

Fundamental Symmetries and Rare Decays

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IMPRS Seminar

based on

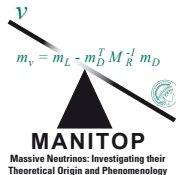
J.H., PRL **111**, 021801 (2013),
J.H., Werner Rodejohann,
EPL **103**, 32001 (2013).



INTERNATIONAL
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FOR PRECISION TESTS
OF FUNDAMENTAL
SYMMETRIES



Introduction

Symmetries:

unbroken	Poincaré (Lorentz), CPT, $SU(3)_C$, $U(1)_{EM}$
broken	C, CP, $SU(2)_L \times U(1)_Y$, lepton numbers L_α, \dots
?	Baryon number B , total lepton number L , strong CP

Discovery of (broken) symmetries always exciting, test via rare decays at low energies.

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Discovery of (broken) symmetries always exciting, test via rare decays at low energies.

- Here: focus on $B - L$ and $U(1)_{EM}$ (later), the abelian symmetries.

Baryon and lepton number

- B and L classically conserved in the Standard Model.
- $B + L$ theoretically broken non-perturbatively by 6 units.
- $B - L$ globally conserved.

Fate of fundamental $U(1)_{B-L}$ from experiments. Linked to neutrino nature and matter–antimatter asymmetry.

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Other possibilities exist!

$$\text{Dirac neutrinos} \Rightarrow \begin{cases} B - L \text{ conserved,} \\ \Delta(B - L) = 4, 6, 10, \dots \neq 2. \end{cases}$$

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Can we test lepton number violation by higher units?

Effective operators

- Lowest order new processes: $\Delta(B - L) = 4$:

$$\mathcal{O}_{d=6} : \bar{\nu}_R^c \nu_R \bar{\nu}_R^c \nu_R$$

$$\mathcal{O}_{d=8} : |H|^2 \bar{\nu}_R^c \nu_R \bar{\nu}_R^c \nu_R, \quad (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) \bar{\nu}_R^c \nu_R, \quad F_Y^{\mu\nu} \bar{\nu}_R^c \sigma_{\mu\nu} \nu_R \bar{\nu}_R^c \nu_R$$

$$\mathcal{O}_{d=10} : (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L), \quad |H|^2 (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) \bar{\nu}_R^c \nu_R, \\ F_Y^{\mu\nu} (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) \bar{\nu}_R^c \sigma_{\mu\nu} \nu_R, \quad W_a^{\mu\nu} (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger \tau^a L) \bar{\nu}_R^c \sigma_{\mu\nu} \nu_R, \\ (\bar{u}_R d_R^c)(\bar{d}_R \tilde{H}^\dagger L)(\bar{\nu}_R^c \nu_R), \dots$$

$$\mathcal{O}_{d=18} : (\bar{d}_R d_R^c \bar{u}_R^c u_R \bar{e}_R^c e_R)(\bar{d}_R d_R^c \bar{u}_R^c u_R \bar{e}_R^c e_R), \dots$$

$$\mathcal{O}_{d=20} : \left[((\bar{D}_\mu L)^c \tilde{H})(H^\dagger D_\nu L) \right]^2 \supset (\bar{e}_L^c W_\mu^+ W_\nu^+ e_L)(\bar{e}_L^c W^{+\mu} W^{+\nu} e_L), \dots$$

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$$\mathcal{O}_{d=18} : (\bar{d}_R d_R^c \bar{u}_R^c u_R \bar{e}_R^c e_R)(\bar{d}_R d_R^c \bar{u}_R^c u_R \bar{e}_R^c e_R), \dots$$

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- ν vs. $\bar{\nu}$ undetectable, use only charged particles, e.g. $\mathcal{O}_{d=18}$.

Dominant at low energies: Neutrinoless quadruple beta decay $0\nu 4\beta$

$$4d \rightarrow 4u + 4e^- \quad \Leftrightarrow \quad 4n \rightarrow 4p + 4e^- .$$

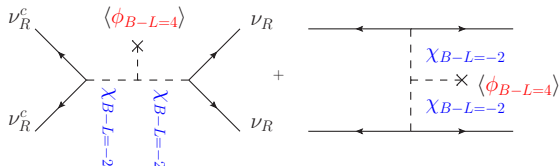
UV completion

- One scalar $\phi_{B-L=4}$ to break $B - L$, one scalar $\chi_{B-L=-2}$ as mediator.

$$\mathcal{L} \supset y_{\alpha\beta} \bar{L}_\alpha H \nu_{R,\beta} + \kappa_{\alpha\beta} \chi_{B-L=-2} \bar{\nu}_{R,\alpha} \nu_{R,\beta}^c + \text{h.c.}$$

- Neutrinos are Dirac (and $\Delta L = 2$ forbidden) if $\langle \chi_{B-L=-2} \rangle = 0$.
- Scalar potential $V(H, \phi, \chi) \supset -\mu \phi_{B-L=4} (\chi_{B-L=-2})^2 + \text{h.c.}$
- Lepton number violation $\Delta L = 4$ still possible!¹

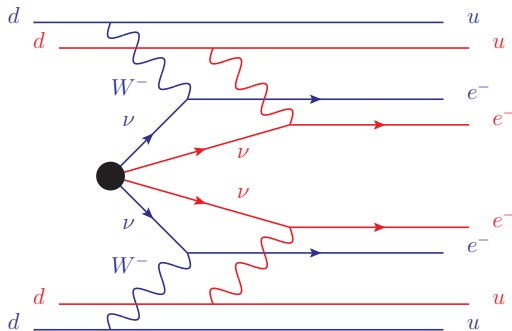
$$\bar{\nu}_R^c \nu_R \bar{\nu}_R^c \nu_R =$$



¹Heeck and Rodejohann, EPL 103, 32001 (2013) [arXiv:1306.0580].

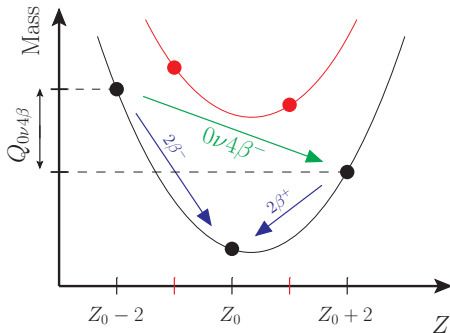
Neutrinoless quadruple beta decay $0\nu 4\beta$

$$(A, Z) \rightarrow (A, Z + 4) + 4 e^- \text{ via } \mathcal{O} = (\bar{\nu}_L^c \nu_L)^2 / \Lambda^2:$$



Candidate nuclei

- Experimental aspects of $0\nu 4\beta$ independent of underlying mechanism.
- Need beta-stable initial state:



- Decay modes: $0\nu 4\beta$ and $2\nu 2\beta$ ($0\nu 2\beta$ forbidden here).

Candidates for nuclear $\Delta L = 4$ processes

	$Q_{0\nu 4\beta}$	Other decays	NA/%
${}^{96}_{40}\text{Zr} \rightarrow {}^{96}_{44}\text{Ru}$	0.629 MeV	$\tau_{1/2}^{2\nu 2\beta} \simeq 2 \times 10^{19} \text{ y}$	2.8
${}^{136}_{54}\text{Xe} \rightarrow {}^{136}_{58}\text{Ce}$	0.044 MeV	$\tau_{1/2}^{2\nu 2\beta} \simeq 2 \times 10^{21} \text{ y}$	8.9
${}^{150}_{60}\text{Nd} \rightarrow {}^{150}_{64}\text{Gd}$	2.079 MeV	$\tau_{1/2}^{2\nu 2\beta} \simeq 7 \times 10^{18} \text{ y}$	5.6
	$Q_{0\nu 4\text{EC}}$		
${}^{124}_{54}\text{Xe} \rightarrow {}^{124}_{50}\text{Sn}$	0.577 MeV	—	0.095
${}^{130}_{56}\text{Ba} \rightarrow {}^{130}_{52}\text{Te}$	0.090 MeV	$\tau_{1/2}^{2\nu 2\text{EC}} \sim 10^{21} \text{ y}$	0.106
${}^{148}_{64}\text{Gd} \rightarrow {}^{148}_{60}\text{Nd}$	1.138 MeV	$\tau_{1/2}^{\alpha} \simeq 75 \text{ y}$	—
${}^{154}_{66}\text{Dy} \rightarrow {}^{154}_{62}\text{Sm}$	2.063 MeV	$\tau_{1/2}^{\alpha} \simeq 3 \times 10^6 \text{ y}$	—
	$Q_{0\nu 3\text{EC}\beta^+}$		
${}^{148}_{64}\text{Gd} \rightarrow {}^{148}_{60}\text{Nd}$	0.116 MeV	$\tau_{1/2}^{\alpha} \simeq 75 \text{ y}$	—
${}^{154}_{66}\text{Dy} \rightarrow {}^{154}_{62}\text{Sm}$	1.041 MeV	$\tau_{1/2}^{\alpha} \simeq 3 \times 10^6 \text{ y}$	—
	$Q_{0\nu 2\text{EC}2\beta^+}$		
${}^{154}_{66}\text{Dy} \rightarrow {}^{154}_{62}\text{Sm}$	0.019 MeV	$\tau_{1/2}^{\alpha} \simeq 3 \times 10^6 \text{ y}$	—

Best candidate: Neodymium $^{150}_{60}\text{Nd}$

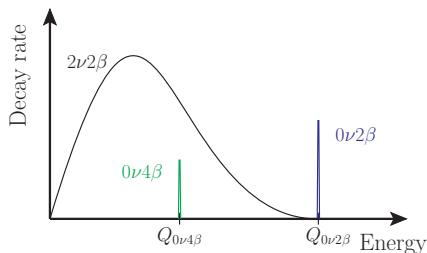
Decay channels:

- $^{150}_{60}\text{Nd} \rightarrow ^{150}_{62}\text{Sm}$ via $2\nu 2\beta$ ($\tau_{1/2}^{2\nu 2\beta} \simeq 7 \times 10^{18}$ y):

$$0 < \sum E_{e,i} < 3.371 \text{ MeV.}$$

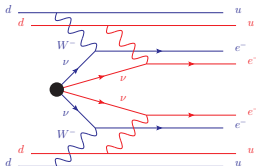
- $^{150}_{60}\text{Nd} \rightarrow ^{150}_{64}\text{Gd}$ via $0\nu 4\beta$:

$$\sum E_{e,i} = Q_{0\nu 4\beta} = 2.079 \text{ MeV.}$$



Neutrinoless quadruple beta decay $0\nu4\beta$

$$(A, Z) \rightarrow (A, Z + 4) + 4 e^- \text{ via } \mathcal{O} = (\bar{\nu}_L^c \nu_L)^2 / \Lambda^2:$$



- Very naive comparison with competing channel $2\nu2\beta$:

$$\frac{\tau_{1/2}^{0\nu4\beta}}{\tau_{1/2}^{2\nu2\beta}} \simeq \left(\frac{Q_{0\nu2\beta}}{Q_{0\nu4\beta}} \right)^{11} \left(\frac{\Lambda^4}{q^{12} G_F^4} \right) \simeq 10^{46} \left(\frac{\Lambda}{\text{TeV}} \right)^4,$$

with $|q| \sim p_\nu \sim 1 \text{ fm}^{-1} \simeq 100 \text{ MeV}$.

- Estimated rate in toy model unobservably small. Elaborate models with resonances overcome this?

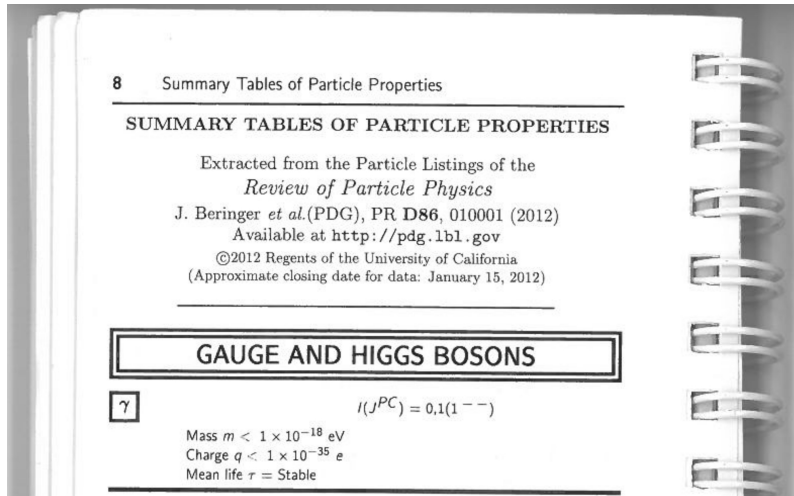
Rare decays in QED

What do we know about photons?

- Mass $m = 0$, charge $Q = 0$, lifetime $\tau_\gamma = \infty$

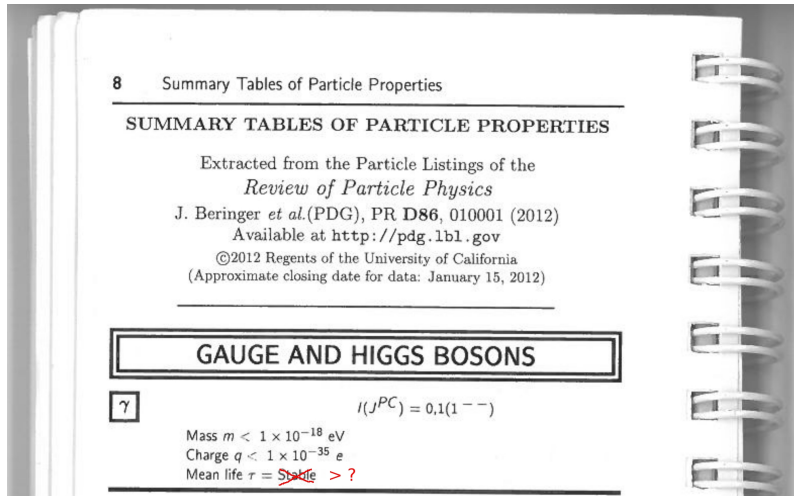
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- Measurements:



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- Measurements:



Massive photons

- Standard argument: $\mathcal{L} \supset \frac{1}{2} m^2 A_\mu A^\mu$ breaks gauge invariance
 $A_\mu \rightarrow A_\mu - \partial_\mu \theta(x)$.
- True, but theory *still* renormalizable, unitary, charge conserved etc.
- Formal reason: Stückelberg mechanism:

$$\frac{1}{2} m^2 A_\mu A^\mu \rightarrow \Delta L \equiv \frac{1}{2} (mA^\mu + \partial^\mu \sigma)(mA_\mu + \partial_\mu \sigma).$$

- Real scalar σ transforms as $\sigma \rightarrow \sigma + m\theta(x)$, gauge invariance restored.
- Mass term $\frac{1}{2} m^2 A_\mu A^\mu$ is just gauge *fixing*, not *breaking*.

$U(1)$ gauge bosons can have mass without symmetry breaking.

Massive photons II

Theory:²

- QED $U(1)_{EM} \subset$ Standard Model $SU(3)_C \times SU(2)_L \times U(1)_Y$.
- Stückelberg mass for hypercharge boson m_Y^2 gives photon mass + corrections m_γ^2/M_Z^2 to SM.
- Not possible in Grand Unified Theories
 $SU(3)_C \times SU(2)_L \times U(1)_Y \subset SU(5) \subset SO(10) \subset E_6$.

Experiment:³

- Coulomb's law $V(r) = -\frac{e}{r}e^{-mr}$ gives $m \lesssim 10^{-14}$ eV.
- Solar wind magnetic field: $m \lesssim 10^{-18}$ eV.
- Galactic magnetic field: $m \lesssim 10^{-26}$ eV.

Massive photon not crazy, simplest SM extension.

²Ruegg and Ruiz-Altaba, arXiv:hep-th/0304245.

³Goldhaber and Nieto, arXiv:0809.1003.

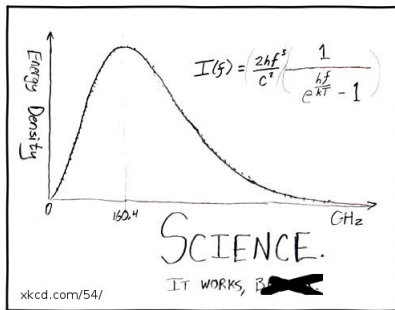
Unstable photons

- Massive photon can kinematically decay,⁴ e.g. to lightest neutrino:
 $\gamma \rightarrow \nu\nu$.
- Model-independent limit on τ_γ : well-known low-energy photons.

⁴Heeck, PRL **111** (2013), 021801 [arXiv:1304.2821].

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- Model-independent limit on τ_γ : well-known low-energy photons.
- Blackbody spectrum from cosmic microwave background!



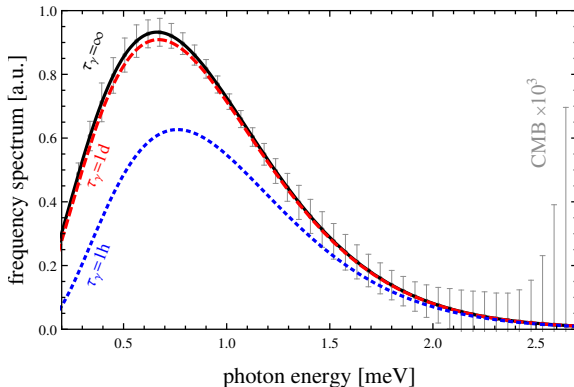
⁴Heeck, PRL **111** (2013), 021801 [arXiv:1304.2821].

Unstable photons

- Modified blackbody spectrum:

$$\rho(E, T)dE \simeq \frac{1}{\pi^2} \frac{E^3 dE}{\exp(\sqrt{E^2 - m^2}/T) - 1} \sqrt{1 - \frac{m^2}{E^2}} \exp\left(-\frac{m}{E} \frac{d_L}{\tau_\gamma}\right)$$

with comoving distance to CMB $d_L \simeq 47$ billion lightyears.



Limit on photon decay

- Fit to precise (10^{-4}) COBE data: $m < 3 \times 10^{-6}$ eV and model-independent limit on photon lifetime:

$$\tau_\gamma > 3 \text{ yr} \left(\frac{m}{10^{-18} \text{ eV}} \right) \quad \text{at 95\% C.L.}$$

- Visible photons are boosted: $\tau_\gamma(\text{red light}) \sim 10^{18} \tau_\gamma$.

Caution:

- Assumed free-streaming CMB photons: interactions with ionized plasma generate plasma-mass for γ .
- Model-*dependent* limits far stronger, because $\gamma \rightarrow XX$ implies milli-charged X .⁵

⁵Davidson, Hannestad, and Raffelt, arXiv:hep-ph/0001179.

Summary

Fundamental abelian symmetries of SM:

$U(1)_{B-L}$

- global, local, unbroken, broken by 2, 4, 6, ... units?
- Now: $\Delta L = 2$ via $0\nu 2\beta$.
- In principle: $\Delta L = 4$ via $0\nu 4\beta$; experimentally (and theoretically) challenging.
- $\Delta L = 4$ lowest LNV of Dirac neutrinos.

$U(1)_{EM}$

- Photon can be massive (gauge invariant!).
- *Could* (kinematically) decay, e.g. $\gamma \rightarrow \nu\nu$.
- First model-independent bound: $\tau_\gamma > 3 \text{ yr}$.
- Severe implications: photon decay (or mass) would kill GUTs.

Phenomenology of LNV Dirac neutrinos

Quick summary:

- Even with Dirac neutrinos, we can have LNV.
- Lowest order is then $\Delta(B - L) = \Delta L = 4$, via $\mathcal{O}_{d=6} = (\bar{\nu}_R^c \nu_R)^2 / \Lambda^2$.

How to check for $\Delta L = 4$?

- Neutrinoless quadruple beta decay $(A, Z) \rightarrow (A, Z + 4) + 4 e^-$.
- Collider process $e^- e^- \rightarrow W^- W^- W^- W^- \ell^+ \ell^+$.
- Rare meson decays etc.?

All tough, many particles in final state!

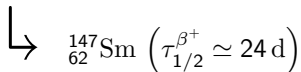
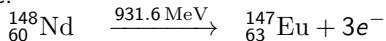
$\Delta L = 4$ can however easily be relevant in the early Universe
 \Rightarrow new Dirac leptogenesis mechanism predicting $3.14 \lesssim N_{\text{eff}} \lesssim 3.29$.⁶

⁶Heeck, PRD **88**, 076004 (2013) [arXiv:1307.2241].

Comments on $0\nu 4\beta$

- Background: electrons from $2\nu 2\beta$ kick out two more e^- .
 $\Rightarrow 4 e^-$ with $\sum E_i \sim Q_{0\nu 4\beta}$ possible.
- $0\nu 4\beta$ to excited state $^{150}_{64}\text{Gd}^*$: Q reduced by 0.6 MeV (2^+) or 1.2 MeV (0^+), but more photons...
- Nuclear matrix elements impossible (?) to calculate.
 \Rightarrow No way to extract fundamental couplings from $\tau_{0\nu 4\beta}$ (?)
- $0\nu 6\beta$ etc. all involve beta-unstable nuclei.
 $\Rightarrow 0\nu 2\beta$ and $0\nu 4\beta$ somewhat unique.
- Very different $\Delta(B - L) = 4$ decay: $4n \rightarrow 3p + 3e^-$, mimics $0\nu 3\beta$.

Candidate:



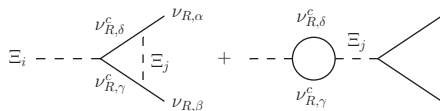
followed by the β^+ decay into $^{147}_{62}\text{Sm}$ with half-life 24 d.

Dirac $B - L$: LeptogenesisLeptogenesis via $\Delta L = 4$?

- Scalar potential $V(H, \phi, \chi) \supset -\mu \phi_{B-L=4} (\chi_{B-L=-2})^2$ breaks complex $\chi_{B-L=-2} = (\Xi_1 + i \Xi_2)/\sqrt{2}$ into two real scalars with mass

$$m_1^2 = m_c^2 - 2\mu \langle \phi_{B-L=4} \rangle, \quad m_2^2 = m_c^2 + 2\mu \langle \phi_{B-L=4} \rangle.$$

- Heavy mediator scalar Ξ_j decays to $\nu_R \nu_R$ or $\bar{\nu}_R \bar{\nu}_R$ out-of-equilibrium in early Universe.⁷



- CP violation requires *second* scalar $\chi_{B-L=-2}$.

Asymmetry in ν_R . How to translate to baryon asymmetry?⁷Heeck, PRD **88**, 076004 (2013) [arXiv:1307.2241].

Baryon Asymmetry

$$Y_{\nu_R} \equiv \frac{n_{\nu_R}}{s} \sim \frac{1}{g_*} \frac{\Gamma(\Xi_i \rightarrow \nu_R \nu_R) - \Gamma(\Xi_i \rightarrow \nu_R^c \nu_R^c)}{\Gamma(\Xi_i \rightarrow \nu_R \nu_R) + \Gamma(\Xi_i \rightarrow \nu_R^c \nu_R^c)}.$$

- Dirac-Yukawa coupling $Y_\nu = m_\nu / \langle H \rangle$ too small to equilibrate $\nu_R \dots$

Add second Higgs doublet H_2 with large Yukawa $\bar{L} H_2 \nu_R$:

- **Neutrinophilic H_2** with small VEV $\langle H_2 \rangle \sim 1 \text{ eV}$
 \Rightarrow Dirac neutrinos light with large Yukawas.
- H_2 moves Y_{ν_R} to Y_{ν_L} .
- Sphalerons move Y_{ν_L} to Y_B .

\Rightarrow Different from neutrino genesis, similar to standard leptogenesis!

- Necessary thermalization of $\nu_R \Rightarrow N_{\text{eff}} > 3!$
- $3.14 \lesssim N_{\text{eff}} \lesssim 3.29$ depending on H_2^+ mass and Yukawa coupling.
- Specific collider signatures of neutrinophilic H_2 .⁸

⁸S. M. Davidson and H. E. Logan, PRD **80**, 095008 (2009).