

NLO SUSY pair production in MadGOLEM

2nd IMPRS seminar

November 18 2011 | Heidelberg



Dorival Gonçalves-Netto

collaborators D. Lopez-Val, T. Plehn, K. Mawatari, I. Wigmore

ITP - Universität Heidelberg

Institut für Theoretische Physik
Ruprecht-Karls Universität Heidelberg

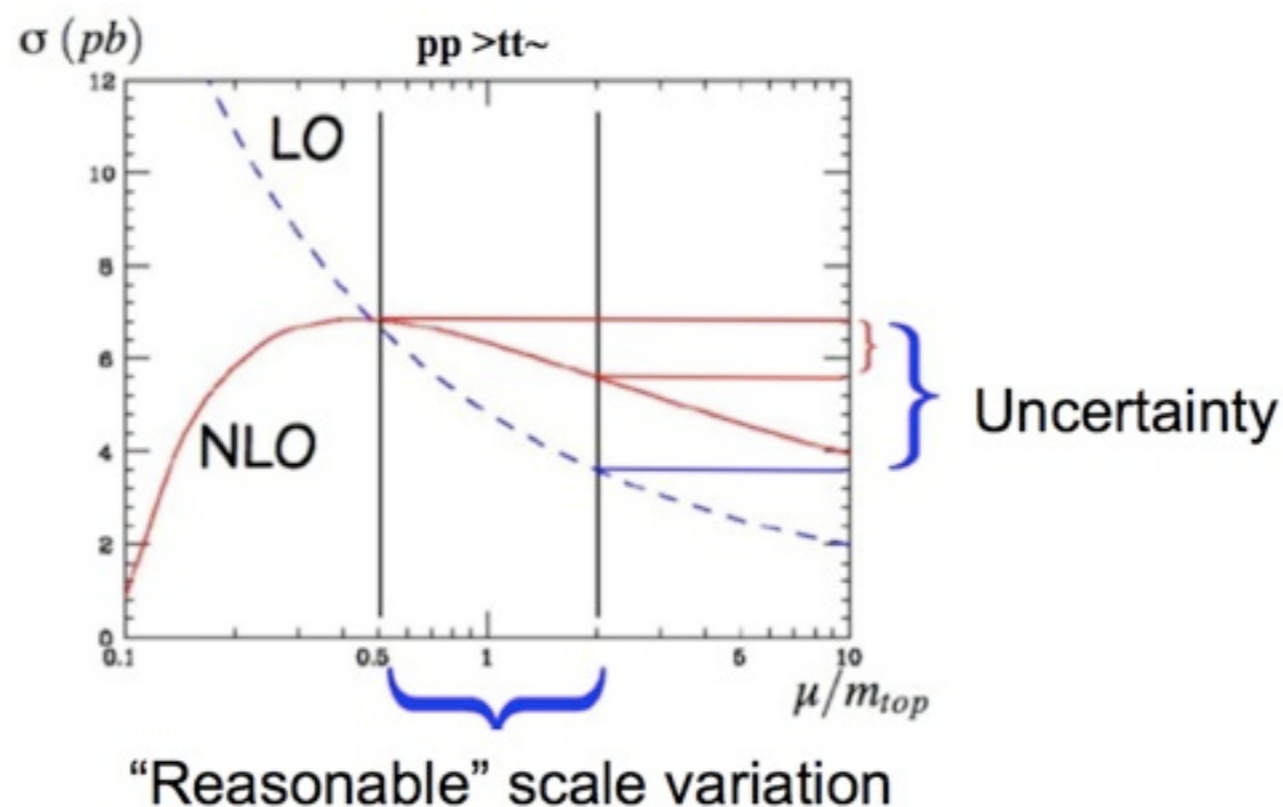


Outline

- Motivations
- Perturbative (SUSY-)QCD
 - Structure of the NLO corrections
 - Catani-Seymour Subtraction Method
 - MadGOLEM
- One major LHC search channel: SUSY Monojet signatures
 - NLO corrections
 - Pheno analysis
- Summary

Motivations

- Why Next-to-Leading order (NLO)?
- Less sensibility from unphysical factorization/renormalization scales



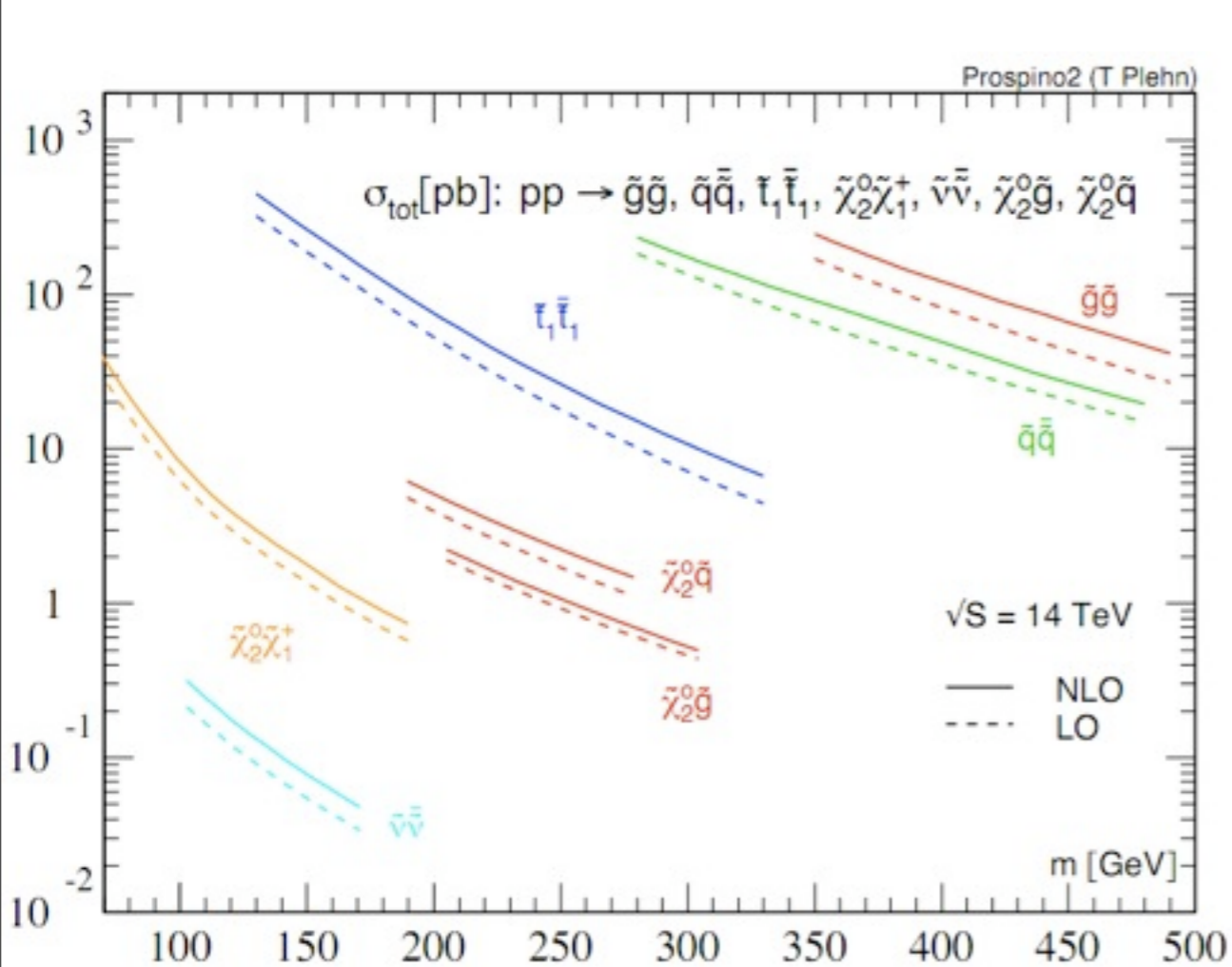
- Improve shape of distributions
- New channels & kinematics arising from NLO can have a high impact (particularly in the presence of cuts)
- Not yet fully automated

Motivations

- PROSPINO (PROduction of Supersymmetric Particles in Next-to-leading Order)
[Beenakker, Höpker, Krämer, Plehn, Spira, Zerwas]
 - ➔ The only public available code to do SUSY NLO cross sections
 - ➔ It's hard coded, process dependent
 - ➔ Just gives total cross sections (no distributions).
- MadGOLEM: Fully automated tool to perform NLO QCD for BSM
(main focus on SUSY models)
 - ➔ Process independent
 - ➔ Gives total cross sections and distributions
 - ➔ Allow the user to apply cuts...

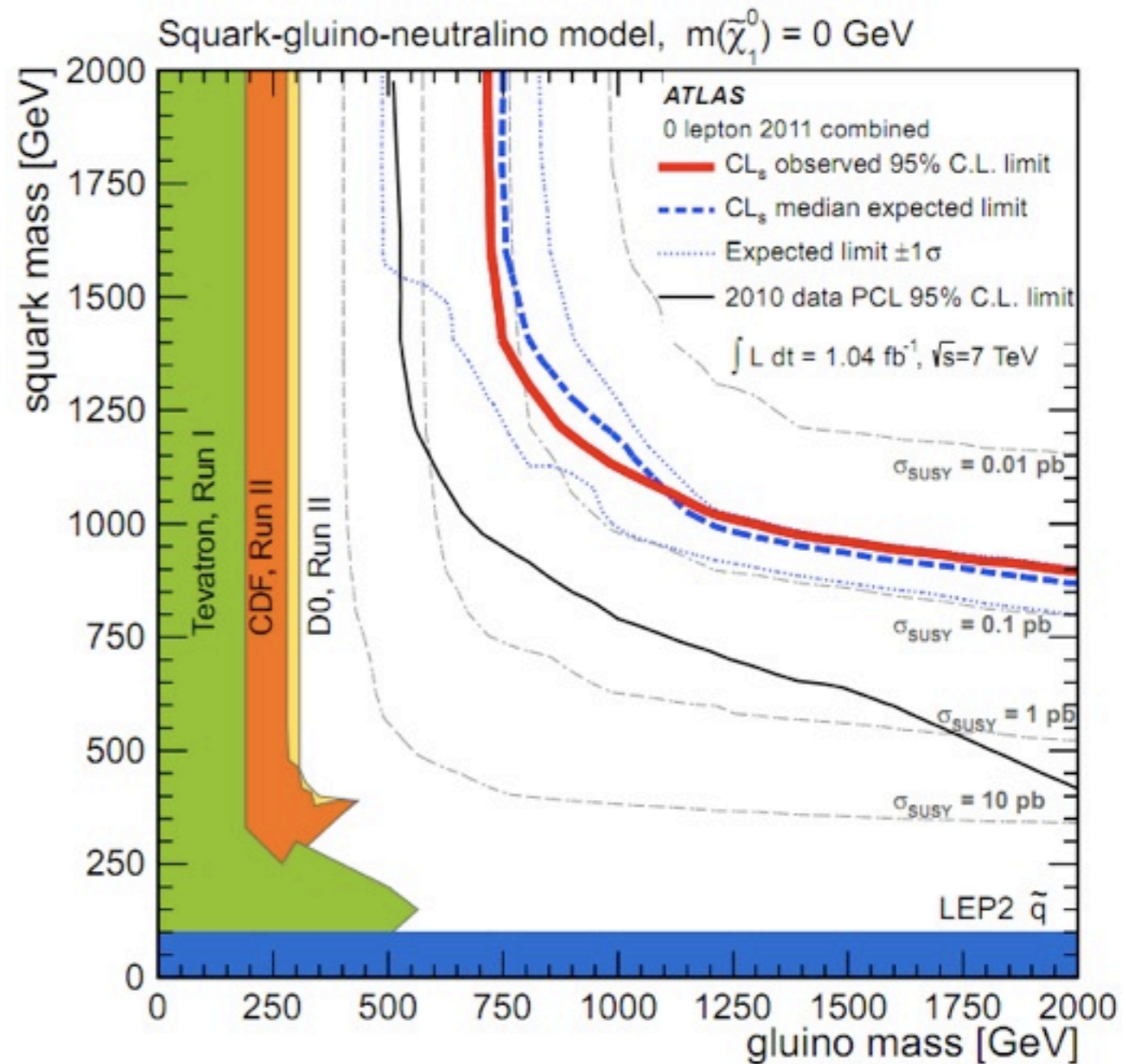
Motivations

SUSY pair production at the LHC:



$$K = \frac{\sigma^{NLO}}{\sigma^{LO}} \sim 1.3 - 1.5$$

NLO correction quantitatively relevant!



“SUSY signal samples are generated with HERWIG++, normalized using the NLO cross section determined by PROSPINO.” [1109.6572[hep-ex]]

Perturbative QCD

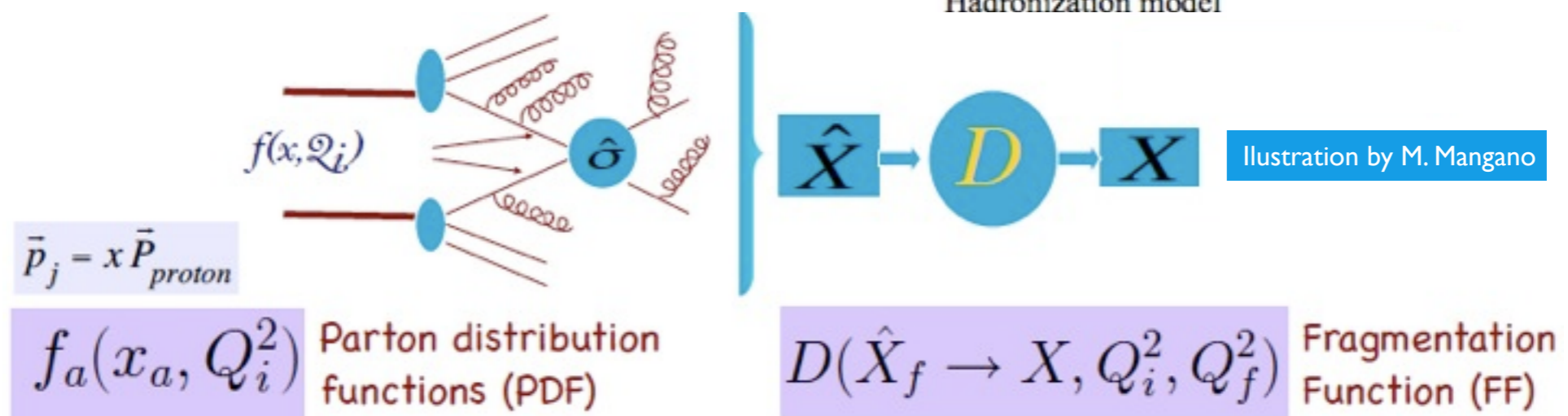
- Master Formula: Factorizes the hard and soft processes.

$$\sigma_{pp \rightarrow X} = \sum_{i,j,\{k\}} \int dx_1 dx_2 f_i(x_1) f_j(x_2) \hat{\sigma}_{ij \rightarrow \{k\}}(\alpha_s, Q) \otimes D_{\{k\} \rightarrow X}$$

Parton distribution function
(Non-perturbative)

Subprocess partonic cross section
(Perturbative)

Jet algorithm
Parton shower
Hadronization model



Perturbative expansion from the partonic cross section:

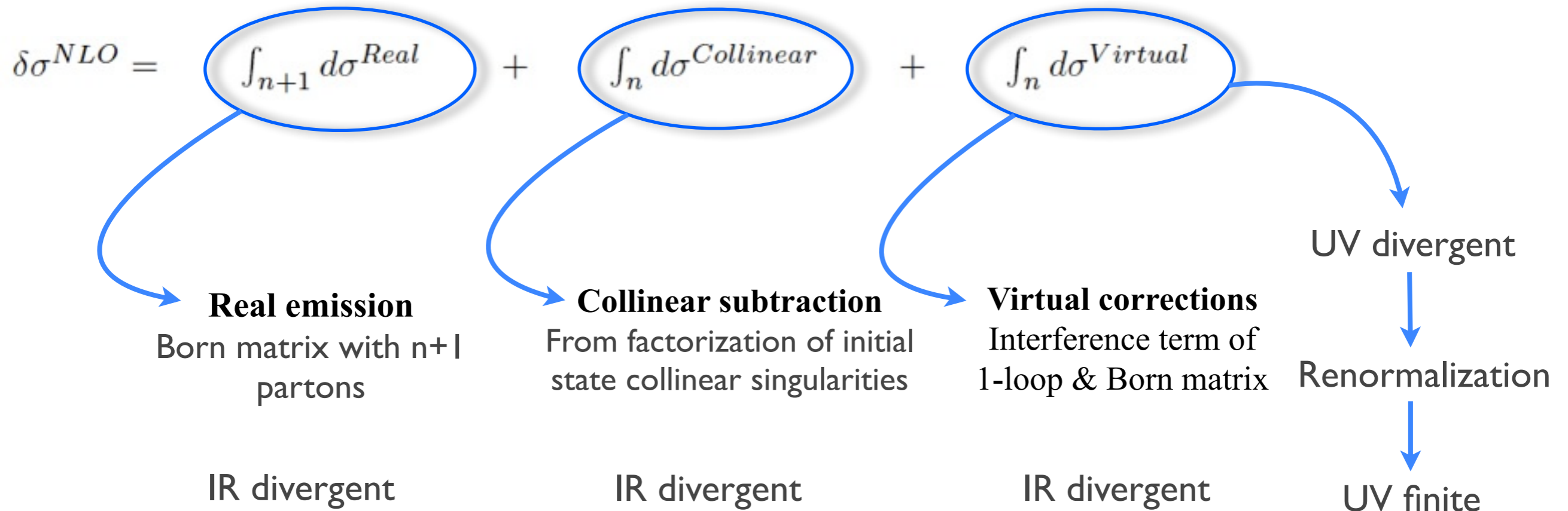
$$\hat{\sigma}_{ab \rightarrow f} = \sigma_0 + \alpha_s \sigma_1 + \alpha_s^2 \sigma_2 + \dots$$

Leading Order

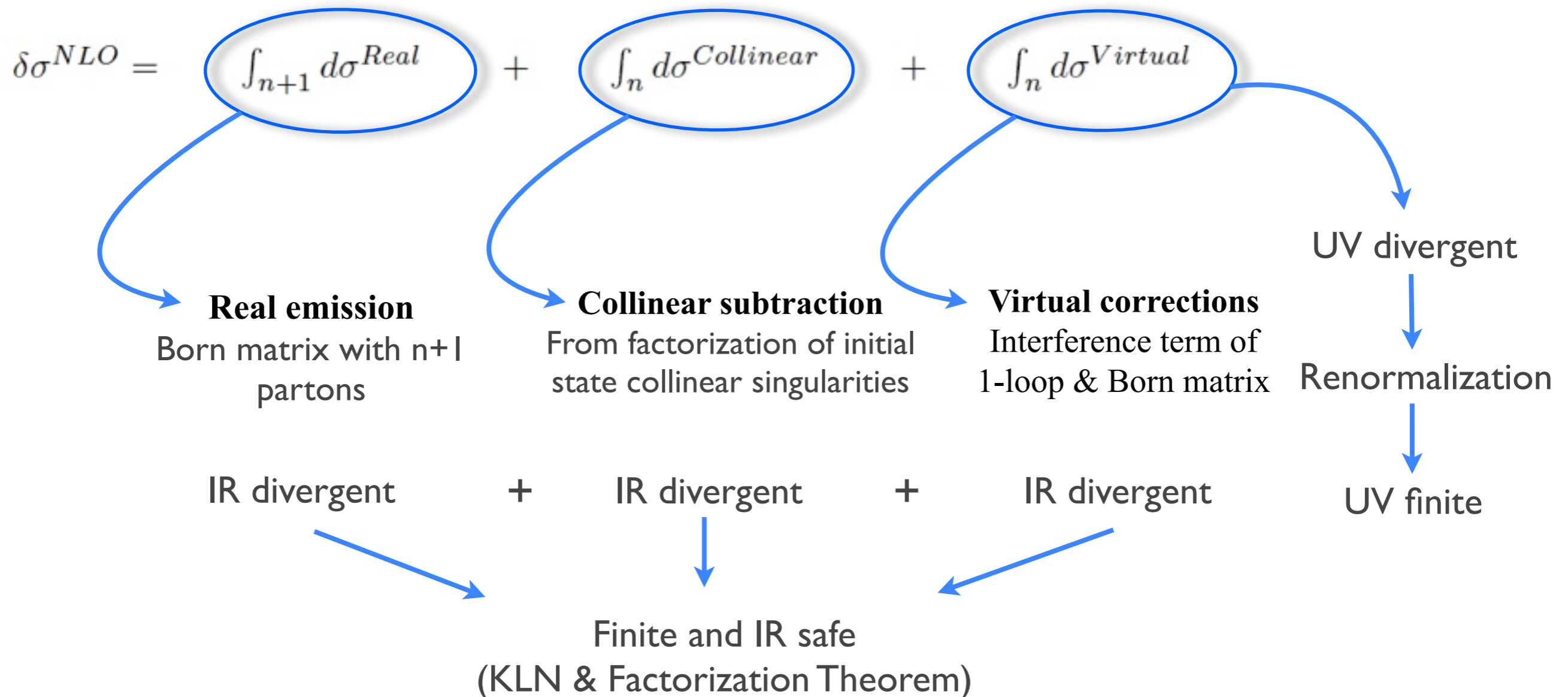
Next-to-Leading Order

Next-to-Next-to-Leading Order

Structure of the NLO corrections



Structure of the NLO corrections



Problems:

- Analytic integration in d dimensions only feasible for very simple fully inclusive processes
- How to get individual contributions finite via MC methods?

Structure of the NLO corrections

Subtraction Method (Warm up):

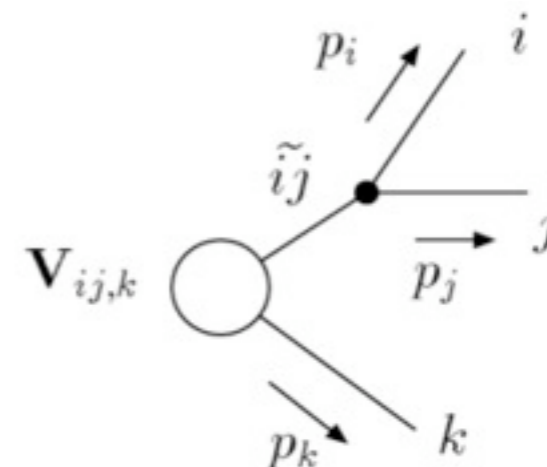
$$\begin{aligned} \int_0^1 \frac{F(x)}{x^{1-\varepsilon}} dx &= \int_0^1 \frac{F(x) - F(0)}{x^{1-\varepsilon}} dx + \int_0^1 \frac{F(0)}{x^{1-\varepsilon}} dx \\ &= \int_0^1 \frac{F(x) - F(0)}{x} dx + \frac{F(0)}{\varepsilon} \end{aligned}$$

Catani-Seymour Subtraction Method: construction of **local counter terms** using the universality of soft and collinear limits

$$|\mathcal{M}_{n+1}|^2 \rightarrow |\mathcal{M}_n|^2 \otimes V_{ij,k} \quad \longrightarrow \quad d\sigma^A \equiv \sum_{\text{dipoles}} d\sigma^B \otimes dV_{\text{dipole}}$$

$$\delta\sigma^{NLO} = \int_{n+1} (d\sigma_{\varepsilon=0}^{\text{Real}} - d\sigma_{\varepsilon=0}^A) + \int_n (d\sigma^{\text{Collinear}} + d\sigma^{\text{Virtual}} + \int_1 d\sigma^A)_{\varepsilon=0}$$

$V_{ij,k}$ is a singular factor, and depends only on the quantum numbers of i , j and k , and on their momenta. It is completely process independent.



Structure of the NLO corrections

Subtraction Method (Warm up):

$$\begin{aligned} \int_0^1 \frac{F(x)}{x^{1-\varepsilon}} dx &= \int_0^1 \frac{F(x) - F(0)}{x^{1-\varepsilon}} dx + \int_0^1 \frac{F(0)}{x^{1-\varepsilon}} dx \\ &= \int_0^1 \frac{F(x) - F(0)}{x} dx + \frac{F(0)}{\varepsilon} \end{aligned}$$

Catani-Seymour Subtraction Method: construction of **local counter terms** using the universality of soft and collinear limits

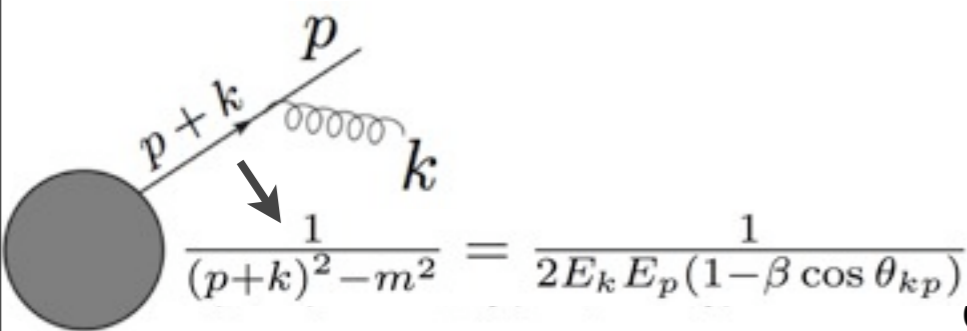
$$|\mathcal{M}_{n+1}|^2 \rightarrow |\mathcal{M}_n|^2 \otimes V_{ij,k} \quad \longrightarrow \quad d\sigma^A \equiv \sum_{\text{dipoles}} d\sigma^B \otimes dV_{\text{dipole}}$$

$$\delta\sigma^{NLO} = \int_{n+1} (d\sigma_{\varepsilon=0}^{\text{Real}} - d\sigma_{\varepsilon=0}^A) + \int_n (d\sigma^{\text{Collinear}} + d\sigma^{\text{Virtual}} + \int_1 d\sigma^A)_{\varepsilon=0}$$

$$\left(\frac{c_2}{\varepsilon_{IR}^2} + \frac{c_1}{\varepsilon_{IR}} + c_0 \right) + \left(\frac{c'_2}{\varepsilon_{IR}^2} + \frac{c'_1}{\varepsilon_{IR}} + c'_0 \right) = c_0 + c'_0$$

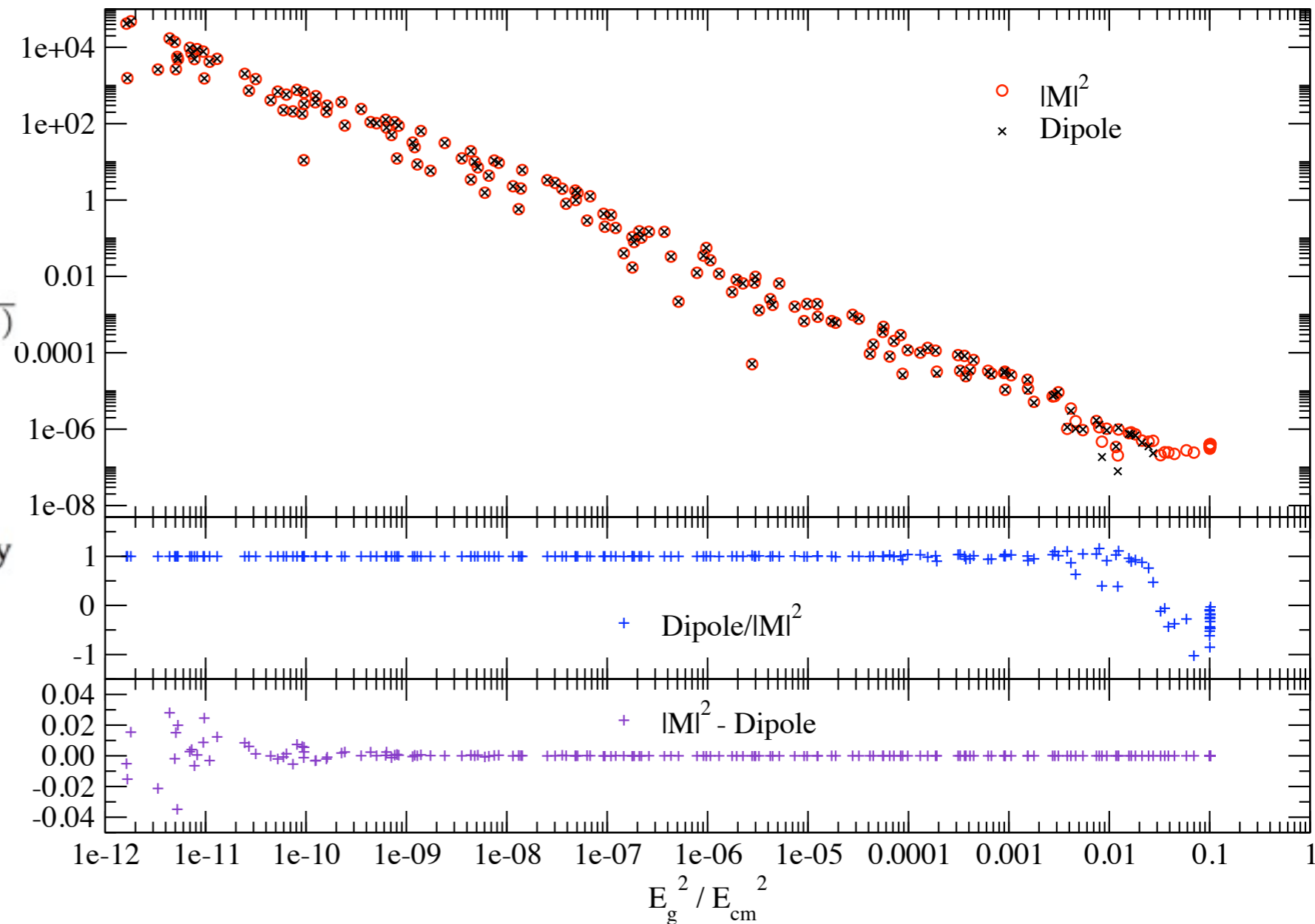
The Virtual part can be integrable in 4D just after cancelation of the poles, where their pole counter part come from the integrated dipoles

Structure of the NLO corrections



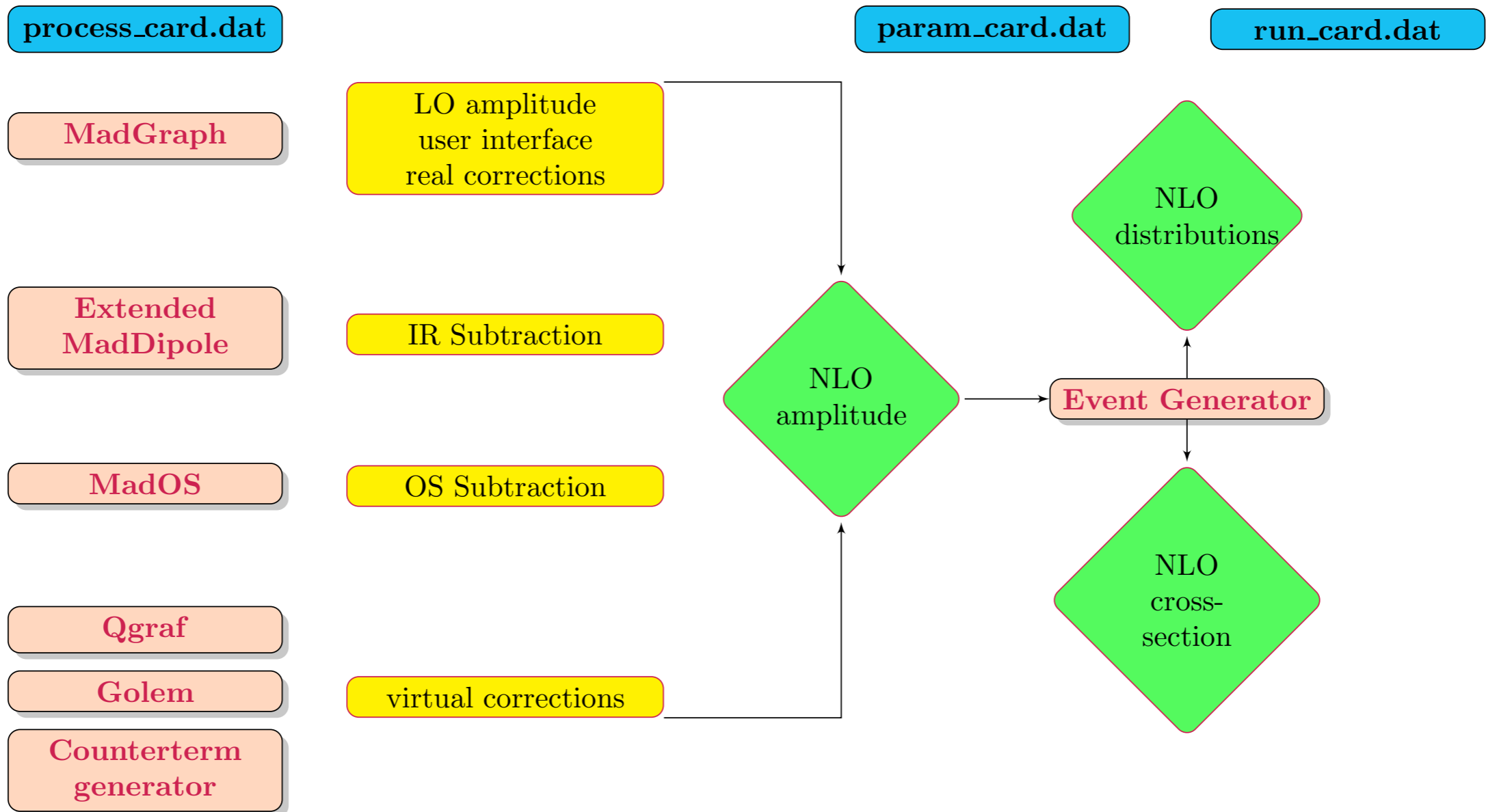
{ Soft limit $E_k \rightarrow 0$: Soft singularity
 Collinear limit $\theta_{kp} \rightarrow 0$: Collinear singularity

Soft limit for gluon
 $e+e- \rightarrow ul\bar{u}l\bar{g}$, $E_{cm} = 500$ GeV, $m_{ul} = 150$ GeV



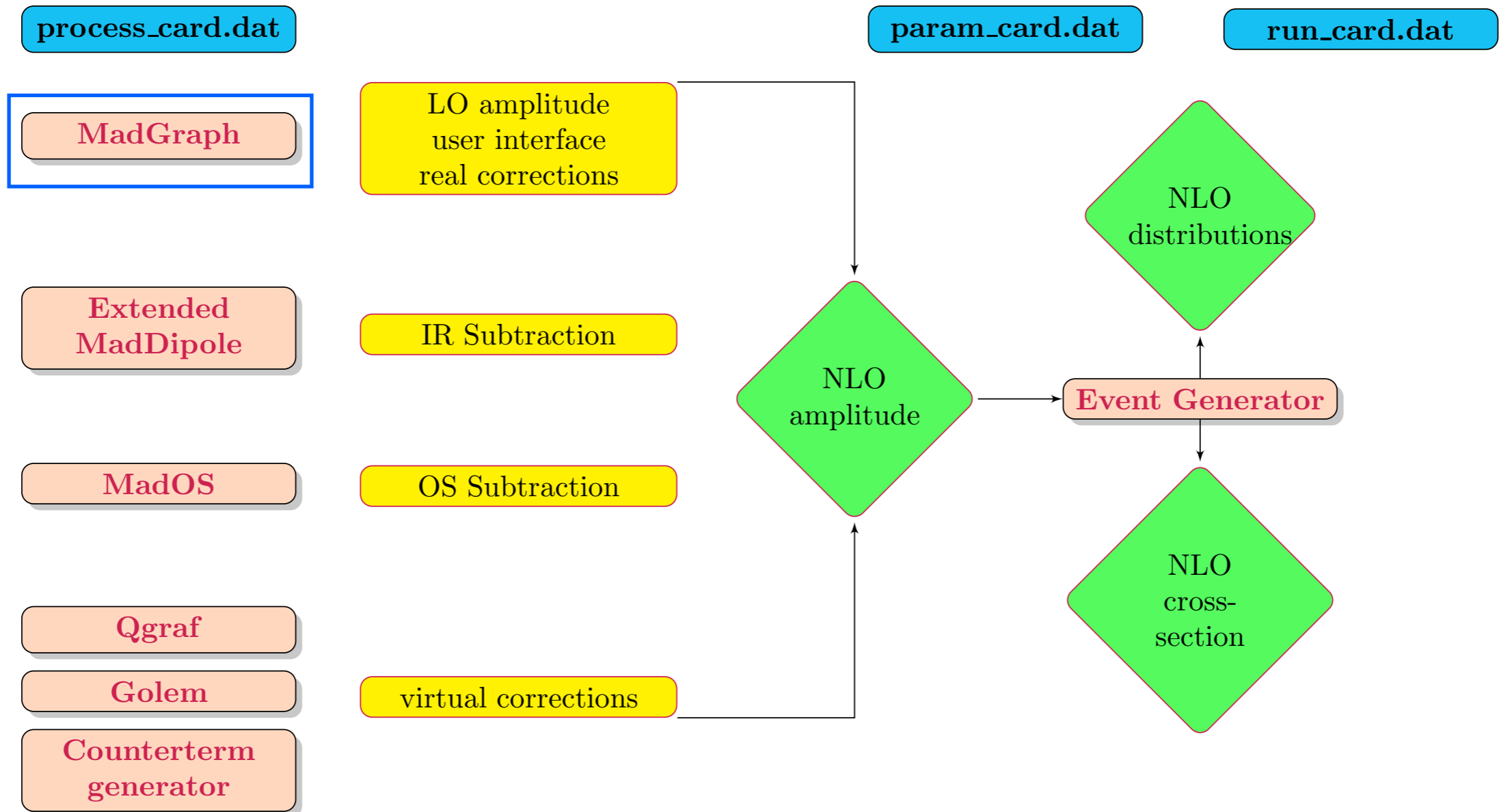
$$\delta\sigma^{NLO} = \int_{n+1} (d\sigma_{\epsilon=0}^{Real} - d\sigma_{\epsilon=0}^A) + \int_n (d\sigma^{Collinear} + d\sigma^{Virtual} + \int_1 d\sigma^A)_{\epsilon=0}$$

MadGOLEM



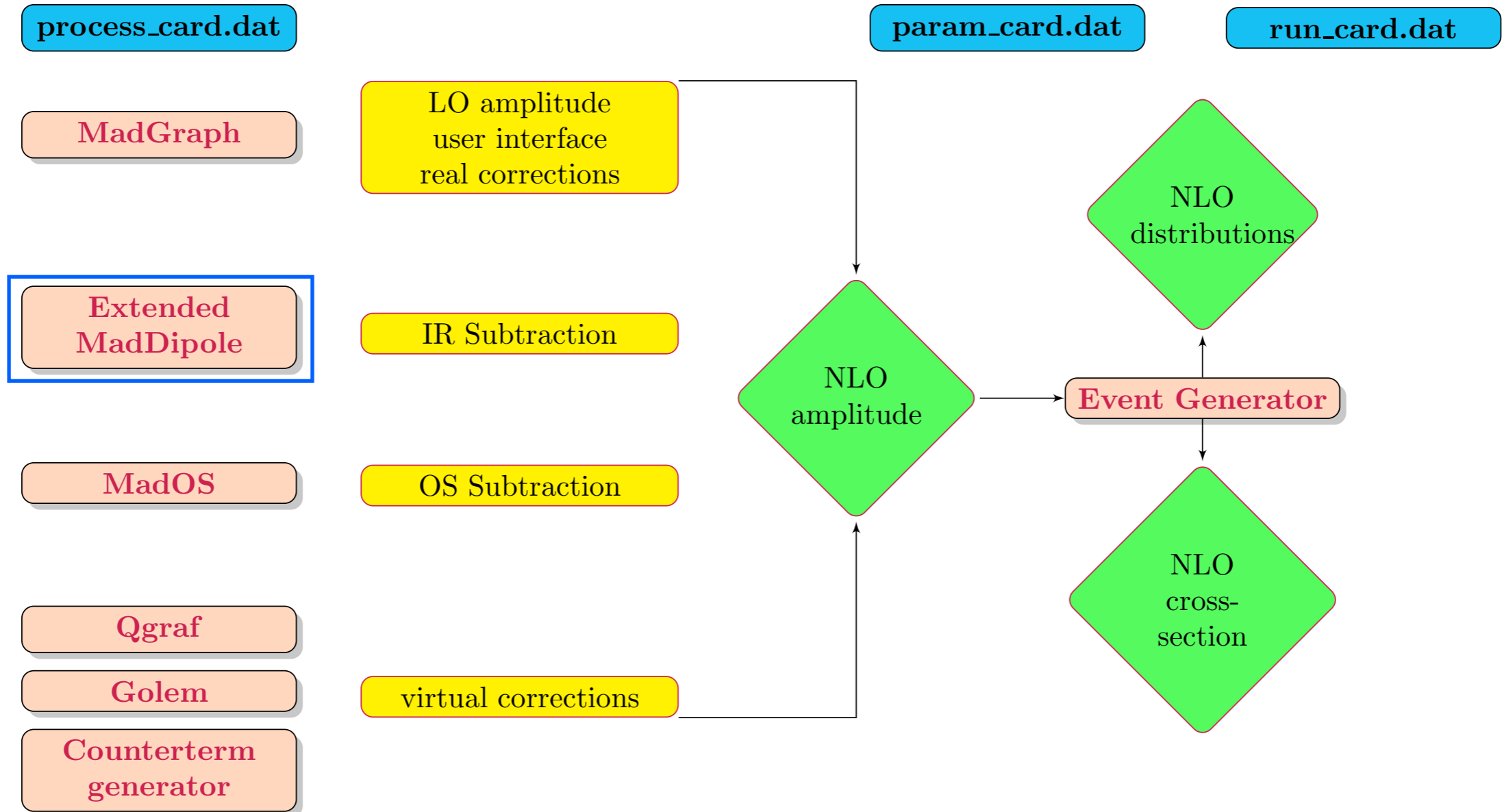
$$\sigma^{NLO} = \int_n d\sigma^{LO} + \int_{n+1} (d\sigma_{\epsilon=0}^{Real} - d\sigma_{\epsilon=0}^A - d\sigma_{\epsilon=0}^{OS}) + \int_n (d\sigma^{Virtual} + \int_1 d\sigma^A)_{\epsilon=0}$$

MadGOLEM



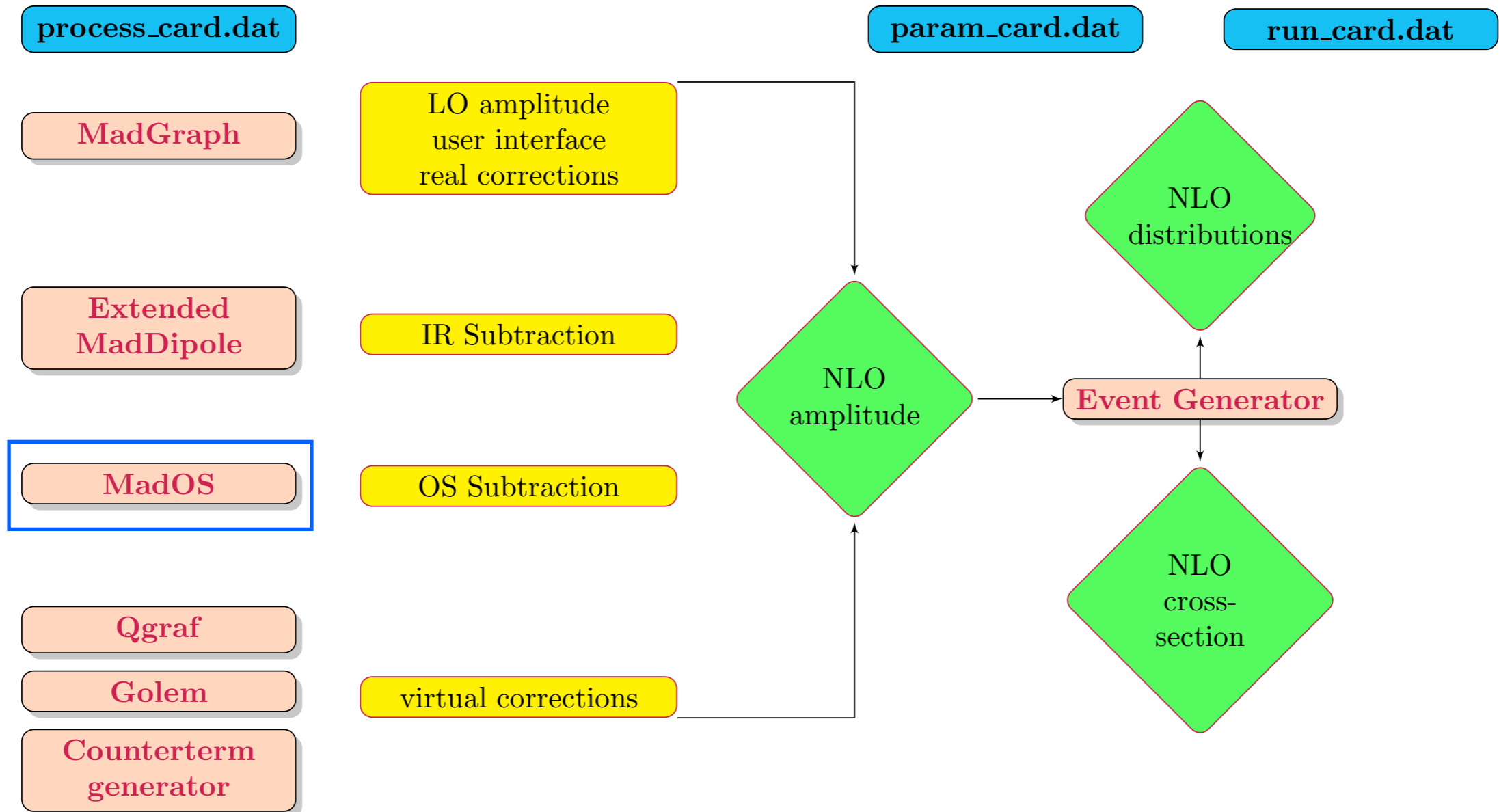
$$\sigma^{NLO} = \int_n d\sigma^{LO} + \int_{n+1} \left(d\sigma_{\epsilon=0}^{Real} - d\sigma_{\epsilon=0}^A - d\sigma_{\epsilon=0}^{OS} \right) + \int_n \left(d\sigma^{Virtual} + \int_1 d\sigma^A \right)_{\epsilon=0}$$

MadGOLEM



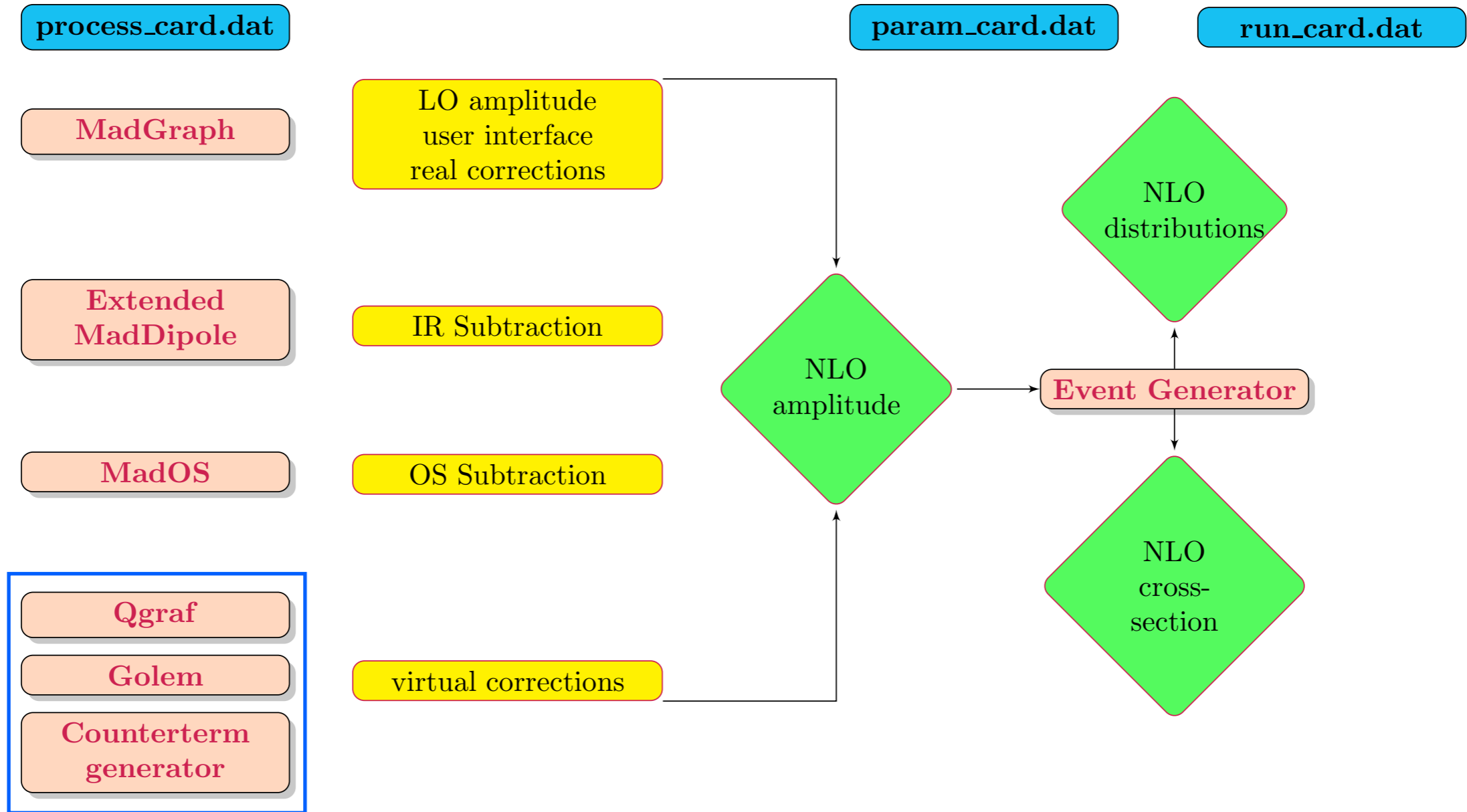
$$\sigma^{NLO} = \int_n d\sigma^{LO} + \int_{n+1} \left(d\sigma_{\epsilon=0}^{Real} - \boxed{d\sigma_{\epsilon=0}^A} - d\sigma_{\epsilon=0}^{OS} \right) + \int_n \left(d\sigma^{Virtual} + \boxed{\int_1 d\sigma^A} \right)_{\epsilon=0}$$

MadGOLEM



$$\sigma^{NLO} = \int_n d\sigma^{LO} + \int_{n+1} \left(d\sigma_{\epsilon=0}^{Real} - d\sigma_{\epsilon=0}^A - d\sigma_{\epsilon=0}^{OS} \right) + \int_n \left(d\sigma^{Virtual} + \int_1 d\sigma^A \right)_{\epsilon=0}$$

MadGOLEM



$$\sigma^{NLO} = \int_n d\sigma^{LO} + \int_{n+1} (d\sigma_{\epsilon=0}^{Real} - d\sigma_{\epsilon=0}^A - d\sigma_{\epsilon=0}^{OS}) + \int_n (d\sigma^{Virtual} + \int_1 d\sigma^A)_{\epsilon=0}$$

DGN, D. Lopez-Val, T. Plehn, K. Mawatari, I. Wigmore

Squark-neutralino at NLO

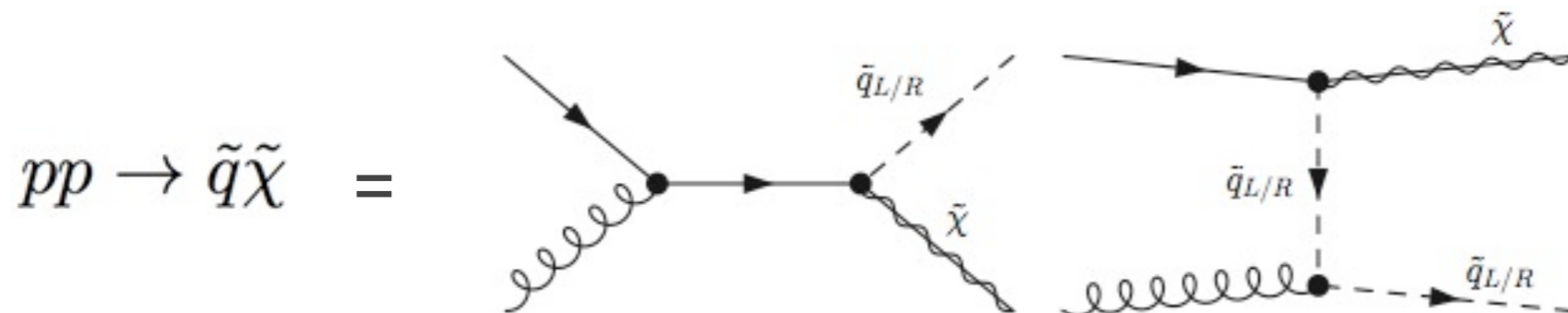
- For SUSY there are 3 main production modes at the LHC:

$$pp \rightarrow \tilde{q}\tilde{q}, \tilde{q}\tilde{g}, \tilde{g}\tilde{g} \text{ (mediated by strong interactions)}$$

- though hard to extract any model parameters beyond masses of new particles
- interactions determined by gauge symmetry and SUSY, e.g.

$$\text{gluon } \mu, a \quad \begin{array}{l} p, i \text{ squark} \\ q, j \text{ squark} \end{array} \quad = -i g_s (T_a)_{ij} (p + q)^\mu$$

- Important to study production process involving the weakly interacting sector



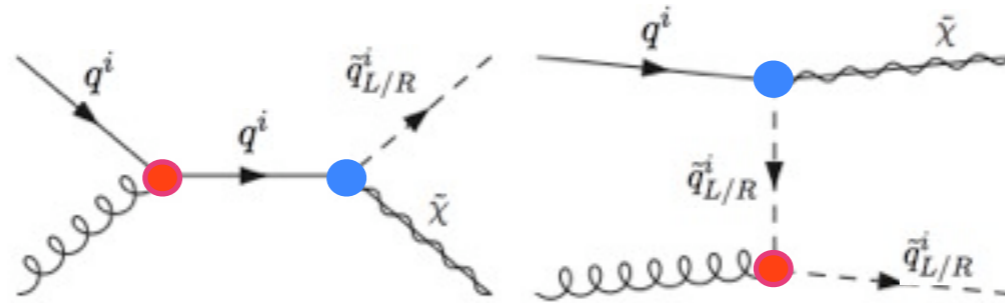
Source of **monojet** + \cancel{E}_T signatures

- One hard jet in association + \cancel{E}_T is one **major LHC search channel for BSM**

- Associated production: semi-weak process, but favored by $m_{\tilde{\chi}_1^0} \ll m_{\tilde{q}}, m_{\tilde{g}}$

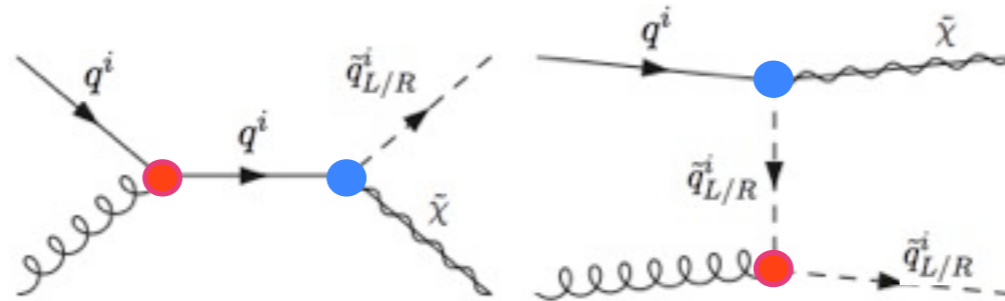
Squark-neutralino at NLO

- Flavor-locked & semi-weak process sensitive to $q\tilde{q}\tilde{\chi}_1$ coupling: $\sigma^{LO} \sim \mathcal{O}(\alpha_{EW}\alpha_s)$



Squark-neutralino at NLO

- Flavor-locked & semi-weak process sensitive to $q\tilde{q}\tilde{\chi}_1$ coupling: $\sigma^{LO} \sim \mathcal{O}(\alpha_{EW}\alpha_s)$



- Couplings size correlated with SUSY breaking:

$$\mathcal{L}_{\tilde{N}_{mass}} = -\frac{1}{2} (\psi^0)^T \mathbf{M}_{\tilde{N}} \psi^0 + c.c.$$

$$\psi^0 = (\tilde{B}, \tilde{W}^0, \tilde{H}_d^0, \tilde{H}_u^0)$$

$$\mathbf{N}^* \mathbf{M}_{\tilde{N}} \mathbf{N}^{-1} = \text{diag}(m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_3^0}, m_{\tilde{\chi}_4^0})$$

$$\mathbf{M}_{\tilde{N}} = \begin{pmatrix} M_1 & 0 & -c_\beta s_W m_Z & s_\beta s_W m_Z \\ 0 & M_2 & c_\beta c_W m_Z & -s_\beta c_W m_Z \\ -c_\beta s_W m_Z & c_\beta c_W m_Z & 0 & -\mu \\ s_\beta s_W m_Z & -s_\beta c_W m_Z & -\mu & 0 \end{pmatrix}$$

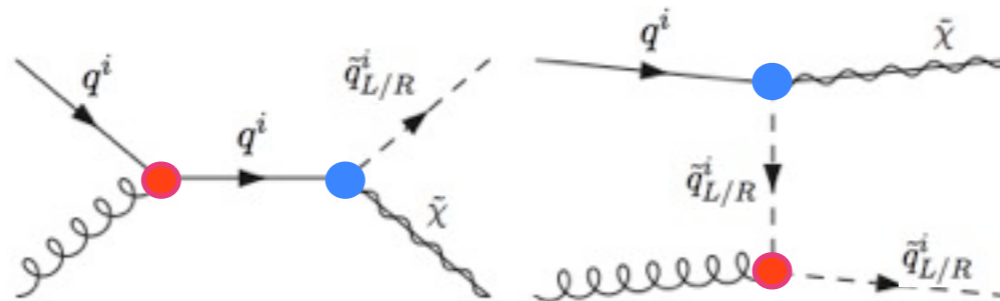
- Msugra models (SPS1-6): typically give $m_Z \lesssim |M_1| \simeq \frac{1}{2}|M_2| \ll |\mu|$

$$\tilde{\chi}_1^0 \simeq \tilde{B} \text{ (Bino like)} \quad \text{e.g. SPS1a } \sigma^{LO}(\tilde{u}_R \tilde{\chi}_1^0) \gg \sigma^{LO}(\tilde{u}_L \tilde{\chi}_1^0), \quad \frac{g_{u\tilde{u}_L \tilde{\chi}_1^0}}{g_{u\tilde{u}_R \tilde{\chi}_1^0}} \approx \frac{1}{6}$$

- Anomaly mediation (SPS9): $M_1 = \frac{F_\phi}{16\pi^2} \frac{33}{5} g_1^2$; $M_2 = \frac{F_\phi}{16\pi^2} g_2^2 \Rightarrow |M_2| \ll |M_1|$

$$\tilde{\chi}_1^0 \simeq \tilde{W} \text{ (Wino like)}$$

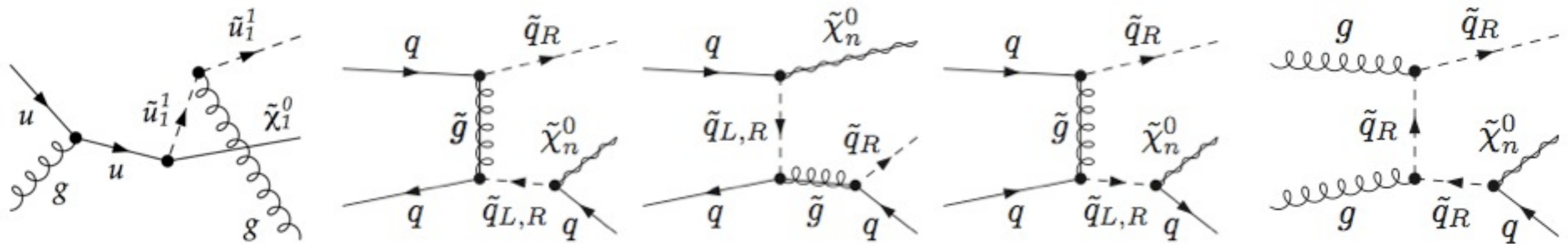
Squark-neutralino at NLO



- Provides information on $q\tilde{q}\tilde{\chi}_1$ coupling
 - Reveals the nature of the LSP (bino or wino-like)
 - Bino (wino) coupling proportional to g' (g)
 - Extra info on this coupling would help DM direct detection bounds
- Recent analysis @LO [Allanach, Grab, Haber arXiv:1010.4261]
Process not yet studied @NLO!
- QCD corrections are quantitatively relevant and important to reduce scale dependence and normalize distributions
- First application of MadGOLEM

Structure of the NLO corrections

Real emission diagrams $pp \rightarrow \tilde{q}\tilde{\chi}_1 j$: quark or gluon emission

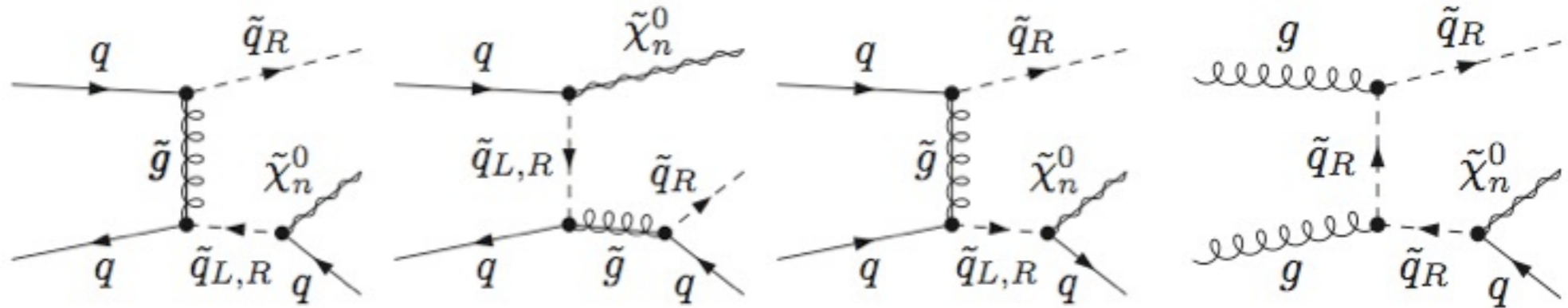
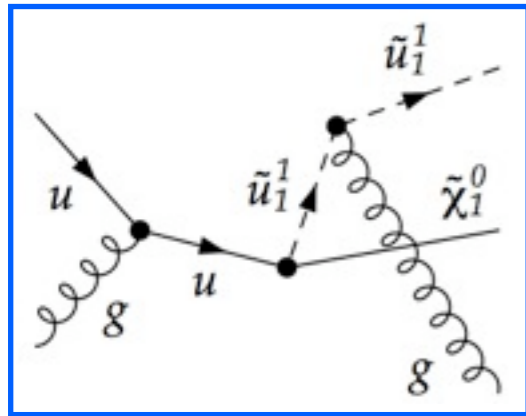


➡ Need Catani-Seymour SUSY dipoles

➡ On-Shell Subtraction Method to avoid double counting

Structure of the NLO corrections

Real emission diagrams $pp \rightarrow \tilde{q}\tilde{\chi}_1^0 j$: quark or gluon emission

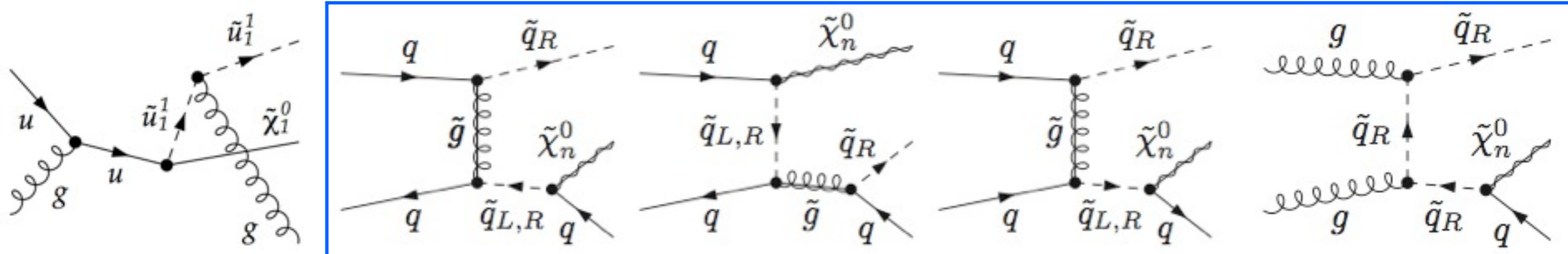


Need Catani-Seymour SUSY dipoles

On-Shell Subtraction Method to avoid double counting

Structure of the NLO corrections

Real emission diagrams $pp \rightarrow \tilde{q}\tilde{\chi}_1^0 j$: quark or gluon emission

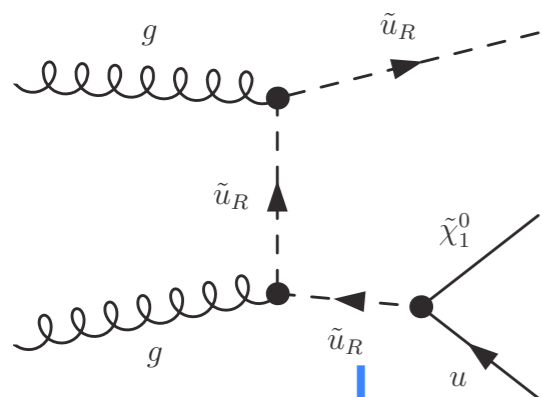


➡ Need Catani-Seymour SUSY dipoles

➡ On-Shell Subtraction Method to avoid double counting

Structure of the NLO corrections

- On-shell subtraction method: differentiation between off & on-shell production to avoid double counting [Beenakker, Hopker, Spira, Zerwas '97] (Prospino scheme)



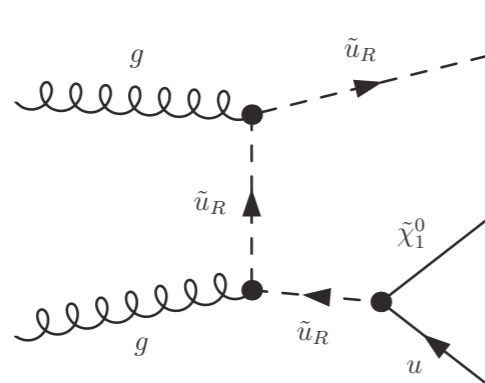
- $gg \rightarrow \tilde{q}\tilde{q}^* \rightarrow \tilde{q}\chi_1^0\bar{q}$ squark neutralino production

- $gg \rightarrow \tilde{q}\tilde{q}^* BR(\tilde{q} \rightarrow \chi_1^0\bar{q})$ squark pair production

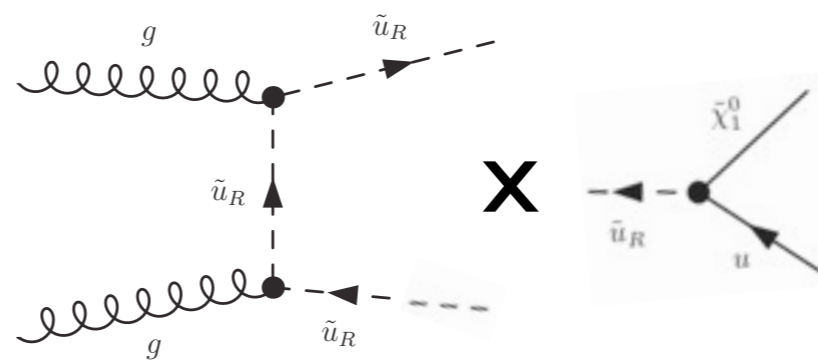
$$\frac{i}{p^2 - m_{os}^2} \rightarrow \frac{i}{p^2 - m_{os}^2 + im_{os}\Gamma_{os}}$$

Γ_{os} is regarded as a **regulator**

- To avoid **double counting** subtract on-shell amplitudes:



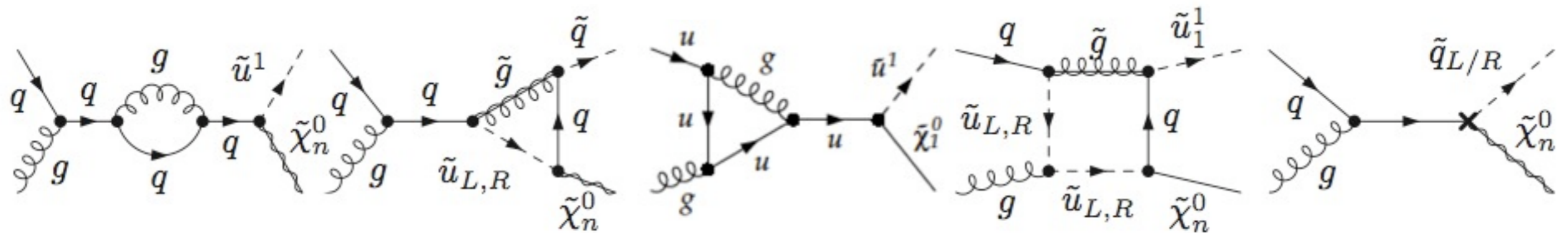
$$\sigma(gg \rightarrow \tilde{q}\chi_1^0\bar{q})$$



$$\sigma(gg \rightarrow \tilde{q}\tilde{q}^*) * BR(\tilde{q} \rightarrow \chi_1^0\bar{q})$$

Structure of the NLO corrections

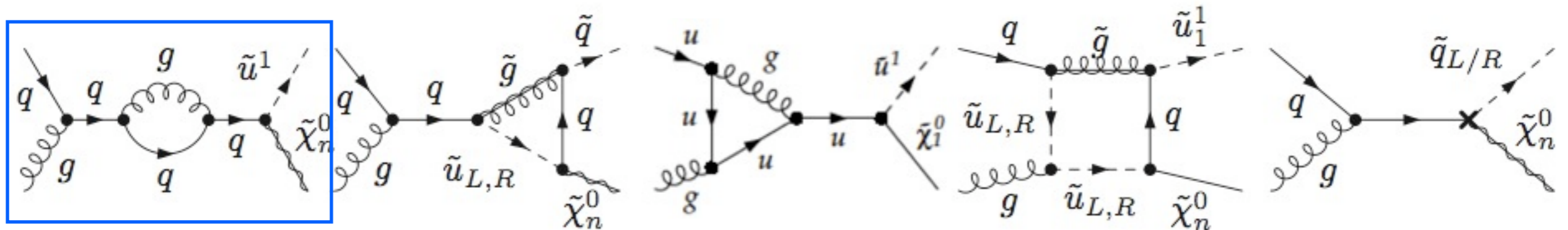
Virtual QCD and SUSY-QCD corrections:



a) self energy corrections; b) vertex corrections; c) box diagrams; d) UV counter terms

Structure of the NLO corrections

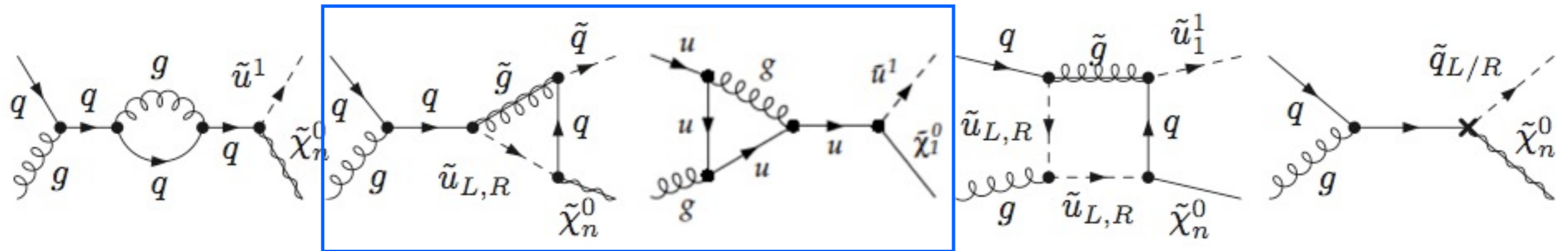
Virtual QCD and SUSY-QCD corrections:



a) self energy corrections; b) vertex corrections; c) box diagrams; d) UV counter terms

Structure of the NLO corrections

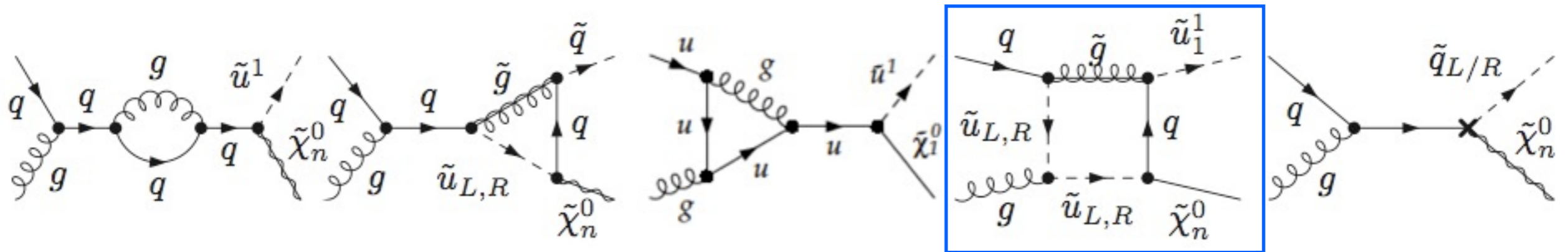
Virtual QCD and SUSY-QCD corrections:



a) self energy corrections; b) vertex corrections; c) box diagrams; d) UV counter terms

Structure of the NLO corrections

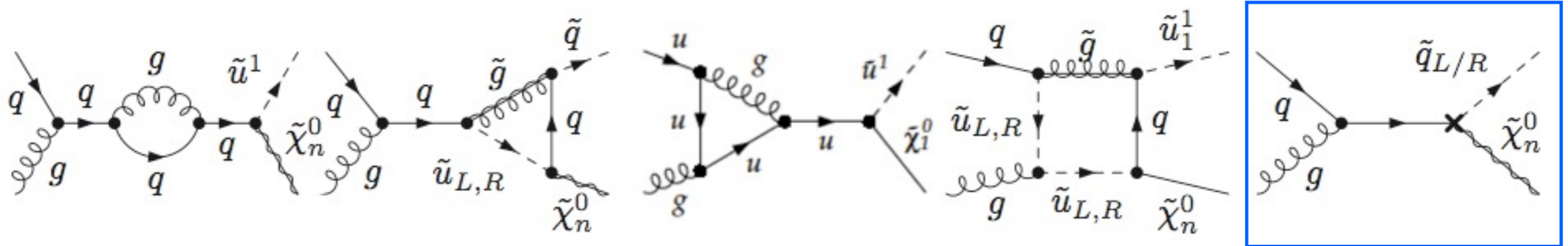
Virtual QCD and SUSY-QCD corrections:



a) self energy corrections; b) vertex corrections; c) box diagrams; d) UV counter terms

Structure of the NLO corrections

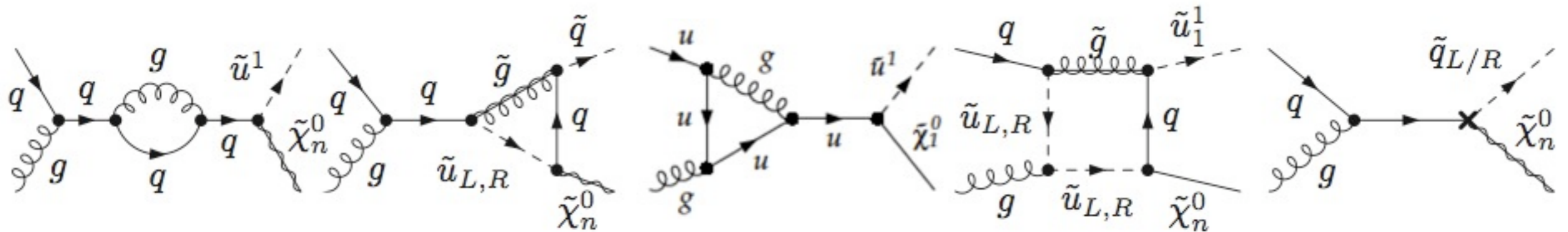
Virtual QCD and SUSY-QCD corrections:



a) self energy corrections; b) vertex corrections; c) box diagrams; d) UV counter terms

Structure of the NLO corrections

Virtual QCD and SUSY-QCD corrections:

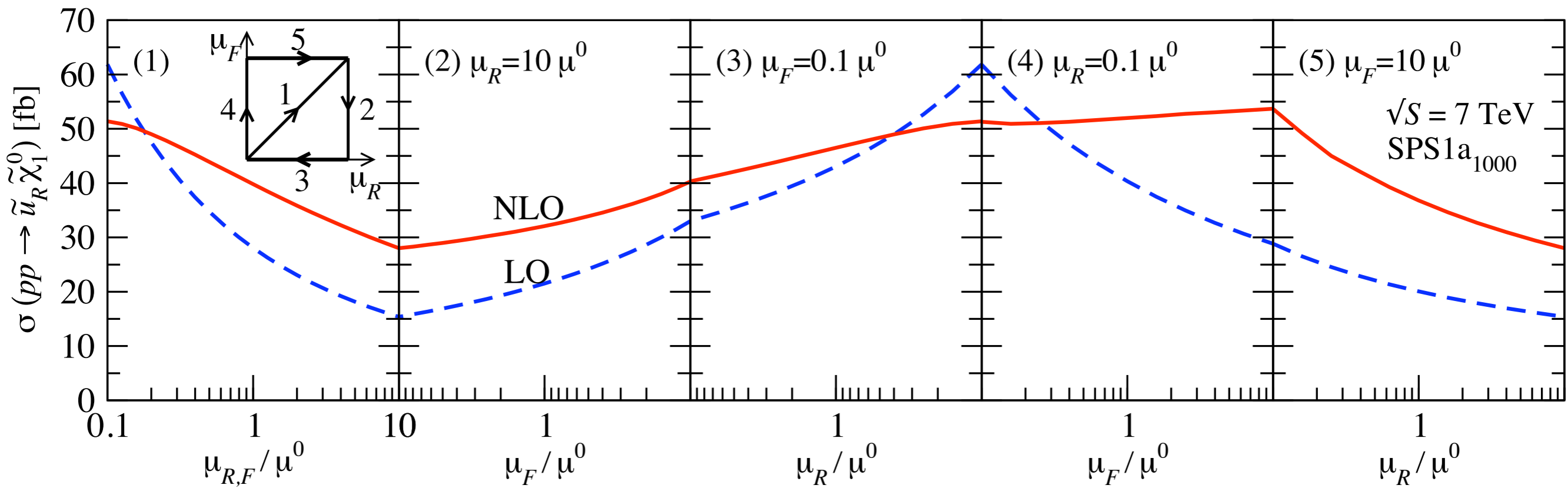


a) self energy corrections; b) vertex corrections; c) box diagrams; d) UV counter terms

After all this have been automatically calculated, let's look at the physics results!

Scale Dependence

Stabilization of the scale dependence on the unphysical μ_R & μ_F



$\frac{\delta\sigma^{NLO}}{\sigma^{NLO}} \leq 20\%$, down from up to $\frac{\delta\sigma^{LO}}{\sigma^{LO}} \leq 70\%$

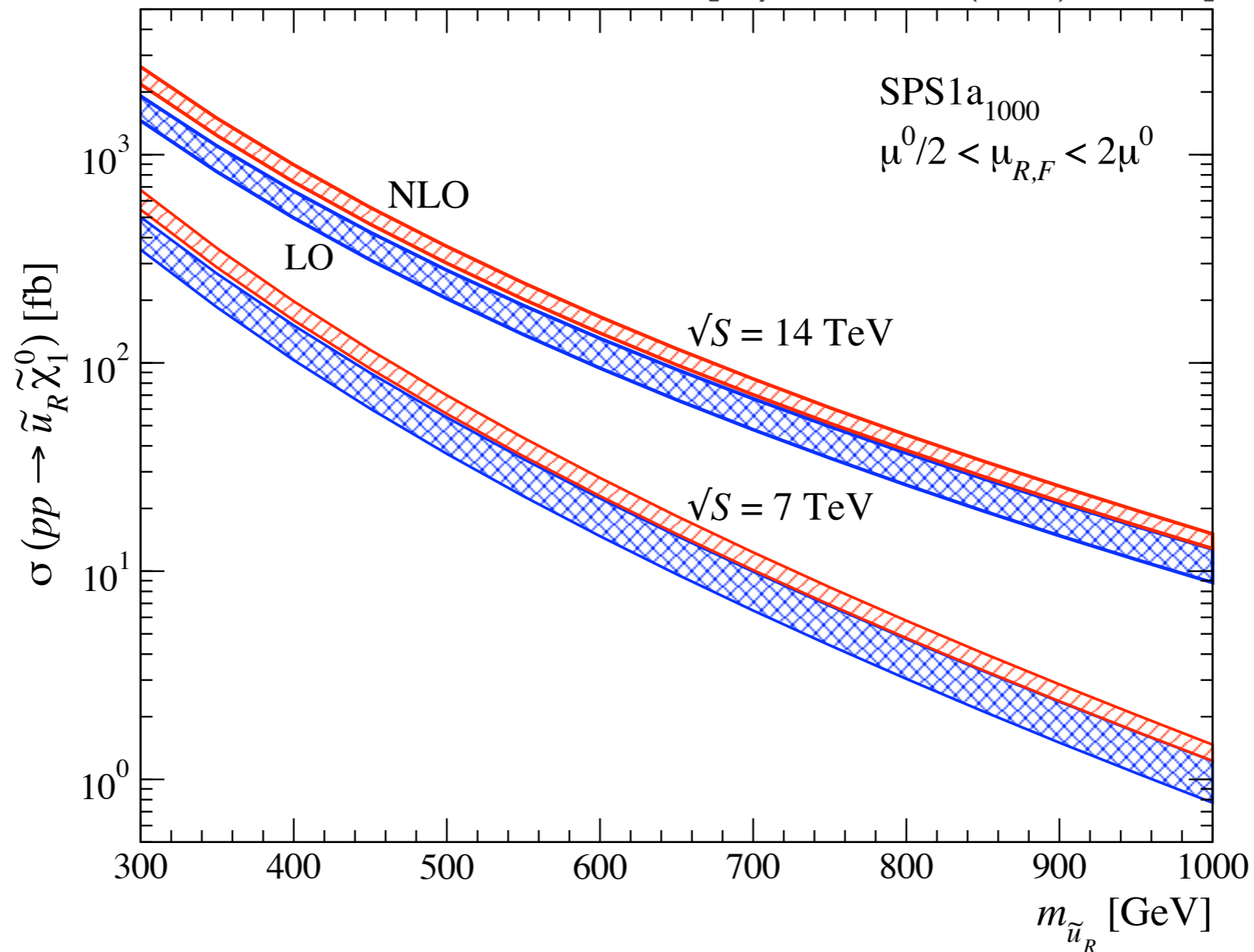
Unlike Drell-Yan-type channels there is μ_R dependence at LO: $\sigma^{LO} \sim \alpha_s$

But doesn't dominate completely the scale dependence as in QCD pair production

T. Binoth, DGN, D. Lopez-Val, T. Plehn, K. Mawatari, I. Wigmore [Phys. Rev. D84 (2011) 075005]

Scale Dependence

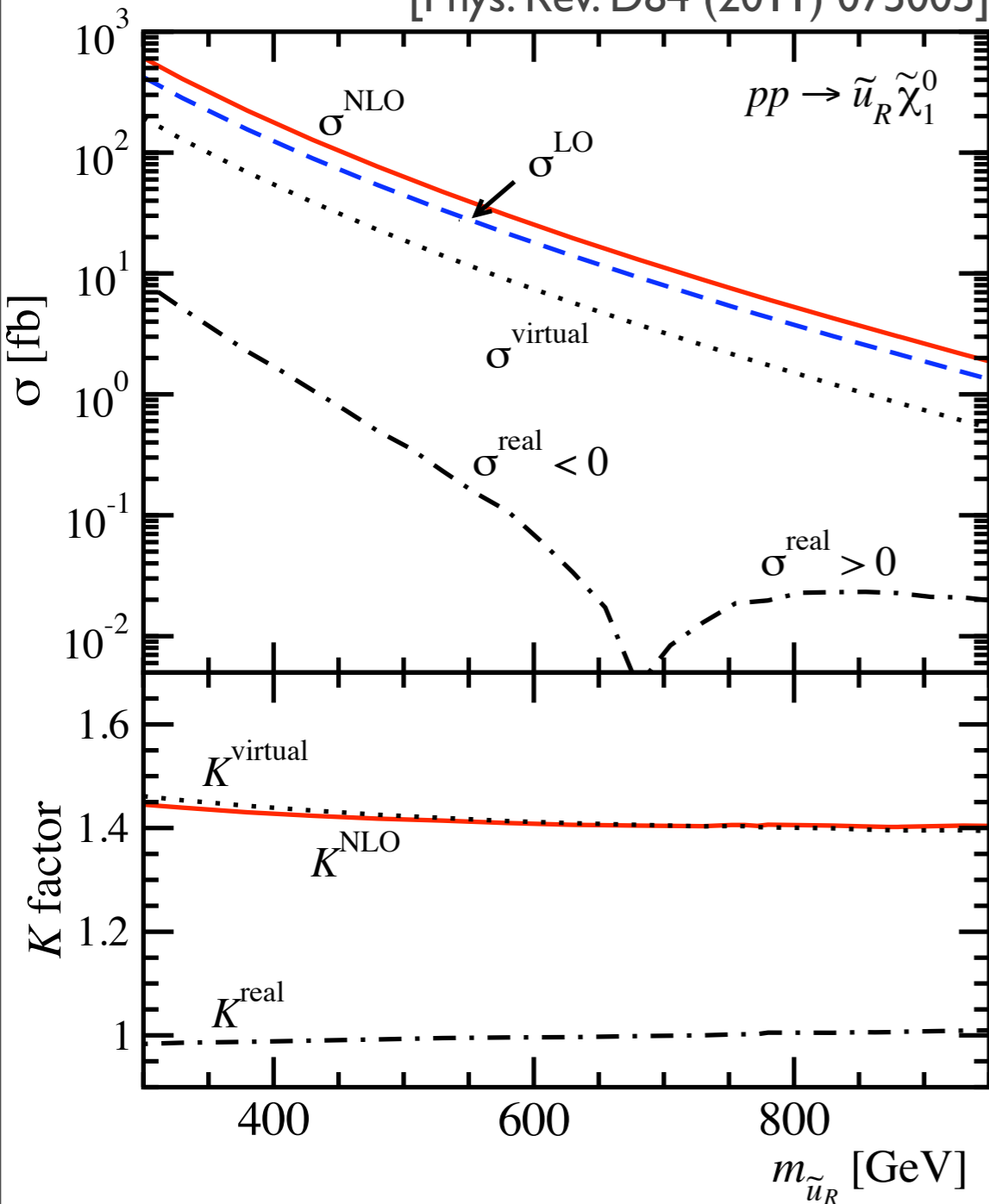
[Phys. Rev. D84 (2011) 075005]



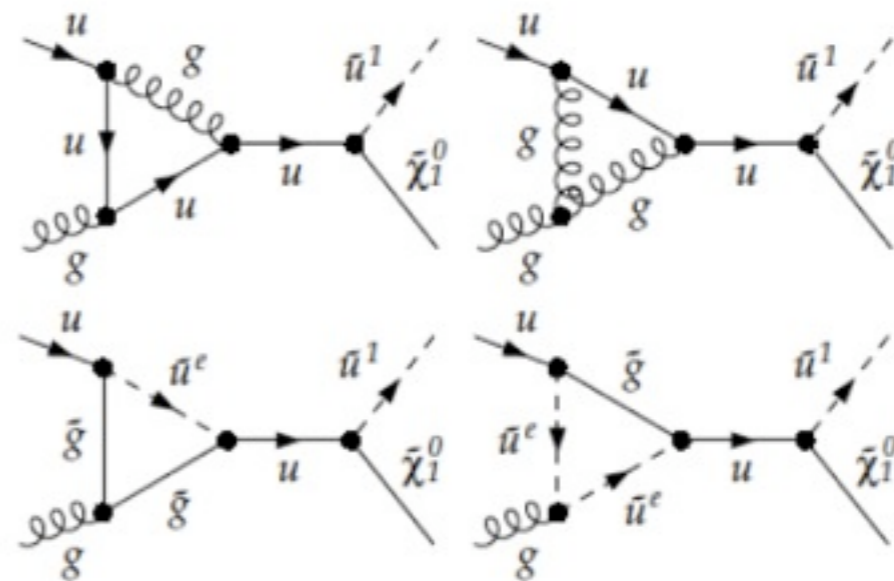
Theory uncertainty largely reduced: $\frac{\delta\sigma^{NLO}}{\sigma^{NLO}} \leq 20\%$, down from up to $\frac{\delta\sigma^{LO}}{\sigma^{LO}} \leq 70\%$

Structure of the NLO corrections

[Phys. Rev. D84 (2011) 075005]

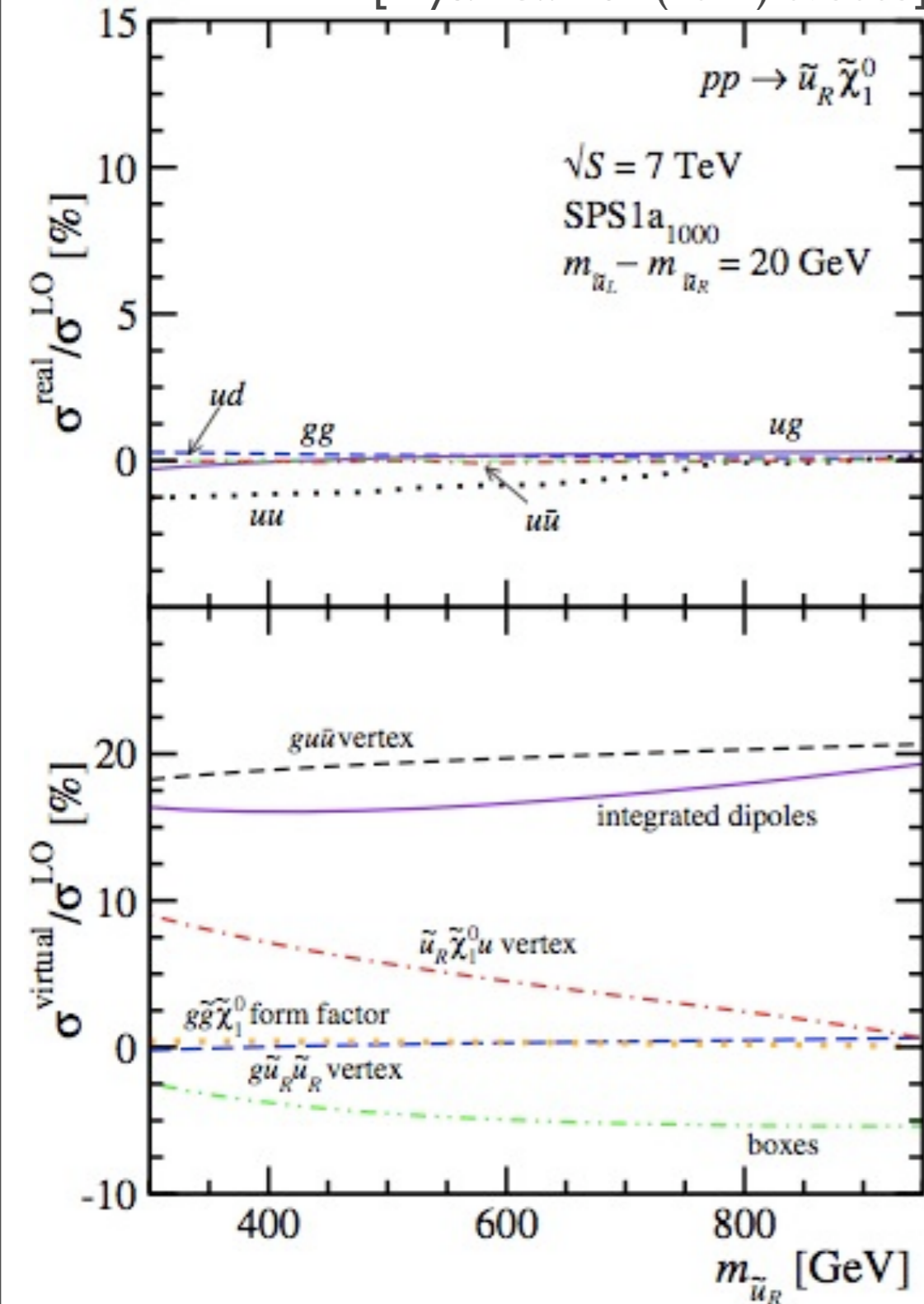


- $u\bar{u}g$ vertex correction basically independent on $m_{\tilde{u}}$
- SQCD effects have a subleading contribution suppressed by $\frac{1}{M_{SUSY}}$
- ➔ Dominance by genuine QCD effects

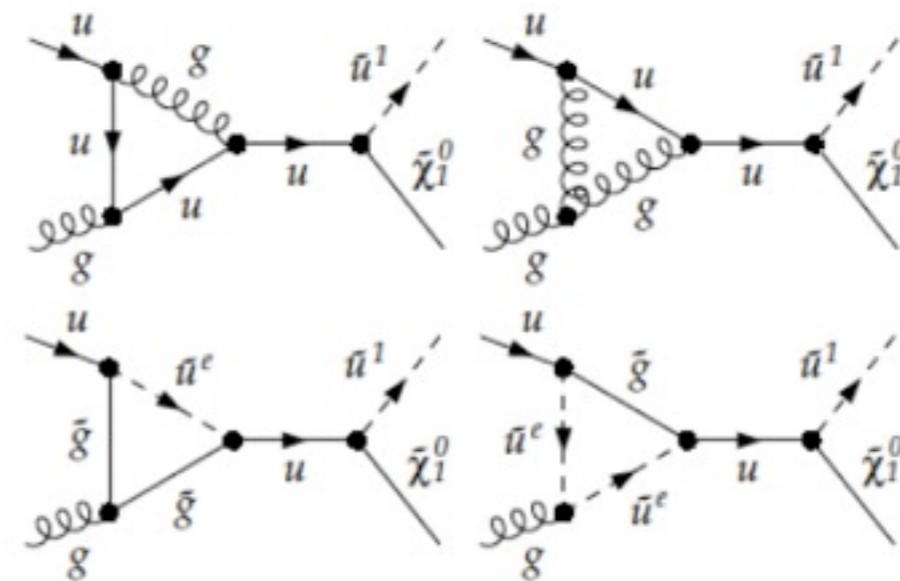


Structure of the NLO corrections

[Phys. Rev. D84 (2011) 075005]



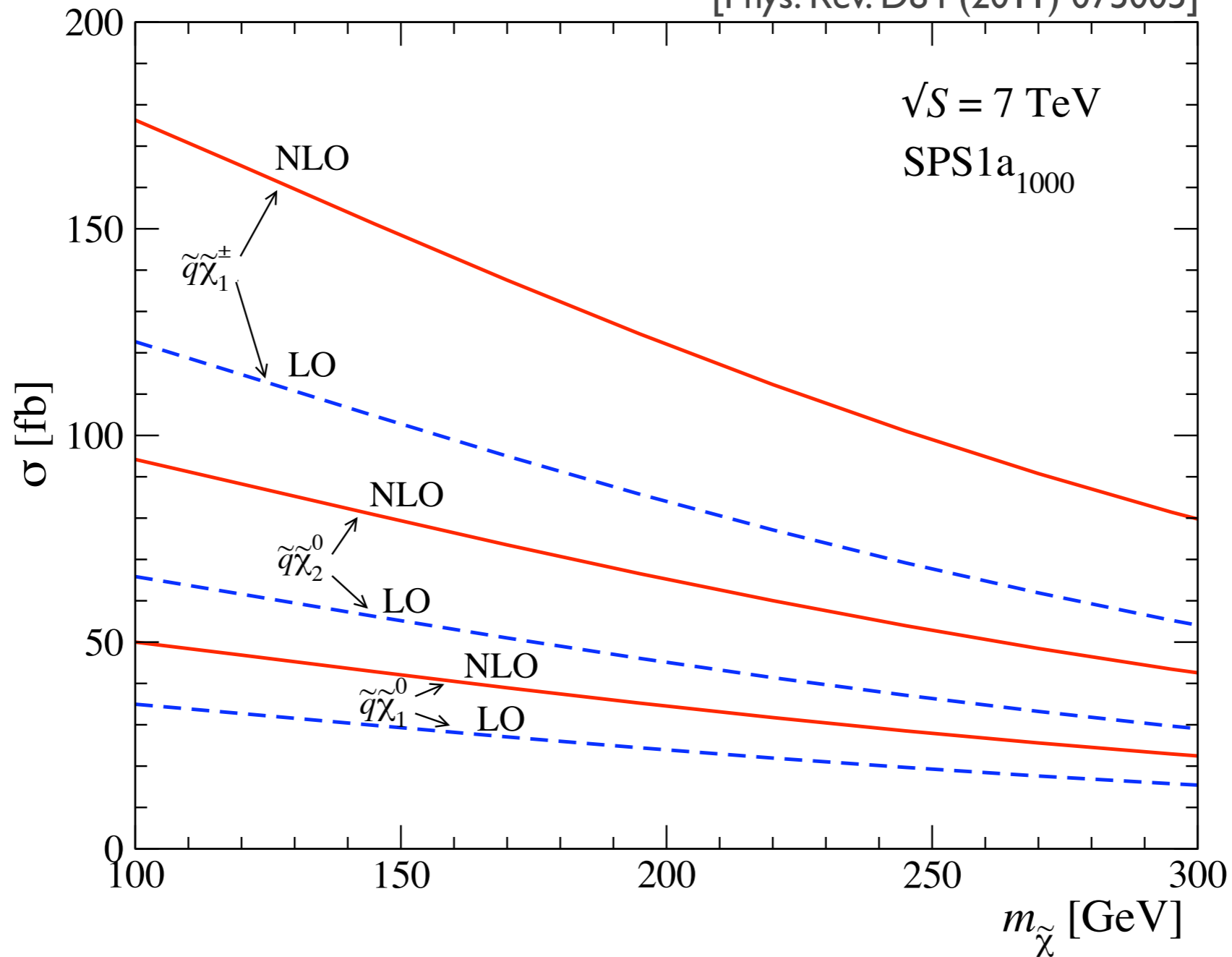
- $u\bar{u}g$ vertex correction basically independent on $m_{\tilde{u}}$
 - SQCD effects have a subleading contribution suppressed by $\frac{1}{M_{SUSY}}$
- ➔ Dominance by genuine QCD effects



squark-gaugino channels

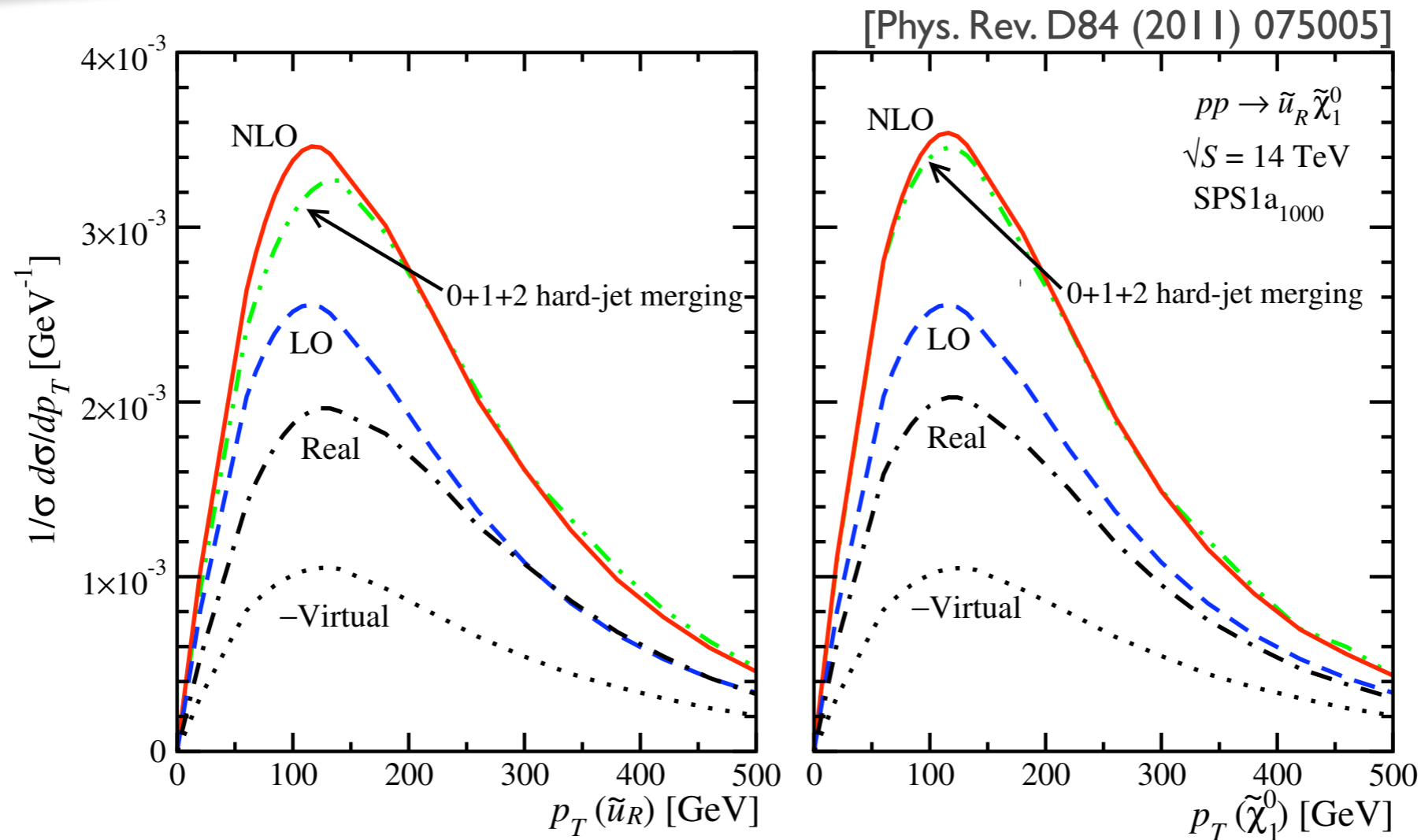
[Phys. Rev. D84 (2011) 075005]

$pp \rightarrow \tilde{q}\tilde{\chi}$



Differences can be traced back to the size of the coupling $g_{q\tilde{q}\tilde{\chi}_1^0}$: $\left(\frac{g_{u\tilde{u}_L\tilde{\chi}_2^0}}{g_{u\tilde{u}_L\tilde{\chi}_1^0}}\right)^2 \sim 1.8$

Comparison with Multi-jet Merging



● Jet merging: combine **ME + Parton Shower** without double counting

Partons are hard
and well separated

Partons are soft/collinear
(resums large logs)

Complementary

● NLO distributions for the heavy final states in good agreement with multi-jet merged calculation via MLM matching with MadGraph5.

Summary

- Structures of the NLO correction

- $pp \rightarrow \tilde{q}\tilde{\chi}_1^0$ @ NLO (First fully automatized BSM NLO computation)

- Source of mono-jets + \cancel{E}_T

- Scale uncertainty largely reduced from 70% @LO to 20% @NLO

- K factors largely insensitive to each SPS point
Dominance from genuine QCD effects

- High K for all SPS points $K \sim 1.4$

- NLO distributions in agreement with MLM matching

- Outlook: All SUSY pair production will be publicly available soon in **MadGOLEM**



MSSM parameter space

	\sqrt{S} [TeV]	σ^{LO} [fb]	σ^{NLO} [fb]	K	$m_{\tilde{u}}$	$m_{\tilde{d}}$	$m_{\tilde{g}}$	$m_{\tilde{\chi}_1^0}$
SPS1a ₁₀₀₀	7	35.27	50.44	1.43	$\tilde{u}_L : 561$	$\tilde{d}_L : 568$	1000	97
	14	215.02	301.27	1.40	$\tilde{u}_R : 549$	$\tilde{d}_R : 545$		
SPS1b	7	2.77	3.99	1.45	$\tilde{u}_L : 872$	$\tilde{d}_L : 878$	938	162
	14	27.21	37.46	1.38	$\tilde{u}_R : 850$	$\tilde{d}_R : 843$		
SPS2	7	0.04	0.07	1.52	$\tilde{u}_L : 1554$	$\tilde{d}_L : 1559$	782	123
	14	1.21	1.64	1.36	$\tilde{u}_R : 1554$	$\tilde{d}_R : 1552$		
SPS3	7	3.15	4.55	1.44	$\tilde{u}_L : 854$	$\tilde{d}_L : 860$	935	161
	14	30.20	41.59	1.38	$\tilde{u}_R : 832$	$\tilde{d}_R : 824$		
SPS4	7	6.44	9.04	1.40	$\tilde{u}_L : 760$	$\tilde{d}_L : 766$	733	120
	14	52.87	71.40	1.35	$\tilde{u}_R : 748$	$\tilde{d}_R : 743$		
SPS5	7	13.26	18.11	1.37	$\tilde{u}_L : 675$	$\tilde{d}_L : 678$	722	120
	14	95.81	132.29	1.38	$\tilde{u}_R : 657$	$\tilde{d}_R : 652$		
SPS6	7	9.84	14.06	1.43	$\tilde{u}_L : 670$	$\tilde{d}_L : 676$	720	190
	14	77.08	107.03	1.39	$\tilde{u}_R : 660$	$\tilde{d}_R : 650$		
SPS7	7	2.19	3.17	1.45	$\tilde{u}_L : 896$	$\tilde{d}_L : 904$	950	163
	14	22.36	30.80	1.38	$\tilde{u}_R : 875$	$\tilde{d}_R : 870$		
SPS8	7	0.65	0.95	1.45	$\tilde{u}_L : 1113$	$\tilde{d}_L : 1122$	839	139
	14	8.73	11.79	1.35	$\tilde{u}_R : 1077$	$\tilde{d}_R : 1072$		
SPS9	7	0.39	0.58	1.49	$\tilde{u}_L : 1276$	$\tilde{d}_L : 1279$	1872	187
	14	7.65	10.42	1.36	$\tilde{u}_R : 1282$	$\tilde{d}_R : 1289$		

● Total cross section strongly depend on the SPS points:

a) Kinematics: dependence on the final state masses in phase space


b) Dynamics: coupling $g_{q\tilde{q}\tilde{\chi}_1^0}$ changes substantially for each scenario

● K factor largely insensitive to the specific SPS point: $K = \sigma^{NLO} / \sigma^{LO} \sim 1.4$

➔ Dominance by genuine QCD effects

Backup slides

\sqrt{S} [TeV]		σ^{LO} [fb]	σ^{NLO} [fb]	K		σ^{LO} [fb]	σ^{NLO} [fb]	K	$m_{\tilde{q}_R}$ [GeV]	$m_{\tilde{q}_L}$ [GeV]
7	$\tilde{u}_R \tilde{\chi}_1^0$	29.62	42.17	1.42	$\tilde{u}_L \tilde{\chi}_1^0$	0.83	1.26	1.52	549	561
14		176.36	245.74	1.39		5.03	7.52	1.49		
7	$\tilde{d}_R \tilde{\chi}_1^0$	3.61	5.31	1.47	$\tilde{d}_L \tilde{\chi}_1^0$	1.21	1.77	1.46	545	568
14		24.89	35.50	1.43		8.67	12.37	1.43		
7	$\tilde{c}_R \tilde{\chi}_1^0$	1.12	1.81	1.61	$\tilde{c}_L \tilde{\chi}_1^0$	0.03	0.06	2.00	549	561
14		13.69	20.69	1.51		0.38	0.66	1.70		
7	$\tilde{s}_R \tilde{\chi}_1^0$	0.57	0.78	1.38	$\tilde{s}_L \tilde{\chi}_1^0$	0.19	0.29	1.56	545	568
14		5.86	8.45	1.44		2.00	2.98	1.49		
7	$\sum \tilde{q}_R \tilde{\chi}_1^0$	34.92	50.07	1.43	$\sum \tilde{q}_L \tilde{\chi}_1^0$	2.26	3.38	1.50		
14		220.80	310.38	1.41		16.08	23.53	1.46		


 $SPS1a_{1000}$ has bino like neutralino $\left(\frac{g_{u\tilde{u}_L\tilde{\chi}_1^0}}{g_{u\tilde{u}_R\tilde{\chi}_1^0}} \right) \sim \frac{1}{6} \Rightarrow \sigma(\tilde{u}_R\tilde{\chi}_1^0) \gg \sigma(\tilde{u}_L\tilde{\chi}_1^0)$

Backup slides

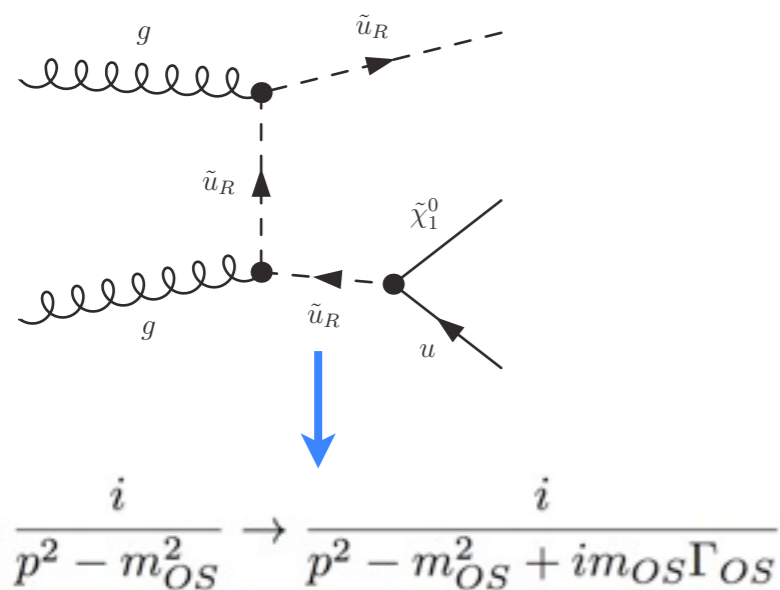
$$\sigma^{Real}(\Gamma_{os}) = \int_{n+1} d\Phi_{n+1} [(|\mathcal{M}_{res}|^2 - d\sigma^{os}) + 2\text{Re}[\mathcal{M}_{res}^* \mathcal{M}_{rem}] + |\mathcal{M}_{rem}|^2 - d\sigma^A]$$

 gg>urnlux

On-Shell Subtraction

SPS1a gg>urnlux

1 possible OS particle: **ur**



Γ_{OS} is a regulator!

