

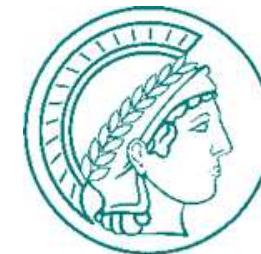
Discovery Reach for Non-Standard Interactions in a Neutrino Factory

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Introduction

References: P. Huber and J. W. F. Valle, Phys. Lett. **B523** (2001) 151. P. Huber, T. Schwetz, J. W. F. Valle, Phys. Rev. **D66** (2002) 013006. A. M. Gago, M. M. Guzzo, H. Nunokawa, W. J. C. Teves, and R. Zukanovich Funchal Phys. Rev. **D64** (2001) 073003. Y. Grossman, Phys. Lett. **B359** (1995) 141. M. C. Gonzalez-Garcia, Y. Grossman, A. Gusso, and Y. Nir, Phys. Rev. **D64** (2001) 096006. G. L. Fogli, E. Lisi, A. Mirizzi, and D. Montanino, Phys. Rev. **D66** (2002) 013009. T. O, J. Sato, and N. Yamashita, Phys. Rev. **D65** (2002) 093015. S. Davidson, C. Peña-Garay, N. Rius, and A. Santamaria, JHEP **0303** (2003) 011. M. Blennow, T. Ohlsson, and W. Winter, hep-ph/0508175. M. Honda, N. Okamura, and T. Takeuchi, hep-ph/0603268. N. Kitazawa, H. Sugiyama, and O. Yasuda hep-ph/0606013. A. Friedland and C. Lunardini, Phys. Rev. **D74** (2006) 033012.

Introduction — Motivation

- The aim of future neutrino experiments is the precision measurement of the oscillation parameters such as θ_{13} and δ_{CP}
- Osc. probabilities will be measured with $\mathcal{O}(1\text{-}0.1)\%$ or higher accuracy.
- We have a good chance to observe not only the standard oscillation phenomena but also the sub-leading effects induced by non-standard interactions (NSIs).

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- NSIs — Flavour violating interactions with neutrinos such as $\nu_\alpha f \rightarrow \nu_\beta f$, $\ell_\alpha^- \rightarrow \nu_\beta e^- \bar{\nu}_e \dots$

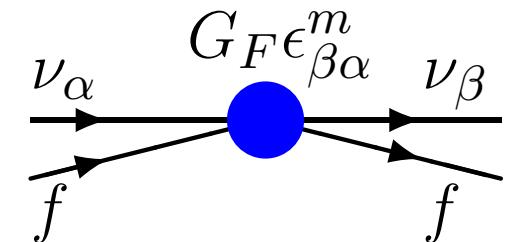
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- NSIs — Flavour violating interactions with neutrinos such as $\nu_\alpha f \rightarrow \nu_\beta f$, $\ell_\alpha^- \rightarrow \nu_\beta e^- \bar{\nu}_e \dots$

- It can be written as eff. 4-Fermi int. as

$$-\mathcal{L}_{\text{NSI}} = 2\sqrt{2}G_F \epsilon_{\beta\alpha}^m (\bar{\nu}_\beta \gamma^\rho P_L \nu_\alpha) (\bar{f} \gamma_\rho P_{L/R} f)$$

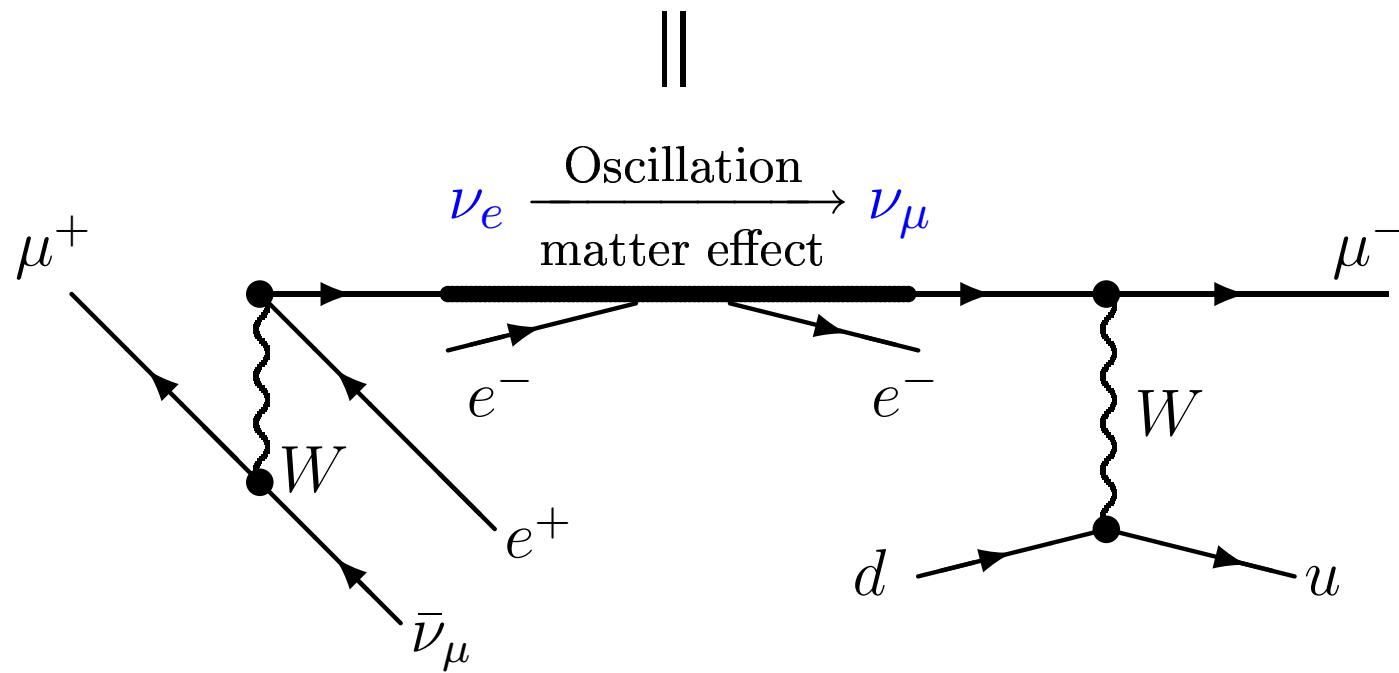


- We study the discovery reach of the NSIs in the osc. exp.

Introduction — Standard oscillation

- A long baseline exp. can be described diagrammatically as

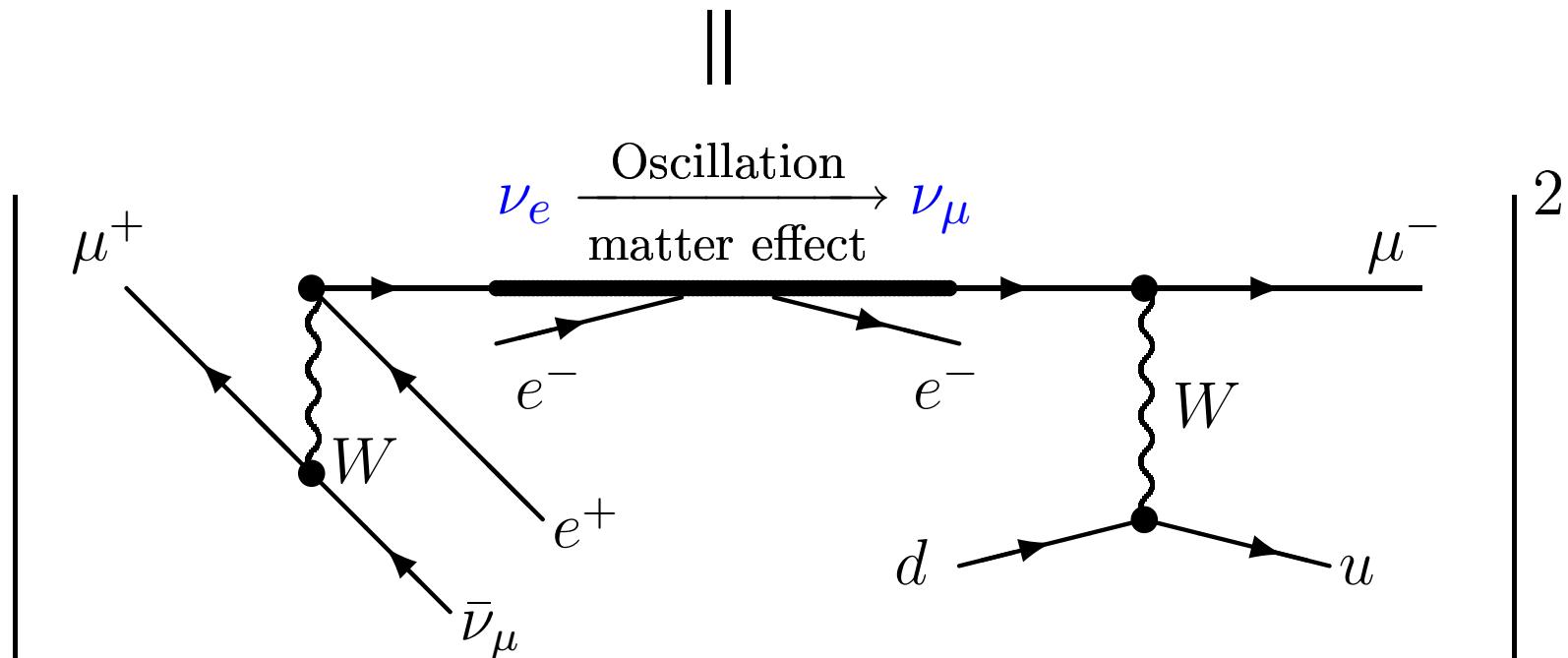
$$\mathcal{A}(\nu_\mu N \rightarrow \mu^- X) \langle \nu_\mu | e^{-iH_L} | \nu_e \rangle \mathcal{A}(\mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e)$$



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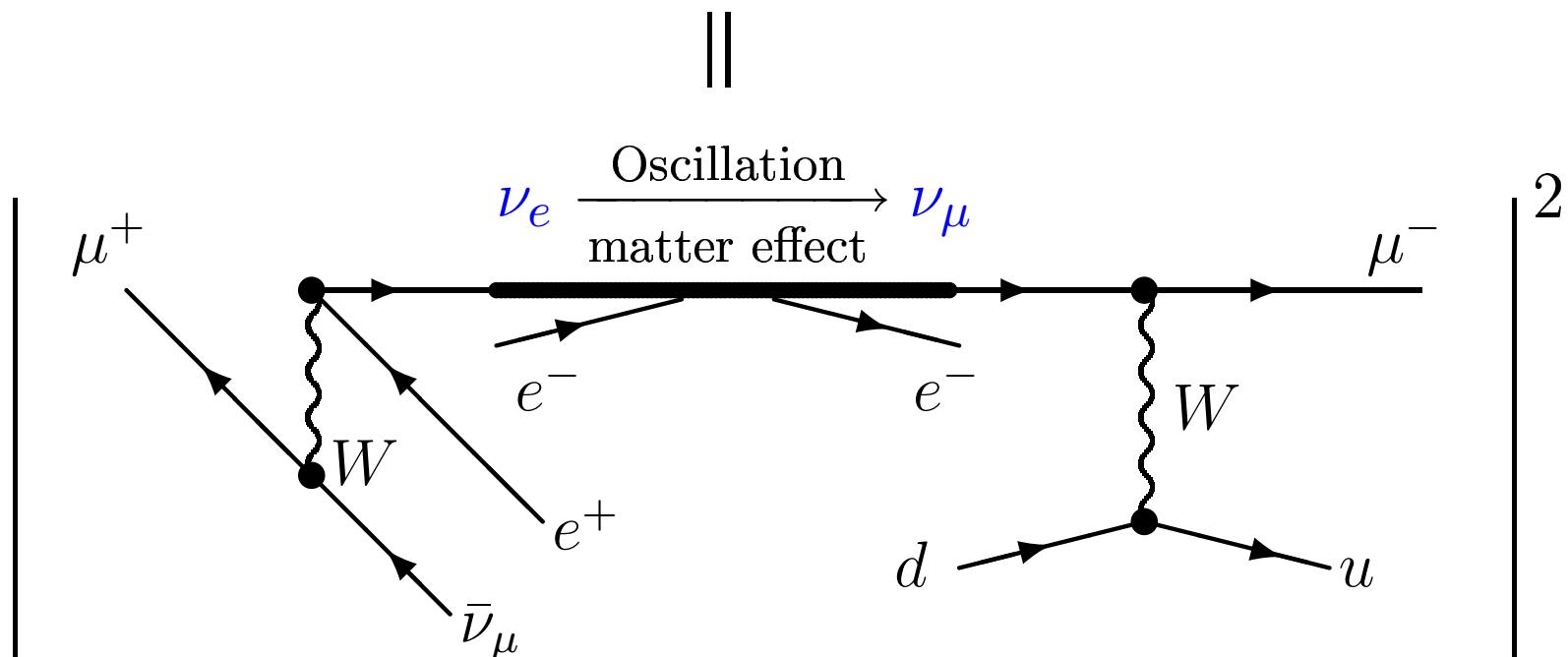
$$\left| \mathcal{A}(\nu_\mu N \rightarrow \mu^- X) \langle \nu_\mu | e^{-iH_L} | \nu_e \rangle \mathcal{A}(\mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e) \right|^2$$



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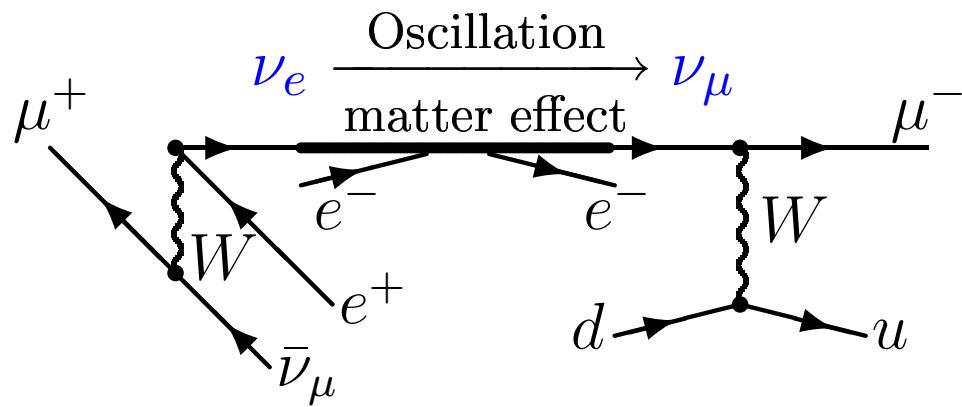
$$\sigma(\nu_\mu N \rightarrow \mu^- X) \times P_{\nu_e \rightarrow \nu_\mu} \times \Gamma(\mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e)$$



Introduction — Oscillation enhanced search for NSIs

- ν osci. = Flavour changing process

$$\ell_\alpha^- \xrightarrow{\text{CC}} \nu_\alpha \xrightarrow{\text{osc}} \nu_\beta \xrightarrow{\text{CC}} \ell_\beta^-$$



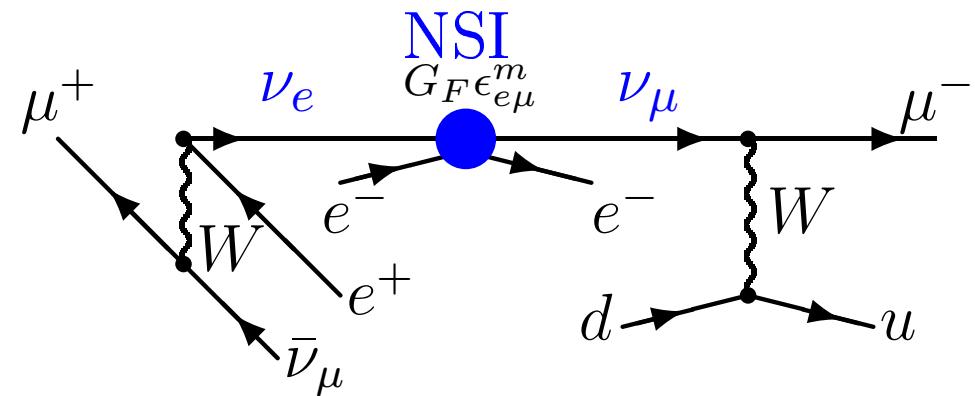
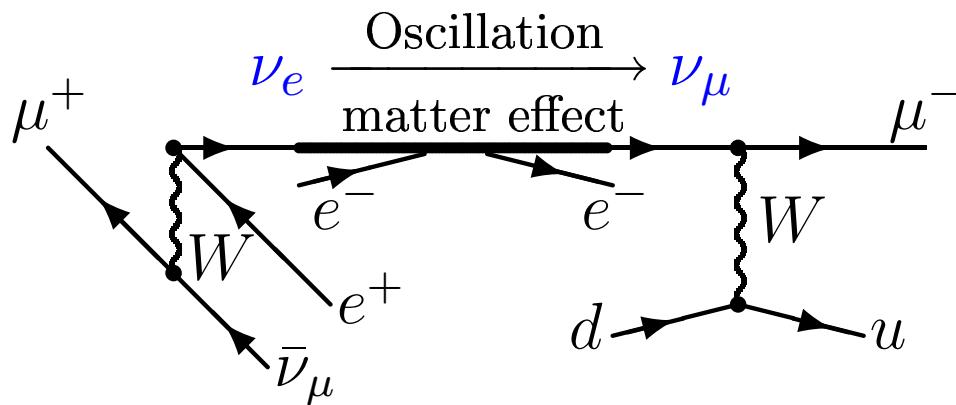
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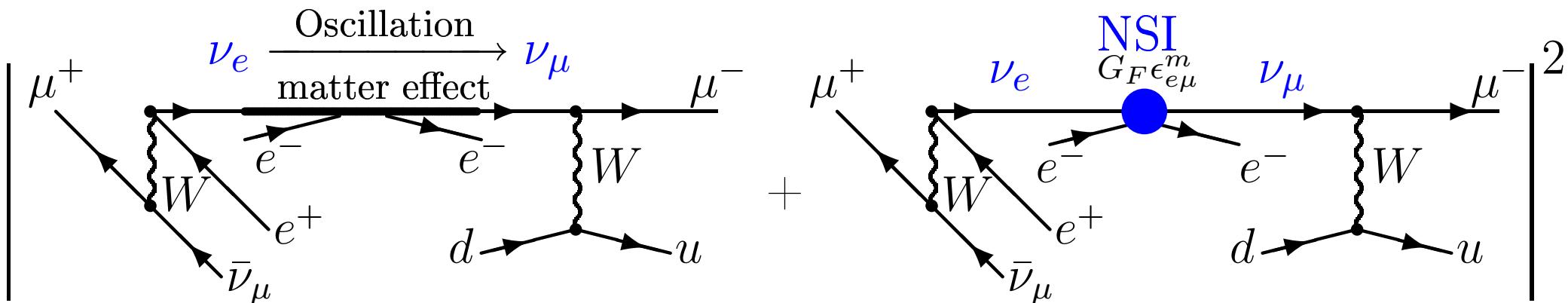
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$$\ell_\alpha^- \xrightarrow{\text{CC}} \nu_\alpha \xrightarrow{\text{NSI}} \nu_\beta \xrightarrow{\text{CC}} \ell_\beta^-$$

— They interfere with each other.



- The signals of NSI appear in the osc. probability at $\mathcal{O}(\epsilon_{e\mu}^m)$.
 - This is quite different from the charged lepton LFV process.
e.g., $\text{Br}(\mu \rightarrow 3e)$ is proportional to $|\epsilon_{e\mu}^m|^2$.

Introduction — Oscillation enhanced search for NSIs

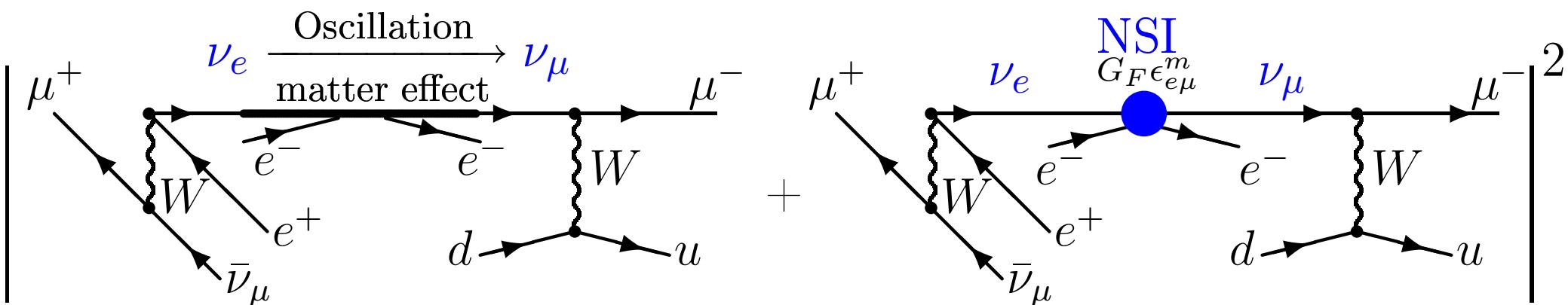
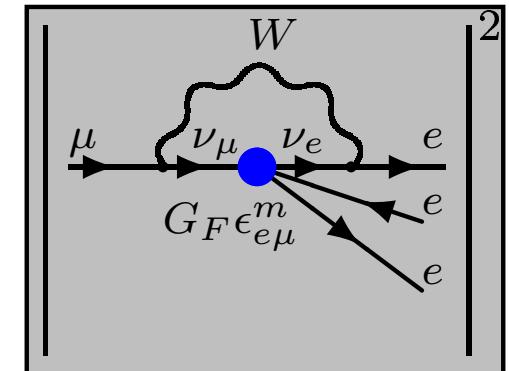
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Introduction — NSIs in matter

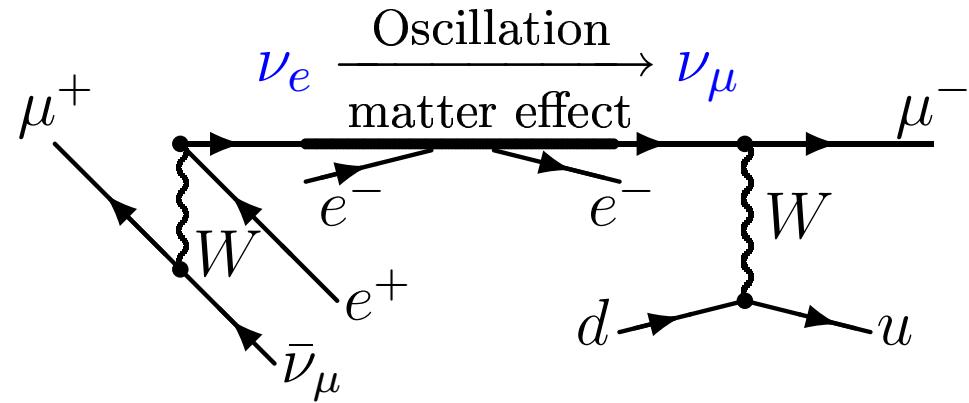
- NSIs in matter can be described by extra potential terms
 - We parametrize them as

$$H_{\beta\alpha} = \frac{1}{2E_\nu} \left\{ U \begin{pmatrix} 0 & & \\ & \Delta m_{21}^2 & \\ & & \Delta m_{31}^2 \end{pmatrix} U^\dagger + \begin{pmatrix} a_{CC} & & \\ & 0 & \\ & & 0 \end{pmatrix} + (V_{\text{NSI}})_{\beta\alpha} \right\},$$

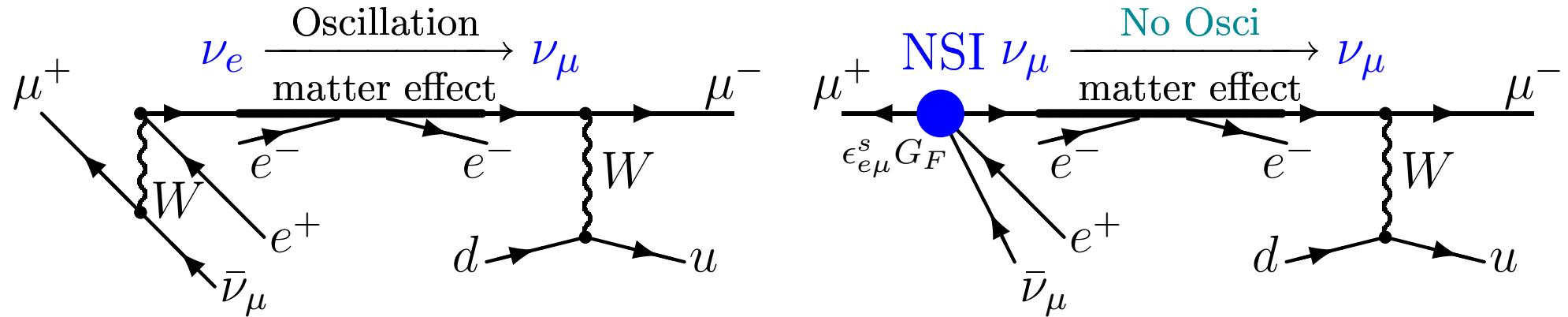
$$(V_{\text{NSI}})_{\beta\alpha} = a_{CC} \begin{pmatrix} \epsilon_{ee}^m & \epsilon_{e\mu}^m & \epsilon_{e\tau}^m \\ (\epsilon_{e\mu}^m)^* & \epsilon_{\mu\mu}^m & \epsilon_{\mu\tau}^m \\ (\epsilon_{e\tau}^m)^* & (\epsilon_{\mu\tau}^m)^* & \epsilon_{\tau\tau}^m \end{pmatrix}$$

- In general, each off-diagonal (flavour violating) element has a complex phase.

Introduction — NSI in beam source



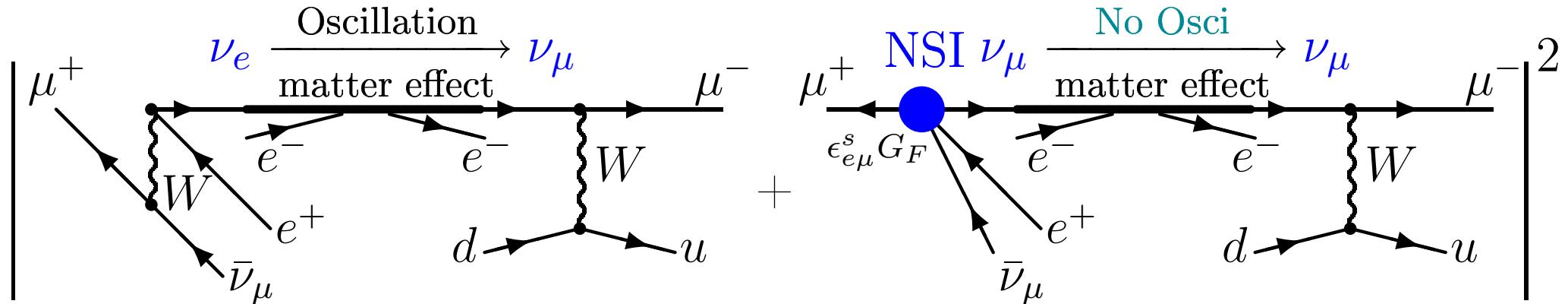
Introduction — NSI in beam source



- NSIs in beam source can be treated by a flavour mixture state

$$|\nu_e^{(s)}\rangle = |\nu_e\rangle + \epsilon_{e\mu}^s |\nu_\mu\rangle.$$

Introduction — NSI in beam source



- NSIs in beam source can be treated by a flavour mixture state

$$|\nu_e^{(s)}\rangle = |\nu_e\rangle + \epsilon_{e\mu}^s |\nu_\mu\rangle.$$

- The oscillation probability is calculated with the *source state* as

$$P_{\nu_e \rightarrow \nu_\mu} = \left| \langle \nu_\mu | e^{-iHL} | \nu_e^{(s)} \rangle \right|^2 = \left| \langle \nu_\mu | e^{-iHL} | \nu_e \rangle + \epsilon_{e\mu}^s \langle \nu_\mu | e^{-iHL} | \nu_\mu \rangle \right|^2$$

— Interference between Osc. Amp. and NSI. Amp.

Discovery reach for NSIs in neutrino factory

Reference: P. Huber, M. Lindner, and W. Winter, Comput. Phys. Commun. **167** (2005) 195.

Discovery reach for NSIs in neutrino factory

- Discovery reach for $\epsilon_{e\mu}^m$ in neutrino factory
 - how small $|\epsilon_{e\mu}^m|$ can be found in the neutrino factory.

- We introduce a NSI as the complex parameter
 - There is no reason to consider it is a real parameter.
 - The discovery reach strongly depends on the phase.
- We turn off all NSIs other than the NSI which we study.
- Modified GLoBES software is used.
- The following values are adopted as the true value of the standard oscillation parameters



$$\sin^2 2\theta_{12}^{\text{true}} = 0.83, \quad \sin^2 2\theta_{13}^{\text{true}} = 0.01, \quad \sin^2 2\theta_{23}^{\text{true}} = 1.0,$$
$$(\Delta m_{21}^2)^{\text{true}} = 8.2 \times 10^{-5} \text{ [eV}^2], \quad (\Delta m_{31}^2)^{\text{true}} = 2.5 \times 10^{-3} \text{ [eV}^2].$$

Discovery reach for NSIs in neutrino factory

- Discovery reach for $|(\epsilon_{e\mu}^m)^{\text{true}}|$ is determined by^a

$$\chi^2 \equiv \min_{\lambda} \sum_i^{\text{bin}} |N_i(\lambda^{\text{true}}, (\epsilon_{e\mu}^m)^{\text{true}}) - N_i(\lambda, \epsilon_{e\mu}^m = 0)|^2 / V_i,$$

where $\lambda \in \{\theta_{12}, \theta_{13}, \theta_{23}, \delta_{\text{CP}}, \Delta m_{21}^2, \Delta m_{31}^2, a_{\text{CC}}\}$.

- If $\chi^2 > \chi^2_{3\sigma}$, the effect induced by the NSI with the value of $|(\epsilon_{e\mu}^m)^{\text{true}}|$ will be discovered at the 3σ level.

- Undetermined parameters: $\delta_{\text{CP}}^{\text{true}}$ and $\arg[(\epsilon_{e\mu}^m)^{\text{true}}]$
 - We scan the value of χ^2 on the $\delta_{\text{CP}}^{\text{true}}\text{-}\arg[(\epsilon_{e\mu}^m)^{\text{true}}]$ plane for the fixed $|(\epsilon_{e\mu}^m)^{\text{true}}|$.

^a In the numerical calculation, we use the χ^2 function for the Poisson distribution.

Discovery reach for $\epsilon_{e\mu}^m$ in neutrino factory

- In the case $|(\epsilon_{e\mu}^m)^{\text{true}}| = 5 \times 10^{-4}$,

- $|\epsilon_{e\mu}^m|$ is too small



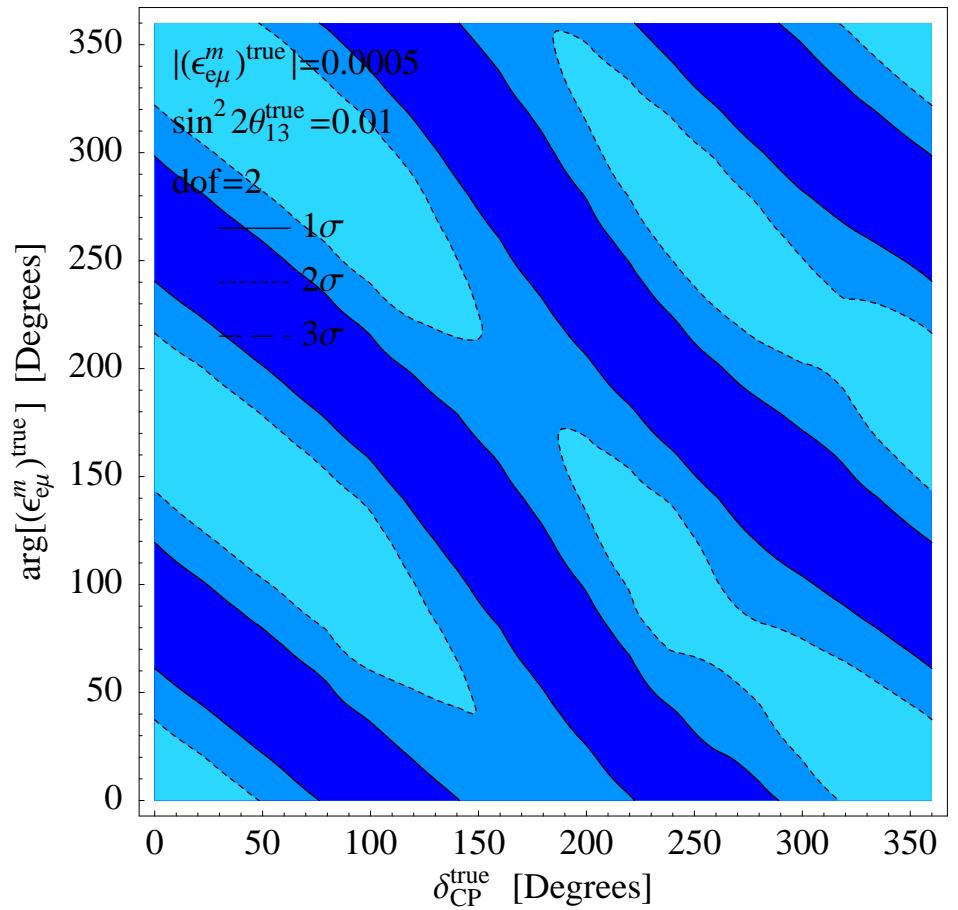
χ^2 cannot exceed 3σ on the whole parameter plane. (Under the sea)



The deviation from the standard oscillation is not significant



No chance to discover!



Discovery reach for $\epsilon_{e\mu}^m$ in neutrino factory

- In the case $|(\epsilon_{e\mu}^m)^{\text{true}}| = 6 \times 10^{-4}$,

- $|\epsilon_{e\mu}^m|$ becomes larger



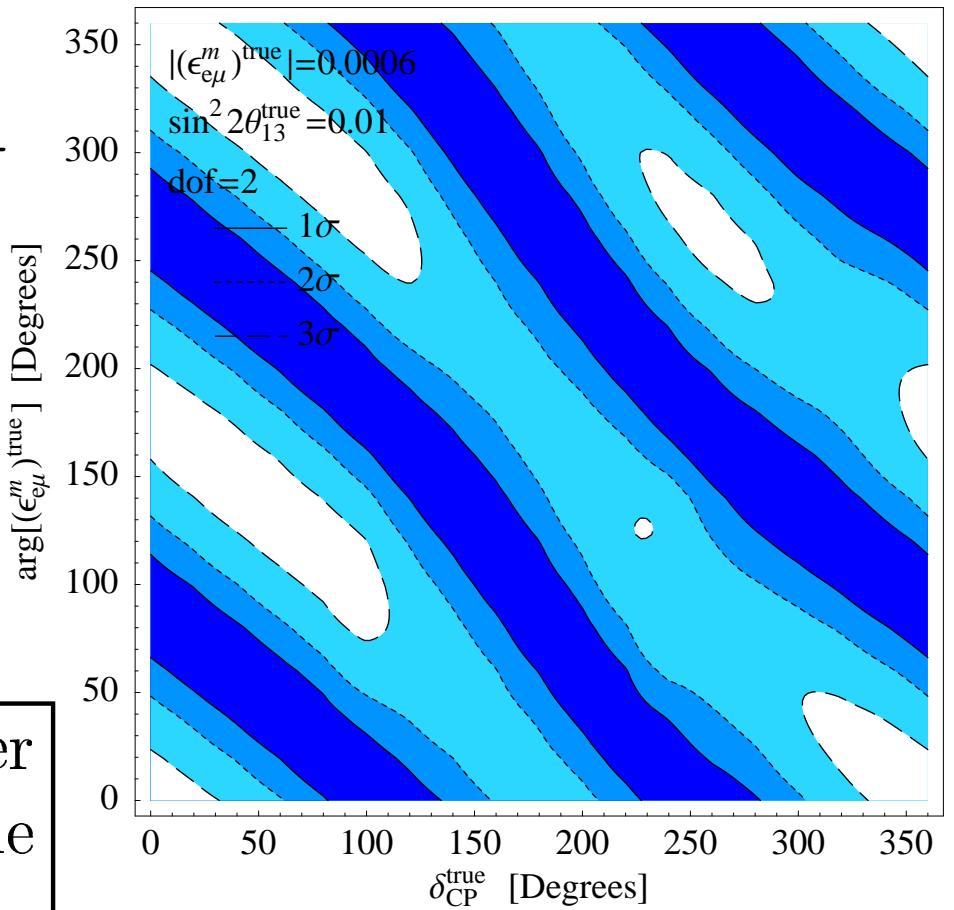
In some regions χ^2 exceeds 3σ
(Islands appear)



The deviation from the
standard oscillation is
significant at 3σ



We have a chance to discover
NSI effect depending on the
phases



Discovery reach for $\epsilon_{e\mu}^m$ in neutrino factory

- In the case $|(\epsilon_{e\mu}^m)^{\text{true}}| = 1 \times 10^{-3}$,

- $|\epsilon_{e\mu}^m|$ becomes larger



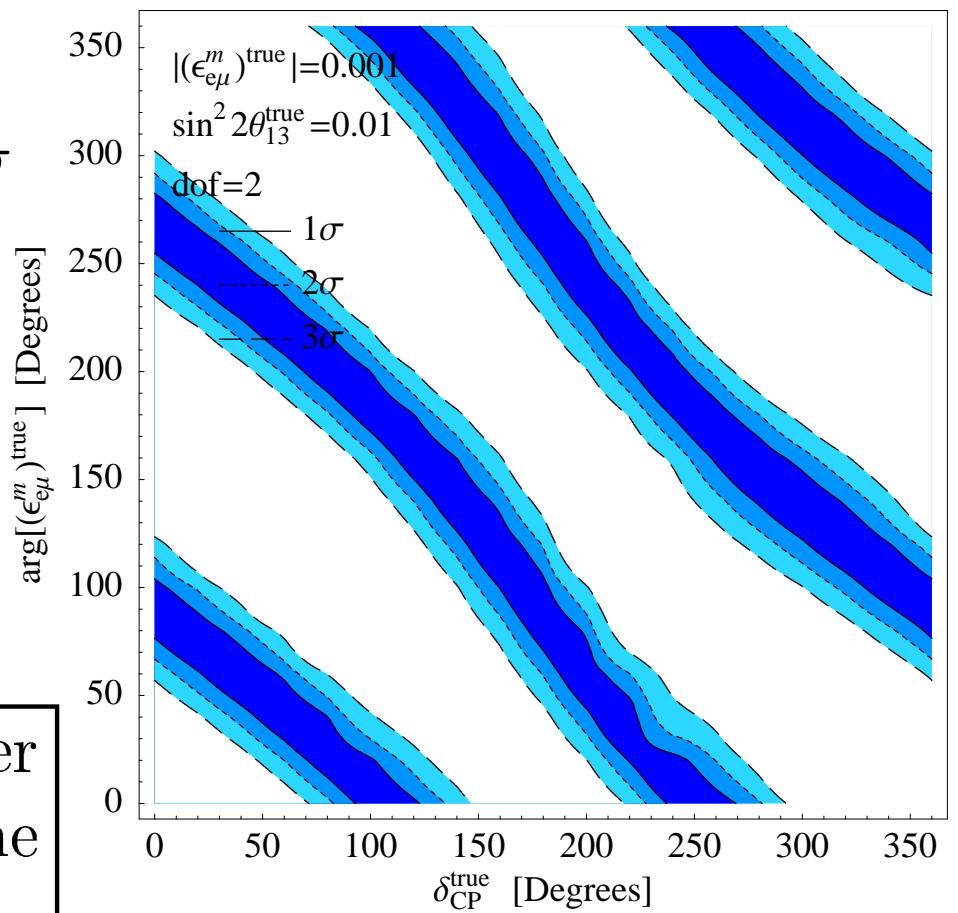
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The deviation from the
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Discovery reach for $\epsilon_{e\mu}^m$ in neutrino factory

- In the case $|(\epsilon_{e\mu}^m)^{\text{true}}| = 2 \times 10^{-3}$,

- $|\epsilon_{e\mu}^m|$ becomes larger



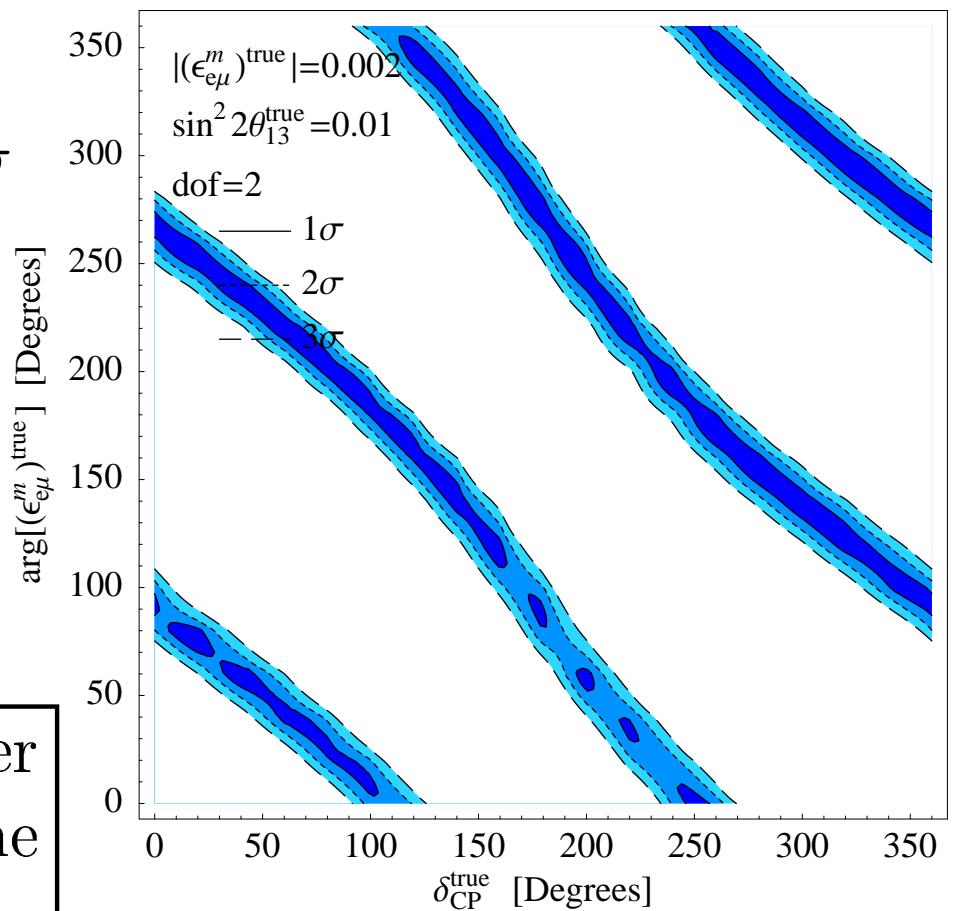
In some regions χ^2 exceeds 3σ
(Islands appear)



The deviation from the
standard oscillation is
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We have a chance to discover
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Discovery reach for $\epsilon_{e\mu}^m$ in neutrino factory

- In the case $|(\epsilon_{e\mu}^m)^{\text{true}}| = 4 \times 10^{-3}$,

- $|\epsilon_{e\mu}^m|$ becomes larger



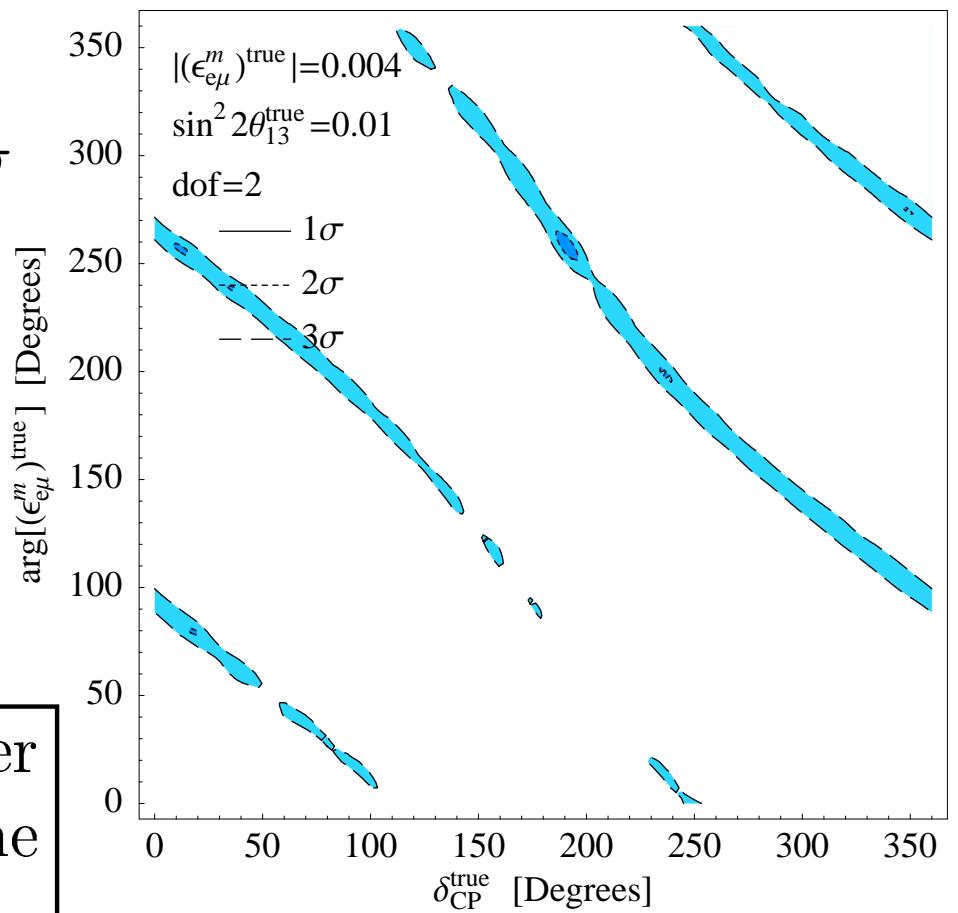
In some regions χ^2 exceeds 3σ
(Islands appear)



The deviation from the
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Discovery reach for $\epsilon_{e\mu}^m$ in neutrino factory

- In the case $|(\epsilon_{e\mu}^m)^{\text{true}}| = 5 \times 10^{-3}$,

- $|\epsilon_{e\mu}^m|$ is large enough



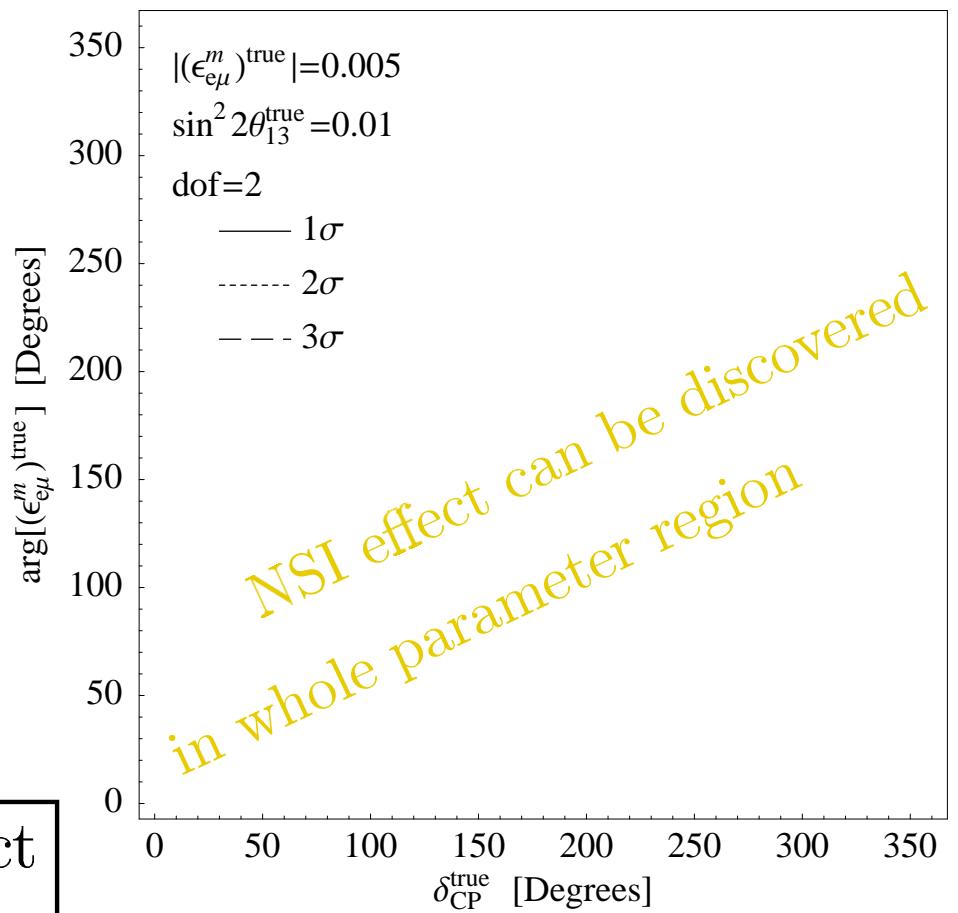
χ^2 exceeds 3σ on the whole parameter plane
(The sea disappears)



The deviation from the standard oscillation is significant at 3σ

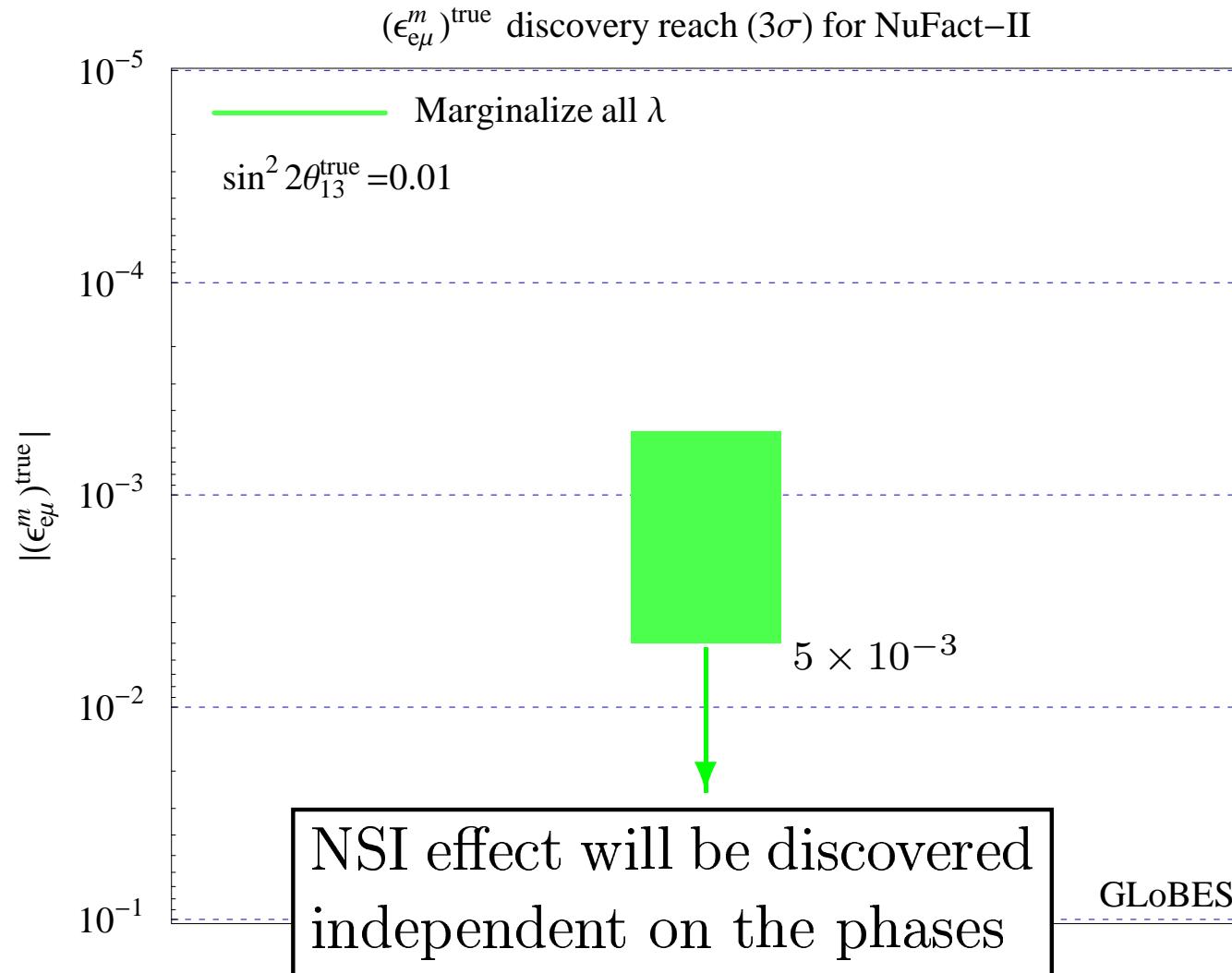


We can observe the NSI effect with any values of phases.



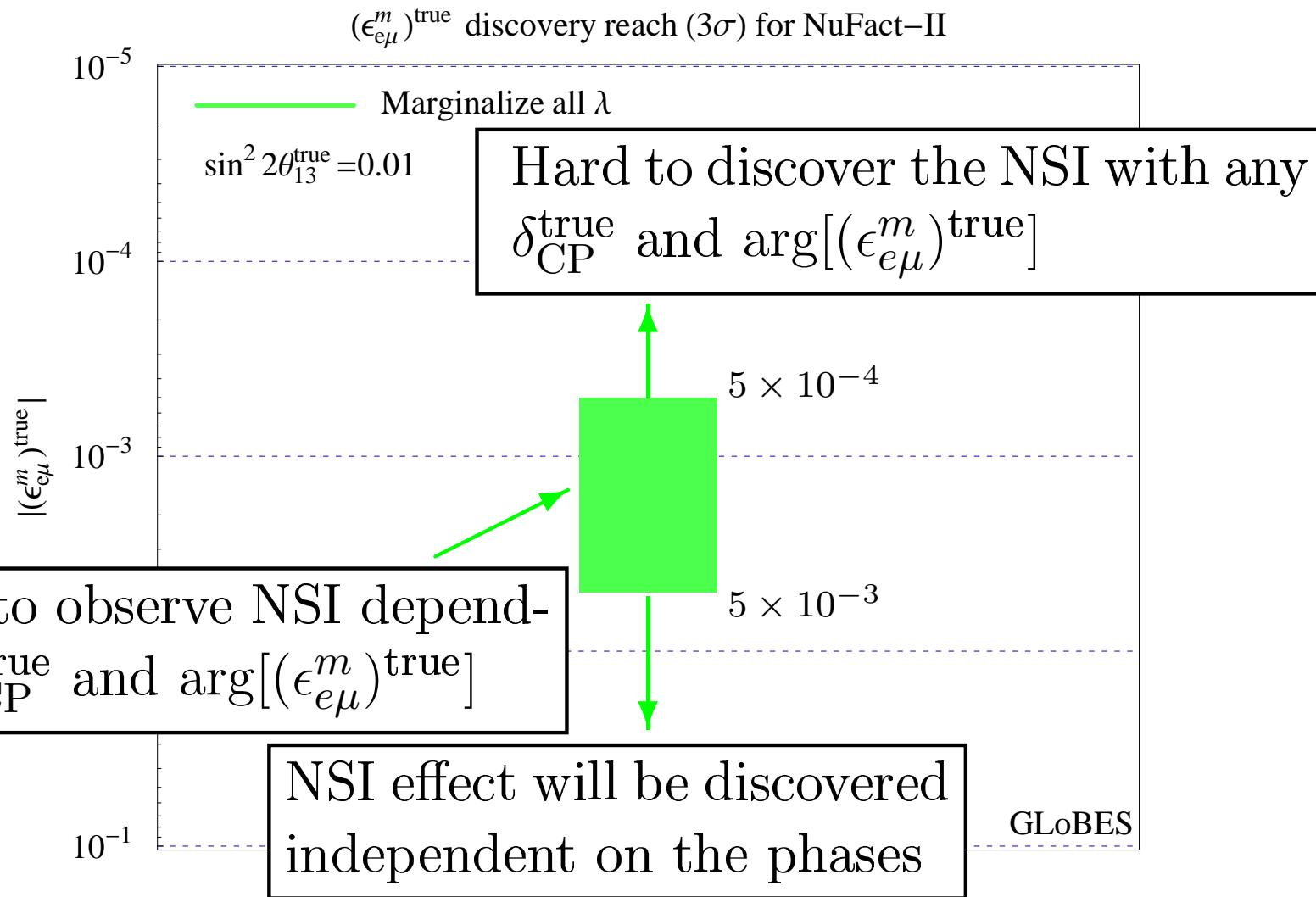
Discovery reach for NSIs in neutrino factory

- Summary plot for the discovery reach of $\epsilon_{e\mu}^m$



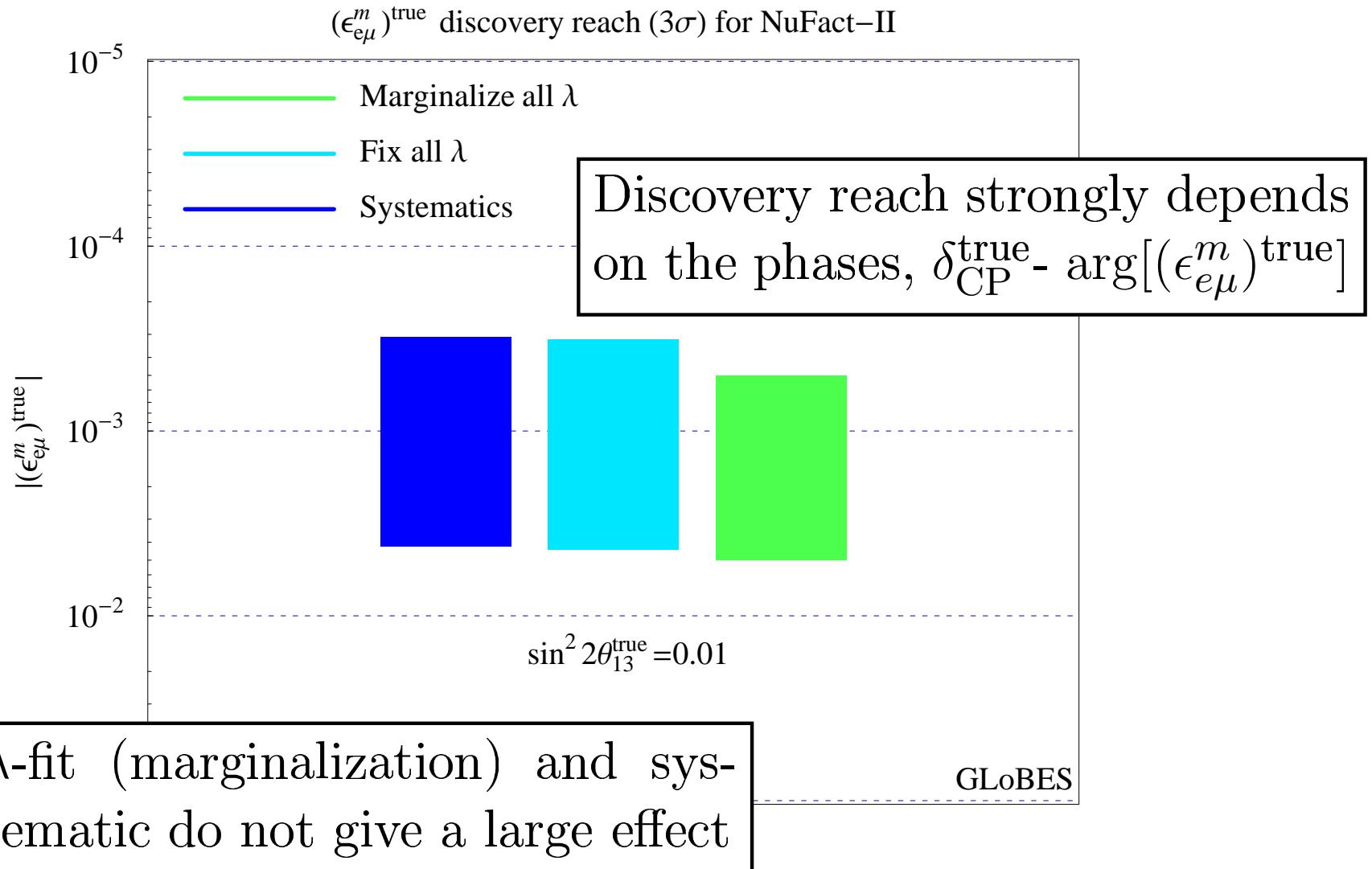
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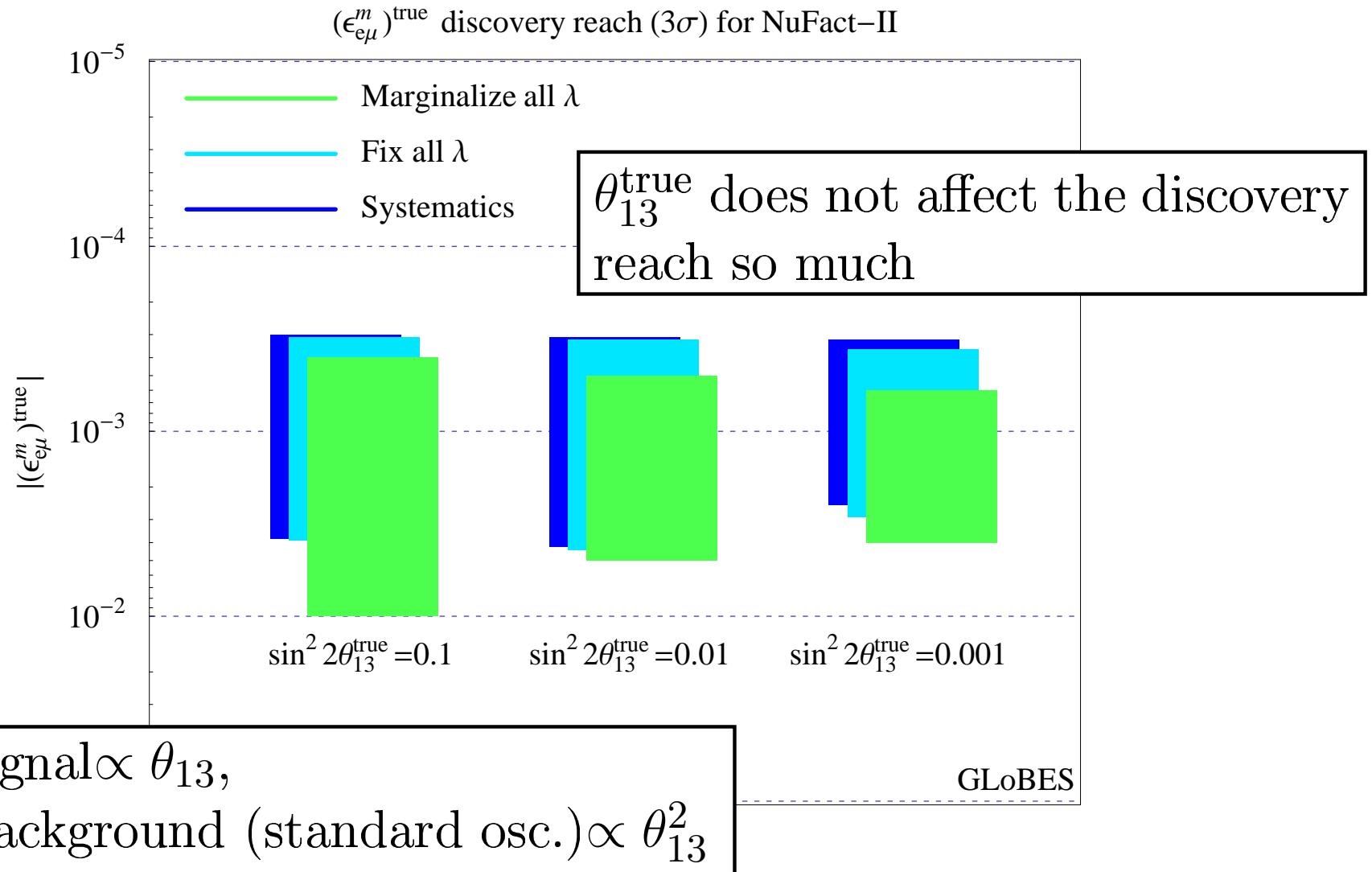
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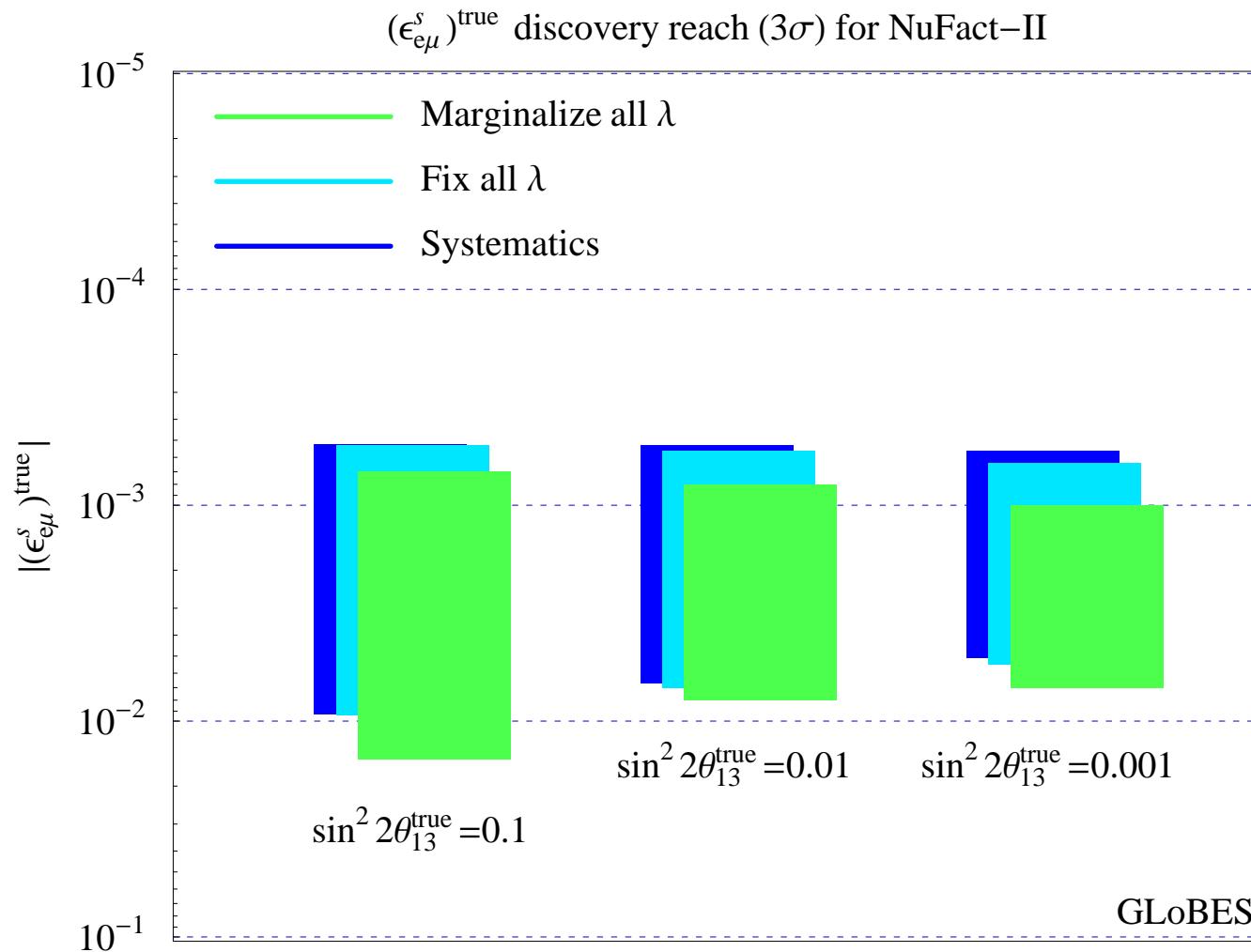
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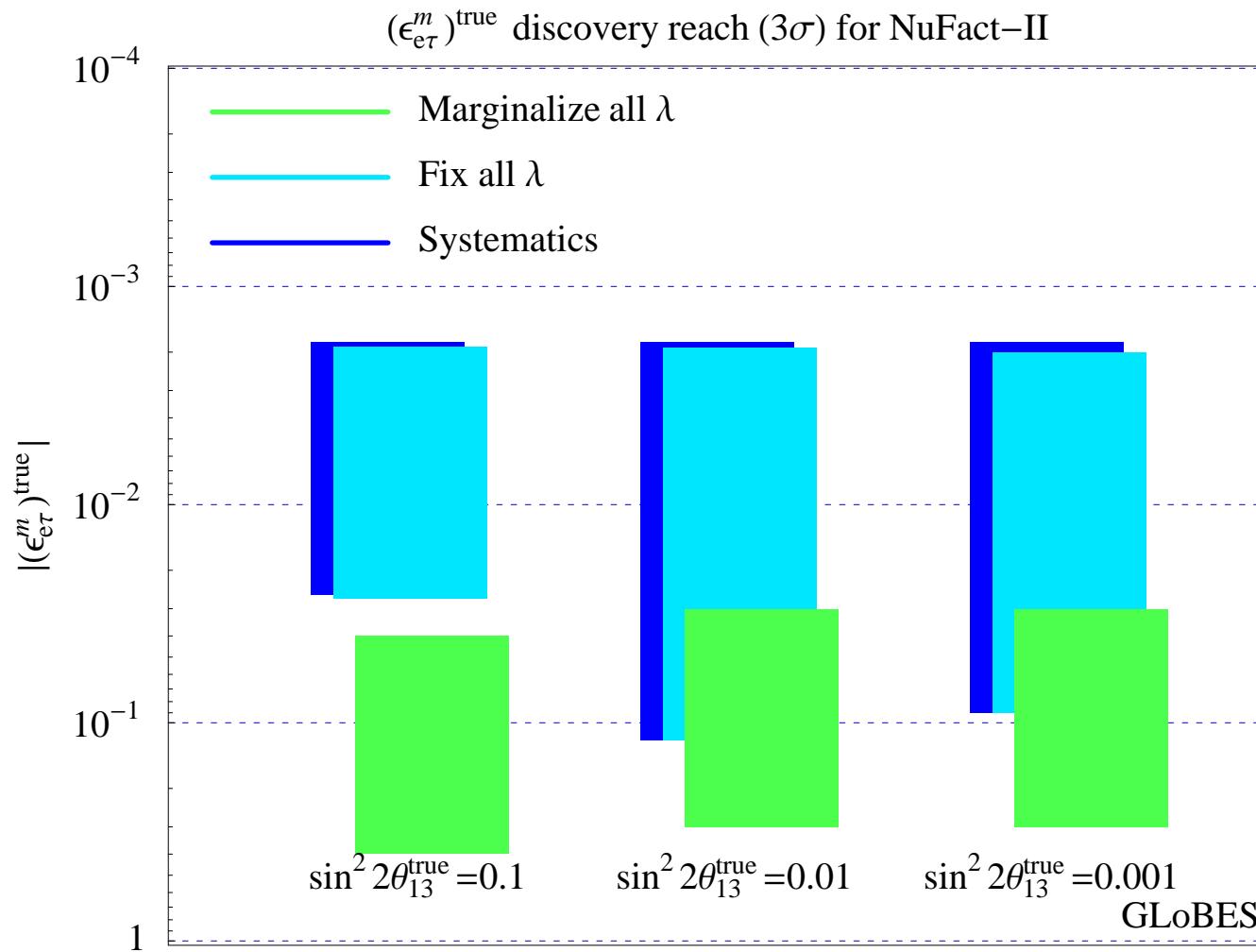
Discovery reach for NSIs in neutrino factory

- Similar plot for the discovery reach of $\epsilon_{e\mu}^s$



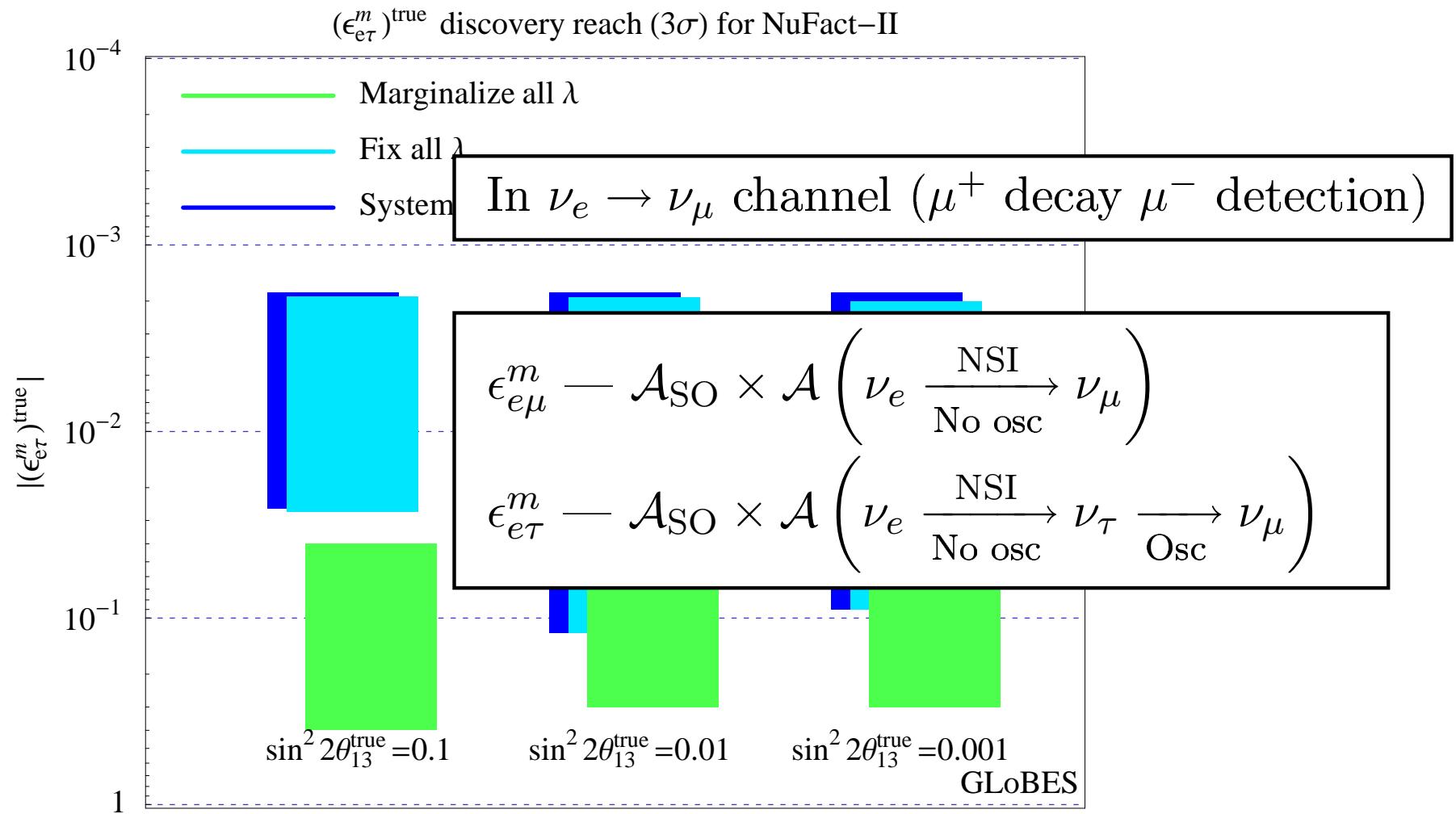
Discovery reach for NSIs in neutrino factory

- Similar plot for the discovery reach of $\epsilon_{e\tau}^m$



Discovery reach for NSIs in neutrino factory

- Similar plot for the discovery reach of $\epsilon_{e\tau}^m$



Implementation of NSIs to GLoBES

- For NSIs in matter effect, e.g., $\epsilon_{e\mu}^m$,

$$H_{\alpha\beta} = H_{\text{SO}} + H_{\text{NSI}}, \quad \begin{cases} 2E(H_{\text{SO}})_{\alpha\beta} = U_{\alpha i} \begin{pmatrix} 0 & & \\ & \Delta m_{21}^2 & \\ & & \Delta m_{31}^2 \end{pmatrix} U_{i\beta}^\dagger + \begin{pmatrix} a_{\text{CC}} & & \\ & 0 & \\ & & 0 \end{pmatrix}, \\ 2E(H_{\text{NSI}})_{\alpha\beta} = \begin{pmatrix} 0 & a_{\text{CC}}|\epsilon_{e\mu}^m|e^{i\arg[\epsilon_{e\mu}^m]} & \\ a_{\text{CC}}|\epsilon_{e\mu}^m|e^{-i\arg[\epsilon_{e\mu}^m]} & 0 & \\ & & 0 \end{pmatrix}. \end{cases}$$

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```
static int ComputeMixingMatrix()
{
    ...
    md[0][0] += msw;

    // two extra-parameters: //
    // abs(epsilon) = nsparams[0], arg(epsilon)=nsparams[1] //

    md[0][1] += msw * nsparams[0] * exp(complex<FLOAT>(0,1) * nsparams[1]);
    md[1][0] += msw * nsparams[0] * exp(complex<FLOAT>(0,-1) * nsparams[1]);
    ...
}
```

Implementation of NSIs to GLoBES

- For NSIs at the source and detection, e.g., $\epsilon_{e\mu}^s$,
 - The initial source state is a mixture of the flavour state

$$|\nu_e^{(s)}\rangle = |\nu_e\rangle + |\nu_\mu\rangle \epsilon_{e\mu}^s.$$

- The oscillation probability for $\nu_e^{(s)} \rightarrow \nu_\beta$ is calculated to be

$$\begin{aligned} P_{\nu_e^s \rightarrow \nu_\beta} &= \left| \langle \nu_\beta | e^{-iH L} | \nu_e^{(s)} \rangle \right|^2 = \left| S_{\beta e} + \epsilon_{e\mu}^s S_{\beta\mu} \right|^2 \\ &= \left| \left\{ \begin{pmatrix} S_{ee} & S_{e\mu} & S_{e\tau} \\ S_{\mu e} & S_{\mu\mu} & S_{\mu\tau} \\ S_{\tau e} & S_{\tau\mu} & S_{\tau\tau} \end{pmatrix} \begin{pmatrix} 1 \\ |\epsilon_{e\mu}^s| e^{i \arg[\epsilon_{e\mu}^s]} & 1 \\ 1 \end{pmatrix} \right\}_{\beta e} \right|^2, \end{aligned}$$

where $S_{\beta\alpha}$ is the standard oscillation amplitudes, i.e.,

$$S_{\beta\alpha} = \langle \nu_\beta | e^{-iH L} | \nu_\alpha \rangle.$$

Implementation of NSIs to GLoBES

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$$P_{\nu_\alpha^s \rightarrow \nu_\beta} = \left| \left\{ \begin{pmatrix} S_{ee} & S_{e\mu} & S_{e\tau} \\ S_{\mu e} & S_{\mu\mu} & S_{\mu\tau} \\ S_{\tau e} & S_{\tau\mu} & S_{\tau\tau} \end{pmatrix} \begin{pmatrix} 1 \\ |\epsilon_{e\mu}^s| e^{i \arg[\epsilon_{e\mu}^s]} & 1 \\ 1 \end{pmatrix} \right\}_{\beta\alpha} \right|^2$$

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```
extern "C" void glb_probability_matrix(FLOAT prob[3][3], int panti, double pen)
{
    ...
    for (int i=0; i<3; i++){
        for (int j=0; j<3; j++){
            amp[i][j] = complex<FLOAT>(0,0);
        }
    }
    for (int i=0; i<3; i++){
        amp[i][i]=complex<FLOAT>(1,0);
    }
    amp[1][0]= nsparams[0] * exp(complex<FLOAT>(0,1) * nsparams[1]);
    ...
    for (int i=0; i<psteps; i++)
        MultiplyAmplitudeMatrix(amp,panti,length[i],pen,density[i]);
    ...
}
```

Summary

Summary

- We have studied the discovery reach for the NSIs in a neutrino factory.
- The undetermined parameters $\delta_{\text{CP}}^{\text{true}}$ and $\arg[\epsilon^{\text{true}}]$ are scanned.

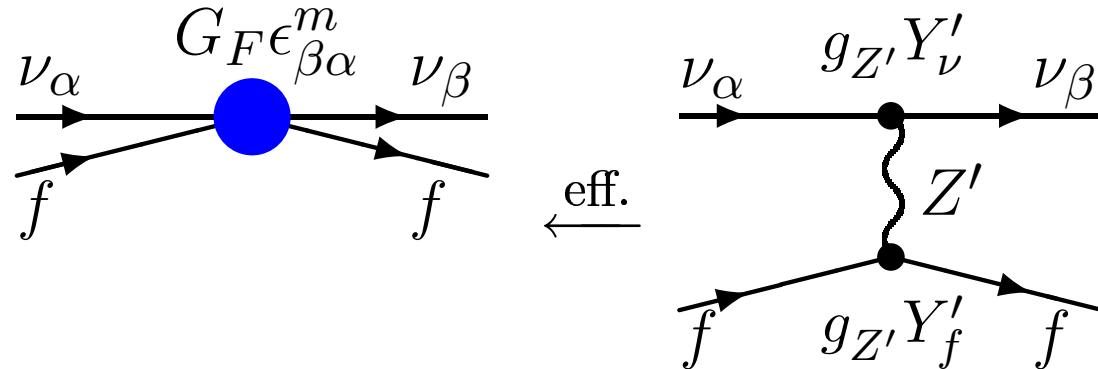
For $\epsilon_{e\mu}^m$, when $\sin^2 2\theta_{13}^{\text{true}} = 0.01$

- With $|\epsilon_{e\mu}^m| \geq 5 \times 10^{-4}$,
we have a chance to discover the effect at the 3σ level,
depending on the phases.
- If $|\epsilon_{e\mu}^m| \geq 5 \times 10^{-3}$,
it can be found in the ν factory regardless of the phases.

- Current bound from $\mu \rightarrow 3e$ is 5×10^{-4} at the 90% CL.
 - Comparable, depending on the phases

Summary

- The discovery reach for $\epsilon_{e\tau}^m$ and $\epsilon_{e\mu}^s$ has also studied.
 - $|\epsilon_{e\mu}^s| \sim \mathcal{O}(10^{-3}, -4)$, $|\epsilon_{e\tau}^m| \sim \mathcal{O}(10^{-1}, -2)$.
- The effective four-Fermi NSIs with $\epsilon \sim \mathcal{O}(10^{-2})$ may mean the TeV scale physics, i.e.,



- If $g_{Z'}$ is the same as g_Z , $\epsilon_{\beta\alpha}^m = m_Z^2/m_{Z'}^2$.

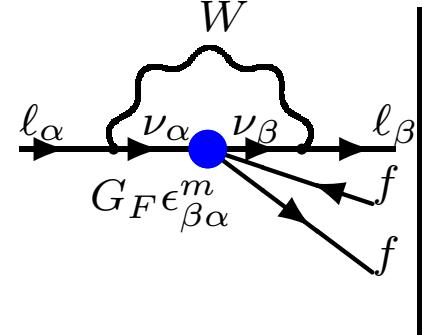
-
- NSIs are not good signals for MSSM
 - They are strongly suppressed
 - NSIs may be the signals for something else than MSSM

Discussion: NSIs in models

References : T. O and J. Sato, Phys. Rev. **D71** (2005) 096004.

NSIs in models

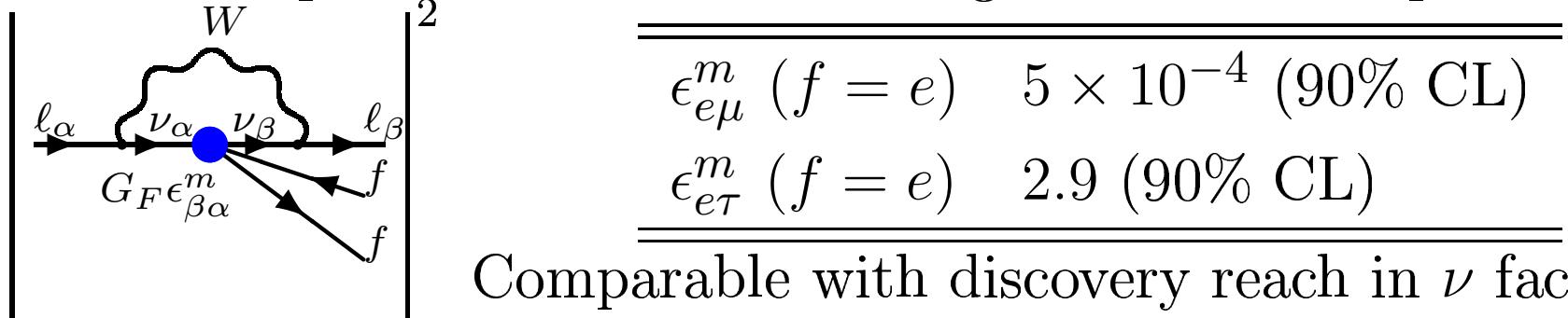
- We dealt with NSIs as effective 4-Fermi interactions so far.
- Current experimental bounds coming from the LFV process

	$G_F \epsilon_{\beta\alpha}^m$	$\left \frac{\epsilon_{\beta\alpha}^m}{G_F} \right ^2$	$\epsilon_{e\mu}^m (f = e)$	5×10^{-4} (90% CL)
			$\epsilon_{e\tau}^m (f = e)$	2.9 (90% CL)

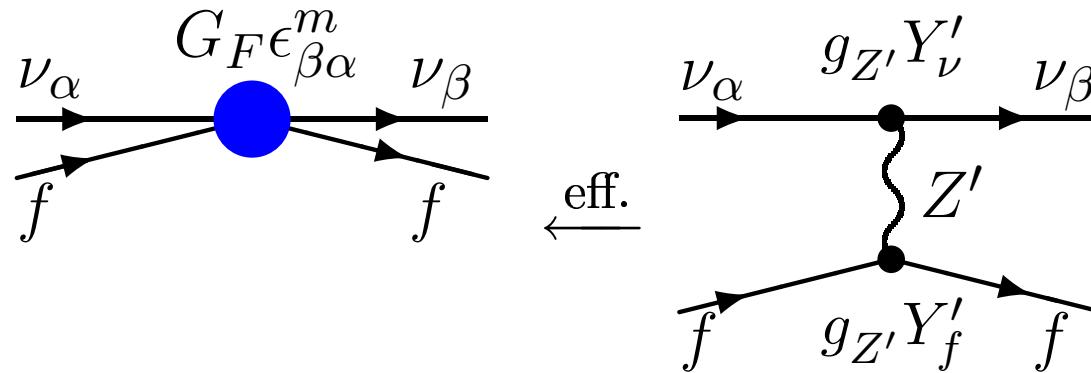
Comparable with discovery reach in ν fact.

NSIs in models

- We dealt with NSIs as effective 4-Fermi interactions so far.
- Current experimental bounds coming from the LFV process



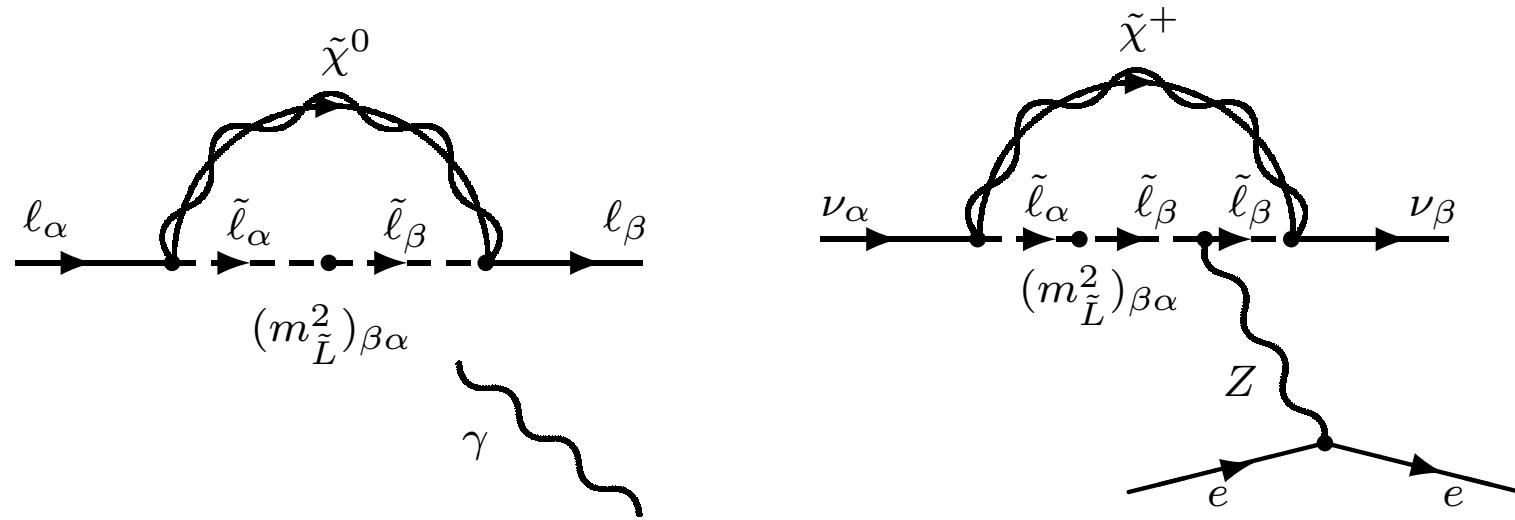
- These eff. int.s can be interpreted as *extra weak interactions*



- If $g_{Z'}$ are the same as those of weak interaction, $\epsilon_{\beta\alpha}^m = m_Z^2/m_{Z'}^2$
- $\epsilon_{\alpha\beta}^m \sim \mathcal{O}(10^{-2})$ means *access to the TeV scale physics*

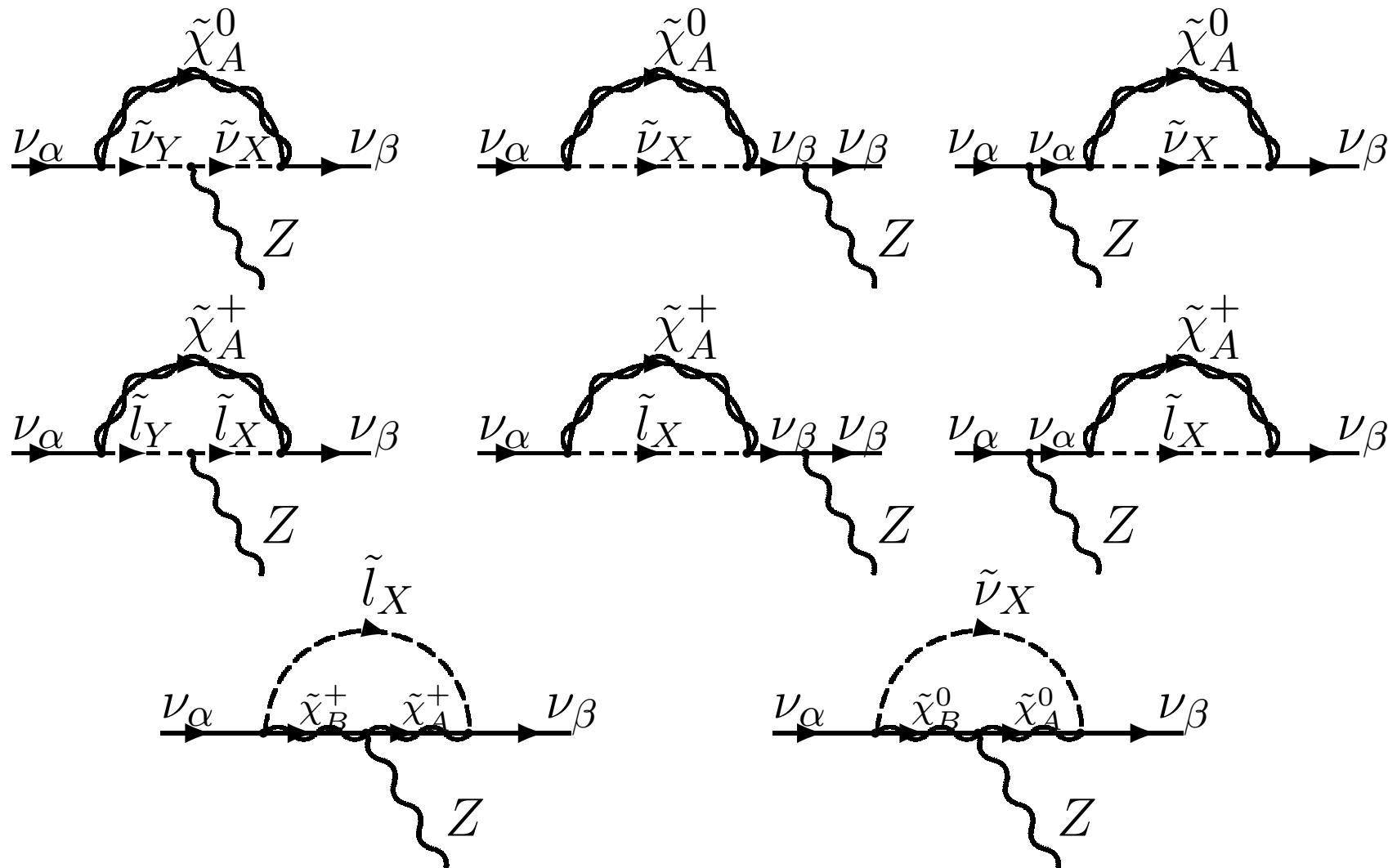
NSIs in models — MSSM with ν_R

- In the MSSM, NSIs and $\ell_\beta \rightarrow \ell_\alpha \gamma$ are provided by similar one-loop diagrams with slepton mixings — they are correlated.



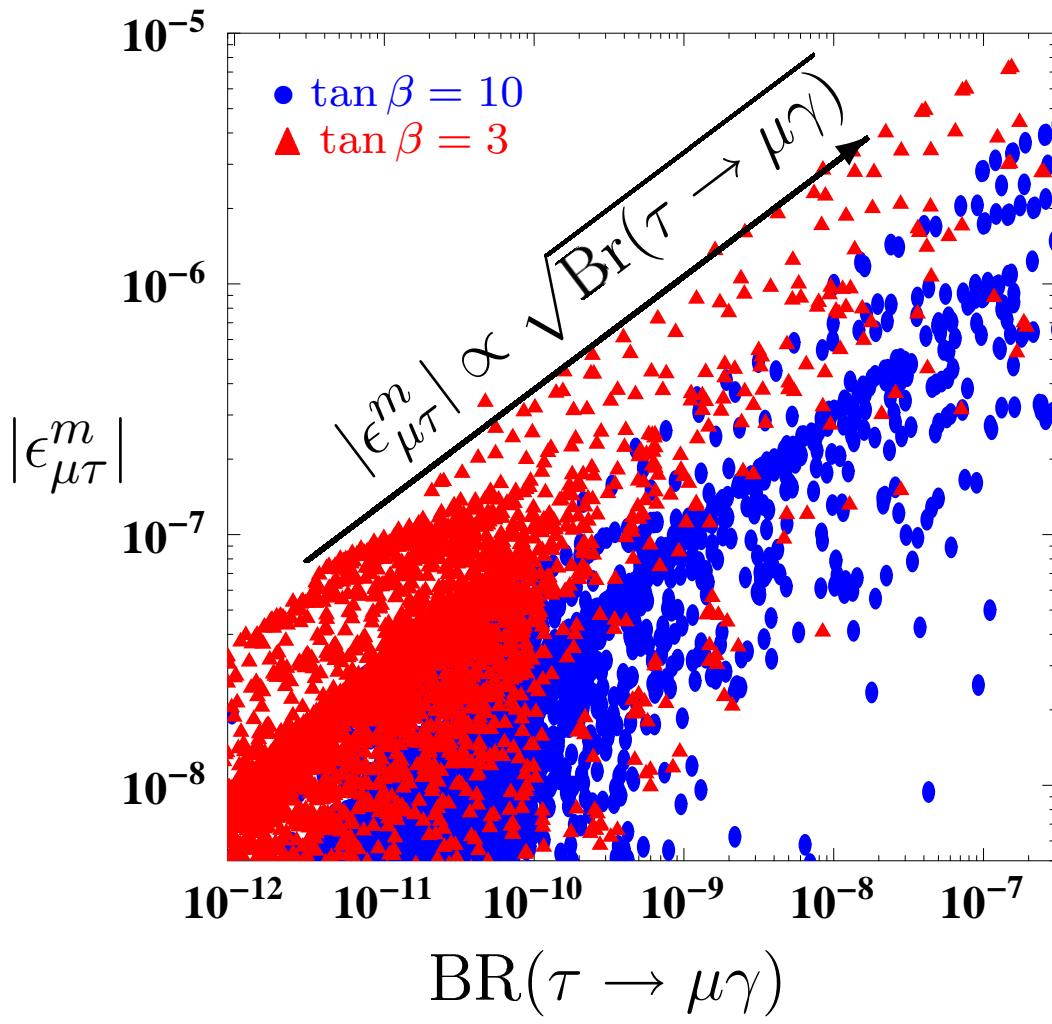
- Large slepton mixings are expected to be induced by the RGE effect associated with the neutrino Yukawa couplings.
- $\epsilon_{e\mu}^{s,m}$ is strongly suppressed, at least $\sqrt{\text{Br}(\mu \rightarrow e\gamma)} = \mathcal{O}(10^{-5})$
- How about $\epsilon_{e\tau}^m$, $\epsilon_{\mu\tau}^m$?

NSIs in models — MSSM with ν_R



and box diagrams ...

NSIs in models — MSSM with ν_R



- Correlation between the NSI coupling $\epsilon_{\mu\tau}^m$ and LFV process $\tau \rightarrow \mu\gamma$.
 - With some different Y_ν s, we scan the m_0 - $M_{1/2}$ space with $a_0 = 0$, $\tan \beta = 3, 10$, and $\mu > 0$.
- The parameter $\epsilon_{\mu\tau}^m$ is constrained at $\mathcal{O}(10^{-6})$ by the current bound of $\tau \rightarrow \mu\gamma$.
- It is smaller than the naive estimation because of cancellation among diagrams.