

LHC Dark Matter Searches

# How Useful Are Effective Operators?

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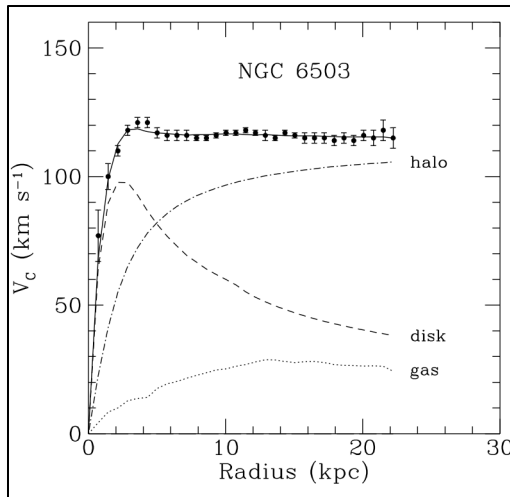
JCAP 10 (2012) 033

arXiv:1208.4605

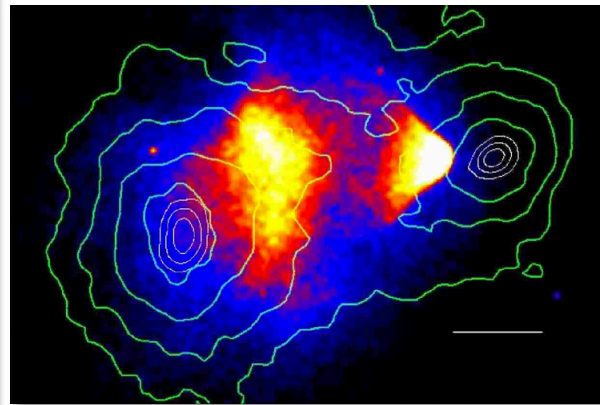
# Outline

- Introduction
- Effective operators and their limitations
- How to treat resonances at the LHC
- Operator mixing and heavy-quark loops
- Conclusions

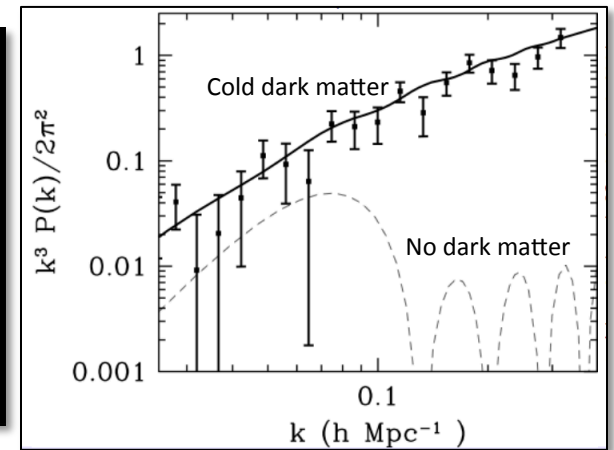
# Evidence for dark matter



Galactic scales



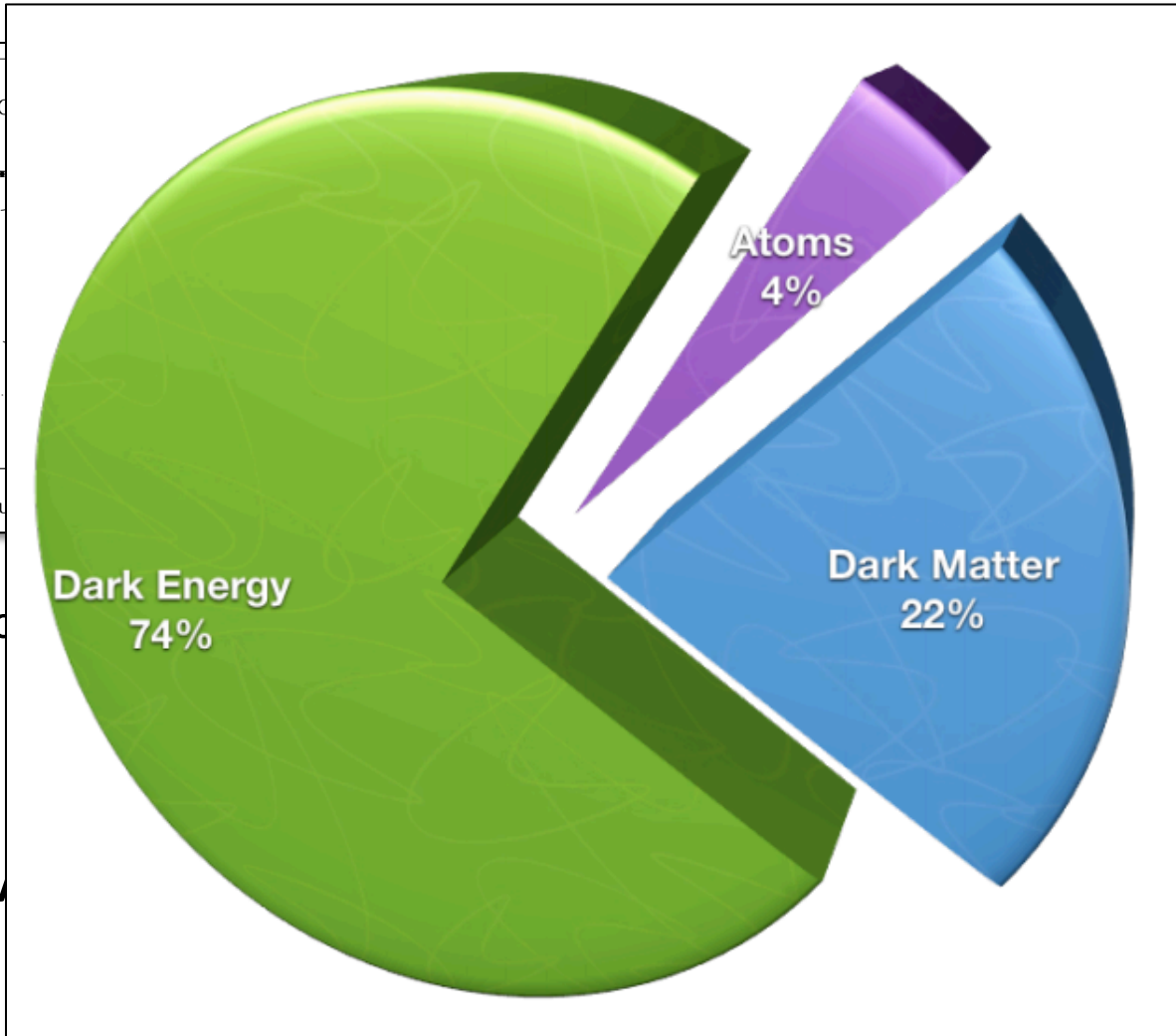
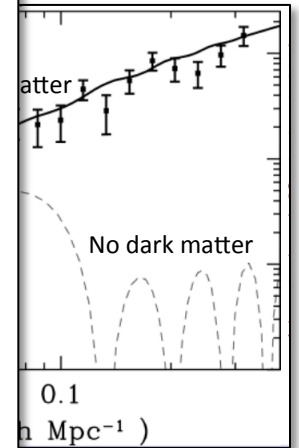
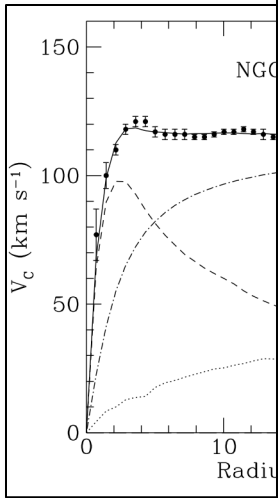
Galaxy cluster scales



Cosmological scales

Conclusive observational evidence for dark matter  
over a wide range of astrophysical scales

# Evidence for dark matter



Galactic scales

Galactic scales

Conclusion  
over

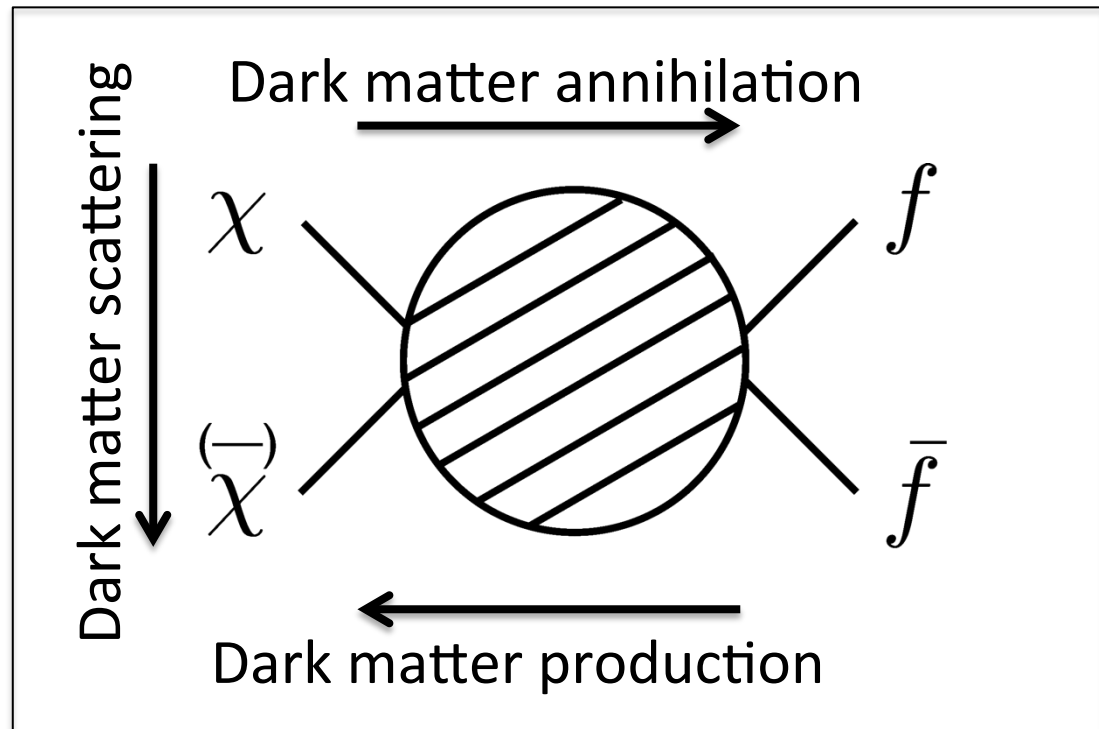
dark matter  
evidence

# Particle candidates for DM

- The most popular candidate is the **WIMP**: A **cold thermal relic** with **weak scale mass and interactions** (e.g. the lightest SUSY particle) which naturally has the **required relic abundance** – the **WIMP miracle**
- The *many* alternative options include:
  - Asymmetric dark matter (with same origin as baryons)
  - Warm dark matter (e.g. sterile keV neutrinos)
  - Axion dark matter
  - ...

# Detecting DM particles

- For most dark matter candidates, we expect **some kind of interactions** with Standard Model particles leading to **thermal equilibrium in the early universe.**



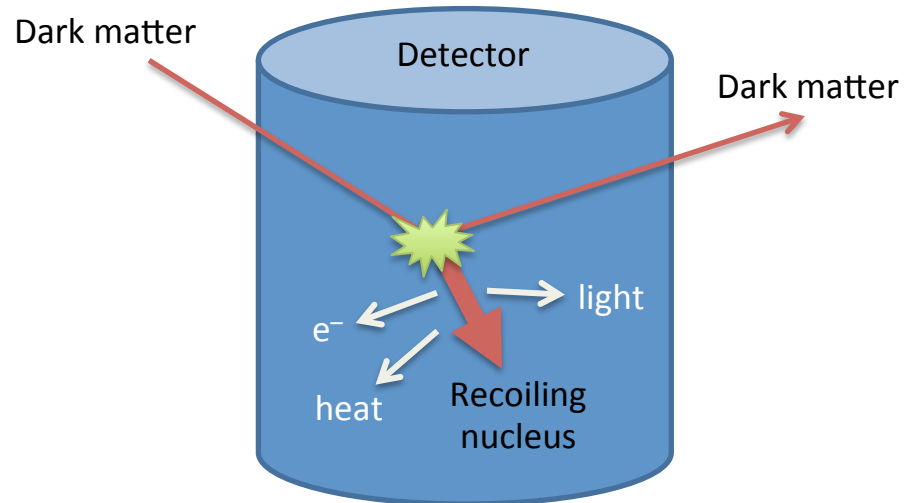
# DM direct detection



Dark matter particles from the Galactic halo that pass through the Earth will occasionally **scatter off nuclei**. The resulting **recoil energy** of the nucleus can be measured in **dedicated low background detectors**.

$$\frac{dR}{dE_{\text{nr}}} = \frac{\rho_0}{m_\chi m_N} \int_{v_{\text{min}}}^{\infty} dv v f(v, v_E) \frac{d\sigma}{dE_{\text{nr}}}$$

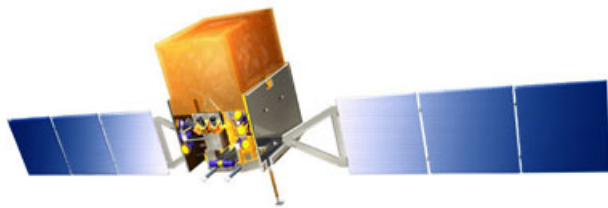
Typical event rates are less than  
**1 event per kg per year**  
A great experimental challenge!



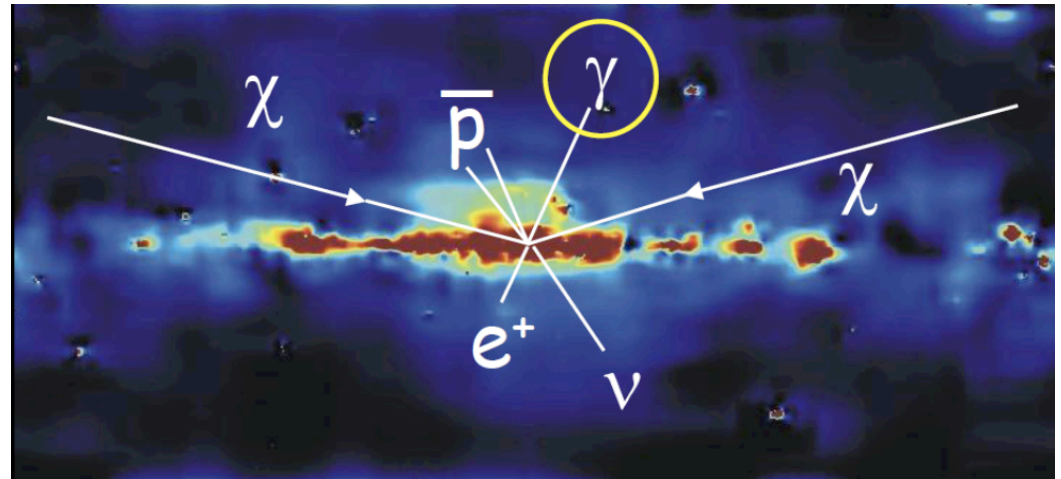
# DM indirect detection



Indirect detection experiments look for the **products of DM annihilation** in regions of **high DM density** (e.g. the galactic center) with satellites, balloons and ground based telescopes.



Difficulties arise from **astrophysical backgrounds** and the DM density profile.

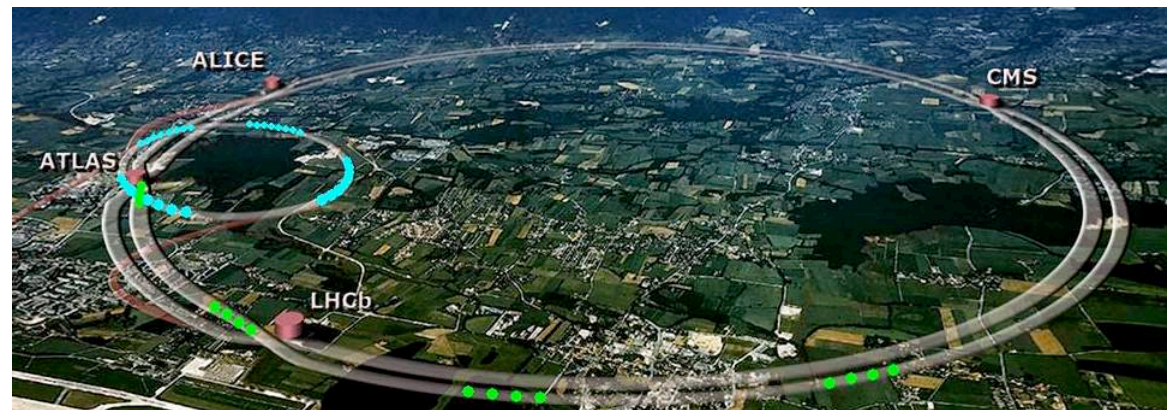
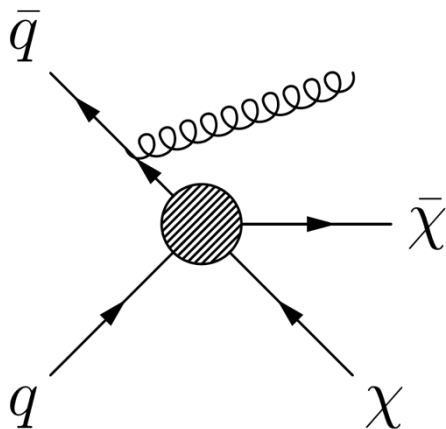




# DM searches at colliders

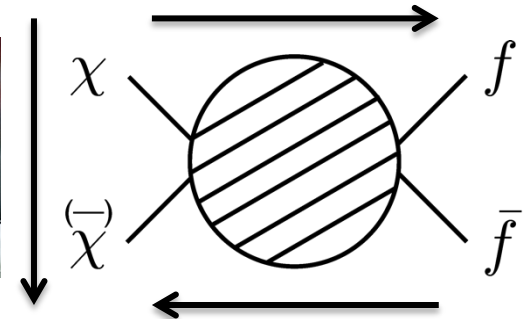


Any DM particles produced at colliders will escape from the detector unnoticed. But if other particles (such as jets) are produced in association with a pair of DM particles, we may observe **large amounts of missing transverse energy**.



# Detecting DM particles

If dark matter particles give a **direct detection signal**, we also expect to see **related processes with distinctive signatures**.

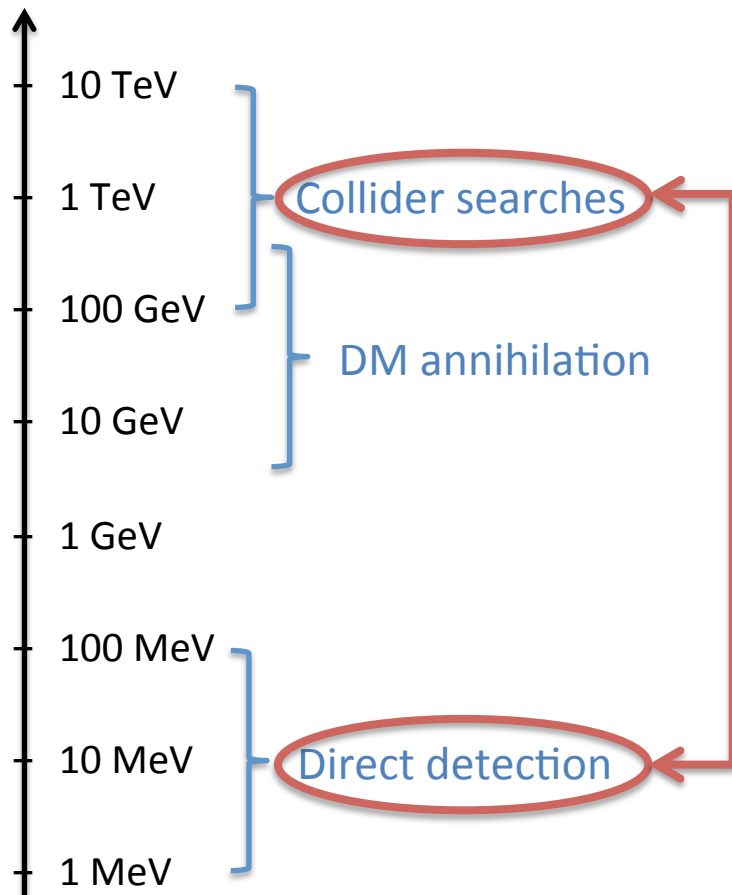


Experiments searching for these signatures can **constrain the direct detection cross section**.



# Separation of scales

Typical momentum transfer



Dark matter direct detection probes the **non-relativistic limit** ( $v_{\text{DM}} \approx 10^{-3}$ ), while the LHC probes the **TeV scale**.

Interactions that look **very similar** at the LHC may look **very different** in direct detection.

# Example

- Assume that DM interacts with quarks via the exchange of a **vector mediator**  $R$  which can couple to the **vector current**  $\chi\gamma^\mu\chi$  or the **axial current**  $\chi\gamma^5\gamma^\mu\chi$  (or a combination).
- At the LHC: **Impossible to distinguish** VC and AC.
- In direct detection:
  - Vector couplings  $\rightarrow$  **Spin-independent**
  - Axial couplings  $\rightarrow$  **Spin-dependent**
  - Mixed couplings  $\rightarrow$  **Momentum suppressed**

# Effective operators

To compare bounds from the LHC to direct detection, we describe interactions between DM and quarks with **effective operators**, e.g.

$$\mathcal{L}_\chi^{\text{eff}} = \frac{1}{\Lambda^2} \bar{\chi} \gamma_\mu \chi \bar{q} \gamma^\mu q$$

This effective operator could arise from **integrating out a vector mediator** with mass  $m_R$  and vector couplings  $g_q$  to quarks and  $g_\chi$  to DM:

$$\Lambda = m_R / \sqrt{g_q g_\chi}$$

# Effective interactions

For  $\mathcal{L}_\chi^{\text{eff}} = \frac{1}{\Lambda^2} \bar{\chi} \gamma_\mu \chi \bar{q} \gamma^\mu q$  the direct detection cross section is given by  $\sigma_p^{\text{SI}} = \frac{f^2 \mu_{\chi n}^2}{\pi \Lambda^4}$ , where  $f = 3$  for  $g_u = g_d$ .

Provided the effective operator remains valid at the LHC, we can use it to calculate the cross section for monojet production.

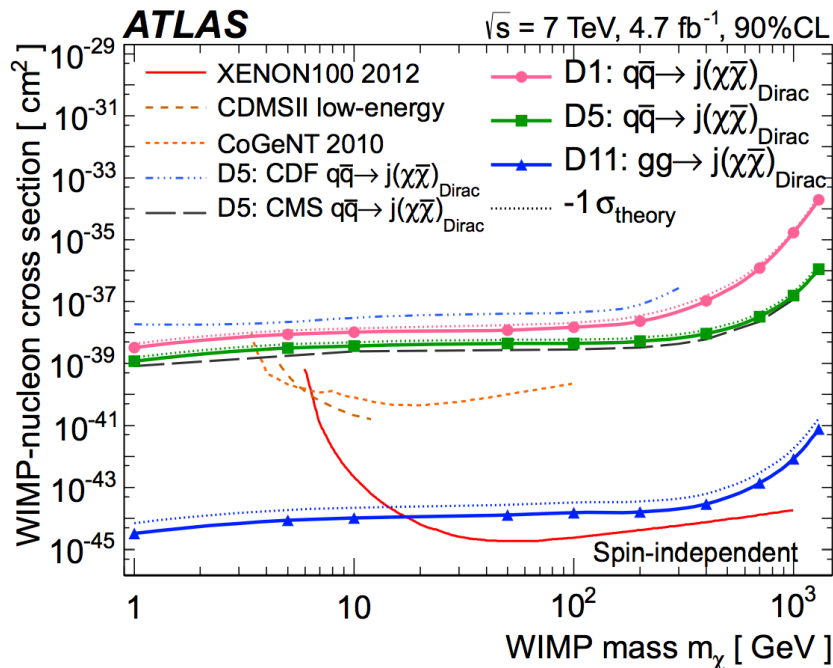
$$\sigma(j + \text{MET}) \sim 1/\Lambda^4 \sim \sigma_p$$

We can *directly* compare LHC searches for dark matter to direct detection experiments

# Monojet searches at the LHC

Search for dark matter candidates and large extra dimensions in events with a jet and missing transverse momentum with the ATLAS detector

arXiv:1210.4491



$M_\chi$ (GeV/c <sup>2</sup> )	Spin-independent	
	$\Lambda$ (GeV)	$\sigma_{\chi N}$ (cm <sup>2</sup> )
0.1	749	$2.90 \times 10^{-41}$
1	751	$8.21 \times 10^{-40}$
10	760	$2.47 \times 10^{-39}$
100	764	$2.83 \times 10^{-39}$
200	736	$3.31 \times 10^{-39}$
300	690	$4.30 \times 10^{-39}$
400	631	$6.15 \times 10^{-39}$
700	455	$2.28 \times 10^{-38}$
1000	302	$1.18 \times 10^{-37}$

CMS Collaboration, arXiv:1206.5663

See also

Goodman et al. arXiv:1005.1286

Bai et al. arXiv:1005.3797

Goodman et al. arXiv:1008.1783

Fox et al. arXiv:1103.0240

Rajaraman et al. arXiv:1108.1196

Fox et al. arXiv:1109.4398

# Problems with perturbativity

- Current monojet searches at CMS & ATLAS probe  $\Lambda \approx 700 \text{ GeV}$ , corresponding to  $\sigma_p \approx 10^{-39} \text{ cm}^2$ .
- To have **perturbativity**, we require  $g_q, g_\chi < (4\pi)^{1/2}$
- From  $\Lambda = m_R / \sqrt{g_q g_\chi}$  we then get  $m_R < 2.5 \text{ TeV}$ .

Fox, Harnik, Kopp, Tsai, arXiv:1109.4398

Fox, Harnik, Kopp, Tsai, arXiv:1103.0240

For collisions with  $\sqrt{s} > 2.5 \text{ TeV}$ , we can no longer rely on an effective operator description, because new physics becomes relevant.



# Problems with unitarity

- For a sensible theory, all predicted probabilities should be **smaller than unity**.
- More formally, we require **partial wave unitarity**

$$|a^J(s)| = \left| \frac{1}{32\pi} \int_{-1}^1 d(\cos \theta) P_J(\cos \theta) \mathcal{M}(s, \cos \theta) \right| < 1$$

- For the effective operator from above  $\mathcal{M} = 2\sqrt{3} \frac{s}{\Lambda^2}$  leading to  **$\sqrt{s} < 2.7 \Lambda \approx 1.9 \text{ TeV}$** .  
Shoemaker, Vecchi, arXiv:1112.5457  
Fox, Harnik, Primulando, Yu, arXiv:1203.1662

For collisions with  $\sqrt{s} > 1.9 \text{ TeV}$ , the effective operator makes nonsensical predictions.

# Resonant production

- Effective operators may *not* be valid at the LHC
- It is quite possible that the mediator mass is comparable to LHC energies ( $m_R \sim \text{TeV}$ )
- The LHC can produce such a mediator *on-shell*:  
$$\sigma(j + \text{MET}) \sim \sigma(pp \rightarrow R + j) \times \text{BR}(R \rightarrow \text{invisible})$$
- As a consequence, the monojet cross section is *no longer proportional* to the direct detection cross-section and the analysis is more involved.

# How to extract a bound

$$\sigma_p \sim \frac{\mu_{\chi n}^2}{\pi} \frac{g_q^2 g_\chi^2}{m_R^4}$$

$g_q$ : Coupling to quarks  
 $g_\chi$ : Coupling to the DM particle  
 $m_R$ : Mass of the mediator  
 $\mu_{\chi n}$ : Reduced mass

$$\Gamma(R \rightarrow \chi \bar{\chi}) \sim \frac{m_R}{12\pi} g_\chi^2$$

$$\Gamma(R \rightarrow \chi \bar{\chi}) \leq \Gamma_R \times \text{BR}(R \rightarrow \text{inv})$$

$$\sigma_p \lesssim 12 \frac{\mu_{\chi n}^2 \Gamma_R}{m_R^5} g_q^2 \cdot \text{BR}(R \rightarrow \text{inv})$$

More difficult to constrain

Constrained by monojet searches

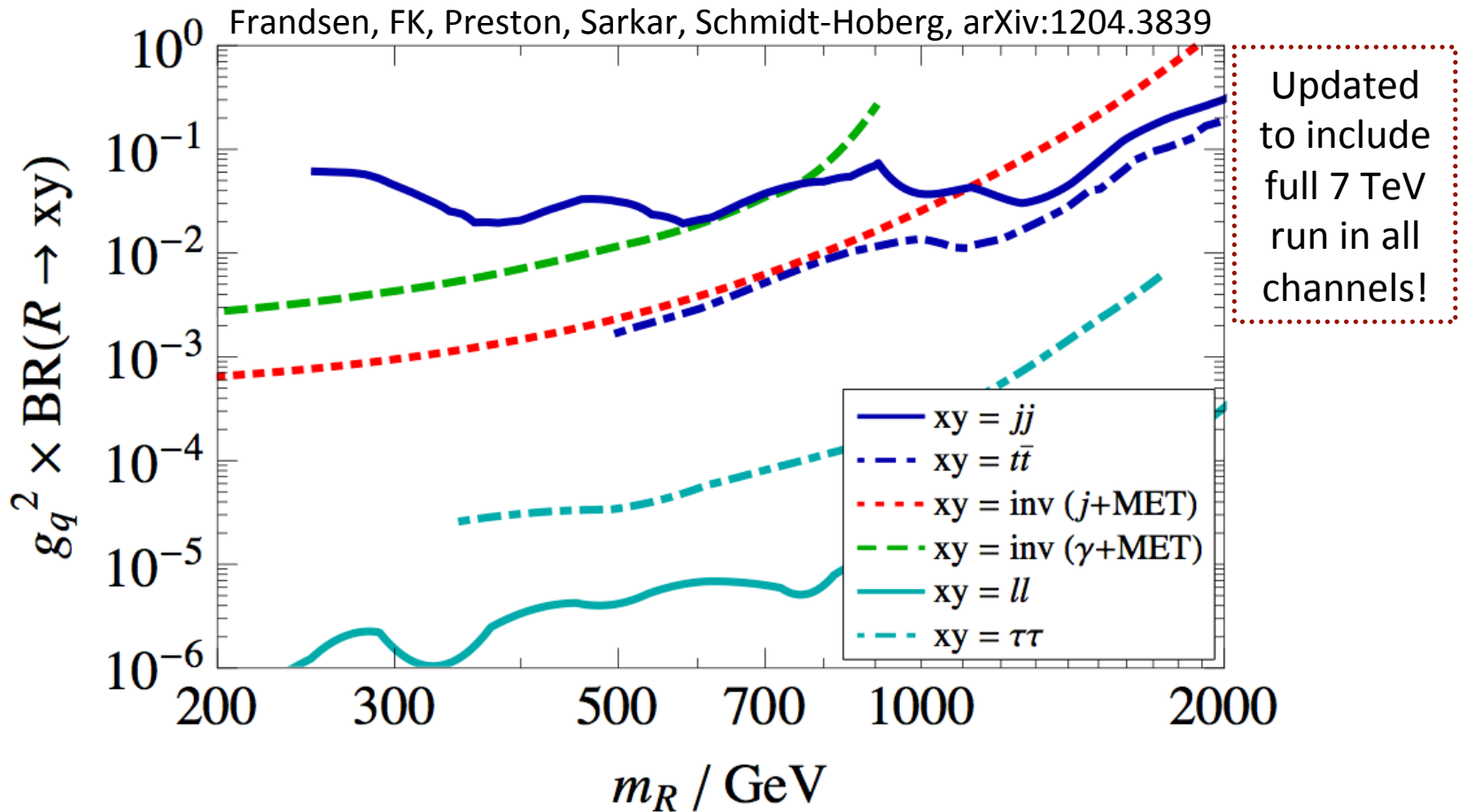
# Decay channels

$R$  can decay into fermions, bosons  
*and* new hidden sector states

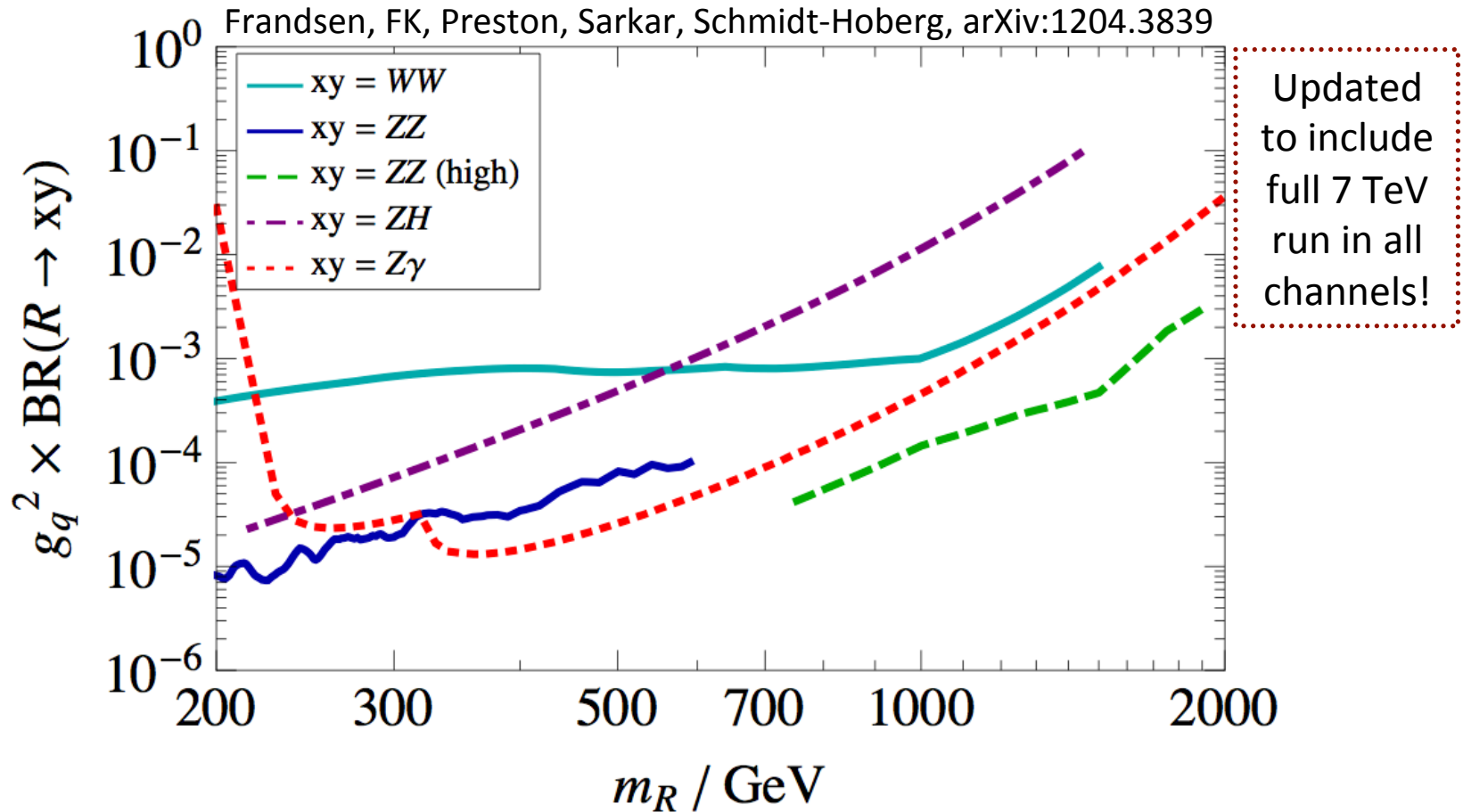
$$\begin{aligned}\Gamma_R = & \Gamma^{\chi\bar{\chi}} + \sum_q \Gamma^{q\bar{q}} + \sum_l \Gamma^{l\bar{l}} + \sum_\nu \Gamma^{\nu\bar{\nu}} \\ & + \Gamma^{W^+W^-} + \Gamma^{ZZ} + \Gamma^{\gamma Z} + \Gamma^{ZH} \\ & + \Gamma^X\end{aligned}$$

*All* of these channels can be constrained by the LHC!

# Constraints: Fermions

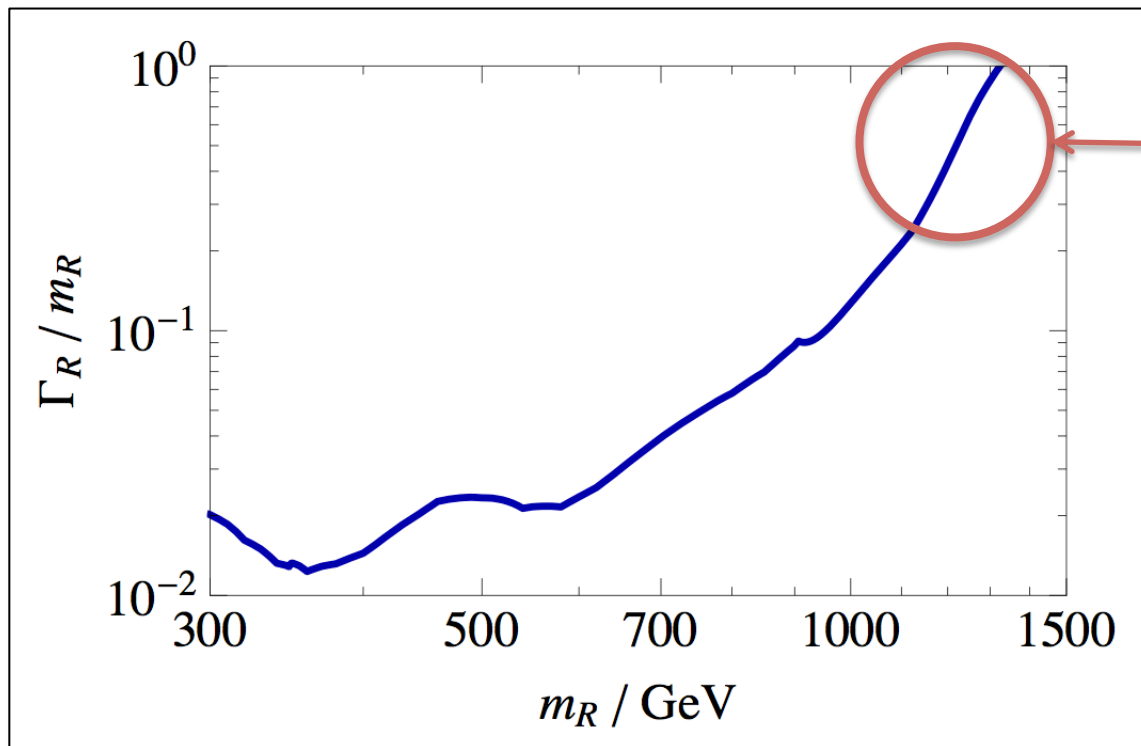


# Constraints: Bosons



# Combined Constraints

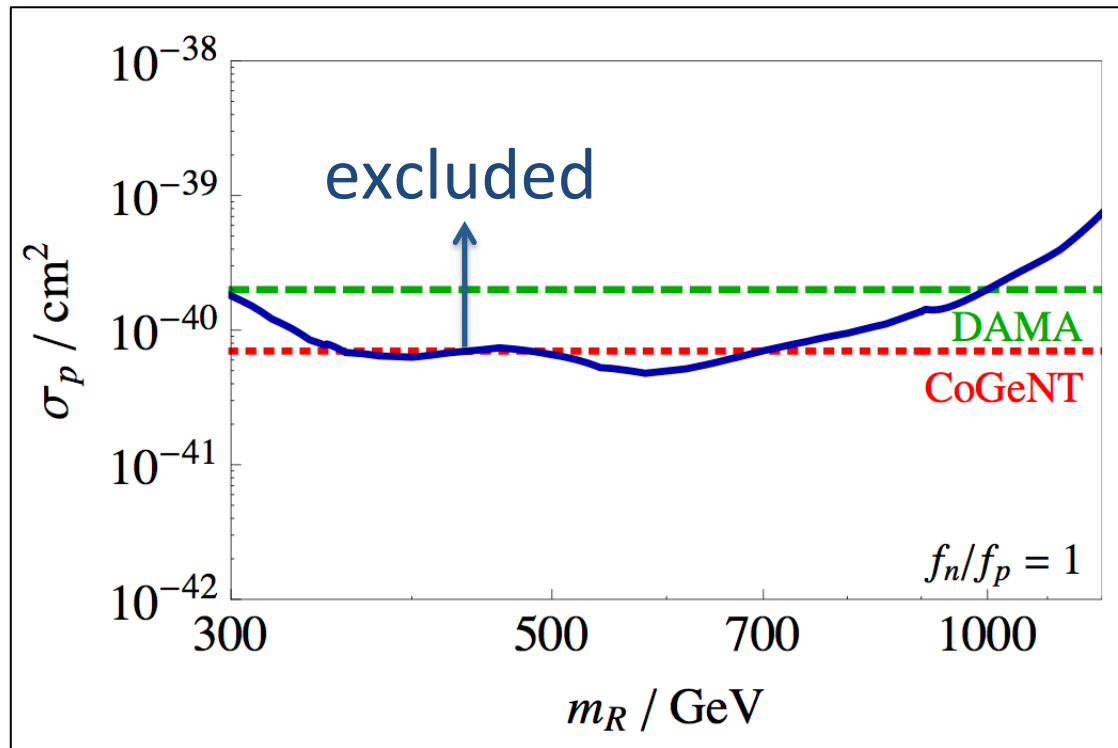
- If  $R$  decays only into SM particles or invisible states, we can obtain a bound on  $\Gamma_R$ .



Narrow-width approximation no longer valid

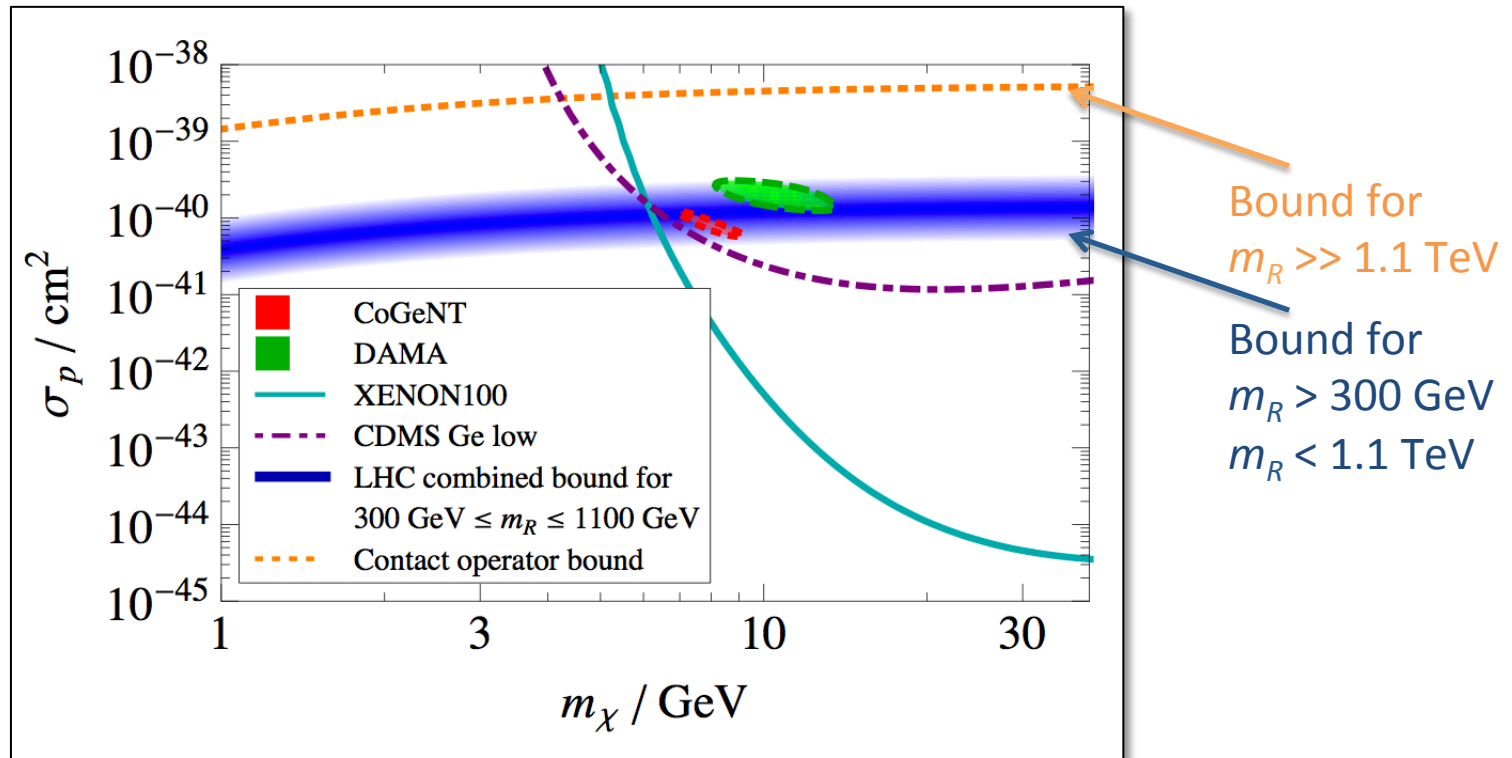
# Direct detection limit

$$\sigma_p \lesssim 12 \frac{\mu_{\chi n}^2 \Gamma_R}{m_R^5} g_q^2 \cdot \text{BR}(R \rightarrow \text{inv})$$





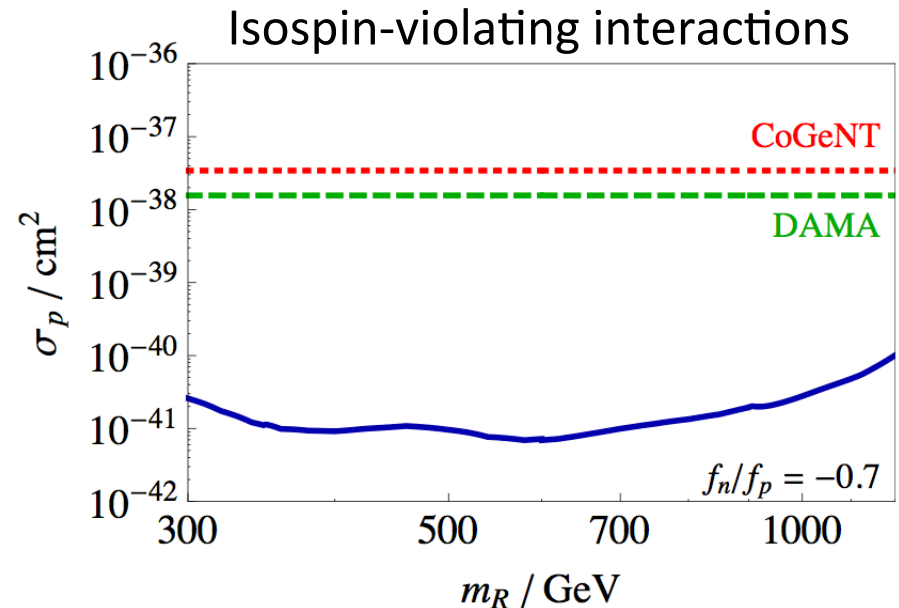
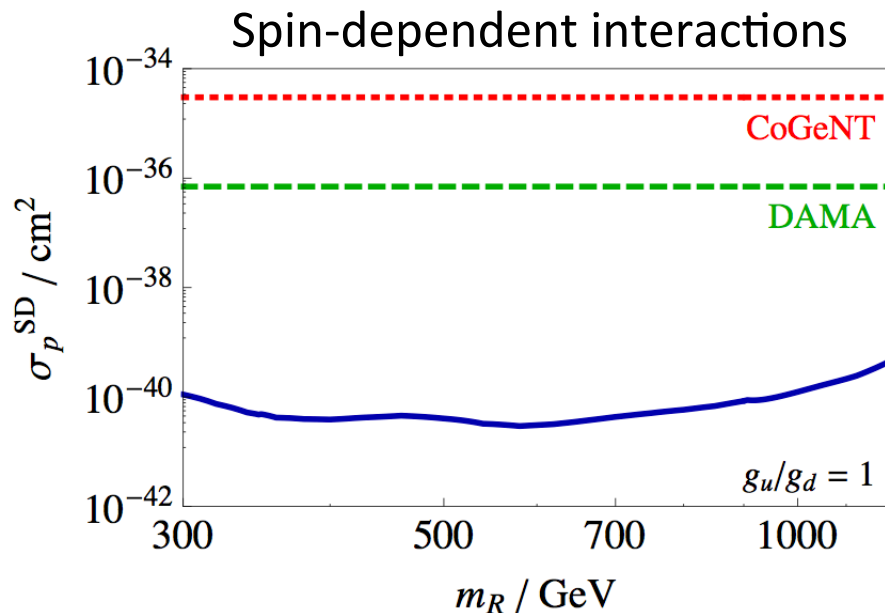
# Direct detection limit



There are strong constraints on the direct detection cross section for vector mediators with  $m_R < 1.1 \text{ TeV}$ .

# Non-standard interactions

- Collider bounds are largely independent of low-energy effects (e.g. nuclear coherence).
- Very strong bounds arise if  $\sigma_p$  is suppressed.



# Possible caveats

1. If the mediator is **lighter than 300 GeV** it becomes very difficult to constrain  $\text{BR}(R \rightarrow qq)$ .
2. If the **DM mass** is comparable to the mediator mass, decays of  $R$  into  $\chi\chi$  are suppressed.
3. If  $R$  can decay into **new hidden sector states** with complicated decay modes,  $\Gamma_R$  can be large.
4. If  $g_q \ll g_\chi$  the production of  $R$  at LHC is insufficient to constrain  $\Gamma_R$ .

How Useful Are Effective Operators?

# Operator mixing



# Operator mixing

- To calculate direct detection cross sections, we must **evolve** all effective operators from the TeV scale **down to the hadronic scale**.
- In the process, **new interactions may be induced at loop-level**, leading to **additional operators**, which are absent (or small) at the TEV scale.
- A full calculation should include the **mixing of all relevant effective operators** under Renormalisation Group evolution.

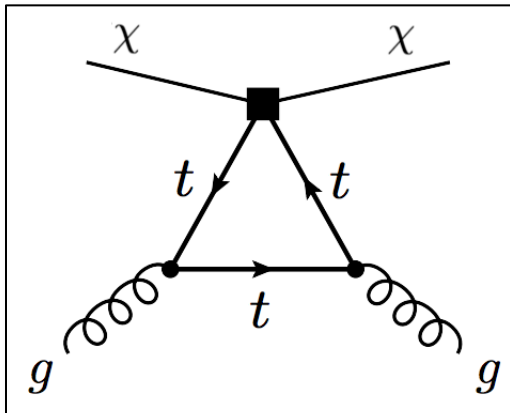
# Example

- Consider the operator which may arise from

$$\mathcal{L}_\chi^{\text{eff}} = \frac{m_q}{\Lambda^3} \bar{q}q \bar{\chi}\chi$$

integrating out a scalar mediator with quark couplings proportional to the quark mass  $m_q$ .

- For energies below the top quark mass  $m_t$ , the top quark can be integrated out to give an effective interaction between DM and gluons:



$$\mathcal{L}_\chi^{\text{eff}} = \frac{\alpha_s}{4\Lambda_g^3} G_{\mu\nu}^a G^{a\mu\nu} \bar{\chi}\chi$$

# Example

- More formally, the operator  $\mathcal{O}_q = C_q m_q \bar{\chi} \chi \bar{q} q$  induces the operator  $\mathcal{O}_G = C_G \bar{\chi} \chi G^{a, \mu\nu} G_{\mu\nu}^a$

with  $C_G(m_t) = -\frac{\alpha_s(m_t)}{12\pi} (1 + \delta_t) C_t(m_t)$

$\delta_t = 11\alpha_s(m_t)/(4\pi)$

- A similar threshold correction arises for the bottom quark below  $m_b$  and for the charm quark below  $m_c$ .

# Direct detection cross-section

- To calculate the direct detection cross-section, we now need to evaluate  $\langle A | \mathcal{O}_q | A \rangle$  and  $\langle A | \mathcal{O}_G | A \rangle$  where  $|A\rangle$  is the target nucleus state. One finds

$$\langle A | \mathcal{O}_q | A \rangle \simeq 2m_N A f_{Tq}^N F_{\text{Helm}}(\bar{q}) \mathcal{C}_q(\mu)$$

and

$$\langle A | \mathcal{O}_G | A \rangle \simeq -2 \frac{8\pi}{9\alpha_s(\mu)} m_N A f_{TG}^N F_{\text{Helm}}(\bar{q}) \mathcal{C}_G(\mu)$$

$$\sigma_{\text{SI}}^\chi = \frac{\mu_A^2}{\pi} |f^\chi|^2 \quad \text{with} \quad f^\chi = \sum_q \langle A | \mathcal{O}_q^\chi | A \rangle + \langle A | \mathcal{O}_G^\chi | A \rangle$$



# LHC bounds

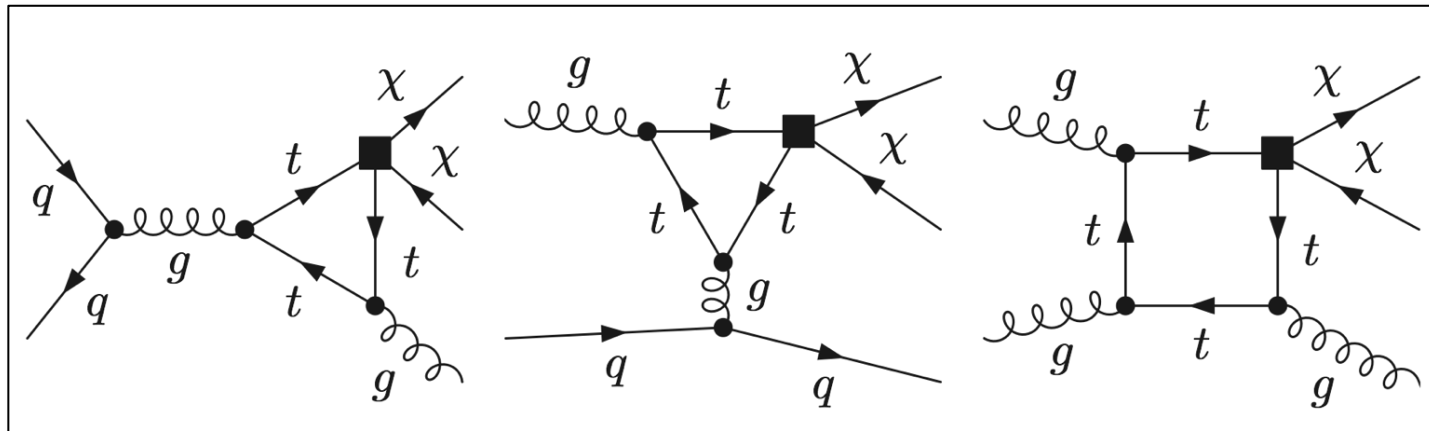
- What is the correct procedure to analyse bounds from monojet searches for the scalar operator?

$$\mathcal{L}_\chi^{\text{eff}} = \frac{m_q}{\Lambda^3} \bar{q}q \bar{\chi}\chi$$

- Tree-level cross section are small, because there are **no heavy quarks** in the initial state.
- We **cannot use effective DM-gluon interactions**, because the typical energies ( $\sqrt{s}$ ,  $p_T$ , ...) are large compared to  $m_t$  (not to mention  $m_b$  and  $m_c$ ).

# LHC bounds

- For an accurate analysis, we must include the full energy dependence of the heavy quark loops using FormCalc + LoopTools (or MCFM).



- While charm and bottom quarks are negligible, top quark loops give the dominant contribution.

# Implementation in MCFM

- Our analysis is based on **analytical results** for the process  $p + p \rightarrow H + j \rightarrow \tau^+ \tau^- + j$ .

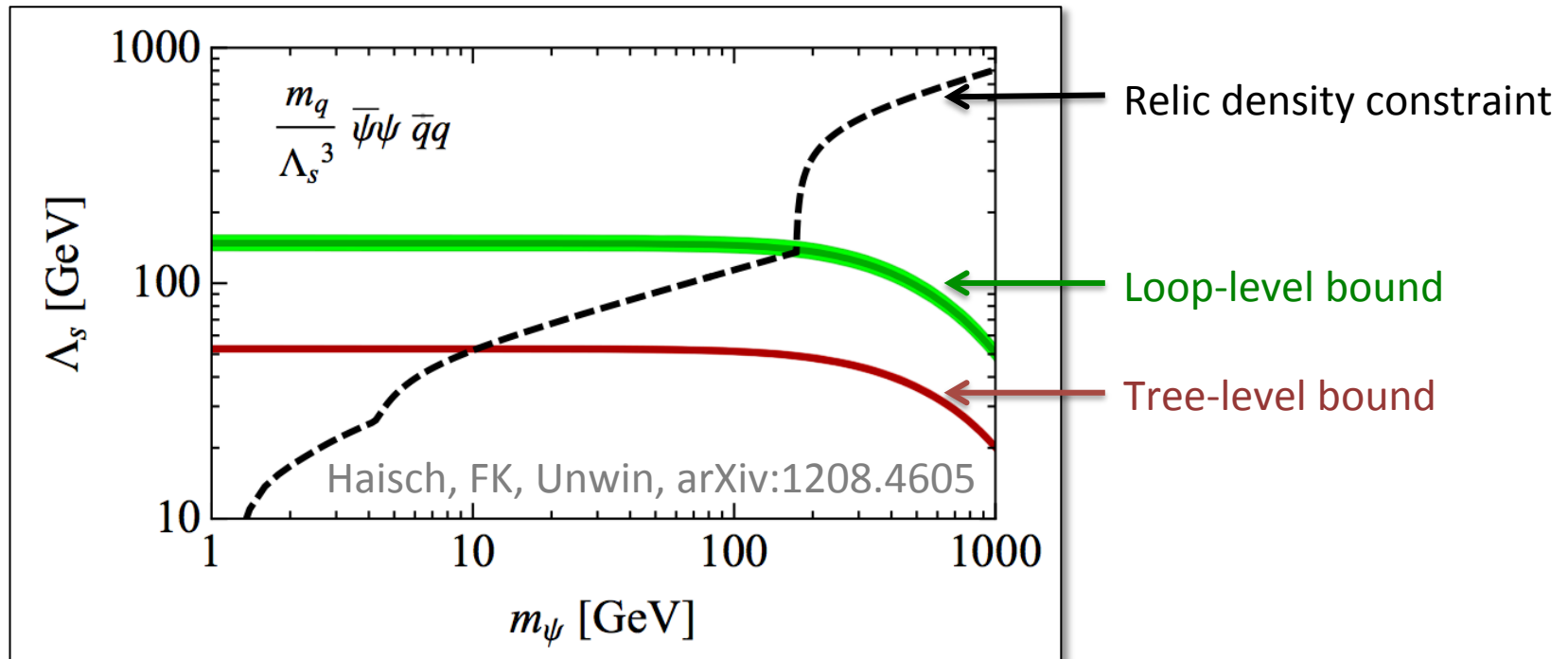
Ellis *et al.*, Nucl.Phys. B297, 221 (1988)

- These results can be **extended to the case of an off-shell mediator** by replacing  $m_H$  with the invariant mass of the DM pair (equal to  $s + t + u$ ).
- Because the primary jet has very large  $p_T$ , **effects of parton showering and hadronisation** are expected to be small.

Bai, Fox, Harnik, arXiv:1005.3797

Choudalakis, arXiv:1110.5295

# LHC bounds



- Including loop-level processes increases predicted monojet cross sections by a factor of around 500.
- Width of the bands reflect scale uncertainties.

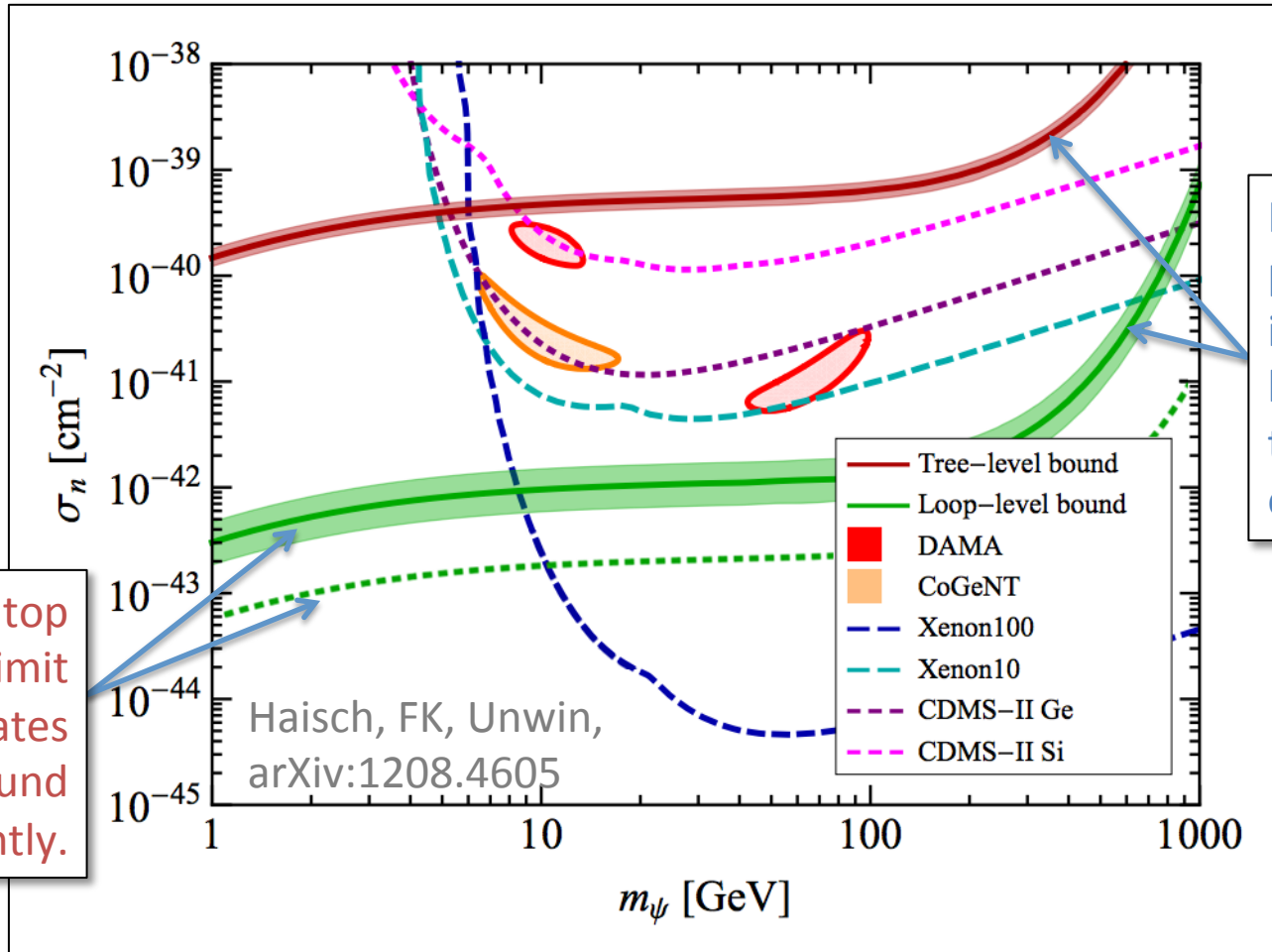
# How heavy are top quarks?

- It is tempting to consider only the limit of infinitely heavy top quark and use the effective DM-gluon interaction

$$\mathcal{O}_G = \mathcal{C}_G \bar{\chi}\chi G^{a,\mu\nu} G_{\mu\nu}^a$$

- We find that this approximation overestimates cross sections by a factor of 3 for small DM masses.
- For large DM masses, the error grows rapidly, reaching a factor of 40 at  $m_\psi = 1$  TeV.
- For accurate results it is essential to allow on-shell top quarks with finite mass in the loops.

# LHC bounds



Heavy top quark limit overestimates the bound significantly.

Including loop processes improves the bounds by more than two orders of magnitude

# Pseudoscalar interactions

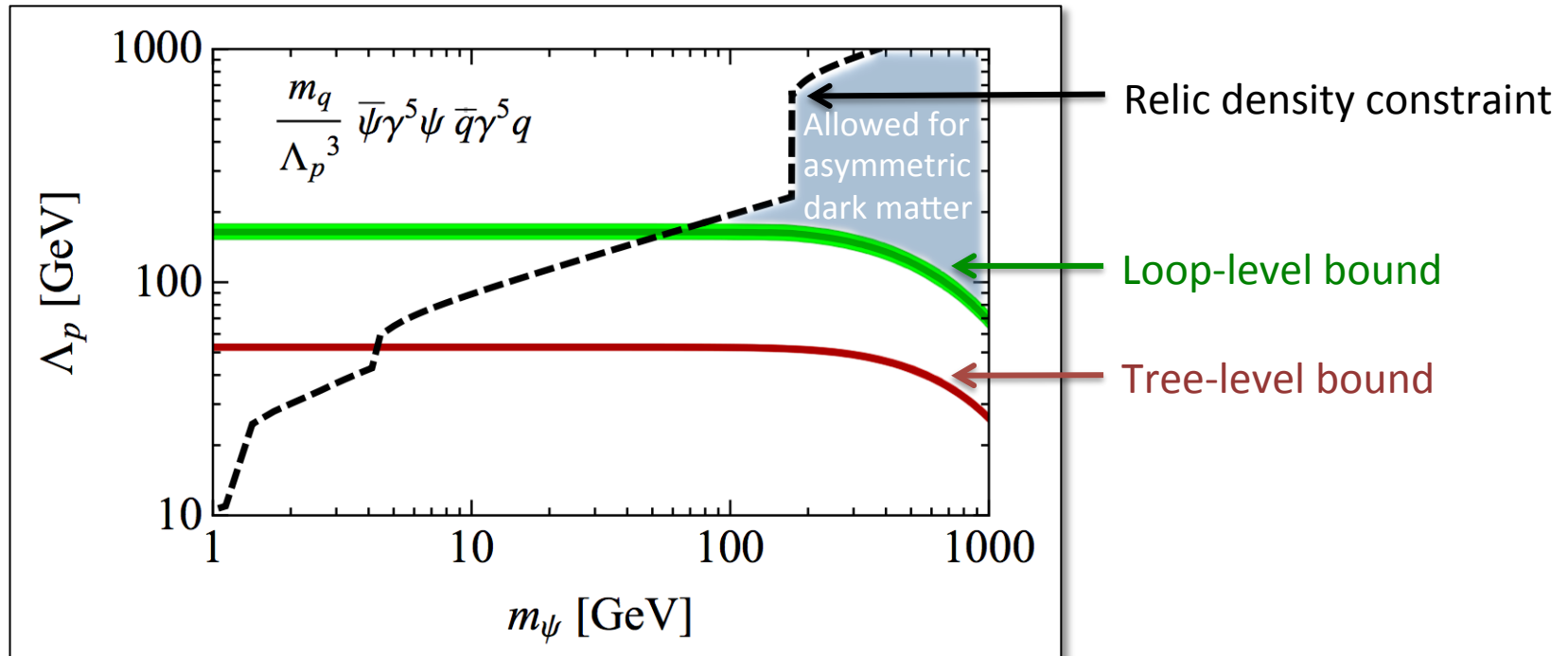
- For the pseudoscalar operator

$$\mathcal{O}_p^\psi = \frac{m_q}{\Lambda_p^3} \bar{q} \gamma^5 q \bar{\psi} \gamma^5 \psi$$

detection cross sections are **spin-dependent and in addition suppressed by  $q^4 / m_N^4$** .

- Consequently, no relevant constraints on  $\Lambda_p$  arise from direct detection experiments.
- At the LHC scalar and pseudoscalar interactions look very similar, so we obtain strong constraints on  $\Lambda_p$ .

# Pseudoscalar interactions



- Imposing that DM is not overproduced leads to the bound  $m_\psi > 60$  GeV (Majorana fermion:  $m_\psi > 85$  GeV).



# Conclusions

- At typical LHC energies effective operators may be insufficient to interpret monojet bounds, because the **intermediate particles can be on-shell**.
- *Example 1:* Resonant production of vector mediators  
Heavy mediators ( $m_R \geq 300$  GeV) can be tested and constrained by current LHC data.
- *Example 2:* Heavy-quark loops for scalar mediators  
Loop-level processes significantly enhance the monojet cross-section, but one needs to include the full top-mass dependence for accurate results.