

# Fully Covering the MSSM Higgs Sector at the LHC

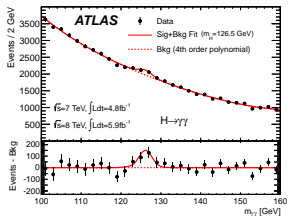
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King's College London

WIN 2015, Heidelberg, 9<sup>th</sup> June 2015



# The 4<sup>th</sup> of July 2012: discovery of a new 125 GeV boson



ATLAS Prelim.

$m_H = 125.5 \text{ GeV}$

$\sigma(\text{stat})$   
 $\sigma(\text{sys inc})$   
 $\sigma(\text{theory})$

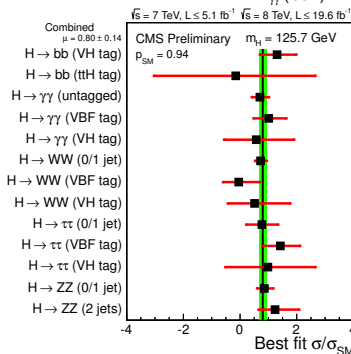
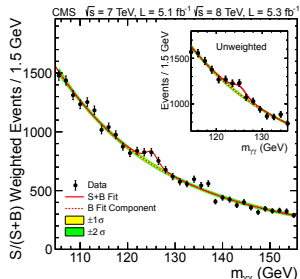
Total uncertainty  $\pm 1\sigma$  on  $\mu$

$H \rightarrow \gamma\gamma$	$\mu = 1.57^{+0.33}_{-0.28}$	$\pm 0.23$ $\pm 0.24$ $\pm 0.18$ $\pm 0.19$	$\pm 1\sigma$ on $\mu$
$H \rightarrow ZZ^* \rightarrow 4l$	$\mu = 1.44^{+0.40}_{-0.35}$	$\pm 0.35$ $\pm 0.30$ $\pm 0.23$ $\pm 0.17$ $\pm 0.20$	$\pm 1\sigma$ on $\mu$
$H \rightarrow WW^* \rightarrow l\nu l\nu$	$\mu = 1.00^{+0.32}_{-0.29}$	$\pm 0.21$ $\pm 0.21$ $\pm 0.24$ $\pm 0.19$ $\pm 0.20$	$\pm 1\sigma$ on $\mu$
Combined $H \rightarrow \gamma\gamma, ZZ^*, WW^*$	$\mu = 1.35^{+0.21}_{-0.20}$	$\pm 0.14$ $\pm 0.14$ $\pm 0.14$ $\pm 0.12$ $\pm 0.11$	$\pm 1\sigma$ on $\mu$
$W, Z H \rightarrow b\bar{b}$	$\mu = 0.2^{+0.7}_{-0.6}$	$\pm 0.5$ $\pm 0.4$ $\pm 0.1$	$\pm 1\sigma$ on $\mu$
$H \rightarrow \tau\tau$ (8 TeV data only)	$\mu = 1.4^{+0.5}_{-0.4}$	$\pm 0.3$ $\pm 0.3$ $\pm 0.2$ $\pm 0.1$	$\pm 1\sigma$ on $\mu$
Combined $H \rightarrow b\bar{b}, \tau\tau$	$\mu = 1.09^{+0.36}_{-0.32}$	$\pm 0.34$ $\pm 0.27$ $\pm 0.21$ $\pm 0.09$ $\pm 0.06$	$\pm 1\sigma$ on $\mu$
Combined	$\mu = 1.30^{+0.18}_{-0.17}$	$\pm 0.12$ $\pm 0.14$ $\pm 0.11$ $\pm 0.10$ $\pm 0.09$	$\pm 1\sigma$ on $\mu$

$\sqrt{s} = 7 \text{ TeV} \int \text{Ldt} = 4.6\text{-}4.8 \text{ fb}^{-1}$      $-0.5$      $0$      $0.5$      $1$      $1.5$      $2$

$\sqrt{s} = 8 \text{ TeV} \int \text{Ldt} = 20.3 \text{ fb}^{-1}$

Signal strength ( $\mu$ )

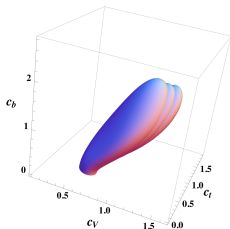


# Is it a Higgs?

with Djouadi et al. (2013)

## Higgs couplings as predicted by Higgs mechanism

- couplings proportional to masses as expected
- couplings to  $WW$ ,  $ZZ$ ,  $\gamma\gamma$  roughly as expected



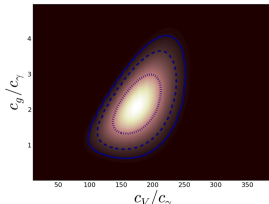
## Is it a spin 0?

- state decays into  $\gamma\gamma \Rightarrow$  not spin-1 (Landau–Yang th.)

- is it a spin-2 like graviton?

A priori no:  $c_g \neq c_\gamma$ ,  $c_V \gg 35c_\gamma$

Ellis and You. (2012)



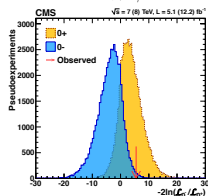
## Is it CP-even?

$$HV_\mu V_\mu \text{ vs } H\epsilon^{\mu\nu\rho\sigma} Z_{\mu\nu} Z_{\rho\sigma}$$

$$\Rightarrow \frac{d\Gamma(H \rightarrow ZZ^*)}{dM^*} \text{ and } \frac{d\Gamma(H \rightarrow ZZ)}{d\Phi}$$

ATLAS/CMS:  $\sim 3\sigma$  for CP-even

$\Rightarrow$  It is THE-A Higgs boson!



# Motivations for SUSY

- The hierarchy problem: why  $M_H \ll M_{Pl}$ ?
  - ▶ The fermion 1-loop correction to the Higgs mass:

$$\delta^{(f)} m_H^2 \supset \frac{\lambda_F^2}{8\pi^2} \left[ -\Lambda^2 + 6m_F^2 \ln \frac{\Lambda}{m_F} \right]$$

- ▶ The scalar 1-loop correction to the Higgs mass:

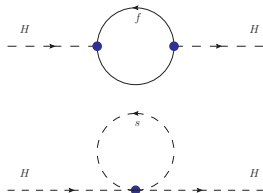
$$\delta^{(s)} m_H^2 \supset \frac{\lambda_S}{16\pi^2} \left[ -\Lambda^2 + (2m_S^2 - 2\lambda_S v^2) \ln \left( \frac{\Lambda}{m_S} \right) \right]$$

- ▶ SUSY theory with  $2N_F = N_S$  and with  $\lambda_S = -\lambda_F^2 \Rightarrow$  the quadratic divergences vanish (remain the logarithmic ones):

$$\delta^{(f+s)} m_H^2 = \frac{\lambda_S^2}{4\pi^2} \left[ (m_F^2 - m_S^2) \ln \left( \frac{\Lambda}{m_S} \right) + 3m_F^2 \ln \left( \frac{m_S}{m_F} \right) \right]$$

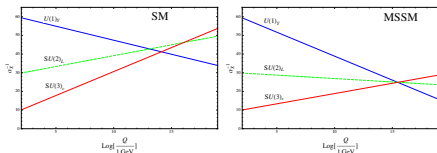
- The gauge coupling unification
- A dark matter candidate (relies on R-parity)

$$\delta m_H^2 \sim \int^\Lambda d^4 k \frac{1}{k^2} \sim \Lambda^2 + m_{loop}^2 \ln \frac{\Lambda}{m_{loop}}$$



$\Rightarrow$  the hierarchy and naturalness problems solved

if  $m_F = \bar{m}_S \Rightarrow M_H$  is protected by SUSY  
 $\Rightarrow$  SUSY must be broken,  $m_S \gg m_F$



- 1 Fully Covering the MSSM Higgs Sector at the LHC
  - The Higgs sector of the MSSM
  - Implications from the Higgs mass
  - Implications from the Higgs couplings
  - Implications from direct Higgs searches
- 2 Covering the MSSM stop sector

# The Higgs sector of the MSSM

One needs 2 complex scalar doublets:  $H_1 = \begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix}$  and  $H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix}$

- give masses to respectively d and u fermions in SUSY invariant way
- cancel the chiral anomalies

After EWSB: 3 d.o.f. to make  $W_L^\pm, Z_L \Rightarrow$  5 physical states left out:  $h, H, A, H^\pm$

At tree-level only 2 free parameters  $\tan \beta, M_A$  :

$$M_{h,H}^2 = \frac{1}{2} \left[ M_A^2 + M_Z^2 \mp \sqrt{(M_A^2 + M_Z^2)^2 - 4M_A^2 M_Z^2 \cos^2 2\beta} \right], \quad \tan 2\alpha = \tan 2\beta \frac{M_A^2 + M_Z^2}{M_A^2 - M_Z^2}$$

$$M_{H^\pm}^2 = M_A^2 + M_W^2$$

Important constraint on the MSSM Higgs boson masses:

$$M_h \leq \min(M_A, M_Z) \cdot |\cos 2\beta| \leq M_Z, \quad M_H > \max(M_A, M_Z), \quad M_{H^\pm} > M_W$$

$M_A \gg M_Z$ : decoupling regime, all Higgses heavy except h:

$$M_h \sim M_Z |\cos 2\beta| \leq M_Z, \quad M_H \sim M_{H^\pm} \sim M_A, \quad \alpha \sim \pi - \beta$$

$\Rightarrow$  Inclusion of radiative corrections to  $M_h$  are essential to explain  $M_h \approx 125 \text{ GeV} > M_Z$

# The radiative corrections to the Higgs mass

Dominant corrections are due to top (s)quark, at the one-loop level:

$$M_h \xrightarrow{M_A \gg M_Z} M_Z |\cos 2\beta| + \frac{3\bar{m}_t^4}{2\pi^2 v^2 \sin^2 \beta} \left[ \ln \frac{M_S^2}{\bar{m}_t^2} + \frac{X_t^2}{2M_S^2} \left( 1 - \frac{X_t^2}{6M_S^2} \right) \right]$$

[Okada+Yamaguchi+Yanagida, Ellis+Ridolfi+Zwirner, Haber+Hempfling (1991)]

depending on  $\tan \beta$ ,  $M_S = \sqrt{\tilde{m}_{t_1} \tilde{m}_{t_2}}$ ,  $X_t = A_t - \frac{\mu}{\tan \beta}$ :  $M_h^{max} \rightarrow M_Z + 30 - 50$  GeV

The mass value 125 GeV is near the upper limit for the MSSM h boson

Increase  $M_h \Rightarrow$  increase R.C. :

- decoupling regime with  $M_A \sim \mathcal{O}$  (TeV)
- large values of  $\tan \beta \gtrsim 10$  to maximize tree-level value
- maximal mixing scenario:  $X_t = \sqrt{6}M_S$
- heavy stops, i.e. large  $M_S = \sqrt{\tilde{m}_{t_1} \tilde{m}_{t_2}}$

Perform a full scan of the pMSSM with 22+19 free parameters

- calculate the Higgs and SUSY spectrum in the MSSM with the full one-loop + dominant two-loop corrections.
- determine the regions of parameter space where  $123 \leq M_h \leq 129$  GeV (3 GeV uncertainty includes both “experimental” and “theoretical” error)

# Implication of a 125 GeV Higgs for the pMSSM

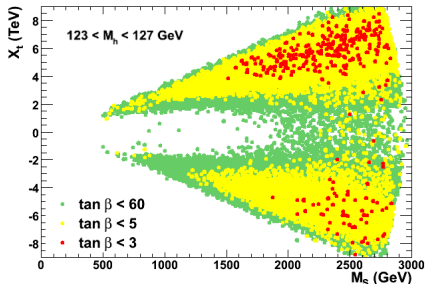
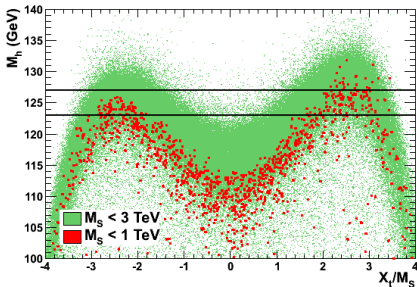
[A. Arbey, M. Battaglia, A. Djouadi, F. Mahmoudi, J. Q., Phys.Lett. B708 (2012) 162]

- Large  $M_S$  values required:
  - ▶  $M_S \sim 1$  TeV: only for maximal mixing
  - ▶  $M_S \sim 3$  TeV: only for typical mixing

⇒ no-mixing scenario excluded  
(unless  $M_S \gg 1$  TeV)

- Large  $\tan \beta$  values favored but  $\tan \beta \sim 3$  allowed if  $M_S \sim 3$  TeV
- Constraints on sparticles:  $m_{\tilde{t}_1} \sim 500$  GeV still possible!

⇒ maximal mixing disfavored for large  $M_S$  and  $\tan \beta$





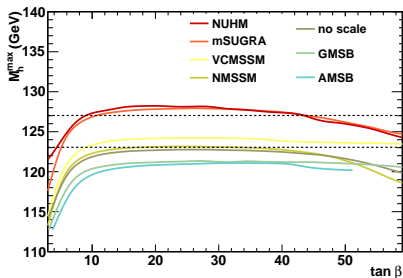
# Implication of a 125 GeV Higgs for the cMSSM

Concrete schemes: SSB occurs in hidden sector

Parameters obey boundary conditions

⇒ small number of inputs:

- **mSUGRA**:  $\tan \beta$ ,  $m_{1/2}$ ,  $m_0$ ,  $A_0$ ,  $\text{sign}(\mu)$
- **GMSB**:  $\tan \beta$ ,  $\text{sign}(\mu)$ ,  $M_{\text{mess}}$ ,  $\Lambda_{\text{SSB}}$ ,  $N_{\text{mess}}$
- **AMSB**:  $m_0$ ,  $m_{3/2}$ ,  $\tan \beta$ ,  $\text{sign}(\mu)$



Full scans of the model parameters with  $123 \text{ GeV} \leq M_h \leq 129 \text{ GeV}$

[ A. Arbey, M. Battaglia, A. Djouadi, F. Mahmoudi, J. Q., Phys.Lett. B708 (2012) 162]

model	AMSB	GMSB	mSUGRA	no-scale	cNMSSM	VCMSSM	NUHM
$M_h^{\text{max}}$	121.0	121.5	128.0	123.0	123.5	124.5	128.5

End of AMSB and GMSB in their minimal versions!

# Implication of a 125 GeV Higgs for high scale SUSY

[A. Arbey, M. Battaglia, A. Djouadi, F. Mahmoudi, J. Q., Phys.Lett. B708 (2012) 162]

As the scale  $M_S$  seems to be large, we can consider 2 extreme possibilities:

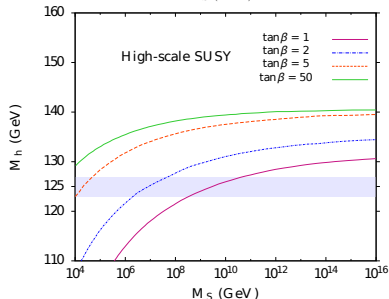
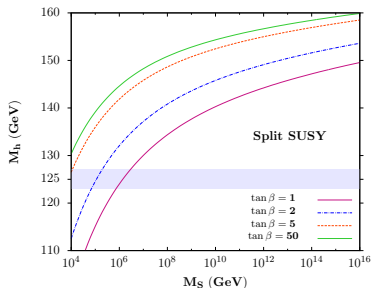
- **Split SUSY**: allow fine-tuning

- ▶ The SSB scalar mass terms at high scale (except 1 Higgs doublet)
- ▶ Gauginos and higgsinos, are left at the EWSB scale (unification+DM still OK)
- ▶ The parameters :  $M_S$ , 1 Higgs mass,  $M_1, M_2, M_3, \mu$  and  $\tan \beta$
- ▶ Boundary condition on the quartic Higgs coupling :  
$$\lambda(M_S) = \frac{1}{4} [g^2(M_S) + g'^2(M_S)] \cos^2 2\beta$$
- ▶ Heavy scalars  $\Rightarrow$  R.C. in the Higgs sector enhanced by  $\ln(M_{EWSB}/M_S)$

- **SUSY broken at the GUT scale**:

- ▶ Abandon fine-tuning, DM, unification
- ▶ SUSY/EWSB matching encoded in the Higgs quartic coupling  $\lambda \propto M_h^2$  related to gauge couplings

**In both cases small  $\tan \beta$  needed!**



## Determination of the h boson couplings in a generic MSSM

- Knowing  $[\tan \beta, M_A]$  and fixing  $M_h = 125$  GeV, the couplings of the Higgs bosons can be derived, including the dominant **radiative corrections that enter in the MSSM Higgs masses** :

$$c_V^0 = \sin(\beta - \alpha) , \quad c_t^0 = \frac{\cos \alpha}{\sin \beta} , \quad c_b^0 = -\frac{\sin \alpha}{\cos \beta}$$

However, there are also **direct/vertex radiative corrections to the Higgs couplings** not contained in the mass matrix. These can alter this simple picture!

- The two important SUSY (QCD) corrections affect the t,b couplings:

$$c_b \approx c_b^0 \times [1 - \Delta_b / (1 + \Delta_b) \times (1 + \cot \alpha \cot \beta)]$$
$$c_t \approx c_t^0 \times \left[ 1 + \frac{m_t^2}{4m_{\tilde{t}_1}^2 m_{\tilde{t}_2}^2} (m_{\tilde{t}_1}^2 + m_{\tilde{t}_2}^2 - (A_t - \mu \cot \alpha)(A_t + \mu \tan \alpha)) \right]$$

- $c_\tau$  ,  $c_c$  and  $c_t$  (from  $pp \rightarrow Ht\bar{t}$ ) do not involve same vertex corrections
- $gg \rightarrow h$  process has  $\tilde{t}$ ,  $\tilde{b}$  loops and  $h \rightarrow \gamma\gamma$  has also  $\tilde{\tau}$  and  $\chi_j^\pm$  loops  
 $\Rightarrow$  **in general, we need (at least) 7 couplings  $c_t, c_b, c_c, c_\tau, c_V, c_g, c_\gamma$**   
**+ invisible decays?** [Djouadi,Falkowski,Mambrini,JQ, arXiv:1205.3169]

8 parameters fit difficult! Simpler to make reasonable approximations:

- low sensitivity on  $h \rightarrow c\bar{c}$ ,  $h \rightarrow \tau\tau$  and  $pp \rightarrow t\bar{t}H$  at the LHC
- in  $h \rightarrow \gamma\gamma$  additional contributions ( $\tilde{b}, \tilde{\tau}, \chi_j^\pm$ ) smaller than those of  $\tilde{t}$   
 $\Rightarrow$  assume  $c_c = c_t, c_\tau = c_b$  and  $c_t(ttH) = c_t(ggF), c_\gamma \simeq c_g \simeq c_t$

**reduce the problem to a fit of three couplings:  $c_t, c_b, c_V$**

## 3D-Fit in the $[c_t, c_b, c_V]$ parameter space

- If large **direct corrections**  $\Rightarrow$  3 independent  $h$  couplings :  
 $c_c = c_t$ ,  $c_\tau = c_b$  and  $c_V = c_V^0$

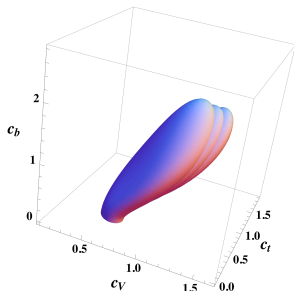
- To study the  $h$  state at the LHC, we define the effective Lagrangian :

$$\begin{aligned} \mathcal{L}_h = & c_V g_{hWW} h W_\mu^+ W^{-\mu} + c_V g_{hZZ} h Z_\mu^0 Z^{0\mu} \\ & - c_t y_t h \bar{t}_L t_R - c_t y_c h \bar{c}_L c_R \\ & - c_b y_b h \bar{b}_L b_R - c_b y_\tau h \bar{\tau}_L \tau_R + \text{h.c.} \end{aligned}$$

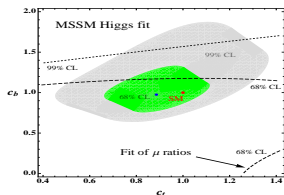
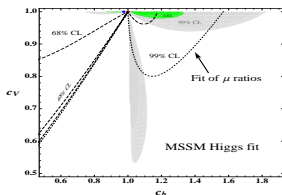
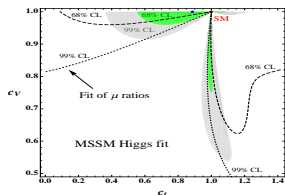
- We fit the Higgs signal strengths :

$$\mu_X \simeq \frac{\sigma(pp \rightarrow h) \times \text{BR}(h \rightarrow XX)}{\sigma(pp \rightarrow h)_{\text{SM}} \times \text{BR}(h \rightarrow XX)_{\text{SM}}}$$

Best-fit value :  $c_t = 0.89$ ,  $c_b = 1.01$  and  $c_V = 1.02$  (ATLAS & CMS data)



If we neglect **direct corrections**  $\rightarrow$  2 parameter fits :



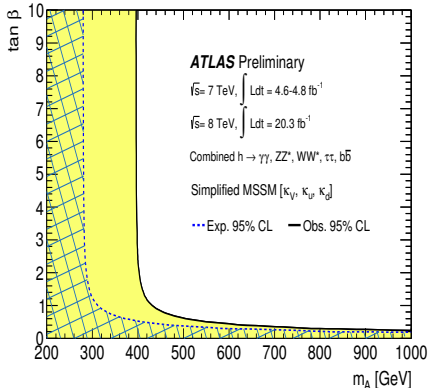
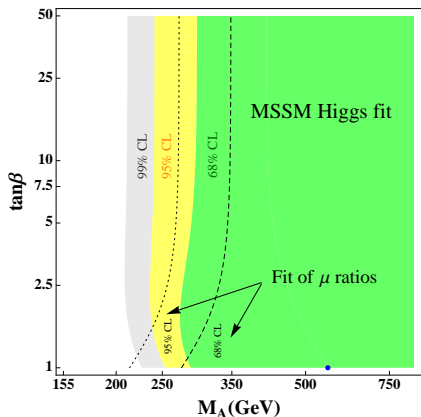
best-fit points :  $(c_t = 0.88, c_V = 1.0)$ ,  $(c_b = 0.97, c_V = 1.0)$  and  $(c_t = 0.88, c_b = 0.97)$

Djouadi, Maiani, Moreau, Polosa, JQ, Riquer, arXiv:1307.5205

# The 2D-fit in the hMSSM

Using the expressions defining the hMSSM one can perform a fit in the plane  $[\tan \beta, M_A]$ :

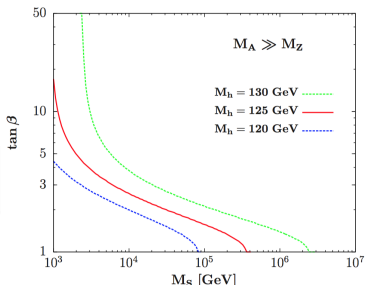
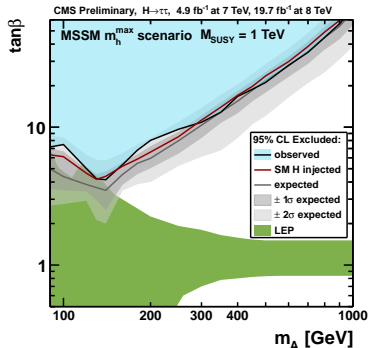
The best-fit point :  $(\tan \beta = 1 \text{ and } M_A = 557 \text{ GeV})$  or  
 $(M_H = 580 \text{ GeV}, M_{H^\pm} = 563 \text{ GeV}, \alpha = -0.837 \text{ rad})$ .



# Direct heavy Higgs searches

- $\tan \beta \lesssim 3$  usually thought to be “excluded” by LEP2 ( $M_h \gtrsim 114$  GeV) but it assumes  $M_S \sim 1\text{TeV}$ !
- Caveat : ATLAS & CMS constraint apply for a specific benchmark :  $X_t/M_S = \sqrt{6}$  and  $M_S = 1$  TeV (the  $m_h^{\text{max}}$  scenario).
- But we can be more relaxed:  
with  $M_S \gg M_Z$ ,  $\tan \beta \approx 1$  could be allowed!

⇒ Let's reopen the low  $\tan \beta$  regime and heavy Higgs searches,  
but in a benchmark independent approach (hMSSM)



# The Higgs couplings and the approach to the decoupling limit

$\Phi$	$g_{\Phi\bar{u}u}$	$g_{\Phi\bar{d}d}$	$g_{\Phi VV}$	$g_{\Phi AZ}/g_{\Phi H^+W^-}$
$h$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$	$\sin(\beta - \alpha)$	$\propto \cos(\beta - \alpha)$
$H$	$\sin \alpha / \sin \beta$	$\cos \alpha / \cos \beta$	$\cos(\beta - \alpha)$	$\propto \sin(\beta - \alpha)$
$A$	$\cot \beta$	$\tan \beta$	0	$\propto 0/1$

The decoupling limit is controlled by  $g_{HVV} = \cos(\beta - \alpha)$  :

$$g_{HVV} \xrightarrow{M_A \gg M_Z} \chi \equiv \frac{1}{2} \frac{M_Z^2}{M_A^2} \sin 4\beta - \frac{1}{2} \frac{M_{22}^2}{M_A^2} \sin 2\beta \rightarrow 0$$

**Tree-level part:** doubly suppressed in both the  $\tan \beta \gg 1$  and  $\tan \beta \sim 1$  cases.

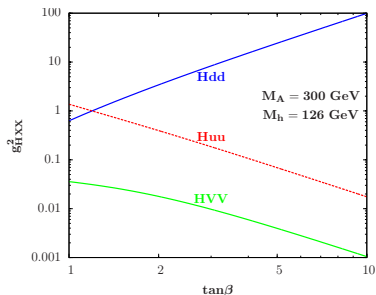
$$\sin 4\beta = \frac{4 \tan \beta (1 - \tan^2 \beta)}{(1 + \tan^2 \beta)^2} \rightarrow \begin{cases} -4/\tan \beta & \text{for } \tan \beta \gg 1 \\ 1 - \tan^2 \beta & \text{for } \tan \beta \sim 1 \end{cases} \rightarrow 0$$

**The radiative part :** behave as  $-\mathcal{M}_{22}^2/M_A^2 \times \cot \beta$ , also vanishes at high  $\tan \beta$  values  $\Rightarrow$  the decoupling limit  $g_{HVV} \rightarrow 0$  is reached very quickly at high  $\tan \beta$ , as soon as  $M_A \gtrsim M_h^{\max}$ . Instead, for  $\tan \beta \approx 1$ , this radiatively generated component is maximal. **Departure from the decoupling limit!**

$$\begin{aligned} g_{huu} &\xrightarrow{M_A \gg M_Z} 1 + \chi \cot \beta \rightarrow 1 \\ g_{hdd} &\xrightarrow{M_A \gg M_Z} 1 - \chi \tan \beta \rightarrow 1 \\ g_{Huu} &\xrightarrow{M_A \gg M_Z} -\cot \beta + \chi \rightarrow -\cot \beta \\ g_{Hdd} &\xrightarrow{M_A \gg M_Z} +\tan \beta + \chi \rightarrow +\tan \beta \end{aligned}$$

At low  $\tan \beta$  :  $g_{HVV}$  is non-zero,  $g_{Htt}$  and  $g_{Att}$  are significant.

$\Rightarrow H/A/H^\pm$  bosons can have sizable couplings to top quarks and massive gauge bosons if  $\tan \beta \sim 3$ .



## The hMSSM

In the basis  $(H_d, H_u)$ , the CP-even Higgs mass matrix can be written as:

$$M_S^2 = M_Z^2 \begin{pmatrix} c_\beta^2 & -s_\beta c_\beta \\ -s_\beta c_\beta & s_\beta^2 \end{pmatrix} + M_A^2 \begin{pmatrix} s_\beta^2 & -s_\beta c_\beta \\ -s_\beta c_\beta & c_\beta^2 \end{pmatrix} + \begin{pmatrix} \Delta M_{11}^2 & \Delta M_{12}^2 \\ \Delta M_{12}^2 & \Delta M_{22}^2 \end{pmatrix}$$

$\Delta M_{ij}^2$ : radiative corrections

One derives the neutral CP-even Higgs boson masses and the mixing angle  $\alpha$ :

$$M_{h/H}^2 = f_{h/H}(M_A, \tan \beta, \Delta M_{11}, \Delta M_{12}, \Delta M_{22})$$

$$\tan \alpha = f_\alpha(M_A, \tan \beta, \Delta M_{11}, \Delta M_{12}, \Delta M_{22})$$

$M_h$  should be an input now...

The post-Higgs MSSM scenario:

- observation of the lighter  $h$  boson at a mass of  $\approx 125$  GeV
- non-observation of superparticles at the LHC

MSSM  $\Rightarrow$  SUSY-breaking scale rather high,  $M_S \gtrsim 1$  TeV.

$\Delta M_{22}^2$  involves the by far dominant stop-top sector correction:  $\Delta M_{22}^2 \gg \Delta M_{11}^2, \Delta M_{12}^2$

$\rightarrow$  One can trade  $\Delta M_{22}^2$  ( $M_S$ ) for the by now known  $M_h$

In this case, one can simply describe the Higgs sector in terms of  $M_A, \tan \beta$  and  $M_h$ :

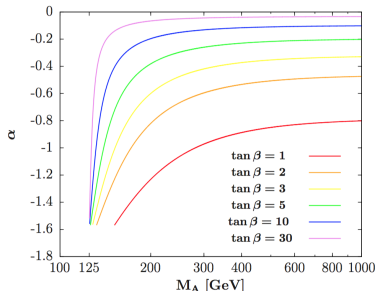
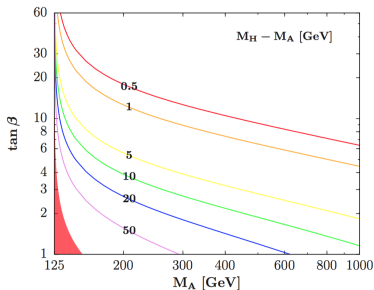
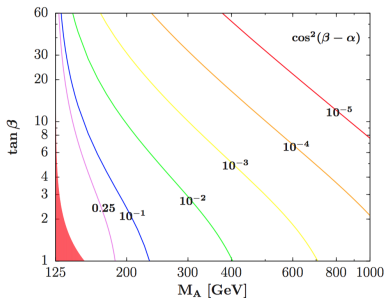
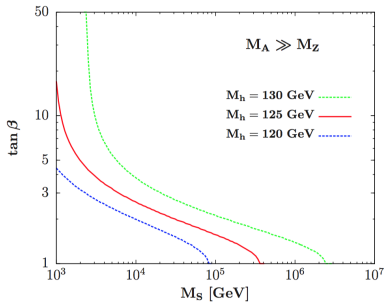
$$\text{hMSSM : } M_H^2 = \frac{(M_A^2 + M_Z^2 - M_h^2)(M_Z^2 c_\beta^2 + M_A^2 s_\beta^2) - M_A^2 M_Z^2 c_\beta^2 s_\beta^2}{M_Z^2 c_\beta^2 + M_A^2 s_\beta^2 - M_h^2}$$

$$\alpha = -\arctan \left( \frac{(M_Z^2 + M_A^2) c_\beta s_\beta}{M_Z^2 c_\beta^2 + M_A^2 s_\beta^2 - M_h^2} \right)$$



# The definition of the hMSSM

Djouadi, Maiani, Polosa, JQ, Riquer, arXiv:1502.05653



## 2. Assumptions: standard mass matrix

The CP-even Higgs sector is usually described by the  $2 \times 2$  mass matrix :

$$\mathbf{M}_{\Phi}^2 = \mathbf{M}_{\mathbf{Z}}^2 \begin{pmatrix} c_{\beta}^2 & -s_{\beta}c_{\beta} \\ -s_{\beta}c_{\beta} & s_{\beta}^2 \end{pmatrix} + \mathbf{M}_{\mathbf{A}}^2 \begin{pmatrix} s_{\beta}^2 & -s_{\beta}c_{\beta} \\ -s_{\beta}c_{\beta} & c_{\beta}^2 \end{pmatrix} + \begin{pmatrix} \Delta\mathcal{M}_{11}^2 & \Delta\mathcal{M}_{12}^2 \\ \Delta\mathcal{M}_{12}^2 & \Delta\mathcal{M}_{22}^2 \end{pmatrix}$$

It is by diagonalizing this matrix that one obtains  $\mathbf{M}_{\mathbf{H}}$ ,  $\mathbf{M}_{\mathbf{h}}$  and  $\alpha$ :

- tree-level masses are given in terms of  $\mathbf{M}_{\mathbf{A}}$  and  $\mathbf{M}_{\mathbf{Z}}$  plus the angle  $\beta$ ;
- **radiative corrections** (with the SUSY parameters) appear only in  $\Delta\mathbf{M}_{ij}^2$ .

**Assumption clearly valid at scales  $\mathbf{M}_{\mathbf{S}}$  not far for 1 TeV (common wisdom...)**

In the hMSSM, we assume that this picture is valid at much higher scales.

This is the main ‘problem’ and subject of discussion:

Question 1): how far can we go in  $\mathbf{M}_{\mathbf{S}}$  while retaining this simple form?

Question 2): when RGE improving, the matrix has still a convenient form?

# The complete approach: effective THDM with heavy SUSY

$$\begin{aligned}
 V = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - m_{12}^2 (\Phi_1^\dagger \Phi_2 + \text{h.c.}) + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 \\
 & + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) \quad \text{Carena et al., (1410.4969)} \\
 & + \left\{ \frac{1}{2} \lambda_5 (\Phi_1^\dagger \Phi_2)^2 + [\lambda_6 (\Phi_1^\dagger \Phi_1) + \lambda_7 (\Phi_2^\dagger \Phi_2)] \Phi_1^\dagger \Phi_2 + \text{h.c.} \right\},
 \end{aligned}$$

**i) Match the THDM quartic couplings to their MSSM values.**

$$\lambda_1 = \lambda_2 = -(\lambda_3 + \lambda_4) = \frac{1}{4}(g^2 + g'^2) = m_Z^2/v^2,$$

$$\lambda_4 = -\frac{1}{2}g^2 = -2m_W^2/v^2,$$

$$\lambda_5 = \lambda_6 = \lambda_7 = 0.$$

**ii) Evolve (RGEs) all seven lambdas from  $M_S$  to the weak scale.**

**iii) CP-even Higgs mass matrix in terms of lambdas at the weak-scale:**

$$m_A^2 \begin{pmatrix} s_\beta^2 & -s_\beta c_\beta \\ -s_\beta c_\beta & c_\beta^2 \end{pmatrix} + v^2 \begin{pmatrix} L_{11} & L_{12} \\ L_{12} & L_{22} \end{pmatrix}$$

$$L_{11} = \lambda_1 c_\beta^2 + 2\lambda_6 s_\beta c_\beta + \lambda_5 s_\beta^2,$$

$$L_{12} = (\lambda_3 + \lambda_4) s_\beta c_\beta + \lambda_6 c_\beta^2 + \lambda_7 s_\beta^2,$$

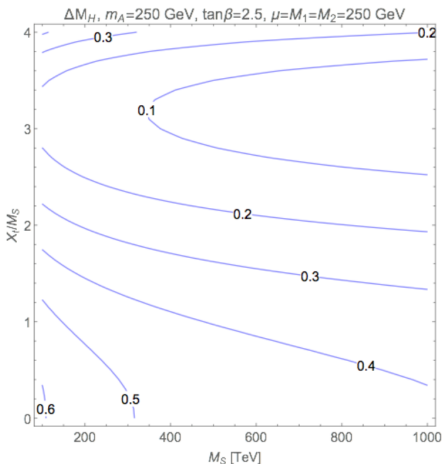
$$L_{22} = \lambda_2 s_\beta^2 + 2\lambda_7 s_\beta c_\beta + \lambda_5 c_\beta^2.$$

_____	$M_S$
THDM(+EWkino)	
_____	$m_A$
SM(+EWkino)	
_____	$\mu$
SM	
_____	$M_t$

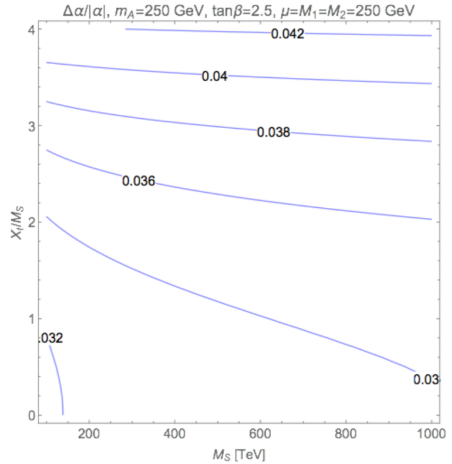
## 2. Assumptions: standard mass matrix

### Comparison: hMSSM vs effective THDM with heavy SUSY at low $\tan\beta$

Gabriel Lee and Carlos Wager (work in progress)  
for the HXSWG



$\Delta M_H < 1\%$

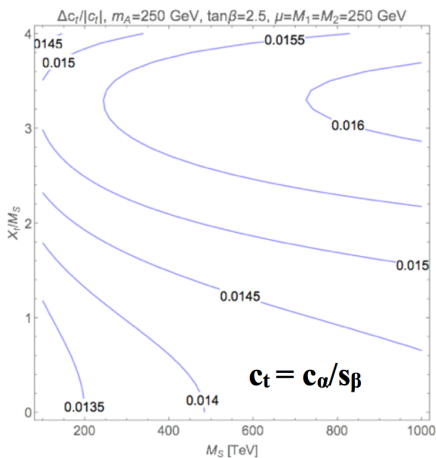


$\Delta\alpha/|\alpha| < 4\%$

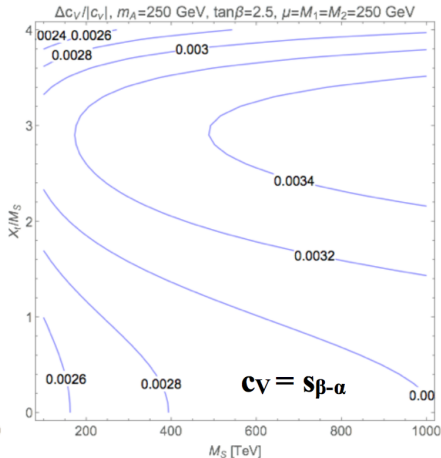
## 2. Assumptions: standard mass matrix

### Comparison: hMSSM vs effective THDM with heavy SUSY at low $\tan\beta$

Gabriel Lee and Carlos Wager (work in progress)  
for the HXSWG



$\Delta c_t/|c_t| < 2\%$



$\Delta c_V/|c_V| < 1\%$

## 2. Assumptions: dominance of main correction

Dominant correction to  $\Delta M^2$  due to top/stop sector and approximately:

$$\Delta \mathcal{M}_{22}^2 \propto \frac{3\bar{m}_t^4}{2\pi^2 v^2 \sin^2 \beta} \left[ \log \frac{M_S^2}{\bar{m}_t^2} + \frac{\tilde{X}_t^2}{M_S^2} \right] + \dots \gg \Delta \mathcal{M}_{11}^2, \Delta \mathcal{M}_{12}^2$$

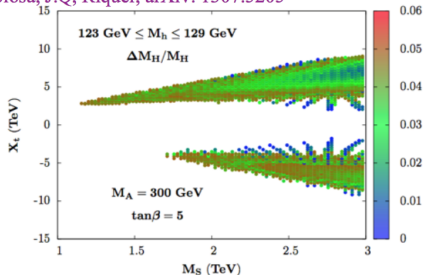
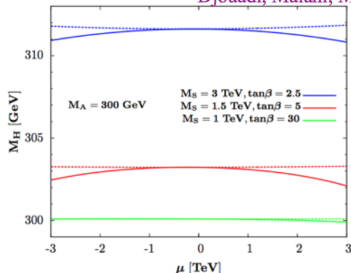
We have checked the approximation in two different configurations:

Include subleading terms in  $\Delta M^2$   
(Carena, Wagner, Haber, Hempfling...)

$\lambda_t, \lambda_b, X_t = X_b$  and varying  $\mu$   
with some choice of  $M_S, \tan\beta$ .

Scan of the MSSM parameters  
with all Higgs rad. corrections  
(we use Suspect with BDSZ RC)  
and impact of  $M_S, A_t, \mu, A_b$

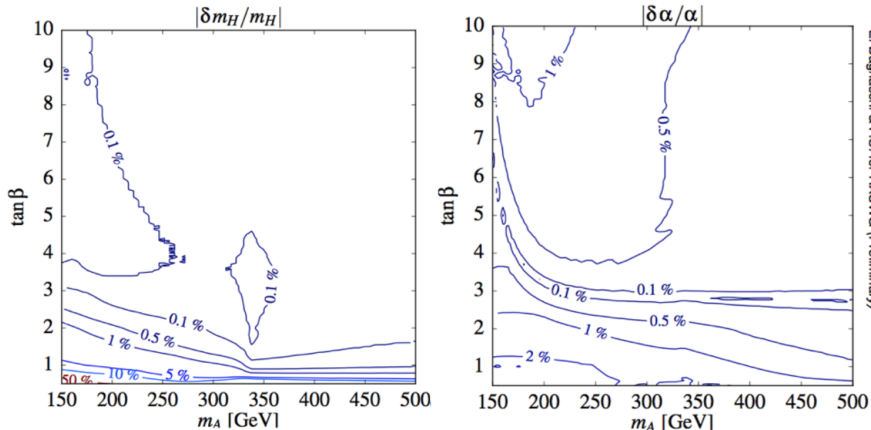
Djouadi, Maiani, Moreau, Polosa, J.Q, Riquer, arXiv: 1307.5205



Very good approximation ( $\leq$  few percent) for  $M_H, \alpha$  for not too large  $\mu$ .

## 2. Assumptions: dominance of main correction

### Comparing hMSSM and FeynHiggs

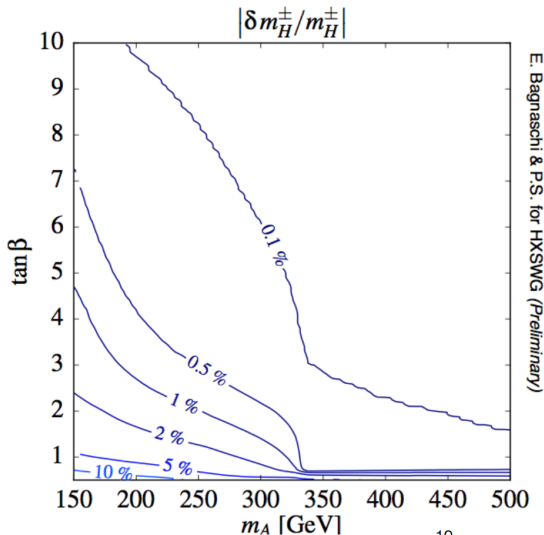


E. Bagnaschi & P.S. for HXSWG (Preliminary)

**Agreement at the level of 0.1% – 1% except for very low  $\tan \beta$**

## 2. Assumptions: dominance of main correction

### hMSSM vs FeynHiggs : charged Higgs mass



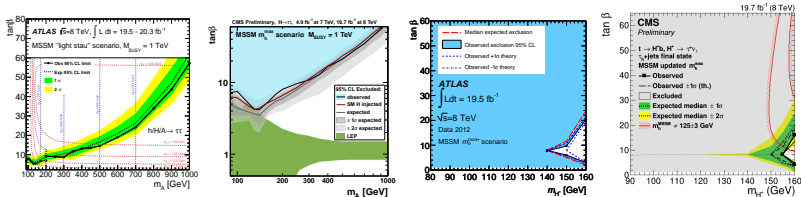
**In the hMSSM approximation the charged Higgs mass sticks to its tree-level value:**

$$m_{H^\pm}^2 = m_A^2 + m_W^2$$



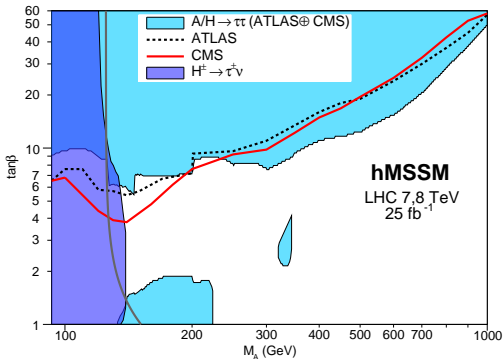
# Implications from heavy Higgs searches

Combine ATLAS+CMS  $pp \rightarrow H^\pm \rightarrow \tau\nu$  and  $pp \rightarrow A/H \rightarrow \tau^+\tau^-$



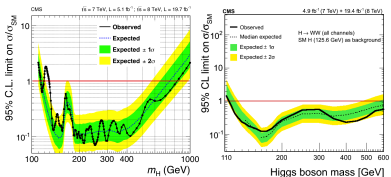
- From  $t \rightarrow bH^+ \rightarrow b\tau\nu$  search:  
 $M_A \lesssim 140$  GeV is now excluded
- $pp \rightarrow \tau\tau$  sensitive at high  $\tan\beta$ :
  - ▶ weaker at low  $M_A$  (no h events)
  - ▶ stronger at high  $M_A$  (no SUSY)
- low  $\tan\beta$  can now be considered  
 A excludes small part of low  $\tan\beta$   
 ⇒ forbidden area excluded!

Djouadi, Maiani, Polosa, JQ, Riquer,  
 arXiv:1502.05653

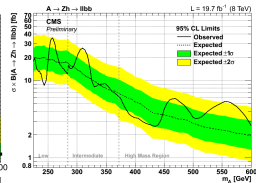
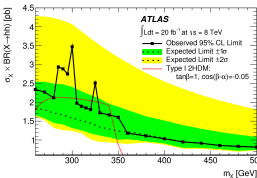


# Implications from heavy Higgs searches

Extend search for heavy SM Higgs for MSSM and consider new channels:  
 $pp \rightarrow H \rightarrow ZZ$  ;  $pp \rightarrow H \rightarrow WW$  ;  $pp \rightarrow H \rightarrow hh$  ;  $pp \rightarrow A \rightarrow hZ$

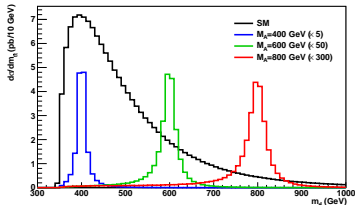
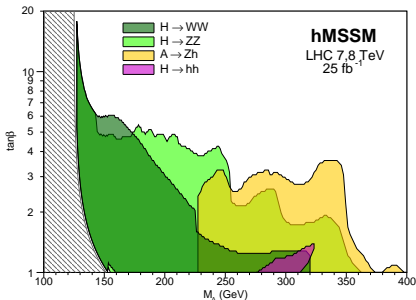


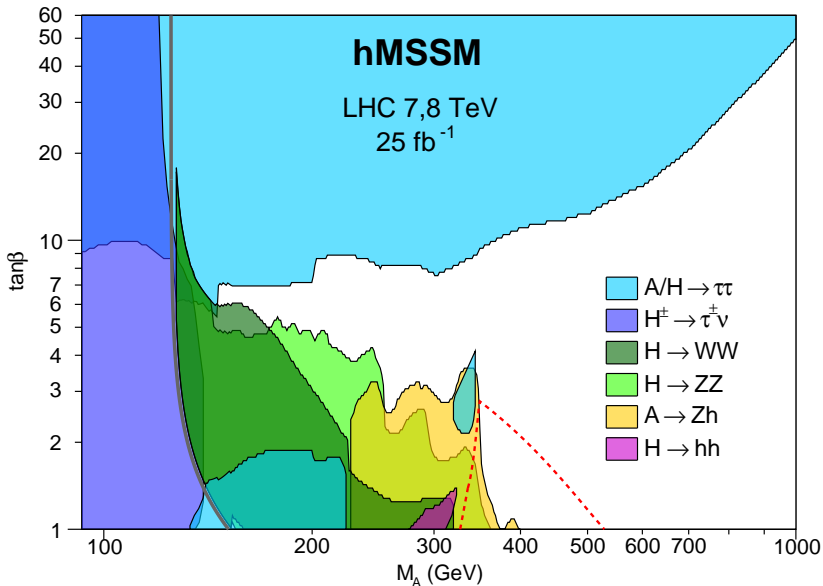
Djouadi, Maiani, Polosa, JQ, Riquer,  
 arXiv:1502.05653

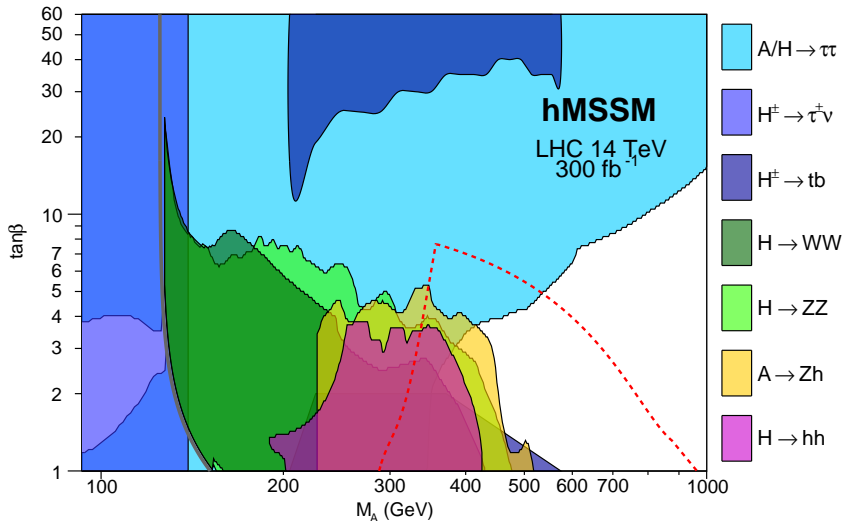


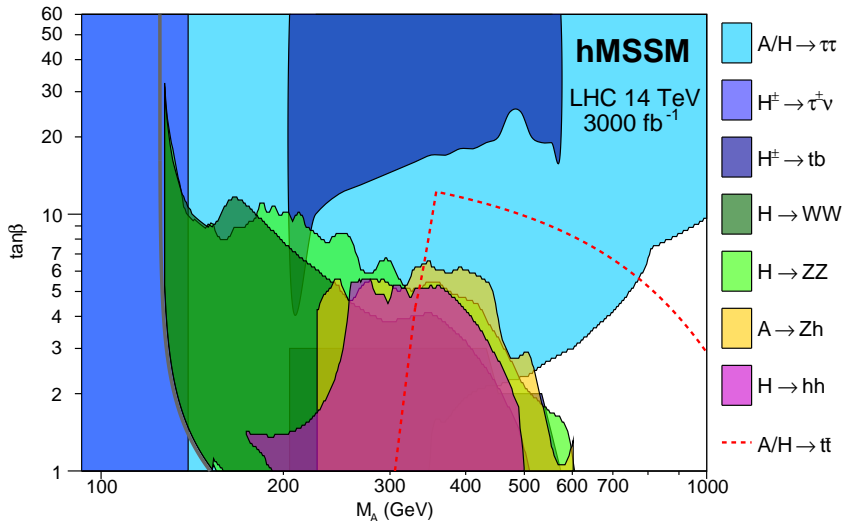
Also consider  $pp \rightarrow \Phi \rightarrow tt$

- crucial at low  $\tan \beta$ , high  $M_A$
- very interesting features...









- 1 Fully Covering the MSSM Higgs Sector at the LHC
- 2 Covering the MSSM stop sector

# Covering the MSSM stop sector at the LHC

## Matching between the MSSM and the dim6-EFT

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i c_i \frac{\mathcal{O}_i}{\Lambda^2}$$

$\uparrow$   
**m<sub>stop</sub>**

$\mathcal{O}_{GG} = g_s^2  H ^2 G_{\mu\nu}^a G^{a,\mu\nu}$	$\mathcal{O}_H = \frac{1}{2} (\partial_\mu  H ^2)^2$
$\mathcal{O}_{WW} = g^2  H ^2 W_{\mu\nu}^a W^{a,\mu\nu}$	$\mathcal{O}_T = \frac{1}{2} (H^\dagger \overleftrightarrow{D}_\mu H)^2$
$\mathcal{O}_{BB} = g'^2  H ^2 B_{\mu\nu} B^{\mu\nu}$	$\mathcal{O}_R =  H ^2  D_\mu H ^2$
$\mathcal{O}_{WB} = 2gg' H^\dagger t^a H W_{\mu\nu}^a B^{\mu\nu}$	$\mathcal{O}_D =  D^2 H ^2$
$\mathcal{O}_W = ig (H^\dagger t^a \overleftrightarrow{D}^\mu H) D^\nu W_{\mu\nu}^a$	$\mathcal{O}_6 =  H ^6$
$\mathcal{O}_B = ig' Y_H (H^\dagger \overleftrightarrow{D}^\mu H) \partial^\nu B_{\mu\nu}$	$\mathcal{O}_{2G} = -\frac{1}{2} (D^\mu G_{\mu\nu}^a)^2$
$\mathcal{O}_{3G} = \frac{1}{3!} g_s^3 f^{abc} G_{\rho\mu}^a G_{\mu\nu}^b G_{\nu\rho}^c$	$\mathcal{O}_{2W} = -\frac{1}{2} (D^\mu W_{\mu\nu}^a)^2$
$\mathcal{O}_{3W} = \frac{1}{3!} g^3 \epsilon^{abc} W_{\rho\mu}^a W_{\mu\nu}^b W_{\nu\rho}^c$	$\mathcal{O}_{2B} = -\frac{1}{2} (\partial^\mu B_{\mu\nu})^2$

$c_{GG} = \frac{h_t^2}{(4\pi)^2} \frac{1}{12} \left[ \left( 1 + \frac{g'^2 c_{2\beta}}{h_t^2} \right) - \frac{1}{2} \frac{X_t^2}{m_t^2} \right]$	$c_{WB} = -\frac{h_t^2}{(4\pi)^2} \frac{1}{24} \left[ \left( 1 + \frac{g'^2 c_{2\beta}}{h_t^2} \right) - \frac{4}{5} \frac{X_t^2}{m_t^2} \right]$
$c_{WW} = \frac{h_t^2}{(4\pi)^2} \frac{1}{16} \left[ \left( 1 - \frac{g'^2 c_{2\beta}}{h_t^2} \right) - \frac{2}{5} \frac{X_t^2}{m_t^2} \right]$	$c_W = \frac{h_t^2}{(4\pi)^2} \frac{1}{40} \frac{X_t^2}{m_t^2}$
$c_{BB} = \frac{h_t^2}{(4\pi)^2} \frac{17}{144} \left[ \left( 1 + \frac{31}{102} \frac{g'^2 c_{2\beta}}{h_t^2} \right) - \frac{38}{85} \frac{X_t^2}{m_t^2} \right]$	$c_B = \frac{h_t^2}{(4\pi)^2} \frac{1}{40} \frac{X_t^2}{m_t^2}$

B. Henning, X. Lu and H. Murayama  
arXiv:1404.1058

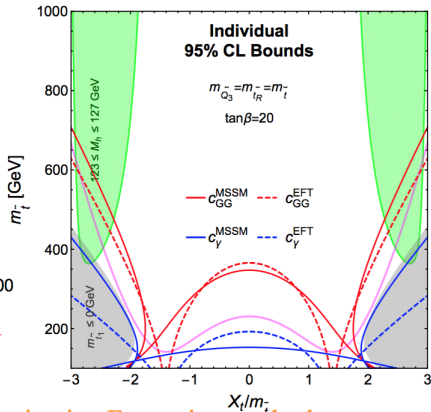
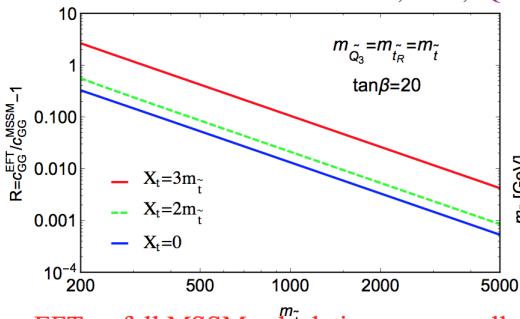
Wilson coefficients for degenerate  
stop soft SUSY breaking masses

$c_{3G} = \frac{g_s^2}{(4\pi)^2} \frac{1}{20}$	$c_H = \frac{h_t^2}{(4\pi)^2} \frac{3}{4} \left[ \left( 1 + \frac{g'^2 c_{2\beta}}{h_t^2} + \frac{g'^4 c_{2\beta}^2}{h_t^4} \right) - \frac{7}{6} \frac{X_t^2}{m_t^2} \left( 1 + \frac{1}{14} \frac{(g^2 + 2g'^2) c_{2\beta}}{h_t^2} \right) + \frac{7}{30} \frac{X_t^4}{m_t^4} \right]$
$c_{3W} = \frac{g^2}{(4\pi)^2} \frac{1}{20}$	$c_T = \frac{h_t^2}{(4\pi)^2} \frac{1}{4} \left[ \left( 1 + \frac{g'^2 c_{2\beta}}{h_t^2} \right)^2 - \frac{1}{2} \frac{X_t^2}{m_t^2} \left( 1 + \frac{1}{2} \frac{g'^2 c_{2\beta}}{h_t^2} \right) + \frac{1}{10} \frac{X_t^4}{m_t^4} \right]$
$c_{2G} = \frac{g_s^2}{(4\pi)^2} \frac{1}{20}$	$c_R = \frac{h_t^2}{(4\pi)^2} \frac{1}{2} \left[ \left( 1 + \frac{g'^2 c_{2\beta}}{h_t^2} \right)^2 - \frac{3}{2} \frac{X_t^2}{m_t^2} \left( 1 + \frac{1}{12} \frac{(3g^2 + g'^2) c_{2\beta}}{h_t^2} \right) + \frac{3}{10} \frac{X_t^4}{m_t^4} \right]$
$c_{2W} = \frac{g^2}{(4\pi)^2} \frac{1}{20}$	$c_D = \frac{h_t^2}{(4\pi)^2} \frac{1}{20} \frac{X_t^2}{m_t^2}$
$c_{2B} = \frac{g'^2}{(4\pi)^2} \frac{1}{20}$	

A. Drozd, J. Ellis, J.Q. and T. You  
arXiv 1504.02409 + work in progress..  
general expression of the Wilson  
coefficients : non-degenerate stop  
masses

# Covering the MSSM stop sector at the LHC

A. Drozd, J. Ellis, J.Q. and T. You arXiv 1504.02409



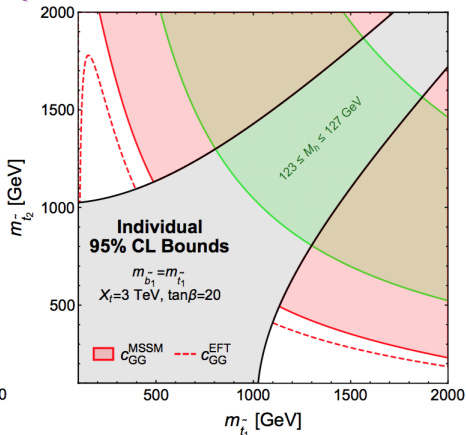
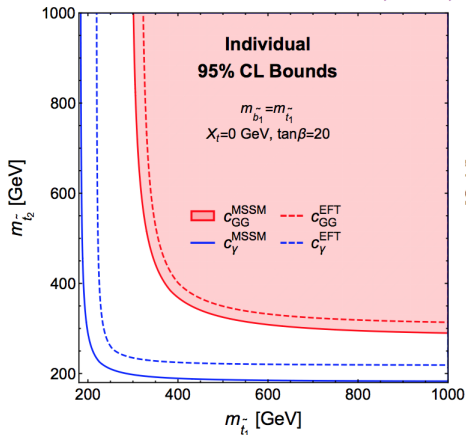
- EFT vs full MSSM calculation agrees well (non-trivial check!)
- EFT calculation simplified by Covariant Derivative Expansion method Henning, Lu & Murayama [arXiv:1412.1837]
- Systematic way of integrating out UV degrees of freedom in manifestly gauge-invariant way
- The universal 1-loop EFT facilitates extending constraints to any UV model: work in progress...



# Covering the MSSM stop sector at the LHC

## General case: non-degenerate stops

A. Drozd, J. Ellis, J.Q. and T. You arXiv 1504.02409

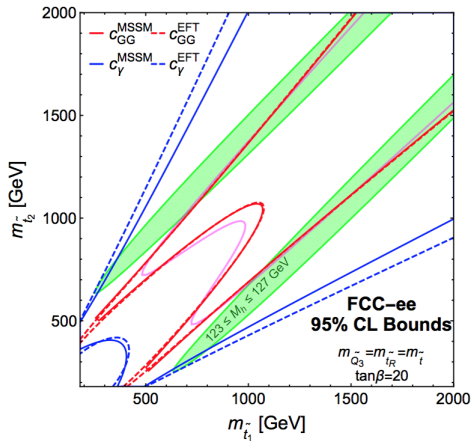
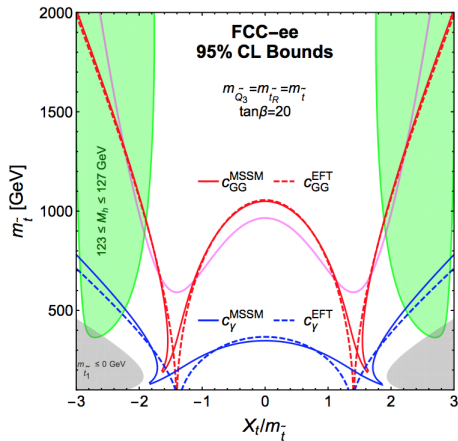


- The current sensitivity is already comparable to that of direct LHC searches

# Covering the MSSM stop sector at the LHC

## General case: non-degenerate stops

A. Drozd, J. Ellis, J.Q. and T. You arXiv 1504.02409



- Future FCC-ee measurements could be sensitive to stop masses above a TeV

# Conclusion

- $M_h \approx 125$  GeV and the non-observation of SUSY particles, seems to indicate that the soft-SUSY breaking scale might be large
- We have discussed the hMSSM, i.e. the MSSM that we seem to have after the discovery of the Higgs boson at the LHC  
⇒ the MSSM Higgs sector can be described by only  $(\tan \beta, M_A)$
- $H/A/H^\pm$  searches at the LHC are becoming very constraining
- Some search channels at low  $\tan \beta$  still relevant:  $H \rightarrow \tau\tau, WW, ZZ, hZ, hh, tt$  ⇒ need to continue/adapt the SM Higgs searches at high masses!
- 7–8 TeV LHC for the lightest h and 13–14 TeV LHC for  $H/A/H^\pm$ ? and maybe some SUSY particles will show up?
  
- The universal 1-loop EFT facilitates extending constraints to any UV model
- The current sensitivity is already comparable to that of direct LHC searches (MSSM)
- Future FCC-ee measurements could be sensitive to stop masses above a TeV

Thanks !

# The Minimal Supersymmetric Standard Model

Defined by 4 assumptions :

**(a) Minimal gauge group:** the MSSM is based on the group  $SU(3)_C \times SU(2)_L \times U(1)_Y$ , i.e. the SM gauge symmetry.

**(b) Minimal particle content:**

gauge bosons + spin 1/2 SUSY partners :  $\hat{G}^a, \hat{W}^a, \hat{B}$  (vector superfields)  
quarks and leptons + squarks and sleptons:  $\hat{Q}, \hat{U}_R, \hat{D}_R, \hat{L}, \hat{E}_R$ . (3 gen. of chiral superfields)  
2 Higgs doublets + spin 1/2 SUSY partners:  $\hat{H}_1, \hat{H}_2$

**(c) Minimal Yukawa interactions and R-parity conservation:** a discrete symmetry called R-parity is imposed (enforce lepton and baryon number conservation)

$$R_p = (-1)^{2s+3B+L}; \quad R_p = \pm 1 \quad \text{for SM/SUSY particule}$$

**(d) Minimal set of soft SUSY-breaking terms:**

- **Mass for gauginos:**  $-\mathcal{L}_{\text{gino}} = \frac{1}{2} \left[ M_1 \tilde{B} \tilde{B} + M_2 \sum_{a=1}^3 \tilde{W}^a \tilde{W}_a + M_3 \sum_{a=1}^8 \tilde{G}^a \tilde{G}_a + \text{h.c.} \right]$
- **Mass for sfermions:**  $-\mathcal{L}_{\text{sf}} = \sum_{i=\text{gen}} m_{\tilde{Q}_i}^2 \tilde{Q}_i^\dagger \tilde{Q}_i + m_{\tilde{L}_i}^2 \tilde{L}_i^\dagger \tilde{L}_i + m_{\tilde{u}_i}^2 |\tilde{u}_{R_i}|^2 + m_{\tilde{d}_i}^2 |\tilde{d}_{R_i}|^2 + m_{\tilde{\ell}_i}^2 |\tilde{\ell}_{R_i}|^2$
- **Mass and bilinear for the Higgs:**  $-\mathcal{L}_{\text{Higgs}} = m_{H_2}^2 H_2^\dagger H_2 + m_{H_1}^2 H_1^\dagger H_1 + B\mu(H_2 \cdot H_1 + \text{h.c.})$
- **Trilinear:**  $-\mathcal{L}_{\text{tril.}} = \sum_{i,j=\text{gen}} \left[ A_{ij}^u Y_{ij}^u \tilde{u}_{R_i}^* H_2 \cdot \tilde{Q}_j + A_{ij}^d Y_{ij}^d \tilde{d}_{R_i}^* H_1 \cdot \tilde{Q}_j + A_{ij}^\ell Y_{ij}^\ell \tilde{\ell}_{R_i}^* H_1 \cdot \tilde{L}_j + \text{h.c.} \right]$

105 parameters (SSB) + 19 (SM)  $\Rightarrow$  phenomenological analysis complicated

Only 22 for the pMSSM:

$M_1, M_2, M_3, m_{\tilde{q}}, m_{\tilde{u}_R}, m_{\tilde{d}_R}, A_u, A_d, A_e, m_{\tilde{\tau}}, m_{\tilde{e}_R}, m_{\tilde{Q}}, m_{\tilde{\ell}_R}, m_{\tilde{b}_R}, m_{\tilde{L}}, m_{\tilde{\tau}_R}, A_\tau, A_b, A_t, \tan \beta, m_{H_1}^2, m_{H_2}^2$