

GRAVITINO DARK MATTER

Wilfried Buchmüller

DESY, Hamburg

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Why Gravitino Dark Matter?

Supergravity predicts the **gravitino**, analog of W and Z bosons in electroweak theory; may be LSP, natural DM candidate:

- $m_{3/2} < 1\text{keV}$, **hot DM**, (Pagels, Primack '81)
- $1\text{keV} \lesssim m_{3/2} \lesssim 15\text{keV}$, **warm DM**, (Gorbunov, Khmelnitsky, Rubakov '08)
- $100\text{keV} \lesssim m_{3/2} \lesssim 10\text{MeV}$, **cold DM**, gauge mediation and thermal leptogenesis (Fuji, Ibe, Yanagida '03); recently proven to be correct by F-theory (Heckman, Tavanfar, Vafa '08)
- $10\text{GeV} \lesssim m_{3/2} \lesssim 1\text{TeV}$, **cold DM**, gaugino/gravity mediation and thermal leptogenesis (Bolz, WB, Plümacher '98)

Baryogenesis, (gravitino) DM and primordial nucleosynthesis (BBN) strongly correlated in cosmological history.

Gravitino Problem

Thermally produced gravitino number density grows with **reheating temperature** after inflation (Khlopov, Linde '83; Ellis, Kim, Nanopoulos '84; ...),

$$\frac{n_{3/2}}{n_\gamma} \propto \frac{\alpha_3}{M_p^2} T_R.$$

For unstable gravitinos, nucleosynthesis implies stringent upper bound on reheating temperature T_R (Kawasaki, Kohri, Moroi '05; ...),

$$T_R < \mathcal{O}(1) \times 10^5 \text{ GeV},$$

hence standard mSUGRA with neutralino LSP incompatible with baryogenesis via **thermal leptogenesis** where $T_R \sim 10^{10}$ GeV !!

Possible way out: **Gravitino LSP**, explains dark matter!

Gravitino Virtue

Can one understand the amount of dark matter, $\Omega_{DM} \simeq 0.23$, with $\Omega_{DM} = \rho_{DM}/\rho_c$, if gravitinos are dominant component, i.e. $\Omega_{DM} \simeq \Omega_{3/2}$?

Production mechanisms: (i) WIMP decays, i.e., ‘Super-WIMPs’ (Covi, Kim, Roszkowski ’99; Feng, Rajaraman, Takayama ’03),

$$\Omega_{3/2} = \frac{m_{3/2}}{m_{\text{NLSP}}} \Omega_{\text{NLSP}} ,$$

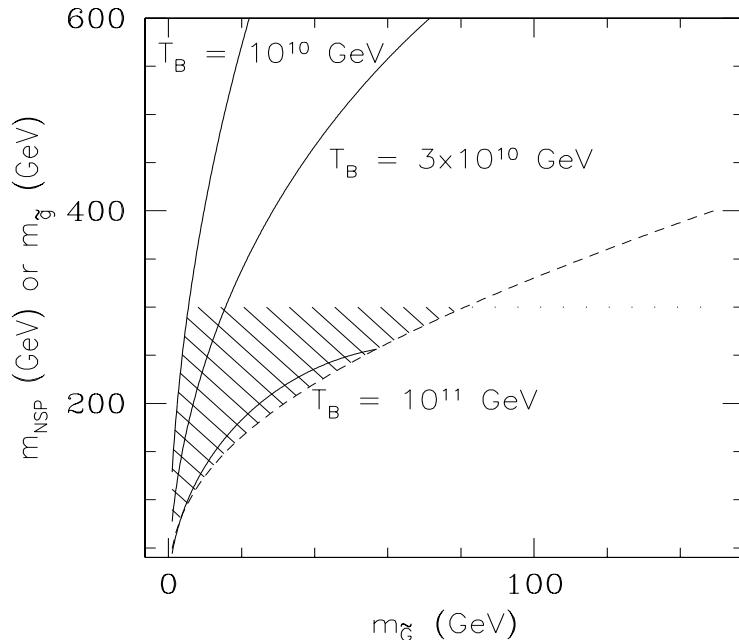
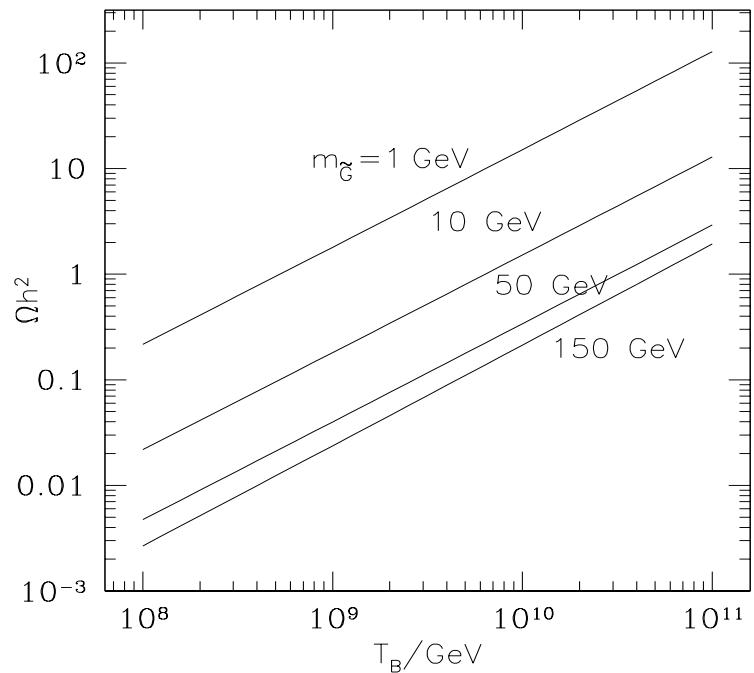
independent of initial temperature T_R (!), but inconsistent with BBN constraints; (ii) Thermal production, from $2 \rightarrow 2$ QCD processes,

$$\Omega_{3/2} h^2 \simeq 0.5 \left(\frac{T_R}{10^{10} \text{GeV}} \right) \left(\frac{100 \text{GeV}}{m_{3/2}} \right) \left(\frac{m_{\tilde{g}}(\mu)}{1 \text{TeV}} \right) .$$

→ $\Omega_{DM} h^2$ for typical parameters of supergravity and leptogenesis!

Leptogenesis, GDM and BBN

(Bolz, WB, Plümacher '98)

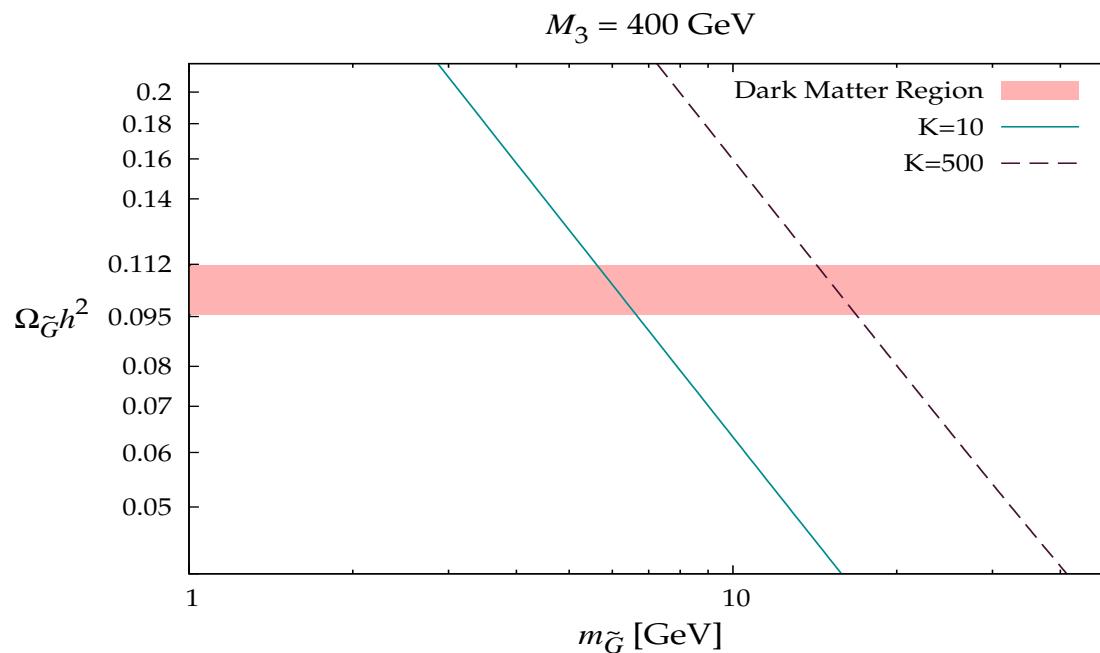


Left: Gravitino abundance as function of reheating temperature. *Right:* Upper bound on gluino mass, lower bound on higgsino NLSP; shaded area: BBN ok. **Note:** gaugino mass unification not possible. Improved BBN constraints $\rightarrow \tilde{\tau}$ NLSP ... $\rightarrow \dots$ Pospelov '06 ... review Steffen '08

Reheating: initial RH-neutrino dominance

(...Asaka et al '99; Hahn-Woernle, Plümacher '08; Erbe '09)

Reheating process from inflaton decay: $\phi \rightarrow N_1 N_1 \rightarrow (lH)(lH) \rightarrow \dots$; combined system of Boltzmann eqs connects LG and gravitino production



parameters: $M_1 = 10^9 \text{ GeV} \sim T_R$, $m_{\tilde{g}} = 1 \text{ TeV}$; for $K = 10$ (strong washout): $m_{3/2} \simeq 6 \text{ GeV}$ (cf. thermal LG: $\Omega h^2 \sim 1$).

Decaying GDM

(WB, Covi, Hamaguchi, Ibarra, Yanagida '07)

BBN, leptogenesis and gravitino dark matter are all consistent in case of a small ‘R-parity’ breaking, which leads to processes $\tilde{\tau}_R \rightarrow \tau \nu_\mu, \mu \nu_\tau$, $\tilde{\tau}_L \rightarrow b^c t$, ... and also $\psi_{3/2} \rightarrow \gamma \nu$. Small R-parity breaking can occur together with B-L breaking,

$$\lambda \sim h^{(e,d)} \Theta \lesssim 10^{-7}, \quad \Theta \sim \frac{v_{B-L}^2}{M_P^2}.$$

The NLSP lifetime becomes sufficiently short (decay before BBN),

$$c\tau_{\tilde{\tau}}^{lep} \sim 30 \text{ cm} \left(\frac{m_{\tilde{\tau}}}{200 \text{ GeV}} \right)^{-1} \left(\frac{\lambda}{10^{-7}} \right)^{-2}.$$

BBN, thermal leptogenesis and gravitino dark matter are consistent for $10^{-14} < \lambda, \lambda' < 10^{-7}$ (B, L washout) and $m_{3/2} \gtrsim 5 \text{ GeV}$.

At LHC one should see characteristic signal with strongly ionising macroscopic charged tracks, followed by a muon track or a jet and missing energy, corresponding to $\tilde{\tau} \rightarrow \mu \nu_\tau$ or $\tilde{\tau} \rightarrow \tau \nu_\mu$.

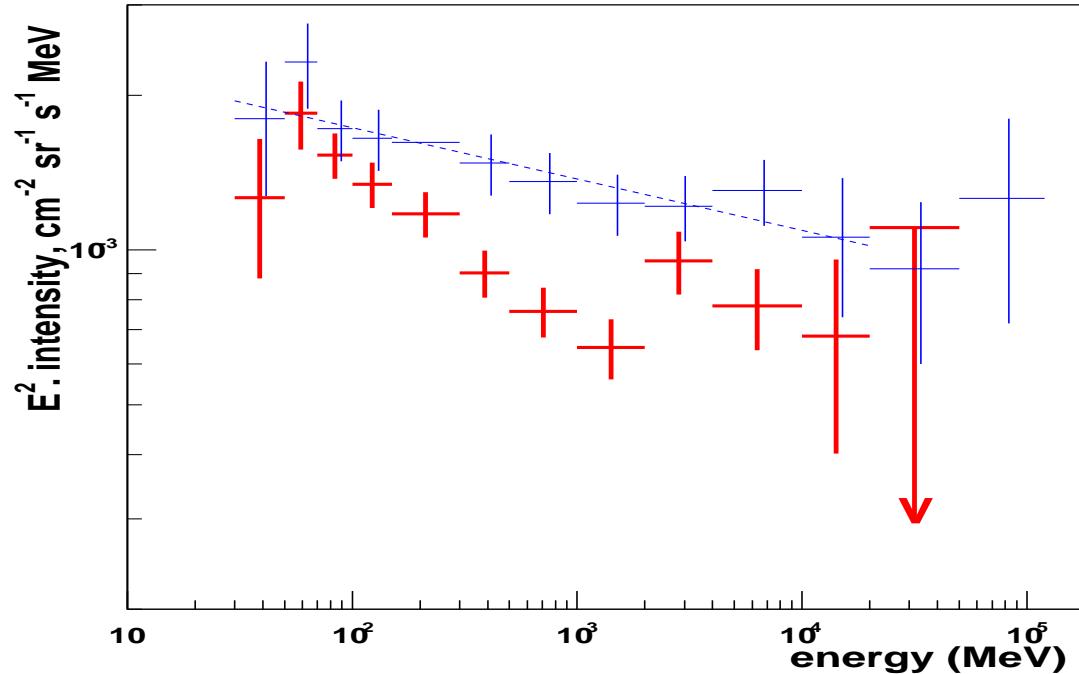
The gravitino decay $\psi_{3/2} \rightarrow \gamma \nu$ is suppressed both by the Planck mass and the small R-parity breaking couplings, so the lifetime is much longer than the age of the universe (Takayama, Yamaguchi '00),

$$\tau_{3/2} \sim 10^{26} \text{ s} \left(\frac{\lambda}{10^{-7}} \right)^{-2} \left(\frac{m_{3/2}}{10 \text{ GeV}} \right)^{-3} ;$$

(Note that this **lifetime** became **very popular** after PAMELA). What are the cosmic ray signatures? Gamma-ray flux of the order of EGRET excess !!

Several other mechanisms to generate small R-parity breaking have been proposed (Mohapatra et al '08; Endo, Shindou '09, ...)

LAUNCH07, March 2007, MPK Heidelberg:
Extragalactic diffuse gamma-ray flux obtained from EGRET data (1998)



analysis of Strong, Moskalenko and Reimer, [astro-ph/0406254](#) (2004), [astro-ph/0506359](#) (2005); subtraction of galactic component difficult [astro-ph/0609768](#); extragalactic gravitino signal consistent with data for $m_{3/2} \sim 10$ GeV; halo component may partly be hidden in anisotropic galactic gamma-ray flux → wait for GLAST !!

Superparticle Mass Window

(WB, Endo, Shindou '08)

What are the constraints from leptogenesis and GDM on superparticle masses for unstable gravitinos, i.e. without BBN? GDM: upper bound on gluino mass for given reheating temperature; low energy observables: lower bound on NLSP.

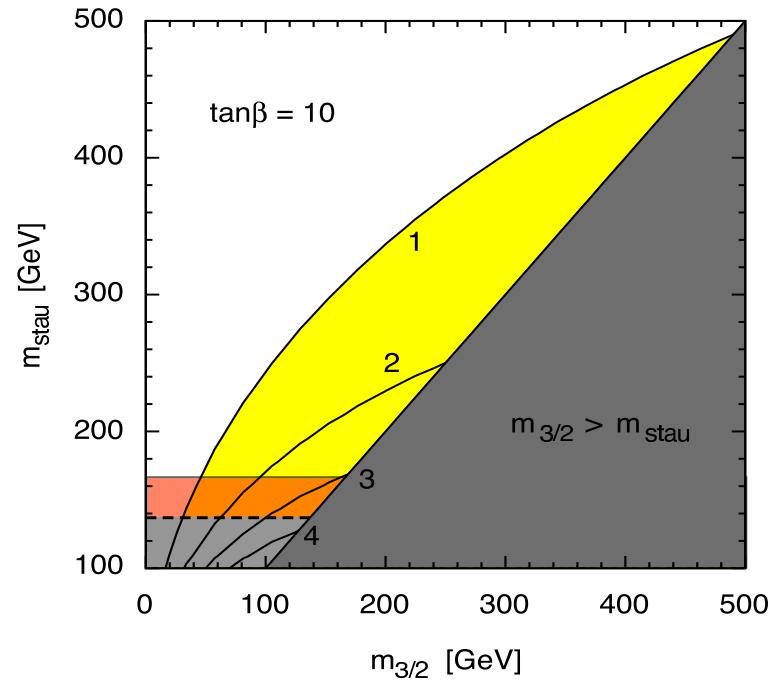
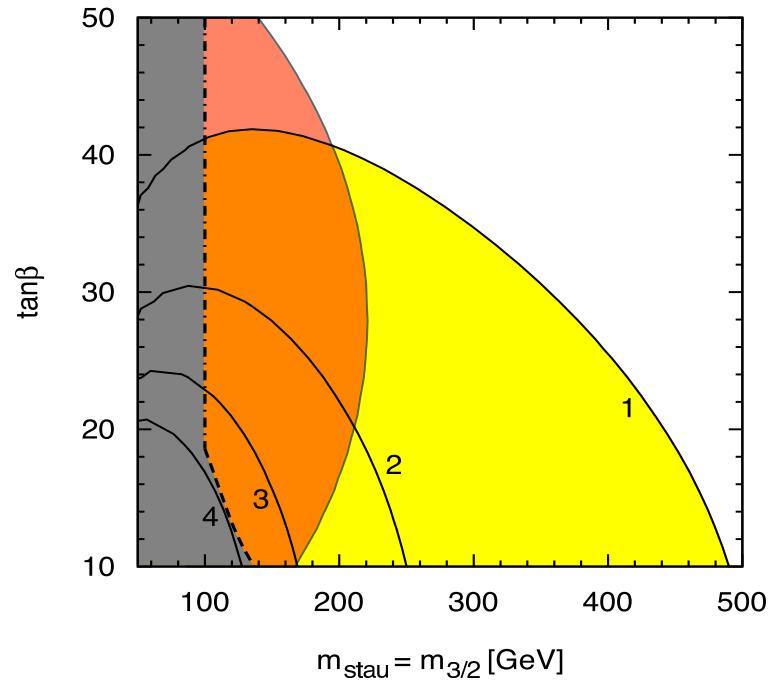
Connection is model dependent; assume gaugino mass unification ($m_{\text{gluino}} \simeq 6m_{\text{bino}}$). Two typical examples (different ratios $m_{\text{NLSP}}/m_{\text{gluino}}$),

- (A) $\tilde{\chi}$ NLSP : $m_0 = m_{1/2}$, $a_0 = 0$, $\tan \beta$;
- (B) $\tilde{\tau}$ NLSP : $m_0 = 0$, $m_{1/2}$, $a_0 = 0$, $\tan \beta$.

Low energy observables: $m_h > 114$ GeV, $\text{BR}(B_d \rightarrow B_s \gamma)$, $m_{\text{charged}} > 100$ GeV. Possible hint for supersymmetry (Marciano, Sirlin '08),

$$a_\mu(\text{exp}) - a_\mu(\text{SM}) = 302(88) \times 10^{-11} .$$

Stau and gravitino masses



Left: (A) gravitino: $m_{3/2} < 490$ GeV. *Right:* (B) stau: 100 GeV $< m_{\text{stau}} < 490$ GeV. Red: mass range favoured by a_μ .

Cosmic-Ray Signatures from Decaying Gravitinos

(WB, Ibarra, Shindou, Takayama, Tran '09)

Gravitino decays: $\psi_{3/2} \rightarrow \gamma\nu; h\nu, Z\nu, W^\pm l^\mp$, leads to continuous gamma-ray and antimatter spectrum: $\psi_{3/2} \rightarrow \gamma X, \bar{p}X, e^\pm X$; qualitative features from operator analysis (hierarchy: $m_{SM} \ll m_{3/2} \ll m_{\text{soft}}$):

$$\mathcal{L}_{\text{eff}} = \frac{i\kappa}{\sqrt{2}M_P} \left\{ \bar{l}\gamma^\lambda \gamma^\nu D_\nu \phi \psi_\lambda + \frac{i}{2} \bar{l}\gamma^\lambda (\xi_1 g' Y B_{\mu\nu} + \xi_2 g W_{\mu\nu}) \sigma^{\mu\nu} \phi \psi_\lambda \right\} + \text{h.c.}$$

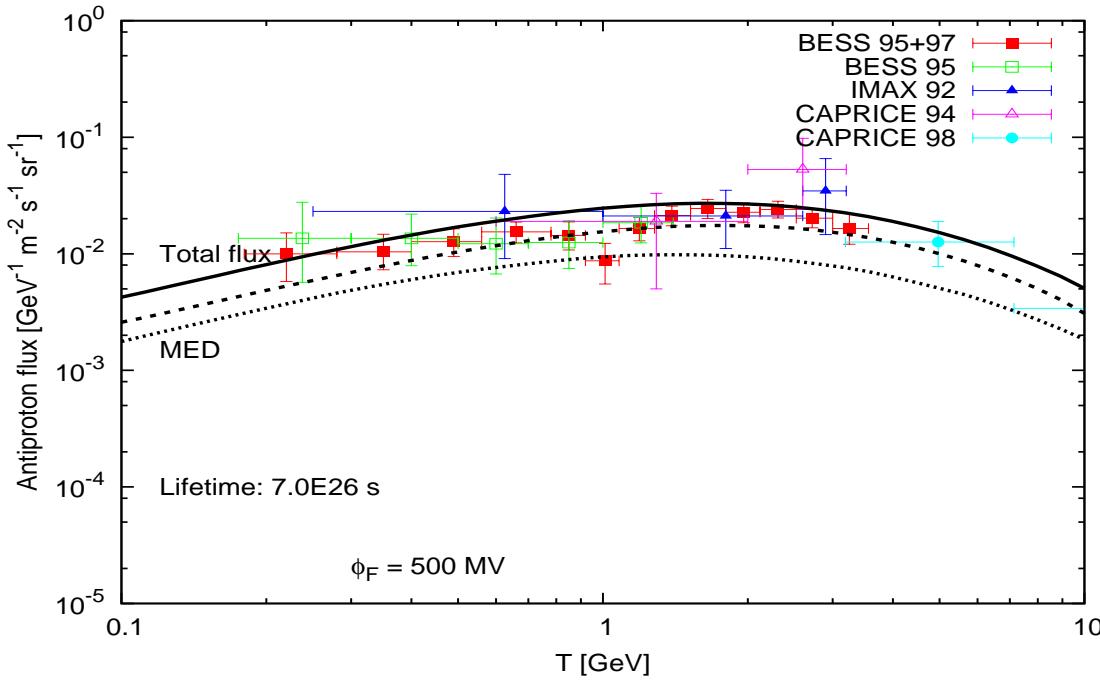
R-parity breaking: κ ; further suppression: $\xi_{1.2} = \mathcal{O}(1/m_{3/2})$

dim 5 : $\psi_{3/2} \rightarrow h\nu, Z\nu, W^\pm l^\mp$; continuous spectrum ,

i.e., single term correlates antiproton flux, PAMELA and Fermi!

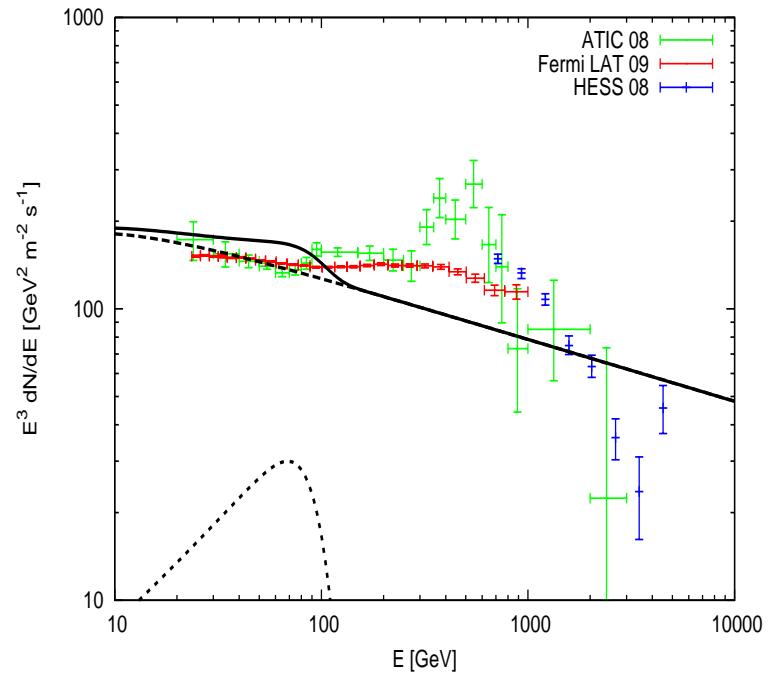
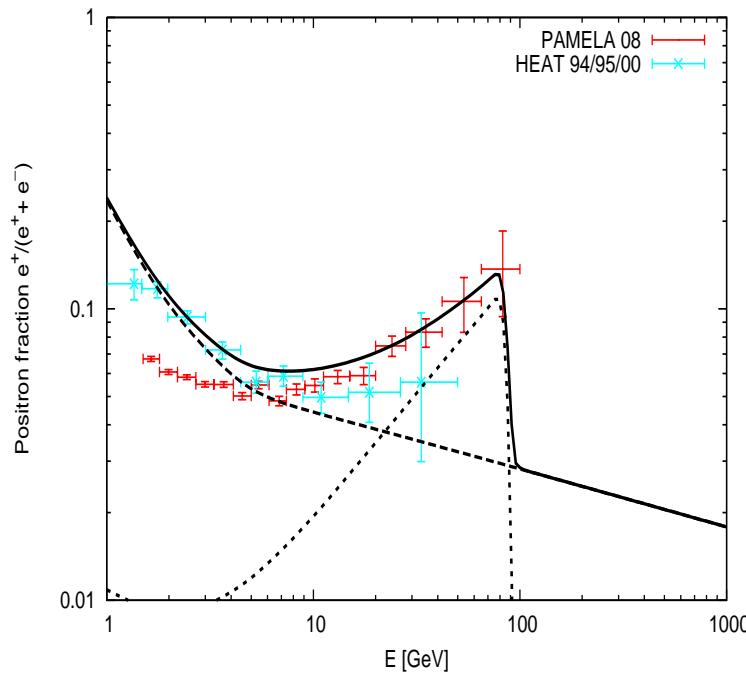
dim 6 : $\psi_{3/2} \rightarrow \gamma\nu$; gamma line

Minimal gravitino lifetime from antiproton flux



conservative propagation model (B/C ratio): MED model; require that total antiproton flux (including gravitino decays) lies below maximal flux from spallation (including astrophysical uncertainties) → **minimal lifetime**; for $m_{3/2} = 200$ GeV one finds $\tau_{3/2}^{\min}(200) = 7 \times 10^{26}$ s.

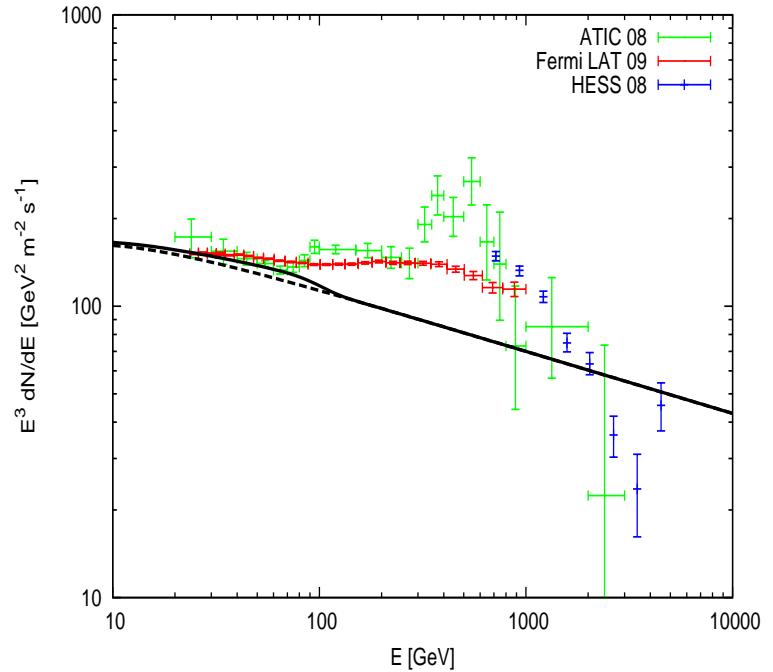
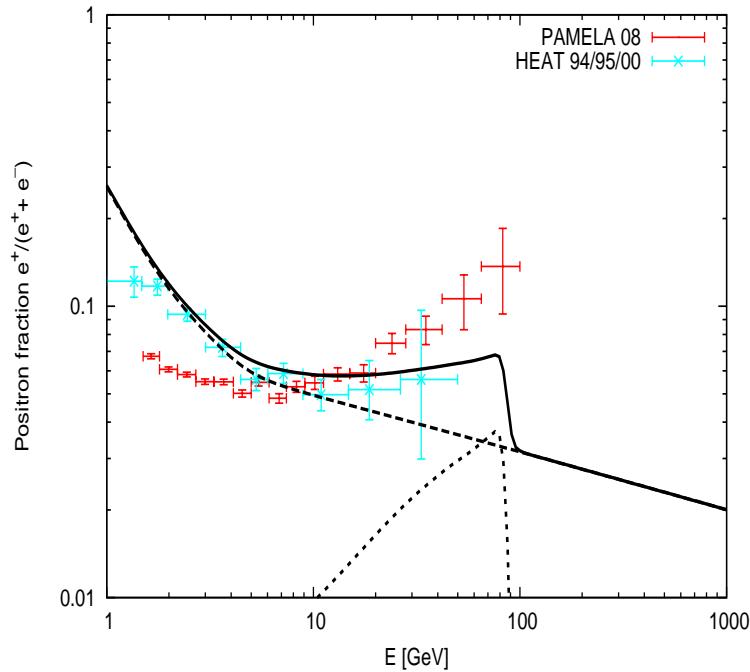
PAMELA & Fermi vs ‘electron dominance’



Input: $m_{3/2} = 200$ GeV, $\tau_{3/2} = 3.2 \times 10^{26}$ s, $\text{BR}(\psi \rightarrow \mu^\pm W^\mp, \tau^\pm W^\mp) \ll \text{BR}(\psi \rightarrow e^\pm W^\mp)$ (**why?**); background: “Model 0” (Grasso et al, Fermi LAT '09)

Conclusion: GALPROP & gravitino **incompatible** with PAMELA & Fermi !!
 [PAMELA & Fermi make CR signature for dark matter **UNLIKELY !!**]

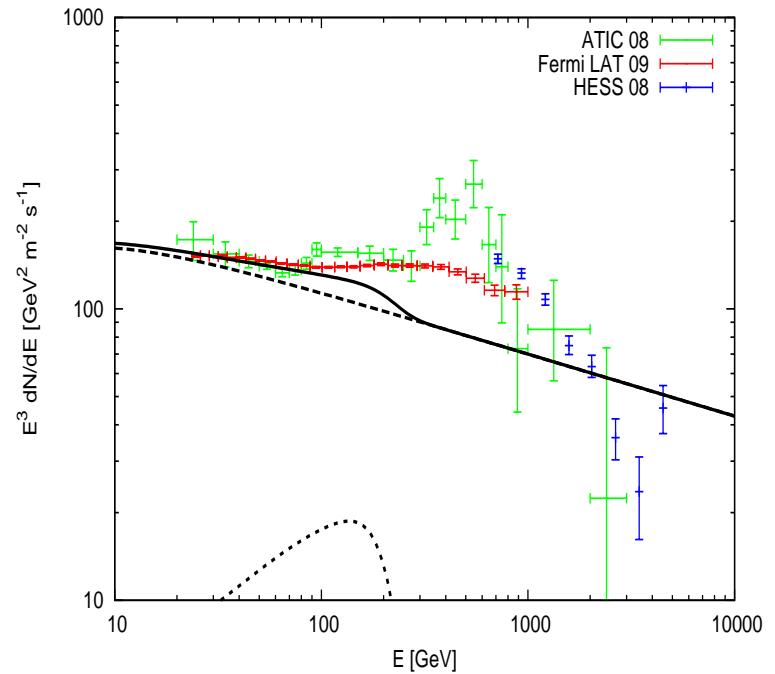
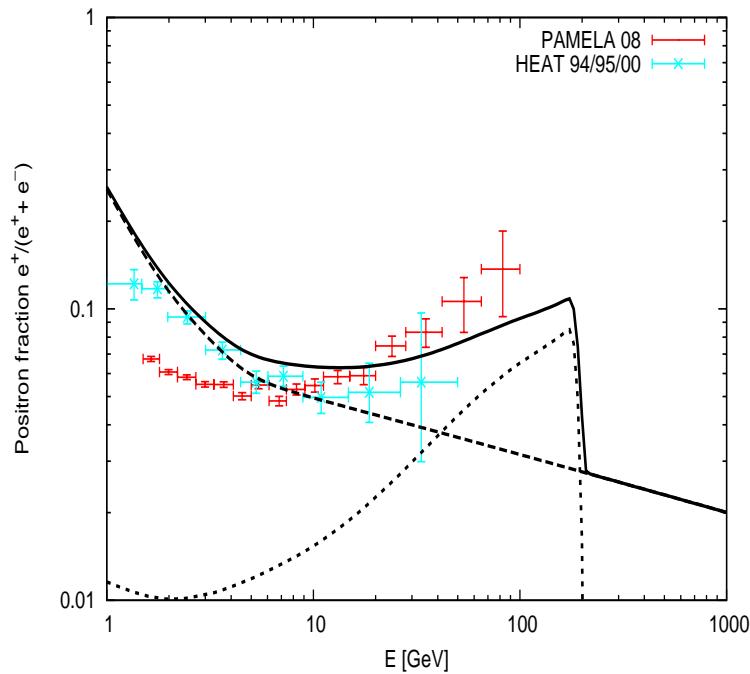
PAMELA & Fermi vs ‘flavour democracy’



Input: $m_{3/2} = 200$ GeV, $\tau_{3/2} = 7 \times 10^{26}$ s, $\text{BR}(\psi \rightarrow l_i^\pm W^\mp)$ universal for $i = e, \mu, \tau$ (theoretical model exists), background: “Model 0”.

Conclusion: **astrophysical sources** needed to explain PAMELA & FERMI!!

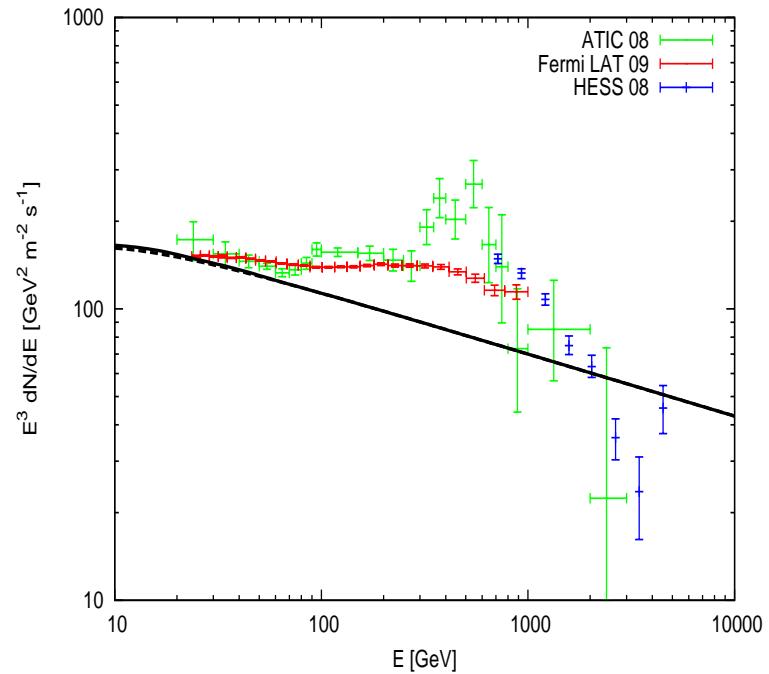
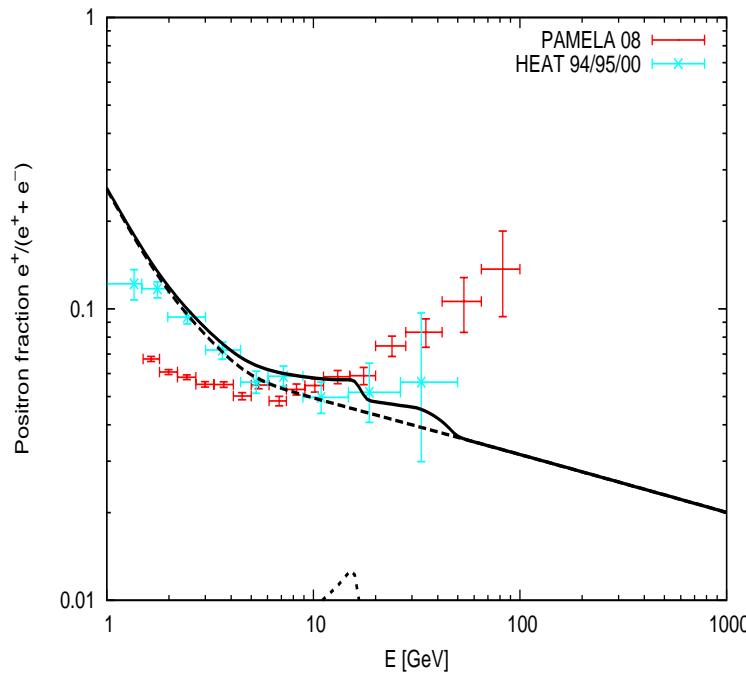
Contribution from gravitino decays to positron fraction **increases** with increasing gravitino mass:



Input: $m_{3/2} = 400 \text{ GeV}$, $\tau_{3/2} = 3 \times 10^{26} \text{ s}$, $\text{BR}(\psi \rightarrow l_i^\pm W^\mp)$ universal for $i = e, \mu, \tau$, background: “Model 0”.

Conclusion: gravitino contribution to electron/positron fluxes may be sizable, has to be complemented by astrophysical sources!

Contribution from gravitino decays to positron fraction **decreases rapidly** for gravitino masses below 200 GeV:



Input: $m_{3/2} = 100$ GeV, $\tau_{3/2} = 1 \times 10^{27}$ s, $\text{BR}(\psi \rightarrow l_i^\pm W^\mp)$ universal for $i = e, \mu, \tau$, background: “Model 0”.

Conclusion: gravitino contribution to electron/positron fluxes may be **negligible**, as for antiproton flux!

Predictions for the Gamma-Ray Spectrum

Important contributions from extragalactic DM and DM in the Milky Way halo; typical branching ratio for gamma line (cf. operator analysis):

$$\text{BR}(\psi_{3/2} \rightarrow \nu\gamma) \sim 0.02 \left(\frac{200 \text{ GeV}}{m_{3/2}} \right)^2 ;$$

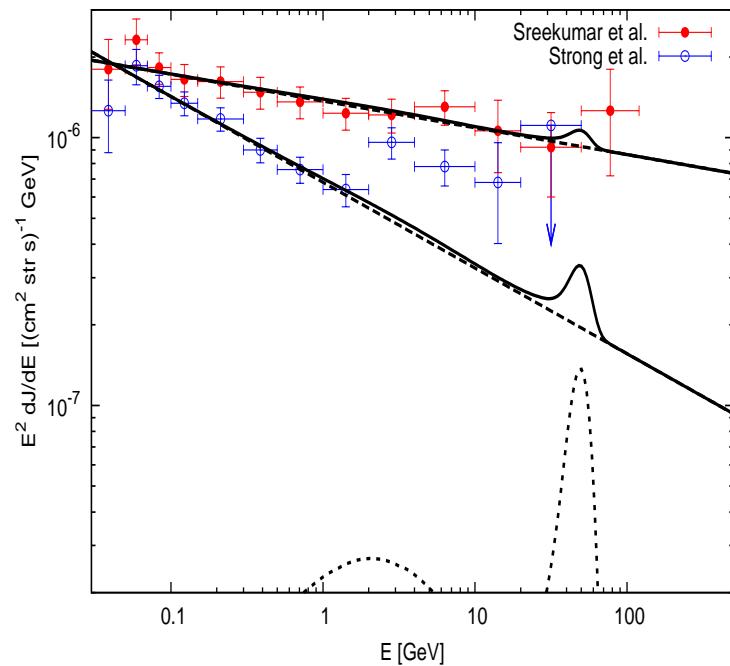
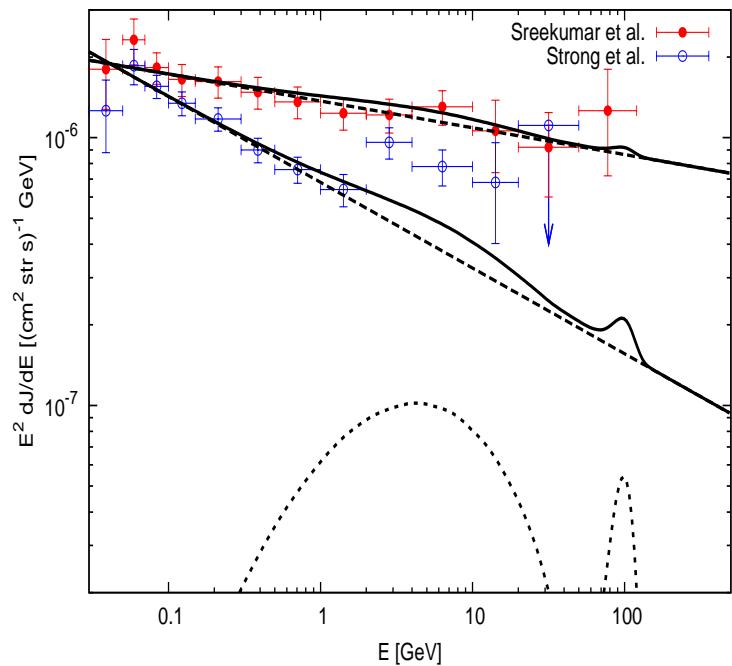
Gamma-ray background presently uncertain, two analyses of EGRET data;
Sreekumar et al:

$$\left[E^2 \frac{dJ}{dE} \right]_{\text{bg}} = 1.37 \times 10^{-6} \left(\frac{E}{\text{GeV}} \right)^{-0.1} (\text{cm}^2 \text{ str s})^{-1} \text{ GeV} ,$$

and Moskalenko et al:

$$\left[E^2 \frac{dJ}{dE} \right]_{\text{bg}} = 6.8 \times 10^{-7} \left(\frac{E}{\text{GeV}} \right)^{-0.32} (\text{cm}^2 \text{ str s})^{-1} \text{ GeV}.$$

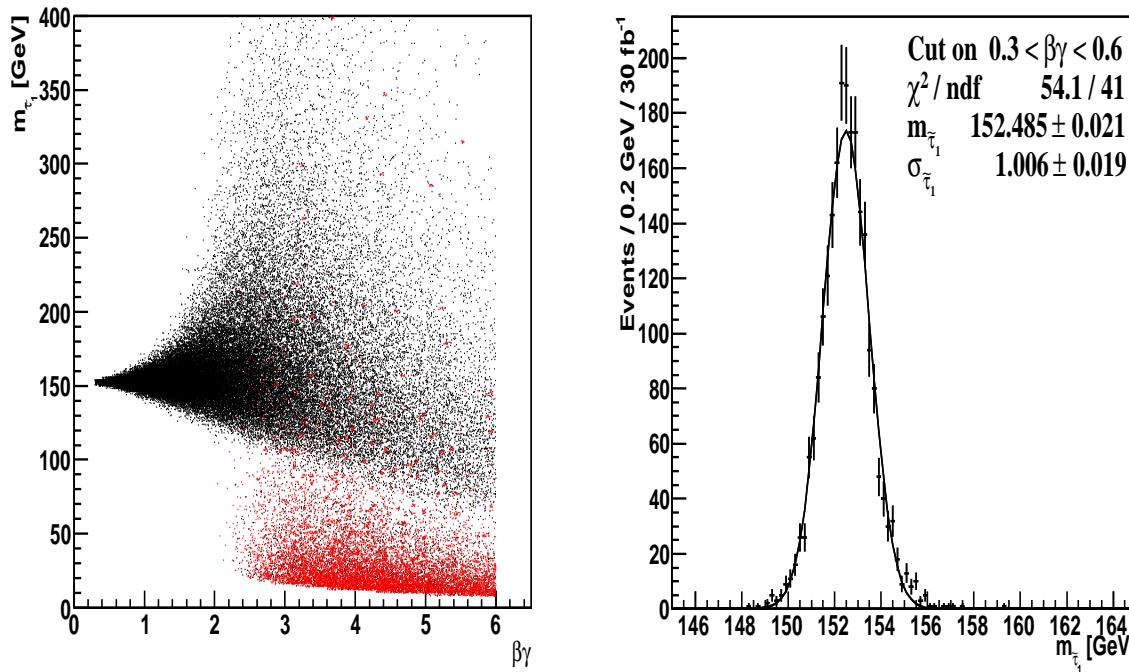
Height of gamma line depends on energy resolution (assumed: $\sigma(E)/E = 15\%$) and background; ‘minimal’ lifetime from antiproton flux constraint give maximal gamma-ray flux:



left: $m_{3/2} = 200 \text{ GeV}, \tau_{3/2} = 7 \times 10^{26} \text{ s}$; right: $m_{3/2} = 100 \text{ GeV}, \tau_{3/2} = 1 \times 10^{27} \text{ s}$; improvement of energy resolution?

Hope for the LHC: $\tilde{\tau}$ -mass measurement (Ellis, Raklev, Oye '06)

$\tilde{\tau}$ -mass can be measured from $m_{\tilde{\tau}} = p_{\text{meas}}/\beta\gamma_{\text{meas}}$, slow $\tilde{\tau}$'s important!
Background from muon tracks, accurate measurement of $\tilde{\tau}$ -mass possible



analysis relevant for sufficiently long lifetimes, such that the $\tilde{\tau}$ -lepton leaves the detector; more work in progress ...

SUMMARY

- Gravitino DM is viable possibility
- Gravitino DM is theoretically motivated: leptogenesis and/or gauge mediation ...
- Decaying gravitino DM consistent with leptogenesis and BBN
- GALPROP & gravitino DM **incompatible** with PAMELA & Fermi, **astrophysical sources** needed !!
- Sizable excess in **gamma-ray** spectrum possible, in particular **line** at $E_\gamma \simeq m_{3/2}/2$. Gravitino DM can be discovered with Fermi LAT and/or falsified at the LHC !!