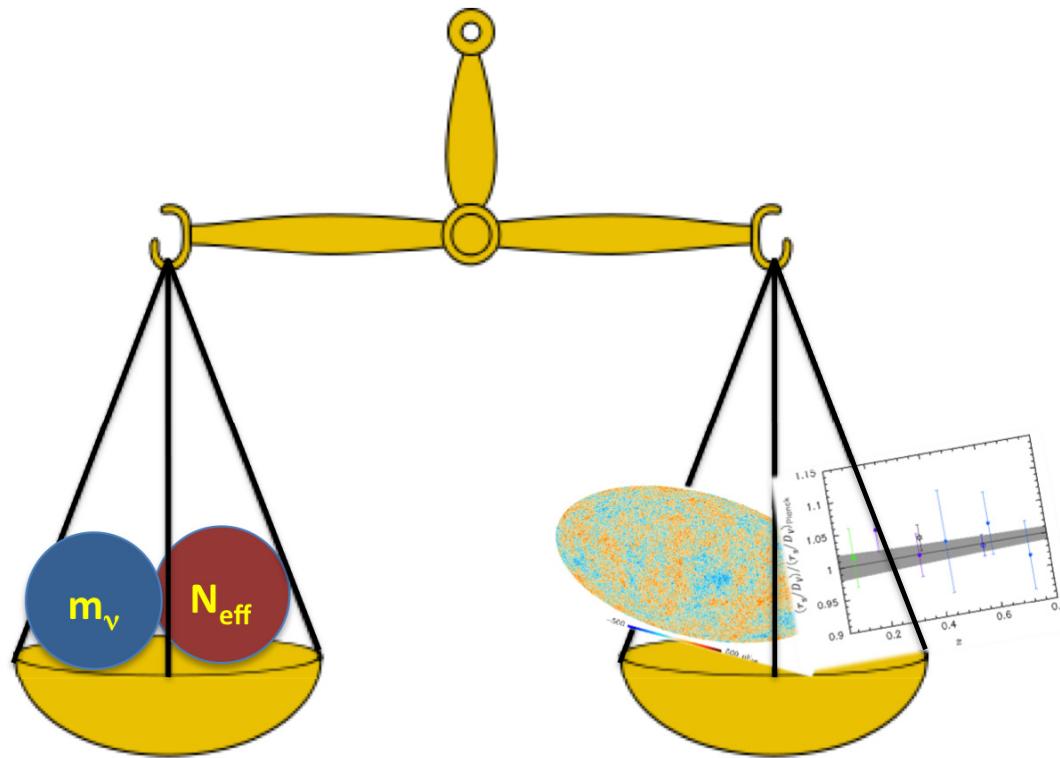


Neutrino properties from cosmological observables after Planck

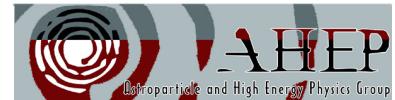


UNIVERSITAT
DE
VALÈNCIA

Sergio Pastor
(IFIC Valencia)

Max-Planck-Institut für Kernphysik
17 June 2013

 **CSIC**
CONSEJO SUPERIOR DE INVESTIGACIONES CIENTÍFICAS


MHEP
Leptoparticle and High Energy Physics Group

Outline



**Introduction: the Cosmic
Neutrino Background**

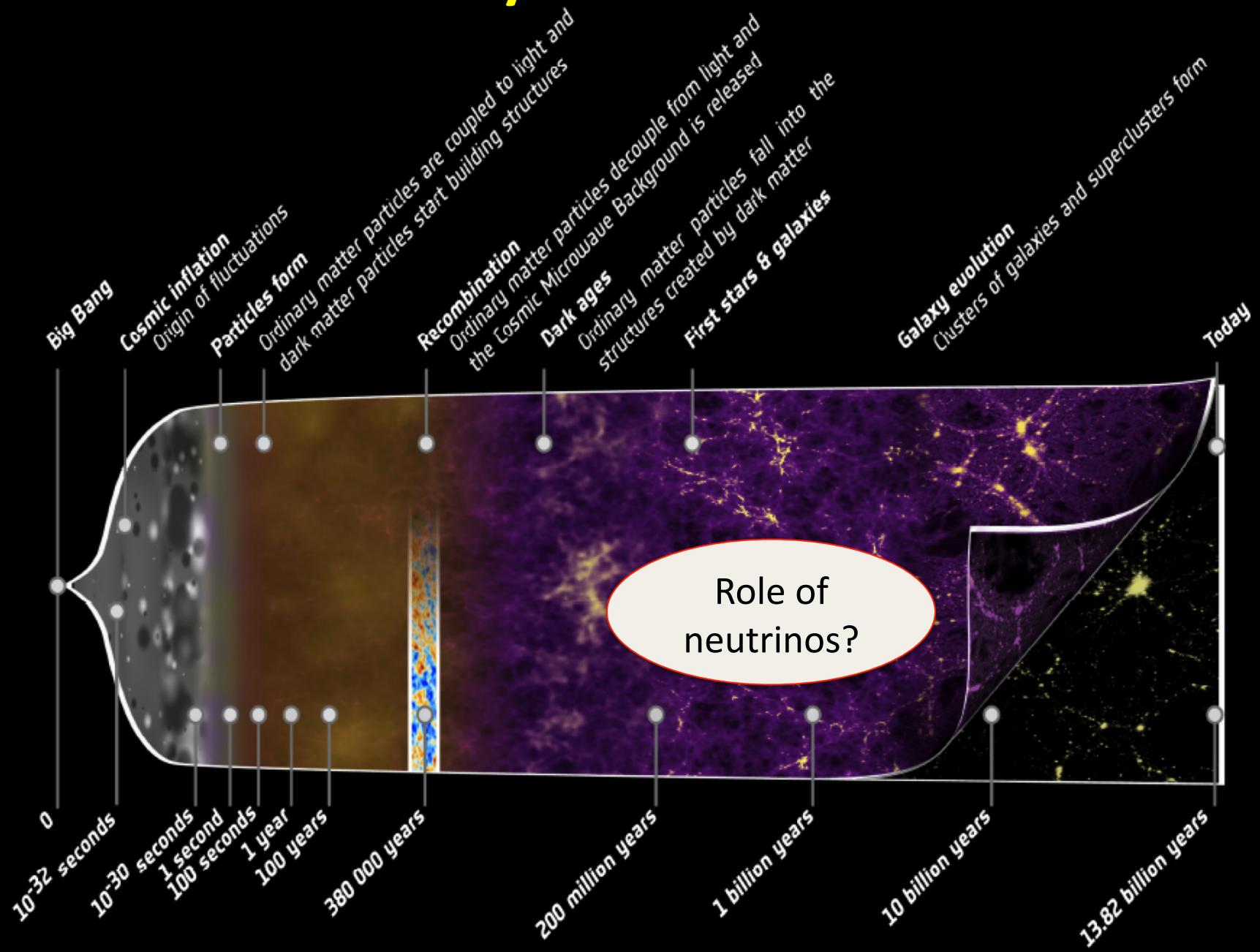
Neutrinos as Dark Matter

**The radiation content
of the Universe (N_{eff})**

**Bounds on neutrino properties from
Planck (& other cosmo data)**

Introduction: the Cosmic Neutrino Background

History of the Universe



History of the Universe

This is a neutrino!

Accelerators:

- CERN-LHC
- FNAL-Tevatron
- BNL-RHIC
- CERN-LEP
- SLAC-SLC

high-energy cosmic rays

BIG BANG

Inflation

$t = 10^{-44}$	$T = 10^{32}$	$E = 10^{19}$
$t = 10^{-37} s$	$T = 10^{28}$	$E = 10^{15}$

possible dark matter
relics

$t = 10^{-10} s$

$t = 10^{-5} s$

$t = 10^{-1} s$

$t = 10^2 s$

$t = 10^9 s$

$t = 3 \times 10^5 y$

$t = 3000 y$

$t = 10^9 y$

$t = 15 y$

$t = 10^{-12} s$

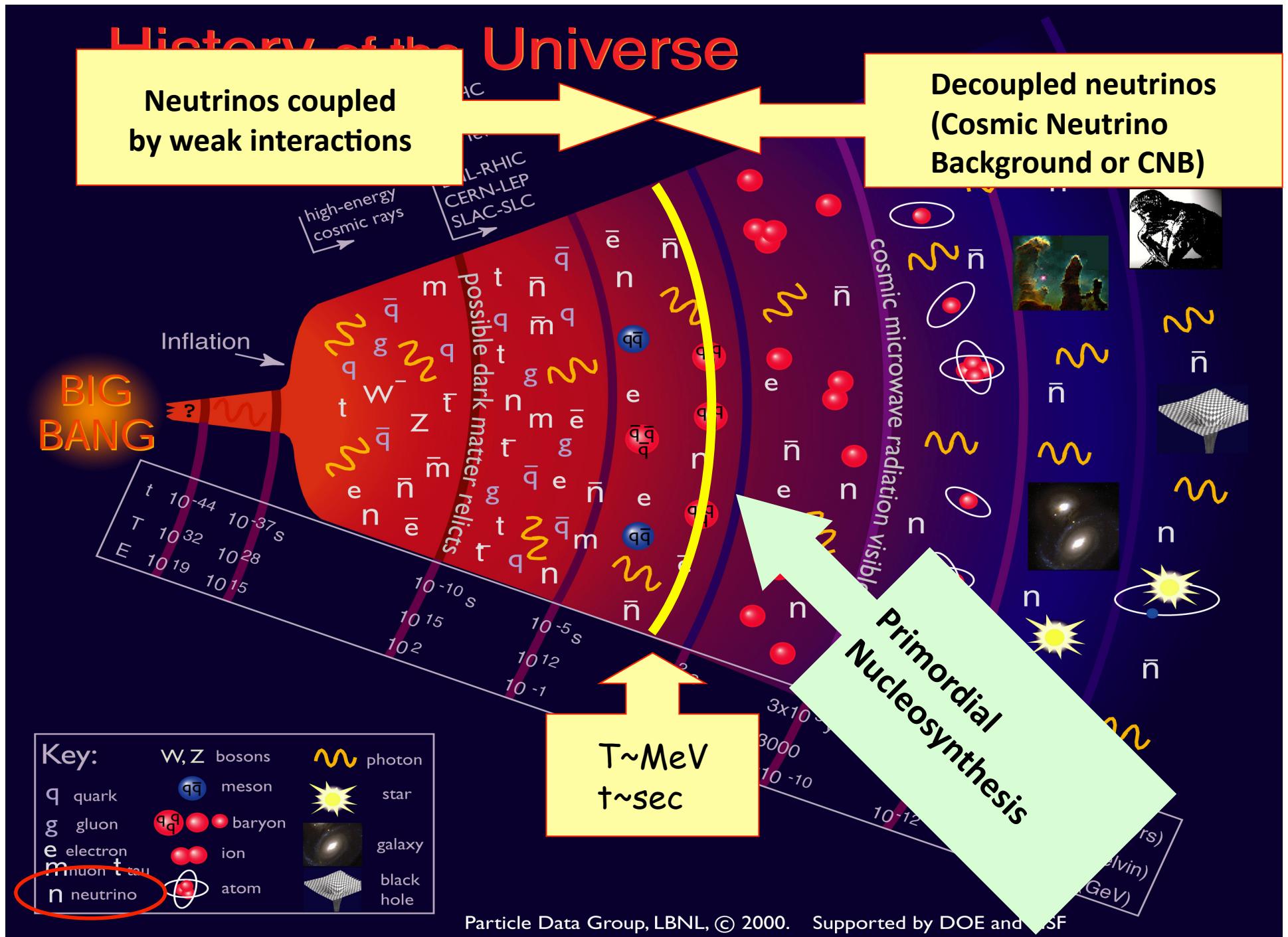
$t = 2.7 y$

$t = 12 \times 10^9 y$ (sec, yrs)

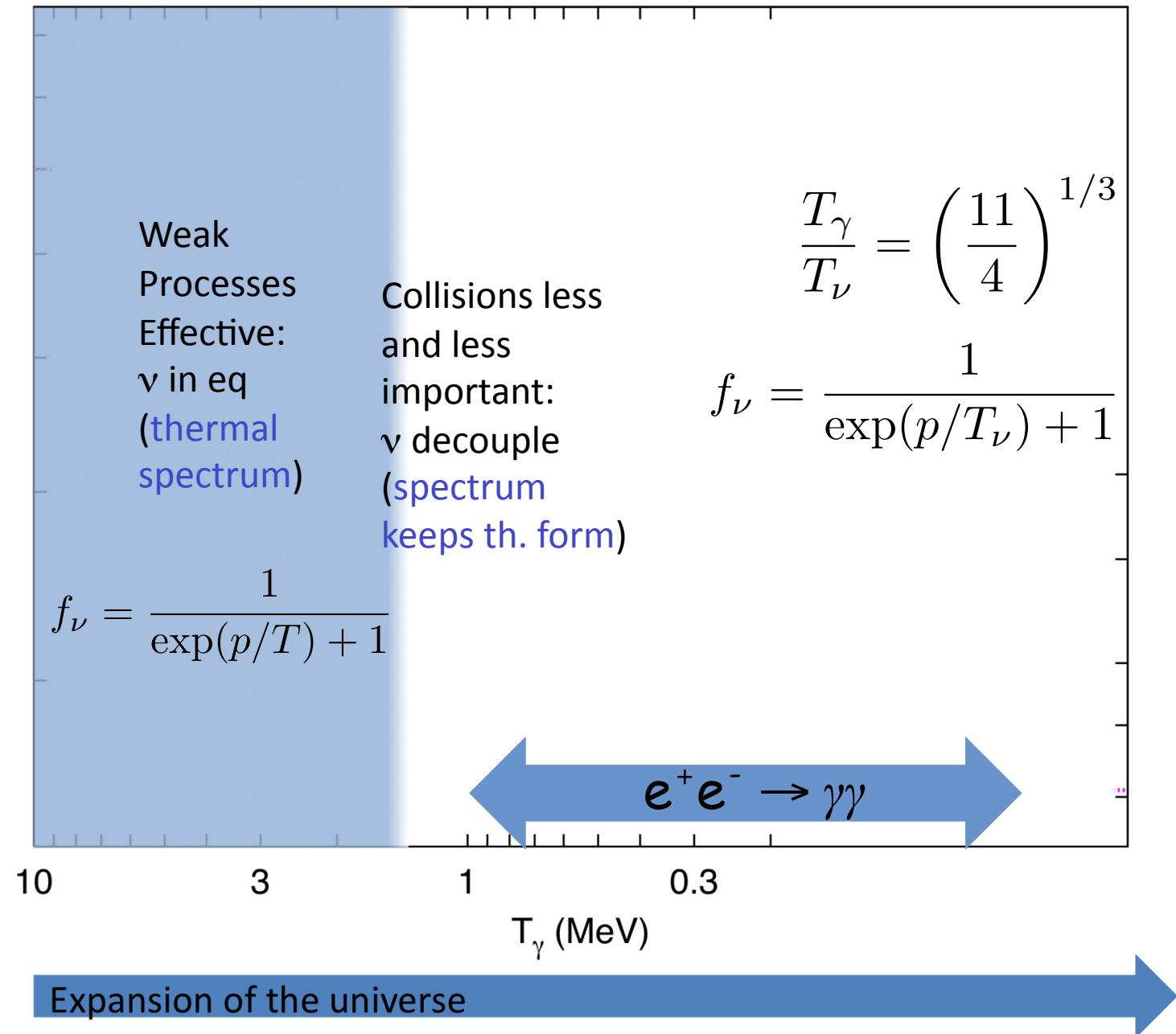
$T = 2.7$ (Kelvin)

$T = 2.3 \times 10^{-13}$ (GeV)

Key:	
q quark	W, Z bosons
g gluon	$\bar{q}q$ meson
e electron	baryon
m muon	ion
n neutrino	atom
	photon
	star
	galaxy
	black hole



ν Decoupling and e^\pm annihilations

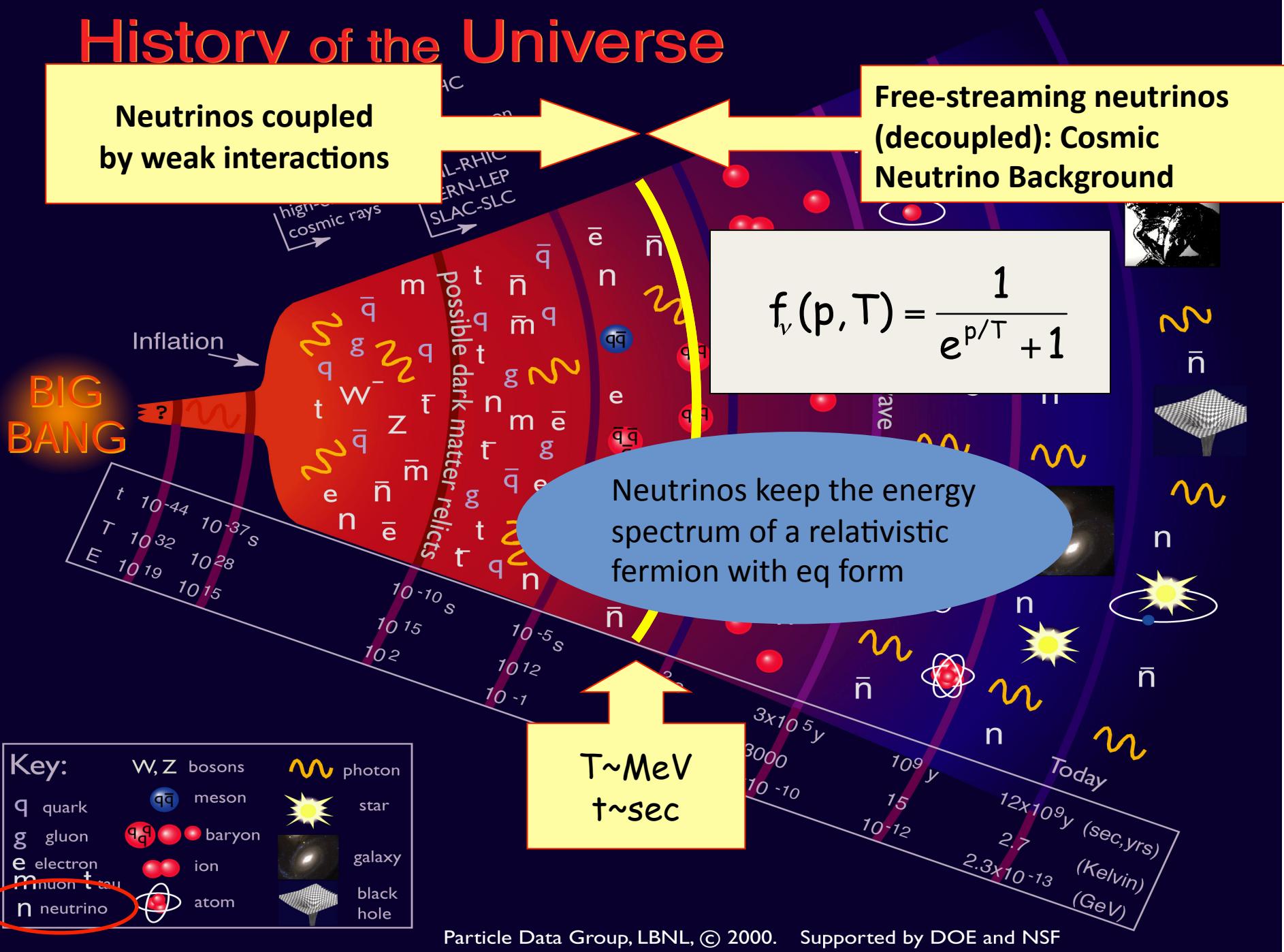


History of the Universe

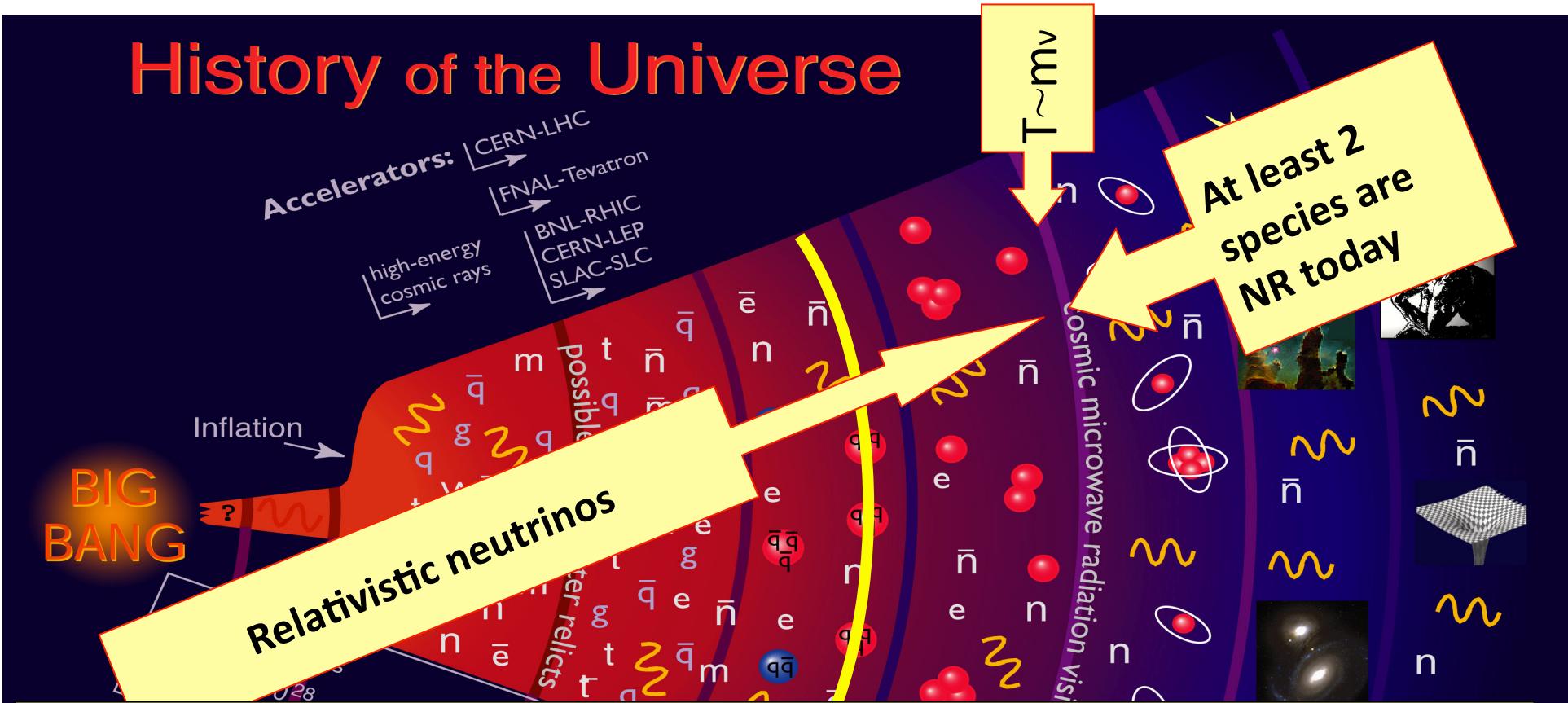
Neutrinos coupled by weak interactions

Free-streaming neutrinos (decoupled): Cosmic Neutrino Background

$$f_\nu(p, T) = \frac{1}{e^{p/T} + 1}$$



History of the Universe



Neutrino cosmology is interesting because Relic neutrinos are very abundant:

- The CNB contributes to **radiation at early times** and to matter at late times (info on the number of neutrinos and their masses)
- Cosmological observables can be used to **test standard or non-standard neutrino properties**



The Cosmic Neutrino Background

Neutrinos decoupled at $T \sim \text{MeV}$, keeping a spectrum as that of a relativistic species

$$f_\nu(p, T) = \frac{1}{e^{p/T_\nu} + 1}$$

- Number density

$$n_\nu = \int \frac{d^3 p}{(2\pi)^3} f_\nu(p, T_\nu) = \frac{3}{11} n_\gamma = \frac{6\zeta(3)}{11\pi^2} T_{CMB}^3$$

- Energy density

$$\rho_{\nu_i} = \int \sqrt{p^2 + m_{\nu_i}^2} \frac{d^3 p}{(2\pi)^3} f_\nu(p, T_\nu) \rightarrow \frac{7\pi^2}{120} \left(\frac{4}{11}\right)^{4/3} T_{CMB}^4 \quad \text{Massless}$$

The Cosmic Neutrino Background

Neutrinos decoupled at $T \sim \text{MeV}$, keeping a spectrum as that of a relativistic species

$$f_\nu(p, T) = \frac{1}{e^{p/T_\nu} + 1}$$

- Number density

At present $112 (\nu + \bar{\nu}) \text{ cm}^{-3}$ per flavour

- Energy density

Contribution to the energy density of the Universe

$$\Omega_\nu h^2 \simeq 1.7 \times 10^{-5} \text{ Massless} \quad \Omega_i = \rho_i / \rho_{\text{crit}}$$

The Cosmic Neutrino Background

Neutrinos decoupled at $T \sim \text{MeV}$, keeping a spectrum as that of a relativistic species

$$f_\nu(p, T) = \frac{1}{e^{p/T_\nu} + 1}$$

- Number density

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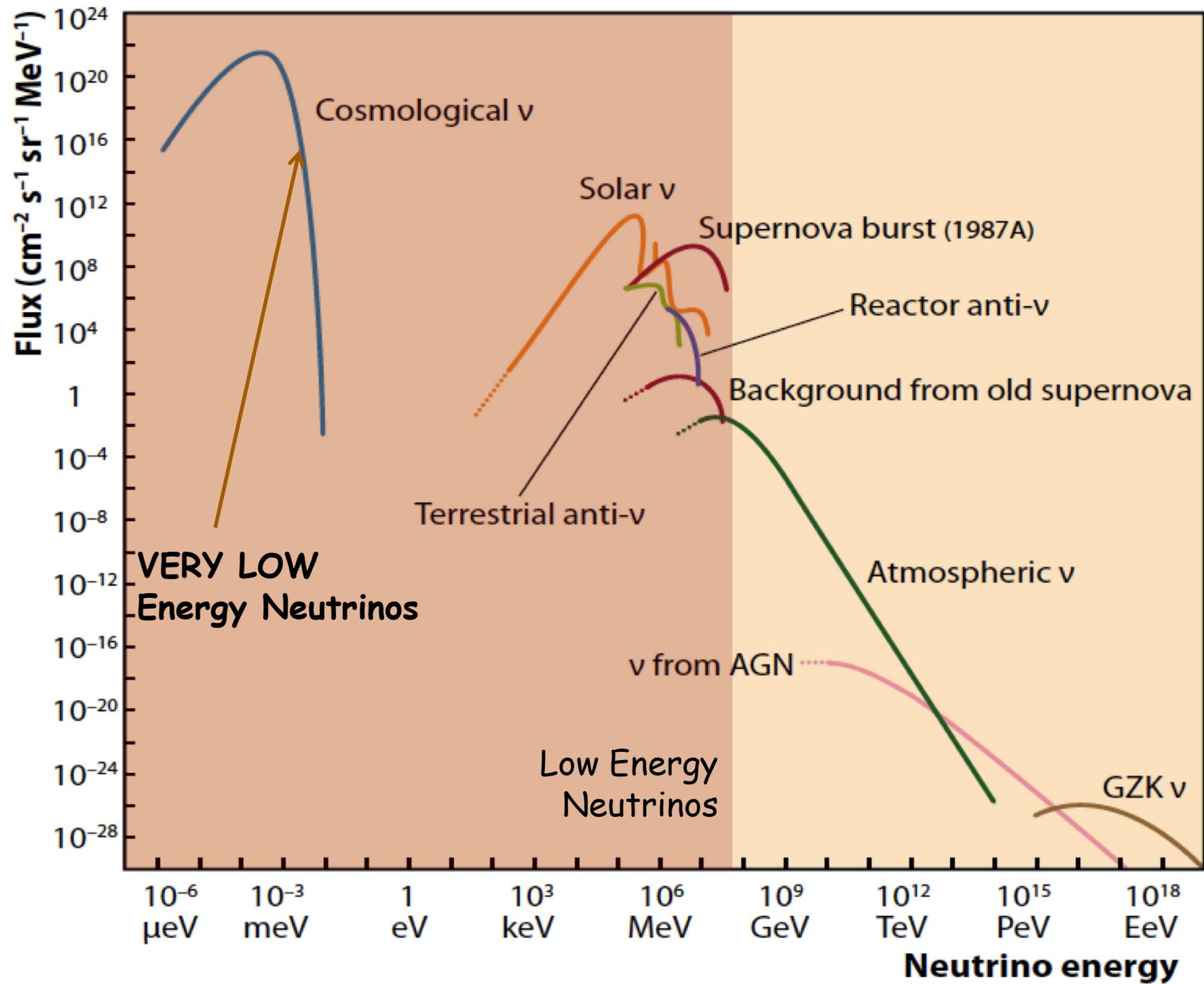
- Energy density

$$\Omega_\nu h^2 \simeq 1.7 \times 10^{-5} \quad \text{Massless}$$

Contribution to the energy density of the Universe

$$\Omega_\nu h^2 = \frac{\sum_i m_{\nu_i}}{94.1 \text{ eV}}$$

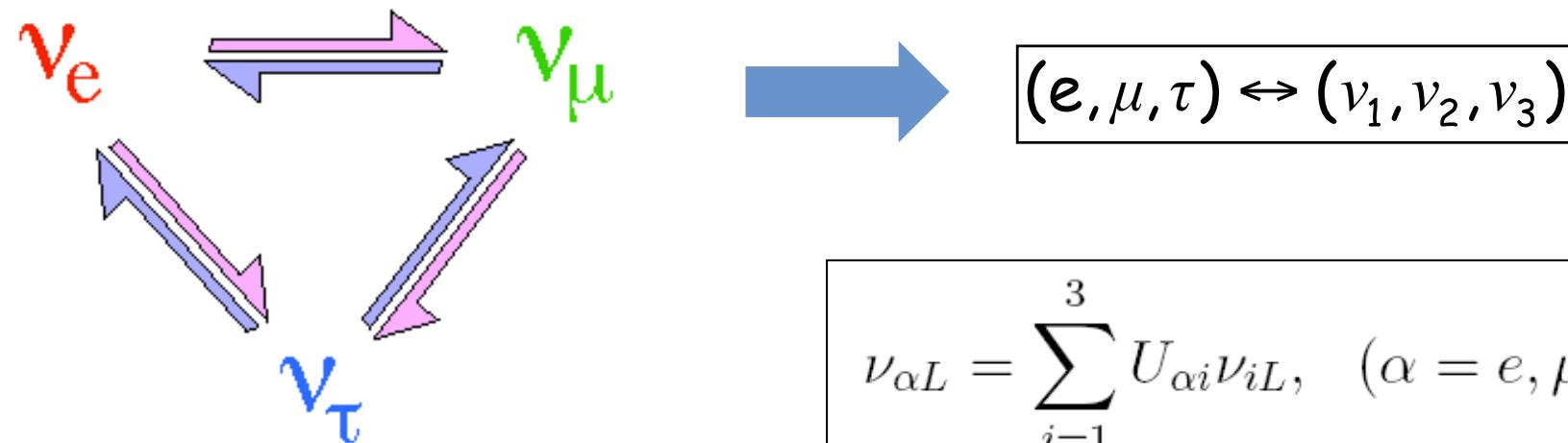
Massive
 $m_\nu \gg T$



Neutrinos as Dark Matter

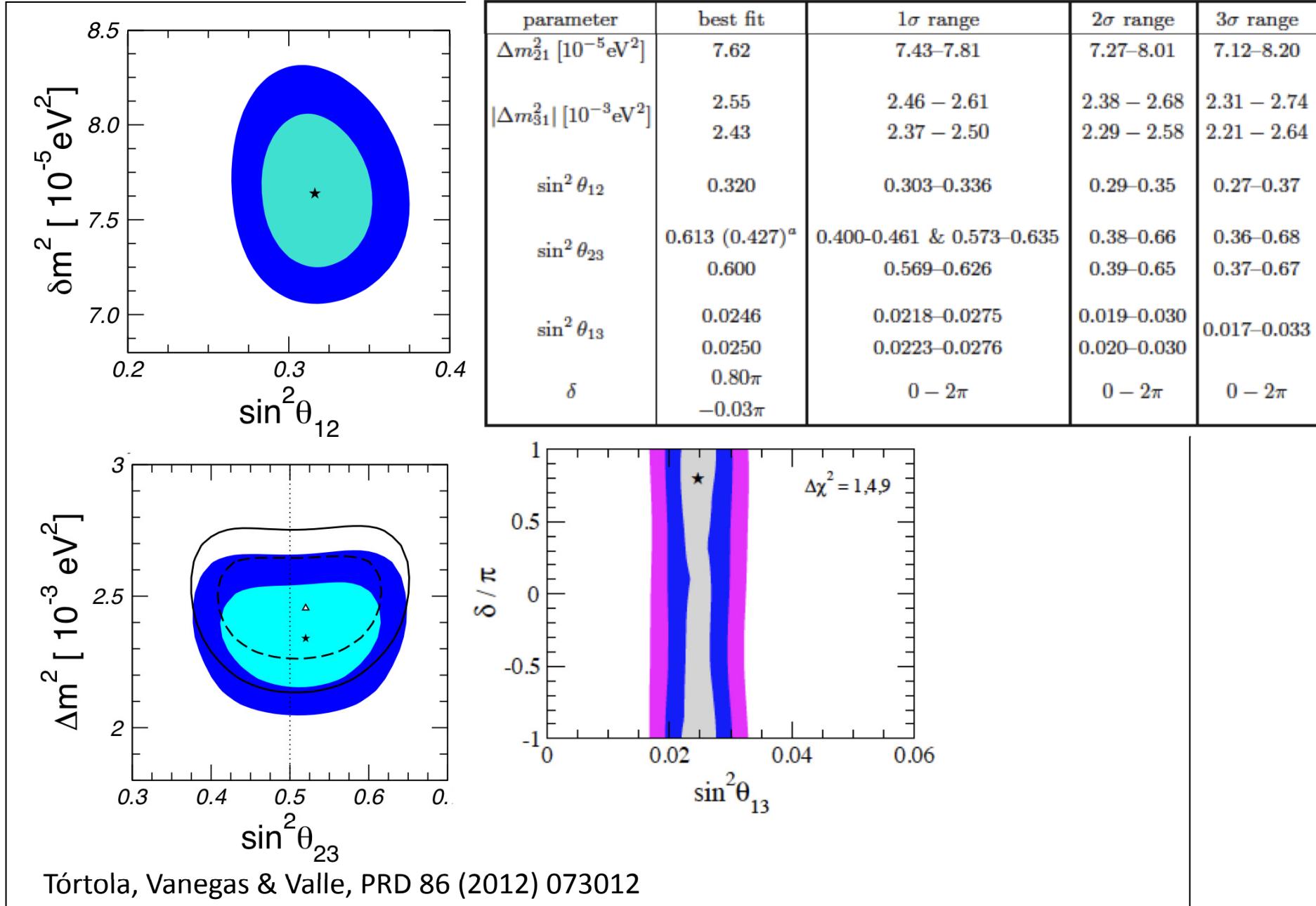
We know that flavour neutrino oscillations exist

From present evidences of oscillations from experiments measuring atmospheric, solar, reactor and accelerator neutrinos



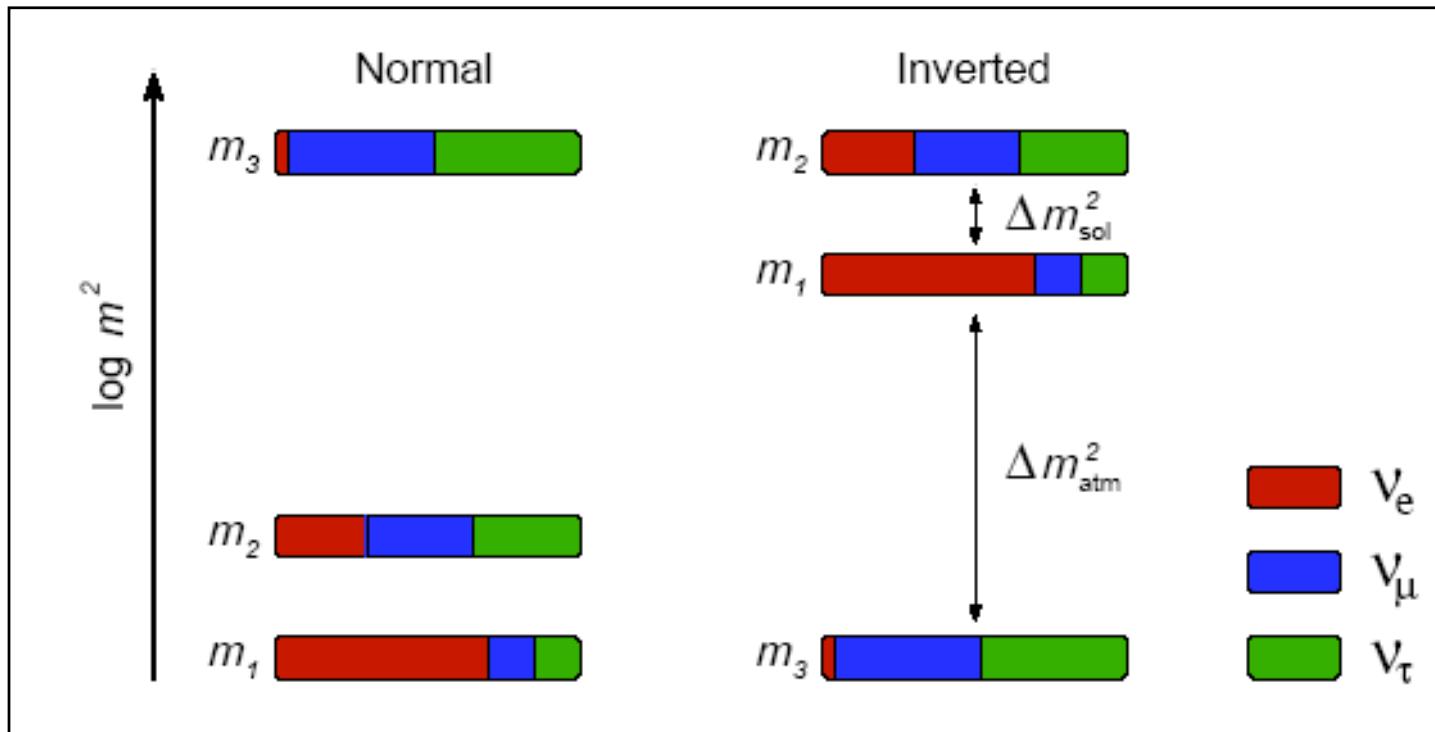
$$\nu_{\alpha L} = \sum_{i=1}^3 U_{\alpha i} \nu_{iL}, \quad (\alpha = e, \mu, \tau)$$

$$\begin{matrix} & \nu_1 & \nu_2 & \nu_3 \\ \nu_e & c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ \nu_\mu & -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ \nu_\tau & s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{matrix} \times \text{diag}(e^{i\alpha_1/2}, e^{i\alpha_2/2}, 1).$$



see also Fogli et al, 86 (2012) 073012; González-García et al, JHEP 1212 (2012) 123

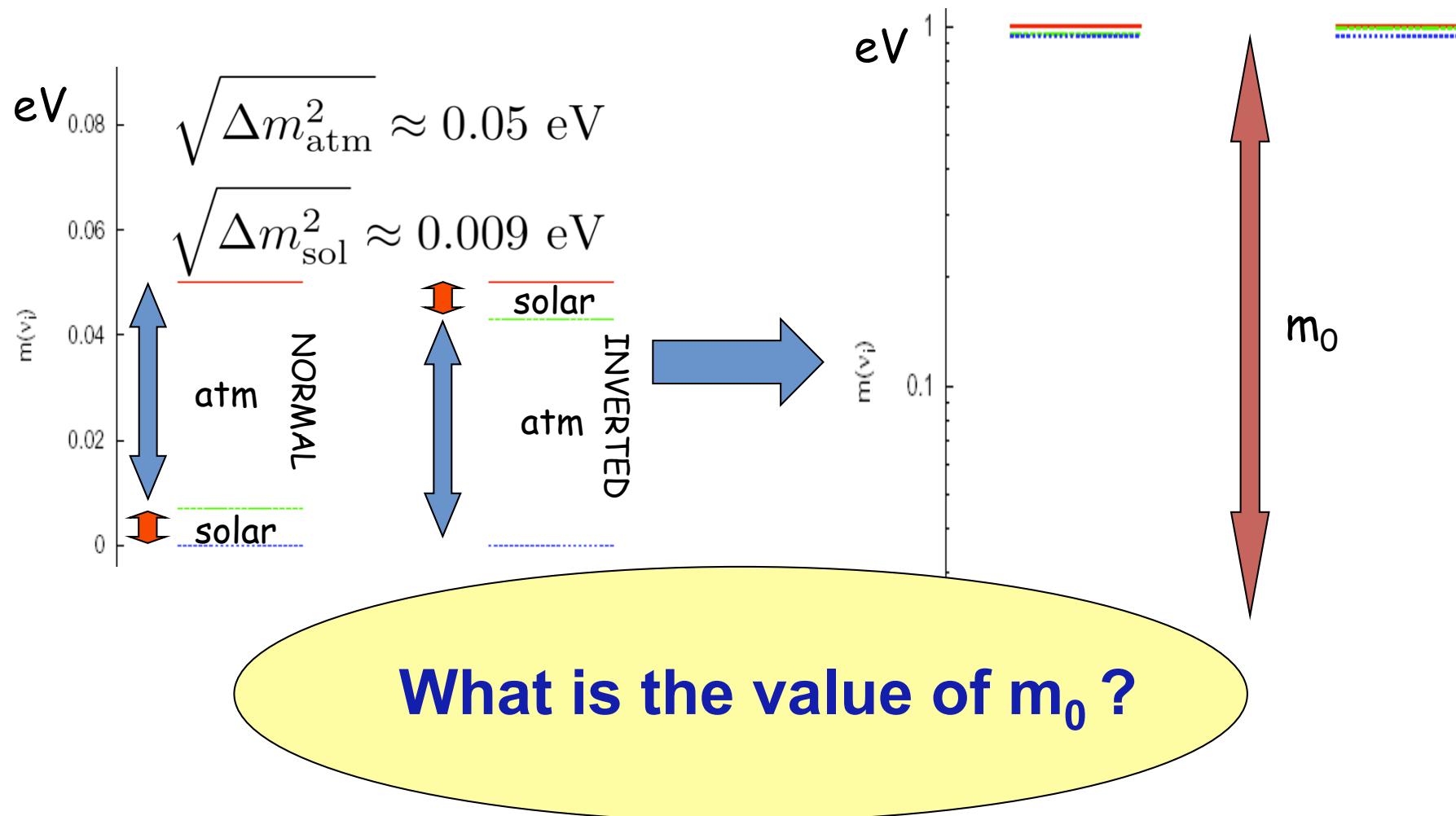
Neutrino masses



$$\nu_{\alpha L} = \sum_{i=1}^3 U_{\alpha i} \nu_{iL}, \quad (\alpha = e, \mu, \tau)$$

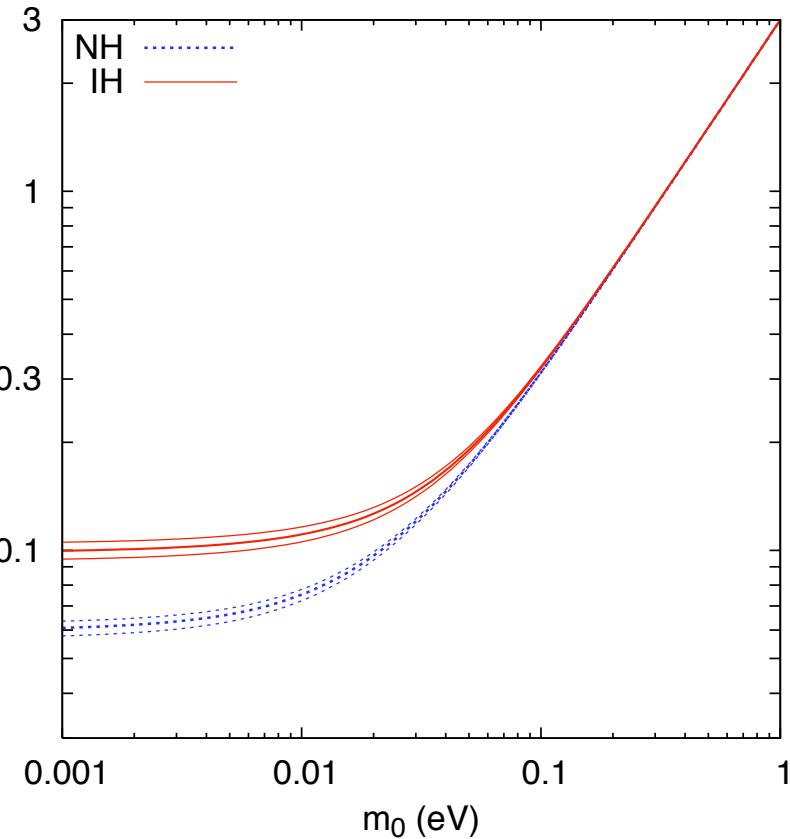
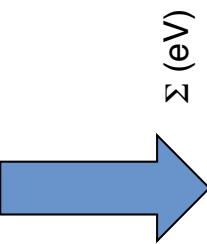
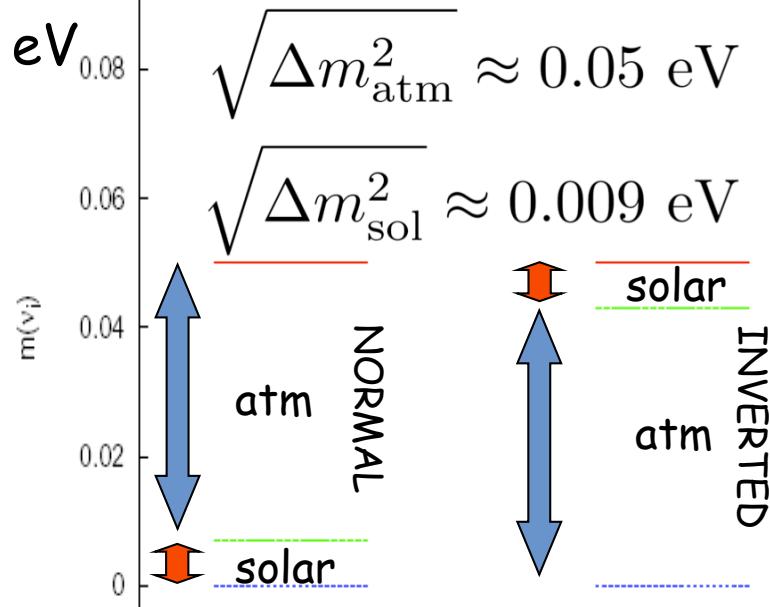
Neutrino masses

Data on flavour oscillations do not fix the absolute scale of neutrino masses



Neutrino masses

Data on flavour oscillations do not fix the absolute scale of neutrino masses



$$0.06(0.1) \text{ eV} \lesssim \sum_i m_i \lesssim 6 \text{ eV}$$

The Cosmic Neutrino Background

Neutrinos decoupled at $T \sim \text{MeV}$, keeping a spectrum as that of a relativistic species

$$f_\nu(p, T) = \frac{1}{e^{p/T_\nu} + 1}$$

- Number density

At present $112 (\nu + \bar{\nu}) \text{ cm}^{-3}$ per flavour

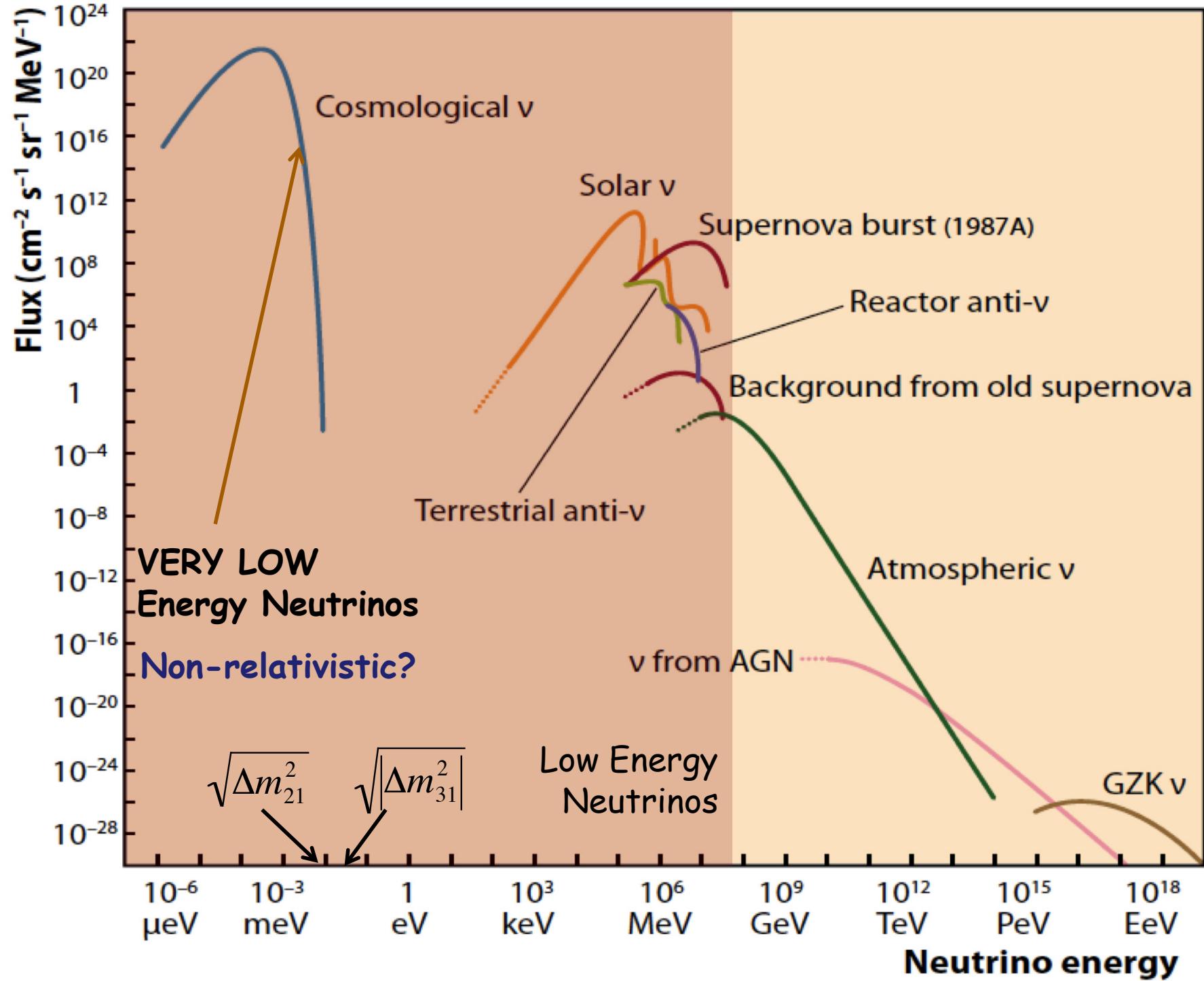
- Energy density

$$\Omega_\nu h^2 \simeq 1.7 \times 10^{-5} \quad \text{Massless}$$

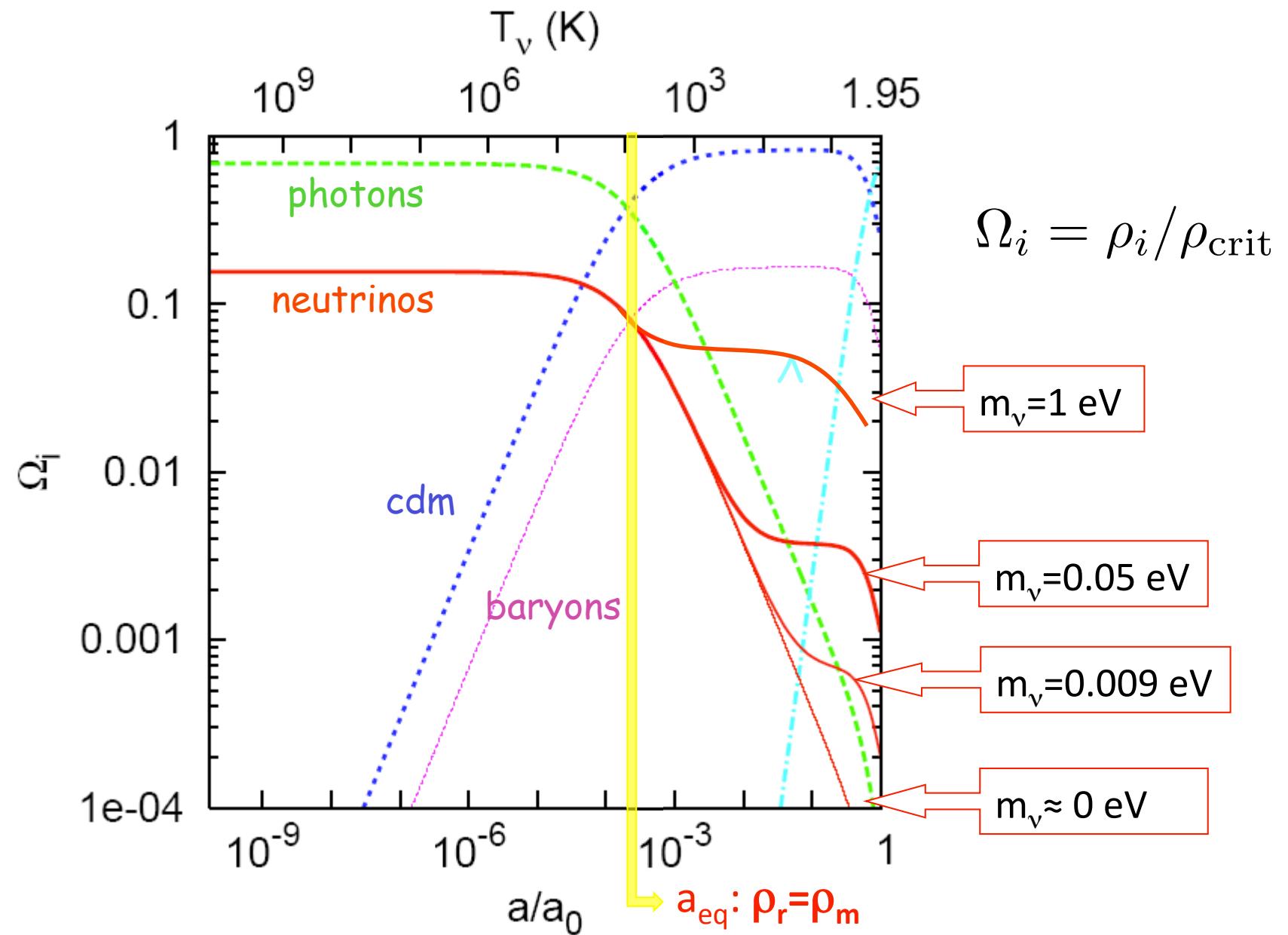
Contribution to the energy density of the Universe

$$\Omega_\nu h^2 = \frac{\sum_i m_{\nu_i}}{94.1 \text{ eV}}$$

Massive
 $m_\nu \gg T$



Evolution of the background densities: 1 MeV → now



Neutrinos as Dark Matter

- Neutrinos are natural **DM candidates**

$$\Omega_\nu h^2 = \frac{\sum_i m_i}{93.2 \text{ eV}} \quad \Omega_\nu < 1 \rightarrow \sum_i m_i \lesssim 46 \text{ eV}$$

$$\Omega_\nu < \Omega_m \simeq 0.3 \rightarrow \sum_i m_i \lesssim 15 \text{ eV}$$

- They stream freely until non-relativistic (collisionless phase mixing) 
Neutrinos are HOT Dark Matter (large thermal motion)
- First structures to be formed when Universe became matter –dominated are very large
- Ruled out by structure formation  CDM

The radiation content of the Universe (Neff)

Relativistic particles in the Universe

At $T < m_e$, the radiation content of the Universe is

$$\rho_r = \rho_\gamma + \rho_\nu + \rho_x = \left[1 + \frac{7}{8} \left(\frac{4}{11} \right)^{4/3} N_{\text{eff}} \right] \rho_\gamma$$

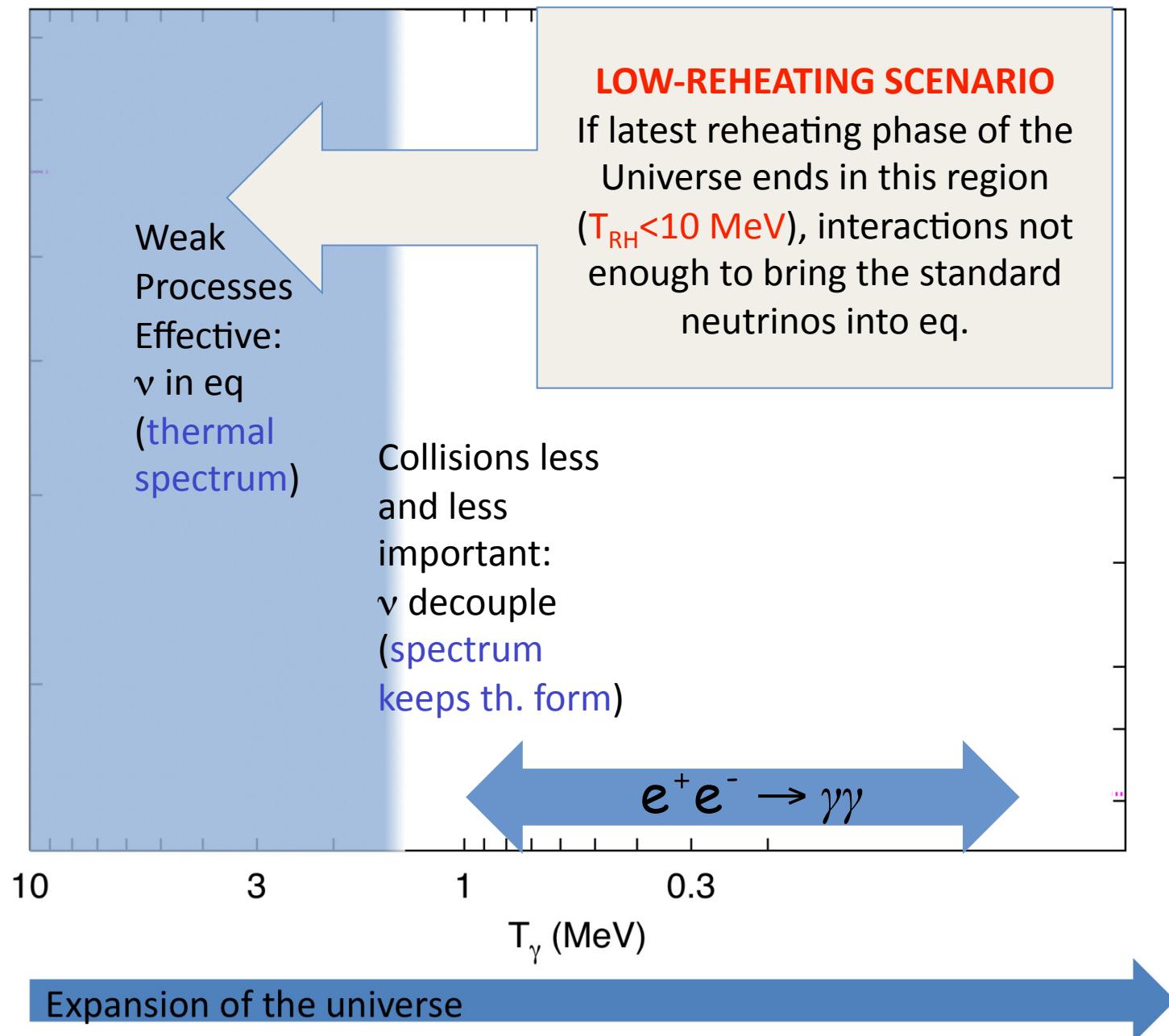
Effective number of relativistic neutrino species

Traditional parametrization of ρ stored in relativistic particles

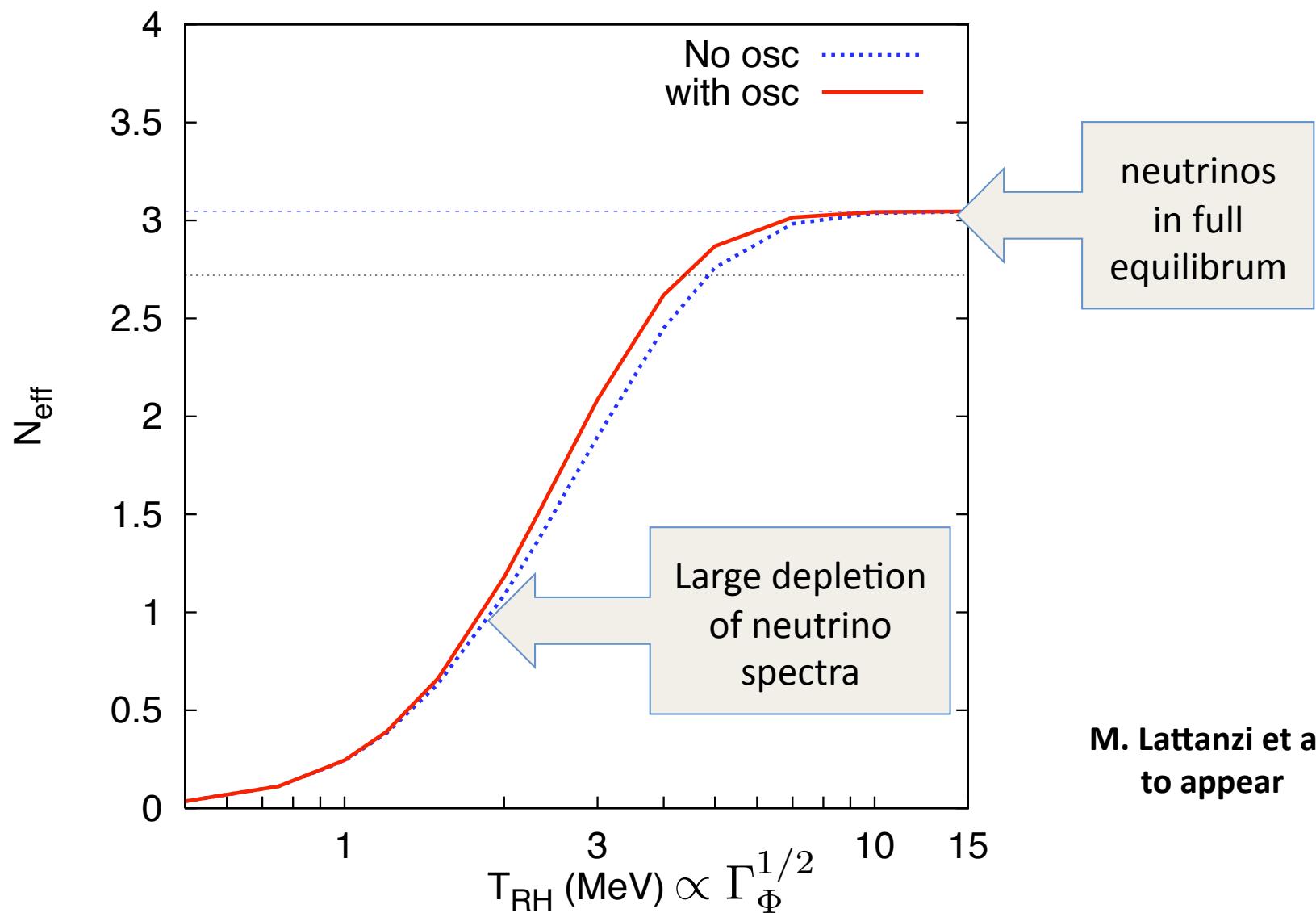
N_{eff} is a way to measure the ratio $\frac{\rho_\nu + \rho_x}{\rho_\gamma}$

- standard neutrinos only: $N_{\text{eff}} \simeq 3$ (3.046)
- $N_{\text{eff}} > 3$ (delays equality time) from additional relativistic particles (scalars, pseudoscalars, decay products of heavy particles,...) or non-standard neutrino physics (primordial neutrino asymmetries, totally or partially thermalized light sterile neutrinos, non-standard interactions with electrons,...)

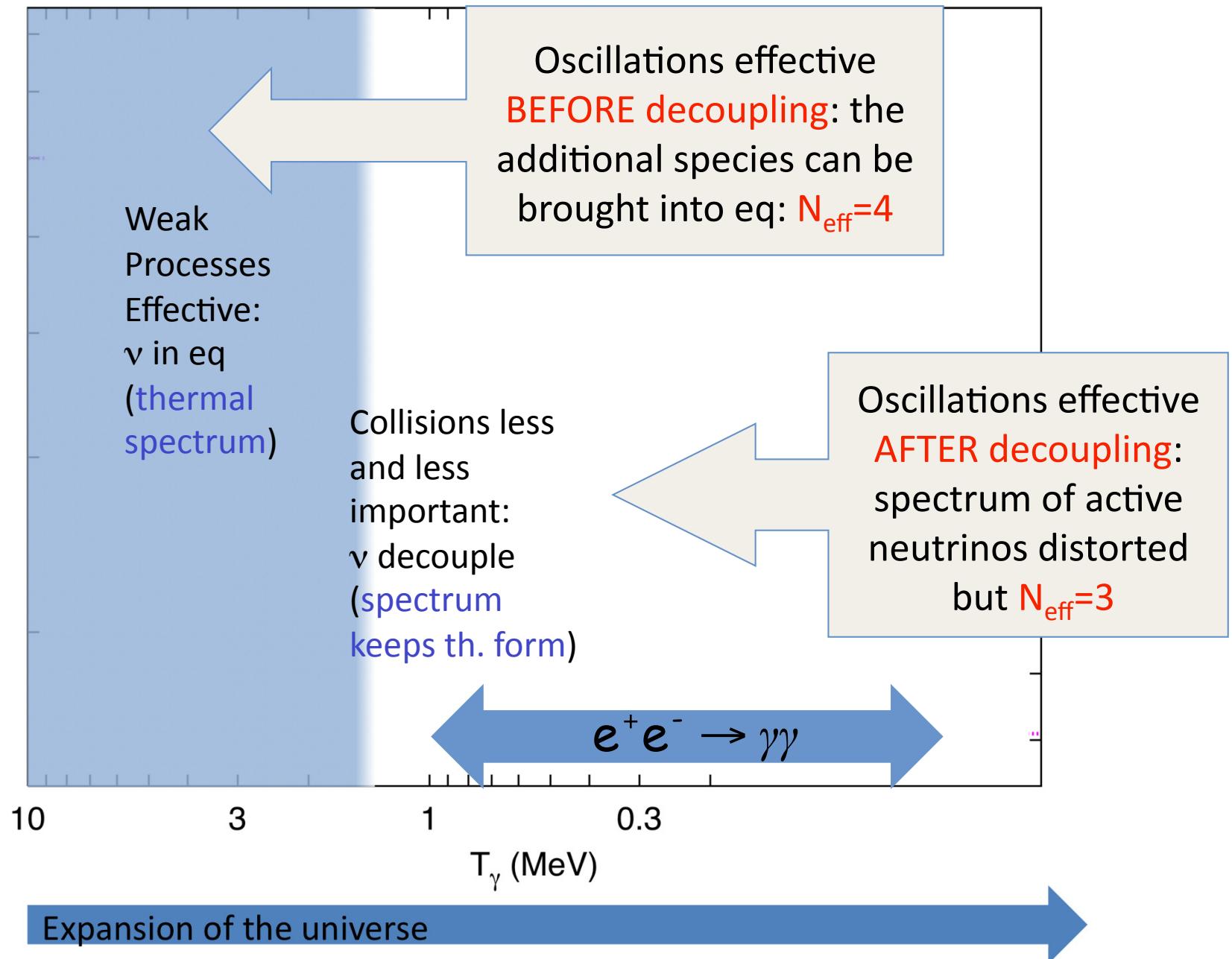
Neff < 3 ?



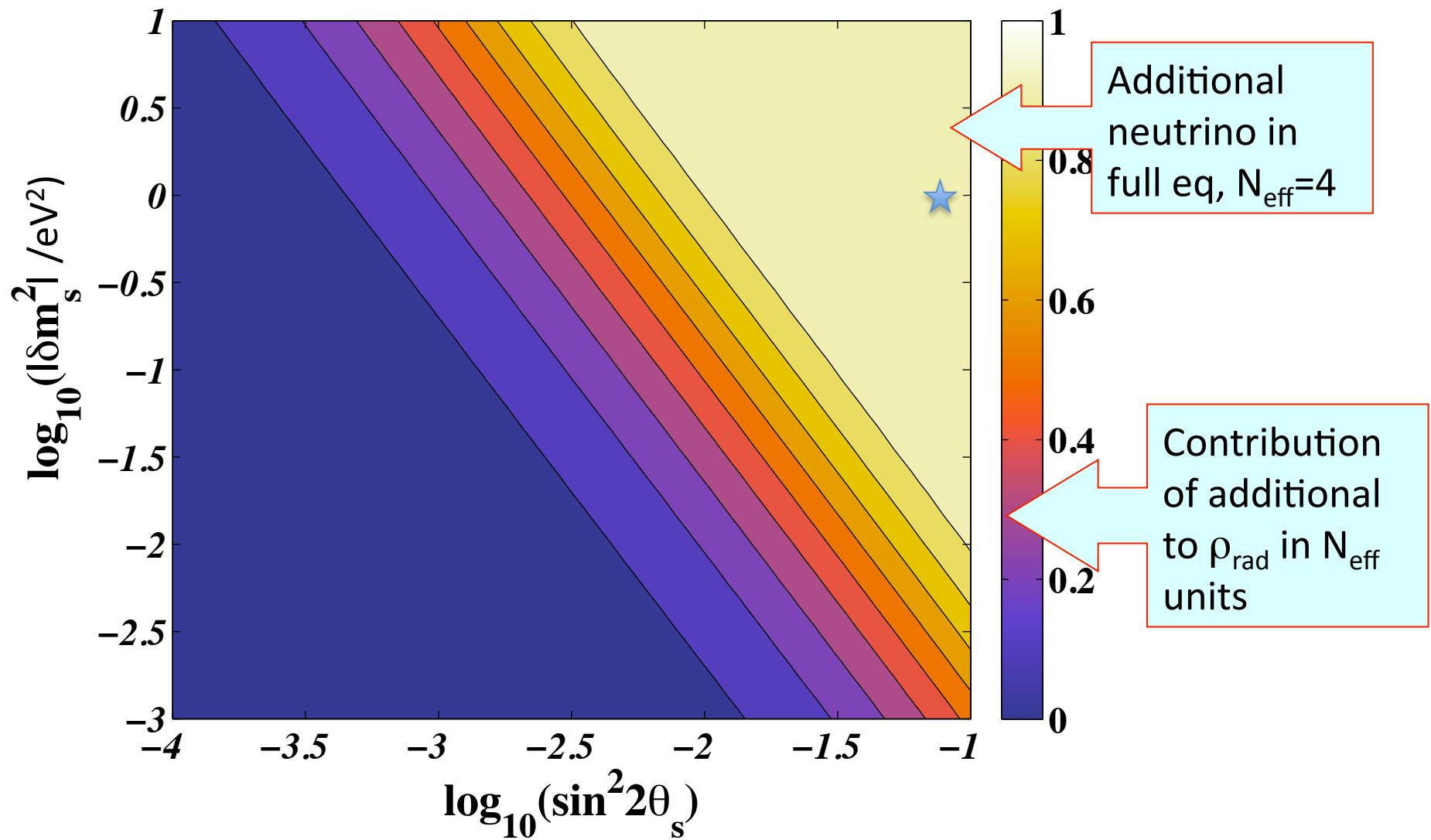
Neff < 3 ?



Neff & Active-sterile neutrino oscillations



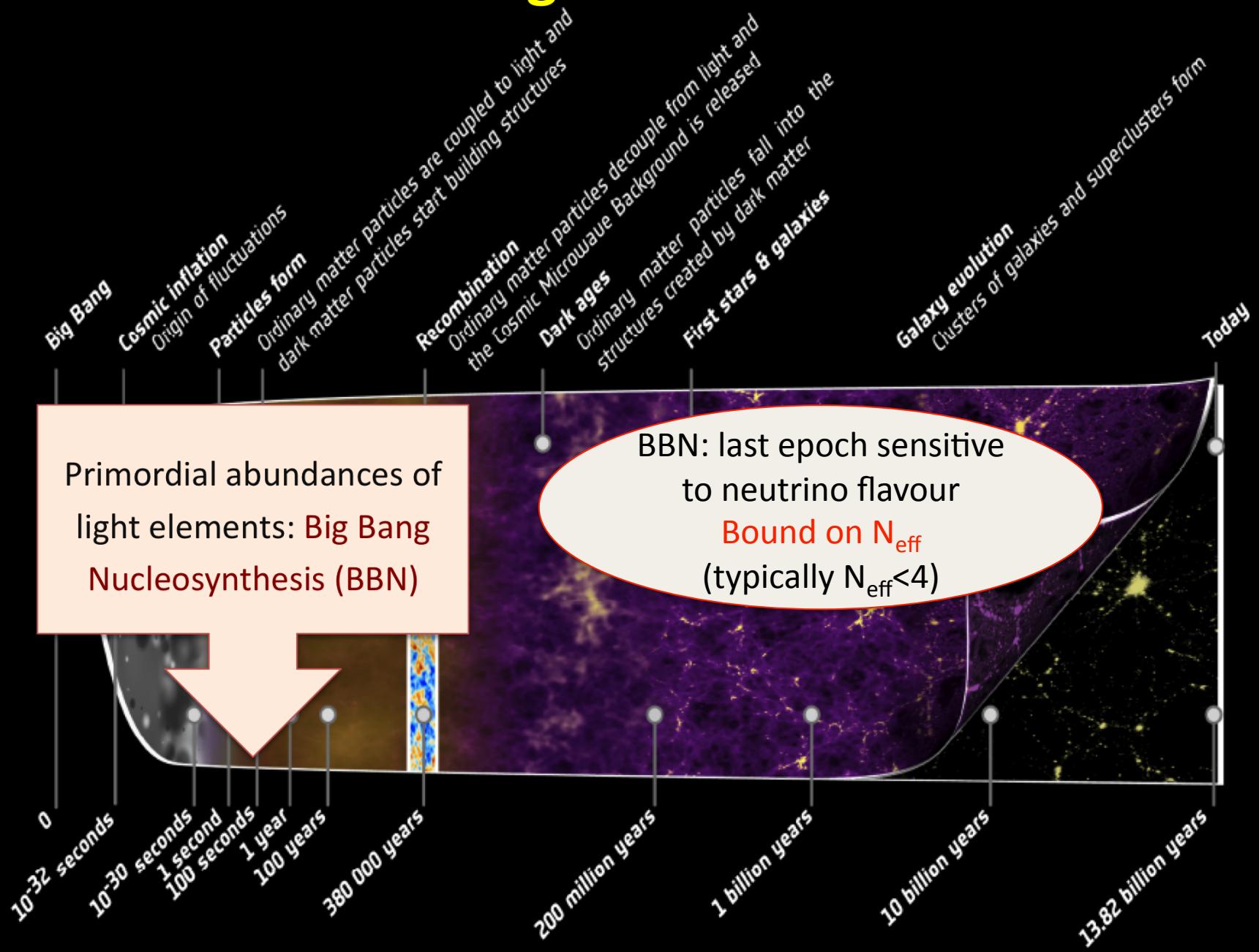
Neff & Active-sterile neutrino oscillations

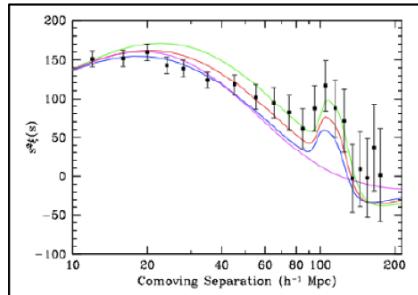


Hannestad, Tamborra & Tram, JCAP 07 (2012) 025

Cosmological Observables

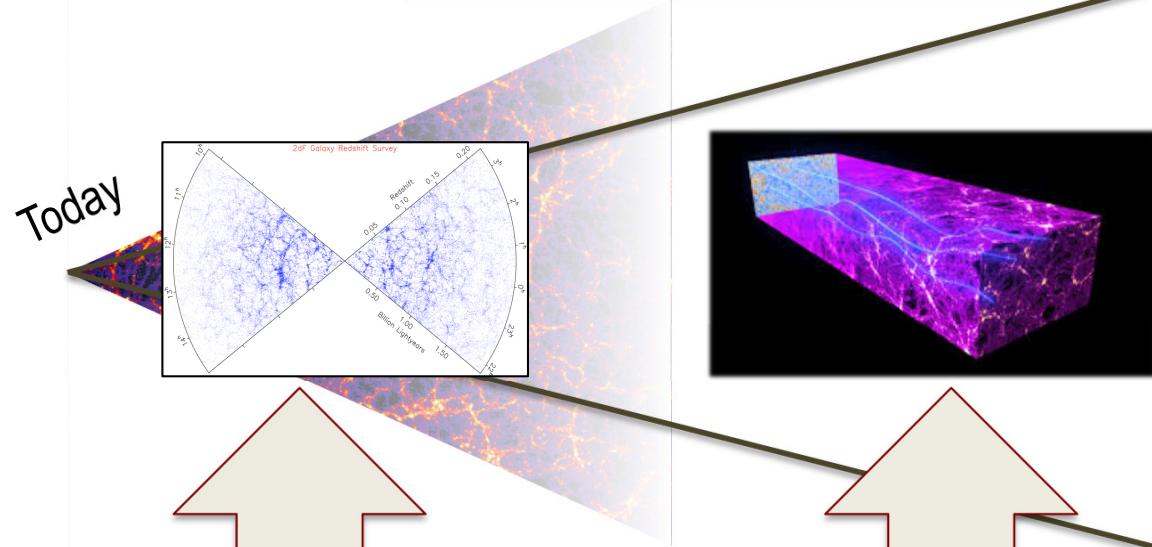
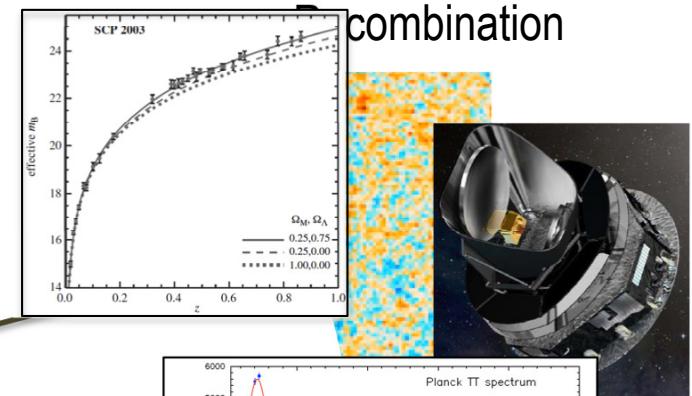
Cosmological Observables





Cosmological Observables

Hubble constant H_0 & cosmic distances
measurements: SN Ia and Baryon
Acoustic Oscillations (BAO)

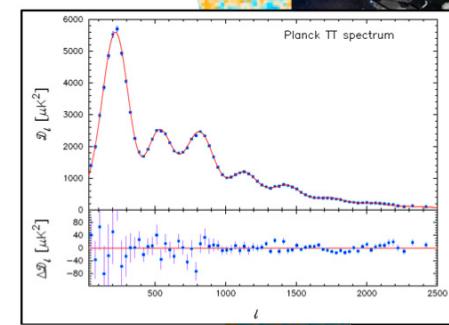


matter density fluctuations

LSS [galaxy / cosmic shear /
 $\text{Ly}\alpha$] spectrum

Photon momentum
after decoupling

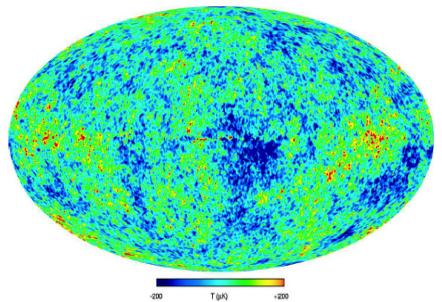
CMB secondary anisotropy
spectrum



Photon density fluctuations
before decoupling

CMB primary anisotropy
spectrum (temp+pol)

CMB data before Planck



Map of CMBR temperature Fluctuations

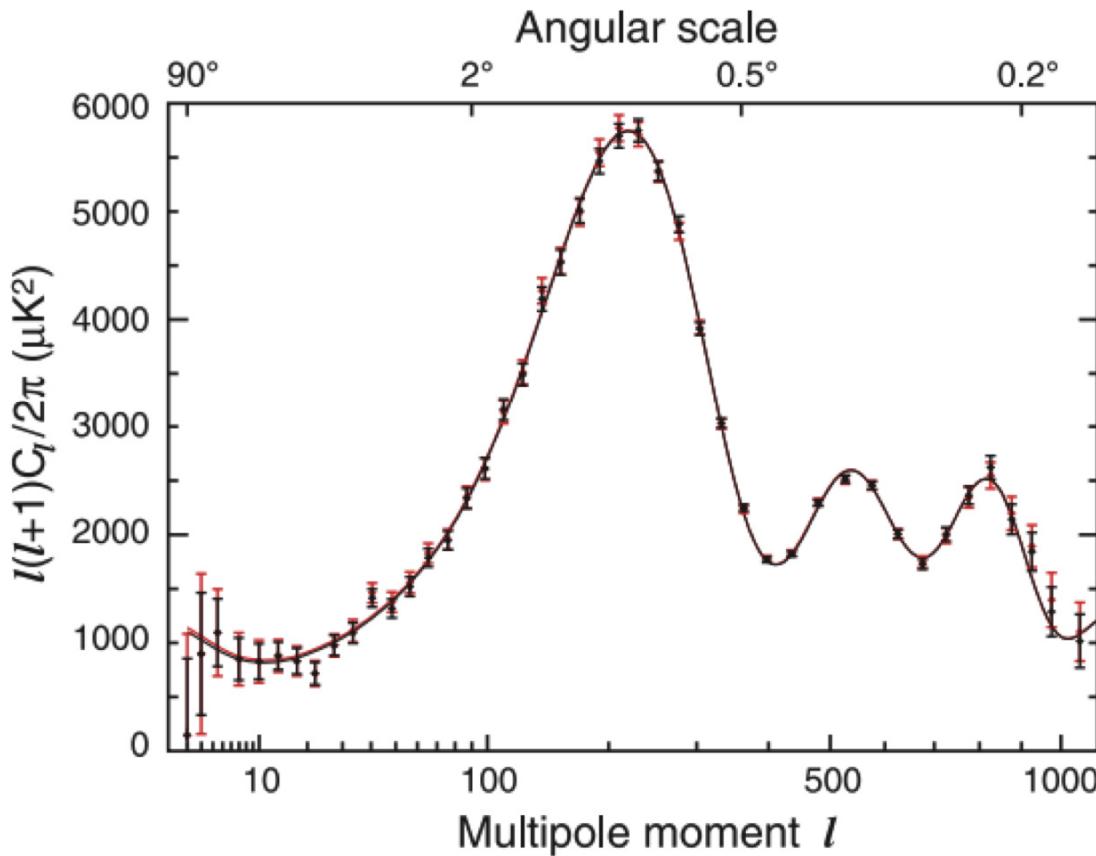
$$\Delta(\theta, \varphi) = \frac{T(\theta, \varphi) - \langle T \rangle}{\langle T \rangle}$$

Multipole Expansion

$$\Delta(\theta, \varphi) = \sum_{\lambda=0}^{\infty} \sum_{m=-\lambda}^{\lambda} a_{\lambda m} Y_{\lambda m}(\theta, \varphi)$$

Angular Power Spectrum

$$C_l = \left\langle a_{lm}^* a_{lm} \right\rangle = \frac{1}{2l+1} \sum_{m=-l}^l a_{lm}^* a_{lm}$$



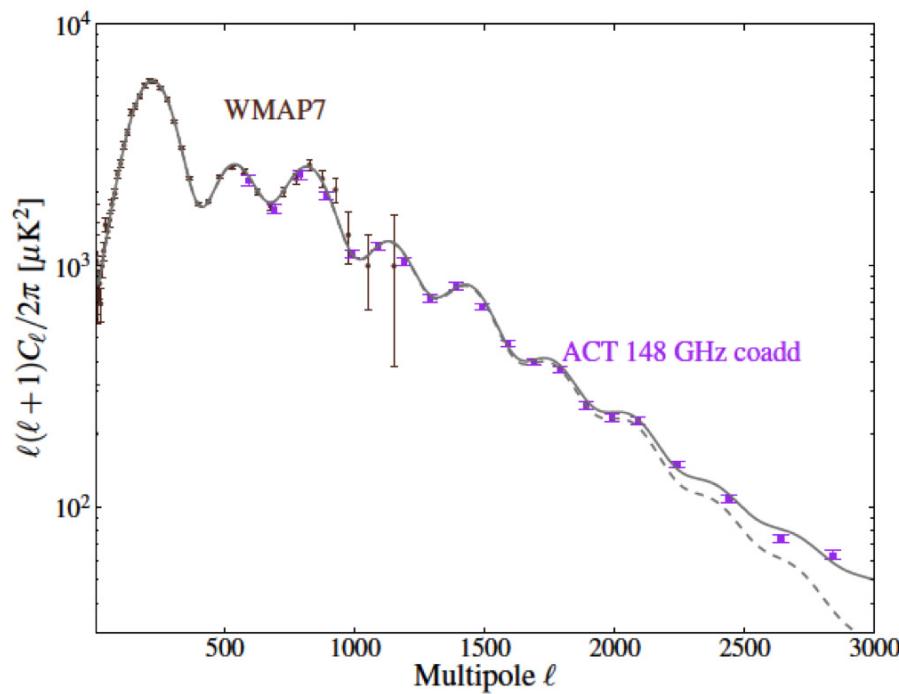
WMAP9: final results after 9 years

Data analysis refined: better treatment of the different frequency channels

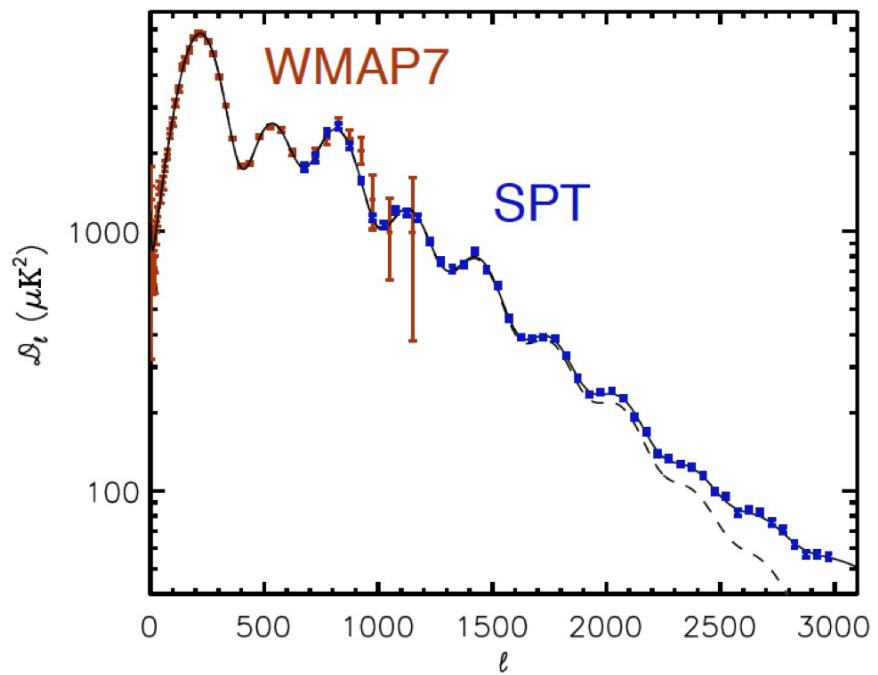
Hinshaw et al, arXiv:1212.5226

CMB data before Planck

Ground telescopes have better angular resolution: measure the CMB spectrum at high l's

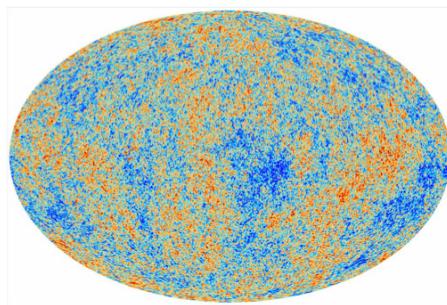


ACT, Sievers et al, arXiv:1301.0824



SPT, Story et al, arXiv:1210.7231

CMB data from Planck



Map of CMBR temperature Fluctuations

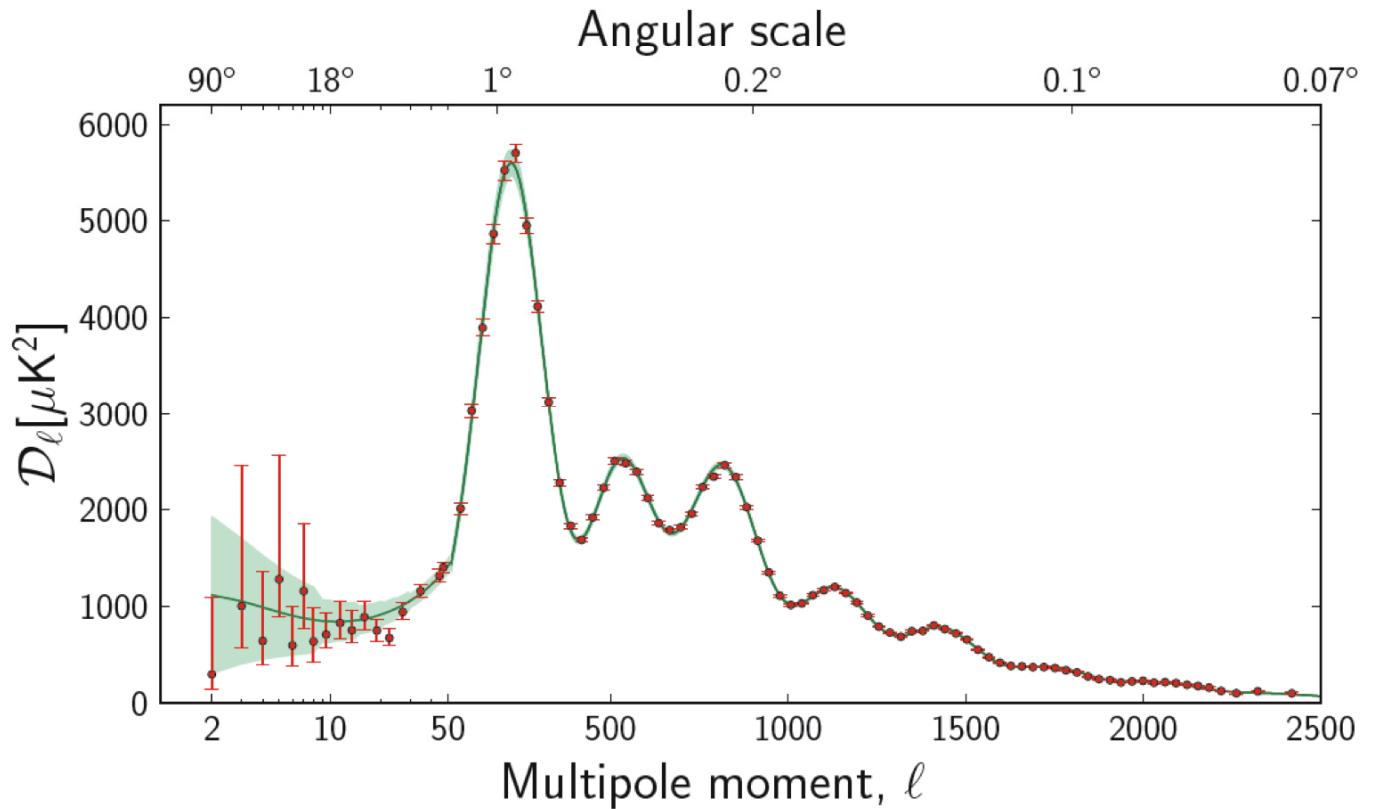
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Multipole Expansion

$$\Delta(\theta, \varphi) = \sum_{\lambda=0}^{\infty} \sum_{m=-\lambda}^{\lambda} a_{\lambda m} Y_{\lambda m}(\theta, \varphi)$$

Angular Power Spectrum

$$C_\lambda = \left\langle a_{\lambda m}^* a_{\lambda m} \right\rangle = \frac{1}{2\lambda+1} \sum_{m=-\lambda}^{\lambda} a_{\lambda m}^* a_{\lambda m}$$

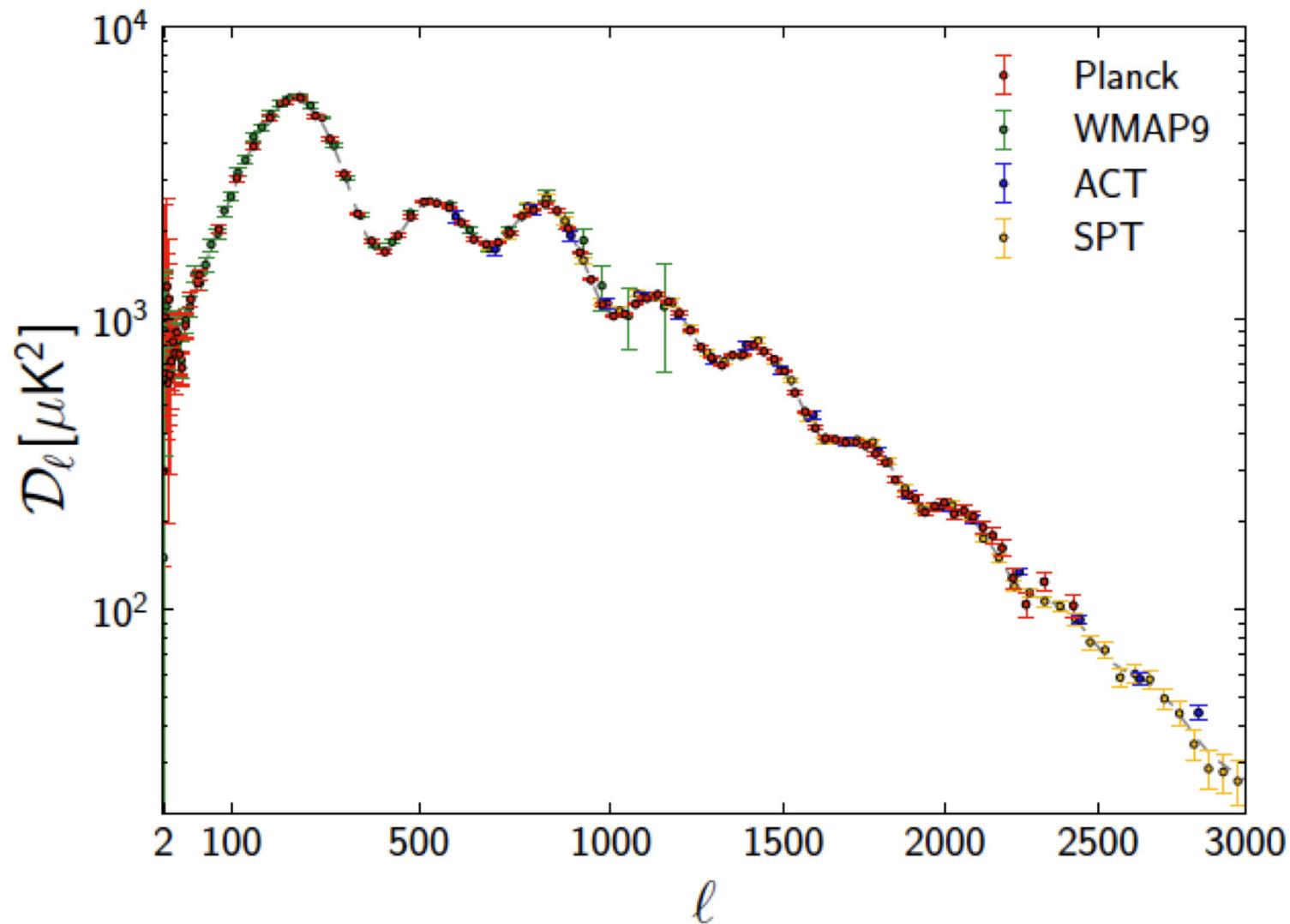


PLANCK 2013: results from 15 months, measures the CMB spectrum in a wide range of ℓ 's
 Only **TT spectrum** with **lensing extraction** (projected gravitational field \sim sensitive to structures at $z \sim 1-3$)

P.A.R. Ade et al, arXiv:1303.5076

Present CMB data

Planck vs other experiments



Bounds on neutrino properties from Planck (& other cosmo data)

The minimal Λ CDM model fits very well the data

Parameter	Planck (CMB+lensing)		Planck+WP+highL+BAO	
	Best fit	68 % limits	Best fit	68 % limits
$\Omega_b h^2$	0.022242	0.02217 ± 0.00033	0.022161	0.02214 ± 0.00024
$\Omega_c h^2$	0.11805	0.1186 ± 0.0031	0.11889	0.1187 ± 0.0017
$100\theta_{\text{MC}}$	1.04150	1.04141 ± 0.00067	1.04148	1.04147 ± 0.00056
τ	0.0949	0.089 ± 0.032	0.0952	0.092 ± 0.013
n_s	0.9675	0.9635 ± 0.0094	0.9611	0.9608 ± 0.0054
$\ln(10^{10} A_s)$	3.098	3.085 ± 0.057	3.0973	3.091 ± 0.025
Ω_Λ	0.6964	0.693 ± 0.019	0.6914	0.692 ± 0.010
σ_8	0.8285	0.823 ± 0.018	0.8288	0.826 ± 0.012
z_{re}	11.45	$10.8_{-2.5}^{+3.1}$	11.52	11.3 ± 1.1
H_0	68.14	67.9 ± 1.5	67.77	67.80 ± 0.77
Age/Gyr	13.784	13.796 ± 0.058	13.7965	13.798 ± 0.037
$100\theta_*$	1.04164	1.04156 ± 0.00066	1.04163	1.04162 ± 0.00056
r_{drag}	147.74	147.70 ± 0.63	147.611	147.68 ± 0.45
$r_{\text{drag}}/D_V(0.57)$	0.07207	0.0719 ± 0.0011		

The minimal Λ CDM model fits very well the data

Comparison of *Planck*-only and *WMAP*-only Six-Parameter Λ CDM Fits^a

Parameter	<i>Planck</i> ("CMB+Lens")	<i>WMAP</i> (9-year)	Difference	
			value	<i>WMAP</i> σ
$\Omega_b h^2$	0.02217 ± 0.00033	0.02264 ± 0.00050	-0.00047	0.9
$\Omega_c h^2$	0.1186 ± 0.0031	0.1138 ± 0.0045	0.0048	1.1
Ω_Λ	0.693 ± 0.019	0.721 ± 0.025	-0.028	1.1
τ	0.089 ± 0.032	0.089 ± 0.014	0	0
t_0 (Gyr)	13.796 ± 0.058	13.74 ± 0.11	56 Myr	0.5
H_0 (km s ⁻¹ Mpc ⁻¹)	67.9 ± 1.5	70.0 ± 2.2	-2.1	1.0
σ_8	0.823 ± 0.018	0.821 ± 0.023	0.002	0.1
Ω_b	0.0481 ^b	0.0463 ± 0.0024	0.0018	0.7
Ω_c	0.257 ^b	0.233 ± 0.023	0.024	1.0

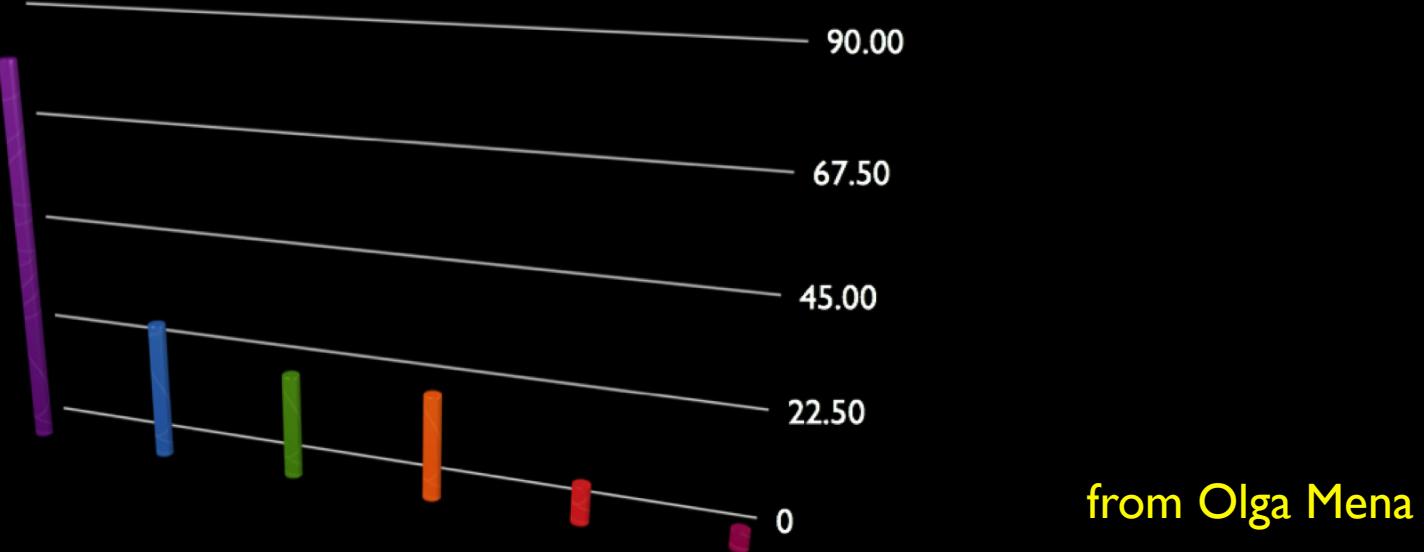
^aThe new *Planck* results strongly favor the standard six-parameter Λ CDM model with parameter values that are consistent with *WMAP* parameters, as shown in this table which compares results derived entirely from *Planck* data with those derived entirely from *WMAP* data.

^bParameters derived from quoted values. No error estimate is given for this data/model combination.

What ingredient, in your opinion, should be mandatory to change in the Λ CDM?

The Λ CDM POLL

- █ Neutrinos
- █ Dark energy
- █ Dark matter
- █ Primordial Spectrum
- █ N_{eff}
- █ Curvature

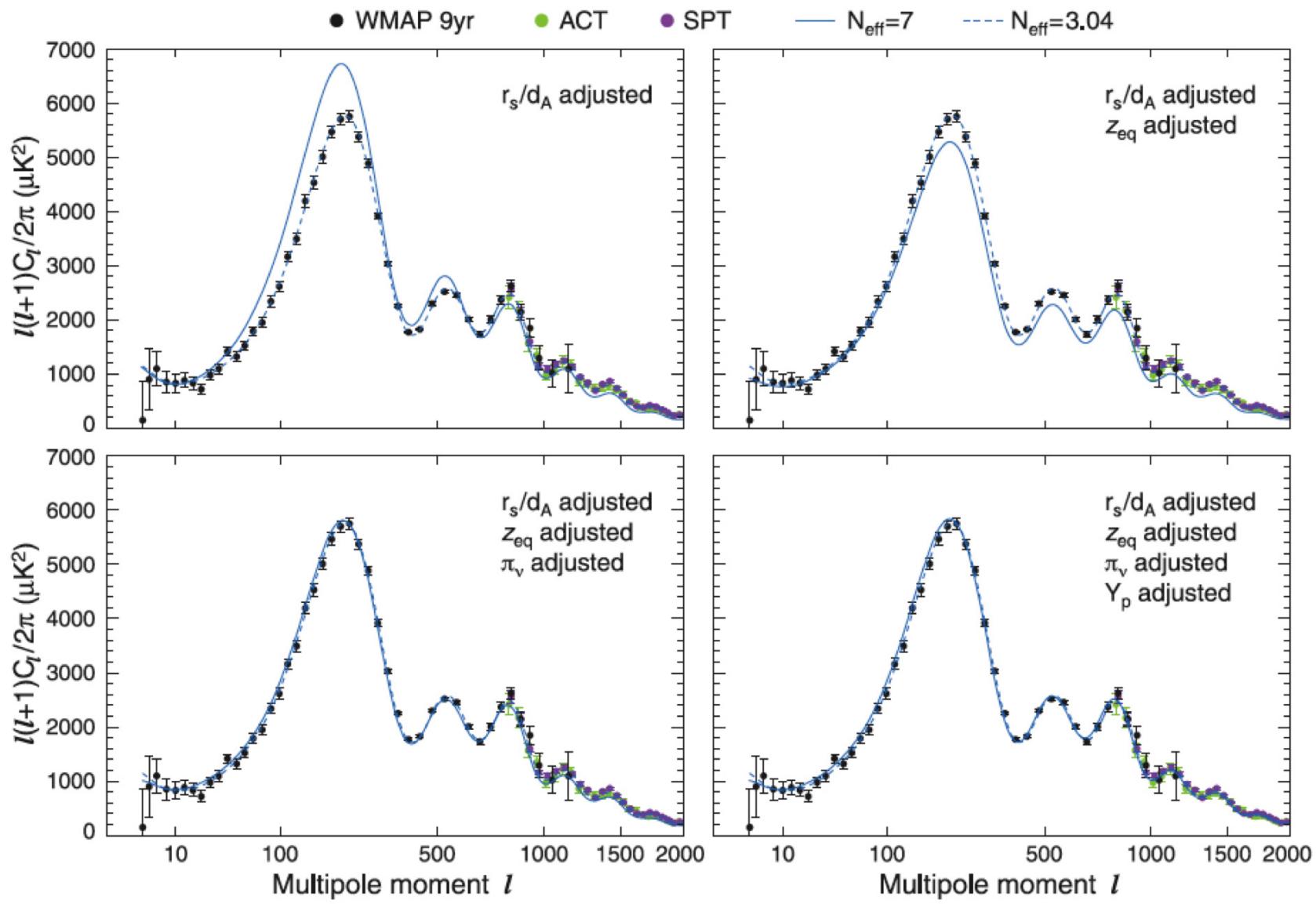


Planck collaboration has already added massive neutrinos in the vanilla-six parameter model, with $\Sigma m_{\nu, \text{fiducial}} = 0.06 \text{ eV}!$

Measuring N_{eff}

- N_{eff} is a parameter for the relativistic density in general
- “background effects” (change in expansion history) **versus** “perturbation effects” (gravitational interactions between photons and relativistic species)
- “effect of N_{eff} ” depends on what is kept fixed.
- Fixing quantities best probed by CMB (angular peak scale, redshift of equality, ...):
 - possible with simultaneous enhancement of radiation, matter, Λ densities, with fixed photon and baryon densities
 - then increase in N_{eff} goes with increase in H_0 : **positive correlation** between the two

Measuring N_{eff}

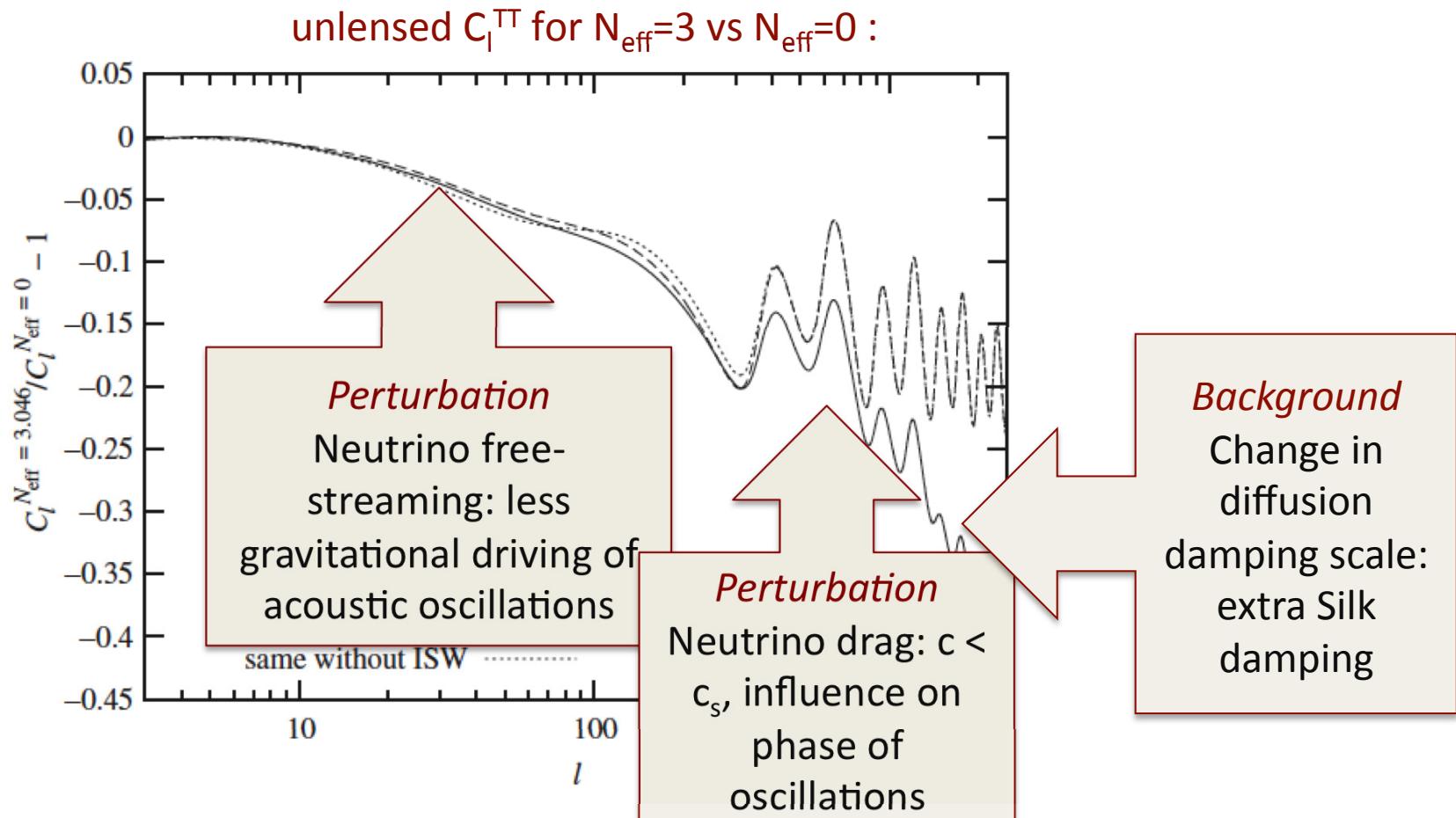


Hinshaw et al, arXiv:1212.5226

Measuring N_{eff}

- Fixing quantities best probed by CMB (angular peak scale, redshift of equality, ...):

simultaneous enhancement of radiation, matter, L densities, with fixed photon and baryon densities



Measuring N_{eff}

- Ultimately, constraints driven by CMB damping tail
 - WMAP+SPT see anomalously low tail: $N_{\text{eff}} > 3$ at 2 sigma
 - Planck and Planck+BAO well compatible with **3.046** at 1 sigma
 - Planck (+BAO) + HST: enforce higher H_0 , hence also higher N_{eff}

- CMB alone (Planck+WP+HighL)

$$N_{\text{eff}} = \mathbf{3.36}^{+0.68}_{-0.64}$$

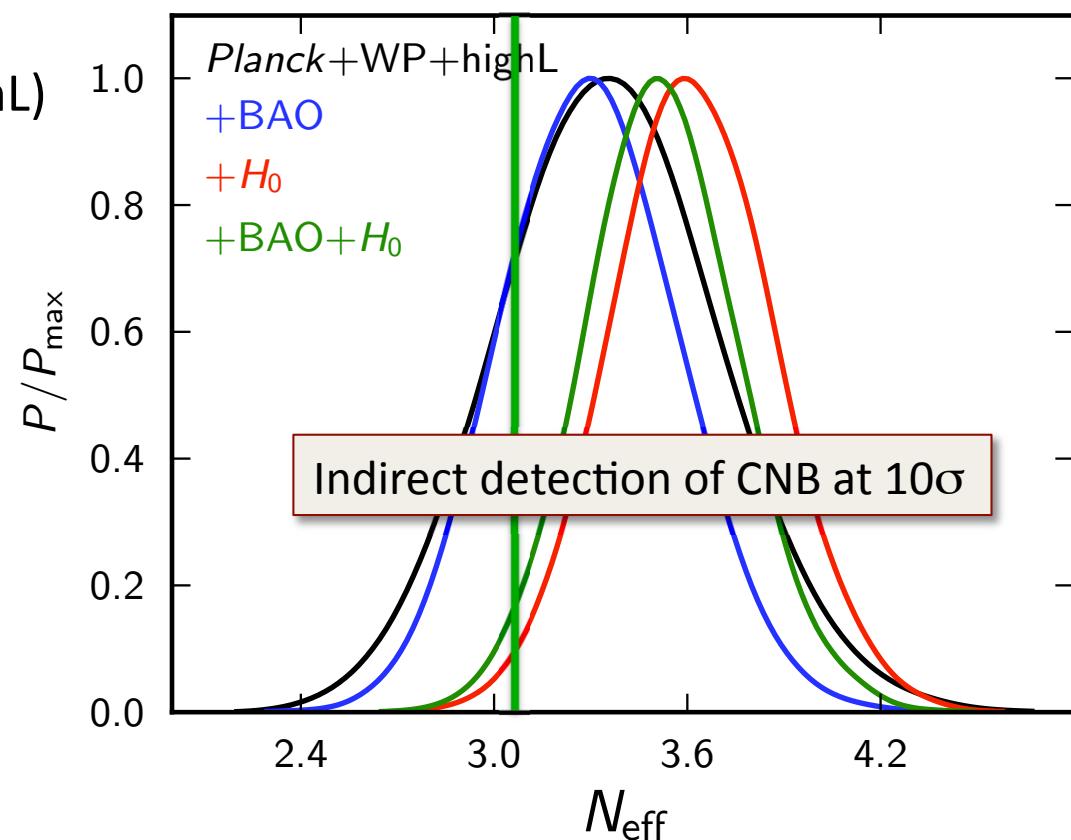
- With lensing and BAO:

$$N_{\text{eff}} = \mathbf{3.30}^{+0.54}_{-0.51}$$

- With H_0 and BAO:

$$N_{\text{eff}} = \mathbf{3.52}^{+0.48}_{-0.45}$$

all 95%CL



Measuring N_{eff}

- Ultimately, constraints driven by CMB damping tail
 - WMAP+SPT see anomalously low tail: $N_{\text{eff}} > 3$ at 2 sigma
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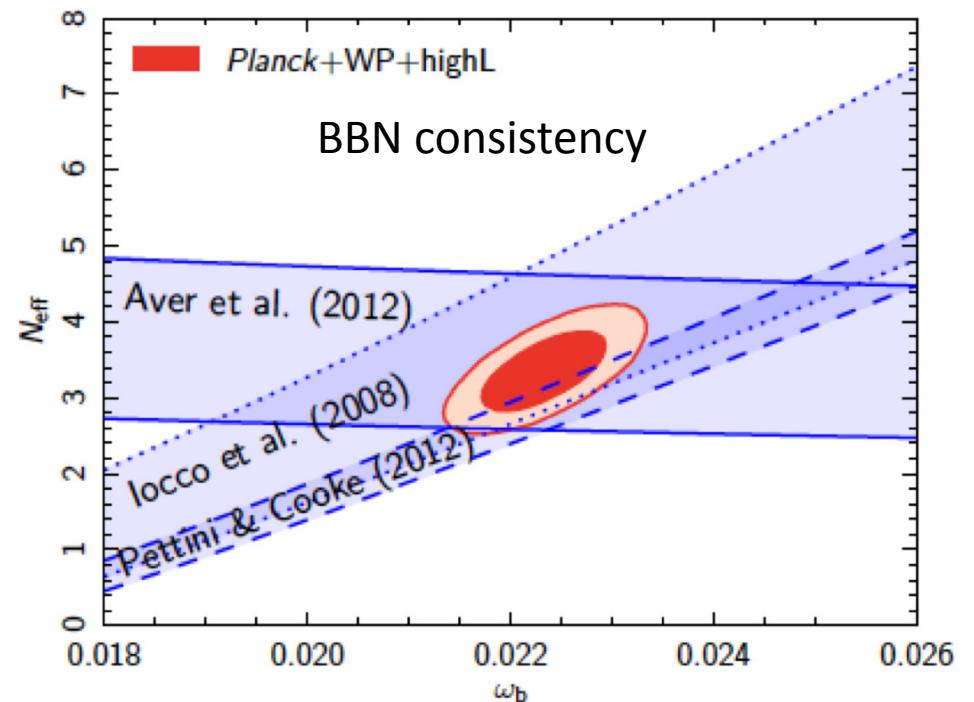
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$$N_{\text{eff}} = 3.30^{+0.54}_{-0.51}$$

- With H_0 and BAO:

$$N_{\text{eff}} = 3.52^{+0.48}_{-0.45}$$

all 95%CL



Measuring m_ν with the CMB

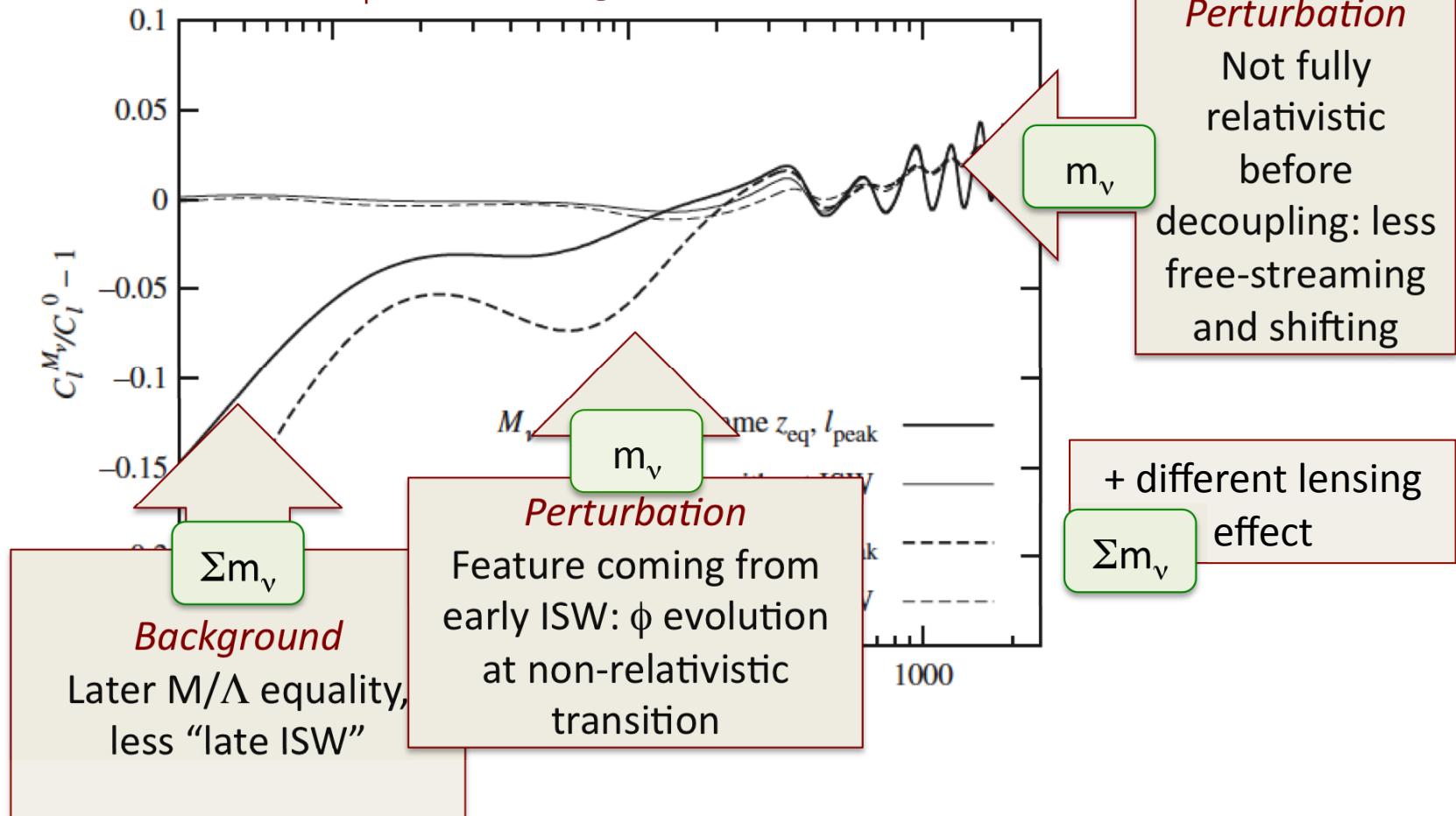
- Neutrinos contribute to **radiation** at early times and **non-relativistic matter** at late times
- If $m_\nu < 0.6$ eV, neutrinos are **relativistic** at photon decoupling. In principle the primary CMB TT spectrum sensitive to $\Sigma m_\nu > 1.5$ eV
- “**effect of m_ν** ” depends on what is kept fixed
- Leave both “**early cosmology**” and **angular diameter dist.** to decoupling invariant:
 - Possible by fixing photon, cdm and baryon densities, while tuning H_0 , W_L
 - then increase in m_n goes with decrease in H_0 : **negative correlation** between the two
 - “base model” in Planck has (0.06, 0, 0) eV masses: shifts best-fitting H_0 by -0.6 h/km/Mpc with respect to massless case

Measuring m_ν with the CMB

- Leaving both “early cosmology” and angular diameter dist. to decoupling invariant:

fixing photon, cdm and baryon densities, while tuning H_0, Ω_Λ

unlensed C_l^{TT} for two degenerate masses vs massless:



Measuring m_ν with Planck

CMB alone (Planck+WP+HighL):

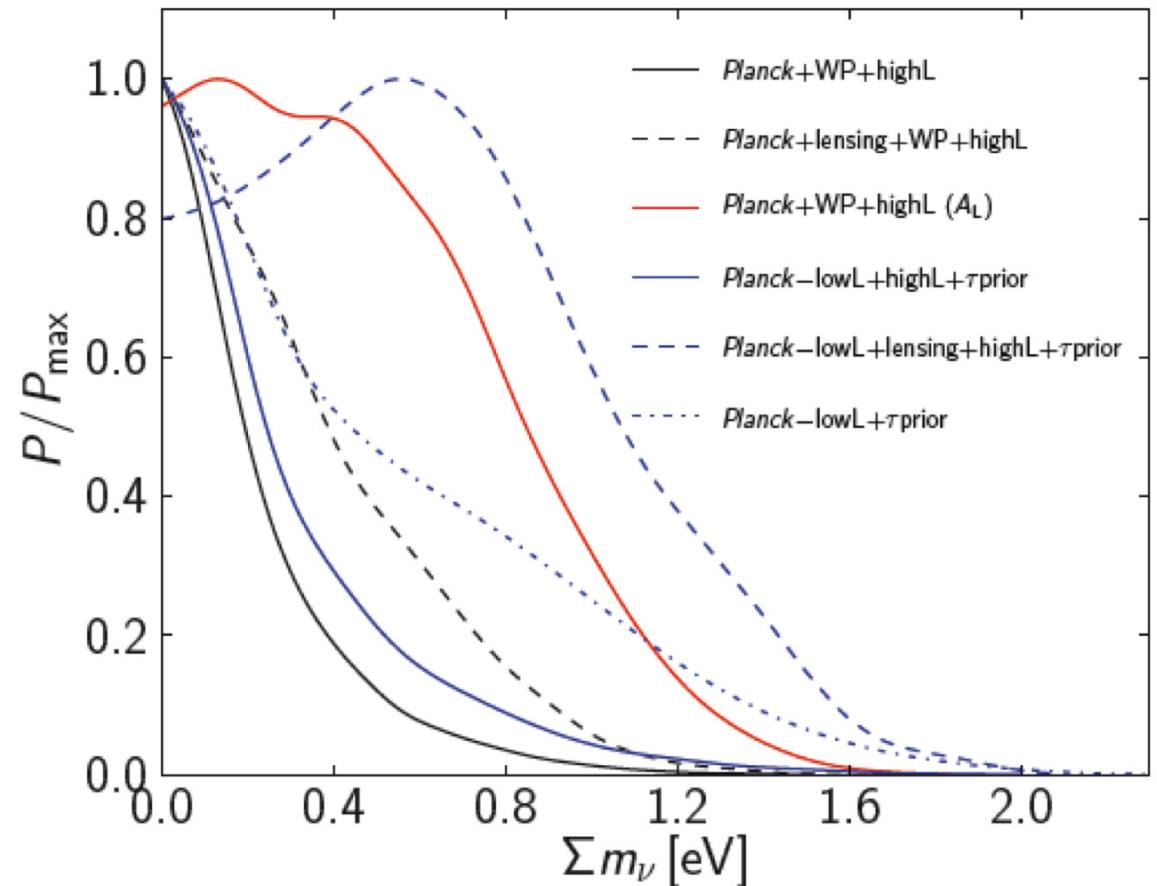
$$\Sigma m_\nu < 0.66 \text{ eV}$$

With BAO:

$$\Sigma m_\nu < 0.23 \text{ eV}$$

With lensing:

$$\Sigma m_\nu < 0.85 \text{ eV}$$



All 95% CL. Robust w.r.t cosmological extensions
(except for curvature: weakens 50%)

Measuring m_ν & N_{eff} with Planck

Results are practically unchanged

CMB alone (Planck+WP+HighL):

$$\Sigma m_\nu < 0.60 \text{ eV}$$

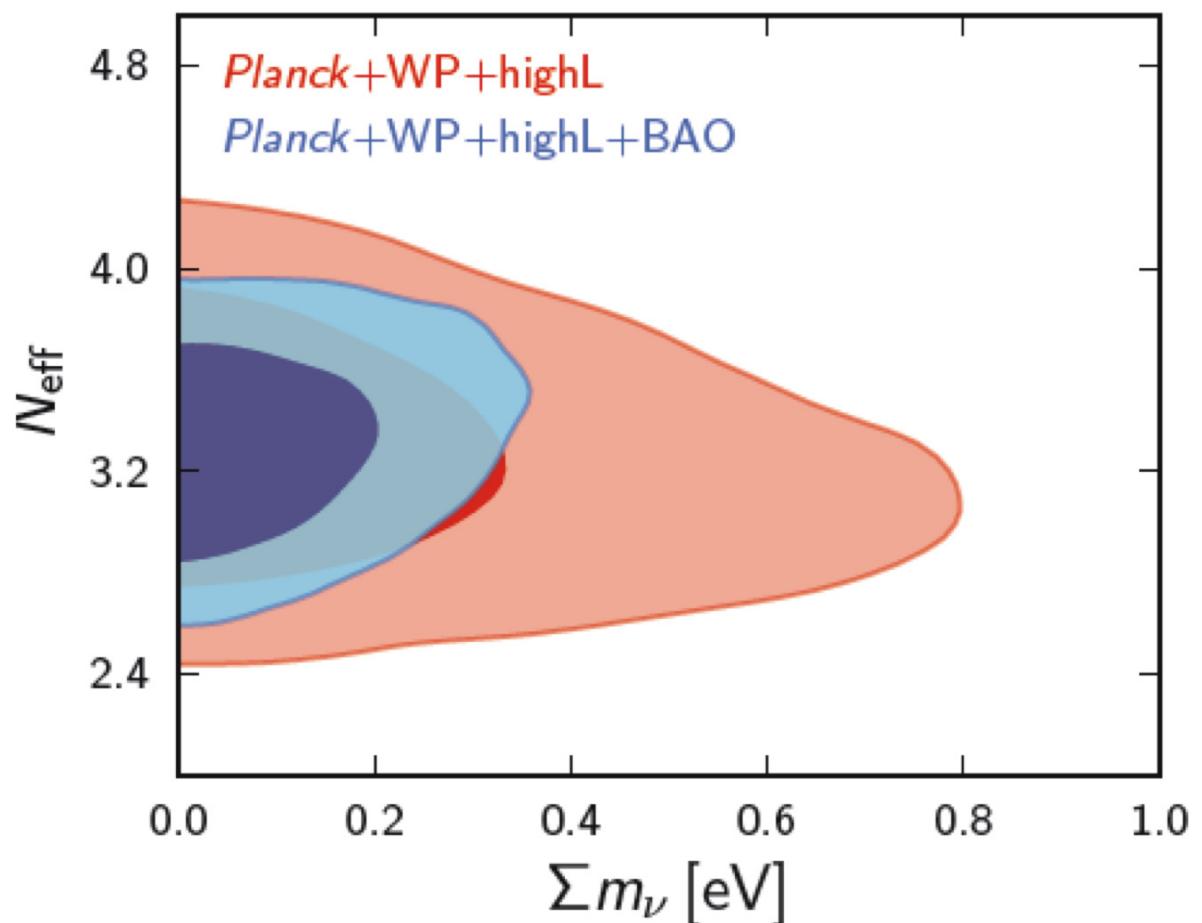
$$N_{\text{eff}} = 3.29^{+0.67}_{-0.64}$$

With BAO:

$$\Sigma m_\nu < 0.28 \text{ eV}$$

$$N_{\text{eff}} = 3.32^{+0.54}_{-0.52}$$

All 95% CL



Probing the absolute neutrino mass scale

Tritium β decay	$m_\beta = \left(\sum_i U_{ei} ^2 m_i^2 \right)^{1/2}$	2.2 eV
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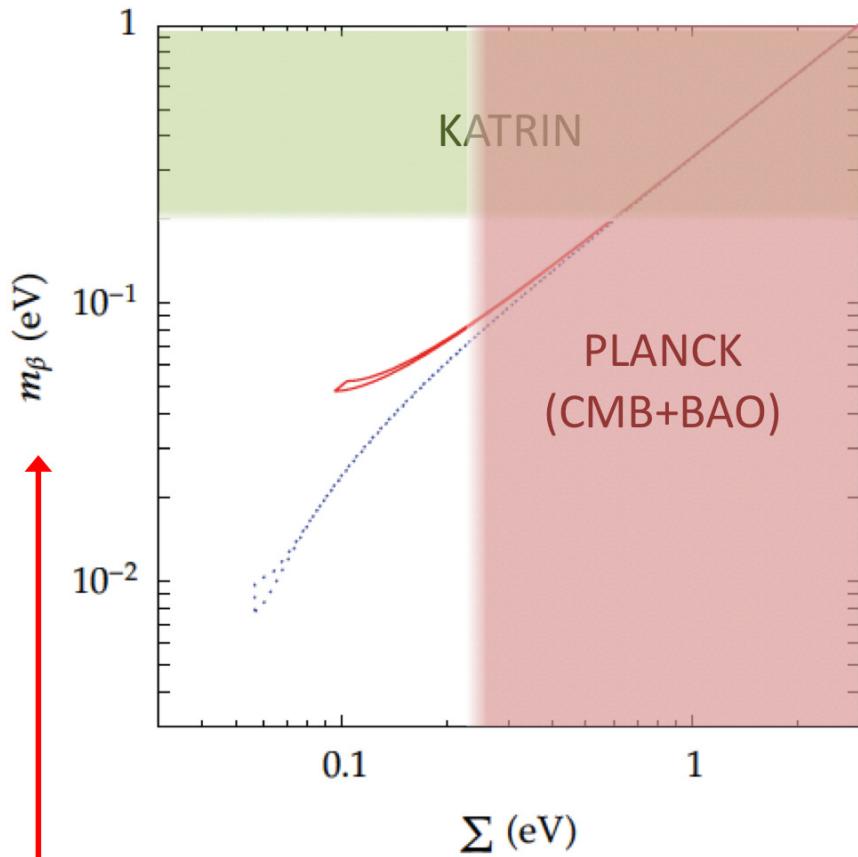
$$\rightarrow [c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{1/2}$$

Neutrinoless double beta decay	$m_{\beta\beta} = \left \sum_i U_{ei}^2 m_i \right $	< 0.2-0.8 eV
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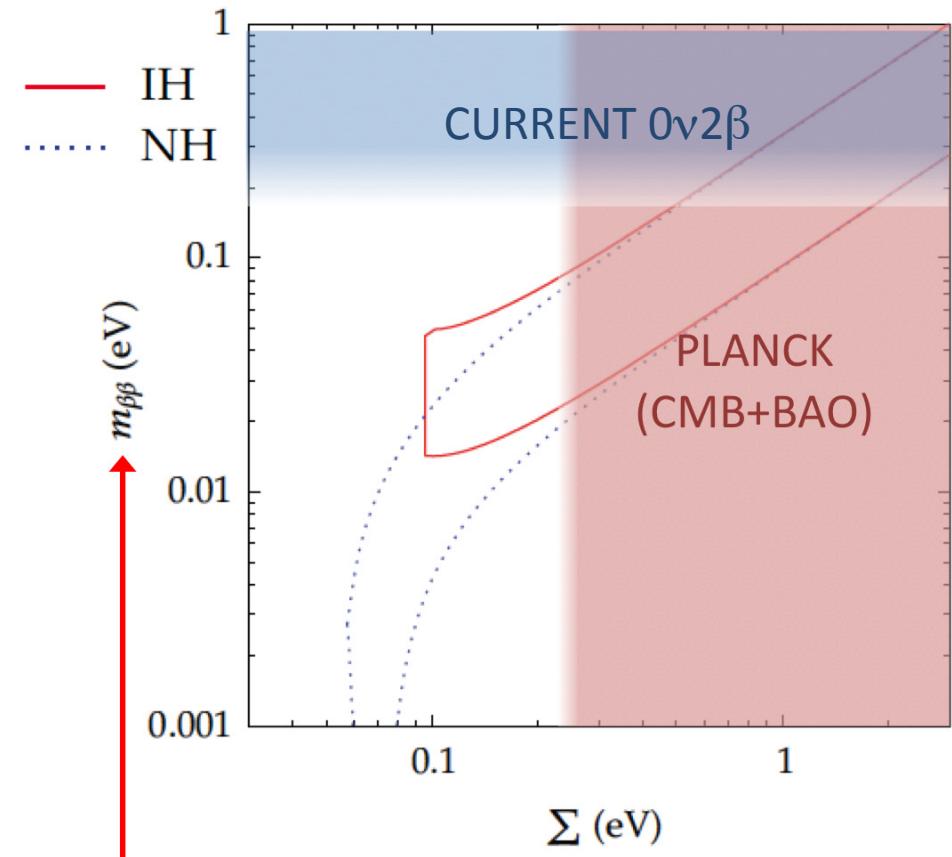
$$\rightarrow |c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3}|$$

Cosmology	$\sim \sum_i m_i$	< 0.23-1.0 eV
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Tritium β decay, $0\nu2\beta$ and Cosmology



$$[c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{1/2}$$



$$|c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3}|$$

Measuring m_ν (sterile) & N_{eff} with Planck

Planck analysis of 3+1 neutrino scenarios (m_ν^{eff}). Two cases: extra state with T_s or with rescaled spectrum

for $m_{\text{sterile}}^{\text{thermal}} < 10 \text{ eV}$

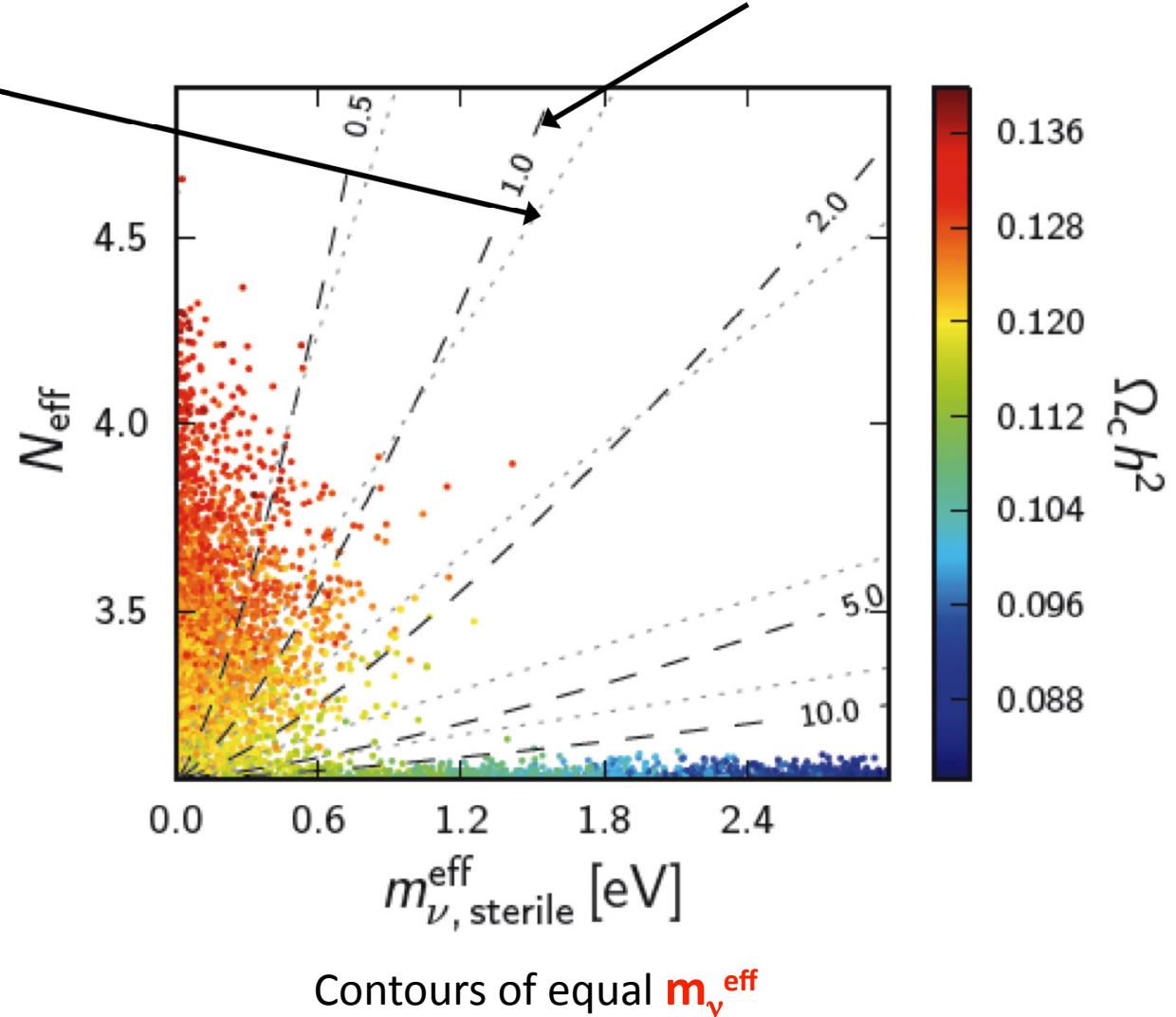
CMB alone (Planck+WP+HighL):

$$\left. \begin{array}{l} N_{\text{eff}} < 3.91 \\ m_{\nu, \text{sterile}}^{\text{eff}} < 0.59 \text{ eV} \end{array} \right\}$$

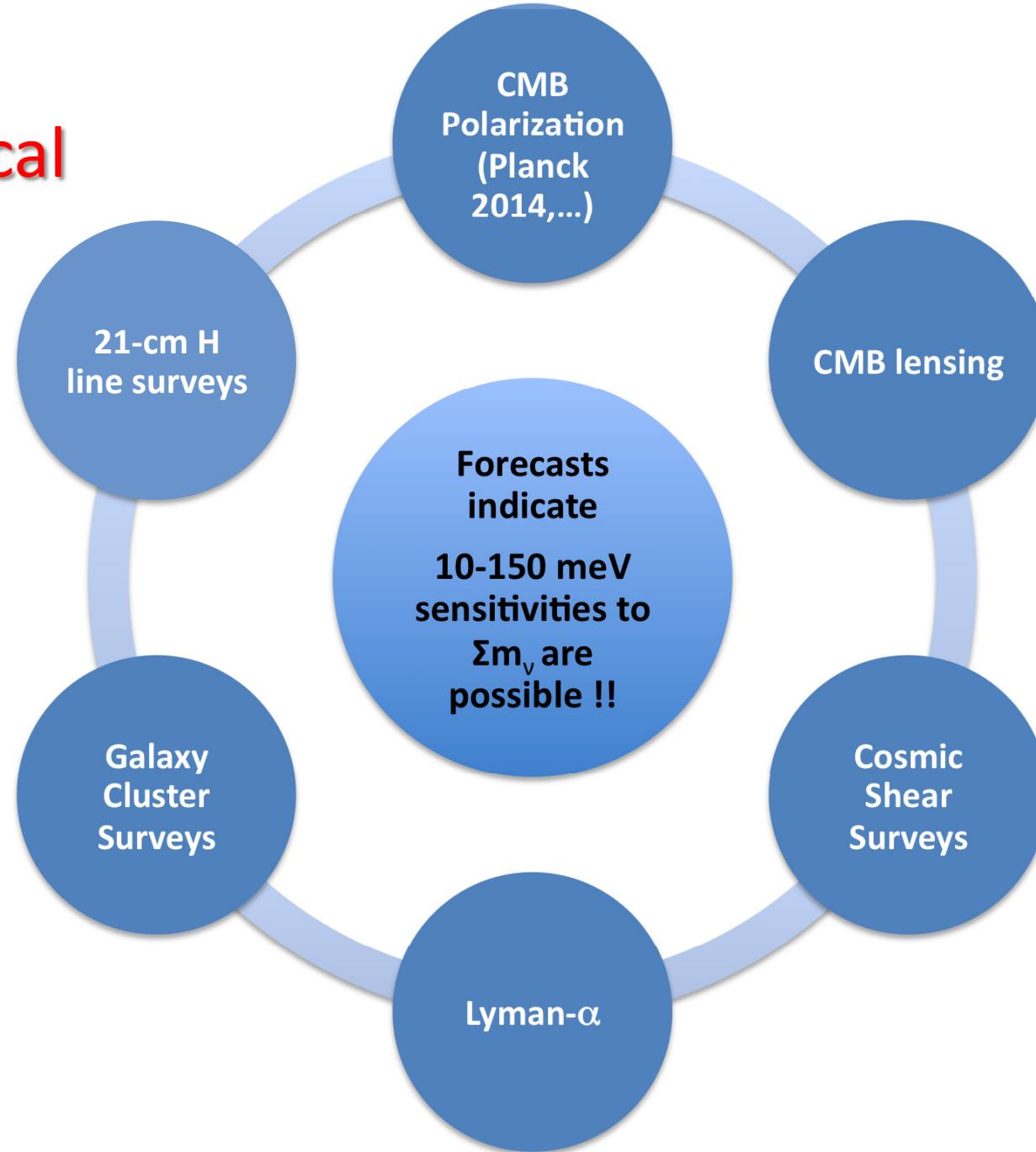
With BAO:

$$\left. \begin{array}{l} N_{\text{eff}} < 3.80 \\ m_{\nu, \text{sterile}}^{\text{eff}} < 0.42 \text{ eV} \end{array} \right\}$$

All 95% CL

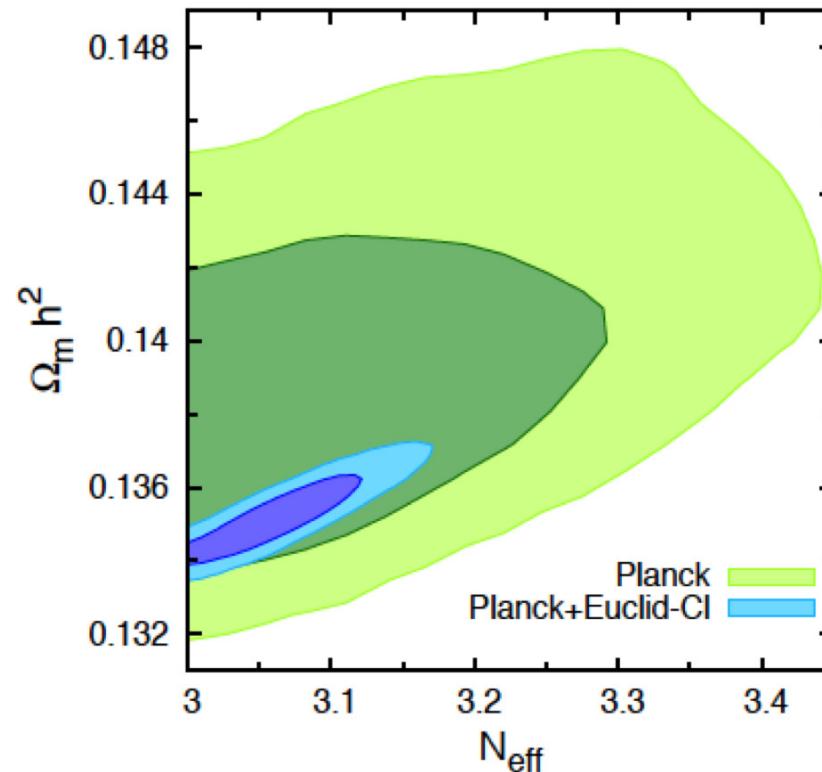
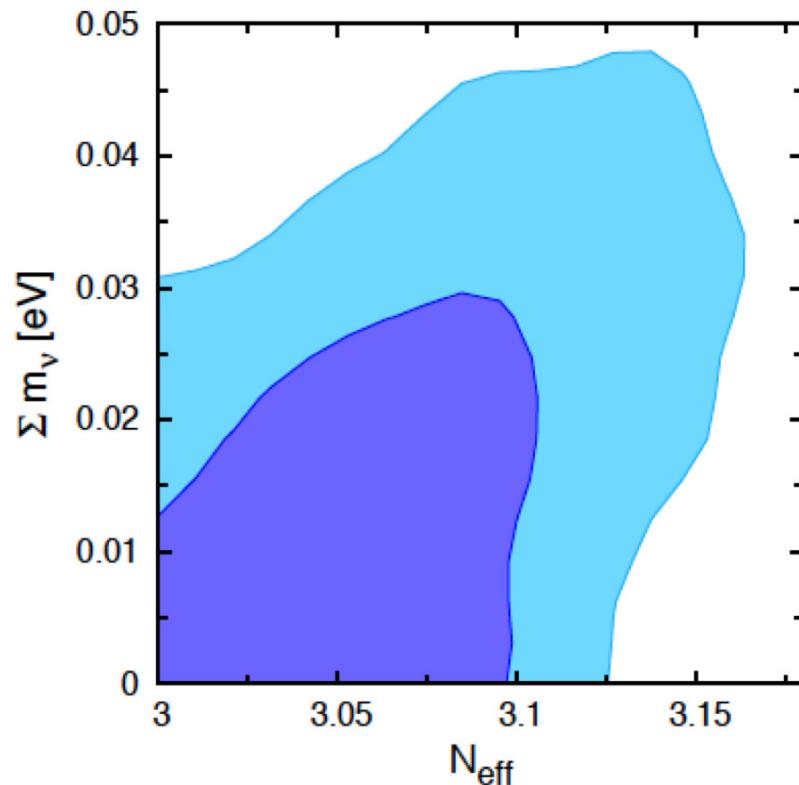


Future cosmological data



Future sensitivities to N_{eff} and Σm_ν

Example of forecast: PLANCK + Euclid-like photometric galaxy cluster survey



Data	Planck+Euclid-Cl		
Model	$w\text{CDM}+m_\nu+N_{\text{eff}}$	$\Lambda\text{CDM}+m_\nu+N_{\text{eff}}+\Omega_k$	
Σm_ν [eV]	68% CL 95% CL	< 0.024 < 0.046	< 0.024 < 0.046
N_{eff}	95% CL	< 3.16	< 3.17

M.C.A. Cerboni et al,
arXiv:1303.4550

Future sensitivities on neutrino masses

Probe	95% C.L.			Key systematics	Current surveys	Future surveys
	Current $\sum m_\nu$ (eV)	Forecast $\sum m_\nu$ (eV)				
CMB primordial	1.3	0.6		Recombination	WMAP, Planck [95]	None
CMB primordial + Distance	0.58	0.35		Distance measurements	WMAP, Planck	None
Lensing of CMB	∞	0.2 – 0.05		NG of Secondary anisotropies	Planck, ACT [38], SPT [97]	EBEX [58], ACTPol [53], SPTPol, POLARBEAR [3], CMBPol [4]
Galaxy distribution	0.6	0.1		Nonlinearities, Bias	SDSS [59,60], BOSS [83]	DES [85], BigBOSS [82], DESpec [86], LSST [93], Subaru PFS [98], HETDEX [34]
Lensing of Galaxies	0.6	0.07		Baryons, NL, Photometric redshifts	CFHT-LS [22], COSMOS [49]	DES [85], Hyper SuprimeCam [52], LSST [93], Euclid [89], WFIRST[101]
Lyman α	0.2	0.1		Bias, Metals, QSO continuum	SDSS, BOSS, Keck	BigBOSS[82], TMT[100], GMT[90]
21 cm	∞	0.1 – 0.006		Foregrounds, Astrophysical modeling	GBT [10], LOFAR [92], PAPER [54], GMRT [87]	MWA [94], SKA [96], FTTT [48]
Galaxy clusters	0.3	0.1		Mass Function, Mass Calibration	SDSS, SPT, ACT, XMM [102]	DES, eRosita [88], LSST Chandra [84]

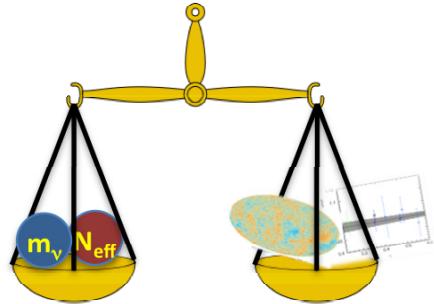
Abazajian et al, Astrop. Phys. 35 (2011) 177

Future sensitivities on neutrino masses

Probe	5-7 years	7-15 years
CMB	0.4-0.6	0.4
CMB with lensing	0.1-0.15	0.04
CMB + Galaxy Distribution	0.2	0.05-0.1
CMB + Lensing of Galaxies	0.1	0.03-0.04
CMB + Lyman- α	0.1-0.2	Unknown
CMB + Galaxy Clusters	-	0.05
CMB + 21 cm	-	0.0003-0.1

Table 1. Future probes of neutrino mass, as well as their projected sensitivity to neutrino mass. Sensitivity in the short term means achievable in approximately 5-7 years, while long term means 7-15 years.

Hannestad, Progr. Part. Nucl. Phys. 65 (2010) 185



Conclusions



- ✓ With Planck data, including CMB lensing, we can measure combinations of cosmological parameters with high precision.
Still Λ CDM fits very well the data
- ✓ No evidence yet for nonzero neutrino masses or an enhanced radiation density (N_{eff}). At 95% CL, bounds $\Sigma m_\nu < 0.23\text{-}0.85 \text{ eV}$ and N_{eff} between **2.79-3.84** or **3.14-4.12**, depending on data
- ✓ Improved sensitivities from a variety of cosmological data (Planck polarization in 2014, cosmic shear surveys...) to reach $\Sigma m_\nu < 0.1 \text{ eV}$

For more details...

