

# Leptonic CP violation in the minimal type-I seesaw model

Bottom-up phenomenology & top-down model-building

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IMPRS-Seminar

based on

TR & K.Schmitz - arXiv:1611.05857[hep-ph], JHEP 1703 (2017) 158

TR, K.Schmitz, T.Yanagida - arXiv:1612.08878[hep-ph]

Massive neutrinos

Bottom up: Yukawa hierarchies from measured CP violation

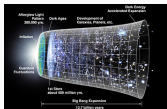
Top down: Minimal seesaw with approximate discrete symmetry

## Massive neutrinos

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# Neutrinos everywhere!

One of the most abundant particles in the universe!



[NASA]

$$T_{C\nu B} \sim 1.95 \text{ K}$$



[NASA]

$$\Phi_{\oplus} \sim 6.5 \times 10^{10} \frac{\nu_e}{\text{cm}^2 \text{ s}}$$



[spacetelescope.org]

$$\Delta E_G \sim 99\% \nu's$$



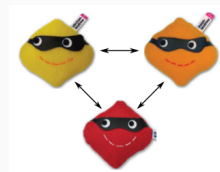
[nuclear-energy.net]

$$P \sim 200 \frac{\text{kW}}{\text{m}^2}$$

In the standard model:

- neutral electric charge  $\rightarrow$  W. Pauli 1930
- weakly interacting  $\rightarrow$  discoveries - (1952, 1962, 2000)
- $SU(2)_L$  partners of charged leptons  $\rightarrow$  Wu & Goldhaber

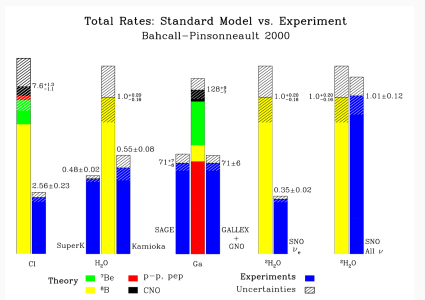
NO RH neutrinos  $\rightarrow$  **massless!**



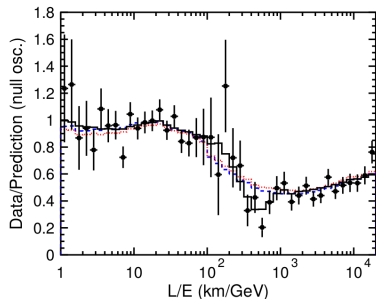
[<https://www.particlezoo.net>]

# Why do we need massive neutrinos?

→ Neutrino flux deficits!



[de Gouvea, 2004]



[Ishitsuka, 2004]

- finite lifetime
  - stronger absorption in matter
  - $B$  field induced  $\nu_L \rightarrow \bar{\nu}_L, \nu_R$
  - exotica (~~equivalence principle,  $\mathcal{U}, \mathcal{M}_L$~~ )
  - flavor conversion during propagation  
→ oscillations
- ⇒ flavor oscillations only convincing explanation, but **non-zero**  $\Delta m$  required!

# Neutrino oscillations

[particlezoo.net]



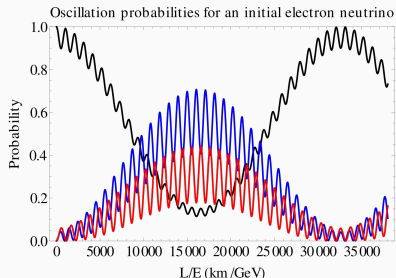
- mismatch between flavor and mass eigenstates:  $|\nu_\alpha\rangle \neq |\nu_i\rangle$
- neutrino mixing incorporated in PMNS matrix:  $|\nu_\alpha\rangle = U_{\alpha i}^* |\nu_i\rangle$

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}c_{13}s_{23}e^{i\delta} & c_{12}c_{23} - s_{12}s_{13}s_{23}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}s_{13}c_{23}e^{i\delta} & -c_{12}s_{23} - s_{12}s_{13}c_{23}e^{i\delta} & c_{13}c_{23} \end{pmatrix} \times \text{diag} (1, e^{i\sigma}, e^{i\tau})$$

with  $s_{ij} \equiv \sin \theta_{ij}, c_{ij} \equiv \cos \theta_{ij}, \theta_{ij} \in [0, \frac{\pi}{2}]$  and  $\delta \in [0, 2\pi), \sigma, \tau \in [0, \pi)$

- transition probability

$$\begin{aligned} \mathcal{P}(\nu_\alpha \rightarrow \nu_\beta; t) &= \langle \nu_\beta | \nu_\alpha(t) \rangle | = U_{\beta j} U_{\alpha j}^* e^{-iE_j t} |^2 \\ &\simeq \sin^2 2\theta \sin^2 \left( 1.27 \Delta m^2 \frac{L[\text{m}]}{E[\text{MeV}]} \right) \end{aligned}$$



black -  $\nu_e$ , blue -  $\nu_\mu$ , red -  $\nu_\tau$

[wikipedia.org]

# Leptonic CP violation

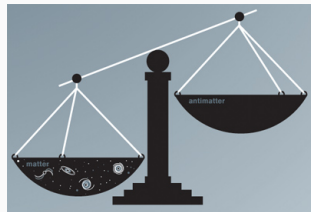
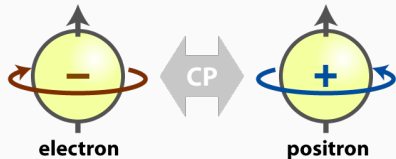
- Dirac phase  $\delta$  through oscillations

$$\Delta\mathcal{P} = \mathcal{P}(\nu_\alpha \rightarrow \nu_\beta; t) - \mathcal{P}(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta; t) \propto \sin \delta$$

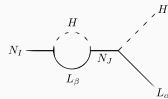
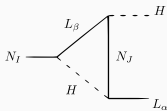
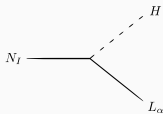
- Majorana phases through  $0\nu\beta\beta$

$$m_{ee}^2 = \left| \sum_i U_{ei}^2 m_i \right|$$

- high-E CP violation  $\epsilon \rightarrow$  Leptogenesis!



[quantumdiaries.org]



# Current experimental status

What we know:

- two non-zero mass-squared differences

$$\Delta m_{sol}^2 \simeq 7.4 \cdot 10^{-5} \text{eV}^2$$

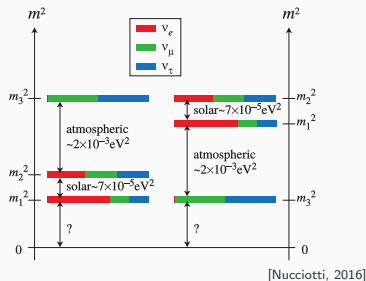
$$\Delta |m_{atm}^2| \simeq 2.5 \cdot 10^{-3} \text{eV}^2$$

- two large and one small mixing angle

$$\theta_{12} = \theta_{sol} \sim (31 \dots 36)^\circ$$

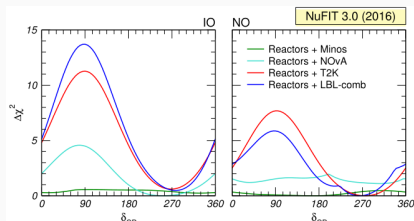
$$\theta_{23} = \theta_{atm} \sim (38 \dots 53)^\circ$$

$$\theta_{13} = \theta_{reac} \sim (8 \dots 9)^\circ$$



Still open questions:

- mass hierarchy - normal or inverted?
- absolute mass scale  $\min\{m_i\} = ?$
- fermion type - Dirac/Majorana
- octant-problem:  $45^\circ (< \text{or } >) \theta_{23}$
- non-zero CP violating phases -  $\delta, \sigma, \tau$





# Neutrino mass models

- natural emergence of neutrino masses in many BSM theories: GUTs, Left-Right-symmetry, etc.
- rich phenomenology:  $\mathcal{L}$ , BAU, etc.
- models strongly depend on neutrino's fermionic nature!

## Majorana neutrino: $\nu = \nu^c$

- seesaw models
- radiative mass generation

## Dirac neutrino: $\nu \neq \nu^c$

- Dirac seesaw + radiative mass generation
- extra dimensions

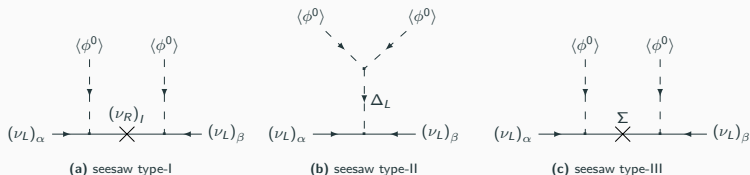
Most popular approach: realizations of eff. dim-5 operator [Weinberg, 1979]

$$\mathcal{L}_5 = \frac{1}{2} \frac{g}{\Lambda} \left( \bar{L}_L \tilde{\phi} \right) \left( \phi^* L_L^c \right)$$

$$\rightarrow \Delta L = 2$$



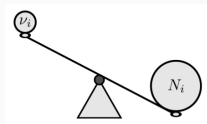
Tree level realization of Weinberg operator:



**Generic feature:** SM neutrino mass is suppressed by mass scale of intermediate particle/new physics scale  $m_\nu \propto \Lambda^{-1}$

simplest: type-I scenario - 3 heavy RH Majorana neutrino  $\rightarrow$  18 real parameters!

$$m_\nu \simeq -m_D M_R^{-1} m_D^T$$



# Minimal type-I seesaw model

Predictions demand reduction of parameter space:

$$\mathcal{L}_{\text{seesaw}} = -y_{\alpha I} L_{\alpha} \phi N_I - \frac{1}{2} N_I N_I + \text{h.c.}, \quad \alpha = e, \mu, \tau \quad I = 1, 2$$

[King, 1998, King, 1999, King, 2000, Frampton et al., 2002]

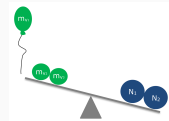
- only two  $N_I$ 's:
  - three complex Yukawa couplings
  - one Majorana mass  $M_I$

→ 11 real parameters, but one  $\nu$  exactly massless!
- zero-texture ansatz (flavor symmetry, xDim, ...)
  - one zero - trivial
  - three zeros - inconsistent with data

→ **two-zero textures**: only  $B_{1,4}$  and  $B_{2,5}$  for IH are allowed, NH completely forbidden!

Precise predictions for CP phases → **maximal CP violation!**

$$\frac{(\delta, \sigma)}{\pi} \simeq \begin{cases} (0.51, 0.94) & \text{or} & (1.49, 0.06) & (B_{1,4}) \\ (0.50, 0.04) & \text{or} & (1.50, 0.96) & (B_{2,5}) \end{cases}$$



$$\begin{aligned} A_1 &: \begin{pmatrix} 0 & 0 \\ \times & \times \\ \times & \times \end{pmatrix}, & A_2 &: \begin{pmatrix} \times & \times \\ 0 & 0 \\ \times & \times \end{pmatrix}, & A_3 &: \begin{pmatrix} \times & \times \\ \times & \times \\ 0 & 0 \end{pmatrix} \\ B_1 &: \begin{pmatrix} 0 & \times \\ \times & 0 \\ \times & \times \end{pmatrix}, & B_2 &: \begin{pmatrix} 0 & \times \\ \times & \times \\ \times & 0 \end{pmatrix}, & B_3 &: \begin{pmatrix} \times & \times \\ 0 & \times \\ \times & 0 \end{pmatrix} \\ B_4 &: \begin{pmatrix} \times & 0 \\ 0 & \times \\ \times & \times \end{pmatrix}, & B_5 &: \begin{pmatrix} \times & 0 \\ \times & \times \\ 0 & \times \end{pmatrix}, & B_6 &: \begin{pmatrix} \times & \times \\ \times & 0 \\ 0 & \times \end{pmatrix} \\ C_1 &: \begin{pmatrix} 0 & \times \\ 0 & \times \\ \times & \times \end{pmatrix}, & C_2 &: \begin{pmatrix} 0 & \times \\ \times & \times \\ 0 & \times \end{pmatrix}, & C_3 &: \begin{pmatrix} \times & \times \\ 0 & \times \\ 0 & \times \end{pmatrix} \\ C_4 &: \begin{pmatrix} \times & 0 \\ \times & 0 \\ \times & \times \end{pmatrix}, & C_5 &: \begin{pmatrix} \times & 0 \\ \times & \times \\ \times & 0 \end{pmatrix}, & C_6 &: \begin{pmatrix} \times & \times \\ \times & 0 \\ \times & 0 \end{pmatrix} \end{aligned}$$

**Bottom up: Yukawa hierarchies from  
measured CP violation**

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## Driving questions:

1. What can we learn about high-energy sector if CP violation is measured? → DUNE 2020's
2. Compatibility of (broken) flavor symmetry with data? → theoretical errors to exact zero-textures
3. Stability against experimental uncertainties?

→ data-driven, "bottom-up" approach to theoretical top-down approaches!

# Motivation & Framework

## Driving questions:

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→ data-driven, "bottom-up" approach to theoretical top-down approaches!

## Framework:

- rescale Yukawa and PMNS matrix:  $\kappa_{\alpha l} = \sqrt{\frac{v_{EW}}{M_l}} y_{\alpha l}$ ,  $V_{\alpha i} = i \sqrt{\frac{m_i}{v_{EW}}} U_{\alpha i}^*$
- minimal set of DOFs:

### 9 free parameters at low energies:

- + 6 complex Yukawa coupling  $y_{\alpha l}$
- + 2 Majorana phases  $M_l$ ,  $l = 1, 2$
- 3 charged-lepton phases
- 2 rescaling,  $M/y^2 = \text{const.}$

### 7 observables at low energies:

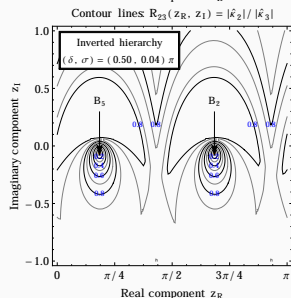
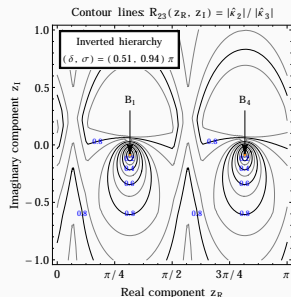
- 2 mass-squared differences  $\Delta m_{atm}^2, \Delta m_{sol}^2$
- 3 mixing angles,  $\theta_{atm}, \theta_{reactor}, \theta_{sol}$
- 1 Dirac CP phase  $\delta$
- 1 Majorana phase  $\sigma$

- Casas-Ibarra parametrization [Casas and Ibarra, 2001] → captures excess DOFs

$$\kappa_{\alpha 1} = \frac{1}{\sqrt{2}} \left( V_{\alpha}^+ e^{-iz} + V_{\alpha}^- e^{+iz} \right) \quad \kappa_{\alpha 2} = \frac{i}{\sqrt{2}} \left( V_{\alpha}^- e^{+iz} - V_{\alpha}^+ e^{-iz} \right), \quad V_{\alpha}^{\pm} = \frac{1}{\sqrt{2}} (V_{\alpha k} \pm iV_{\alpha l})$$

## Accessing hierarchies within Yukawa matrices:

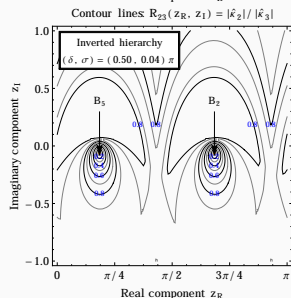
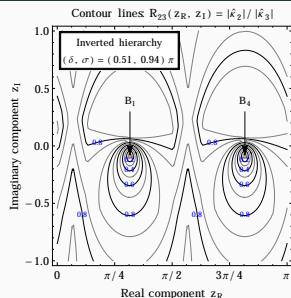
- for each  $(\delta, \sigma)$ : two DOFs - real and imaginary part of complex rotation angle,  $z_R$  and  $z_I$   
 $\rightarrow$  label for all possible Yukawa matrices  $y_{\alpha I}$



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- @ each point of the complex  $z$  plane: sort Yukawa according to their abs. values  
 $\hat{\kappa}_{\alpha I} \rightarrow \hat{\kappa} = (\hat{\kappa}_1, \hat{\kappa}_2, \hat{\kappa}_3, \hat{\kappa}_4, \hat{\kappa}_5, \hat{\kappa}_6)$
- **Hierarchy parameter  $R_{23} \equiv \frac{|\hat{\kappa}_2|}{|\hat{\kappa}_3|}$** 
  - $R_{23} = 0 \rightarrow$  exact two-zero texture
  - $0 < R_{23} \ll 1 \rightarrow$  approximate texture
- Minimization of auxiliary parameter  $z$ :

$$H_{23} = \min_z R_{23}$$



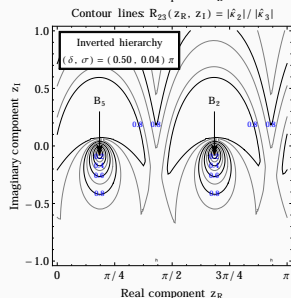
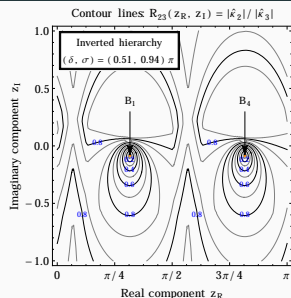


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$\min_z \equiv$  scan over all UV flavor models of the minimal type-I seesaw model  
 $\rightarrow$  upper hierarchy bounds  $H_{23}(\delta, \sigma)$ !



$R_{23}$  has useful properties:

- probe actual Yukawa coupling if RH masses are degenerate or at least of some order of magnitude; otherwise simple rescaling

$$R_{23}(\delta, \sigma; z) = \frac{|\hat{\kappa}_2|}{|\hat{\kappa}_3|} = \left( \frac{\hat{M}_3}{\hat{M}_2} \right)^{\frac{1}{2}} \frac{|\hat{y}_2|}{|\hat{y}_3|} \approx \frac{|\hat{y}_2|}{|\hat{y}_3|}$$

- periodic behavior:

$$R_{23}(\delta, \sigma; z) = R_{23}\left(\delta, \sigma; z + n\frac{\pi}{2}\right), \quad n \in \mathbb{Z}$$

$$\implies z \rightarrow z + \frac{\pi}{2} : \kappa_{\alpha 1} \rightarrow \kappa_{\alpha 1}, \kappa_{\alpha 2} \rightarrow -\kappa_{\alpha 1}$$

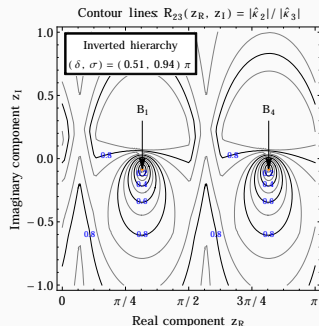
- reflection symmetry:

$$R_{23}(2\pi - \delta, \sigma; z) = R_{23}(\delta, \pi - \sigma; z)^*$$

invariance under  $\delta \rightarrow -\delta, \sigma \rightarrow -\sigma, z \rightarrow z^*$

- independence of  $z$  in flavor-aligned limit:

$$z_l \rightarrow \pm\infty \implies R_{23} \rightarrow R_{23}^{\pm} = \left| \frac{V_{\alpha 1 k} \pm iV_{\alpha 1 l}}{V_{\alpha 2 k} \pm iV_{\alpha 2 l}} \right|$$



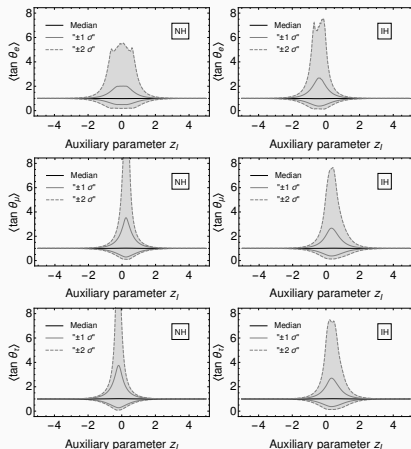
## Observation:

- for large  $Z_I$ :  $\kappa_{\alpha 1} \simeq \kappa_{\alpha 2}$
- special configuration in flavor space, inconsistent with data
- systematic study of transition to alignment  
[TR, K.Schmitz, T.Yanagida, 2016]

$$y_{\alpha I} = \begin{pmatrix} \epsilon \cos \theta_e e^{i\phi_e} & \epsilon \sin \theta_e e^{i(\phi_e + \Delta\phi_e)} \\ \cos \theta_\mu e^{i\phi_\mu} & \sin \theta_\mu e^{i(\phi_\mu + \Delta\phi_\mu)} \\ c_{\mu\tau} \cos \theta_\tau e^{i\phi_\tau} & c_{\mu\tau} \sin \theta_\tau e^{i(\phi_\tau + \Delta\phi_\tau)} \end{pmatrix} y_0$$

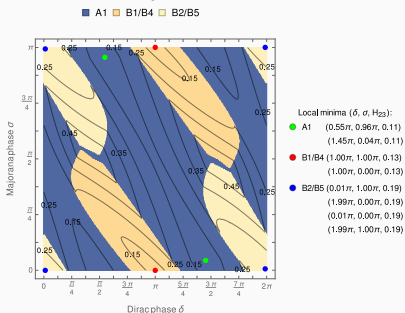
→ **flavor alignment** for  $|z_I| \gg 1$ !

- separated study of aligned and un-aligned parameter space regions  
[TR, K.Schmitz, 2016]

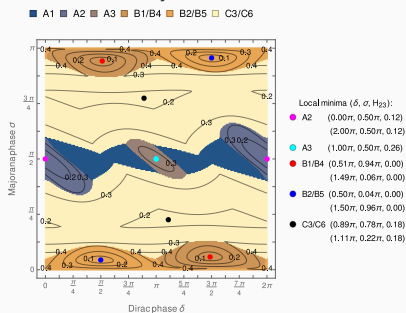


## Minimized hierarchy parameter $H_{23}$ :

### Normal hierarchy



### Inverted hierarchy



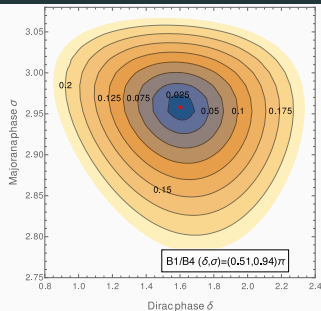
- Exact zero-textures are recovered:  $B_{1,4}$  and  $B_{2,5}$
- Maximal hierarchies for different flavor texture
- New approximate solution for NH and IH!

→ NH  $A_1$  predicts max. CP violation with  $\delta \sim 270^\circ \Rightarrow$  UV origin?

# Theoretical error bars and robustness study

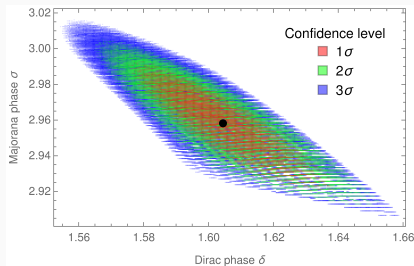
## Perturbations around exact predictions:

- exact textures may receive correction by loops, gravity, etc.
- quantifications of maximally allowed perturbations
- complementary to experimental uncertainties owing to experimental error bars



## Stability against experimental uncertainties:

- naive  $\chi^2$  analysis as first estimate
- **negligible** shifts of CP phases if best-fit values vary

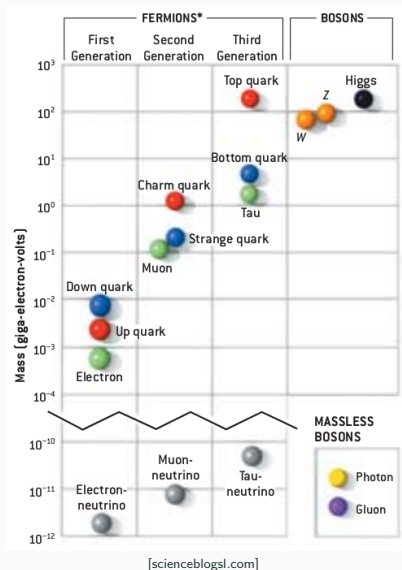


## **Top down: Minimal seesaw with approximate discrete symmetry**

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# Generation of Yukawa textures

Flavor physics provide useful tools!



- Radiative generation [Georgi and Glashow, 1972]
- Extra dimensions [Grossman and Neubert, 2000]
- Compositeness [Kaplan, 1991]
- Froggatt-Nielsen [Froggatt and Nielsen, 1979]

Aim:

Yukawa matrix with A1 texture yielding

NH at  $\delta \simeq \frac{\pi}{2}, \frac{3\pi}{2}$

$$\kappa_{\alpha l} \sim \begin{pmatrix} 0.1 & 0.1 \\ 1 & 1 \\ 1 & 1 \end{pmatrix}$$

→  $SU(5)$  Froggatt-Nielsen mechanism [Buchmuller and Yanagida, 1999]

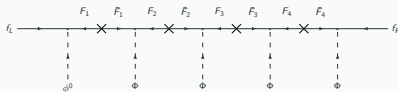
# Froggatt-Nielsen mechanism [Froggatt and Nielsen, 1979]

Dynamical generation of Yukawa coupling through a globally/locally conserved charge  $Q_{FN}$ !

0. Generate heavy fermion masses at  $\Lambda_{FN}$
1. Introduce "spaghetti" interactions at high scale through flavon fields  $\Phi$  (charge assignment according to chain length)

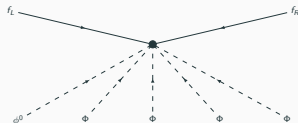
$$\mathcal{L} \supset b_{ij} \Phi f_i F_j + c_{ij} \Phi F_i F_j + d_{ij} \phi f_i F_j + M_{ij} F_i F_j + \text{h.c.}$$

$$M_{ij} = a_{ij} \Lambda_{FN}, a_{ij} \sim \mathcal{O}(1)$$



2. Integrate out heavy fields  $F_i$

$$\mathcal{L}_{\text{eff}} \supset e_{ij} \left( \frac{\Phi}{\Lambda_{FN}} \right)^{\Delta Q_{FN}} f_i f_j \phi$$



3. SSB of FN symmetry  $\Phi \rightarrow \langle \Phi \rangle$

$$\mathcal{L}_{\text{eff}} \supset e_{ij} \epsilon^{\Delta Q_{FN}} f_i f_j \phi, \epsilon \equiv \left( \frac{\langle \Phi \rangle}{\Lambda_{FN}} \right)$$





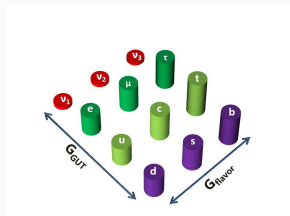
# $SU(5) \times U(1)_5$ GUT [Georgi and Glashow, 1972], etc.

- "smallest" group containing the SM gauge group

$$SU(5) \xrightarrow{m_X} SU(3)_C \times SU(2)_L \times U(1)_Y$$

$$\xrightarrow{m_{W,Z}} SU(3)_C \times U(1)_Q$$

- unify one generation in a  $(\bar{5} + 10)$ -representation
- additional  $U(1)$  requires RH singlets for anomaly cancellation  $\psi_1 \simeq N \rightarrow S_1$  to break  $U(1)$
- nice features, but common problems (proton decay, etc.)  
 $\rightarrow SO(10) \subset SU(5) \times U(1)$



[<http://theophys.kth.se/tepp/>]

$$H_5 = (h_1, h_2, h_3, h^+, -h^0)^T = (3, 1) + (1, 2)$$

$$\psi_5 = (d_1, d_2, d_3, e^c, \nu^c)^T_R = (3, 1) + (1, 2)$$

$$X_{10} = \begin{pmatrix} 0 & u_3^c & -u_2^c & -u_1 & -d_1 \\ -u_3^c & 0 & u_1^c & -u_2 & -d_2 \\ u_2^c & -u_1^c & 0 & -u_3 & -d_3 \\ u_1 & u_2 & u_3 & 0 & -e^+ \\ d_1 & d_2 & d_3 & e^+ & 0 \end{pmatrix}_L$$

$$= (3, 2) + (\bar{3}, 1) + (1, 1)$$

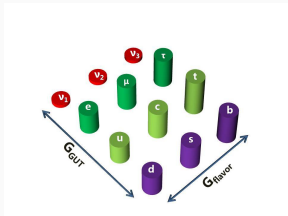
# $SU(5) \times U(1)_5$ GUT [Georgi and Glashow, 1972], etc.

- "smallest" group containing the SM gauge group

$$SU(5) \xrightarrow{m_X} SU(3)_C \times SU(2)_L \times U(1)_Y$$

$$\xrightarrow{m_{W,Z}} SU(3)_C \times U(1)_Q$$

- unify one generation in a  $(\bar{5} + 10)$ -representation
- additional  $U(1)$  requires RH singlets for anomaly cancellation  $\psi_1 \simeq N \rightarrow S_1$  to break  $U(1)$
- nice features, but common problems (proton decay, etc.)  $\rightarrow SO(10) \subset SU(5) \times U(1)$



[<http://theophys.kth.se/tepp/>]

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$$= (3, 2) + (\bar{3}, 1) + (1, 1)$$

$SU(5)$  Froggatt-Nielsen mechanism  $\rightarrow$  one generation has same FN charge!

$$\mathcal{L}_{Yuk}^5 = h_{ij}^u \epsilon^{\Delta Q} (X_{10})_i (X_{10})_j H_5 + h_{ij}^d \epsilon^{\Delta Q} (\psi_5)_i^* (X_{10})_j H_5^*$$

$$+ h_{ij}^\nu \epsilon^{\Delta Q} (\psi_5)_i^* (\psi_1)_j H_5 + h_{ij}^s \epsilon^{\Delta Q} (\psi_1)_i (\psi_1)_j S_1$$

# Modified Buchmuller-Yanagida-model

- Parametrize SM mass pattern  
 → for  $\epsilon_0 \simeq 0.17$  SM mass pattern is recovered!

$$m_t : m_c : m_u \simeq 1 : \epsilon^2 : \epsilon^4$$

$$m_b : m_s : m_d \simeq m_\tau : m_\mu : m_e \simeq 1 : \epsilon : \epsilon^3$$

$SU(5)$ multiplet	$\mathbf{10}_1$	$\mathbf{10}_2$	$\mathbf{10}_3$	$\mathbf{5}_1^*$	$\mathbf{5}_2^*$	$\mathbf{5}_3^*$	$\mathbf{1}_1$	$\mathbf{1}_2$	$\mathbf{1}_3$	$\Phi$
Minimal seesaw embedding	2	1	0	2	1	1	$q$	$q$	\	-1

- heavy neutrino mass spectrum also generated via FN mechanism

$$m_R \sim \begin{pmatrix} \epsilon_0^{q_1} & 0 \\ 0 & \epsilon_0^{q_2} \end{pmatrix} m_0, \quad q_i = 2 Q_{FN}(N_i)$$

- resulting neutrino Yukawa couplings

$$y_{\alpha l} \sim \begin{pmatrix} \epsilon_0 & \epsilon_0 \\ 1 & 1 \\ 1 & 1 \end{pmatrix} y_0, \quad y_0 \equiv \epsilon_0^q$$

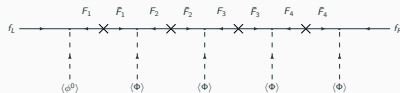
# Minimal seesaw model + discrete heavy-neutrino exchange symmetry

## Ingredients:

- Yukawa structures generated through Froggatt-Nielsen flavor symmetry at high energy

$$\mathcal{L}_{eff} \supset \left( \frac{\Phi}{\Lambda} \right)^{q_i+q_j} \psi_i \psi_j \phi$$

- Charge assignment inspired by  $SU(5)$  GUT
- Discrete exchange symmetry



$$[L_e] = 2, \quad [L_{\mu,\tau}] = 1, \quad [N_{1,2}] = q$$

$$\begin{aligned} \text{Yukawa interaction} & N_1 \leftrightarrow iN_2 \\ \text{mass term} & N_1 \leftrightarrow N_2 \end{aligned}$$

$$\mathcal{L}_{seesaw} \sim -y_0 (\epsilon l_e + l_\mu + c_{\mu\tau} l_\tau) (N_1 + iN_2) \phi - \frac{1}{2} M (N_1 N_1 + N_2 N_2)$$

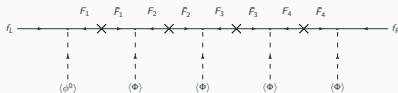
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## All desired properties are reproduced:

- minimal<sup>3</sup> model: only two N's, approx. two-zero texture, flavor alignment
- Casas-Ibarra parametrization: in flavor-aligned regions independence of  $z$
- Yukawa hierarchies fixed by FN model  $\rightarrow$  CP phase predictions

**Open questions:** Origin of discrete symmetry (orbifolds?)

# Generic set of parameters

Benchmark model:

$$\mathcal{L}_{\text{seesaw}} \sim -y_0 (\epsilon l_e + l_\mu + c_{\mu\tau} l_\tau) (N_1 + iN_2) \phi - \frac{1}{2} M (N_1 N_1 + N_2 N_2)$$

Assume "natural" hierarchies in Yukawa matrix:

- $SU(5)$  FN flavor model:

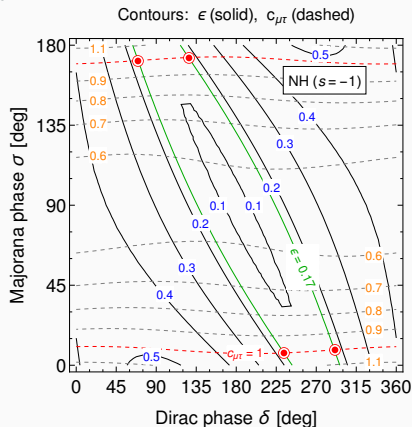
$$\epsilon \simeq 0.17 \rightarrow \frac{|y_e|}{|y_{\mu,\tau}|}$$

- equal muon and tauon Yukawa

$$\text{couplings: } c_{\mu,\tau} \simeq 1 \rightarrow \frac{|y_\mu|}{|y_\tau|}$$

→ NH with maximal CP violation!

$$(\delta, \sigma) \simeq \begin{cases} (234^\circ, 7^\circ) \\ (291^\circ, 9^\circ) \\ (69^\circ, 171^\circ) \\ (126^\circ, 173^\circ) \end{cases}$$



# Heavy neutrino mass scale & theoretical arguments

Absolute neutrino mass scale of the constructed model:  $M \simeq 4.6 \epsilon_0^{-2q} e^{2z_i} 10^{15} \text{ GeV}$

Application of further theoretical arguments:

- electroweak naturalness [t Hooft, 1980]

$$\delta\mu^2 \simeq \frac{M^3}{4\pi^2 v_{EW}^2} \cosh 2z_i \sum_i m_i$$

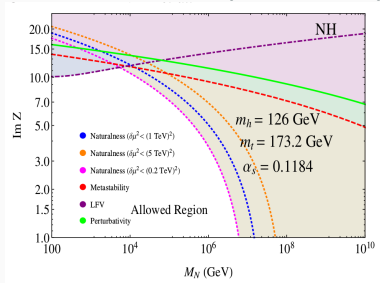
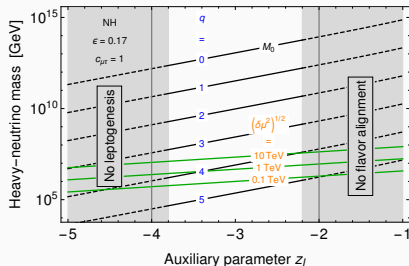
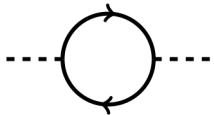
[Bambhaniya et al., 2016]

- successful (resonant) leptogenesis [Pilaftsis, 1997]

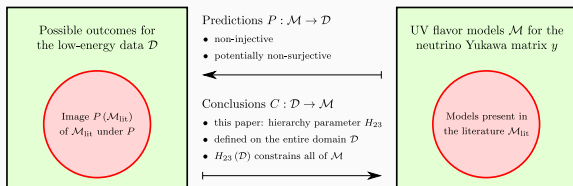
$$Y_{BAU} \propto \epsilon_{\alpha\alpha} \eta_{\alpha} \stackrel{!}{\simeq} 10^{-10 \dots -11}$$

→ constrain last free parameters!

[Bambhaniya et al., 2016]



**Bottom-Up:** Yukawa textures in term of CP phases  $\delta, \sigma$



- general method for assessing Yukawa structures
- maximal hierarchies for **approximate** two-zero textures consistent with data
- theoretical uncertainties for **exact** two-zero textures & robustness of results

**Top-Down:** Benchmark model

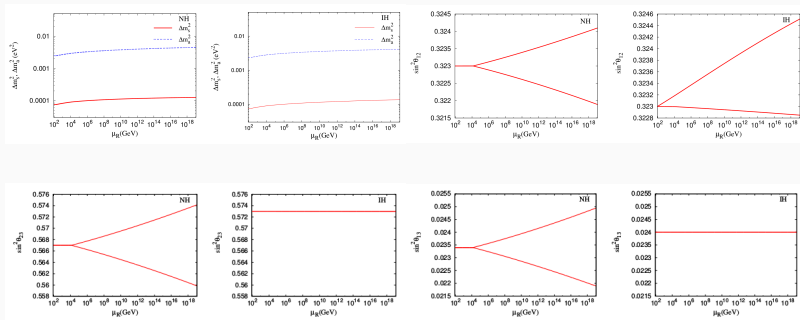
- reproduction of current data sets
- embedding of minimal seesaw model in broader UV context
- prediction: NH A1 texture -  $\delta \sim 270^\circ$ !



**Thank you for your attention!**

# RGE of neutrino mass parameters

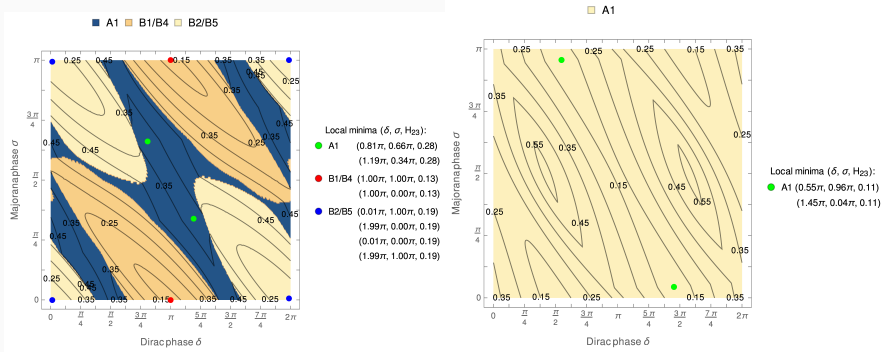
RGE can safely be neglected



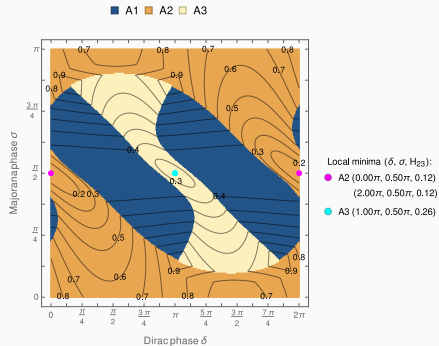
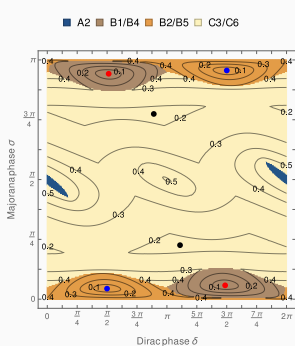
[Bambhaniya et al., 2016]






→ Experimental uncertainties outweigh RGE effects!

# Normal hierarchy - flavor-(un)aligned regions



# Inverted hierarchy - flavor-(un)aligned regions



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