

Lecture:

Standard Model of Particle Physics

Heidelberg SS 2013

(Weak) Neutral Currents

Contents

- Theoretical Motivation for Neutral Currents
- NC Processes
- Experimental Discovery
- Measurement of the Weinberg Angle
- NC Fermion couplings

Recap: Weinberg-Salam Theory

Left handed fermions (doublets): $\psi_1 =$

$$\begin{pmatrix} \nu_e \\ e^- \end{pmatrix}_L \quad \begin{pmatrix} \nu_\mu \\ \mu^- \end{pmatrix}_L \quad \begin{pmatrix} \nu_\tau \\ \tau^- \end{pmatrix}_L \quad \begin{pmatrix} u \\ d' \end{pmatrix}_L \quad \begin{pmatrix} c \\ s' \end{pmatrix}_L \quad \begin{pmatrix} t \\ b' \end{pmatrix}_L$$

Right handed fermions (singlets): $\psi_2 =$

$$\begin{matrix} \nu_{e,R} & \nu_{\mu,R} & \nu_{\tau,R} & u_R & c_R & t_R \\ \psi_3 = & e_R^- & \mu_R^- & \tau_R^- & d_R & s_R & b_R \end{matrix}$$

Gauge Transformations:

$$\psi_j(x) \rightarrow \psi'_j(x) = \exp\left(i\vec{\alpha}(x) \cdot \frac{\vec{\tau}}{2}\right) \cdot \exp\left(i\beta(x) \frac{Y_j}{2}\right) \psi_j(x)$$

SU(2)

U(1)

τ : Pauli matrices Y_j : hypercharge

Smallest gauge group representation with >1 gauge boson is **SU(2)**:

W^+ , W^- represented by

$$\tau^\pm = \frac{1}{2} (\tau_1 \pm i\tau_2)$$

additional W_3 field represented by:

$$\tau_3 \quad (\rightarrow 4\text{th gauge boson})$$

Recap: Weinberg-Salam Theory

Left handed fermions (doublets): $\psi_1 = \begin{pmatrix} \mathbf{v}_e \\ e^- \end{pmatrix}_L \quad \begin{pmatrix} \mathbf{v}_\mu \\ \mu^- \end{pmatrix}_L \quad \begin{pmatrix} \mathbf{v}_\tau \\ \tau^- \end{pmatrix}_L \quad \begin{pmatrix} u \\ d' \end{pmatrix}_L \quad \begin{pmatrix} c \\ s' \end{pmatrix}_L \quad \begin{pmatrix} t \\ b' \end{pmatrix}_L$

Right handed fermions (singlets): $\psi_2 = \mathbf{v}_{e,R} \quad \mathbf{v}_{\mu,R} \quad \mathbf{v}_{\tau,R} \quad u_R \quad c_R \quad t_R$
 $\psi_3 = e_R^- \quad \mu_R^- \quad \tau_R^- \quad d_R \quad s_R \quad b_R$

Gauge Transformations:

$$\psi_j(x) \rightarrow \psi'_j(x) = \exp\left(i\vec{\alpha}(x) \cdot \frac{\vec{\tau}}{2}\right) \cdot \exp\left(i\beta(x) \frac{Y_j}{2}\right) \psi_j(x)$$

SU(2)

U(1)

τ : Pauli matrices Y_j : hypercharge

Note:

- SU(2) fields W_1, W_2, W_3 , and U(1) field B (hypercharge) correspond to **massless** bosons!
- fields W_3 (V-A coupling) and B (hypercharge) can/do **mix!**

Electroweak Symmetry Breaking

$$\begin{pmatrix} Z \\ A \end{pmatrix} = \begin{pmatrix} \cos \theta_W & -\sin \theta_W \\ \sin \theta_W & \cos \theta_W \end{pmatrix} \begin{pmatrix} W_3 \\ B \end{pmatrix} \leftrightarrow \begin{pmatrix} W_3 \\ B \end{pmatrix} = \begin{pmatrix} \cos \theta_W & \sin \theta_W \\ -\sin \theta_W & \cos \theta_W \end{pmatrix} \begin{pmatrix} Z \\ A \end{pmatrix}$$

$$L_{ew} = g j_L^3 W_3 + \frac{1}{2} g' j^Y B$$



symmetry breaking

$$L_{elm} = g j_L^3 \sin \theta_W A + \frac{1}{2} g' j^Y \cos \theta_W A$$

$$L_{NC} = g j_L^3 \cos \theta_W Z - \frac{1}{2} g' j^Y \sin \theta_W Z$$

Electromagnetic Interaction

$$L_{elm} = g j_L^3 \sin \theta_W A + \frac{1}{2} g' j^Y \cos \theta_W A$$

Left-Handed Current:

Pauli matrix τ_3 : $\tau_3 = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$ $j_L^3 = \frac{1}{2} (\bar{U}_L U_L - \bar{D}_L D_L)$

isospin up isospin down

Hypercharge Current:

$$j_Y = \bar{\psi} \hat{Y} \psi = Y_{doublet} \bar{U}_L U_L + Y_{doublet} \bar{D}_L D_L + Y_{singlet} \bar{D}_R D_R$$

only “down” component here (leptons)!

Photon field: vector current and coupling to electric charges:

1. $e = g \sin \theta_W = g' \cos \theta_W \quad \rightarrow \quad j_{elm} = j_L^3 + \frac{1}{2} j^Y \quad \rightarrow \quad Q = I + \frac{1}{2} Y$ Gell-Mann Nishijima
2. Leptons: $Y_{doublet} = -1, Y_{singlet} = -2 \quad \rightarrow \quad j_{elm} = -\bar{D}_L D_L - \bar{D}_R D_R \quad (e, \mu, \tau)$
3. Quarks: $Y_{doublet} = \frac{1}{3}, Y_{u-singlet} = \frac{4}{3}, Y_{d-singlet} = -\frac{2}{3}$

Weak Neutral Current

$$L_{NC} = g j_L^3 \cos \theta_W Z - \frac{1}{2} g' j^Y \sin \theta_W Z$$

$$\propto \left(\frac{g}{\cos \theta_W} \right) \cos^2 \theta_W \quad \propto g' \sin \theta_W = \left(\frac{g}{\cos \theta_W} \right) \sin^2 \theta_W$$

$$\frac{ig\gamma^\mu}{\cos \theta_W} \frac{1}{2} (C_V - C_A \gamma_5)$$

$$(j_{NC})^\mu = \bar{\Psi} \gamma^\mu \frac{1}{2} [c_L (1 - \gamma^5) + c_R (1 + \gamma^5)] \Psi_e$$

$$I_3 = -1/2$$

$$I_3 = +1/2$$

$$c_L = -1/2 - Q_f \sin^2 \Theta_W \quad +1/2 - Q_f \sin^2 \Theta_W$$

$$c_R = -Q_f \sin^2 \Theta_W' \quad -Q_f \sin^2 \Theta_W'$$

no pure V-A coupling
for non-zero
Weinberg angle!

$$(j_{NC}^e)^\mu = \bar{\Psi}_e \gamma^\mu \frac{1}{2} (C_V - C_A \gamma_5) \Psi_e$$

$$I_3 = -1/2$$

$$I_3 = +1/2$$

$$C_A = -1/2 \quad +1/2$$

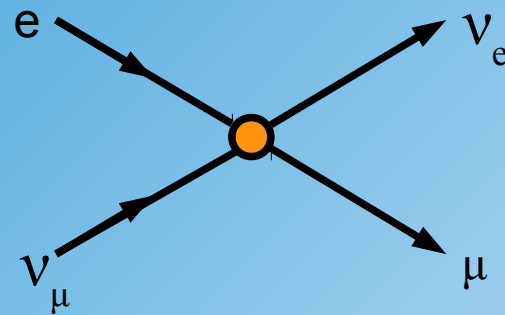
$$C_V = -1/2' - 2Q_f \sin^2 \Theta_W \quad +1/2' - 2Q_f \sin^2 \Theta_W$$

Unitarity in SU(2) Gauge Group

Recall:

divergent behavior at high energies

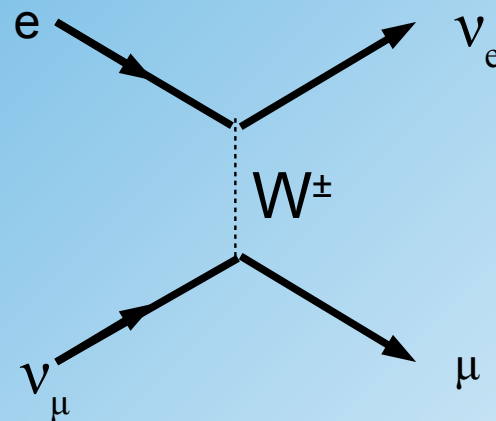
$$\sigma(\nu_\mu e \rightarrow \mu \nu_e) \propto G_F^2 s$$



four-fermion interaction

fixed by introducing the W-boson

$$\sigma(\nu_\mu e \rightarrow \mu \nu_e) \propto G_F^2$$



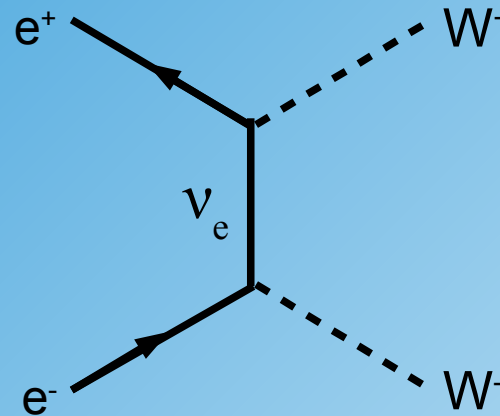
W-exchange

Unitarity in SU(2) Gauge Group

Fermion W-boson Scattering

$$\sigma(e^- e^+ \rightarrow W_0^- W_0^+) \propto G_F^2 s$$

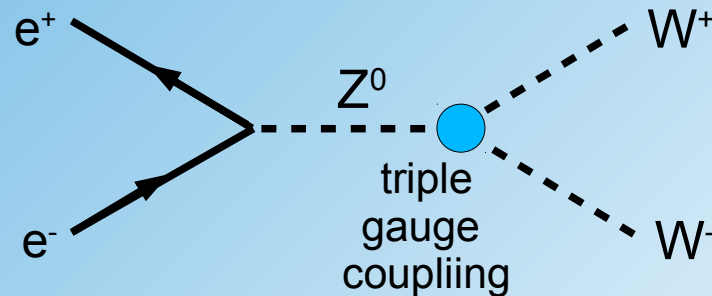
divergent high energy behavior
of longitudinal ($J_3=0$) spin component



e.g. W-pair production

fixed by introducing the Z boson (predicted by non-abelian SU(2))

$$\sigma(e^- e^+ \rightarrow W_0^- W_0^+) \propto G_F^2$$



General Rule (1970, t'Hooft, Veltmann):

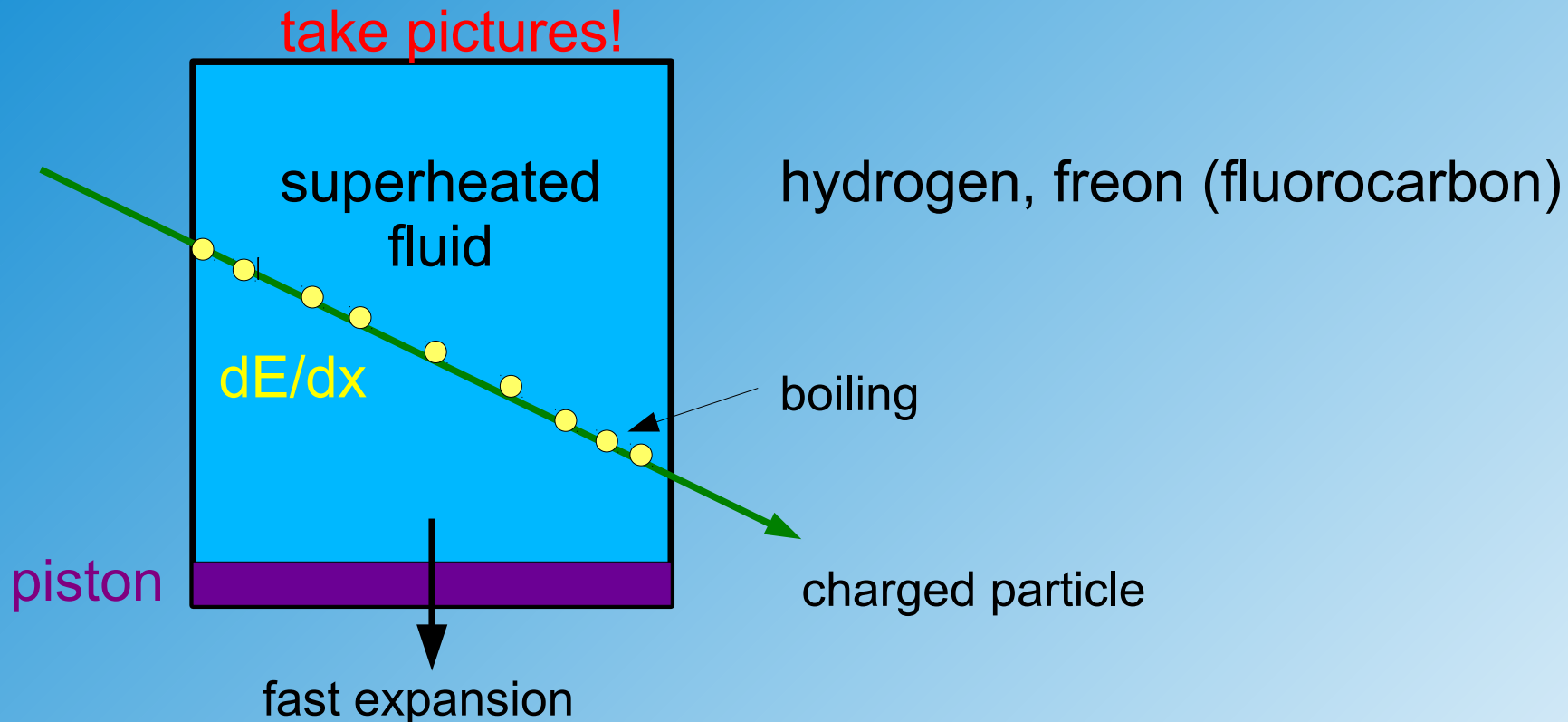
UV-divergences vanish only in gauge invariant theories

Neutrino-Nucleon Scattering Experiments

Experimental Discovery of NC

in early 70ties bubble chambers where used to study particle interactions

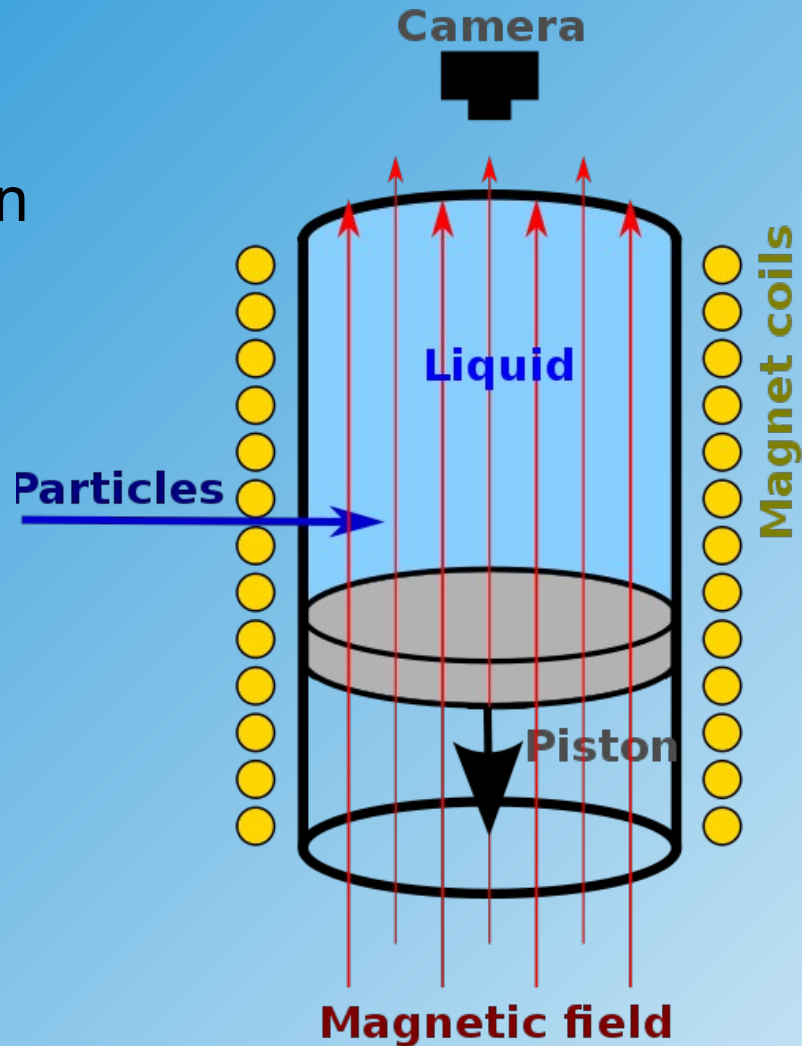
Principle:



- reconstruction of all charged particles!
- problem: low repetition rate, difficult analysis

BEBC principle

Liquid = hydrogen

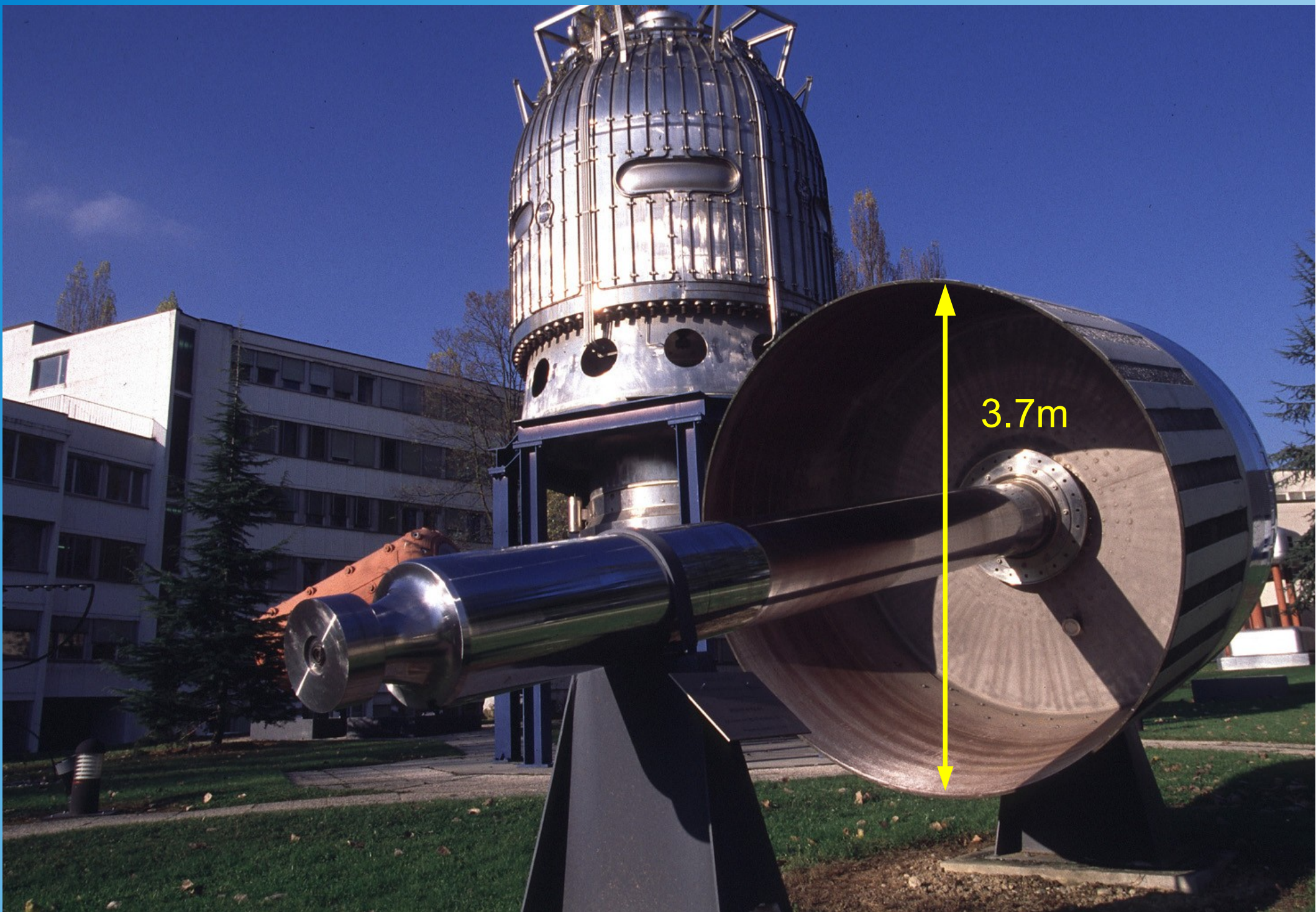


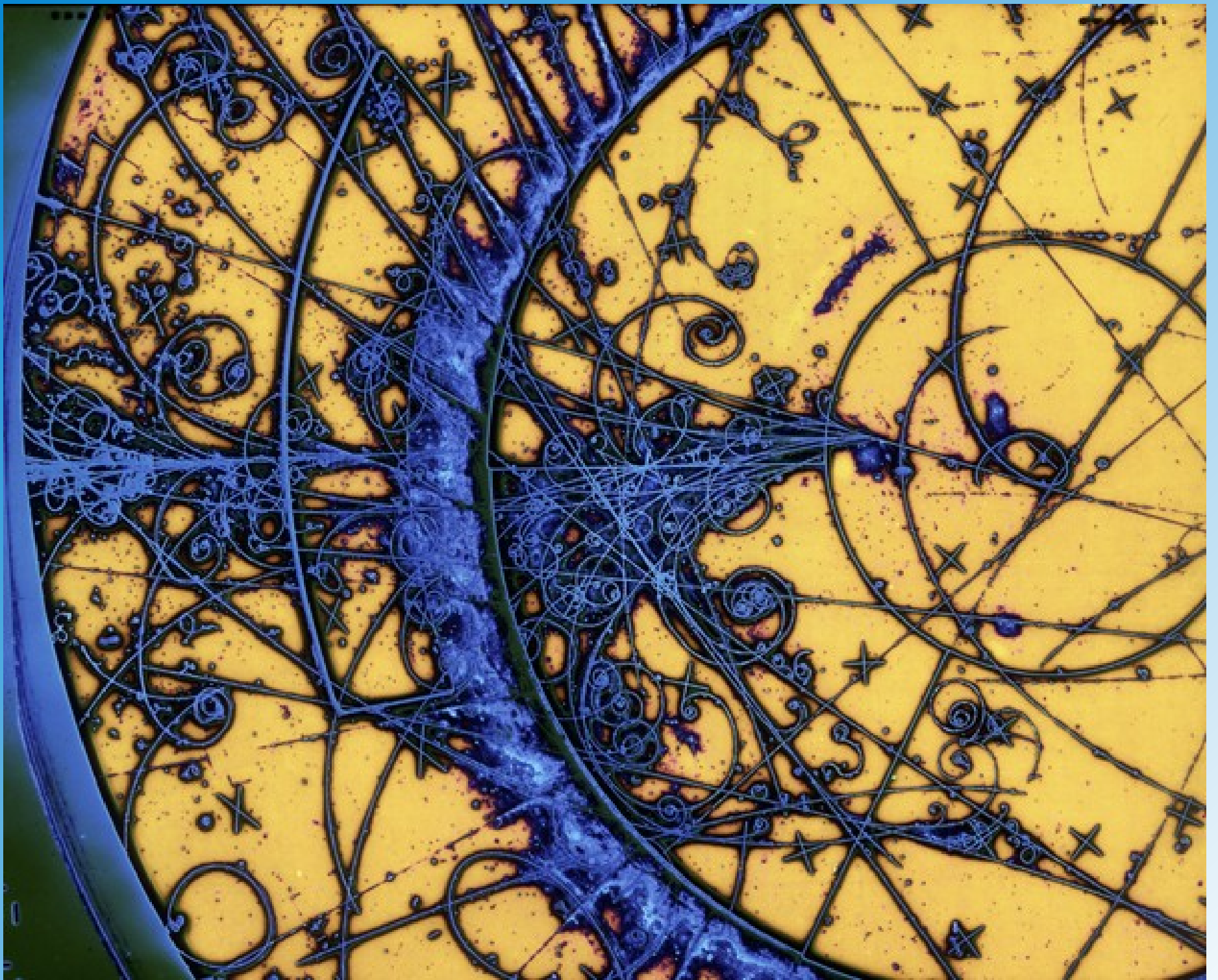
BEBC (CERN, 1967-1984)

Heidelberg -Saclay-CERN

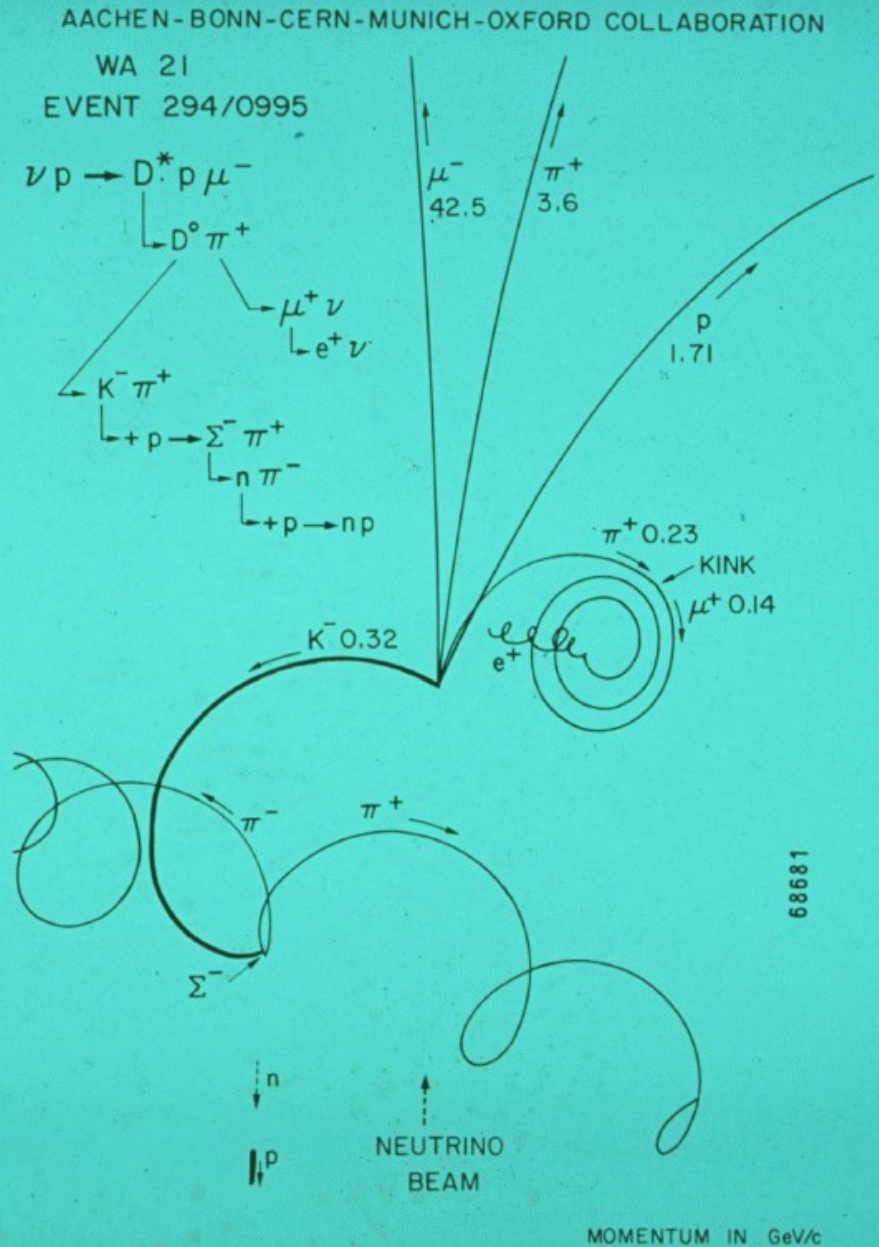
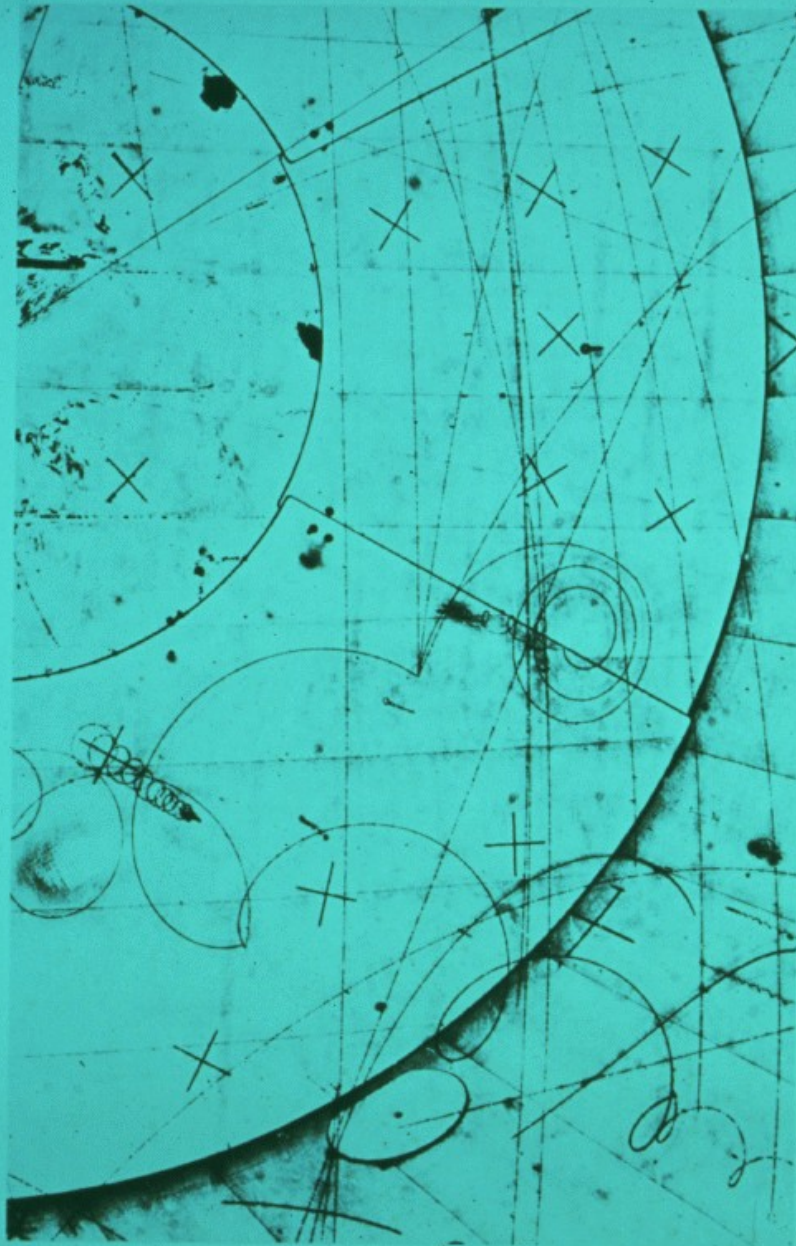
6.3 million photographs







Neutrino-Proton Scattering (Charged Current)

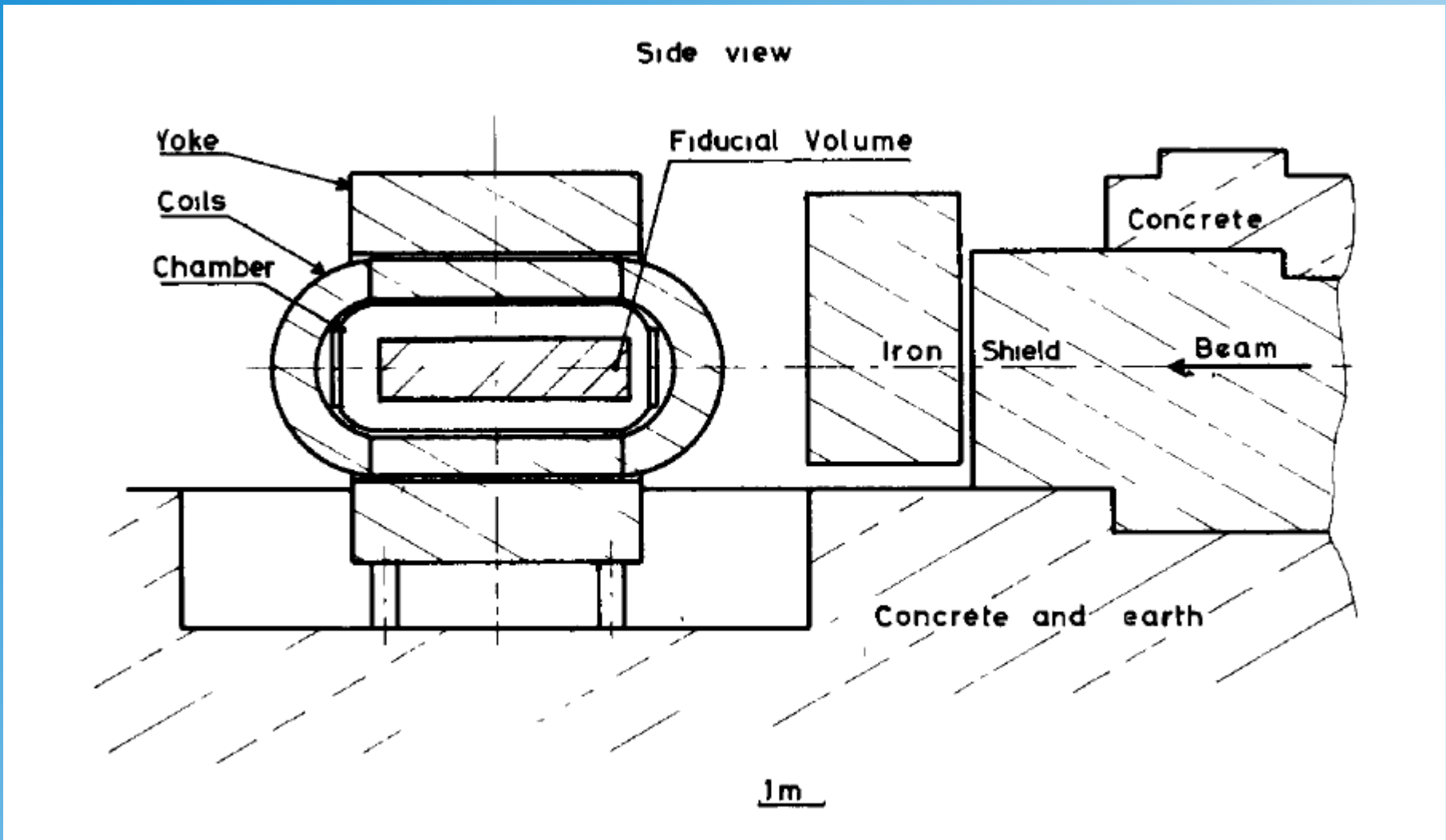


Gargamelle

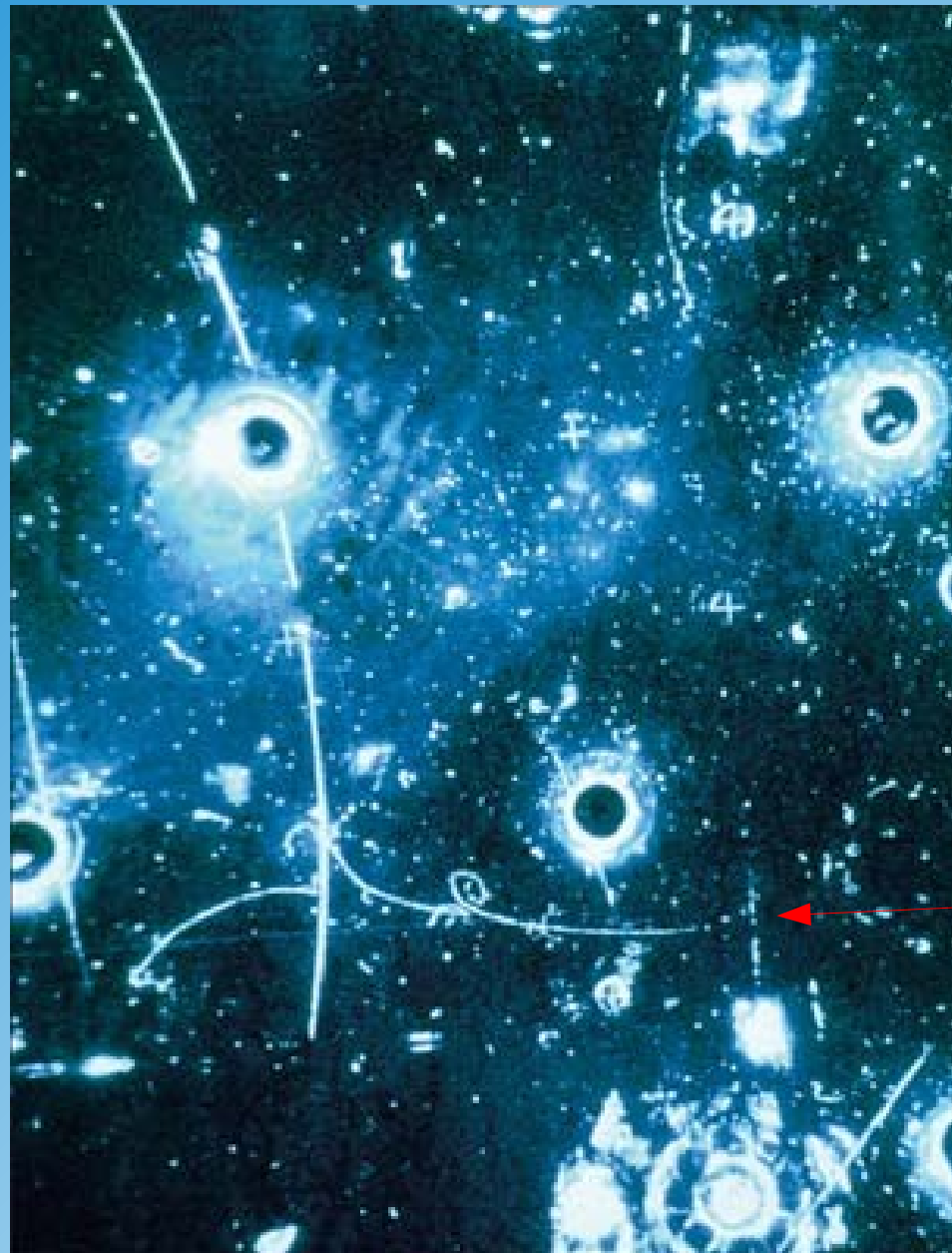
Liquid: freon (CF_3Br).



Cross Section of Experiment



Elastic Neutral Current $\nu_e \rightarrow \nu_e$



Discovery of Neutral Currents

SEARCH FOR ELASTIC MUON-NEUTRINO ELECTRON SCATTERING

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Table 1
Number of single e^- events of $E_e > 300$ MeV, $\theta_e < 5^\circ$

Flux neutrinos/m ²	Weinberg predictions		Background	Observed
	Mini- mum	Maxi- mum		
ν 1.8×10^{15}	0.6	6.0	0.3 ± 0.2	0
$\bar{\nu}$ 1.2×10^{15}	0.4	8.0	0.03 ± 0.02	1

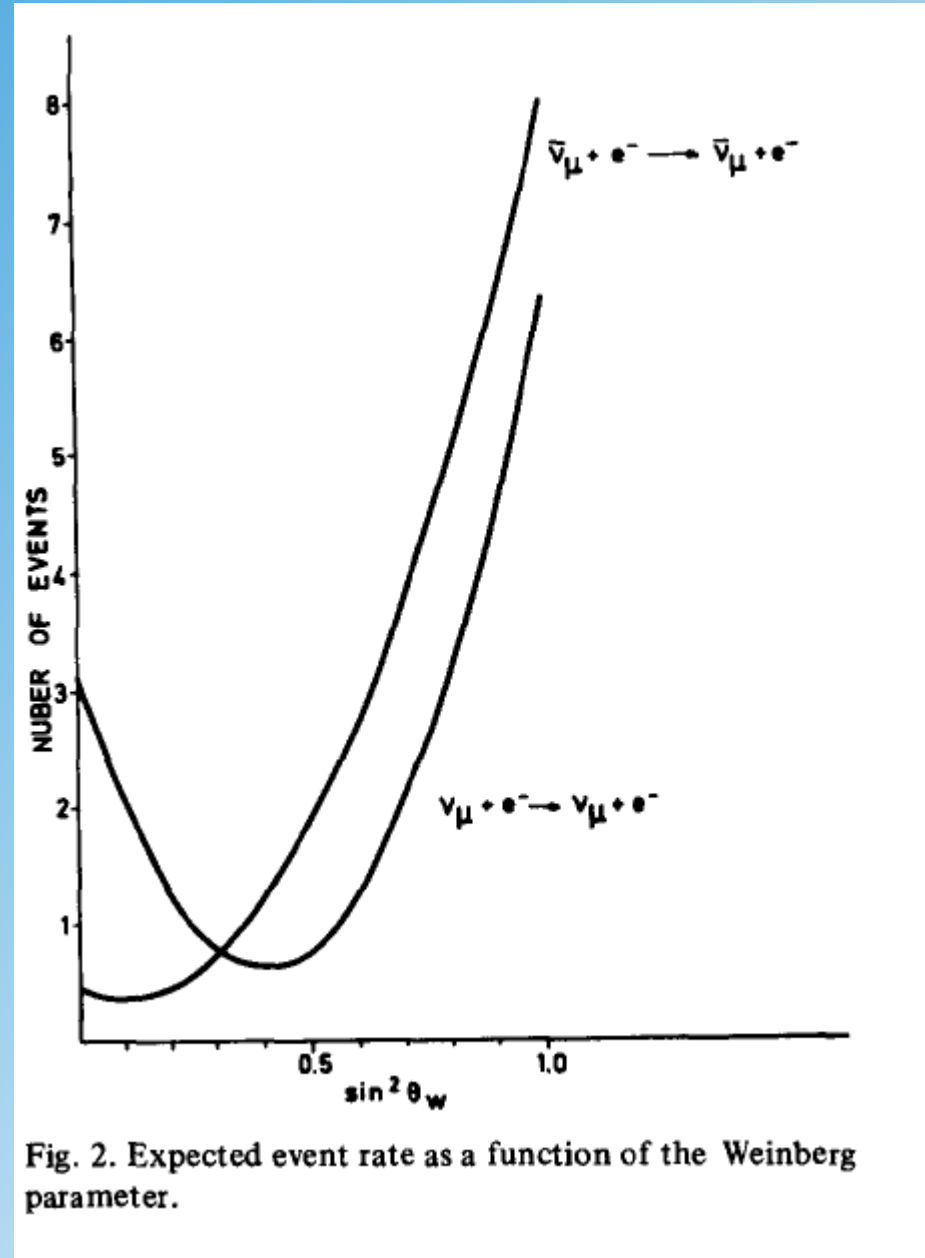


Fig. 2. Expected event rate as a function of the Weinberg parameter.

$$0.1 < \sin^2 \theta_W < 0.6.$$

Hasert et al.

Classification of Inelastic Events

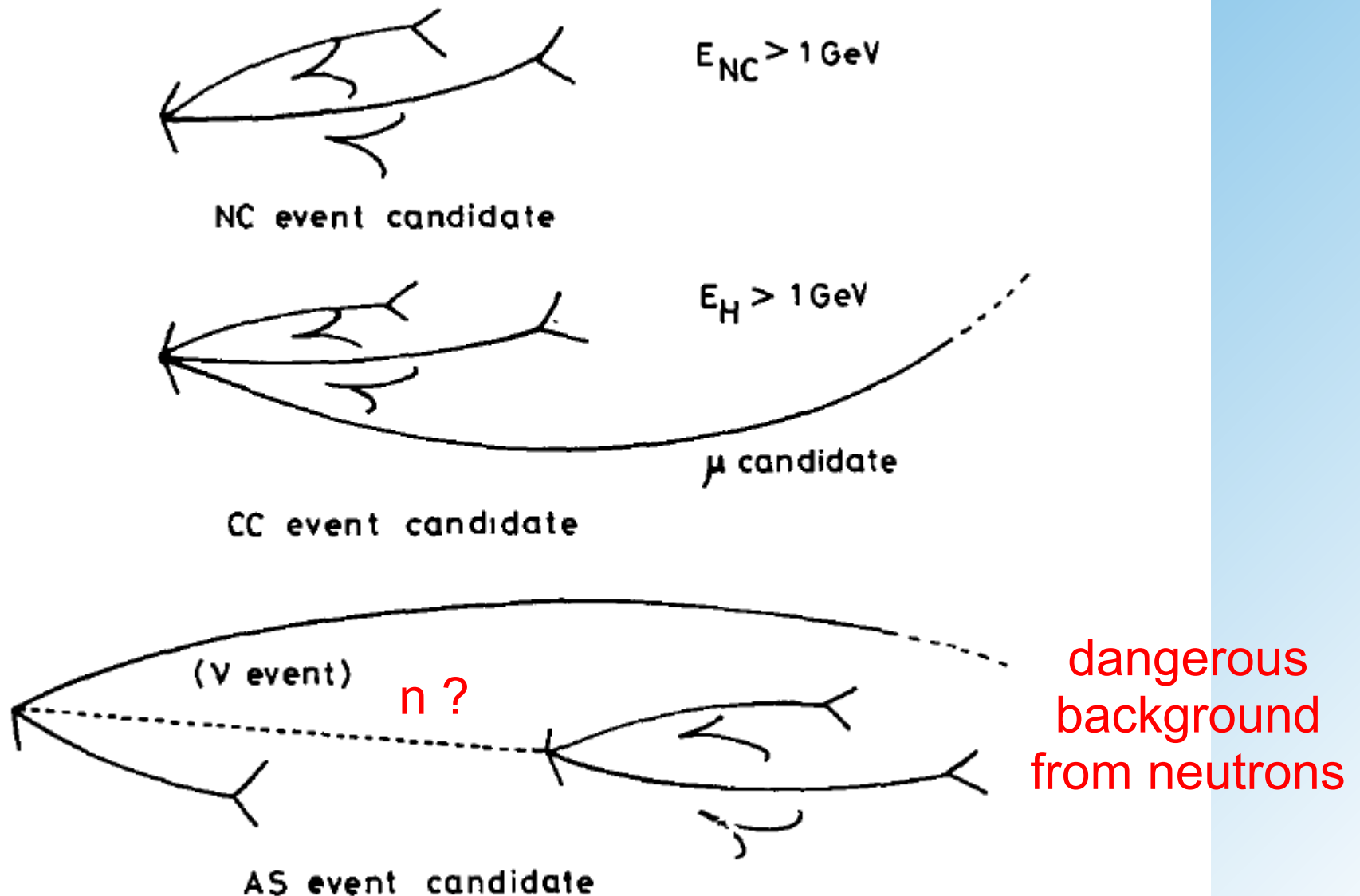
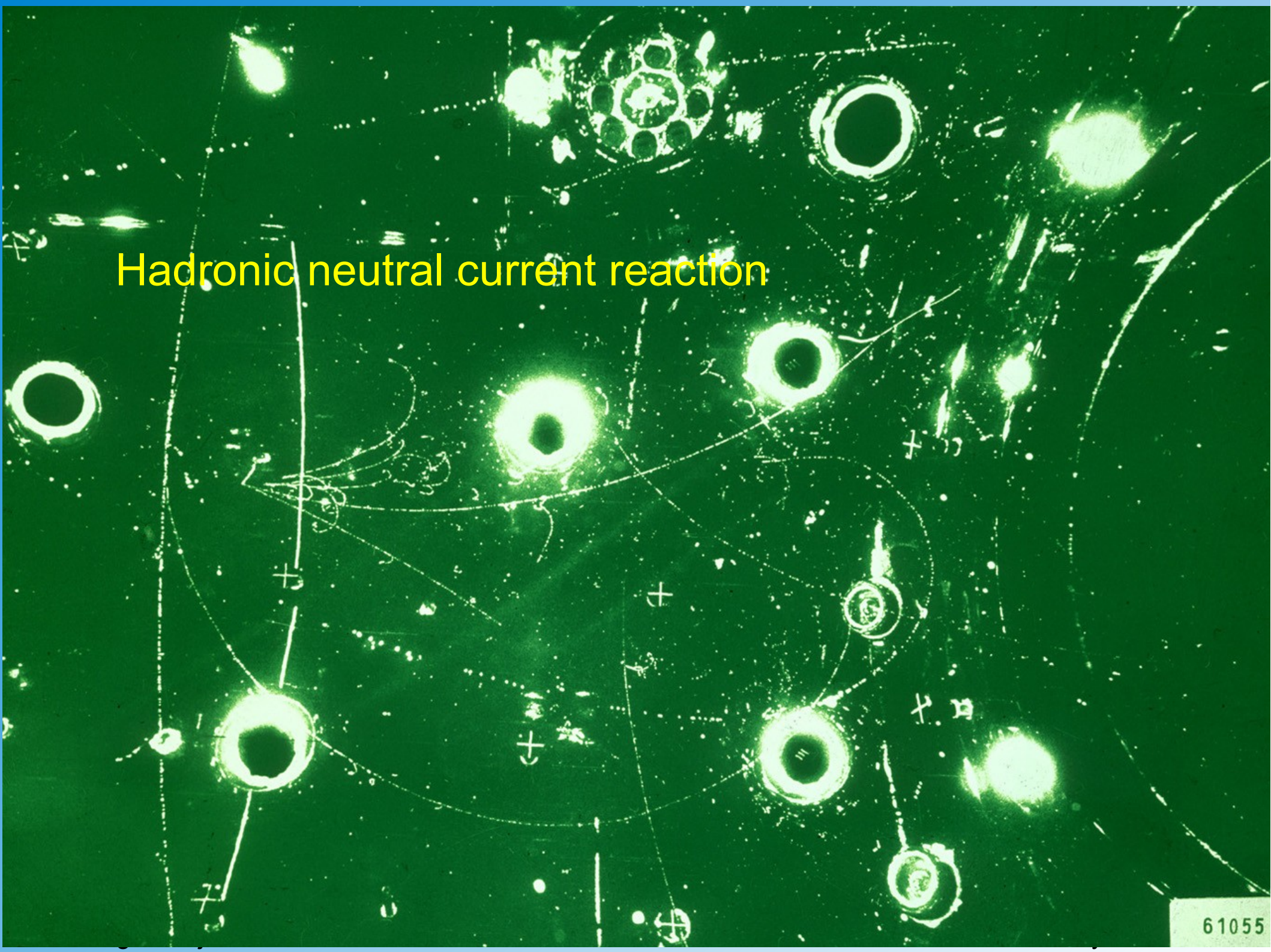


Fig. 4. Diagrammatic representations of NC, CC and AS events.

Hadronic neutral current reaction



NC/CC Ratio

Neutrino-Nucleon Scattering

Anti-neutrino Beam

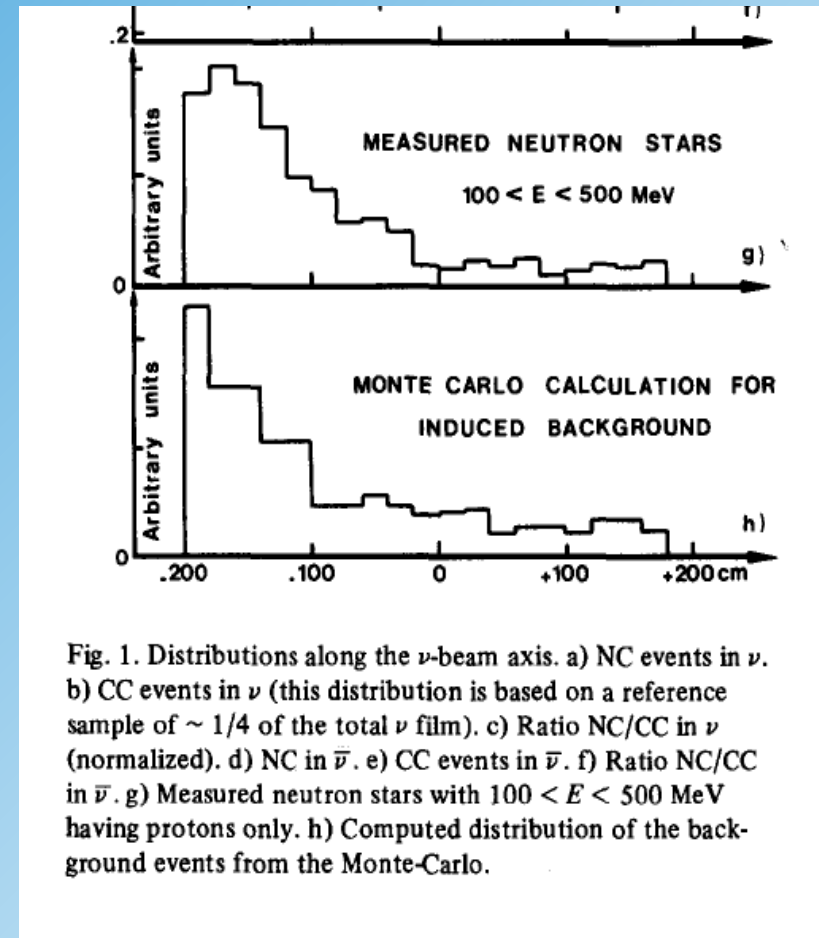
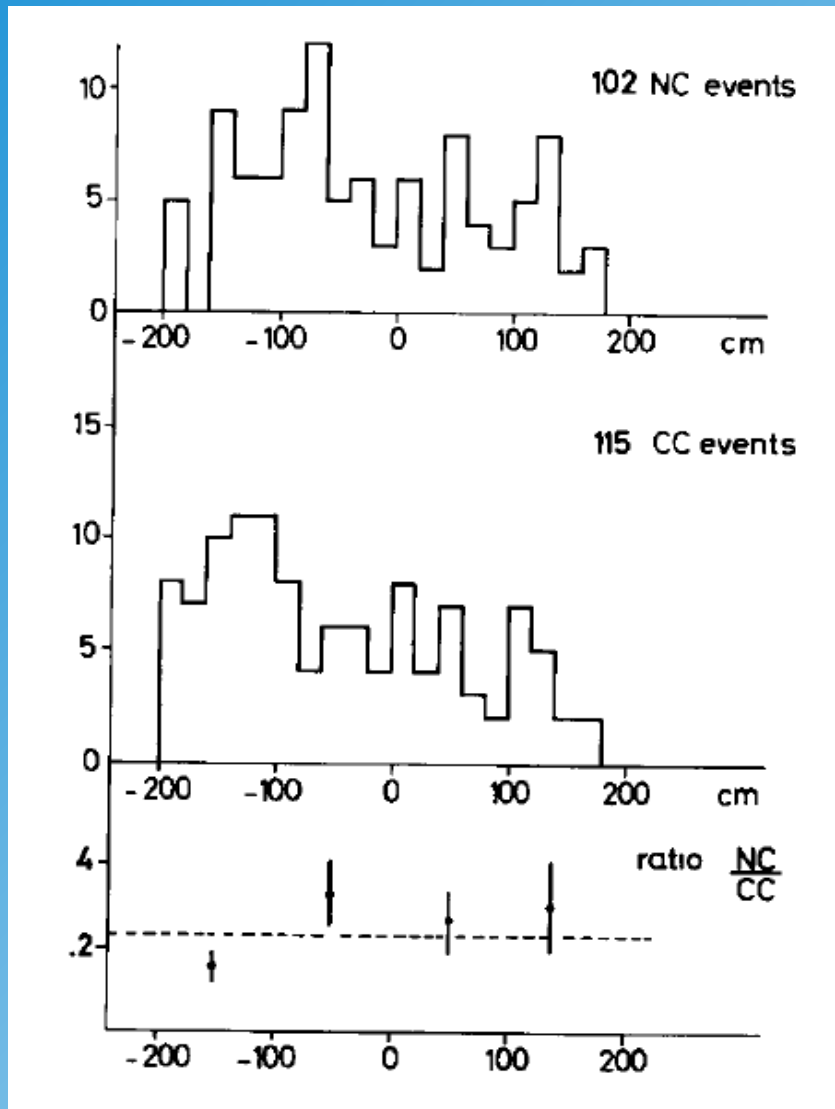


Fig. 1. Distributions along the ν -beam axis. a) NC events in ν . b) CC events in ν (this distribution is based on a reference sample of $\sim 1/4$ of the total ν film). c) Ratio NC/CC in ν (normalized). d) NC in $\bar{\nu}$. e) CC events in $\bar{\nu}$. f) Ratio NC/CC in $\bar{\nu}$. g) Measured neutron stars with $100 < E < 500$ MeV having protons only. h) Computed distribution of the background events from the Monte-Carlo.

R-Measurements in Gargamelle

Neutrino-Nucleon Scattering

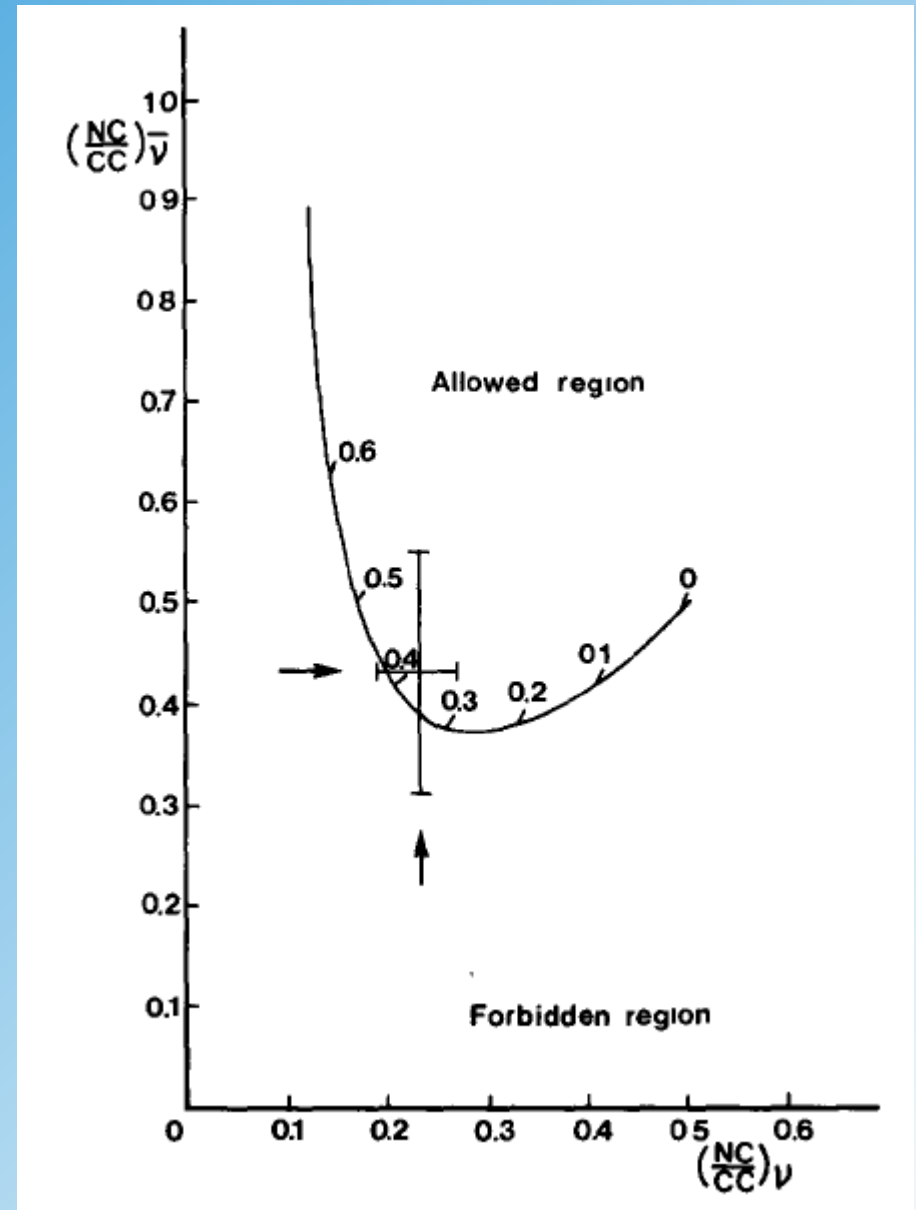
$NC(\nu) = 88.2$ events , $NC(\bar{\nu}) = 45.3$ events .

$CC(\nu) = 403$ events; $CC(\bar{\nu}) = 104.5$ events .

Finally we obtain the ratios:

$$\frac{NC}{CC}(\nu) = 0.22 \pm 0.04; \quad \frac{NC}{CC}(\bar{\nu}) = 0.43 \pm 0.12 .$$

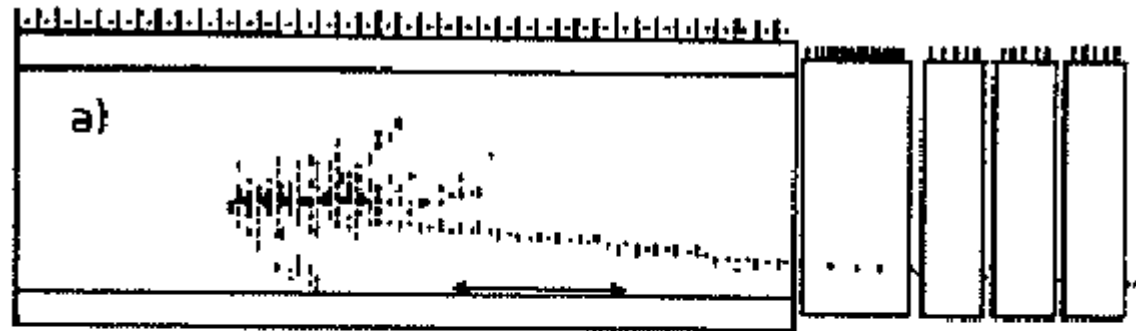
NC event in every ~ 1000 th film



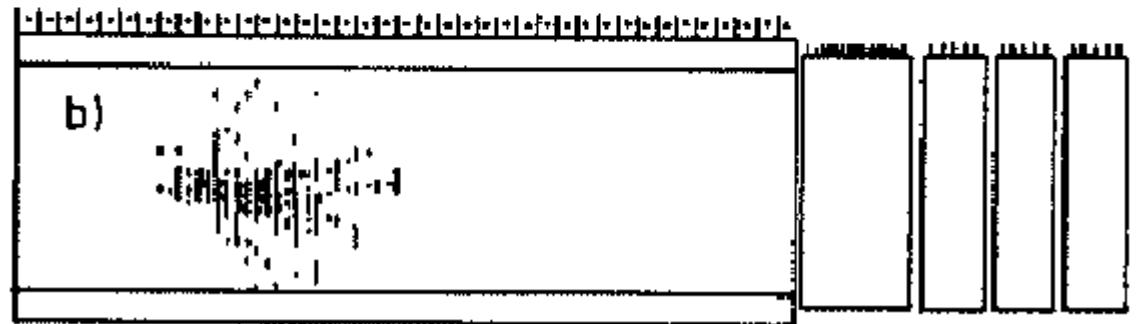
Signatures in CHARM Experiment

Drift Chambers:

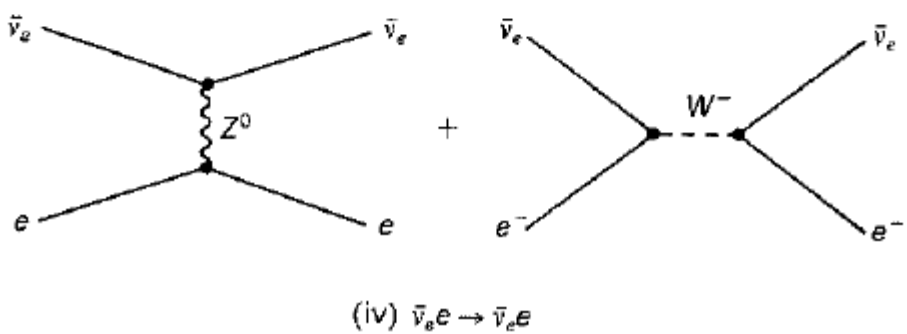
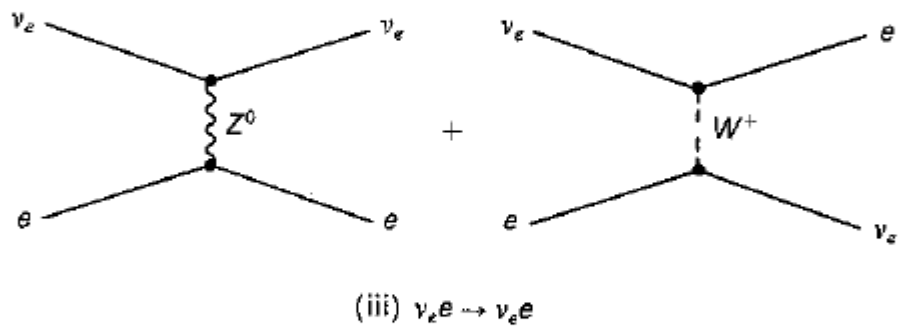
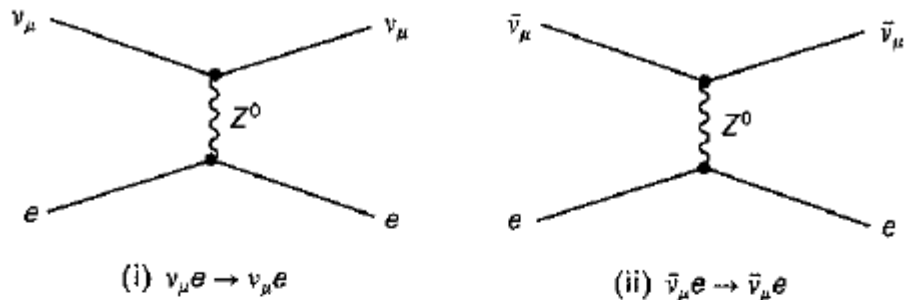
charged currents



neutral currents



Neutrino-Electron Scattering



$$\frac{d\sigma^{\nu e(\text{NC})}}{dy} = \frac{2G^2 m E}{\pi} [g_L^2 + g_R^2 (1-y)^2],$$

and similar for anti-neutrinos

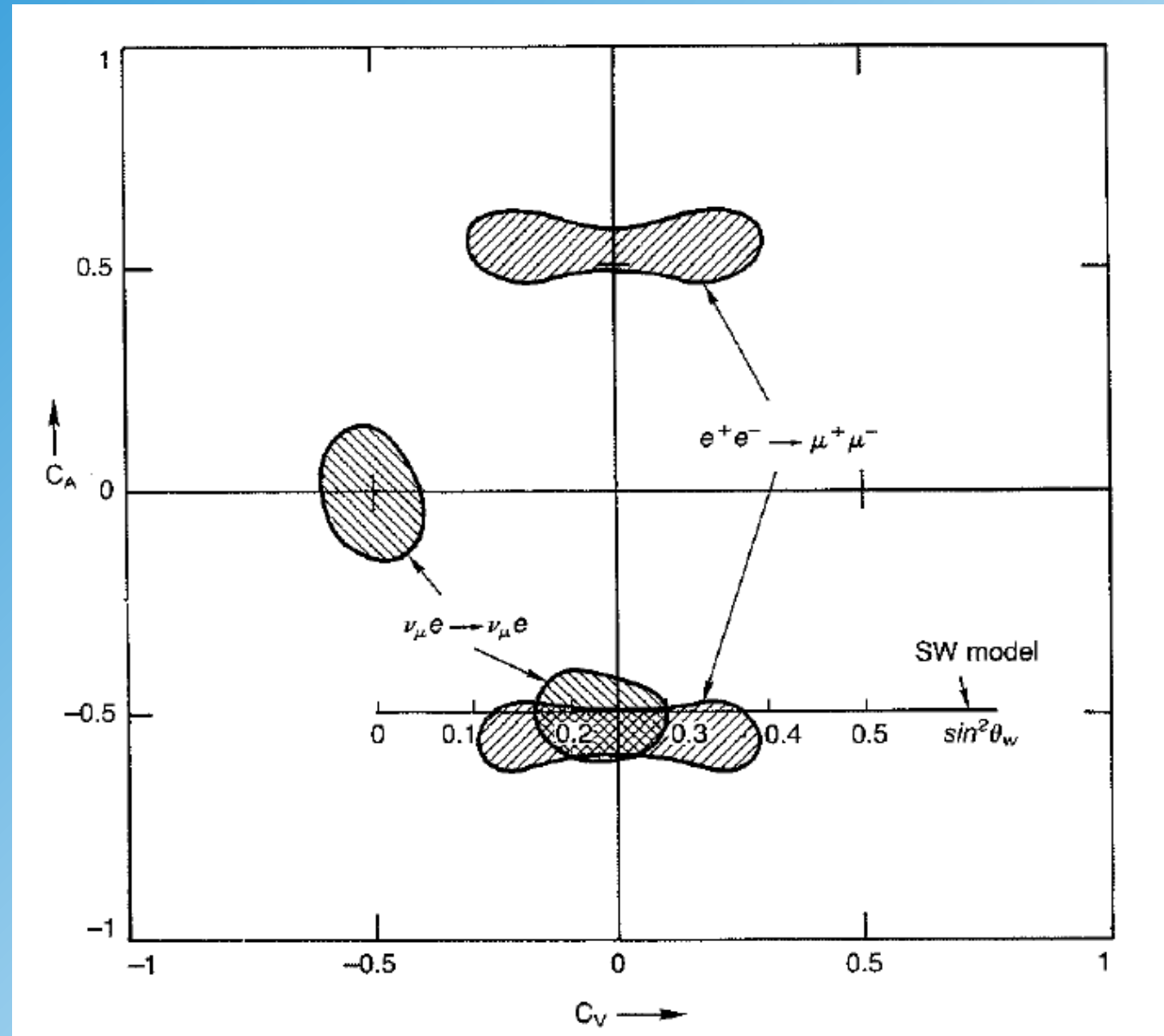
	g_L	g_R
(i) $\nu_\mu e \rightarrow \nu_\mu e$	$-\frac{1}{2} + \sin^2 \theta_w$	$\sin^2 \theta_w$
(ii) $\bar{\nu}_\mu e \rightarrow \bar{\nu}_\mu e$	$\sin^2 \theta_w$	$-\frac{1}{2} + \sin^2 \theta_w$
(iii) $\nu_e e \rightarrow \nu_e e$	$\frac{1}{2} + \sin^2 \theta_w$	$\sin^2 \theta_w$
(iv) $\bar{\nu}_e e \rightarrow \bar{\nu}_e e$	$\sin^2 \theta_w$	$\frac{1}{2} + \sin^2 \theta_w$

possible to determine couplings and Weinberg angle from different reactions

Lepton Couplings

$$\begin{aligned}
 C_A &= I_3 - Q_f \sin^2 \Theta_W \\
 C_V &= I_3 - 2Q_f \sin^2 \Theta_W
 \end{aligned}$$

compilation of several experiments (Wu)



Deep Inelastic Neutrino-Lepton Scattering and Weinberg Angle

$$\frac{d^2\sigma^{\nu N(\text{CC})}}{dx dy} = \frac{G^2 M E x}{2\pi} [u(x) + d(x)],$$

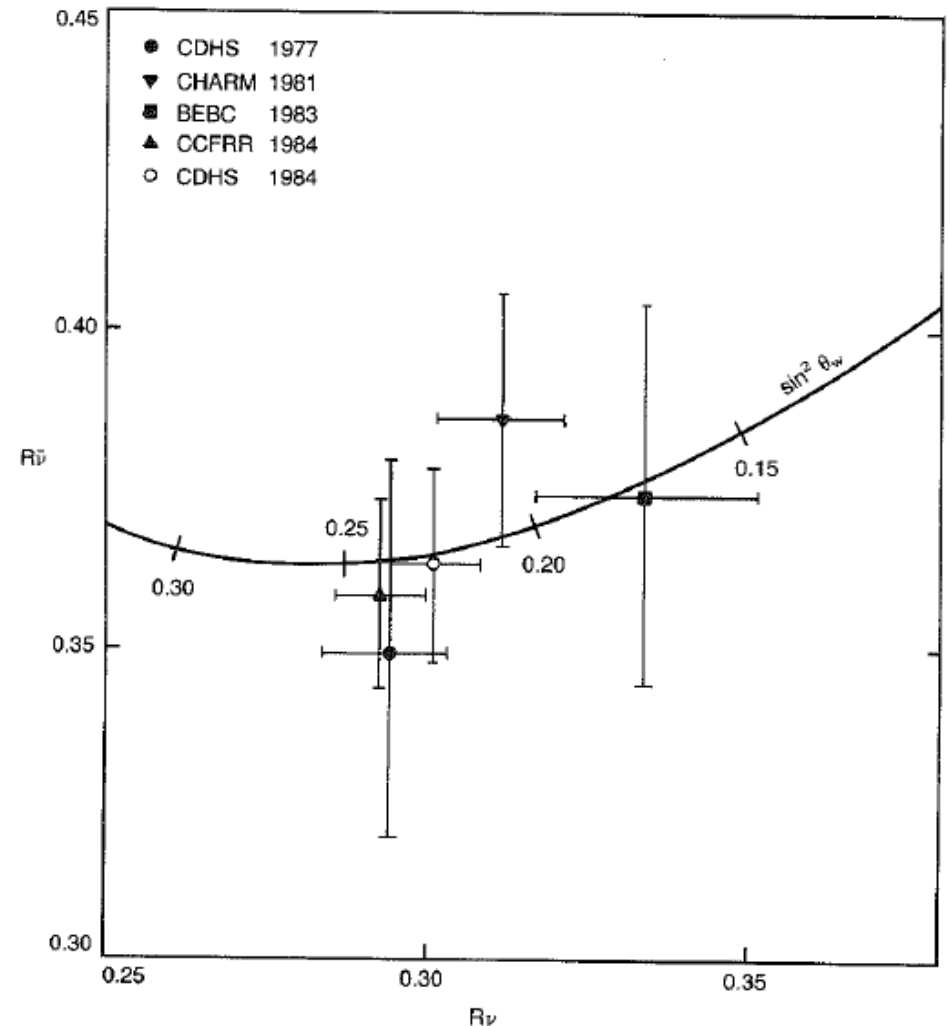
$$\frac{d^2\sigma^{\bar{\nu} N(\text{CC})}}{dx dy} = \frac{G^2 M E x}{2\pi} [u(x) + d(x)](1 - y)^2.$$

$$R = \frac{\sigma^{\nu N(\text{NC})}}{\sigma^{\nu N(\text{CC})}} = \frac{1}{2} - \sin^2 \theta_w + \frac{20}{27} \sin^4 \theta_w,$$

$$\bar{R} = \frac{\sigma^{\bar{\nu} N(\text{NC})}}{\sigma^{\bar{\nu} N(\text{CC})}} = \frac{1}{2} - \sin^2 \theta_w + \frac{20}{9} \sin^4 \theta_w.$$

Geweniger 1984:

$$\sin^2 \theta_w = 0.223 \pm 0.010$$



Lorentz Invariant Kinematics of the Deep Inelastic Scattering Process

The virtuality of the exchanged photon is given by:

$$Q^2 = -q^2 = -(p - p')^2$$

$$\propto \frac{1}{\sin^4 \theta / 2}$$

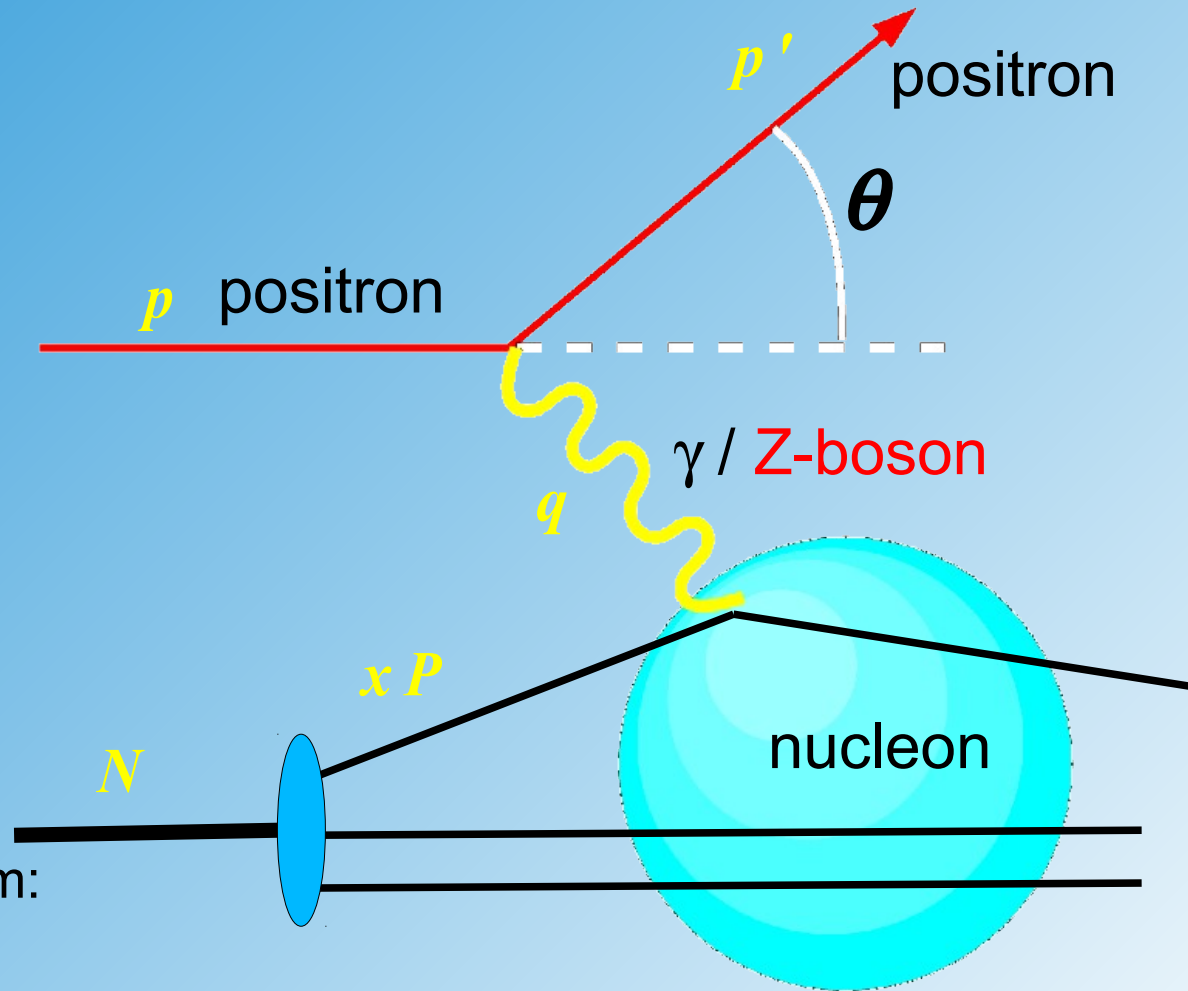
Relative energy loss (inelasticity):

$$y = \frac{\nu}{E_\nu} = \frac{q P}{p P}$$

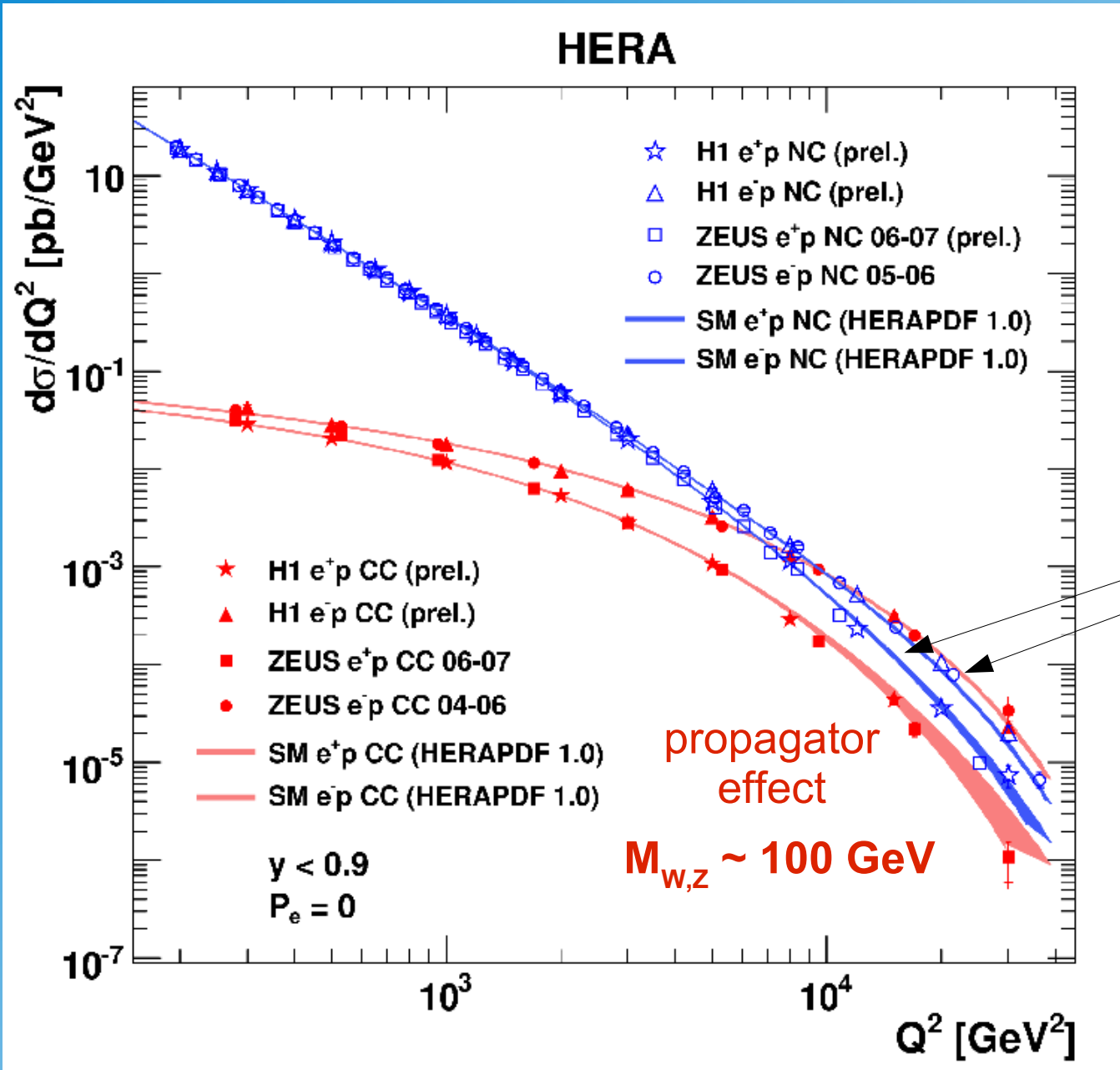
relative fraction of parton momentum:

$$x = \frac{q^2}{2qP} = \frac{Q^2}{S y}$$

with cms energy: $S = 2pP$



HERA NC (CC) Cross Sections



Difference between e⁺p and e⁻p cross section due to electroweak (c_V, c_A) Z-boson couplings

DIS Structure Functions at HERA

Deep Inelastic Scattering for $e^\pm p$ described by:

$$\frac{d^2\sigma_{\text{NC}}^\pm}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} (Y_+ \tilde{F}_2 \mp Y_- x \tilde{F}_3 - y^2 \tilde{F}_L)$$

Generalised functions \tilde{F}_2 and \tilde{F}_3 :

$$\begin{aligned} \tilde{F}_2^\pm &= F_2 - (v_e \pm P_e a_e) \kappa \frac{Q^2}{Q^2 + M_Z^2} F_2^{\gamma Z} + (v_e^2 + a_e^2 \pm P_e 2v_e a_e) \kappa^2 \left[\frac{Q^2}{Q^2 + M_Z^2} \right]^2 F_2^Z \\ x \tilde{F}_3^\pm &= -(a_e \pm P_e v_e) \kappa \frac{Q^2}{Q^2 + M_Z^2} x F_3^{\gamma Z} + (2a_e v_e \pm P_e [v_e^2 + a_e^2]) \kappa^2 \left[\frac{Q^2}{Q^2 + M_Z^2} \right]^2 x F_3^Z \end{aligned}$$

Structure Functions F_2 and F_3 :

with $\kappa^{-1} = 4 \frac{M_W^2}{M_Z^2} \left(1 - \frac{M_W^2}{M_Z^2}\right)$

$$\begin{aligned} [F_2, F_2^{\gamma Z}, F_2^Z] &= x \sum_q [e_q^2, 2e_q v_q, v_q^2 + a_q^2] (q + \bar{q}) \\ [x F_3^{\gamma Z}, x F_3^Z] &= 2x \sum_q [e_q a_q, v_q a_q] (q - \bar{q}), \end{aligned}$$

Summary

- Neutral Currents = Virtual exchange of Z-boson discovered with the Gargamelle experiment in 1973
- Electroweak Symmetry Breaking:
 - Triplet field \mathbf{W} couples to left handed particles (V-A)
 - Singlet field B couples to hypercharge
 - parity violation fields W_3 and B are broken into Z and A field
 - The Photon field is massless and parity conserving (V-coupling)
 - The Z-field has V and A couplings depending on fermion type
- Electroweak Symmetry Breaking needs Higgs field to explain masses of W and Z particles
$$m_Z = \frac{m_W}{\cos \theta_W} \sim 90 \text{ GeV}$$
- Masses of W and Z particles $\sim 100 \text{ GeV}$, precise determination in resonant production (LEP \rightarrow Wednesday)

