} \Gamma_{h \rightarrow \text{dark}} m_h n_h(T)$$

- relate ρ'/ρ to entropy ratio $S/S' = s/s' \equiv \zeta$

$$T'_{\text{fi}} = T_{\text{fi}} \left(\frac{g_{\text{SM}}(T_{\text{fi}})}{g_{\text{dark}}(T'_{\text{fi}})} \cdot \left. \frac{\rho'}{\rho} \right|_{\text{fi}} \right)^{1/4}$$

$$\zeta \equiv \frac{s}{s'} = \left(\frac{T}{T'} \right)^3 \left. \frac{h_{\text{eff}}(T)}{h'_{\text{eff}}(T')} \right|_{T=10 \text{ GeV}}$$



SIMP Boltzmann equation

- General Boltzmann eqn. can be recast as

$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle \sigma v^3 \rangle_{4 \rightarrow 2} \left(n_\chi^4 - n_\chi^2 n_\chi^{\text{eq} \, 2} \right)$$

where in the non-rel.-limit

$$\langle \sigma v^3 \rangle_{4 \rightarrow 2} \simeq \frac{\int d^3v_1 d^3v_2 d^3v_3 d^3v_4 (\sigma v^3) \delta^3(\vec{v}_1 + \vec{v}_2 + \vec{v}_3 + \vec{v}_4) e^{-\frac{m_\chi}{2T'}(v_1^2 + v_2^2 + v_3^2 + v_4^2)}}{\int d^3v_1 d^3v_2 d^3v_3 d^3v_4 \delta^3(\vec{v}_1 + \vec{v}_2 + \vec{v}_3 + \vec{v}_4) e^{-\frac{m_\chi}{2T'}(v_1^2 + v_2^2 + v_3^2 + v_4^2)}}$$

with all particle physics contained in

$$(\sigma v^3) = \frac{\sqrt{3}}{6144\pi m_\chi^4} \int \frac{d\Omega}{4\pi} |\mathcal{M}|^2$$

- result

$$\frac{1201}{245760\sqrt{3}\pi\Lambda^8} \frac{T'^2}{m_\chi^2}$$

- more versatile treatment, including relativistic effects [1906.07659]

$$\Gamma_{4 \rightarrow 2} = \Gamma_{2 \rightarrow 4} e^{2\mu/T}$$

