

Pulsed emission and flaring activity of the Crab pulsar unified through magnetic reconnection in its striped wind?

Jérôme Pétri¹

Iwona Mochol¹

Hubert Baty¹

Makoto Takamoto^{2,*}

Seiji Zenitani³

¹Observatoire astronomique de Strasbourg, Université de Strasbourg, France.

²Max-Planck Institute for Nuclear Physics, 69117 Heidelberg, Germany. (* now in Japan)

³National Astronomical Observatory of Japan, Tokyo 181-8588, Japan.



Summary

1 A (very) brief reminder

2 Motivations

- Pulsed (very) high energy emission
- Flares in the Crab

3 Magnetic reconnection in the wind

- The striped wind model
- Single current sheet dynamics and VHE pulsed emission
- Double current sheet dynamics and flaring activity

4 Conclusions

1 A (very) brief reminder

2 Motivations

- Pulsed (very) high energy emission
- Flares in the Crab

3 Magnetic reconnection in the wind

- The striped wind model
- Single current sheet dynamics and VHE pulsed emission
- Double current sheet dynamics and flaring activity

4 Conclusions

Pulsars: orders of magnitude

From observations

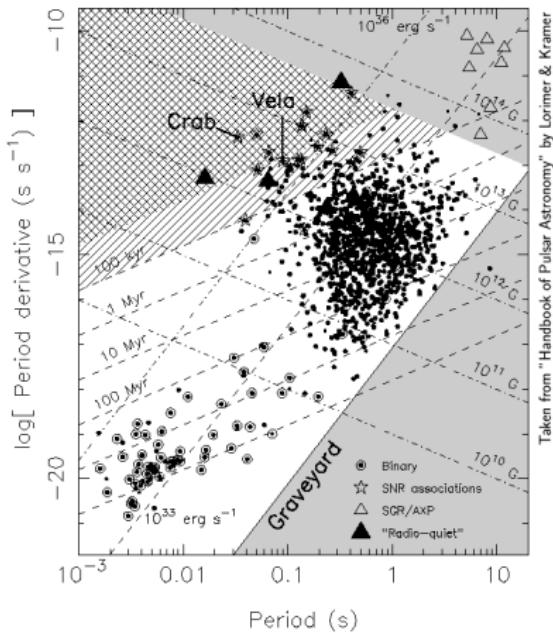
- period $P \in [1 \text{ ms}, 1 \text{ s}]$
- period derivative $\dot{P} \in [10^{-18}, 10^{-15}]$
- spin-down losses well constrained

$$L_{\text{sp}} = 4\pi^2 I \dot{P} P^{-3} \approx 10^{24-31} \text{ W}$$

very different from black holes or accreting neutron stars

- inferred magnetic field estimate by dipole radiation

$$B = 3.2 \times 10^{15} \sqrt{P \dot{P}} = 10^{5-8} \text{ T}$$



1 A (very) brief reminder

2 Motivations

- Pulsed (very) high energy emission
- Flares in the Crab

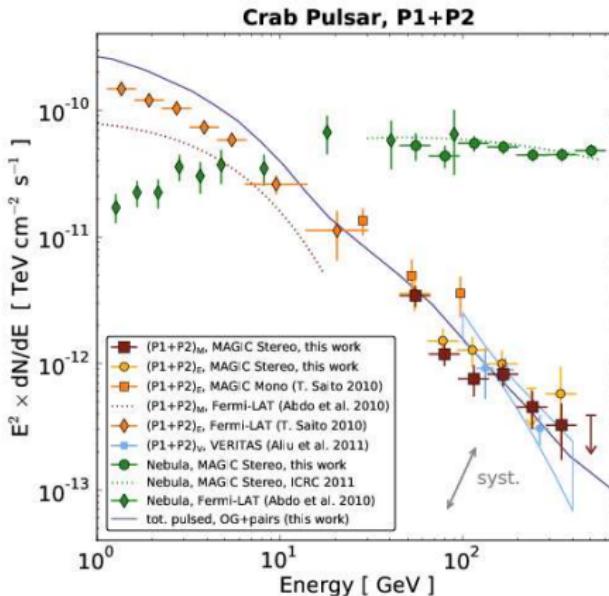
3 Magnetic reconnection in the wind

- The striped wind model
- Single current sheet dynamics and VHE pulsed emission
- Double current sheet dynamics and flaring activity

4 Conclusions

Gamma-ray pulsars: from MeV/GeV up to TeV?

- detection of pulsed emission from the Crab at 200-400 GeV
- compatible with the spectrum in the Fermi band
- spectrum as a broken power law rather exponential cut-off



(Aleksic et al, 2012)

Crab Flares: light-curves

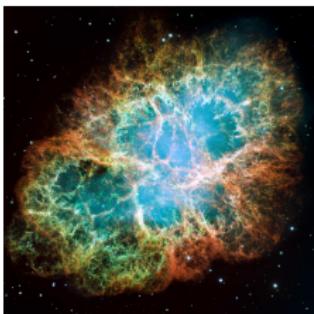


Figure : The Crab nebula.

- unexpected fluctuations in the gamma-ray flux
- increase by a factor 10
- variations on a day scale
 - strong flares (F) lasting one day
 - weak waves (W) lasting one or two weeks
- short but powerful flares ($E \approx 10^{34}$ J)
- isotropic power = sizeable fraction of the spin-down luminosity

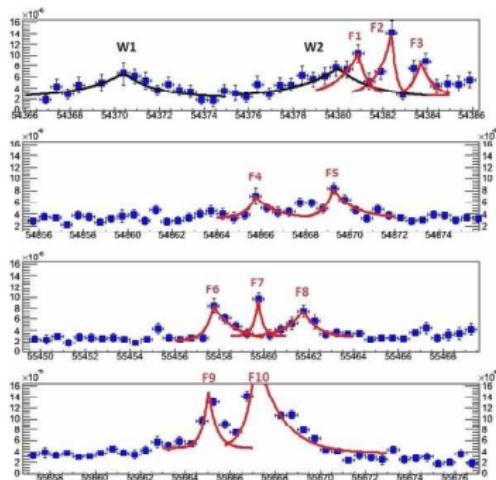


Figure : Temporal evolution of the Crab flares seen in gamma-rays (Striani et al., 2013).

1 A (very) brief reminder

2 Motivations

- Pulsed (very) high energy emission
- Flares in the Crab

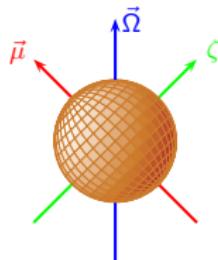
3 Magnetic reconnection in the wind

- The striped wind model
- Single current sheet dynamics and VHE pulsed emission
- Double current sheet dynamics and flaring activity

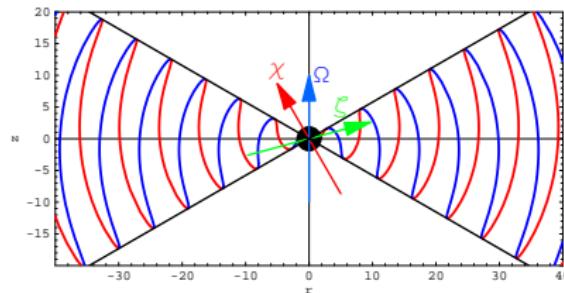
4 Conclusions

The striped wind

Near the star:
a rotating magnetic dipole



At large distances:
a relativistic striped wind



- $\vec{\Omega}$: rotation axis
- χ : magnetic axis inclination with respect to $\vec{\Omega}$
- ζ : line of sight inclination with respect to $\vec{\Omega}$

Presence of a current sheet wobbling around the equatorial plane.

- hot and magnetized plasma in the sheet
 - relativistic beaming $\Gamma_{\text{vent}} \gg 1$
- $\} \Rightarrow$ pulsed emission

Reconnection in the striped wind: two regimes

Current sheets are usually prone to magnetic reconnection through

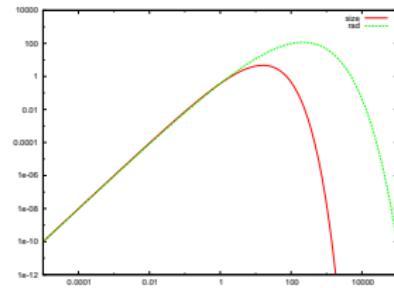
- plasma resistivity in MHD description.
- kinetic effects in a Vlasov description
(electron inertia, anisotropic pressure tensor).

When radiation is included, we distinguish two regimes for which efficiency is limited

- ➊ by radiation reaction: cut-off Lorentz factor of particles γ determined by $\tau_{\text{sync}} = \tau_{\text{acc}}$
 \Rightarrow exponential particle distribution cut off

$$n(\gamma) \propto \gamma^{-p} e^{-\gamma/\gamma_{\text{rad}}} \quad \Rightarrow \quad \varepsilon F_\varepsilon \propto e^{-\varepsilon^{1/3}}$$

- ➋ by escape: cut-off Lorentz factor of particles γ determined by the escape probability from the acceleration region $R_{\text{Larmor}} = \delta_{\text{thickness}}$
 \Rightarrow sharper cut off



$$n(\gamma) \propto \gamma^{-p} e^{-\gamma^2/\gamma_{\text{sl}}^2} \quad \Rightarrow \quad \varepsilon F_\varepsilon \propto e^{-\varepsilon^{1/2}}$$

(Mochol & Pétri, 2015)

SSC examples: Crab

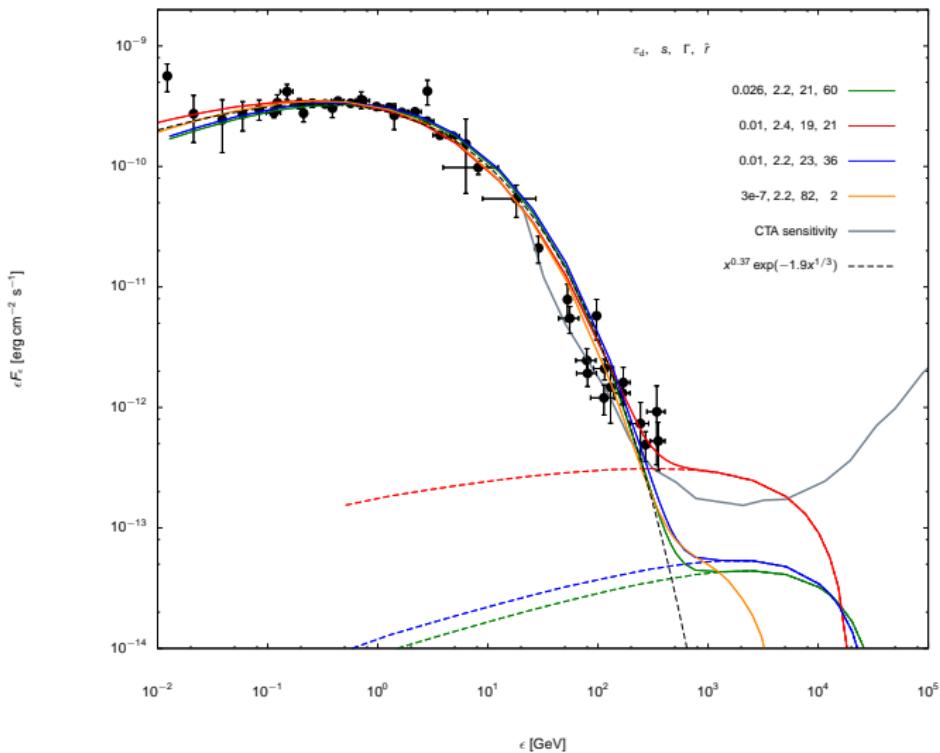


Figure : Crab synchrotron and SSC spectrum for different parameters of the model. CTA sensitivity is shown in grey.

SSC examples: Vela

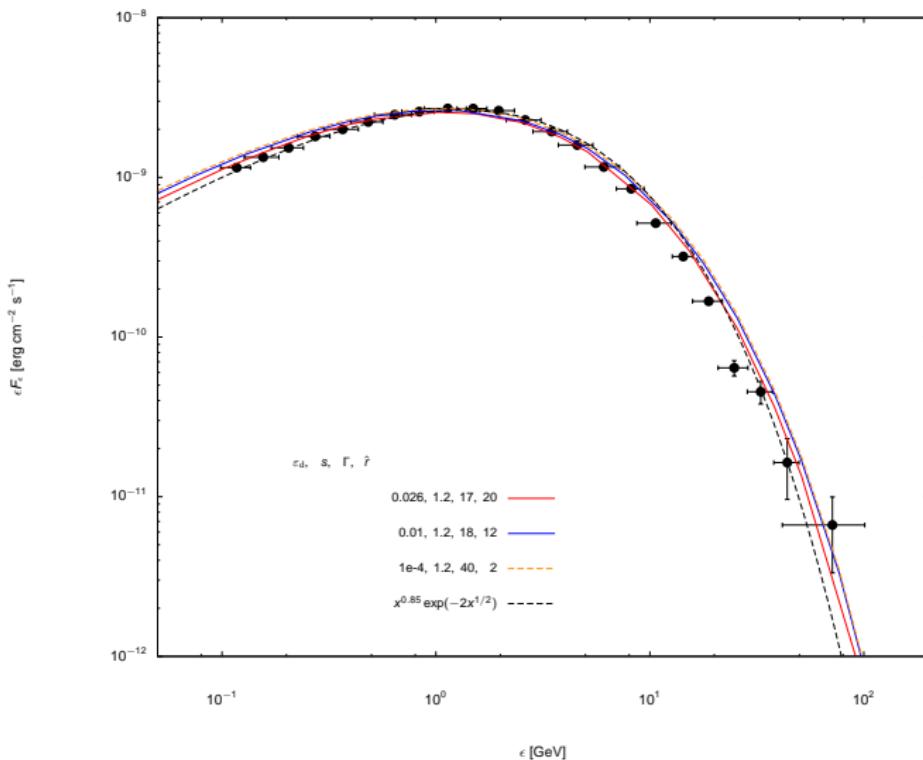
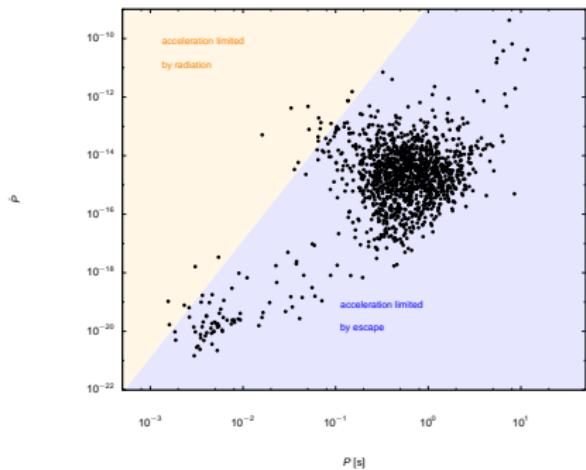


Figure : Vela synchrotron spectrum for different parameters of the model. SSC is not shown because to weak.

“Best fits” parameters and the two reconnection regimes in $P - \dot{P}$

Different high energy particle tails distributions
⇒ different sub-exponential cut-off spectra
Parameters: $\Gamma, \varepsilon_d, r_d, p$



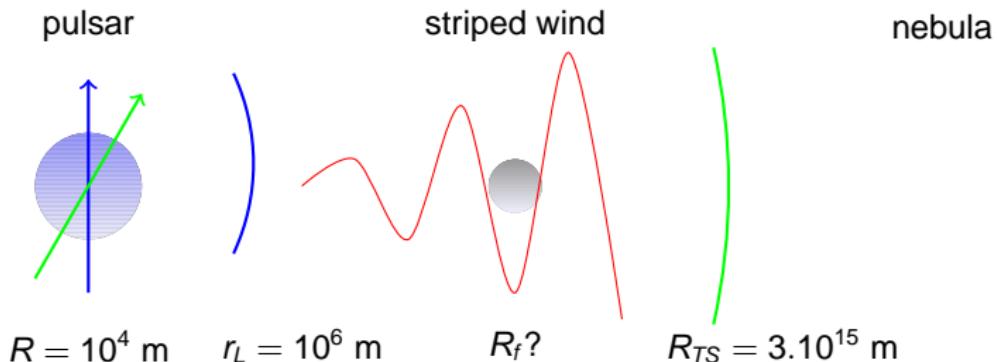
	Γ	ε_d	r_d	p	κ
Crab	23	0.01	36	2-2.4	10^4
Vela	18	0.01	12	1.2	14

The transition line between both reconnection regimes depends only on the observables P, \dot{P} as

$$\frac{\dot{E}_{38}^{3/2}}{P_{-2}} \sim 0.002$$

Figure : The two reconnection regimes in the $P - \dot{P}$ plot.

Simple estimates about the flares



Comparing the time scales

- too long for the Crab pulsar (33 ms)
- too short for the nebula evolution (years)
- size of emitting region, $L_f \approx c \Delta t \approx 1\text{d} \approx 3.10^{13} \text{ m} \approx 0.01 R_{TS}$.

Possible locations

- within the striped wind $r_L < R_f < R_{TS}$.
- at the termination shock $R_f = R_{TS}$.
- within the nebula $R_f > R_{TS}$.

Flares in the unshocked wind!

- timescale of reconnection $\tau \approx \sqrt{\tau_A \tau_D} = S^{1/2}$
as in classical MHD
 τ_A Alfvén timescale
 τ_D diffusion timescale
 S Lundquist number
- outflow not relativistic
- reconnection rate too slow for the flares
- ⇒ tearing instability unable to explain fast rising time
- the answer: double tearing mode
(Baty et al., 2013; Pétri et al., 2015)

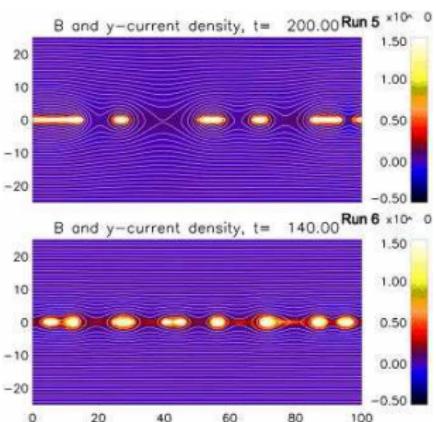


Figure : Relativistic pair plasma reconnection (Hesse & Zenitani, 2007).

Numerical setup

Double Harris current sheet

$$B_x = B_0 \left(1 + \tanh\left(\frac{y - y_0}{L}\right) - \tanh\left(\frac{y + y_0}{L}\right) \right)$$

- width of one current sheet, $L = 1$
- separation $2y_0 = 6L$
- uniform temperature $T = 1$
- normalization: magnetic field $B^2 = 2$ and density $\rho = 1$
- specific heat ratio $\Gamma = 4/3$
- Alfvén speed

$$v_A = c \sqrt{\frac{\sigma}{\sigma + 1}}$$

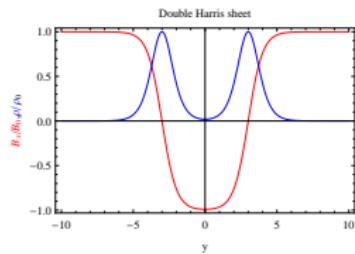
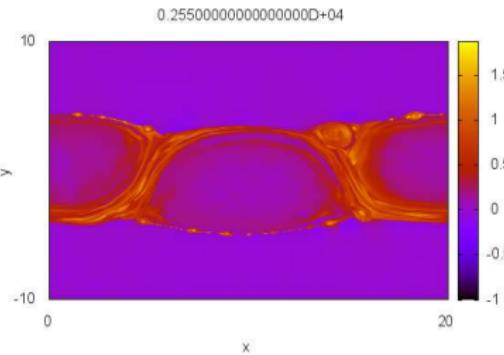
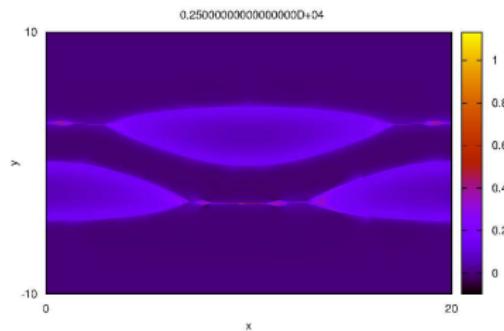


Figure : The two current sheets in the simulations.

Two free parameters

- magnetization $\sigma \gg 1$
- Lundquist number $S = L c / \eta \gg 1$

Simulation example



Simulation example: four stages

- 1 linear evolution of the DTM as an antisymmetric pattern
- 2 saturation: Rutherford regime (maximal size of the islands with diffusion)
- 3 secondary instability: fast non-linear evolution
- 4 relaxation to the final state: magnetic field dissipated into bulk motion and particle thermalization

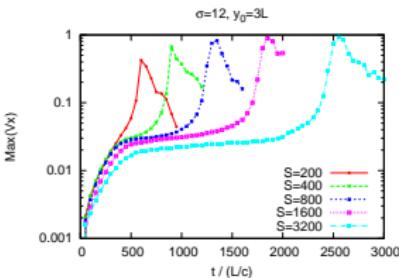


Figure : Maximum flow velocity V_x with $\sigma = 12$.

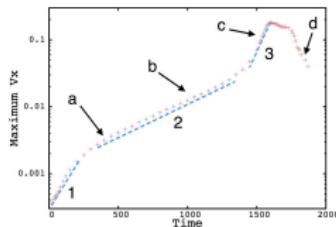


Figure : The four phases in the DTM (Baty et al., 2013).

Flares in the Crab

Time scales

- observational constrain $\Delta T \lesssim \tau_r \approx 10$ hr $\Rightarrow \Gamma \lesssim 150$
- consistent with $\Gamma \approx 20 - 50$ from Pétri & Kirk (2005)

Energetics

- energy release in a flare 10^{34} J
- local magnetic field in the flare around 2 T
- wave nature of the striped wind implies emission at $r \approx 50 r_L$.
- luminosity according to $L = \mathcal{D}^4 L'$
- in agreement with the 2011 flare
 $L_{>100\text{ MeV}} \propto \varepsilon_c^{3.42 \pm 0.86}$
(Buehler et al., 2012)

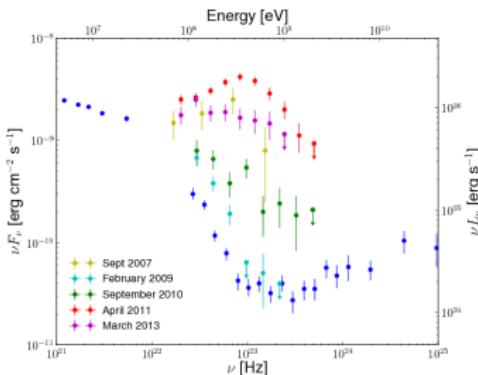


Figure : Spectra of several Crab flares.

1 A (very) brief reminder

2 Motivations

- Pulsed (very) high energy emission
- Flares in the Crab

3 Magnetic reconnection in the wind

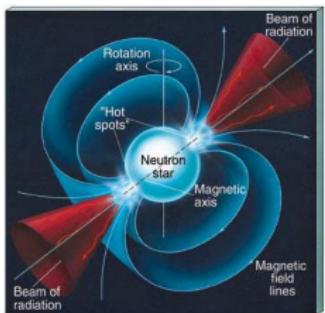
- The striped wind model
- Single current sheet dynamics and VHE pulsed emission
- Double current sheet dynamics and flaring activity

4 Conclusions

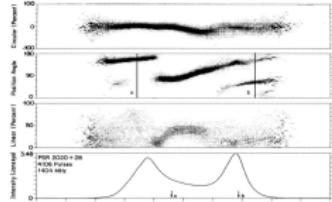
Relativistic magnetic reconnection in pulsar striped wind can explain

- ➊ pulsed gamma-ray emission in MeV-Gev (TeV)
 - particle acceleration in two regimes: radiative cooling or size-limited
 - for Crab spectrum, a new pulsed SSC component at (sub)TeV? (CTA)
 - wind Lorentz factor $\Gamma_{\text{Crab}} < 100$ and $\Gamma_{\text{Vela}} < 50$
- ➋ DTM good candidate to explain short and powerful gamma-ray flares in strongly magnetized plasmas
 - striped wind is a natural place where to expect double/multiple tearing modes
 - wind parameters consistent with independent estimates (pulsed gamma radiation/optical polarization)

Contribution of multipolar fields to radio and high-energy emission of pulsars

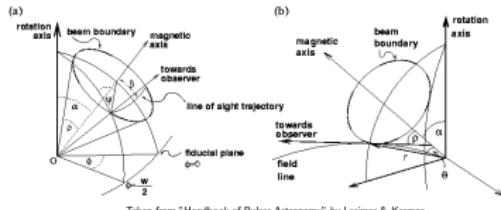


Schematic view of a pulsar.

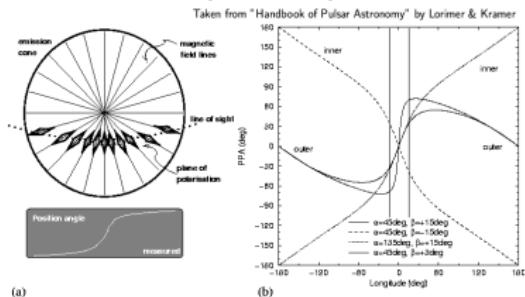


Example of radio-polarisation.

Website: <http://amwdb.u-strasbg.fr/HighEnergy/spip.php?article271>



A polar cap.



Rotating vector model and explanation for polarisation.

1 A (very) brief reminder

2 Motivations

- Pulsed (very) high energy emission
- Flares in the Crab

3 Magnetic reconnection in the wind

- The striped wind model
- Single current sheet dynamics and VHE pulsed emission
- Double current sheet dynamics and flaring activity

4 Conclusions

- Abdo A. A. et al., 2013, ApJS, 208, 17
- Baty H., Petri J., Zenitani S., 2013, MNRAS, 436, L20
- Buehler R. et al., 2012, ApJ, 749, 26
- Hesse M., Zenitani S., 2007, Physics of Plasmas, 14, 112102
- Kirk J. G., Lyubarsky Y., Petri J., 2009, 357, 421
- Mochol I., Pétri J., 2015, MNRAS, 449, L51
- Petri J., 2012, MNRAS, 424, 2023
- Pétri J., Kirk J. G., 2005, ApJL, 627, L37
- Pétri J., Takamoto M., Baty H., Zenitani S., 2015, Plasma Physics and Controlled Fusion, 57, 014034
- Striani E. et al., 2013, ApJ, 765, 52