

All-optical probes of quantum vacuum nonlinearity

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(i) Abstract

In this talk,

- I will exemplarily focus on **vacuum birefringence** in strong **inhomogeneous** (laser) **fields**.
- I will present new key ideas that can make the experimental verification of vacuum birefringence with high-intensity lasers feasible
 - with **state of the art** technology,
 - e.g. at the **H**elmholtz **I**nternational **B**eamline for **E**xtrême **F**ields at the European XFEL.

(ii) Our approach

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Effective theory for **probe photon** (A^μ) propagation in inhomogeneous **electromagnetic background** (\mathcal{A}^μ):

$$S_{\text{eff}}[A, \mathcal{A}] = -\frac{1}{4} \int_x \mathbb{F}_{\mu\nu}(x) \mathbb{F}^{\mu\nu}(x)$$

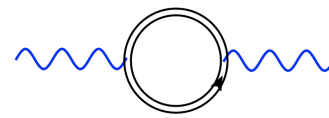
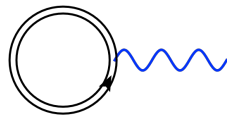
where $\mathbb{A}^\mu = \mathcal{A}^\mu + A^\mu$

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$$+ \int_x j^\mu(x|\mathcal{A}) A_\mu(x) - \frac{1}{2} \int_x \int_{x'} A_\mu(x) \Pi^{\mu\nu}(x, x'|\mathcal{A}) A_\nu(x') + \dots$$



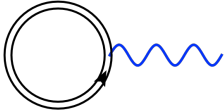
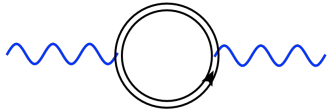
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Problem: Most analytical calculations have been performed either for uniform, constant or planewave (null-field) **backgrounds**.

- e.g. photon polarization tensor [\[Batalin, Shabad: Sov. Phys. JETP **33** 483 \(1971\)\]](#)
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- ↔ the electromagnetic fields delivered by focused high-intensity lasers are highly inhomogeneous

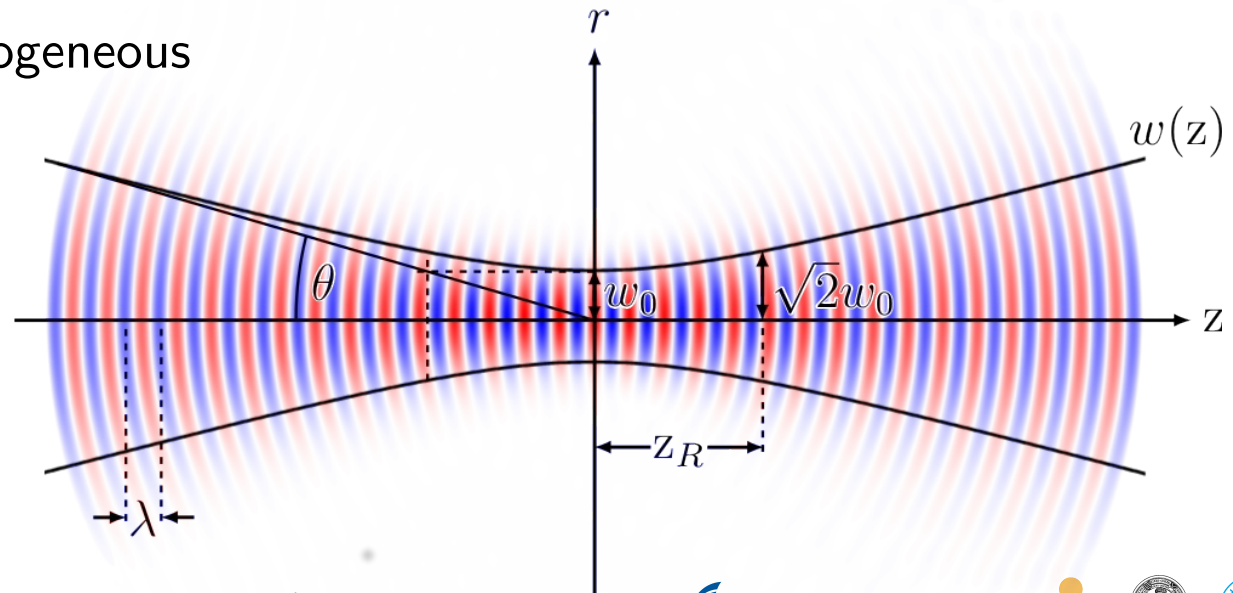
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Gaussian beams
$$I(x) = I_0 \left[e^{-\frac{(z-t)^2}{(\tau/2)^2}} \frac{w_0}{w(z)} e^{-\frac{x^2+y^2}{w^2(z)}} \times \cos \left(\Omega(z-t) + \frac{x^2+y^2}{w^2(z)} \frac{z}{z_R} - \arctan\left(\frac{z}{z_R}\right) + \varphi_0 \right) \right]^2$$

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But: On the other hand, we have the Heisenberg-Euler Lagrangian:

[Heisenberg, Euler: Z. Phys. **98** 714 (1936)]

$$\mathcal{L}(\mathcal{F}, \mathcal{G}) = \text{[Feynman diagram: two concentric circles with an arrow on the inner circle]} + \dots$$
$$\mathcal{F} = \frac{1}{4} F_{\mu\nu} F^{\mu\nu} = \frac{1}{2} (\vec{B}^2 - \vec{E}^2),$$
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→ photon polarization tensor, current, etc. for slowly varying fields
can be derived therefrom (decomposition $\mathcal{A}^\mu(x) \rightarrow \mathcal{A}^\mu + A^\mu(x)$)

[Bialynicka-Birula, Bialynicka-Birula: Phys. Rev. D **2** 2341 (1970)]

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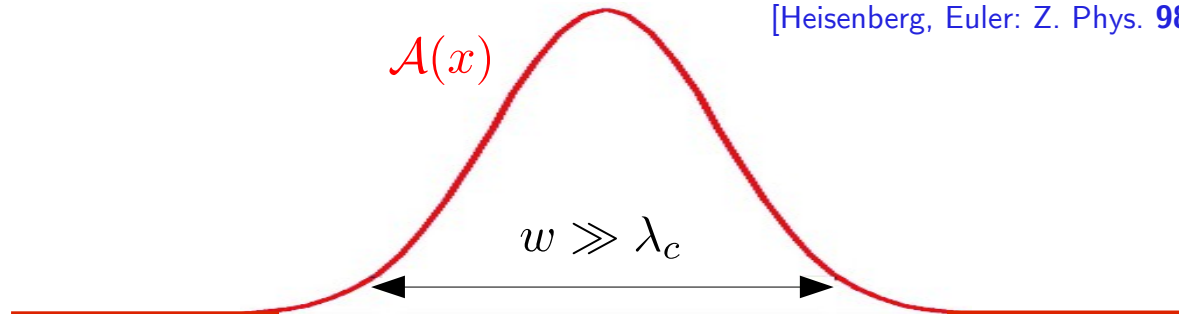
[FK, Shaisultanov: Phys. Rev. D **91** 085027 (2015)]

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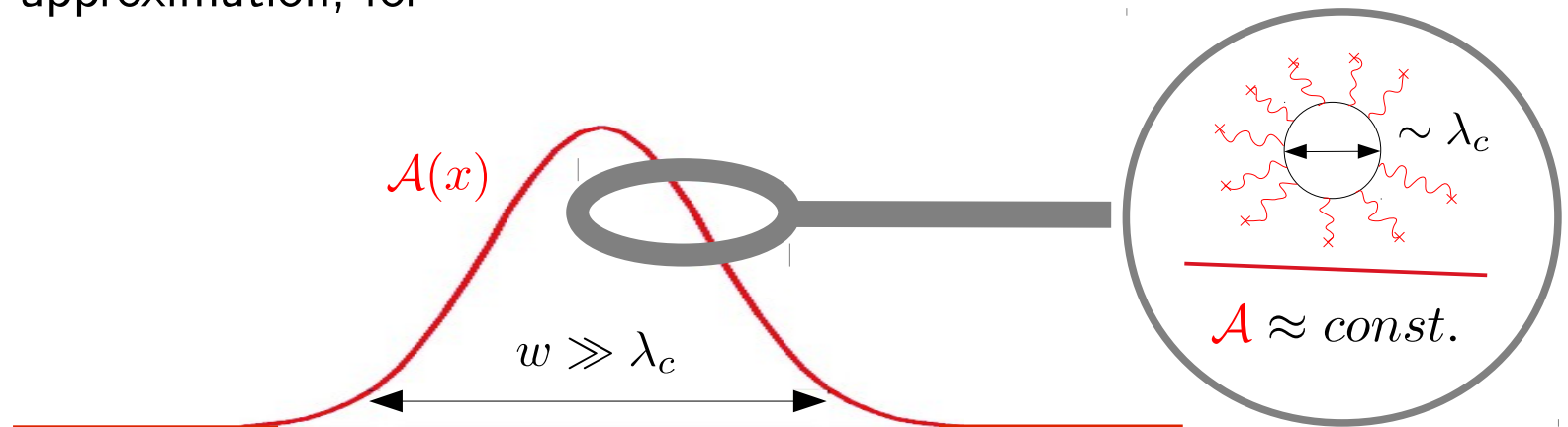
[...] den speziellen Fall [...], in dem keine wirklichen Elektronen und Positronen vorhanden sind, und in dem sich das Feld auf Strecken der Compton-Wellenlänge nur wenig ändert.

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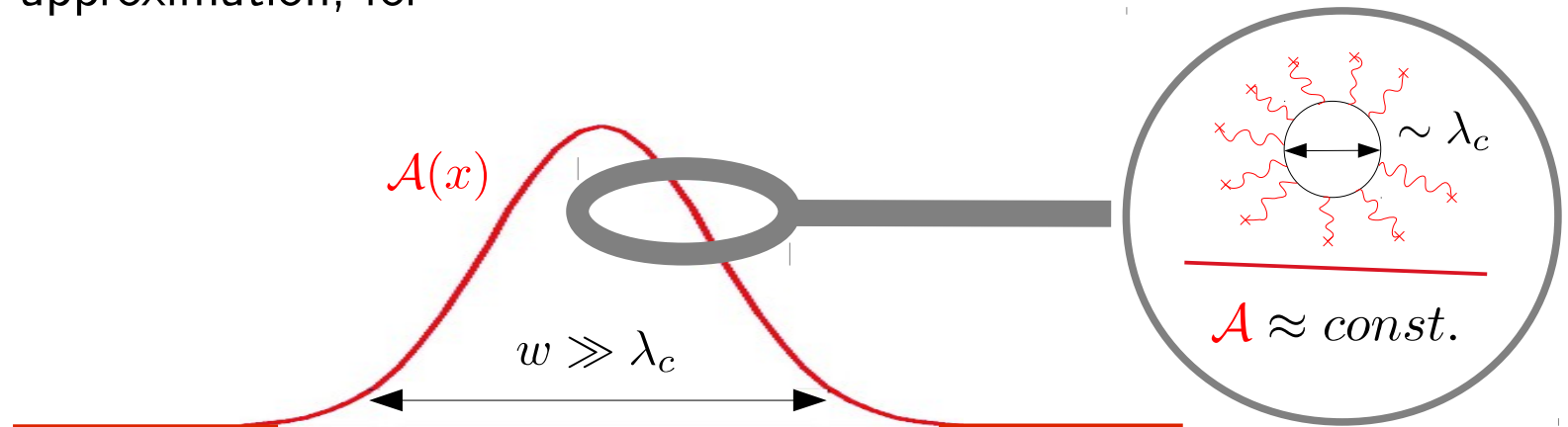
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- analytical insights possible without having to solve the problem for the exact, inhomogeneous **background field** configuration.

→ Polarization tensor in inhomogeneous, slowly varying **backgrounds**

$$\Pi^{\rho\sigma}(k', k|\mathcal{A}) = (g^{\rho\beta}k'^{\alpha} - g^{\rho\alpha}k'^{\beta}) \left[\int_x e^{i(k'+k)x} \frac{\partial^2 \mathcal{L}}{\partial F^{\alpha\beta} \partial F^{\mu\nu}}(x) \right] (k^{\mu}g^{\nu\sigma} - k^{\nu}g^{\mu\sigma})$$

[FK, Shaisultanov: Phys. Rev. D **91** 085027 (2015)]

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- mediates between two distinct photon momenta k'^μ, k^μ

→ for orthogonal electric and magnetic fields of same amplitude
we have $\mathcal{F}(x) = \mathcal{G}(x) = 0$, such that

$$\Pi^{\rho\sigma}(k', k|\mathcal{A}) = \frac{\alpha}{\pi} \frac{1}{45} \left(\frac{e}{m^2} \right)^2 \int_x e^{i(k'+k)x} \left[4 (k'F)^\rho (kF)^\sigma + 7 (k'^*F)^\rho (k^*F)^\sigma \right]$$

(iii) Vacuum birefringence

[Toll: PhD thesis, Princeton University, unpublished (1952)]

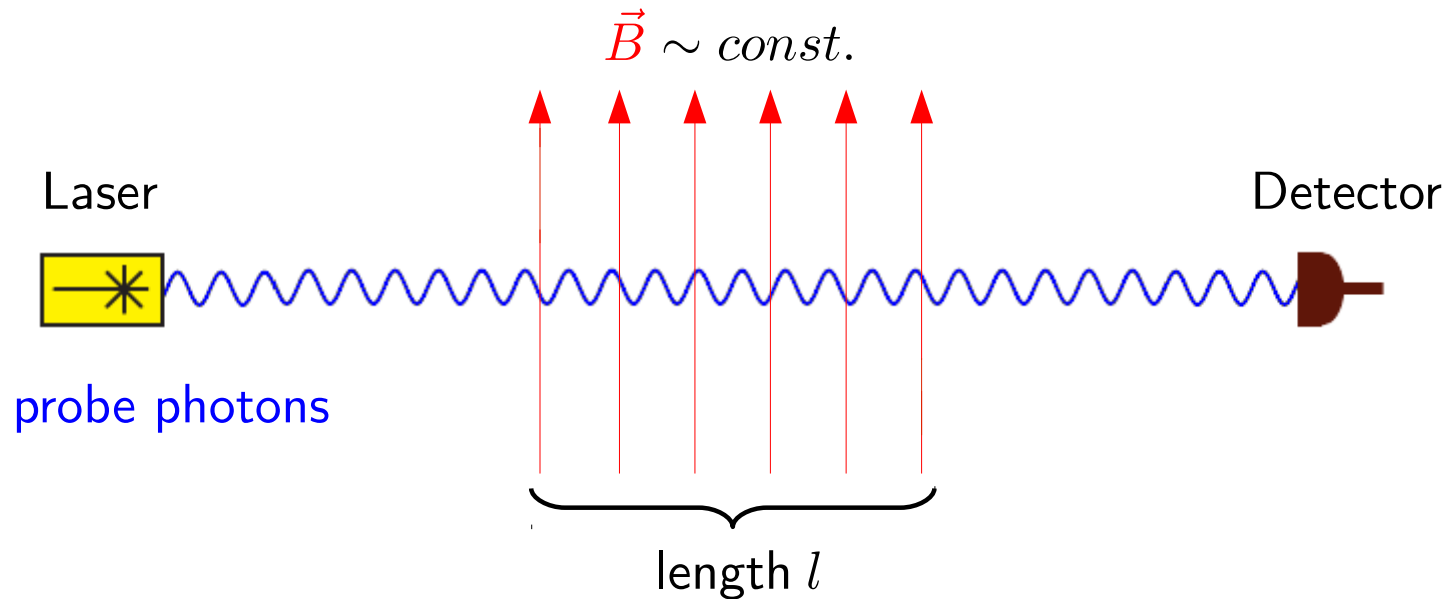
[Baier, Breitenlohner: Act. Phys. Austriaca **25** 212 (1967) & Nuov. Cim. B **47** 117 (1967)]

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Conventional scenario:

[BMV (Biréfringence Magnétique du Vide) experiment, Toulouse]

[PVLAS (Polarizzazione del Vuoto con Laser) experiment, Padova/Ferrara]

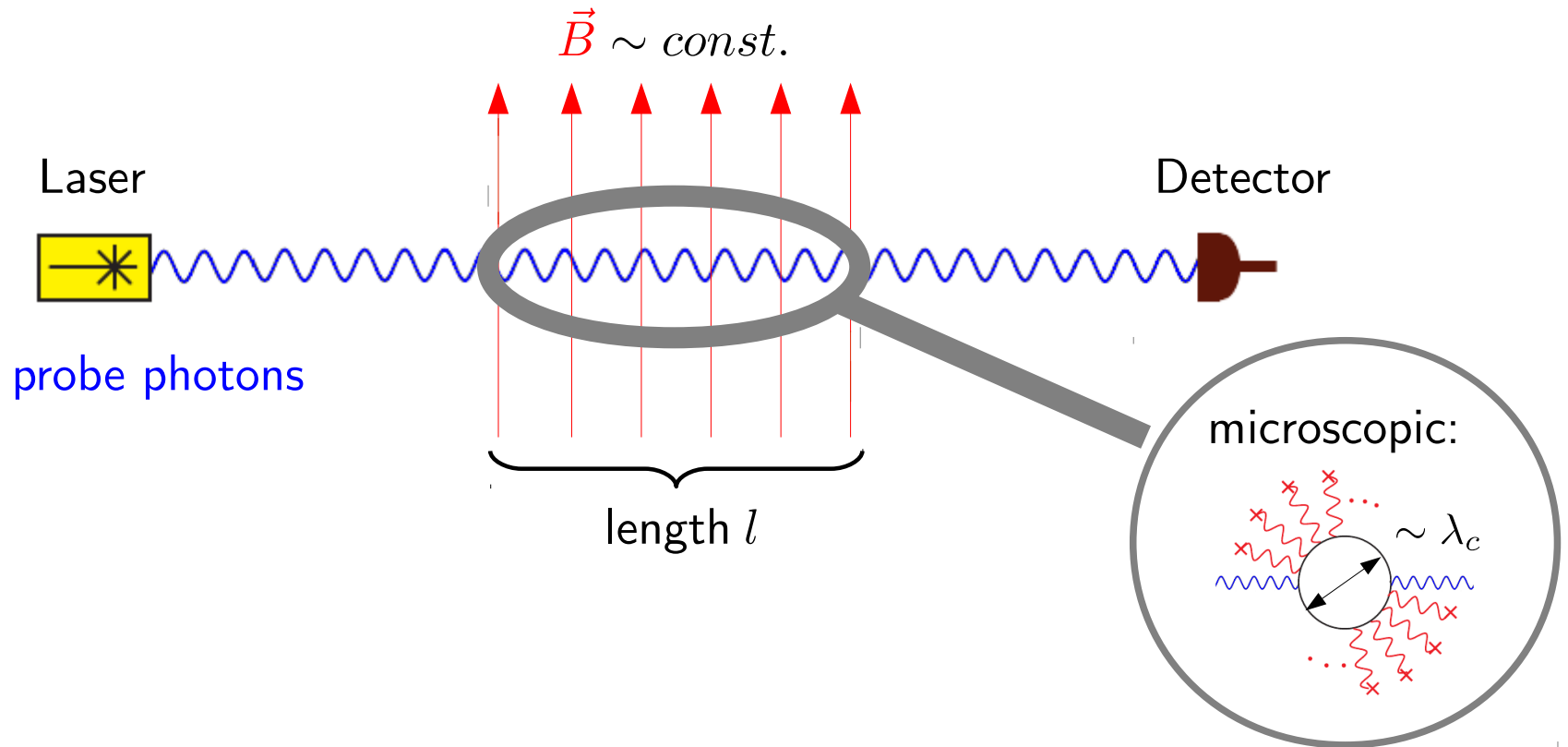


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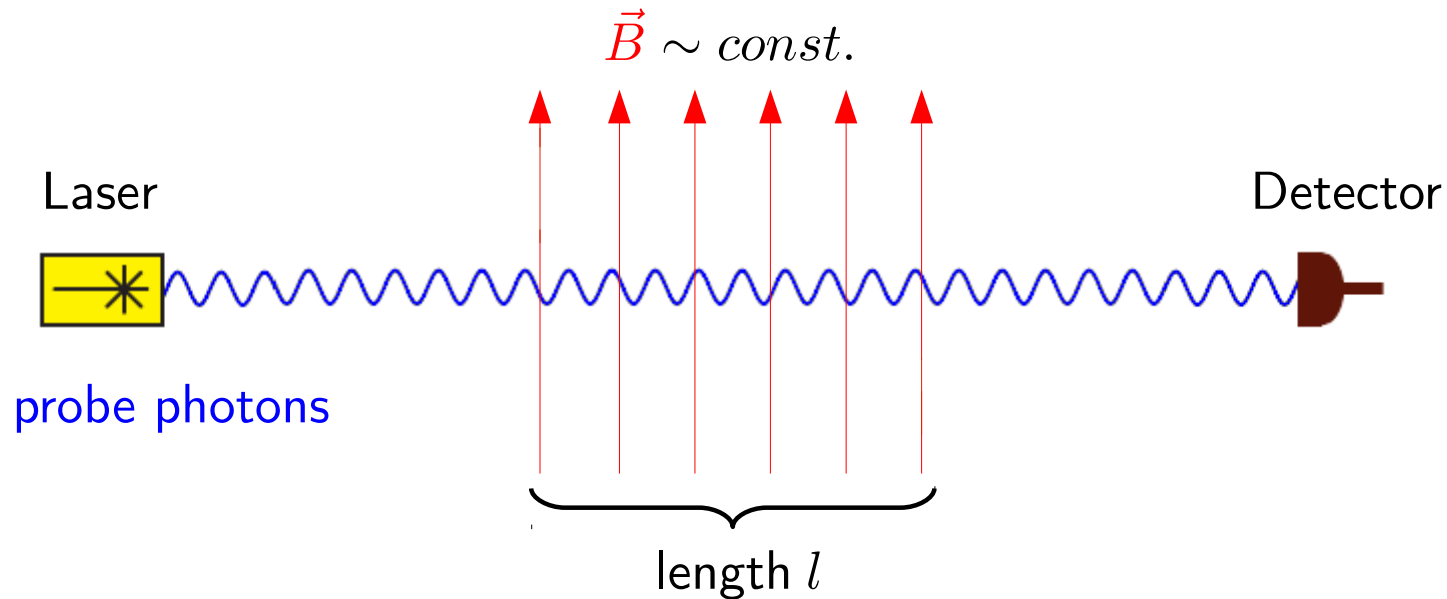


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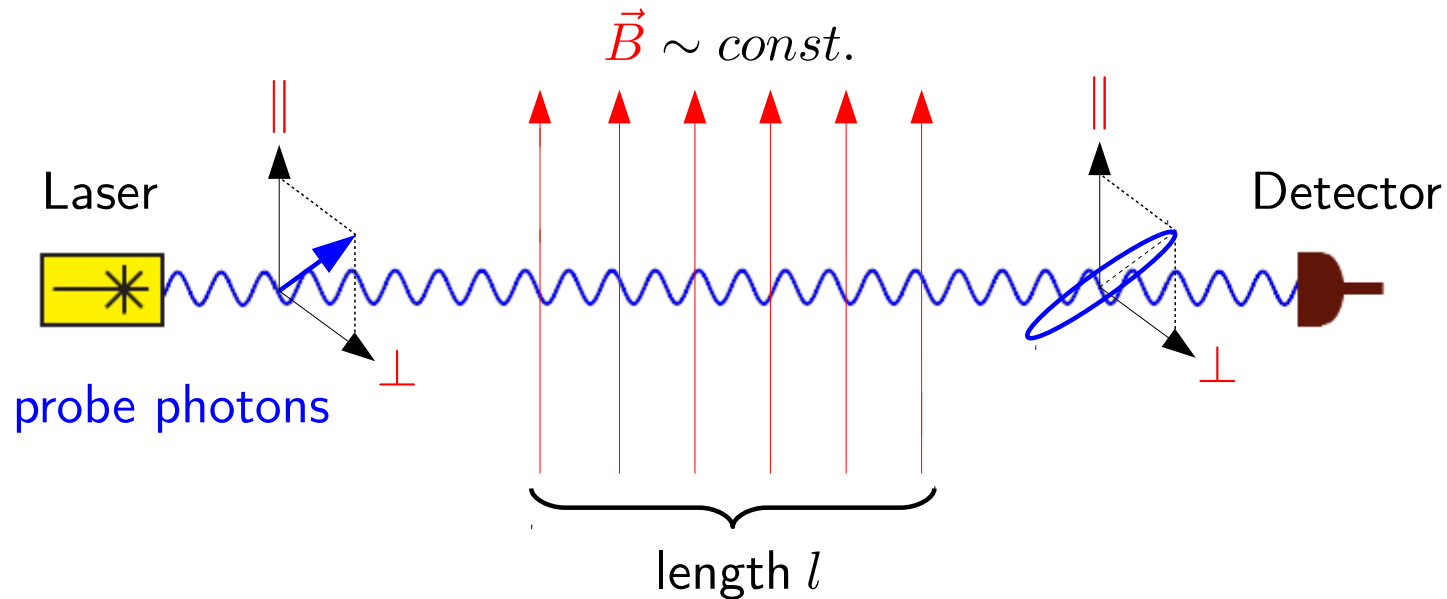


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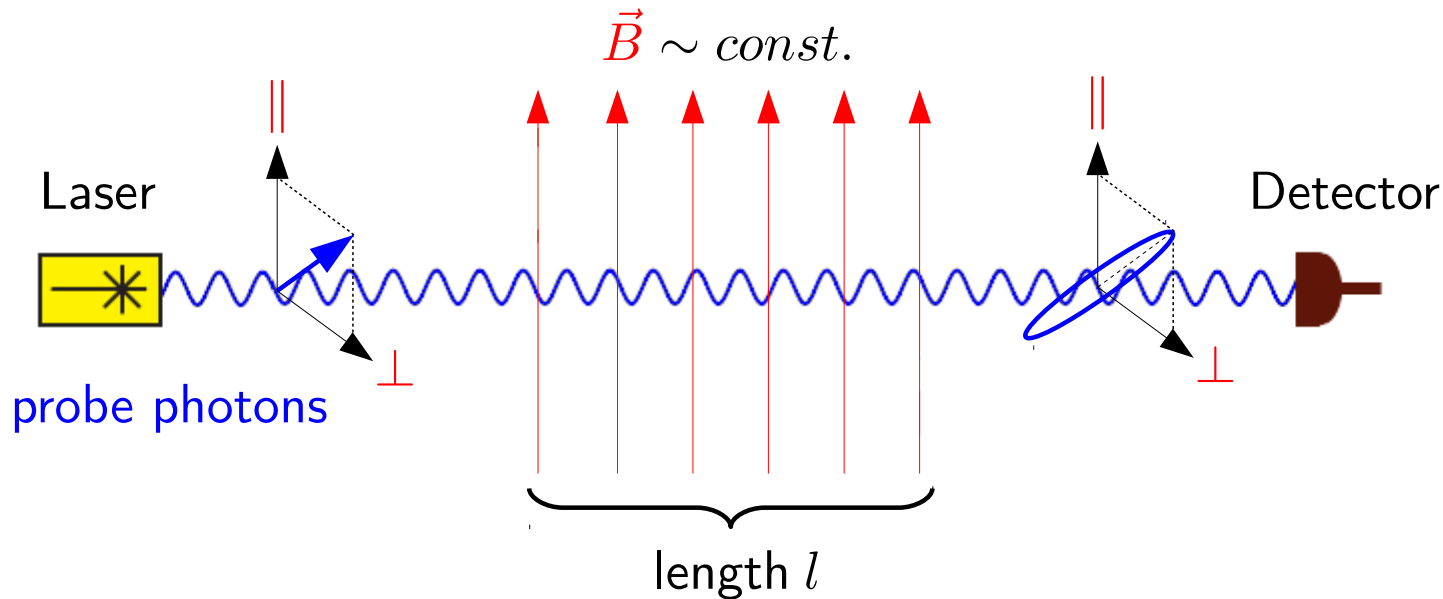
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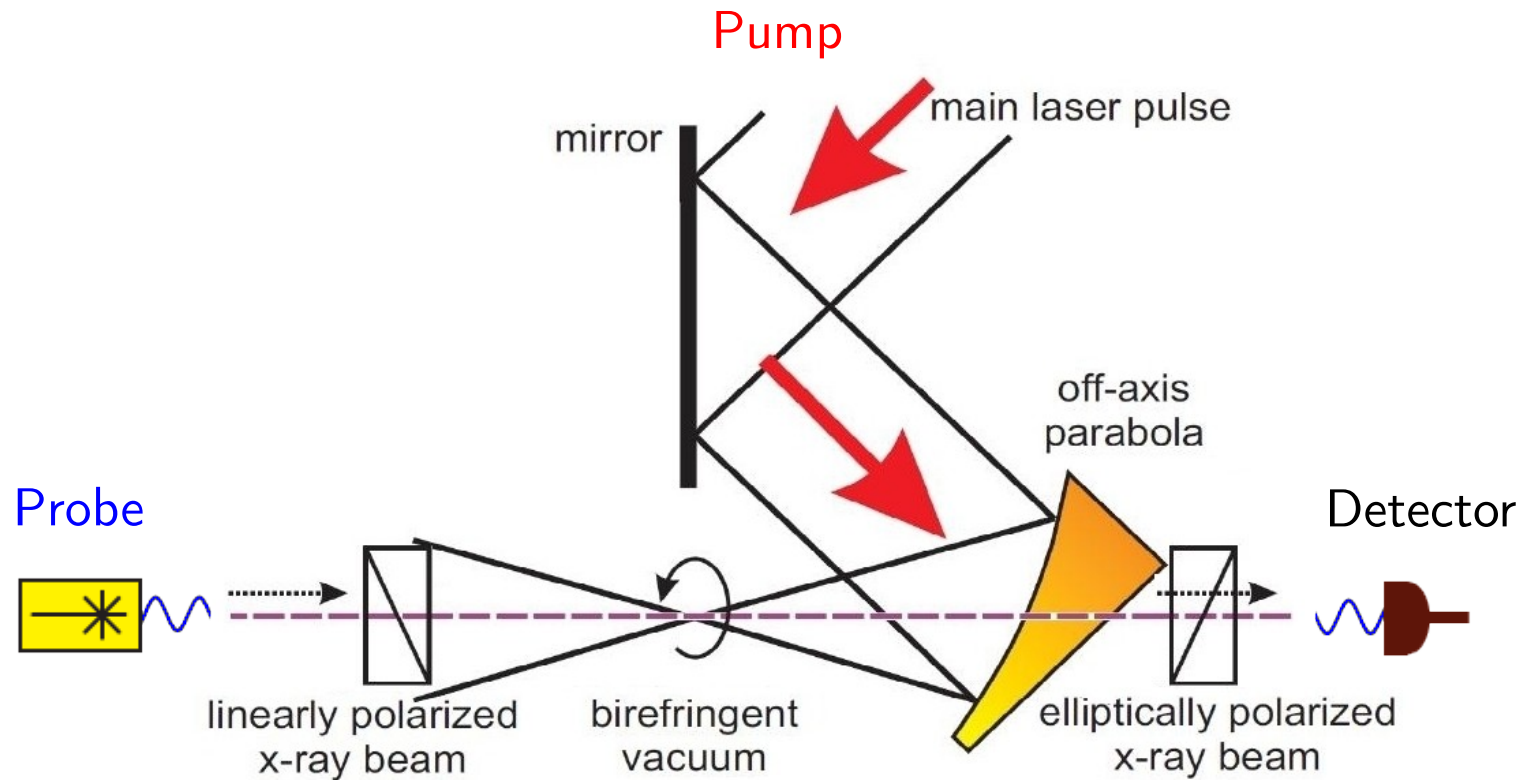
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\leftrightarrow photons in \perp polarization mode induced: $N_{\perp} \simeq \left(\frac{\Delta\phi}{2} \right)^2 N_{\text{in}}$

(iii) Vacuum birefringence

Analogous scenario with **pump = high-intensity laser**:

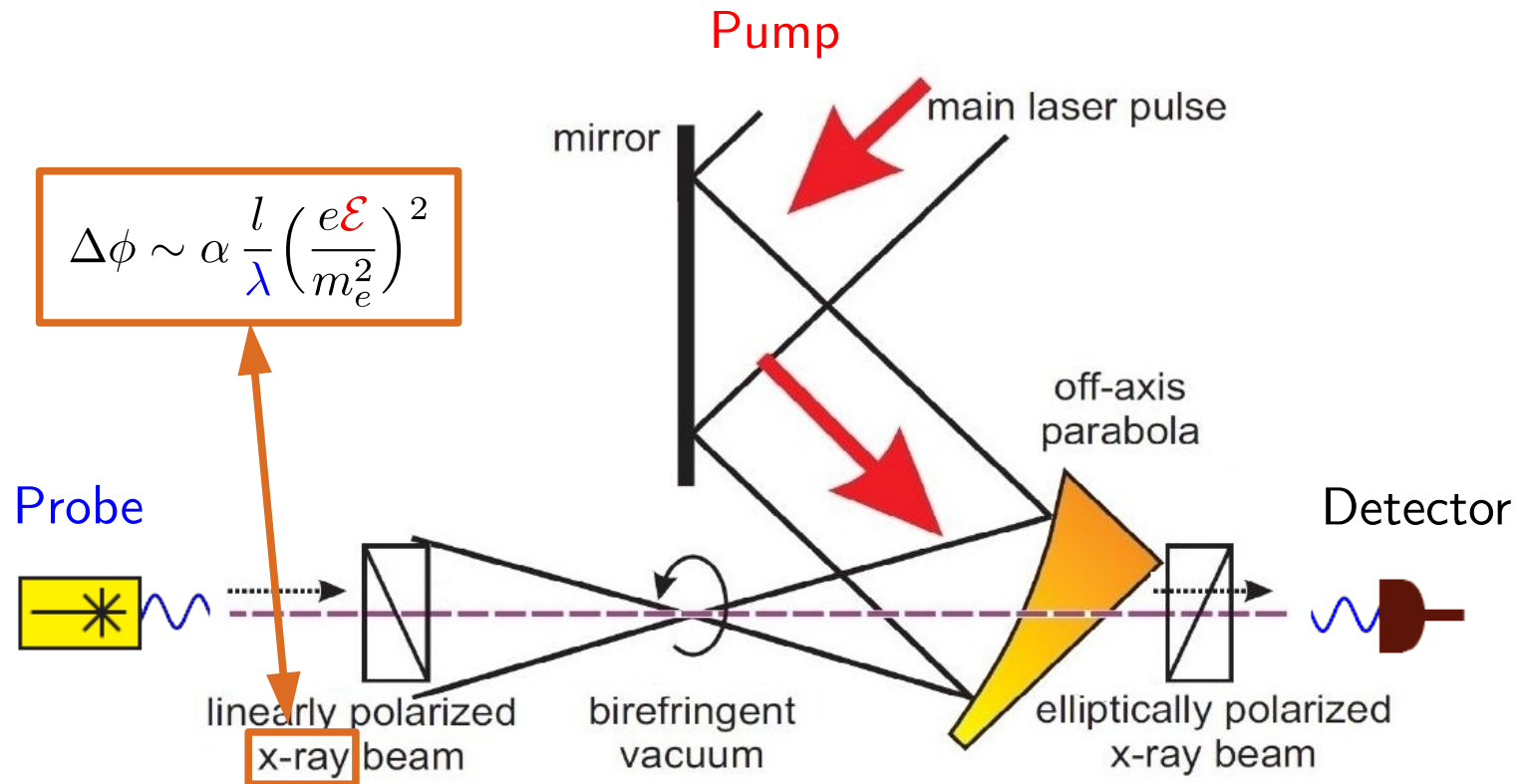
[Heinzl, Liesfeld, Amthor, Schworer, Sauerbrey, Wipf: Opt. Comm. **267** 318 (2006)]



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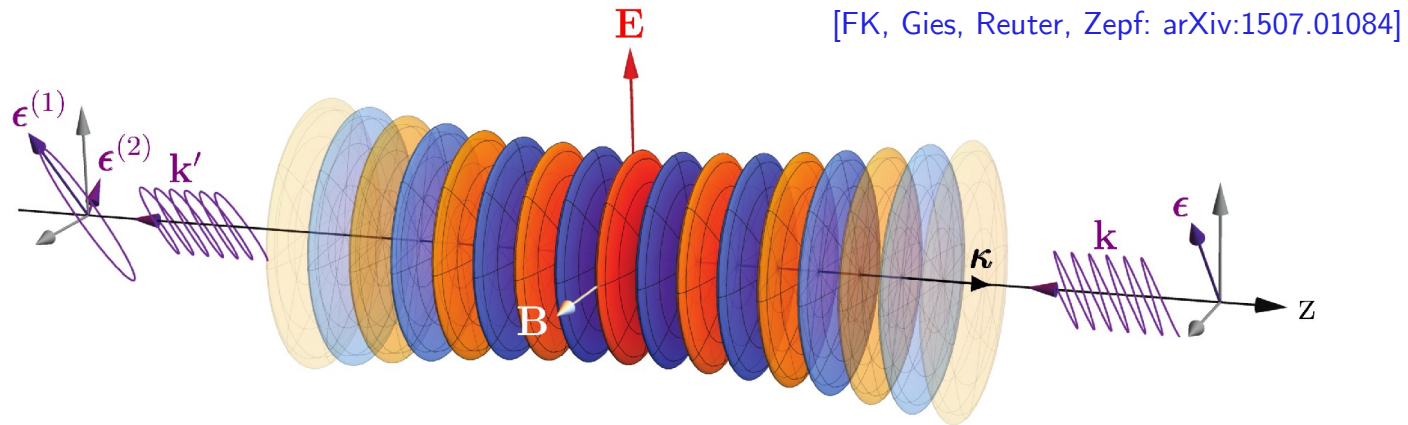
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Analogous scenario with **pump = high-intensity laser**:

- in a recent study we account for the full inhomogeneous field profile of a linearly polarized, pulsed Gaussian laser beam



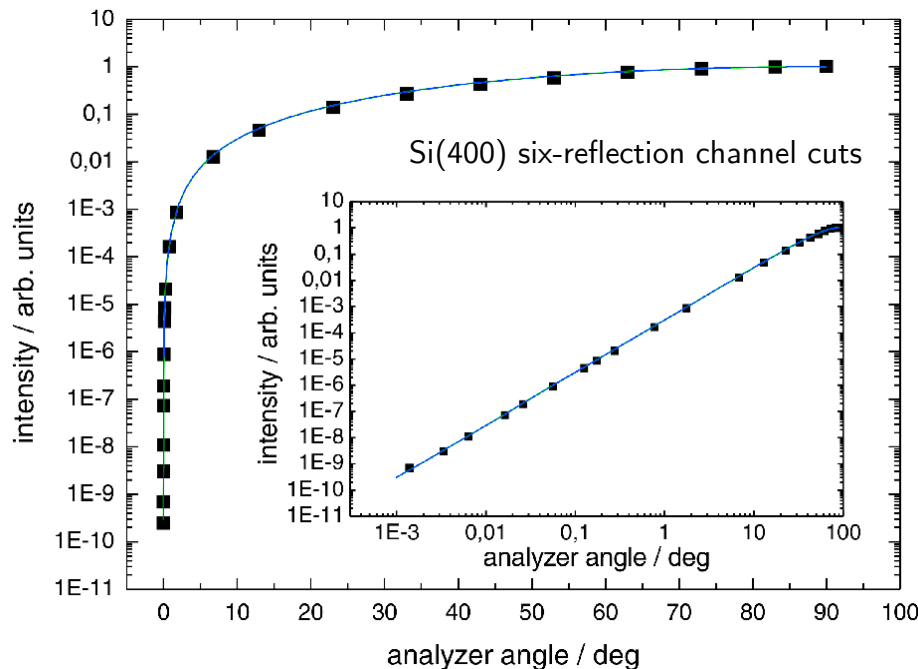
- **pump**: 1PW class laser ($W = 30\text{J}$, $\tau = 30\text{fs}$, $\lambda = 800\text{nm}$, $w_0 = 1\mu\text{m}$)
- **probe**: x-ray beam from FEL ($\omega = 12914\text{eV}$, $N_{\text{in}} \simeq 10^{12}$)

cf. also [Dinu, Heinzl, Ilderton, Marklund, Torggrimsson: Phys. Rev. D **89**, 125003 & **90** 045025 (2014)]

(iii) Vacuum birefringence

Analogous scenario with **pump = high-intensity laser**:

→ demand for high-purity x-ray polarimetry



[Marx, Schulze, Uschmann, Kämpfer, Löttsch, Wehrhan, Wagner, Detlefs, Roth, Härtwig, Förster, Stöhlker, Paulus: Phys. Rev. Lett. **110** 254801 (2013)]

Polarization purity
record @ $\omega = 12914\text{eV}$:
 $\mathcal{P} = 5.7 \cdot 10^{-10}$

↔ experimental confirmation of vacuum birefringence requires $\frac{N_{\perp}}{N_{\text{in}}} > \mathcal{P}$.

(iii) Vacuum birefringence

Our theoretical approach:

Idea: Interpret vacuum birefringence as **vacuum emission process:**

[FK, Shaisultanov: Phys. Rev. D **91** 113002 (2015)]

- laser fields correspond to macroscopic electromagnetic fields
- taking this literally means not to resolve the individual photons constituting the beams

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↔ vacuum in the presence of **pump** and **probe** beams = $|0\rangle$

- the signal of quantum vacuum nonlinearity is encoded in (single) photons = $|\gamma_{(p)}(\vec{k}')\rangle$ emitted from the strong field region

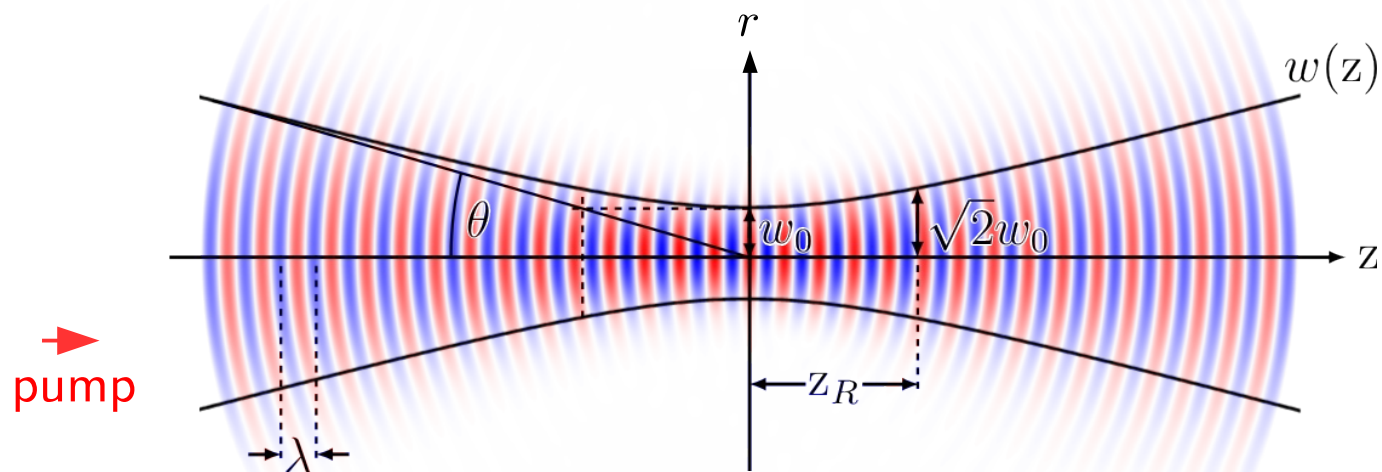
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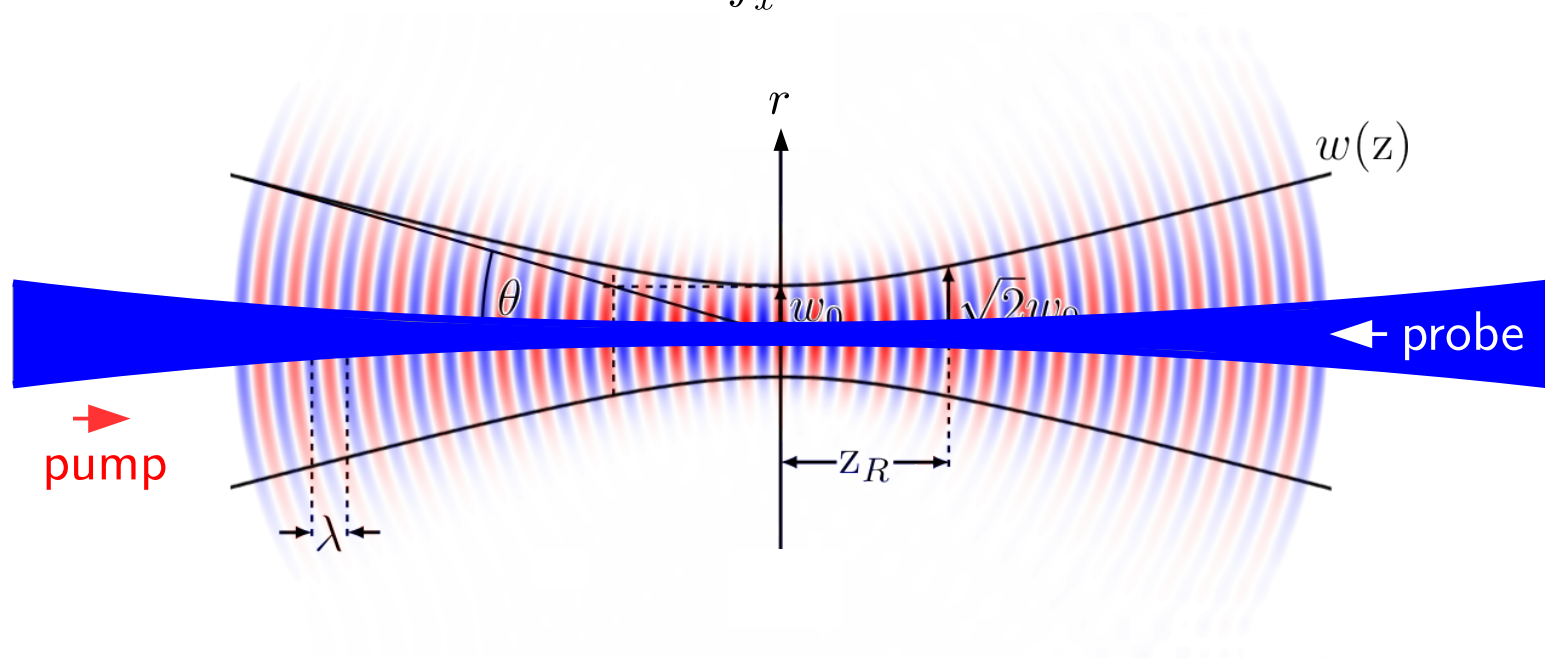


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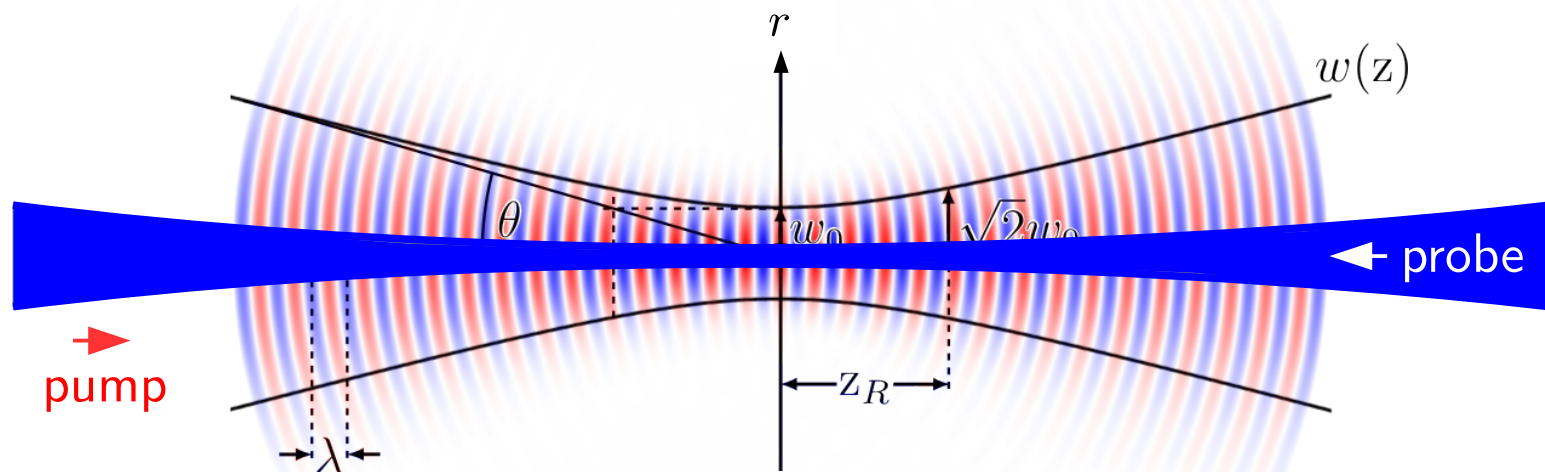


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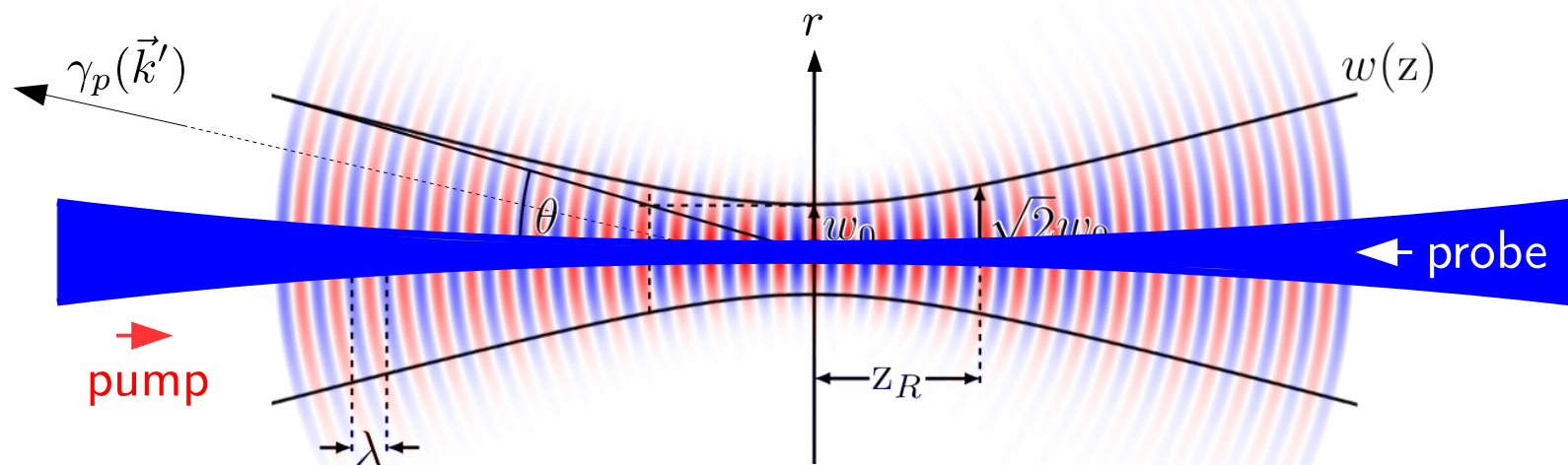
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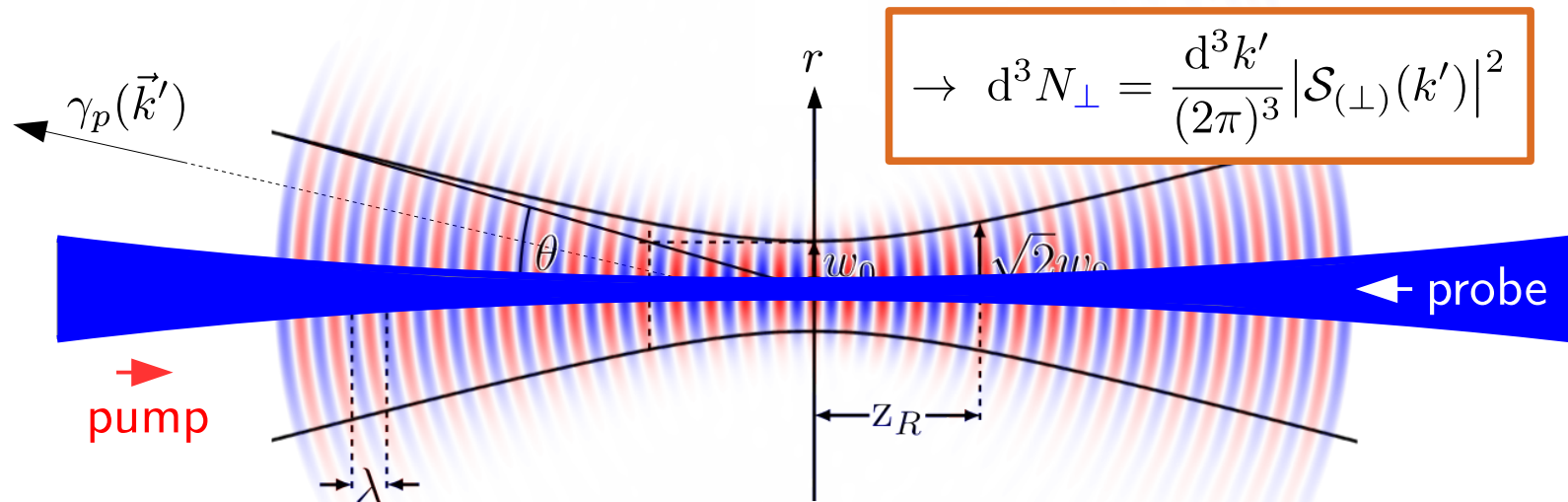
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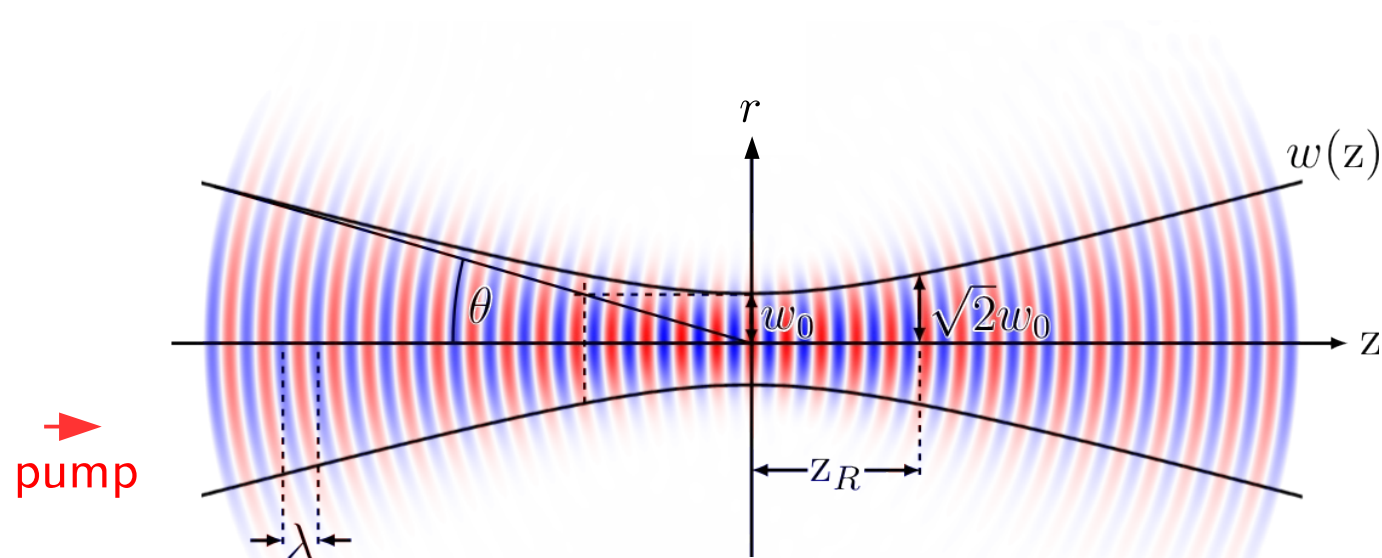
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[FK, Gies, Reuter, Zepf: arXiv:1507.01084]

- we consider three different cases

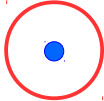


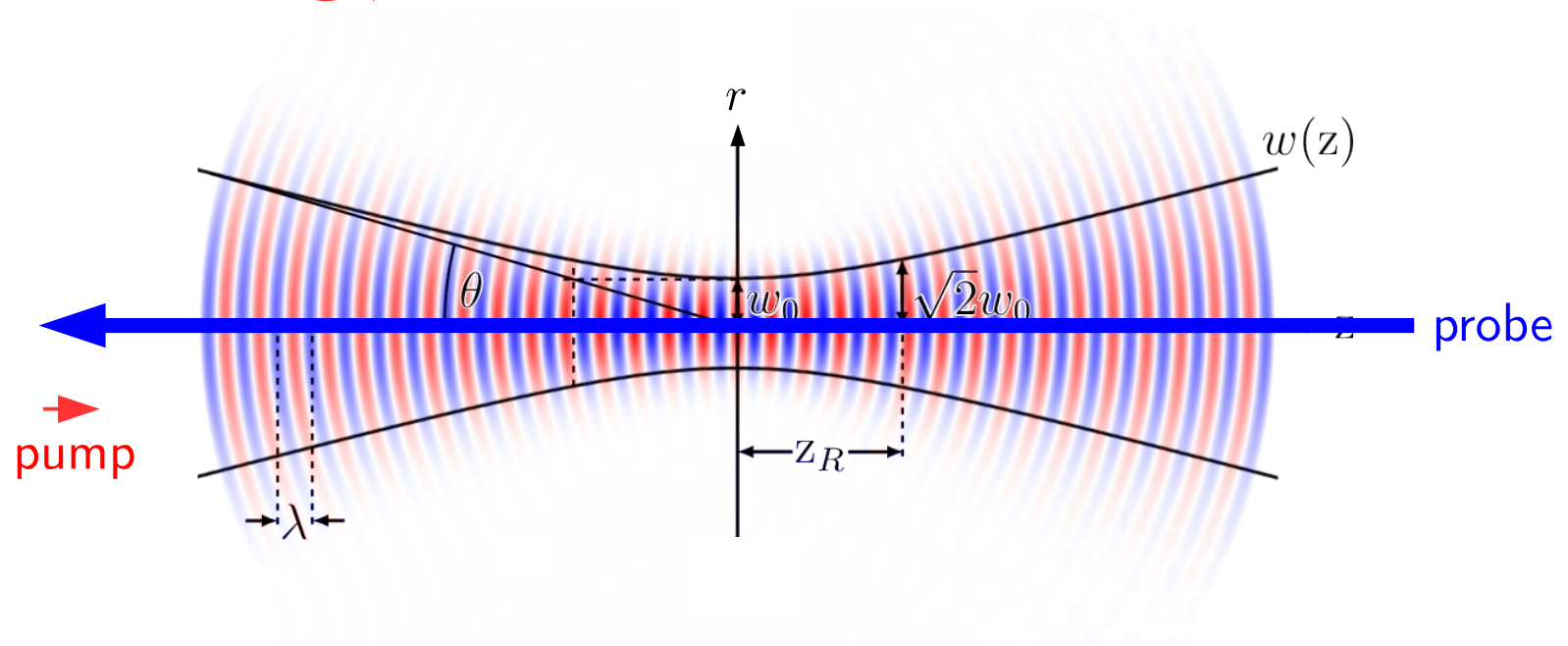
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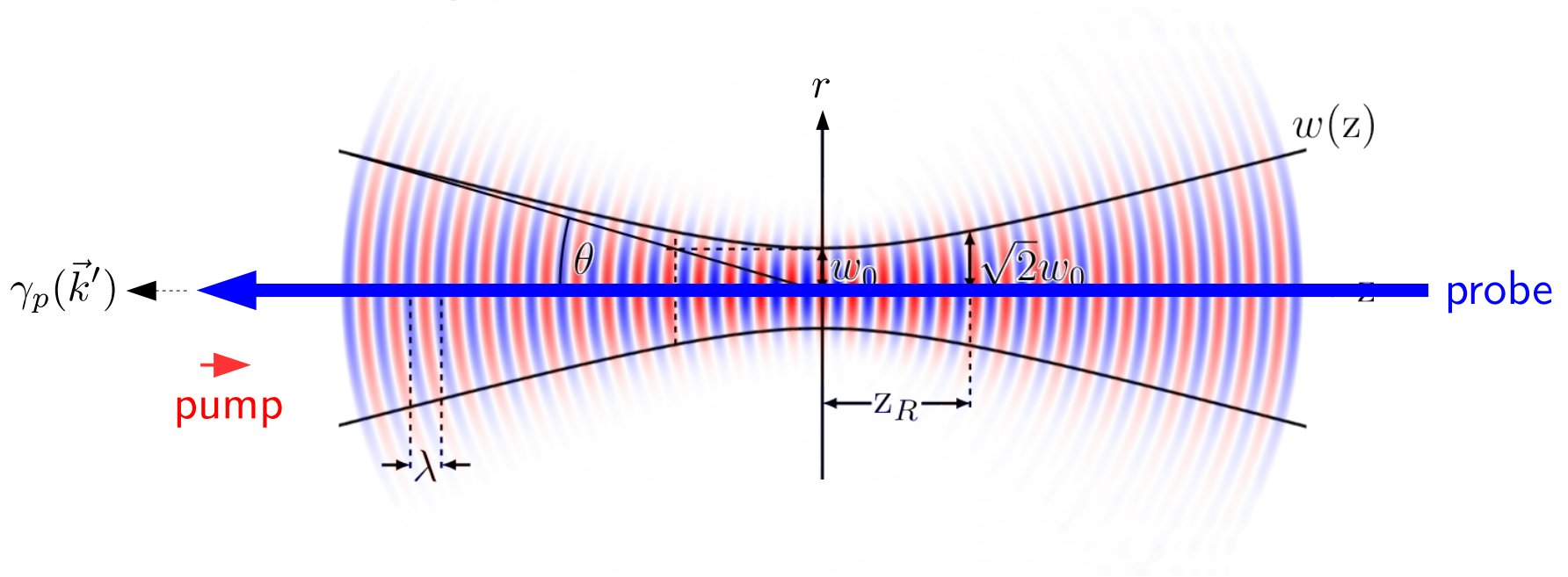
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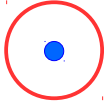


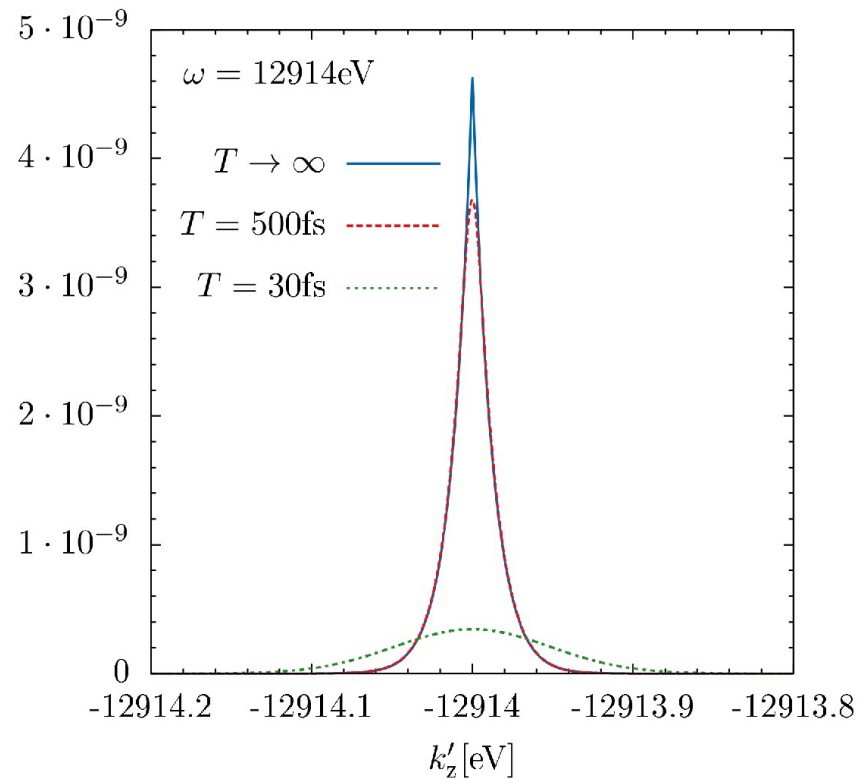
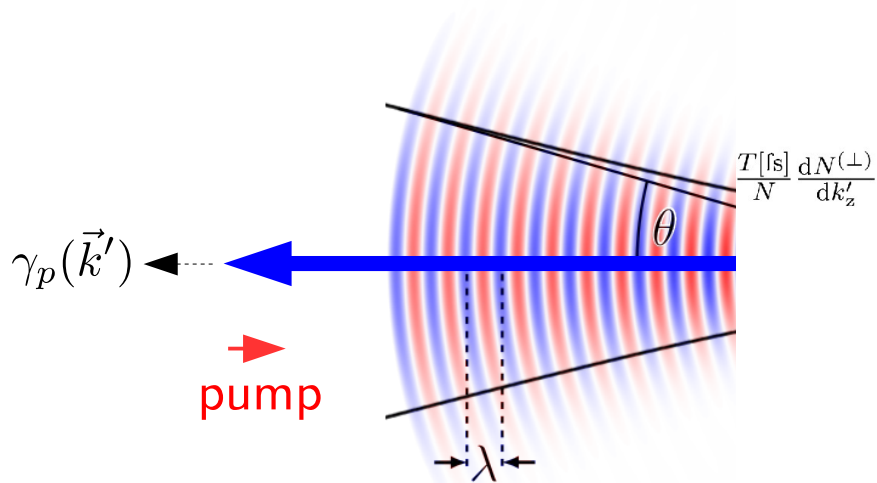
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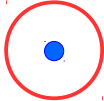


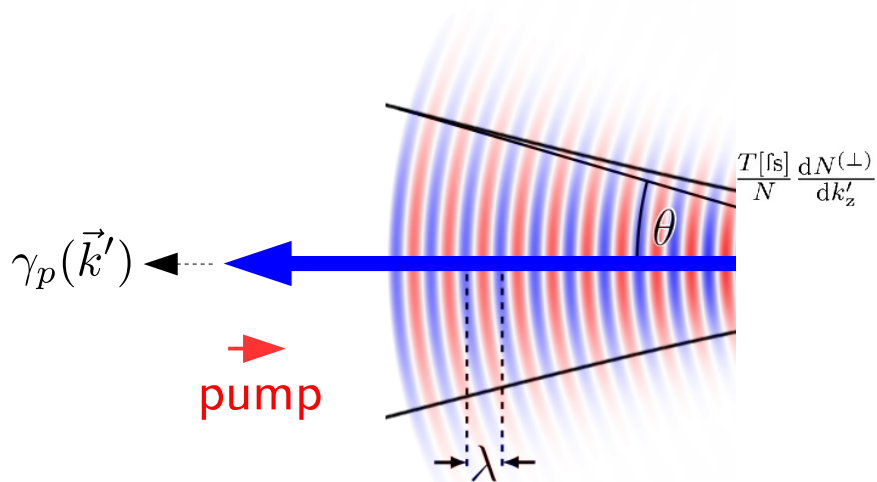
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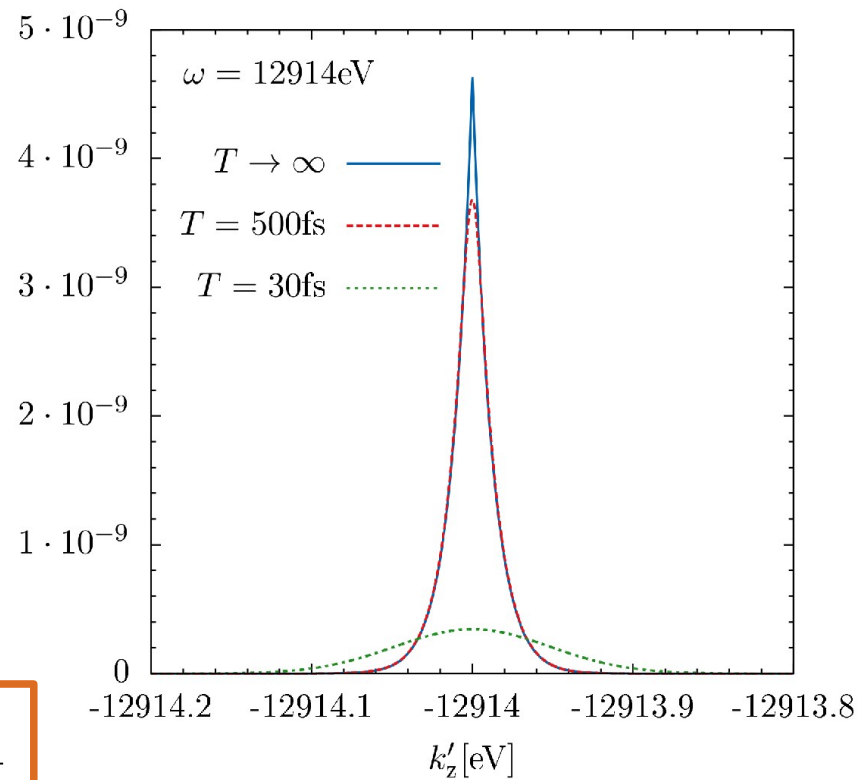
[FK, Gies, Reuter, Zepf: arXiv:1507.01084]

- we consider three different cases

→ case (a): 



$$\left. \frac{N_{\perp}}{N_{\text{in}}} \right|_{T=30\text{fs}} = 1.39 \cdot 10^{-12} \approx \frac{\mathcal{P}}{410}$$

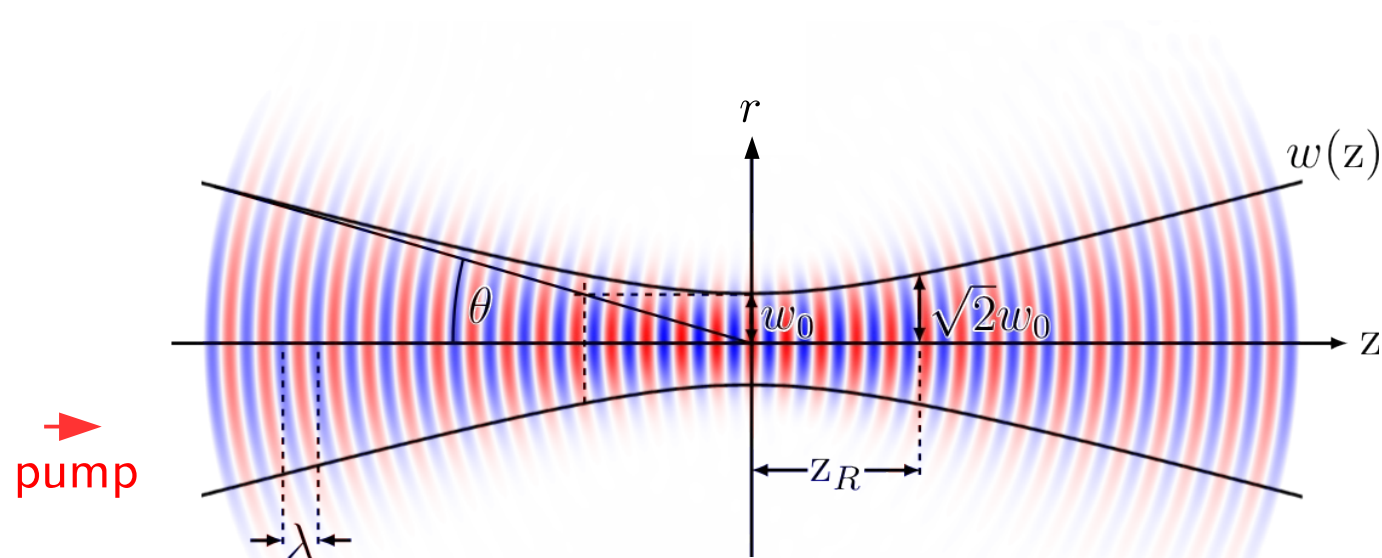


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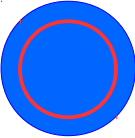


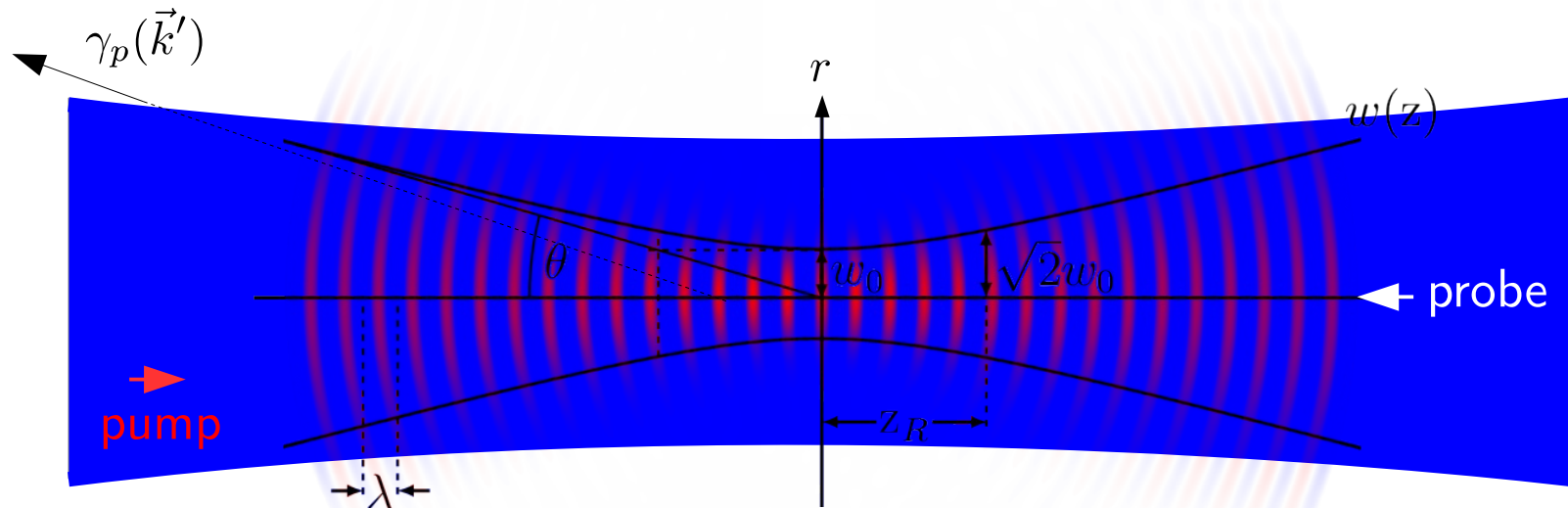
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→ case (b): 

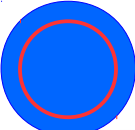
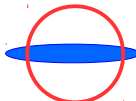


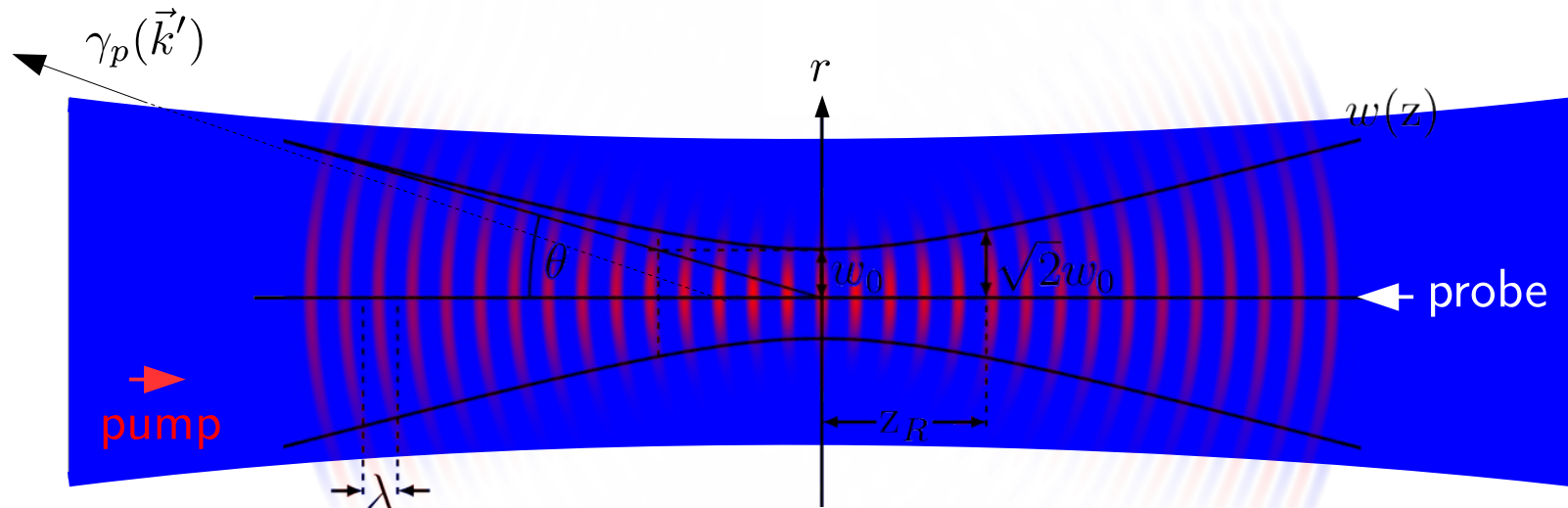
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[FK, Gies, Reuter, Zepf: arXiv:1507.01084]

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→ case (b):  and case (c): 

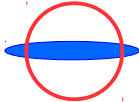


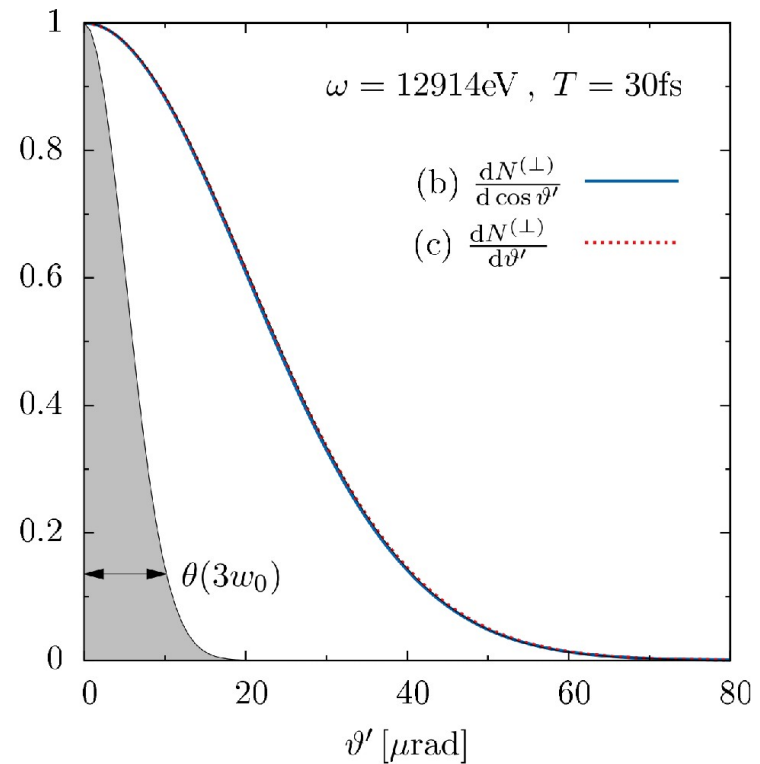
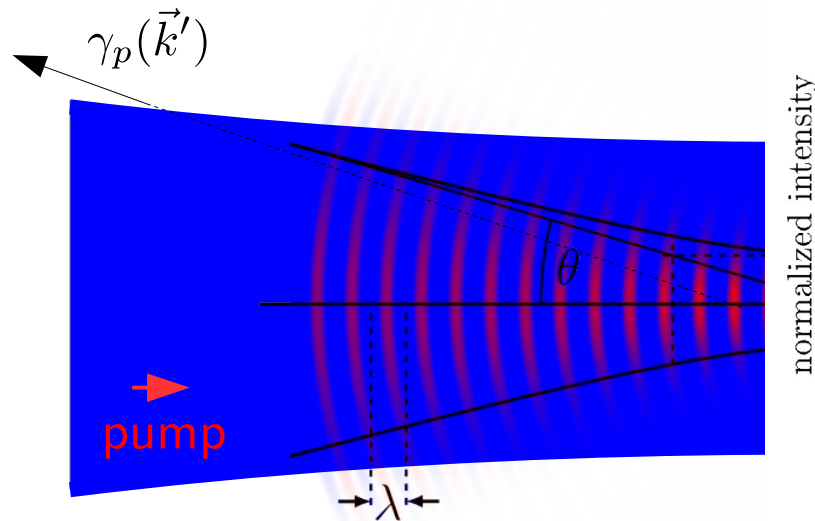
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[FK, Gies, Reuter, Zepf: arXiv:1507.01084]

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→ case (c): 

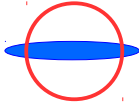


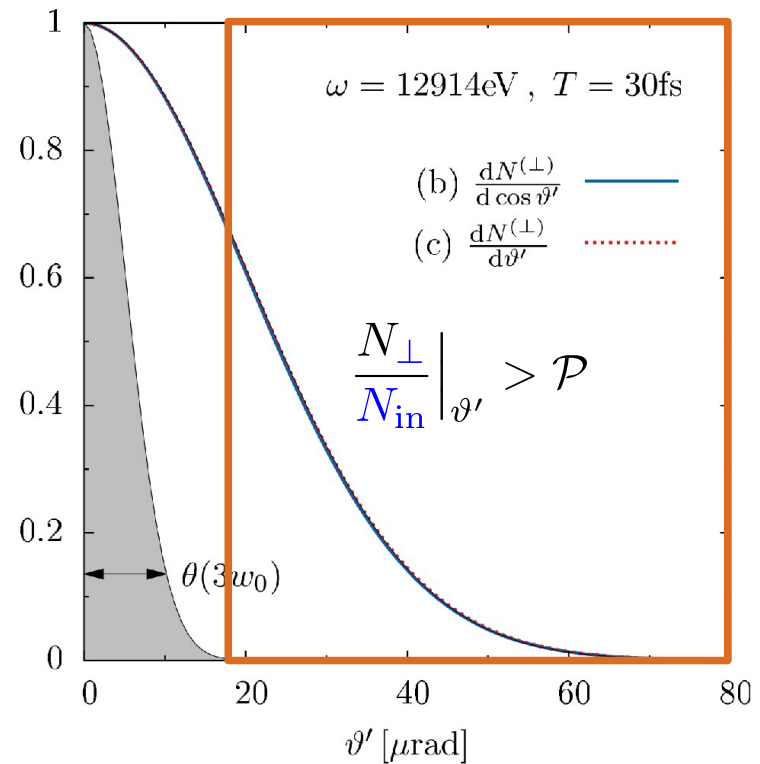
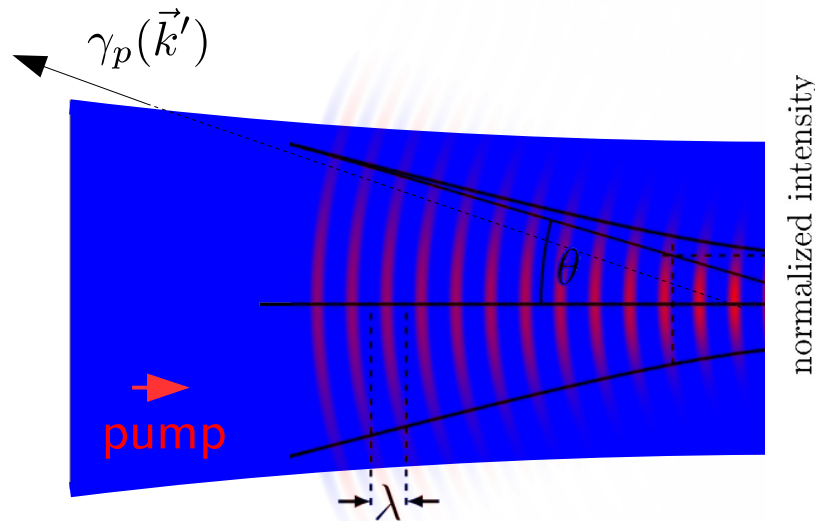
(iii) Vacuum birefringence

Our **results**:

[FK, Gies, Reuter, Zepf: arXiv:1507.01084]

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→ case (c): 

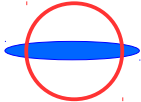


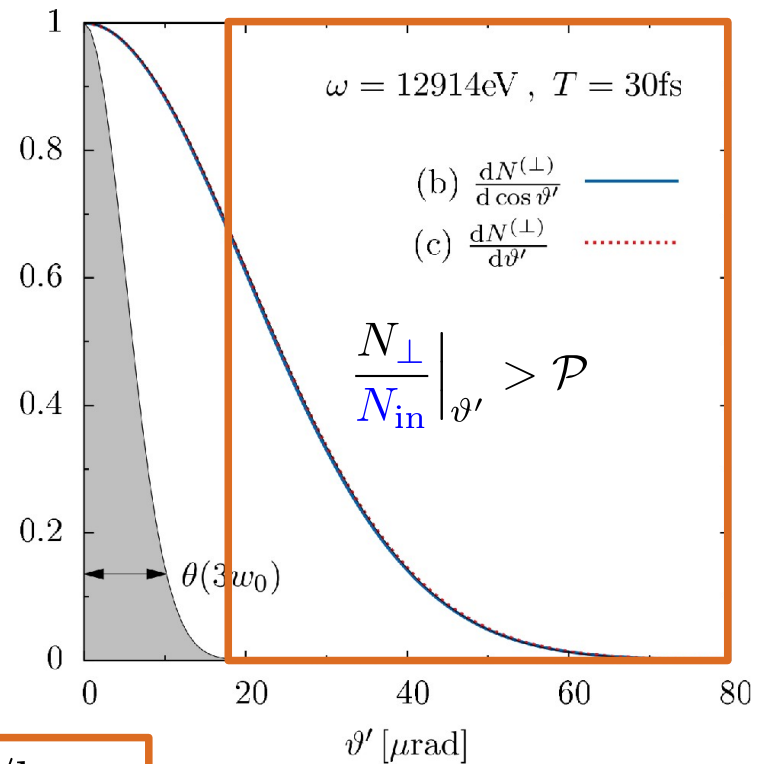
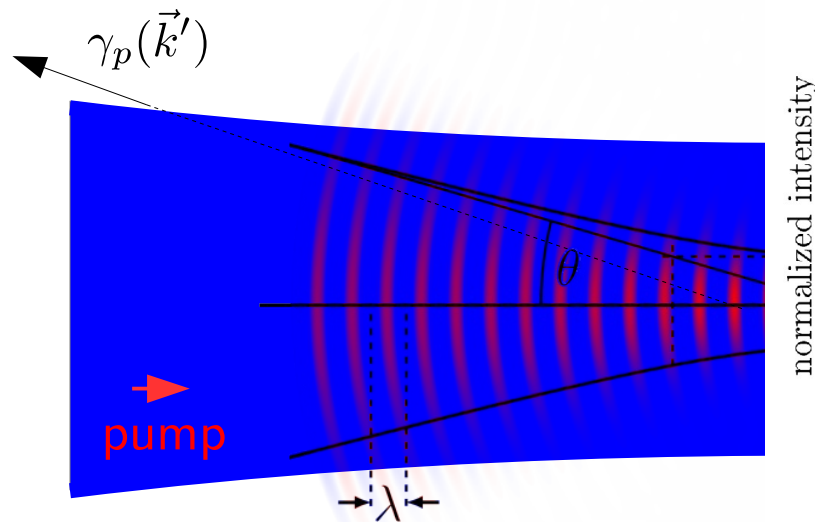
(iii) Vacuum birefringence

Our **results**:

[FK, Gies, Reuter, Zepf: arXiv:1507.01084]

- we consider three different cases

→ case (c): 



→ repetition rate 1Hz : $N_{\perp} \approx 265/\text{hour}$

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[Gies, FK, Seegert: New J. Phys. **15** 083002 (2013) & **17** 043060 (2015)]

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Thank you for your attention!