

FLAVOR THEORY SUMMARY

Gudrun Hiller, Dortmund

Generational structure & mixing is feature of SM and many BSM d.o.f.'s; VIRTUES:

i) high sensitivity to BSM in flavor violation;

FCNCs $b \rightarrow sll, \mu \rightarrow e\gamma, h \rightarrow \tau\mu, \dots$

we may discover BSM in flavor physics (even first)

ii) flavorful processes are intrinsically linked to "flavor puzzle"

Y_{SM} hierarchies from where?

with BSM-signal, we may be able to progress here

iii) plenty of modes $s \rightarrow d, c \rightarrow u, b \rightarrow s, d, t \rightarrow c, u, \mu \rightarrow e, \tau \rightarrow \mu, e$

plus charged ones; plenty of ongoing & future experiments, too.

we may identify \mathcal{L}_{BSM} ; complementary to direct searches

- SM precision: Higher order, hadronic matrix elements, lattice QCD
- bottom-up model-building/simplified models (Z' , extra Higgses, leptoquarks..) "data-driven"
- multi-observable fits to couplings "Wilson coefficients" $C_{7,9,10}$ of standardized $|\Delta B| = |\Delta S| = 1$ effective hamiltonian; few groups, dedicated effort, exploit correlations, precision test of the SM
- design/use clean observables; related to (approximate) symmetries of the SM: lepton-nonuniversality, CP, helicity, LFV .. "null tests"
- Higgs physics: $hf\bar{f}$ and $hf\bar{f}'$ – are couplings SM-like?
- quarks together with leptons: hint of lepton-nonuniversality in B -decays; searches for LFV

Flavor anomalies

$h \rightarrow \mu\tau$

$b \rightarrow s$

Current flavor anomalies

- CMS [1502.07400]: 2.4σ lepton flavor violation:

$$\text{BR}(h \rightarrow \mu\tau) = (0.84^{+0.39}_{-0.37}) \%$$

- LHCb [1406.6482]: 2.6σ lepton non-universality:

$$R(K) \equiv \frac{B \rightarrow K\mu\mu}{B \rightarrow Kee} = 0.745^{+0.090}_{-0.074} \pm 0.036,$$

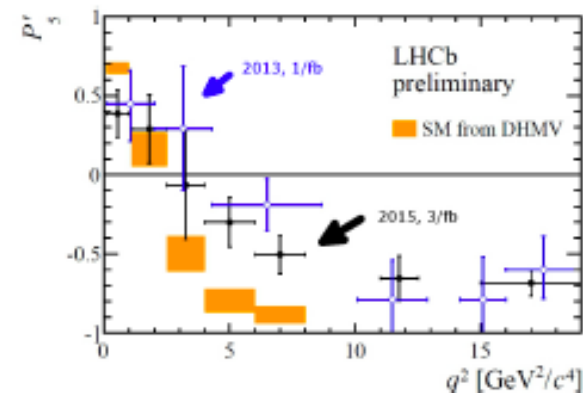
SM prediction $R(K) = 1 \pm \mathcal{O}(10^{-4})$ [Bobeth, Hiller, Piranishvili, 0709.4174].

- LHCb [LHCb-CONF-2015-002]: 3.7σ deviation in angular observable P'_5 of

$$B \rightarrow K^*\mu\mu \rightarrow K^+\pi^-\mu\mu,$$

confirming 1/fb analysis [1308.1707].

Might be QCD, charm-loop...



Exciting new physics or boring statistics?

HIGGS Flavor

Avital Dery, Erik Schumacher, Matthias König, Avelino Vicente

	BEST FIT TO $B(H \rightarrow \mu\tau)$, %
Expected limit: $BR(h \rightarrow \tau\mu) < 0.75\%$	Best fit value:
Observed limit: $BR(h \rightarrow \tau\mu) < 1.51\%$	$BR(h \rightarrow \tau\mu) = (0.84^{+0.39}_{-0.37})\%$

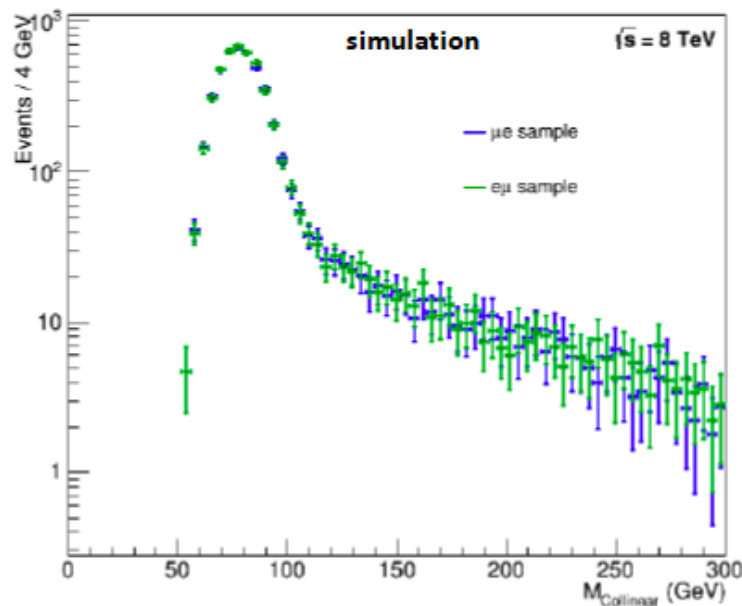
2.4 σ from zero

Avital Dery, Multi Higgs Models, 2/9/14

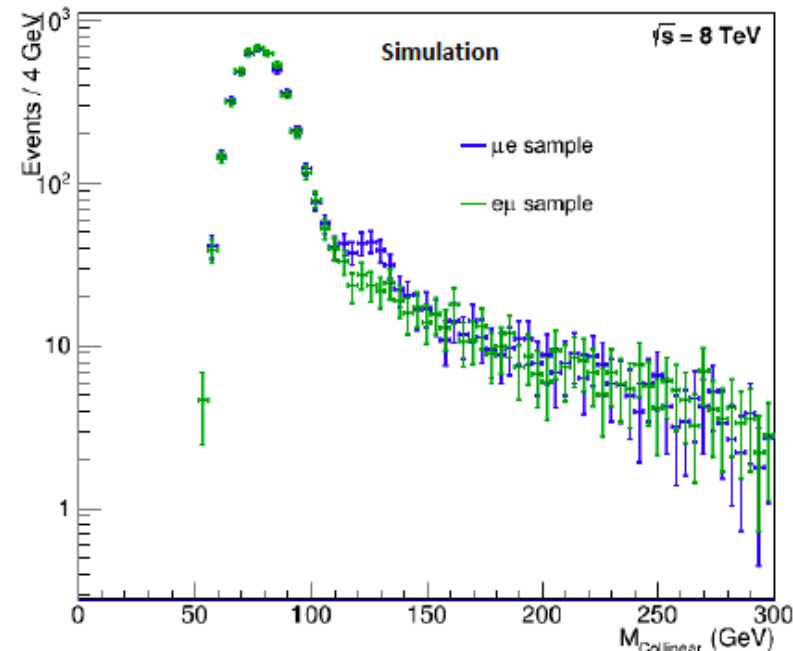
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New exp method to search for $h \rightarrow \tau\mu$ with $h \rightarrow \tau_e\mu$; in prep. for ATLAS A.Dery

**SM Background simulation
Pythia + Delphes ATLAS card**



**SM Background + BR($h \rightarrow \tau\mu$) = 2%
Pythia + Delphes ATLAS card**



[S. Bressler, AD, A. Efrati, Phys. Rev. D 90 (2014) Editors Selection arXiv:1405.4545]

Explaining the CMS anomaly at face value is non-trivial (Dery, Vicente, Schumacher, Heeck):

Can do the trick: Multi-Higgs doublet models, $U(1)_{FN}$ w. holomorphic zeros, models with "more LFV spurions e.g from seesaw

Strong constraints in general from radiative FCNCs $\tau \rightarrow \mu\gamma$ and other flavor violation. Successful models generically are testable/predictive!

S_4 flavor symmetry explaining higgs anomalies; E.Schumacher "PMNS"-type model-building tools

The Model (charged leptons)

Objective: Build a model with LFV and Triality in S_4

Ingredients:

- $L = (L_e, L_\mu, L_\tau) : \mathbf{3}$, $\tau_R : \mathbf{1}$, $(e_R, \mu_R) : \mathbf{2}$
required for LFT structure
- Three $SU(2)$ doublets to induce LFV $\phi = (\phi_1, \phi_2, \phi_3) : \mathbf{3}$
- VEV alignment $\frac{v}{\sqrt{3}}(1, 1, 1)$ of the ϕ_i breaks S_4 down to Z_3

Result:

$$M_l = \frac{v_{SM}}{\sqrt{6}} \begin{pmatrix} 1 & 1 & 1 \\ \omega^2 & \omega & 1 \\ \omega & \omega^2 & 1 \end{pmatrix} \text{diag}(y_e, y_\mu, y_\tau)$$

\Rightarrow Charged lepton mass basis coincides with Z_3 basis $(e, \mu, \tau) \sim (\omega, \omega^2, 1)$

predicts $h \rightarrow \tau e$ not far from $h \rightarrow \tau \mu$

Predictions

@ 1σ and $m_\eta = 200$ GeV

$$\begin{array}{ccccc} 0.002 & < & \theta & < & 0.090, \\ 126 \text{ GeV} & < & m_H & < & 204 \text{ GeV} \end{array}$$

- With these parameters we predict

$$\begin{array}{lll} \text{Br}(\tau \rightarrow \mu\gamma) & \in (0.3 - 1.3) \times 10^{-8}, & < 4.4 \times 10^{-8} \\ \text{Br}(\tau \rightarrow e\gamma) & \in (0.3 - 1.3) \times 10^{-8}, & < 1.2 \times 10^{-7} (?) \\ \text{Br}(\tau \rightarrow 3\mu) & \in (1.9 - 8.1) \times 10^{-10}, & < 2.1 \times 10^{-8} \\ \text{Br}(\tau \rightarrow 3e) & \in (0.9 - 4.1) \times 10^{-9}, & < 2.7 \times 10^{-8} \\ \text{Br}(h \rightarrow e\tau) & \in (0.4 - 1.2) \times 10^{-2} & \\ \text{Br}(h \rightarrow e\mu) & \in (1.5 - 4.2) \times 10^{-5} & \end{array}$$

- The LFV channels with τ lepton final states are closely related

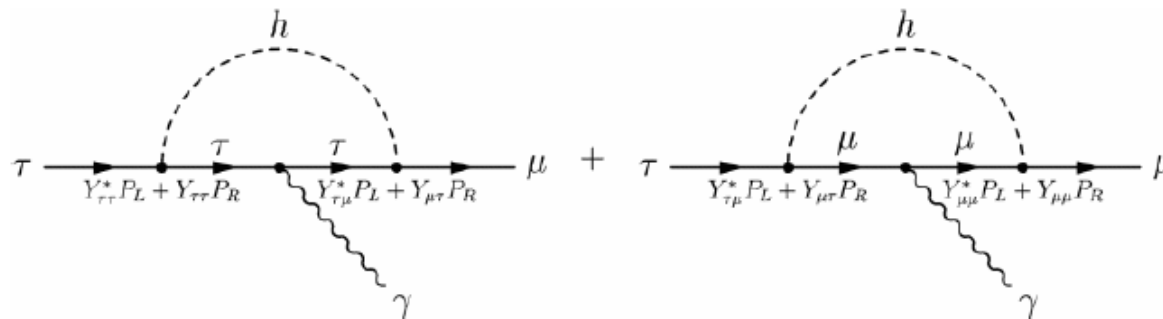
$$\frac{\text{Br}(h \rightarrow \mu\tau)}{\text{Br}(h \rightarrow e\tau)} \approx \frac{|y_{\mu\tau}|^2}{|y_{e\tau}|^2} \approx 1 \quad \text{for small } \theta$$

Therefore large LFV also expected in $h \rightarrow e\tau$ channel

A new hope: Type-III 2HDM

[Davidson, Grenier, 2010; Harnik et al, 2013; Kopp, Nardecchia, 2014]

$$\mathcal{L}_Y = m_i \bar{f}_L^i f_R^i - Y_{ij} (\bar{f}_L^i f_R^j + \text{h.c.})$$



[Figure from Harnik et al, arXiv:1209.1397]

A model!
2HDM type III



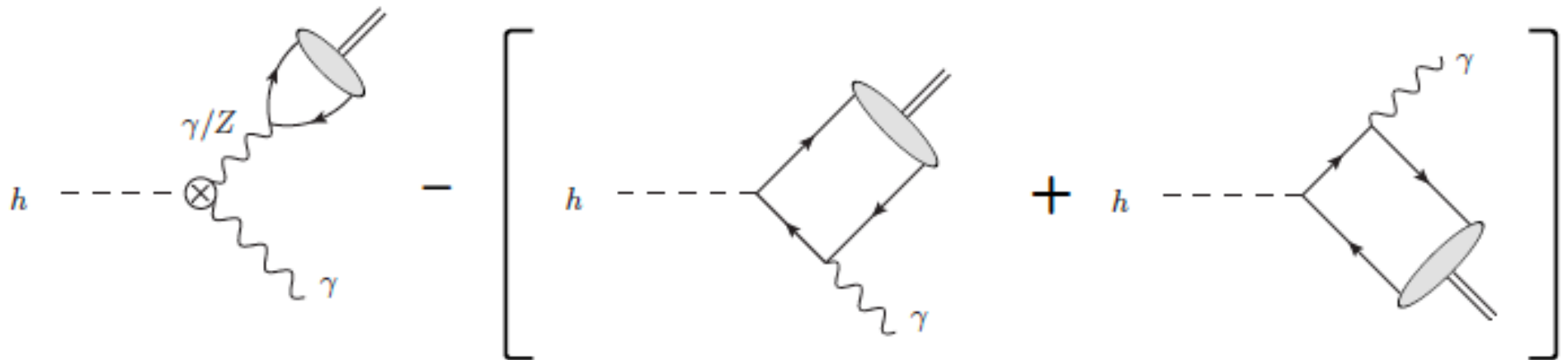
In *principle*... it is possible to account for the **CMS excess**!

Higgs LFV couplings and other LFV processes: [Celis et al, 2014]

See also some recipes for model builders: [Dery et al, 2014]

Probing light quark yukawas with exclusive higgs decays; M.König

Several different diagram topologies:



$$\frac{|\Gamma(h \rightarrow V\gamma)|}{\Gamma(h \rightarrow \gamma\gamma)} = \frac{8\pi\alpha^2(m_V)}{\alpha} \frac{Q_V^2 f_V^2}{m_V^2} \left(1 - \frac{m_V^2}{m_h^2}\right)^2 |1 - \kappa_q \Delta_V - \delta_V|^2$$

SM predictions

Numerical results

Assuming SM couplings of all particles, we find:

$$\text{BR}(h \rightarrow \rho^0 \gamma) = (1.68 \pm 0.02_f \pm 0.08_{h \rightarrow \gamma\gamma}) \cdot 10^{-5}$$

$$\text{BR}(h \rightarrow \omega \gamma) = (1.48 \pm 0.03_f \pm 0.07_{h \rightarrow \gamma\gamma}) \cdot 10^{-6}$$

$$\text{BR}(h \rightarrow \phi \gamma) = (2.31 \pm 0.03_f \pm 0.11_{h \rightarrow \gamma\gamma}) \cdot 10^{-6}$$

$$\text{BR}(h \rightarrow J/\psi \gamma) = (2.95 \pm 0.07_f \pm 0.06_{\text{direct}} \pm 0.14_{h \rightarrow \gamma\gamma}) \cdot 10^{-6}$$

$$\text{BR}(h \rightarrow \Upsilon(1S) \gamma) = (4.61 \pm 0.06_{f_{-1.21}^{+1.75}} \pm 0.22_{h \rightarrow \gamma\gamma}) \cdot 10^{-9}$$

$$\text{BR}(h \rightarrow \Upsilon(2S) \gamma) = (2.34 \pm 0.04_{f_{-0.99}^{+0.75}} \pm 0.11_{h \rightarrow \gamma\gamma}) \cdot 10^{-9}$$

$$\text{BR}(h \rightarrow \Upsilon(3S) \gamma) = (2.13 \pm 0.04_{f_{-1.12}^{+0.75}} \pm 0.10_{h \rightarrow \gamma\gamma}) \cdot 10^{-9}$$

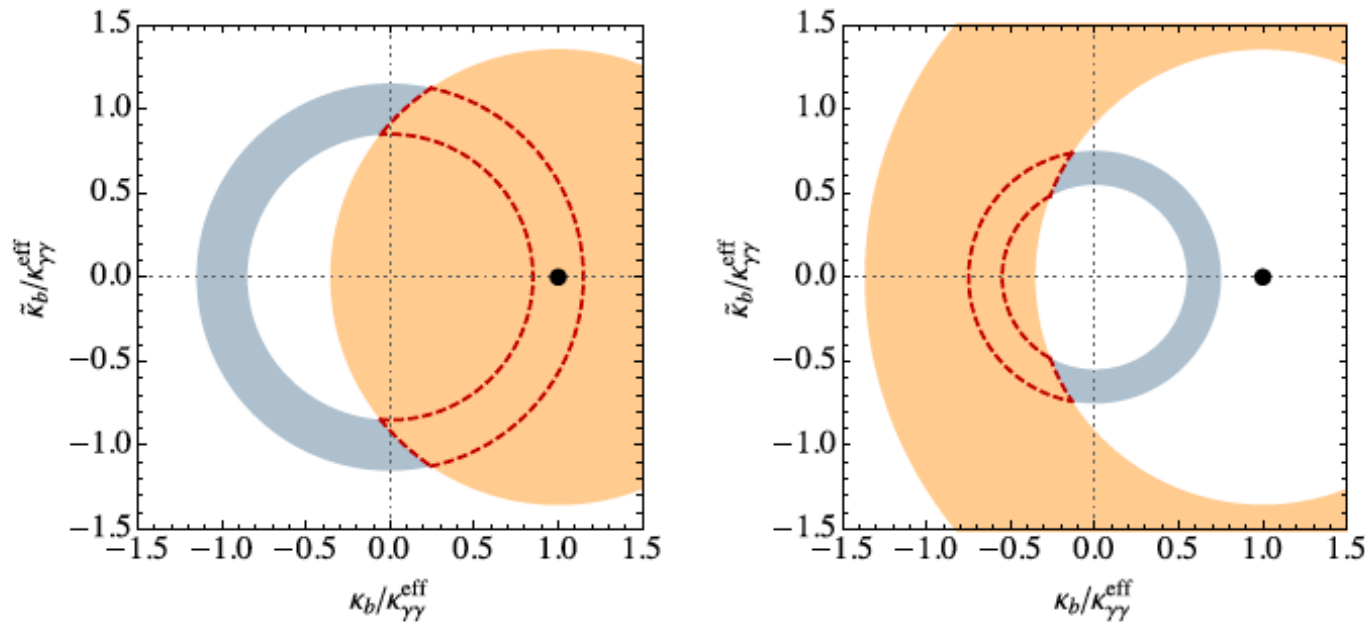
M.König

Correlations with $h \rightarrow b\bar{b}$

Phenomenology

JG|U

Possible future scenarios:



Blue circles: direct measurements of $h \rightarrow q\bar{q}$ constrain $\kappa_q^2 + \tilde{\kappa}_q^2$
 Red circles: measurements of $h \rightarrow \Upsilon\gamma$ constrain $(1 - \kappa_q)^2 + \tilde{\kappa}_q^2$

M.König

Precision Tests in $b \rightarrow sl\ell, \gamma$

Sebastien Descotes-Genon, Morimitsu Tanimoto

$$H_{eff} = -4G_F/\sqrt{2}V_{tb}V_{ts}^*\frac{\alpha_e}{4\pi} \sum C_i O_i$$

$$O_9 = \bar{s}\gamma_\mu P_L b \bar{\ell}\gamma^\mu \ell, \quad O_{10} = \bar{s}\gamma_\mu P_L b \bar{\ell}\gamma^\mu \gamma_5 \ell \quad O' \text{ from } O \text{ with } P_L \leftrightarrow P_R.$$

$$C_9^{SM} = 4.2, \quad C_{10}^{SM} = -4.2, \quad C'^{SM} \simeq 0.$$

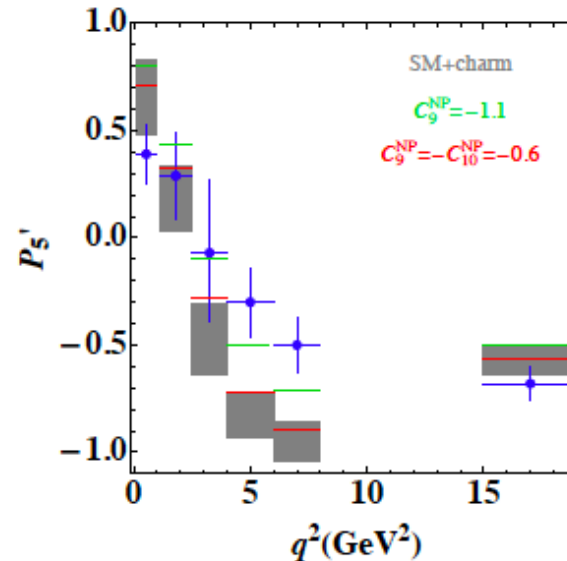
$$\text{Model-independent fits: } C = C^{SM} + C^{BSM}.$$

Fitting dimuon observables globally; S. Descotes-Genon

Global fits: 1D hypotheses

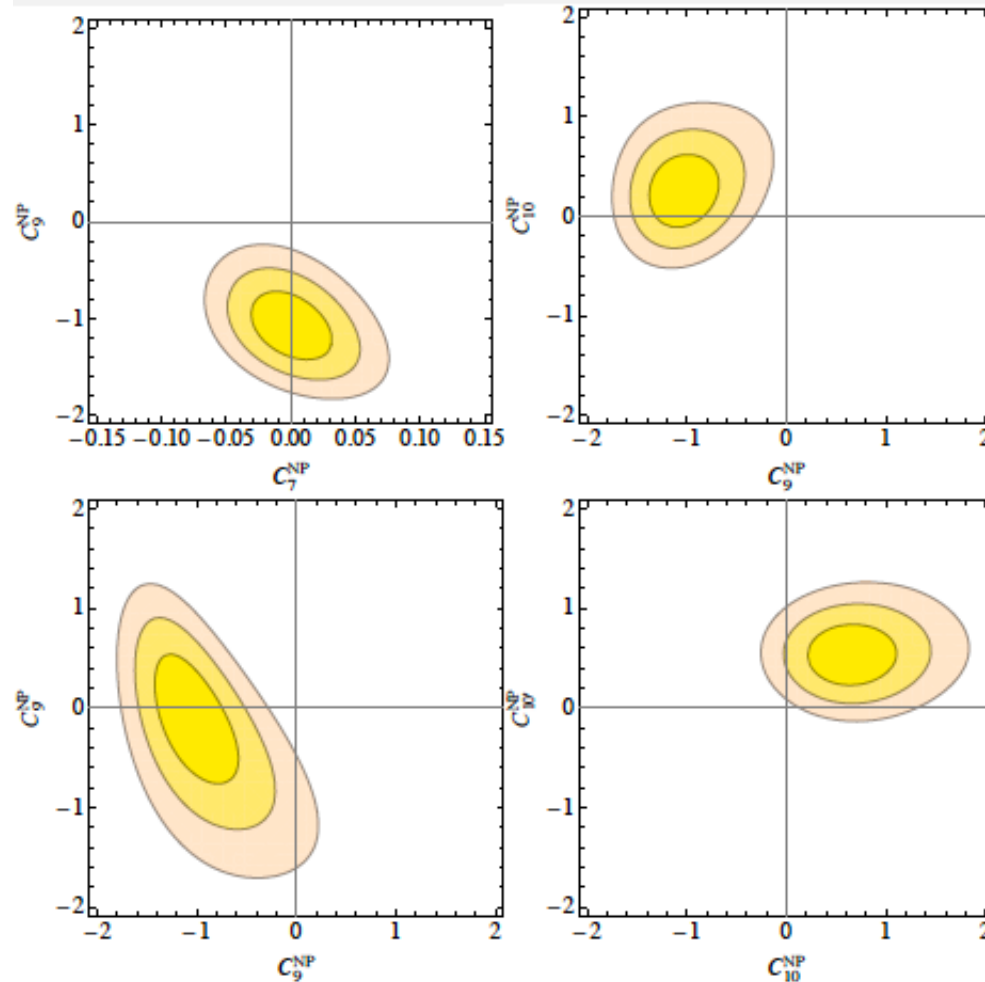
- χ^2 frequentist analysis to determine $C_i(\mu_{ref}) = C_i^{SM} + C_i^{NP}$
- $B \rightarrow K^* \mu\mu$ ($P_{1,2}, P'_{4,5,6,8}, F_L$: 5 large-recoil + 1 low-recoil bins),
 $B^+ \rightarrow K^+ \mu\mu, B^0 \rightarrow K^0 \mu\mu, B \rightarrow X_S \gamma, B \rightarrow X_S \mu\mu, B_S \rightarrow \mu\mu$ (Br),
 $B \rightarrow K^* \gamma$ (A_I and $S_{K^* \gamma}$)
 [Moriond 15, no correlations]

Hypothesis	Best fit	Pull
C_9^{NP}	-1.1	4.6
C_{10}^{NP}	0.62	2.4
C'_9	-1.0	3.4
C'_{10}	0.61	3.3
$C_9^{NP} = -C_{10}^{NP}$	-0.62	4.0
$C_9^{NP} = C_{10}^{NP}$	-0.37	1.7
$C_{9'} = C_{10'}$	0.32	1.3
$C_9^{NP} = C_{9'}$	-0.67	4.3
$C_{9'} = -C_{10'}$	-0.42	3.6



$C_9^{NP} < 0$ preferred, but alternatives with $C_9^{NP} = -C_{10}^{NP}$ and $C_9^{NP} = C_{9'}$

Global fits: 2D hypotheses



Hyp.	Best-fit pt	Pull
$(C_7^{\text{NP}}, C_9^{\text{NP}})$	(0.0, -1.1)	4.2
$(C_9^{\text{NP}}, C_{10}^{\text{NP}})$	(-1.1, 0.2)	4.2
$(C_9^{\text{NP}}, C_{9'})$	(-1.0, -0.1)	4.2
$(C_{10}^{\text{NP}}, C_{10'})$	(0.5, 0.6)	3.4

→ Main effect from C_9

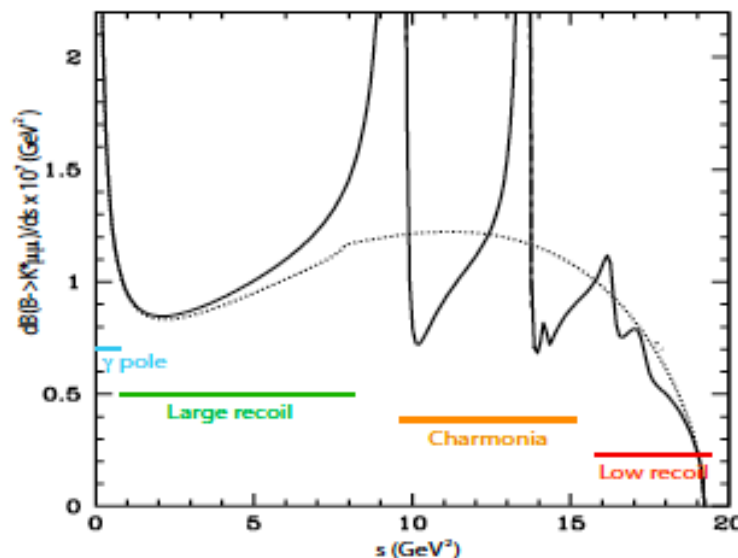
Explanations ?

- Z' boson
- Leptoquarks
- Composite models
- Difficult with susy (?)

[Almannshofer, Straub, Haisch, Gauld, Peczak,
Buras, De Fazio, Girrbach, Hiller, Schmaltz,
Varzielas, Crivellin...]

The global fits indicate a hint for BSM in $C_9^{\mu BSM} \simeq -1$; other coefficients can be affected, but to a lesser degree, too. A good fit is obtained with the $SU(2)_L$ relation $C_9 = -C_{10} \simeq -0.6$.

Main TH tasks: understand hadronic uncertainties: power corrections at low q^2 , $c\bar{c}$ contributions and improved form factors



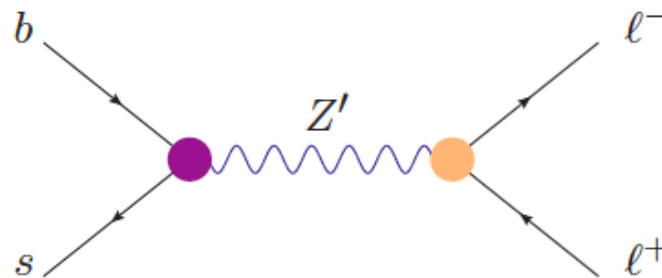
- Very large K^* -recoil ($4m_\ell^2 < q^2 < 1 \text{ GeV}^2$): γ almost real (C_7/q^2 divergence and light resonances)
- Large K^* -recoil ($q^2 < 9 \text{ GeV}^2$): energetic K^* ($E_{K^*} \gg \Lambda_{QCD}$: form factors via light-cone sum rules LCSR)

If taken at face value, the fit outcome $|C_9^{BSM}| \geq |C_{10}^{BSM}|$ requires non-standard model building. $Z \rightarrow \ell^+ \ell^-$ in SM opposite hierarchy.

Current proposals: Z' models (Heeck, Fuentes, Vicente),
Leptoquarks (de Medeiros Varzielas)

Z' model building

$$G \equiv SU(3)_c \otimes SU(2)_L \otimes U(1)_Y \otimes \underline{U(1)'}$$

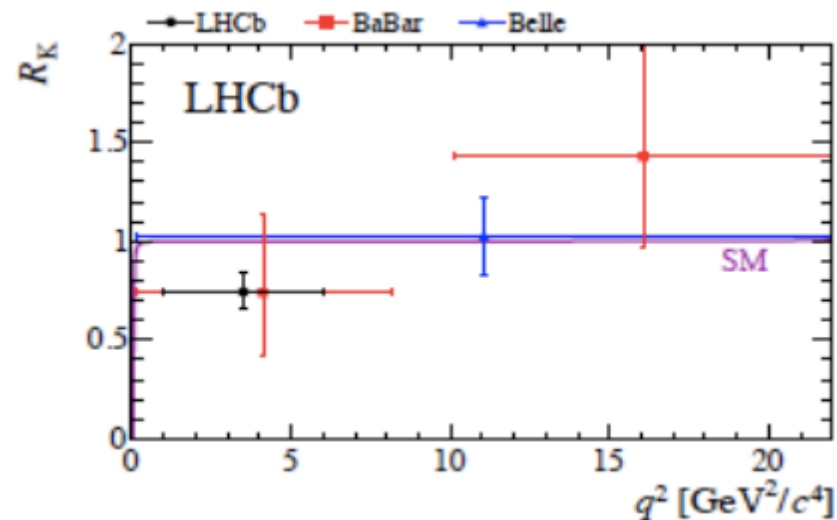


Flavor violating couplings to quarks Lepton-flavor universality violation

(J.Fuentes) Explain simultaneously with R_K – avoids large hadronic uncertainties

LNU and LFV in $b \rightarrow s$

Ivo de Medeiros, Javier Fuentes, Avelino Vicente, Julian Heeck

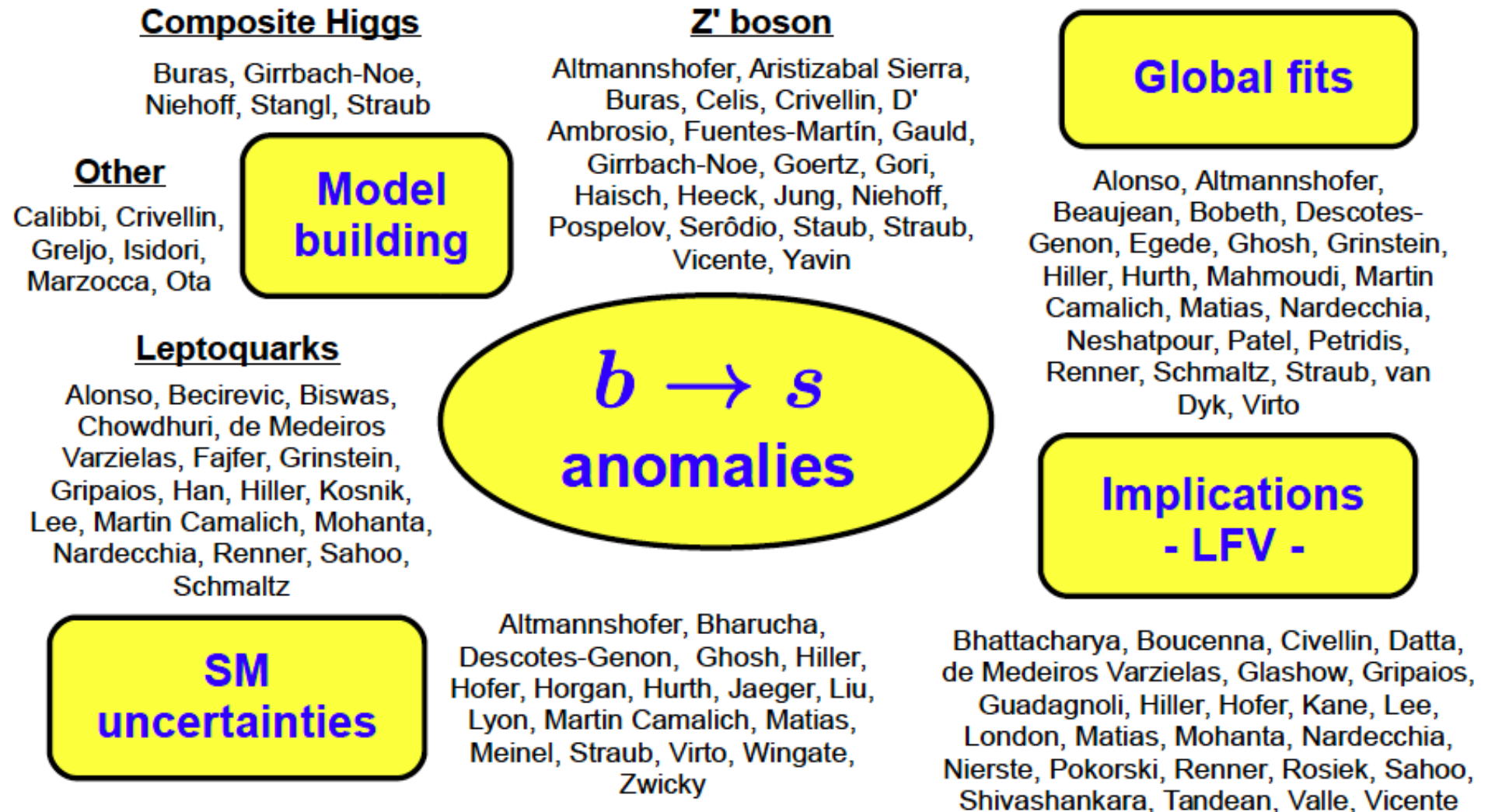


$$R_K = \frac{\mathcal{B}(\bar{B} \rightarrow \bar{K} \mu \mu)}{\mathcal{B}(\bar{B} \rightarrow \bar{K} e e)}$$

Lepton-universal models(SM): $R_K \simeq 1$ very clean

LHCb: $R_K = 0.745 \pm_{0.074}^{0.090} \pm 0.036 < 1$

Activity counter; A.Vicente



Explanations: Z' -models (BSM in $b \rightarrow s\mu\mu$, not in $b \rightarrow see$), leptoquarks (both $\mu\mu$ and ee possible), R-Parity violation

Vicente: dark $SM \times U(1)_X$ simultaneous expl of $b \rightarrow s$ anomalies and relic density

Fuentes: minimal input $SM \times U(1)$; uses anomaly conditions

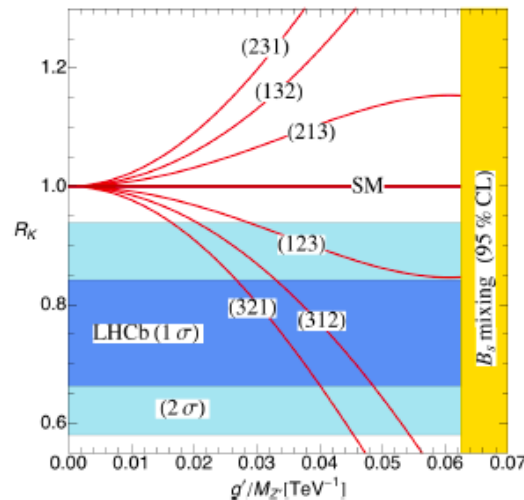
Heeck: gauged $SM \times U(1)_{\tau-\mu}$; amended by extra Higgs-dublet gives $h \rightarrow \tau\mu$

Varzielas: Leptoquarks with flavor symmetries, e.g. $U(1)_F$ (quarks) and $A_4 \times Z_3$ for leptons; relate leptoquark couplings to SM masses and mixings.

Correlations $B \rightarrow K$ with $B \rightarrow K^*$; J.Fuentes

Z' contributions: ratios and double ratios

- $$R_M \equiv \frac{\text{Br}(\bar{B} \rightarrow \bar{M}\mu^+\mu^-)}{\text{Br}(\bar{B} \rightarrow \bar{M}e^+e^-)} \quad M \in \{K, K^*, X_s, K_0(1430), \dots\}$$



Model	$C_9^{\text{NP}\mu}(1\sigma)$	$C_9^{\text{NP}\mu}(2\sigma)$
(1,2,3)	–	$[-2.92, -0.61]$
(3,1,2)	$[-0.93, -0.43]$	$[-1.16, -0.17]$
(3,2,1)	$[-1.20, -0.53]$	$[-1.54, -0.20]$

Good for $B \rightarrow K^*\mu^+\mu^-$ ✓

- $$\hat{R}_M \equiv \frac{R_M}{R_K} = 1$$

[Hiller, Schmaltz '15]

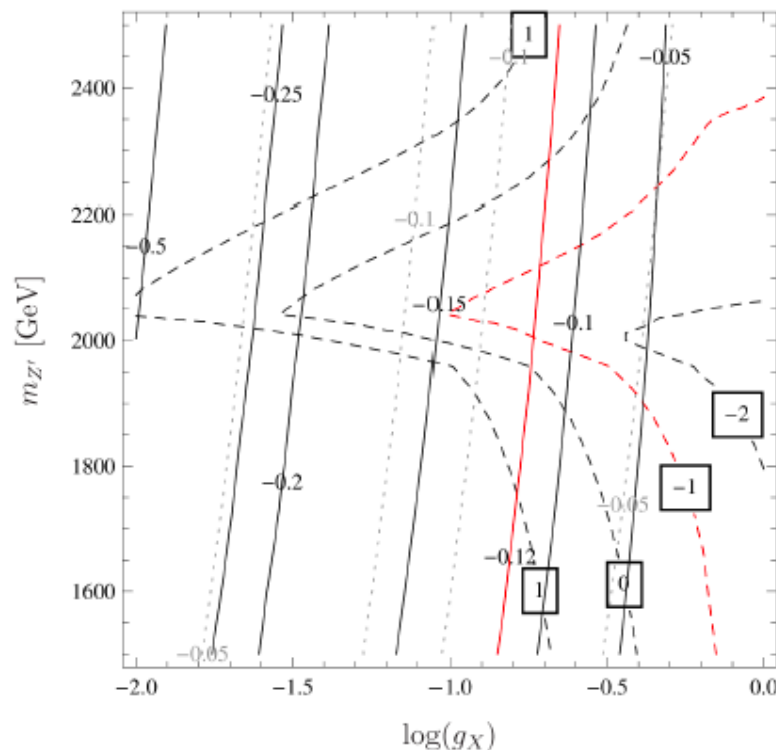
Test of the flavor structure of the model!

$SM \times U(1)_X$: A.Vicente

Dark matter and LHCb anomalies

$C_9^{\text{NP}}/C_9^{\text{SM}}$ (full) $\log(\Omega_{\text{DM}} h^2)$ (dashed) $C_9^{\text{NP}}/C_9^{\text{SM}}$ (tree) (dotted gray)

[DM RD Computed with **micrOMEGAs**]



Parameters:

$$\lambda_Q^b = \lambda_Q^s = 0.025$$

$$\lambda_L^\mu = 0.5$$

$$m_Q = m_L = 1 \text{ TeV}$$

$$m_\chi^2 = 1 \text{ TeV}^2$$

- Compatible with **flavor constraints** (small quark mixings)
- **Resonance** required to get the correct DM relic density
- Large **loop effects** for low g_X

$b \rightarrow s$ anomalies – correlations with direct searches: J.Heeck

LHC constraints

Z' couples to first-gen. quarks \Rightarrow direct detection via $pp \rightarrow Z' \rightarrow \mu^+ \mu^-$.

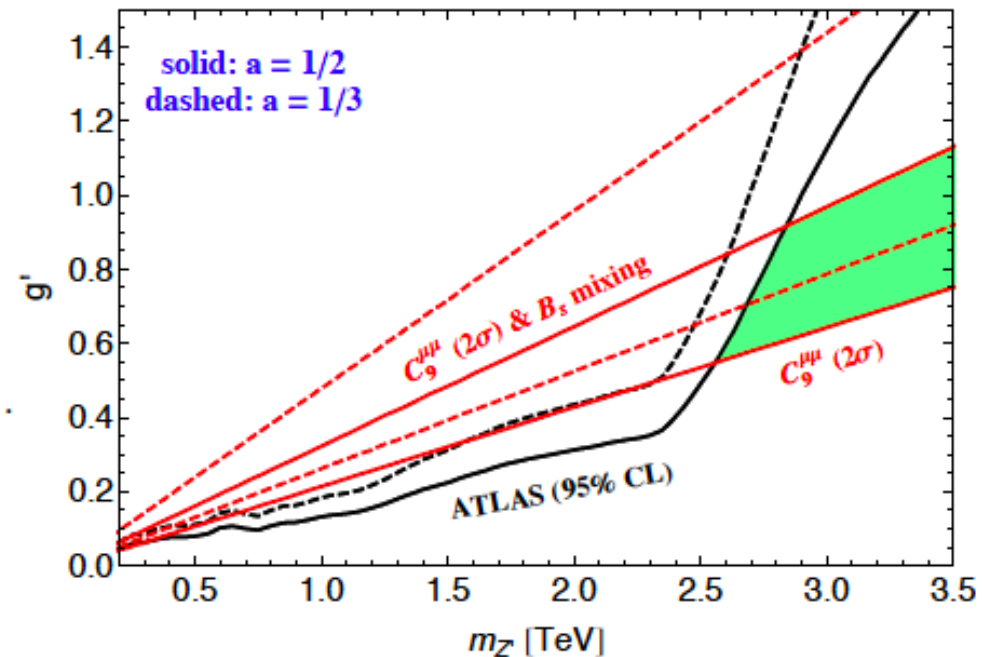
- For $m_t \ll m_{Z'} < 2m_{\nu_R}$:

$$\text{BR}(Z' \rightarrow \mu\mu) \simeq \frac{1}{3 + 4a^2},$$

and

$$ee : \mu\mu : \tau\tau : uu : dd : ss : cc : bb : tt \\ = 0 : 1 : 1 : \frac{a^2}{3} : \frac{a^2}{3} : \frac{a^2}{3} : \frac{a^2}{3} : \frac{4a^2}{3} : \frac{4a^2}{3}.$$

- Can rescale $B - L$ limits from ATLAS [1405.4123].
- Flavor violating decays $Z' \rightarrow bs$ suppressed.



Look forward to new LHC run!

In models with LNU there is generically also LFV.

An exception is the minimal $U(1)$ extension by Fuentes.

LFV can show up in B -decays and Higgs decay (Heeck)

predictions in leptoquark model with flavor symmetries (Varzielas):

$M \lesssim 50 \text{ TeV}$

$$\mathcal{B}(B \rightarrow K \mu^\pm e^\mp) \simeq 3 \cdot 10^{-8} \kappa^2 \left(\frac{1 - R_K}{0.23} \right)^2, \quad (1)$$

$$\mathcal{B}(B \rightarrow K e^\pm \tau^\mp) \simeq 2 \cdot 10^{-8} \kappa^2 \left(\frac{1 - R_K}{0.23} \right)^2, \quad (2)$$

$$\mathcal{B}(B \rightarrow K \mu^\pm \tau^\mp) \simeq 2 \cdot 10^{-8} \left(\frac{1 - R_K}{0.23} \right)^2, \quad (3)$$

and

$$\mathcal{B}(\mu \rightarrow e\gamma) \simeq 2 \cdot 10^{-12} \frac{\kappa^2}{\rho^2} \left(\frac{1 - R_K}{0.23} \right)^2, \quad (4)$$

$$\mathcal{B}(\tau \rightarrow e\gamma) \simeq 4 \cdot 10^{-14} \frac{\kappa^2}{\rho^2} \left(\frac{1 - R_K}{0.23} \right)^2, \quad (5)$$

$$\mathcal{B}(\tau \rightarrow \mu\gamma) \simeq 3 \cdot 10^{-14} \frac{1}{\rho^2} \left(\frac{1 - R_K}{0.23} \right)^2, \quad (6)$$

$$\mathcal{B}(\tau \rightarrow \mu\eta) \simeq 4 \cdot 10^{-11} \rho^2 \left(\frac{1 - R_K}{0.23} \right)^2. \quad (7)$$

asymmetric branching ratios:

$$\frac{\mathcal{B}(B_s \rightarrow \ell^+ \ell'^-)}{\mathcal{B}(B_s \rightarrow \ell^- \ell'^+)} \simeq \frac{m_\ell^2}{m_{\ell'}^2}. \quad \text{Left-handed leptons only} \quad (8)$$

$$\frac{\mathcal{B}(B_s \rightarrow \mu^+ e^-)}{\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}}} \simeq 0.01 \kappa^2 \cdot \left(\frac{1 - R_K}{0.23} \right)^2, \quad (9)$$

$$\frac{\mathcal{B}(B_s \rightarrow \tau^+ e^-)}{\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}}} \simeq 4 \kappa^2 \cdot \left(\frac{1 - R_K}{0.23} \right)^2, \quad (10)$$

$$\frac{\mathcal{B}(B_s \rightarrow \tau^+ \mu^-)}{\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}}} \simeq 4 \cdot \left(\frac{1 - R_K}{0.23} \right)^2, \quad (11)$$

A.Vicente

Great experimental perspectives!

LFV Process	Present Bound	Future Sensitivity
$\mu \rightarrow e\gamma$	5.7×10^{-13}	6×10^{-14} (MEG)
$\tau \rightarrow e\gamma$	3.3×10^{-8}	$\sim 10^{-8} - 10^{-9}$ (B factories)
$\tau \rightarrow \mu\gamma$	4.4×10^{-8}	$\sim 10^{-8} - 10^{-9}$ (B factories)
$\mu \rightarrow 3e$	1.0×10^{-12}	$\sim 10^{-16}$ (Mu3e)
$\tau \rightarrow 3e$	2.7×10^{-8}	$\sim 10^{-9} - 10^{-10}$ (B factories)
$\tau \rightarrow 3\mu$	2.1×10^{-8}	$\sim 10^{-9} - 10^{-10}$ (B factories)
$\mu^-, \text{Au} \rightarrow e^-, \text{Au}$	7.0×10^{-13}	—
$\mu^-, \text{SiC} \rightarrow e^-, \text{SiC}$	—	2×10^{-14} (DeeMe)
$\mu^-, \text{Al} \rightarrow e^-, \text{Al}$	—	$10^{-15} - 10^{-17}$ (COMET)
$\mu^-, \text{Ti} \rightarrow e^-, \text{Ti}$	4.3×10^{-12}	$10^{-17} - 10^{-18}$ (Mu2e)
		$\sim 10^{-18}$ (PRISM/PRIME)

- Anomalies in the flavor sector have inspired new types of bottom-up model-building.
- Leptons and quarks flavor links are becoming important – current $b \rightarrow s, c$ -anomalies hint at non-SM lepton flavor.
- If LHCb's measurement of R_K substantiates it implies that there is more difference between a muon and an electron than their mass. Lepton-universality, a feature of the $SU(3)_C \times SU(2)_L \times U(1)_Y$ SM appears to be violated in $b \rightarrow s$ FCNC transitions.
- Fantastic prospects to progress in understanding of flavor and BSM.

We thank the organizers of WIN'15, all our speakers for great talks and our fantastic session chairs.