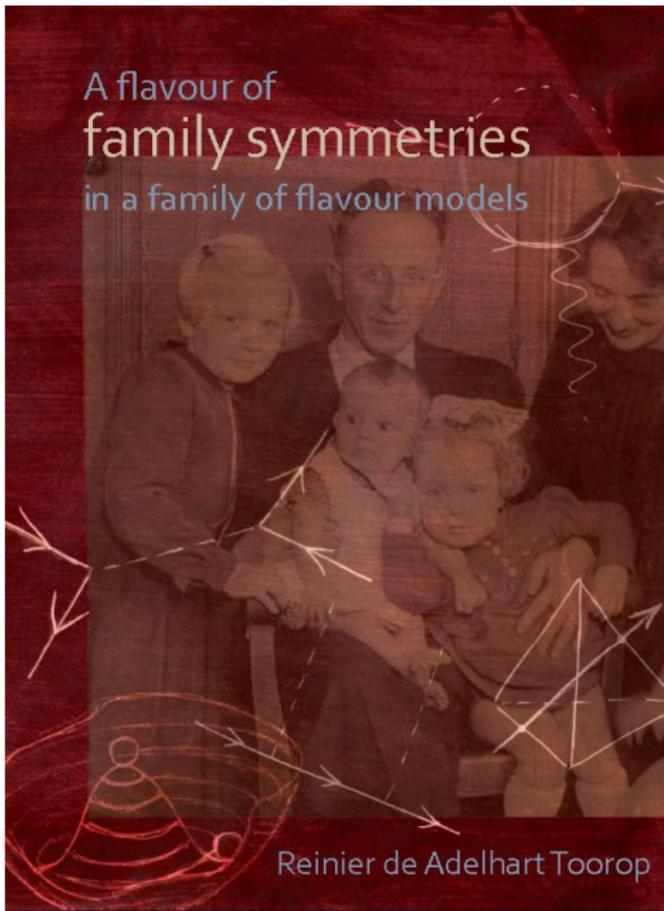


A flavour of  
family symmetries  
in a family of flavour models

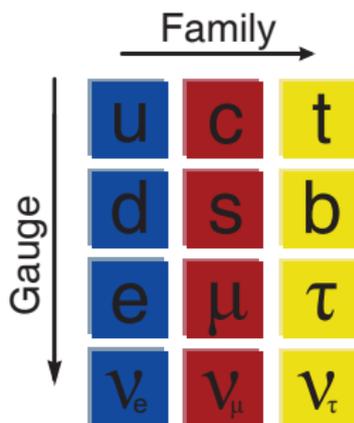


Reinier de Adelhart Toorop

# Outline

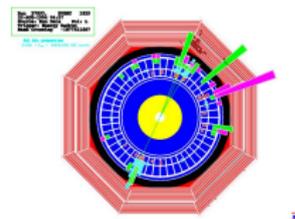
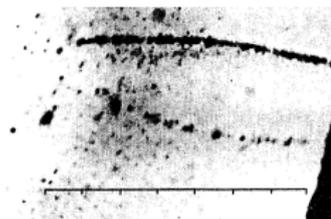
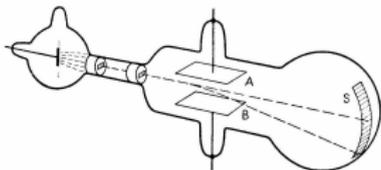
- 1 Motivation of family symmetries
- 2 A 'vanilla' family symmetry model
  - The Altarelli-Feruglio  $A_4$  model
- 3 Non-zero  $\theta_{13}$ 
  - Mixing patterns of finite modular groups
  - Mixing patterns with large NLO corrections
  - Flavour symmetries at the Electroweak scale
- 4 conclusions

- Central theme of my thesis: family symmetries.
- Related to the existence of three families
- Motivation is threefold.
  - Structure in similarity
  - Structure in difference 1: masses
  - Structure in difference 2: mixing



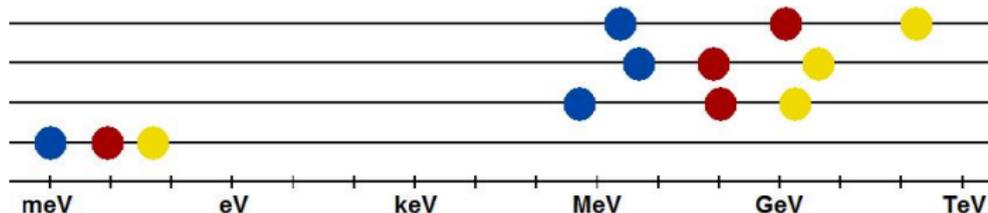
# Structure in similarity

- Charged leptons of all three generations
  - Same charges
  - Same spin
- Complete generation replication quite special
  - Although partly explained by anomalies
- In the Standard Model this is considered an experimental fact...
  - ...but not explained by a deeper reason.



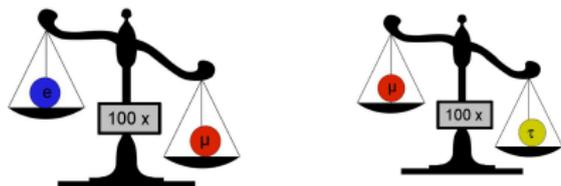
# Structure in difference 1: masses

- Particles of the three generations differ in their masses.
- The masses are highly hierarchical.
- On a logarithmic scale, there might be some structure.



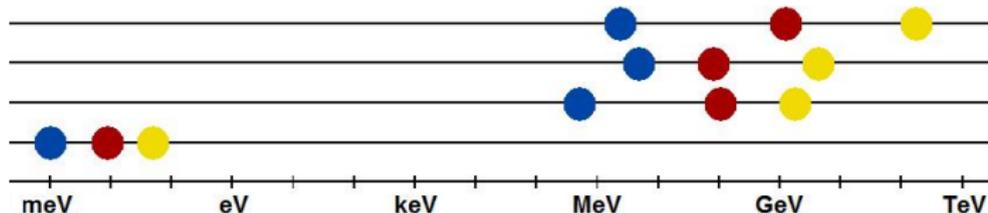
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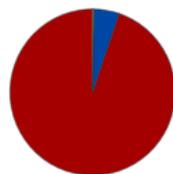
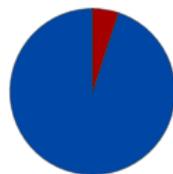
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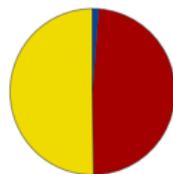
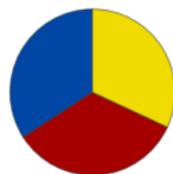
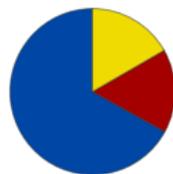
$$|(V_{CKM})_{ij}| = \begin{pmatrix} 0.97 & 0.23 & 0.0039 \\ 0.23 & 1.0 & 0.041 \\ 0.0081 & 0.038 & 1? \end{pmatrix}$$



## Structure in difference 2: mixing

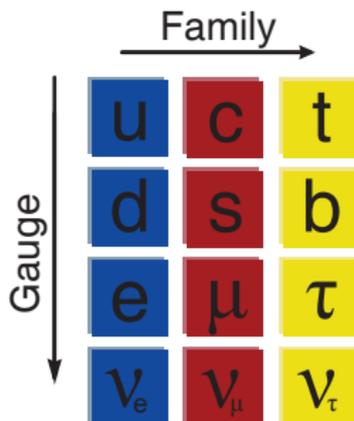
- Mass and weak interaction eigenstates do not coincide.
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  - Leptons: strong PMNS-mixing.

$$|(U_{PMNS})_{ij}| = \begin{pmatrix} 0.81 & 0.56 & <0.22 \\ 0.39 & 0.59 & 0.68 \\ 0.38 & 0.55 & 0.70 \end{pmatrix}$$



# Coincidence or symmetry?

- The observed patterns might be purely coincidental.
  - 22 of 28 free parameters in SM relate to fermion mass sector.
  - Their values may just be like this.
- More interesting: the patterns follow from a symmetry principle.



# Flavour Symmetries

These structures might be explained by flavour/family symmetries

- We charge the families under a symmetry group.
- To make the Lagrangian invariant, we need to add Higgs-like fields 'flavons'.
- Structure in flavon-VEVs leads to structure in the fermion masses.
- Non-renormalizable operators often occur
  - Terms suppressed by  $\text{VEV}/\Lambda$ .

A very good introduction: [G. Altarelli, Models of neutrino masses and mixings; hep-ph/0611117](#)

	Family →		
Gauge ↓	u	c	t
	d	s	b
	e	$\mu$	$\tau$
	$\nu_e$	$\nu_\mu$	$\nu_\tau$



# The Altarelli-Feruglio model

- We consider a model by Altarelli and Feruglio

G. Altarelli and F. Feruglio, Nucl. Phys. B741 (2006) 215-235. [[hep-ph/0512103](#)]

- It discusses only the lepton sector.
  - It explains charged lepton and neutrino masses.
- It reproduces tribimaximal mixing.



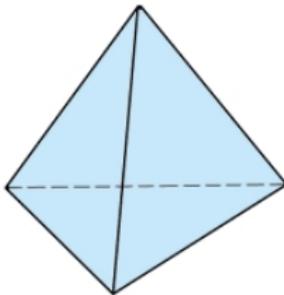
# The group $A_4$ and the A-F model

- The flavour symmetry group is  $A_4$
- The symmetry group of the tetrahedron.
  - “toprotations”  $120^\circ$  and  $240^\circ$ .
  - “axisrotations”  $180^\circ$ .

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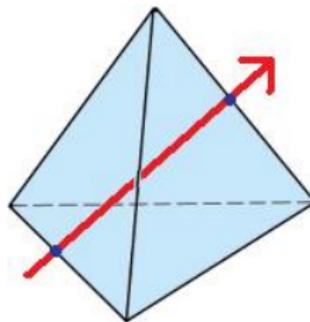
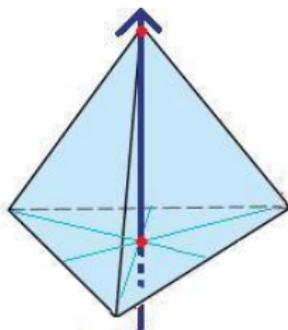
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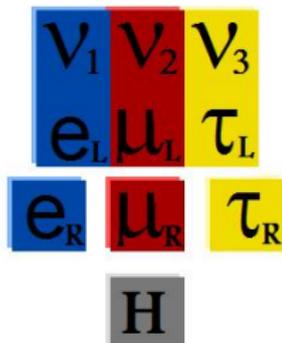
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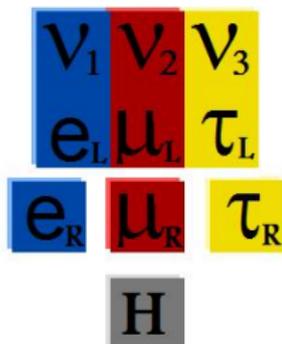
# Matter in the A-F model

- The group  $A_4$  has
  - Three 1-d irreps: 1, 1' and 1''.
  - One 3-d irrep
- Matter assignment:
  - Lepton doublets in 3
    - lefthanded electron
    - normal neutrino
  - Lepton singlets are in the three different 1-d reps.
    - righthanded electron
  - The Higgs transforms trivially under  $A_4$ .
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# Flavons in the A-F model

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- One couples to the neutrinos.
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  - But leaves a  $Z_2$  symmetry.
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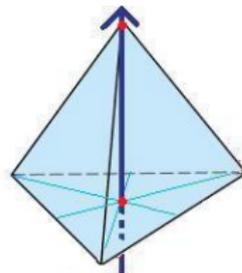
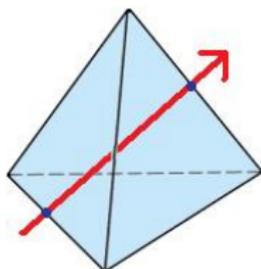
$$w_e = \frac{y_e}{\Lambda} \bar{e}_R (\varphi_T l_L)_1 h + \frac{y_\mu}{\Lambda} \bar{\mu}_R (\varphi_T l_L)_{1'} h + \frac{y_\tau}{\Lambda} \bar{\tau}_R (\varphi_T l_L)_{1''} h$$

$$w_\nu = \frac{x_a}{\Lambda} (\tilde{h} l) (\tilde{h} l) + \frac{x_a}{\Lambda^2} \varphi_S (\tilde{h} l) (\tilde{h} l)$$

$$\langle H \rangle = v, \quad \langle \varphi_T \rangle = (u, 0, 0) \Lambda, \quad \langle \varphi_S \rangle = (u', u', u') \Lambda$$

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# Tri-bimaximal mixing in the A-F model

- The superpotential
- Together with the vev structures
- Gives the mass matrices
- That is exactly diagonalized by the tribimaximal matrix

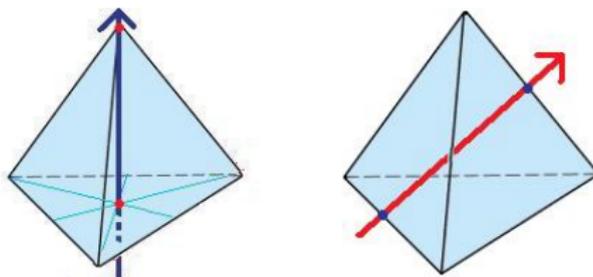
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$$M_l = \text{diag}(y_e, y_\mu, y_\tau) v u$$
$$M_\nu = \begin{pmatrix} a + 2b & -b & -b \\ -b & 2b & a - b \\ -b & a - b & 2b \end{pmatrix} v^2$$

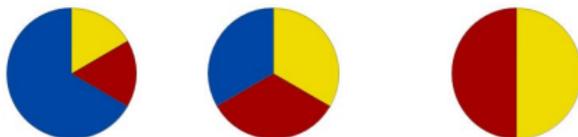
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$$U_{\text{TBM}}^T M_\nu U_{\text{TBM}} = \begin{pmatrix} m_1 = a + b & 0 & 0 \\ 0 & m_2 = a & 0 \\ 0 & 0 & m_3 = -a + b \end{pmatrix}$$

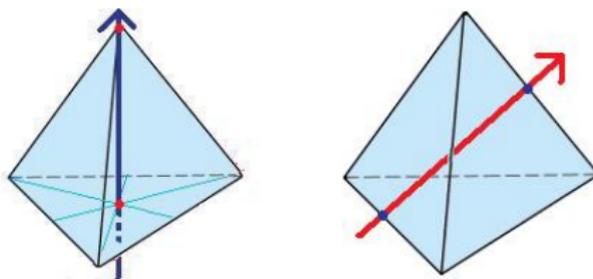
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- The Altarelli-Feruglio model can reproduce tribimaximal mixing.
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- Basically, the  $Z_3$  and the  $Z_2$  give the *tri* and the *bi* of tribimaximal mixing.



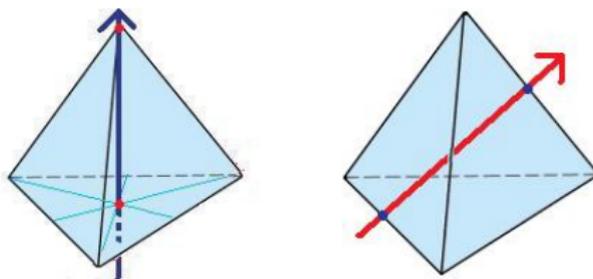
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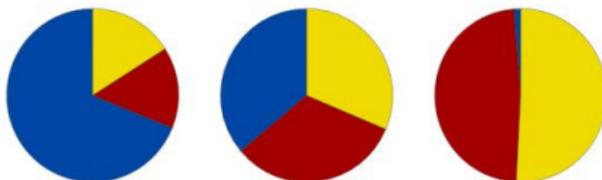
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# Vanishing reactor mixing angle $\theta_{13} = 0$

- The Altarelli-Feruglio model reproduces tribimaximal mixing.
- It thus gives  $\theta_{13} = 0$ .
  - Subleading corrections can give tiny corrections.
- Allowed at  $\sim 2\sigma$  at the time of the model.





# Non-zero reactor mixing angle $\theta_{13} \neq 0$

- Recent results of T2K, Minos, Double Chooz and (last week) Daya Bay.
- $\theta_{13} \neq 0$  at the 3-5 sigma level.
- But 'vanilla' flavour symmetry models predict it to be zero.

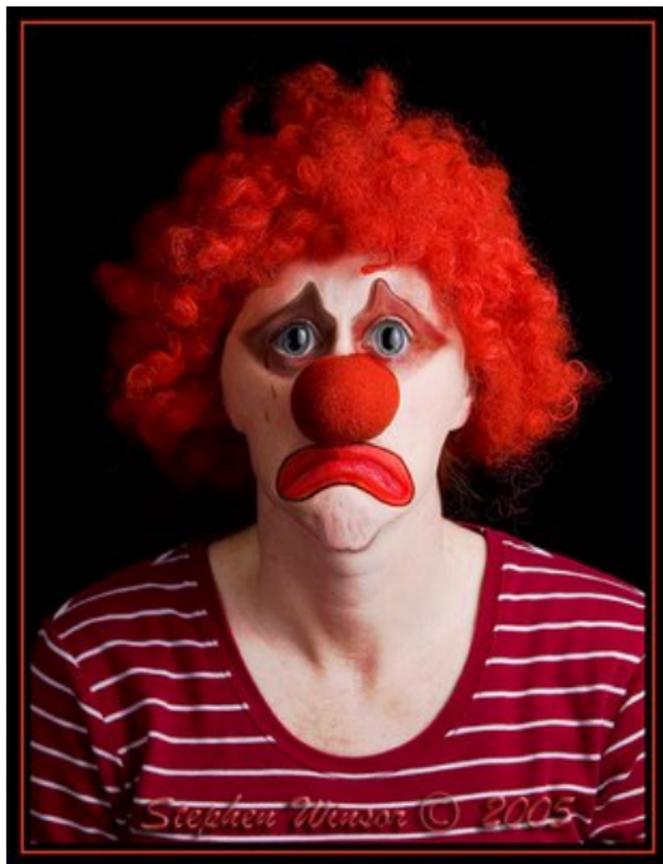


# What to do?

- Directions in theory space.
  - 1 Give up on flavour symmetries.
  - 2 Work out new mixing patterns apart from TBM mixing.
  - 3 Build models with (T)BM and large corrections.
  - 4 Build models that do not predict mixing angles.
    - Keep the other good properties.
    - At the electroweak scale.



1. Give up on flavour symmetries.

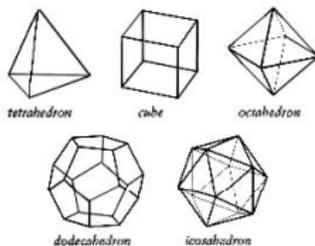


## 2. Find new mixing patterns.

# Modular Subgroups

Based on R. de Adelhart Toorop, F. Feruglio and C. Hagendorf *Phys.Lett. B703* (2011) 447 and *Nucl.Phys. B858* (2012) 437

- In the Altarelli-Feruglio model, the group  $A_4$  reproduced tribimaximal mixing
- Many other models in the literature use the groups  $S_4$  and  $A_5$
- These groups have in common
  - That they are symmetry groups of Platonic solids.
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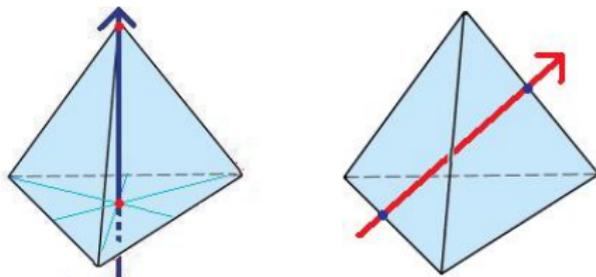
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$$S^2 = 1, \quad (S.T)^3 = 1, \quad \begin{cases} T^3 = 1, & \text{for } A_4 \\ T^4 = 1, & \text{for } S_4 \\ T^5 = 1, & \text{for } A_5 \end{cases}$$

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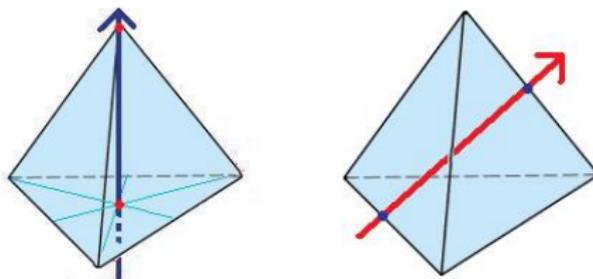
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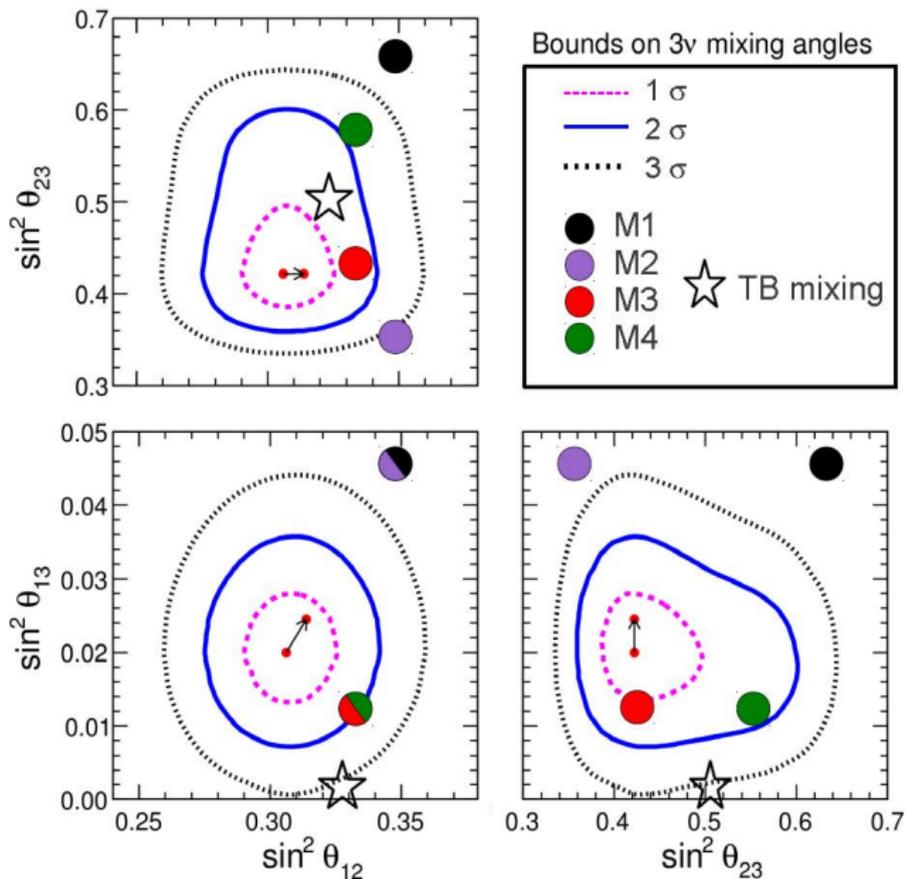
- The second criterion easily generalizes
- If we demand three-dimensional irreps
- Three new candidate groups
  - $PSL(2, 7)$  with  $T^7 = 1$  (and  $(ST^{-1}ST)^4 = 1$ )
  - $\Delta(96)$  with  $T^8 = 1$  (and  $(ST^{-1}ST)^3 = 1$ )
  - $\Delta(384)$  with  $T^{16} = 1$  (and  $(ST^{-1}ST)^3 = 1$ )



# Modular Subgroups

- We investigate lepton mixing patterns from these groups.
- Same assumptions as in Altarelli-Feruglio model.
  - Residual symmetries in charged lepton and neutrino sectors
- Interesting mixing patterns from  $\Delta(96)$  and  $\Delta(384)$



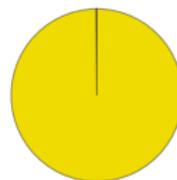
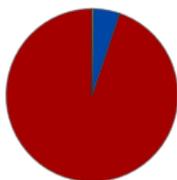


### 3. Mixing patterns with large corrections

# Large NLO corrections

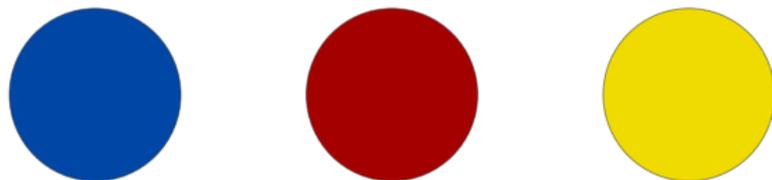
Based on R. de Adelhart Toorop, F. Bazzocchi and L. Merlo JHEP 1008 (2010) 001 (and many other papers)

- look again at quark mixing
- Only very moderate mixing.
- Even Cabibbo angle remarkably small.



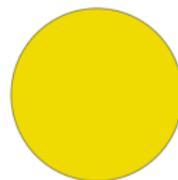
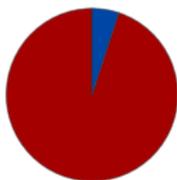
# Large NLO corrections

- Idea: in first approximation no mixing
- The reproduce the Cabibbo angle by NLO effects
- NLO terms have an extra flavon
  - And are thus (even more) non-renormalizable.
  - Effect suppressed by (extra) factor of  $\text{VEV}/\Lambda \sim 0.2$ .
- The two other (tiny) mixing follow at even higher order.



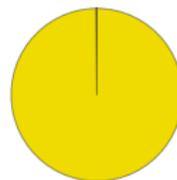
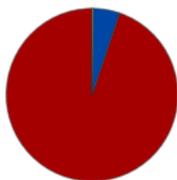
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# Quark-lepton complementarity



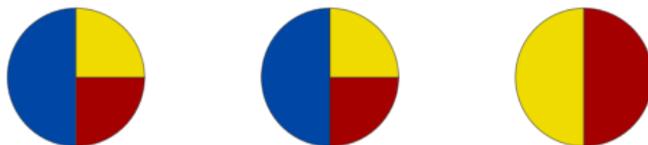
- Philosophy of the previous slide:
  - Quark sector
  - moderate corrections from LO to NLO.
- This might also be the case in the neutrino sector.
  - At LO: reproduce tribimaximal mixing
  - Or the similar bimaximal mixing
  - Large corrections then give  $\theta_{13} \neq 0$ .
  - In accordance with the data

# Quark-lepton complementarity

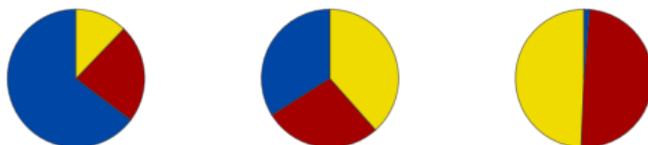
- Neutrino data



- LO approximation



- NLO approximation



# 4. Flavour symmetries at the Electroweak scale

# Flavour symmetries at the Electroweak scale

Based on R. de Adelhart Toorop, F. Bazzocchi, L. Merlo and A. Paris JHEP 1103 (2011) 035 and 040

- Models discussed so far: very high energy scale.
- Alternatively: at the Electroweak scale.
  - Models very predictive.
  - But not in mixing angles.
  - Non-zero  $\theta_{13}$  no problem.



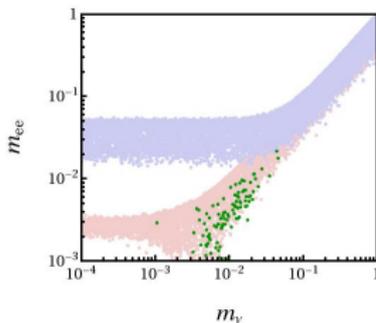
# Problems of models with flavons

- Models with flavons can become quite baroque.
  - Model of the previous section: 10 new flavon fields.
- New physics at a high (GUT) scale.
  - Only indirect signals - Theory hard to test.
- Flavon alignment non-trivial
  - Theoretical techniques need susy or x-dims.



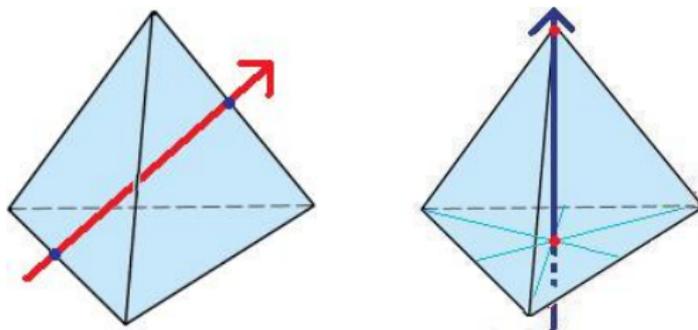
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  - Only indirect signals - Theory hard to test.
- Flavon alignment non-trivial
  - Theoretical techniques need susy or x-dims.



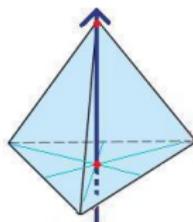
# Problems of models with flavons

- Models with flavons can become quite baroque.
  - Model of the previous section: 10 new flavon fields.
- New physics at a high (GUT) scale.
  - Only indirect signals - Theory hard to test.
- Flavon alignment non-trivial
  - Theoretical techniques need susy or x-dims.



# Flavo-Higgs

- Alternative: assume only one direction in flavon space.
- The SM Higgs can play the role of the flavons.
  - Much simpler models.
  - Flavour scale = Higgs scale  $\rightarrow$  testable at LHC.



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# The $A_4$ -Higgs model

- Assume three copies of the SM Higgs field.



# The $A_4$ -Higgs model

- Assume three copies of the SM Higgs field.
- In a triplet of the flavour group  $A_4$ .

$$\Phi_1 \rightarrow \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_1^1 \\ v_1 e^{i\omega_1} + \phi_1^0 \end{pmatrix}, \quad \Phi_2 \rightarrow \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_2^1 \\ v_2 e^{i\omega_2} + \phi_2^0 \end{pmatrix},$$

$$\Phi_3 \rightarrow \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_3^1 \\ v_3 e^{i\omega_3} + \phi_3^0 \end{pmatrix}.$$

- The vector of vevs  $(v_1 e^{i\omega_1}, v_2 e^{i\omega_2}, v_3 e^{i\omega_3})$  serves as the flavon.



# The $A_4$ -invariant Higgs potential

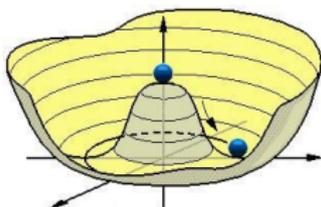
- The Higgs potential

$$\begin{aligned}
 V = & \mu^2(\Phi_1^\dagger\Phi_1 + \Phi_2^\dagger\Phi_2 + \Phi_3^\dagger\Phi_3) + \lambda_1(\Phi_1^\dagger\Phi_1 + \Phi_2^\dagger\Phi_2 + \Phi_3^\dagger\Phi_3)^2 \\
 & + \lambda_3(\Phi_1^\dagger\Phi_1\Phi_2^\dagger\Phi_2 + \Phi_1^\dagger\Phi_1\Phi_3^\dagger\Phi_3 + \Phi_2^\dagger\Phi_2\Phi_3^\dagger\Phi_3) \\
 & + \lambda_4(\Phi_1^\dagger\Phi_2\Phi_2^\dagger\Phi_1 + \Phi_1^\dagger\Phi_3\Phi_3^\dagger\Phi_1 + \Phi_2^\dagger\Phi_3\Phi_3^\dagger\Phi_2) \\
 & + \frac{\lambda_5}{2} \left[ e^{i\epsilon} [(\Phi_1^\dagger\Phi_2)^2 + (\Phi_2^\dagger\Phi_3)^2 + (\Phi_3^\dagger\Phi_1)^2] + \right. \\
 & \left. e^{-i\epsilon} [(\Phi_2^\dagger\Phi_1)^2 + (\Phi_3^\dagger\Phi_2)^2 + (\Phi_1^\dagger\Phi_3)^2] \right],
 \end{aligned}$$

- allows a number of minimum configurations.

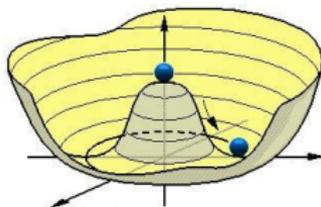
# Minima of the Higgs potential

- The Higgs potential allows a number of minimum configurations.
  - If all vevs are real: CP conserving
    - $(v, v, v)$
    - $(v, 0, 0)$
  - If some vevs are complex: CP violating
    - $(ve^{i\omega}, rv, 0)$
    - $(ve^{i\omega}, ve^{-i\omega}, rv)$



# Constraining flavo-Higgs models

- Not all parameter choices give realistic models.
- We constrain the models by
  - Positive  $m^2$  for all 5 neutral and 2 charged Higgses
  - Unitarity constraints
  - Z- and W-decay constraints
  - Oblique parameters
  - For models with explicit fermion content
    - Rare decays
    - Meson oscillations

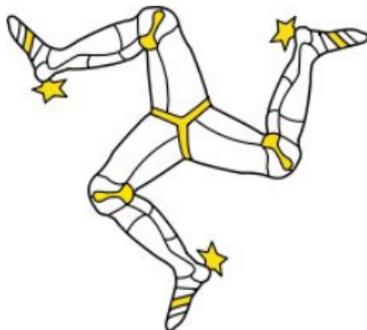


# The alignment $(v, v, v)$

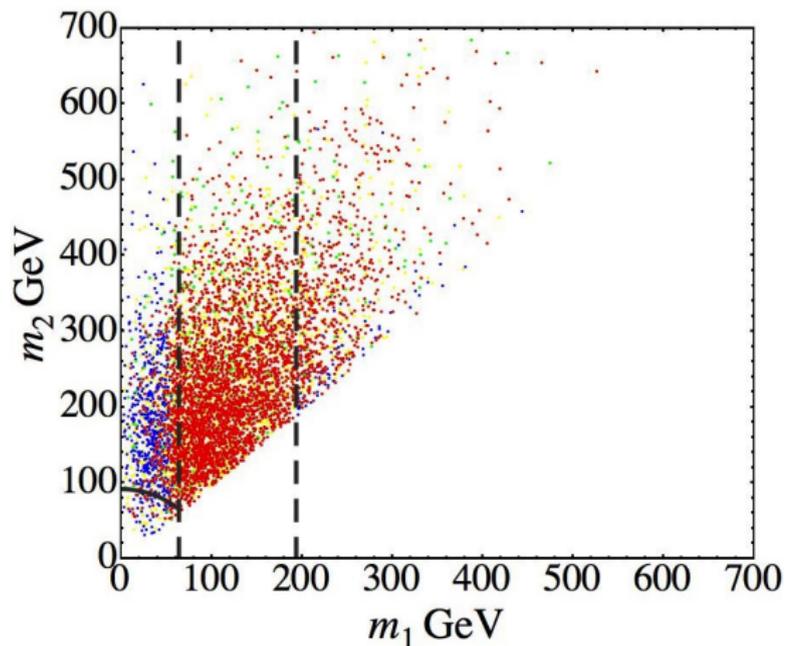
- The CP conserving alignment  $(v, v, v)$

E. Ma and G. Rajasekaran, Phys. Rev. D **64**, 113012 (2001)

- Residual  $Z_3$  symmetry
- Higgs spectrum
  - SM Higgs boson
  - Two degenerate scalars
  - Two degenerate pseudoscalars



# Fermion independent constraints



All masses  $\geq 0$ : yellow points. Unitarity OK: blue points.

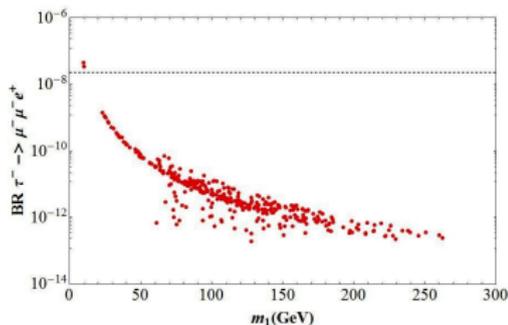
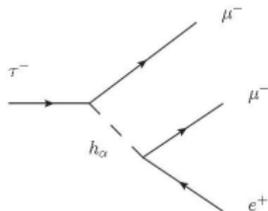
Z decay OK: green points. Oblique parameters OK: red points

## Tests

- $M^2 > 0$
- Unitarity
- Z and W
- Oblique

# Fermion dependent constraints

- In the Ma-Rajasekaran setup, many rare decays are indeed forbidden.
  - No  $\mu^- \rightarrow e^- e^- e^+$  and  $\mu^- \rightarrow e^- \gamma$
- Allowed decays are below experimental bounds.
  - $\tau^- \rightarrow \mu^- \mu^- e^+$



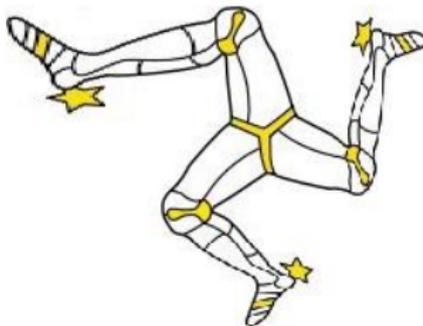
# The alignment $(ve^{i\omega}, ve^{-i\omega}, rv)$

- The CP violating alignment  $(ve^{i\omega}, ve^{-i\omega}, rv)$  (or permutations)

Lepton sector: S. Morisi and E. Peinado, *Phys. Rev. D* **80**, 113011 (2009)

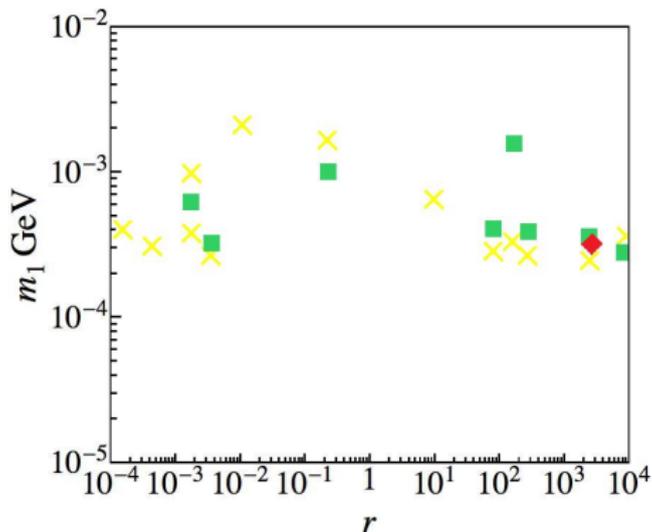
Quark sector: L. Lavoura and H. Kuhbock, *Eur. Phys. J. C* **55**, 303 (2008)

- No residual symmetry
- Five Higgses are mixes of scalars and pseudoscalars.
- Without softly breaking the  $A_4$ -invariant potential, not possible to have all  $m_h^2 \geq 0$



# Fermion independent constraints (with soft $A_4$ -breaking terms)

- Scan over 100.000 points

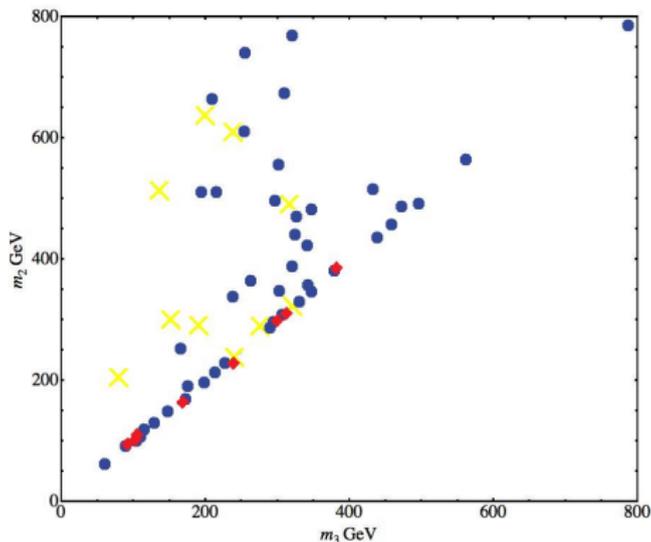


All masses  $\geq 0$ : yellow points. Unitarity OK: blue points.

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# Fermion independent constraints (with soft $A_4$ -breaking terms)

- Scan over few 1000 points;  $r$  fixed

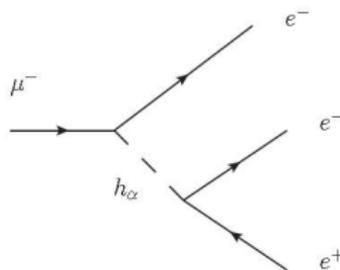


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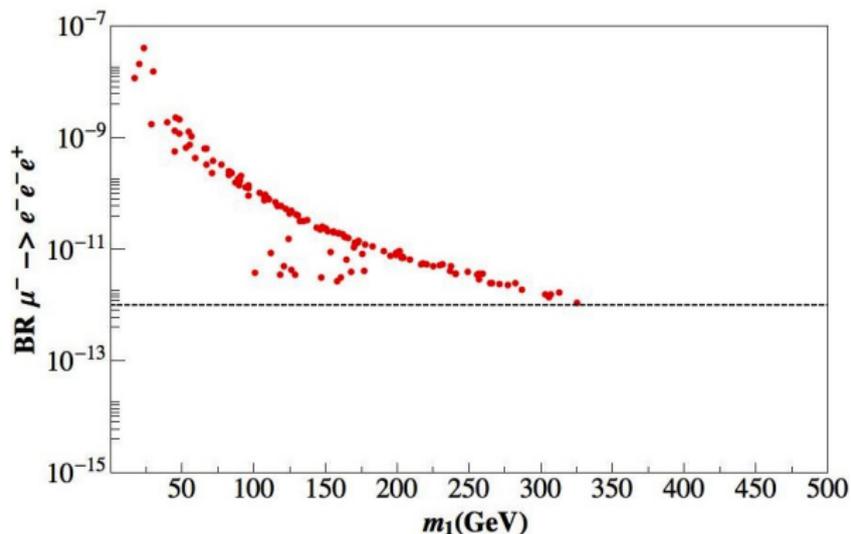
# Rare fermion decays

- Rare fermion decays can be very constraining
  - $\mu^- \rightarrow e^- e^- e^+$  in Morisi and Peinaldo's model.
  - $\mu^- \rightarrow e^- \gamma$  less constraining



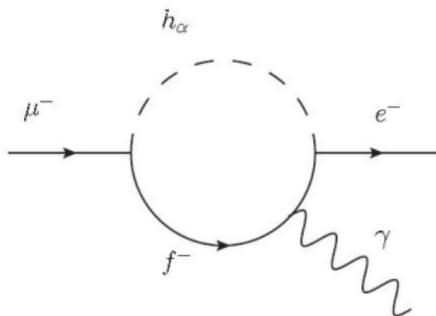
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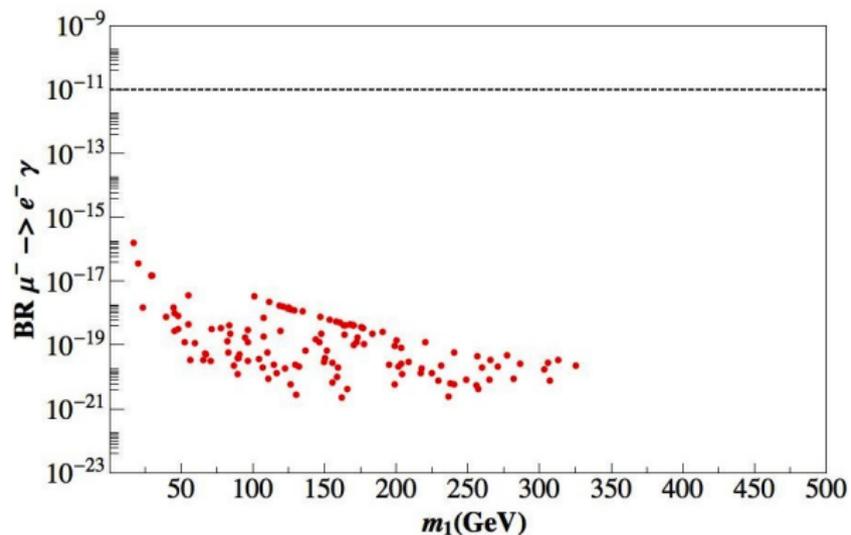
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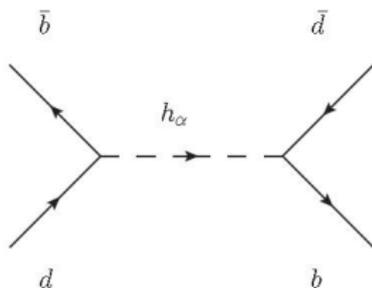
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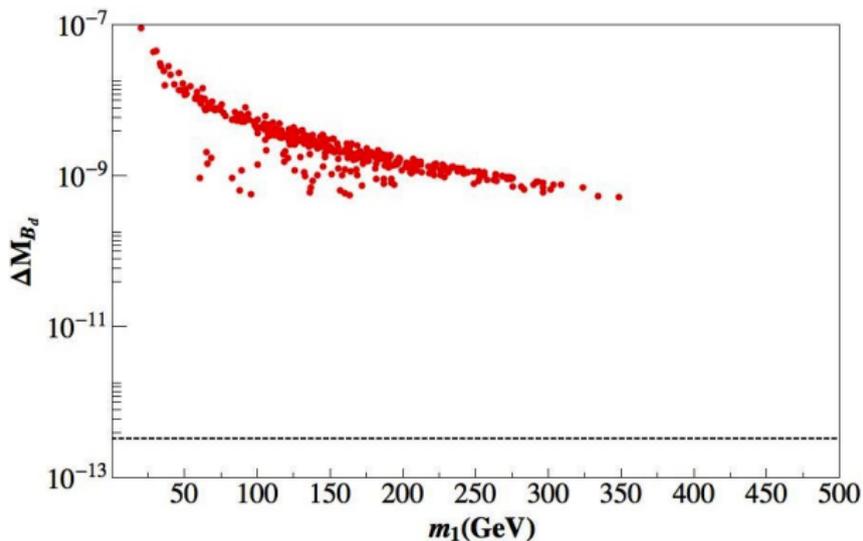
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- In models with quarks, meson oscillations give very strong bounds.
  - $\Delta_{M_{B_d}}$  in  $B_d \leftrightarrow B_d^*$  oscillations in Lavoura and Kuhbock's model.



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# Conclusions

- Evidence that  $\theta_{13} > 0$  ruled out 'vanilla' family symmetries.
- Other flavours are still interesting.
  - New mixing patterns beyond tribimaximal.
  - Mixing patterns with large NLO corrections.
  - Flavour symmetries at the EW scale.
- Thanks for your attention!

	Family →		
Gauge ↓	u	c	t
	d	s	b
	e	$\mu$	$\tau$
	$\nu_e$	$\nu_\mu$	$\nu_\tau$

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