

Collective Escape of Cosmic Rays from their Acceleration Sites

Mikhail Malkov

UCSD

Collaborators: F. Aharonian, P. Diamond,
I. Moskalenko and R. Sagdeev

- 1 Why CR Escape is important
 - Observational significance of CR escape
 - The role of escape in acceleration theory
 - Escape and proof of SNR origin of CR
- 2 Approaches to CR escape from accelerators
 - TP/self-confinement
- 3 Formulation of the Problem/Technique
 - Geometry/Equations
- 4 Results/Discussion of Observations/Summary
 - Self-similar solution/SNR W44

- 1 Why CR Escape is important
 - Observational significance of CR escape
 - The role of escape in acceleration theory
 - Escape and proof of SNR origin of CR
- 2 Approaches to CR escape from accelerators
 - TP/self-confinement
- 3 Formulation of the Problem/Technique
 - Geometry/Equations
- 4 Results/Discussion of Observations/Summary
 - Self-similar solution/SNR W44

Understanding accelerator by observing CR escape

- nearby molecular clouds (MC) illuminated by escaping CR probe accelerator (e.g. SNR)
- escape spectrum may considerably deviate from the source spectrum (source reconstruction problem)
- escape geometry is complicated (field aligned vs isotropic)
- morphology of emission from SNR dense gas surroundings probe magnetic field configuration around the source
- calculation of flux of escaping CRs, understanding geometry of escape provide access to (indirect) source calorimetry by measuring emission flux from illuminated MC

Understanding accelerator by observing CR escape

- nearby molecular clouds (MC) illuminated by escaping CR probe accelerator (e.g. SNR)
- escape spectrum may considerably deviate from the source spectrum (source reconstruction problem)
- escape geometry is complicated (field aligned vs isotropic)
- morphology of emission from SNR dense gas surroundings probe magnetic field configuration around the source
- calculation of flux of escaping CRs, understanding geometry of escape provide access to (indirect) source calorimetry by measuring emission flux from illuminated MC

Understanding accelerator by observing CR escape

- nearby molecular clouds (MC) illuminated by escaping CR probe accelerator (e.g. SNR)
- escape spectrum may considerably deviate from the source spectrum (source reconstruction problem)
- escape geometry is complicated (field aligned vs isotropic)
- morphology of emission from SNR dense gas surroundings probe magnetic field configuration around the source
- calculation of flux of escaping CRs, understanding geometry of escape provide access to (indirect) source calorimetry by measuring emission flux from illuminated MC

Understanding accelerator by observing CR escape

- nearby molecular clouds (MC) illuminated by escaping CR probe accelerator (e.g. SNR)
- escape spectrum may considerably deviate from the source spectrum (source reconstruction problem)
- escape geometry is complicated (field aligned vs isotropic)
- morphology of emission from SNR dense gas surroundings probe magnetic field configuration around the source
- calculation of flux of escaping CRs, understanding geometry of escape provide access to (indirect) source calorimetry by measuring emission flux from illuminated MC

Understanding accelerator by observing CR escape

- nearby molecular clouds (MC) illuminated by escaping CR probe accelerator (e.g. SNR)
- escape spectrum may considerably deviate from the source spectrum (source reconstruction problem)
- escape geometry is complicated (field aligned vs isotropic)
- morphology of emission from SNR dense gas surroundings probe magnetic field configuration around the source
- calculation of flux of escaping CRs, understanding geometry of escape provide access to (indirect) source calorimetry by measuring emission flux from illuminated MC

- 1 Why CR Escape is important
 - Observational significance of CR escape
 - The role of escape in acceleration theory
 - Escape and proof of SNR origin of CR
- 2 Approaches to CR escape from accelerators
 - TP/self-confinement
- 3 Formulation of the Problem/Technique
 - Geometry/Equations
- 4 Results/Discussion of Observations/Summary
 - Self-similar solution/SNR W44

CR escape/confinement and diffusive shock acceleration (DSA) theory

- CR escape/confinement is an integral, **but poorly understood**, part of acceleration theory
- strongly influences the spectrum, particularly cut-off energy
- as the **DSA**¹ is based on **self-confinement** the escape theory must also be
- escaping particles drive (Alfvén) waves that slow down the escape
- the level of self-excited waves is orders of magnitude higher than the ISM background turbulence level at relevant scales
- test particle escape theory is irrelevant near the accelerator where $\delta B \gg \delta B_{\text{ISM}}$

¹ Bell's talk on Monday, Bykov's this morning **other talks this session**

CR escape/confinement and diffusive shock acceleration (DSA) theory

- CR escape/confinement is an integral, **but poorly understood**, part of acceleration theory
- strongly influences the spectrum, particularly cut-off energy
- as the **DSA**¹ is based on **self-confinement** the escape theory must also be
- escaping particles drive (Alfvén) waves that slow down the escape
- the level of self-excited waves is orders of magnitude higher than the ISM background turbulence level at relevant scales
- test particle escape theory is irrelevant near the accelerator where $\delta B \gg \delta B_{\text{ISM}}$

¹ Bell's talk on Monday, Bykov's this morning **other talks this session**

CR escape/confinement and diffusive shock acceleration (DSA) theory

- CR escape/confinement is an integral, **but poorly understood**, part of acceleration theory
- strongly influences the spectrum, particularly cut-off energy
- as the **DSA**¹ is based on **self-confinement** the escape theory must also be
- escaping particles drive (Alfvén) waves that slow down the escape
- the level of self-excited waves is orders of magnitude higher than the ISM background turbulence level at relevant scales
- test particle escape theory is irrelevant near the accelerator where $\delta B \gg \delta B_{\text{ISM}}$

¹ Bell's talk on Monday, Bykov's this morning other talks this session

CR escape/confinement and diffusive shock acceleration (DSA) theory

- CR escape/confinement is an integral, **but poorly understood**, part of acceleration theory
- strongly influences the spectrum, particularly cut-off energy
- as the **DSA**¹ is based on **self-confinement** the escape theory must also be
- escaping particles drive (Alfvén) waves that slow down the escape
- the level of self-excited waves is orders of magnitude higher than the ISM background turbulence level at relevant scales
- test particle escape theory is irrelevant near the accelerator where $\delta B \gg \delta B_{\text{ISM}}$

¹ Bell's talk on Monday, Bykov's this morning other talks this session

CR escape/confinement and diffusive shock acceleration (DSA) theory

- CR escape/confinement is an integral, **but poorly understood**, part of acceleration theory
- strongly influences the spectrum, particularly cut-off energy
- as the **DSA**¹ is based on **self-confinement** the escape theory must also be
- escaping particles drive (Alfvén) waves that slow down the escape
- the level of self-excited waves is orders of magnitude higher than the ISM background turbulence level at relevant scales
- test particle escape theory is irrelevant near the accelerator where $\delta B \gg \delta B_{\text{ISM}}$

¹ Bell's talk on Monday, Bykov's this morning other talks this session

CR escape/confinement and diffusive shock acceleration (DSA) theory

- CR escape/confinement is an integral, **but poorly understood**, part of acceleration theory
- strongly influences the spectrum, particularly cut-off energy
- as the **DSA**¹ is based on **self-confinement** the escape theory must also be
- escaping particles drive (Alfvén) waves that slow down the escape
- the level of self-excited waves is orders of magnitude higher than the ISM background turbulence level at relevant scales
- test particle escape theory is irrelevant near the accelerator where $\delta B \gg \delta B_{\text{ISM}}$

¹ **Bell's talk on Monday, Bykov's this morning other talks this session** 

- 1 Why CR Escape is important
 - Observational significance of CR escape
 - The role of escape in acceleration theory
 - Escape and proof of SNR origin of CR
- 2 Approaches to CR escape from accelerators
 - TP/self-confinement
- 3 Formulation of the Problem/Technique
 - Geometry/Equations
- 4 Results/Discussion of Observations/Summary
 - Self-similar solution/SNR W44

- electrons are known to be accelerated in SNR
- protons should be accelerated by the same mechanism in much larger amounts but radiatively poorly expressed
- visibility of CR protons depends on environment (dense gas required for pp collisions and detectable γ -emission) and their escape into this environment
- without understanding CR escape it is hard to disentangle $pp \rightarrow \pi^0 \rightarrow \gamma$ channel from electron inverse Compton emission and to proof the SNR origin of CR protons
- electrons are parasitically confined by proton generated waves and (modulo wave polarization²) are transported similarly to the protons of the same rigidity
- however, different targets for γ production: gas/photons: magnetic connectivity of gas with the CR source should be instrumental in $e - p$ disentangling

²unlikely to be important

- electrons are known to be accelerated in SNR
- protons should be accelerated by the same mechanism in much larger amounts but radiatively poorly expressed
- visibility of CR protons depends on environment (dense gas required for pp collisions and detectable γ -emission) and their escape into this environment
- without understanding CR escape it is hard to disentangle $pp \rightarrow \pi^0 \rightarrow \gamma$ channel from electron inverse Compton emission and to proof the SNR origin of CR protons
- electrons are parasitically confined by proton generated waves and (modulo wave polarization²) are transported similarly to the protons of the same rigidity
- however, different targets for γ production: gas/photons: magnetic connectivity of gas with the CR source should be instrumental in $e - p$ disentangling

²unlikely to be important

- electrons are known to be accelerated in SNR
- protons should be accelerated by the same mechanism in much larger amounts but radiatively poorly expressed
- visibility of CR protons depends on environment (dense gas required for pp collisions and detectable γ -emission) and their escape into this environment
- without understanding CR escape it is hard to disentangle $pp \rightarrow \pi^0 \rightarrow \gamma$ channel from electron inverse Compton emission and to proof the SNR origin of CR protons
- electrons are parasitically confined by proton generated waves and (modulo wave polarization²) are transported similarly to the protons of the same rigidity
- however, different targets for γ production: gas/photons: magnetic connectivity of gas with the CR source should be instrumental in $e - p$ disentangling

²unlikely to be important

- electrons are known to be accelerated in SNR
- protons should be accelerated by the same mechanism in much larger amounts but radiatively poorly expressed
- visibility of CR protons depends on environment (dense gas required for pp collisions and detectable γ -emission) and their escape into this environment
- without understanding CR escape it is hard to disentangle $pp \rightarrow \pi^0 \rightarrow \gamma$ channel from electron inverse Compton emission and to proof the SNR origin of CR protons
- electrons are parasitically confined by proton generated waves and (modulo wave polarization²) are transported similarly to the protons of the same rigidity
- however, different targets for γ production: gas/photons: magnetic connectivity of gas with the CR source should be instrumental in $e - p$ disentangling

²unlikely to be important

- electrons are known to be accelerated in SNR
- protons should be accelerated by the same mechanism in much larger amounts but radiatively poorly expressed
- visibility of CR protons depends on environment (dense gas required for pp collisions and detectable γ -emission) and their escape into this environment
- without understanding CR escape it is hard to disentangle $pp \rightarrow \pi^0 \rightarrow \gamma$ channel from electron inverse Compton emission and to proof the SNR origin of CR protons
- electrons are parasitically confined by proton generated waves and (modulo wave polarization²) are transported similarly to the protons of the same rigidity
- however, different targets for γ production: gas/photons: magnetic connectivity of gas with the CR source should be instrumental in $e - p$ disentangling

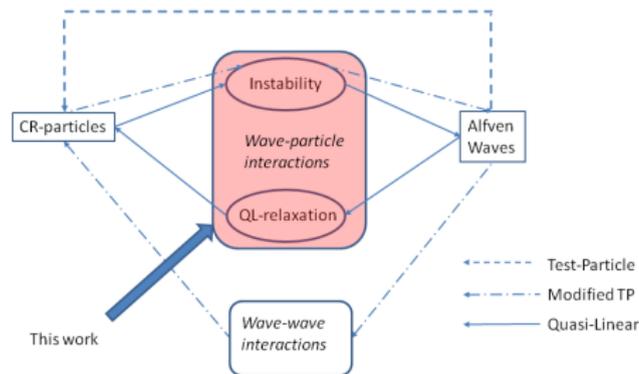
²unlikely to be important

- electrons are known to be accelerated in SNR
- protons should be accelerated by the same mechanism in much larger amounts but radiatively poorly expressed
- visibility of CR protons depends on environment (dense gas required for pp collisions and detectable γ -emission) and their escape into this environment
- without understanding CR escape it is hard to disentangle $pp \rightarrow \pi^0 \rightarrow \gamma$ channel from electron inverse Compton emission and to proof the SNR origin of CR protons
- electrons are parasitically confined by proton generated waves and (modulo wave polarization²) are transported similarly to the protons of the same rigidity
- however, different targets for γ production: gas/photons: magnetic connectivity of gas with the CR source should be instrumental in $e - p$ disentangling

²unlikely to be important

- 1 Why CR Escape is important
 - Observational significance of CR escape
 - The role of escape in acceleration theory
 - Escape and proof of SNR origin of CR
- 2 Approaches to CR escape from accelerators
 - TP/self-confinement
- 3 Formulation of the Problem/Technique
 - Geometry/Equations
- 4 Results/Discussion of Observations/Summary
 - Self-similar solution/SNR W44

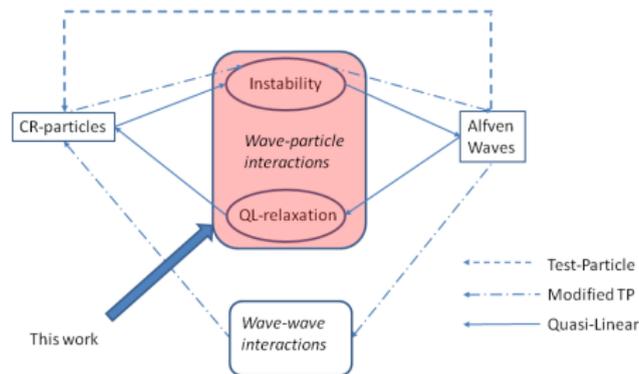
From test particle (TP) scattering to self-confinement



Three levels of treatment of
CR escape/propagation

- CR diffusion in preexisting ISM turbulence
- CR diffusion in nonlinearly evolving turbulence
- quasi-linear relaxation of localized CR cloud on self-generated waves

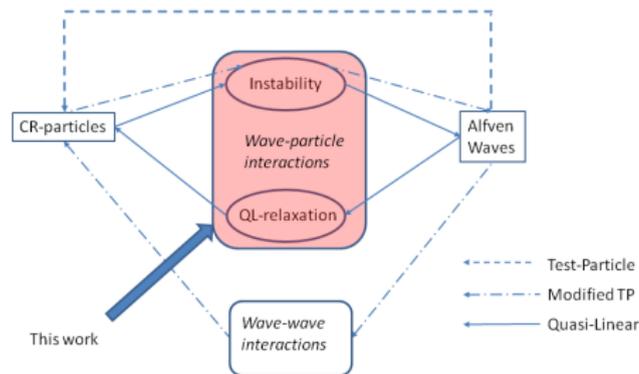
From test particle (TP) scattering to self-confinement



Three levels of treatment of
CR escape/propagation

- CR diffusion in preexisting ISM turbulence
- CR diffusion in nonlinearly evolving turbulence
- quasi-linear relaxation of localized CR cloud on self-generated waves

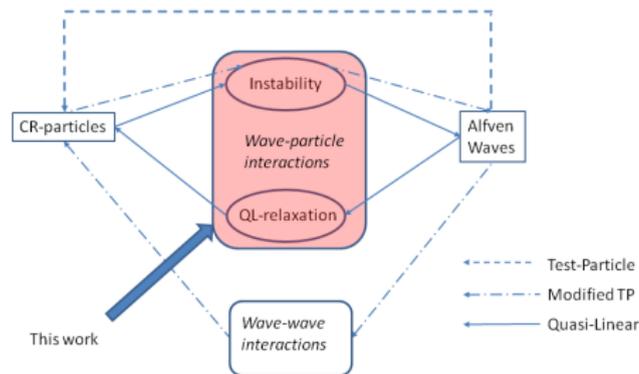
From test particle (TP) scattering to self-confinement



Three levels of treatment of
CR escape/propagation

- CR diffusion in preexisting ISM turbulence
- CR diffusion in nonlinearly evolving turbulence
- quasi-linear relaxation of localized CR cloud on self-generated waves

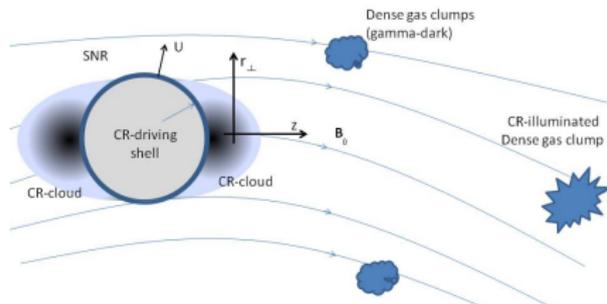
From test particle (TP) scattering to self-confinement



Three levels of treatment of
CR escape/propagation

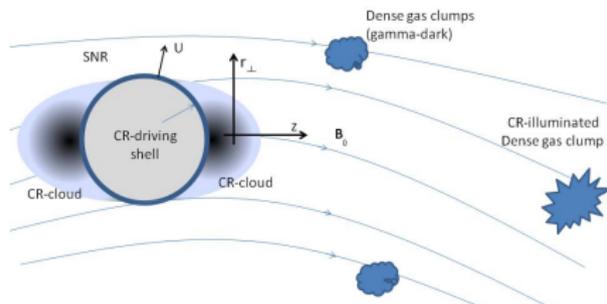
- CR diffusion in preexisting ISM turbulence
- CR diffusion in nonlinearly evolving turbulence
- quasi-linear relaxation of localized CR cloud on self-generated waves

- 1 Why CR Escape is important
 - Observational significance of CR escape
 - The role of escape in acceleration theory
 - Escape and proof of SNR origin of CR
- 2 Approaches to CR escape from accelerators
 - TP/self-confinement
- 3 Formulation of the Problem/Technique
 - Geometry/Equations
- 4 Results/Discussion of Observations/Summary
 - Self-similar solution/SNR W44



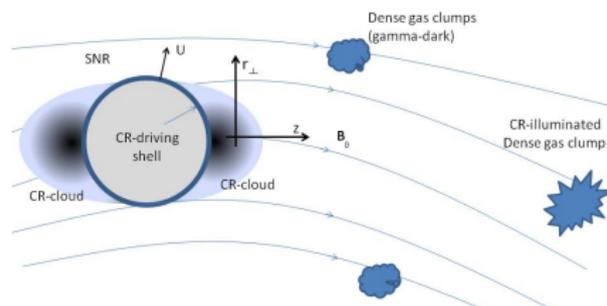
CR escape along MF from
two polar cusps of SNR

- CR diffuse along MF
- generate Alfvén waves that suppress diffusion
- to obtain CR distribution both processes are treated self-consistently
- result will determine MC emissivity



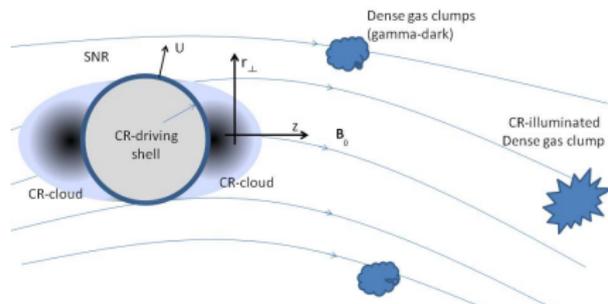
CR escape along MF from
two polar cusps of SNR

- CR diffuse along MF
- generate Alfvén waves that suppress diffusion
- to obtain CR distribution both processes are treated self-consistently
- result will determine MC emissivity



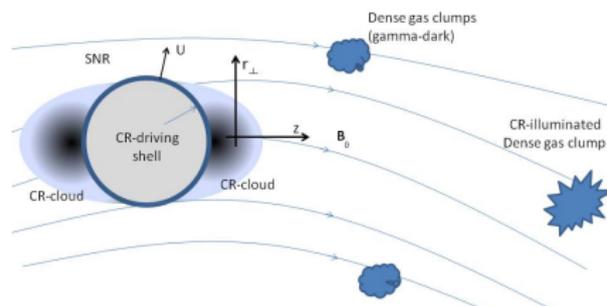
CR escape along MF from two polar cusps of SNR

- CR diffuse along MF
- generate Alfvén waves that suppress diffusion
- to obtain CR distribution both processes are treated self-consistently
- result will determine MC emissivity



CR escape along MF from
two polar cusps of SNR

- CR diffuse along MF
- generate Alfvén waves that suppress diffusion
- to obtain CR distribution both processes are treated self-consistently
- result will determine MC emissivity



CR escape along MF from
two polar cusps of SNR

- CR diffuse along MF
- generate Alfvén waves that suppress diffusion
- to obtain CR distribution both processes are treated self-consistently
- result will determine MC emissivity

- CR propagation in self-excited waves

$$\frac{d}{dt} P_{\text{CR}}(\rho) = \frac{\partial}{\partial z} \frac{\kappa_{\text{B}}}{l} \frac{\partial P_{\text{CR}}}{\partial z}$$

$P_{\text{CR}}(\rho)$ -partial pressure, $l(\rho)$ -wave energy, resonance $k\rho = eB_0/c$,
 $d/dt = [\partial/\partial t + (U + C_A)\partial/\partial z]$

- Wave generation by ∇P_{CR} associated with the CR pitch-angle anisotropy

$$\frac{d}{dt} l = -C_A \frac{\partial P_{\text{CR}}}{\partial z} - \Gamma l$$

- QL integral

$$P_{\text{CR}}(z, t) = P_{\text{CR}0}(z') - \frac{\kappa_{\text{B}}}{C_A} \frac{\partial}{\partial z} \ln \frac{l(z, t)}{l_0(z')}$$

$$z' = z - (U + C_A)t$$

- CR propagation in self-excited waves

$$\frac{d}{dt} P_{\text{CR}}(\rho) = \frac{\partial}{\partial z} \frac{\kappa_{\text{B}}}{l} \frac{\partial P_{\text{CR}}}{\partial z}$$

$P_{\text{CR}}(\rho)$ -partial pressure, $l(\rho)$ -wave energy, resonance $k\rho = eB_0/c$,
 $d/dt = [\partial/\partial t + (U + C_A)\partial/\partial z]$

- Wave generation by ∇P_{CR} associated with the CR pitch-angle anisotropy

$$\frac{d}{dt} l = -C_A \frac{\partial P_{\text{CR}}}{\partial z} - \Gamma l$$

- QL integral

$$P_{\text{CR}}(z, t) = P_{\text{CR}0}(z') - \frac{\kappa_{\text{B}}}{C_A} \frac{\partial}{\partial z} \ln \frac{l(z, t)}{l_0(z')}$$

$$z' = z - (U + C_A)t$$

- CR propagation in self-excited waves

$$\frac{d}{dt} P_{\text{CR}}(\rho) = \frac{\partial}{\partial z} \frac{\kappa_{\text{B}}}{l} \frac{\partial P_{\text{CR}}}{\partial z}$$

$P_{\text{CR}}(\rho)$ -partial pressure, $l(\rho)$ -wave energy, resonance $kp = eB_0/c$,
 $d/dt = [\partial/\partial t + (U + C_A) \partial/\partial z]$

- Wave generation by ∇P_{CR} associated with the CR pitch-angle anisotropy

$$\frac{d}{dt} l = -C_A \frac{\partial P_{\text{CR}}}{\partial z} - \Gamma l$$

- QL integral

$$P_{\text{CR}}(z, t) = P_{\text{CR}0}(z') - \frac{\kappa_{\text{B}}}{C_A} \frac{\partial}{\partial z} \ln \frac{l(z, t)}{l_0(z')}$$

$$z' = z - (U + C_A) t$$

Reduction of Equations

- CR/Alfven wave coupling

$$\frac{\partial W}{\partial t} - \frac{\partial}{\partial z} \frac{1}{W} \frac{\partial W}{\partial z} = -\frac{\partial}{\partial z} \mathcal{P}_0(z)$$

$W = \frac{c_A^2(\rho)}{\kappa_B(\rho)}$ -dimensionless wave energy, $d/dt \approx \partial/\partial t$, \mathcal{P}_0 -initial CR distribution, $|z/a| < 1$

- Self-similar solution in variable $\zeta = z/\sqrt{t}$, $W(z, t) = w(\zeta)$ for $|z| > a$, outside initial CR cloud

$$\frac{d}{d\zeta} \frac{1}{w} \frac{dw}{d\zeta} + \frac{\zeta}{2} \frac{dw}{d\zeta} = 0$$

- solution depends on integrated CR pressure in the cloud and background turbulence level $W_0 \ll 1$.

$$\Pi = \int_0^1 \mathcal{P}_0 dz \gg 1$$

Reduction of Equations

- CR/Alfven wave coupling

$$\frac{\partial W}{\partial t} - \frac{\partial}{\partial z} \frac{1}{W} \frac{\partial W}{\partial z} = -\frac{\partial}{\partial z} \mathcal{P}_0(z)$$

$W = \frac{c_A a(\rho)}{\kappa_B(\rho)}$ -dimensionless wave energy, $d/dt \approx \partial/\partial t$, \mathcal{P}_0 -initial CR distribution, $|z/a| < 1$

- Self-similar solution in variable $\zeta = z/\sqrt{t}$, $W(z, t) = w(\zeta)$ for $|z| > a$, outside initial CR cloud

$$\frac{d}{d\zeta} \frac{1}{w} \frac{dw}{d\zeta} + \frac{\zeta}{2} \frac{dw}{d\zeta} = 0$$

- solution depends on integrated CR pressure in the cloud and background turbulence level $W_0 \ll 1$.

$$\Pi = \int_0^1 \mathcal{P}_0 dz \gg 1$$

Reduction of Equations

- CR/Alfven wave coupling

$$\frac{\partial W}{\partial t} - \frac{\partial}{\partial z} \frac{1}{W} \frac{\partial W}{\partial z} = -\frac{\partial}{\partial z} \mathcal{P}_0(z)$$

$W = \frac{c_A^2(\rho)}{\kappa_B(\rho)}$ -dimensionless wave energy, $d/dt \approx \partial/\partial t$, \mathcal{P}_0 -initial CR distribution, $|z/a| < 1$

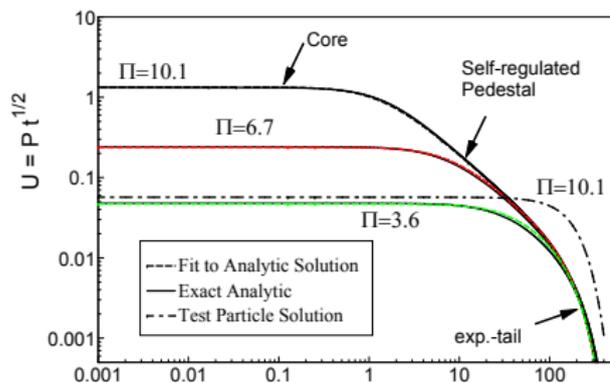
- Self-similar solution in variable $\zeta = z/\sqrt{t}$, $W(z, t) = w(\zeta)$ for $|z| > a$, outside initial CR cloud

$$\frac{d}{d\zeta} \frac{1}{w} \frac{dw}{d\zeta} + \frac{\zeta}{2} \frac{dw}{d\zeta} = 0$$

- solution depends on integrated CR pressure in the cloud and background turbulence level $W_0 \ll 1$.

$$\Pi = \int_0^1 \mathcal{P}_0 dz \gg 1$$

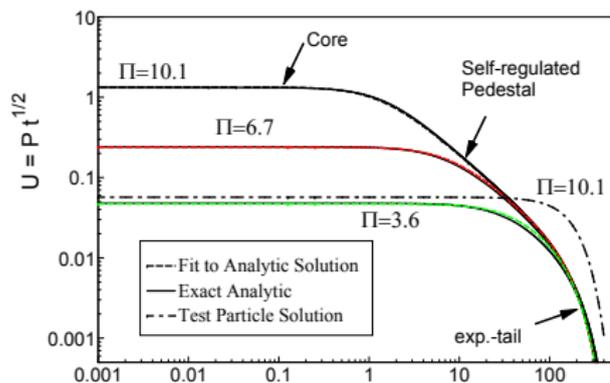
- 1 Why CR Escape is important
 - Observational significance of CR escape
 - The role of escape in acceleration theory
 - Escape and proof of SNR origin of CR
- 2 Approaches to CR escape from accelerators
 - TP/self-confinement
- 3 Formulation of the Problem/Technique
 - Geometry/Equations
- 4 Results/Discussion of Observations/Summary
 - Self-similar solution/SNR W44



Self-confinement vs test-particle escape, $\sqrt{t}P_{CR}$ vs z/\sqrt{t} for different initial partial pressure parameters Π

Comparing and Contrasting with conventional TP predictions:

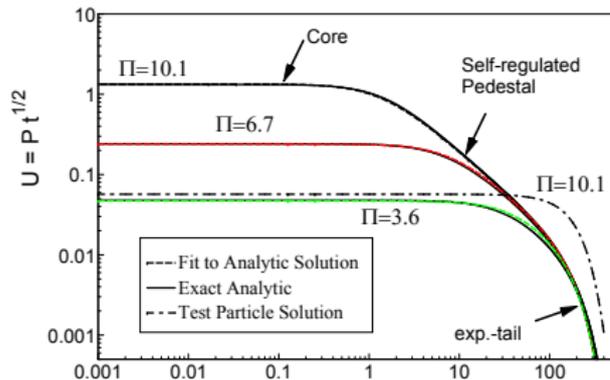
- considerable delay of CR escape
- narrower spatial distribution of CR cloud
- presence of extended self-similar, $\mathcal{P} \propto 1/z$ region



Self-confinement vs test-particle escape, $\sqrt{t}P_{CR}$ vs z/\sqrt{t} for different initial partial pressure parameters Π

Comparing and Contrasting with conventional TP predictions:

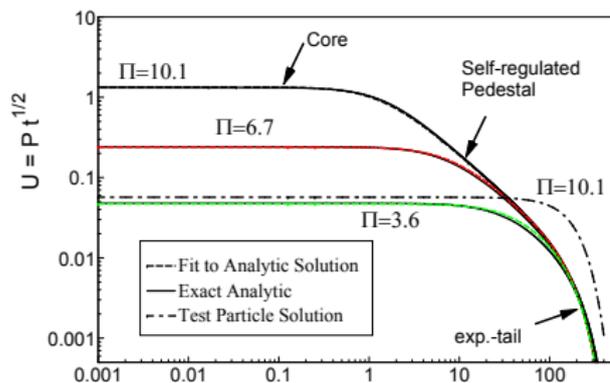
- considerable delay of CR escape
- narrower spatial distribution of CR cloud
- presence of extended self-similar, $\mathcal{P} \propto 1/z$ region



Self-confinement vs test-particle escape, $\sqrt{t}P_{CR}$ vs z/\sqrt{t} for different initial partial pressure parameters Π

Comparing and Contrasting with conventional TP predictions:

- considerable delay of CR escape
- narrower spatial distribution of CR cloud
- presence of extended self-similar, $P \propto 1/z$ region



Self-confinement vs test-particle escape, $\sqrt{t}P_{CR}$ vs z/\sqrt{t} for different initial partial pressure parameters Π

Comparing and Contrasting with conventional TP predictions:

- considerable delay of CR escape
- narrower spatial distribution of CR cloud
- presence of extended self-similar, $\mathcal{P} \propto 1/z$ region

- CR partial pressure (found in closed but implicit form) is well approximated by:

$$\sqrt{t}\mathcal{P} = 2 \left[\zeta^{5/3} + (D_{\text{NL}})^{5/6} \right]^{-3/5} e^{-W_0 \zeta^2/4}$$

- particle diffusivity is strongly suppressed by **self-confinement** effect:

$$D_{\text{NL}} = \frac{2}{V_0^2} D_{\text{ISM}} e^{-\Pi}, \quad V_0 \sim 1$$

- as integrated CR pressure parameter is typically large:

$$\Pi \simeq 3 \frac{C_A}{c} \frac{a(p)}{r_g(p)} \frac{\bar{P}_{\text{CR}}(p)}{B_0^2/8\pi} \gg 1$$

- CR partial pressure (found in closed but implicit form) is well approximated by:

$$\sqrt{t}\mathcal{P} = 2 \left[\zeta^{5/3} + (D_{\text{NL}})^{5/6} \right]^{-3/5} e^{-W_0 \zeta^2/4}$$

- particle diffusivity is strongly suppressed by **self-confinement** effect:

$$D_{\text{NL}} = \frac{2}{V_0^2} D_{\text{ISM}} e^{-\Pi}, \quad V_0 \sim 1$$

- as integrated CR pressure parameter is typically large:

$$\Pi \simeq 3 \frac{C_A}{c} \frac{a(p)}{r_g(p)} \frac{\bar{P}_{\text{CR}}(p)}{B_0^2/8\pi} \gg 1$$

- CR partial pressure (found in closed but implicit form) is well approximated by:

$$\sqrt{t}\mathcal{P} = 2 \left[\zeta^{5/3} + (D_{\text{NL}})^{5/6} \right]^{-3/5} e^{-W_0 \zeta^2/4}$$

- particle diffusivity is strongly suppressed by **self-confinement** effect:

$$D_{\text{NL}} = \frac{2}{V_0^2} D_{\text{ISM}} e^{-\Pi}, \quad V_0 \sim 1$$

- as integrated CR pressure parameter is typically large:

$$\Pi \simeq 3 \frac{C_A}{c} \frac{a(p)}{r_g(p)} \frac{\bar{P}_{\text{CR}}(p)}{B_0^2/8\pi} \gg 1$$

CR Escape: Energy Spectrum

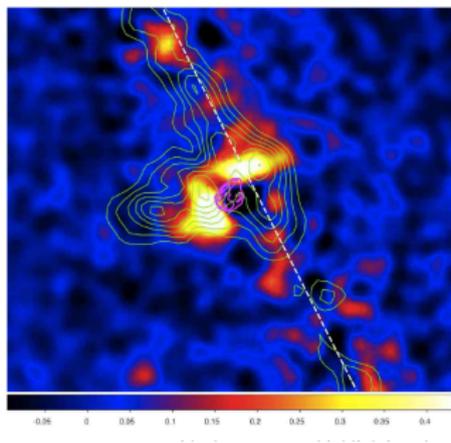
- CR partial pressure for $\delta B_{\text{ISM}} \ll B_0$:

$$\mathcal{P} \approx 2 \left\{ z^{5/3} + [D_{\text{NL}}(p) t]^{5/6} \right\}^{-3/5} \Rightarrow f_{\text{CR}} \propto \kappa_B p^{-4} / a z$$

- for $a \propto \kappa_B$ the spectrum is DSA like (evenly distributed partial pressure, wave generation takes care of that!)

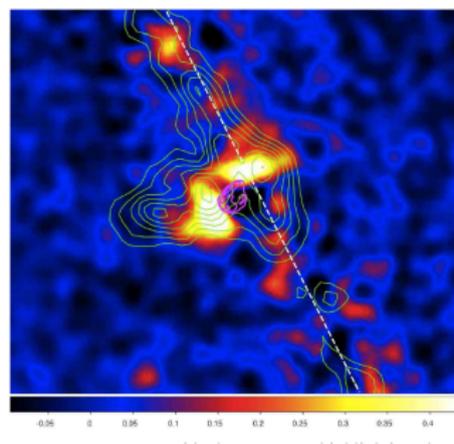
$$f_{\text{CR}} \propto p^{-4} \quad \text{where} \quad D_{\text{NL}}(p) < z^2/t$$

- at $p = p_{\text{br}}$, where $D_{\text{NL}}(p_{\text{br}}) = z^2/t$, spectrum incurs a break
- if $D_{\text{NL}} \propto p^\delta$ near $p \sim p_{\text{br}}$, break has index $\delta/2$
- δ determined by $D_{\text{ISM}}(p)$ and CR pressure $\Pi(p)$
- $\exp(-\Pi) \propto p^{-\sigma}$, $D_{\text{ISM}} \propto p^\lambda$ at $p \sim p_{\text{br}}$, so that $\delta = \lambda - \sigma$
- $\delta > 0$: \mathcal{P} is flat for $p < p_{\text{br}}$ steepens to $p^{-\delta/2}$ at $p = p_{\text{br}}$
- $\delta < 0$: \mathcal{P} raises as $p^{-\delta/2}$ for $p < p_{\text{br}}$ and flat for $p > p_{\text{br}}$



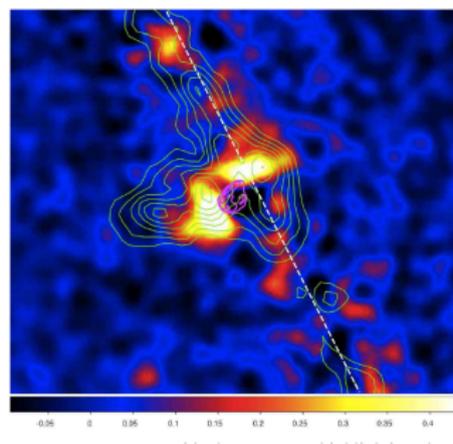
Fermi-LAT γ -image of SNR W44, *Uchiyama et al 2012*

- central source (magenta radio image) emission is masked
- bi-polar morphology of escaping CR is clearly seen
- not everywhere correlated with the dense gas (green contours) distribution: strong γ -flux is expected from overlapping regions of CR and gas density
- strong indication of field aligned propagation
- various analyses of various sources (*e.g.* *Uchiyama et al 2012*) indicate that CR diffusivity is suppressed by up to a factor of ten



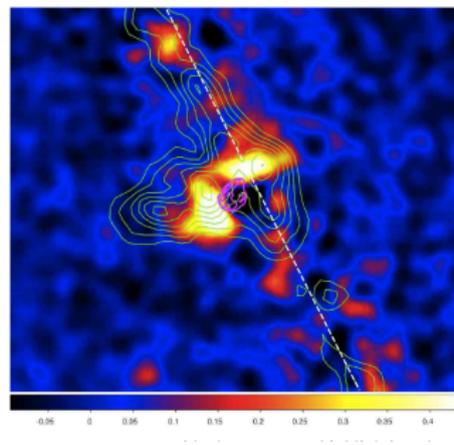
Fermi-LAT γ -image of SNR W44, *Uchiyama et al 2012*

- central source (magenta radio image) emission is masked
- bi-polar morphology of escaping CR is clearly seen
- not everywhere correlated with the dense gas (green contours) distribution: strong γ -flux is expected from overlapping regions of CR and gas density
- strong indication of field aligned propagation
- various analyses of various sources (*e.g.* *Uchiyama et al 2012*) indicate that CR diffusivity is suppressed by up to a factor of ten



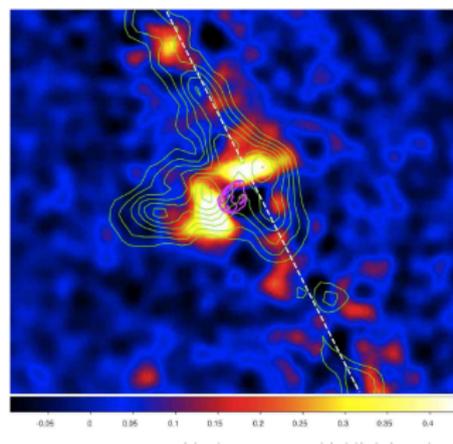
Fermi-LAT γ -image of SNR W44, *Uchiyama et al 2012*

- central source (magenta radio image) emission is masked
- bi-polar morphology of escaping CR is clearly seen
- not everywhere correlated with the dense gas (green contours) distribution: strong γ -flux is expected from overlapping regions of CR and gas density
- strong indication of field aligned propagation
- various analyses of various sources (*e.g. Uchiyama et al 2012*) indicate that CR diffusivity is suppressed by up to a factor of ten



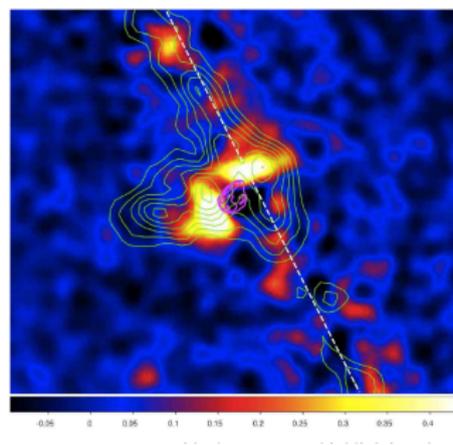
Fermi-LAT γ -image of SNR W44, *Uchiyama et al 2012*

- central source (magenta radio image) emission is masked
- bi-polar morphology of escaping CR is clearly seen
- not everywhere correlated with the dense gas (green contours) distribution: strong γ -flux is expected from overlapping regions of CR and gas density
- strong indication of field aligned propagation
- various analyses of various sources (*e.g.* *Uchiyama et al 2012*) indicate that CR diffusivity is suppressed by up to a factor of ten



Fermi-LAT γ -image of SNR W44, *Uchiyama et al 2012*

- central source (magenta radio image) emission is masked
- bi-polar morphology of escaping CR is clearly seen
- not everywhere correlated with the dense gas (green contours) distribution: strong γ -flux is expected from overlapping regions of CR and gas density
- strong indication of field aligned propagation
- various analyses of various sources (*e.g.* *Uchiyama et al 2012*) indicate that CR diffusivity is suppressed by up to a factor of ten



Fermi-LAT γ -image of SNR W44, *Uchiyama et al 2012*

- central source (magenta radio image) emission is masked
- bi-polar morphology of escaping CR is clearly seen
- not everywhere correlated with the dense gas (green contours) distribution: strong γ -flux is expected from overlapping regions of CR and gas density
- strong indication of field aligned propagation
- various analyses of various sources (*e.g.* *Uchiyama et al 2012*) indicate that CR diffusivity is suppressed by up to a factor of ten

- escape of CR from their acceleration site is treated **self-consistently with self-generated Alfvén waves**
- resulting CR distribution is obtained in closed form
- strong **self-confinement** of escaping CR is demonstrated
- results are consistent with recent observations of W44 by *Fermi*-LAT
- escape spectra are roughly DSA-like power law, no signs of energy peaked escape

- Outlook
 - turbulence spreading across MF field likely to be important at lateral part of expanding CR cloud
 - CR pitch angle anisotropy must be strong at the edge of the cloud and needs to be included
 - combine escape with acceleration (ongoing work)