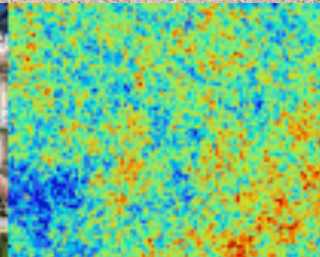
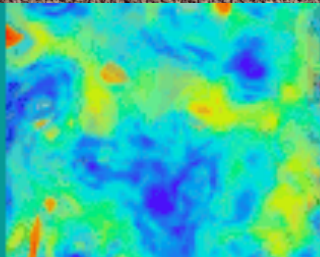


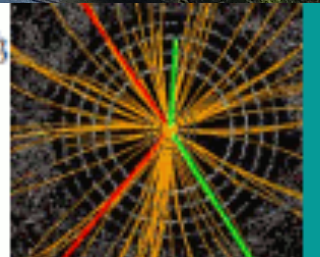


Baryogenesis via leptonic phase transition

Ye-Ling Zhou, Southampton, 11 Nov 2019



$$\begin{aligned} & \Lambda_3^D \\ & t - 2m_\pi^2) \tilde{B}(m_\pi^2, t) + \frac{1}{4} \tilde{B} \\ & + \Lambda_3^D \\ & 2) \tilde{B}(m_\pi^2, t) \end{aligned}$$

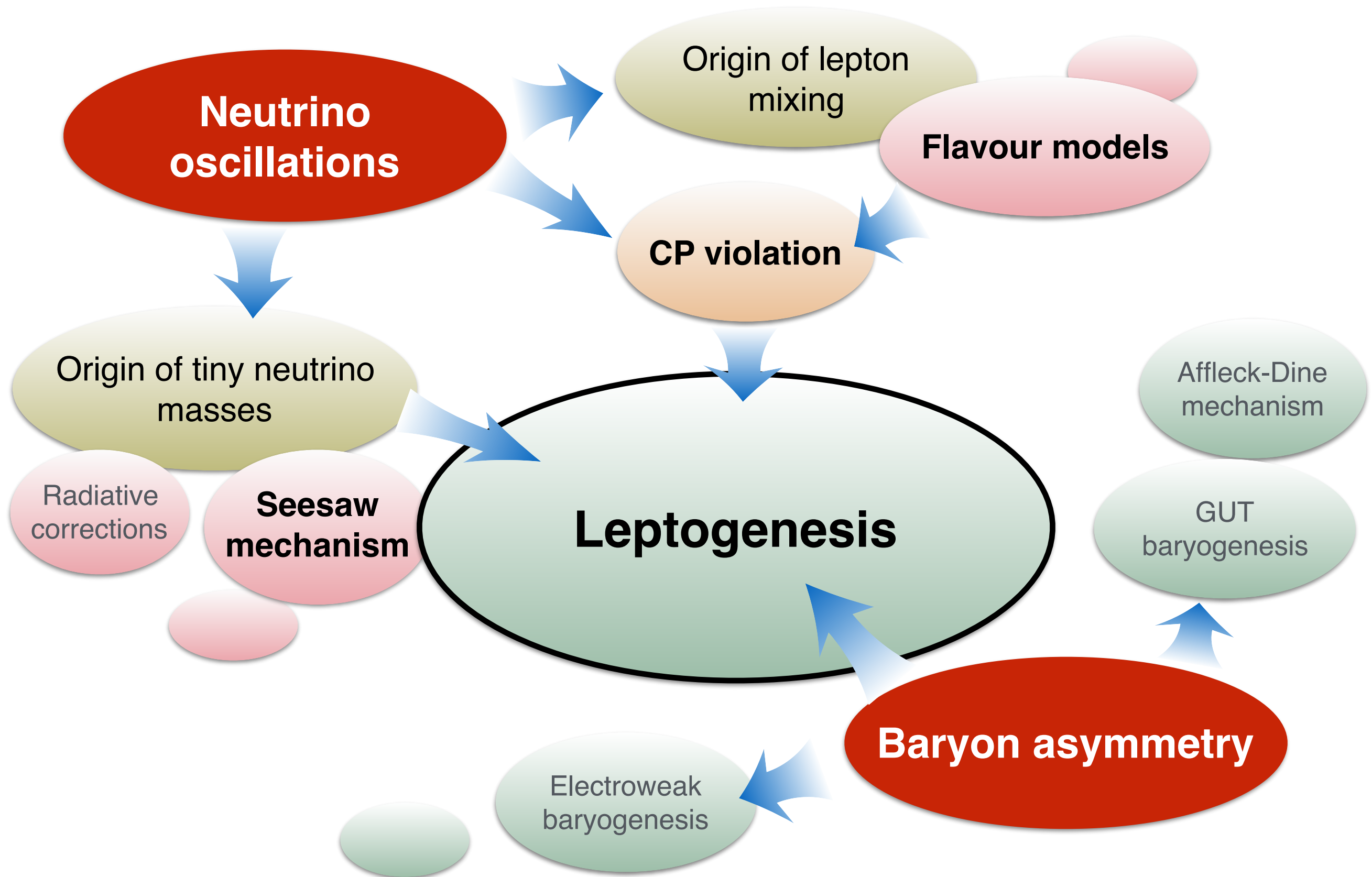


Introduction

**Neutrino
oscillations**

Baryon asymmetry

Introduction

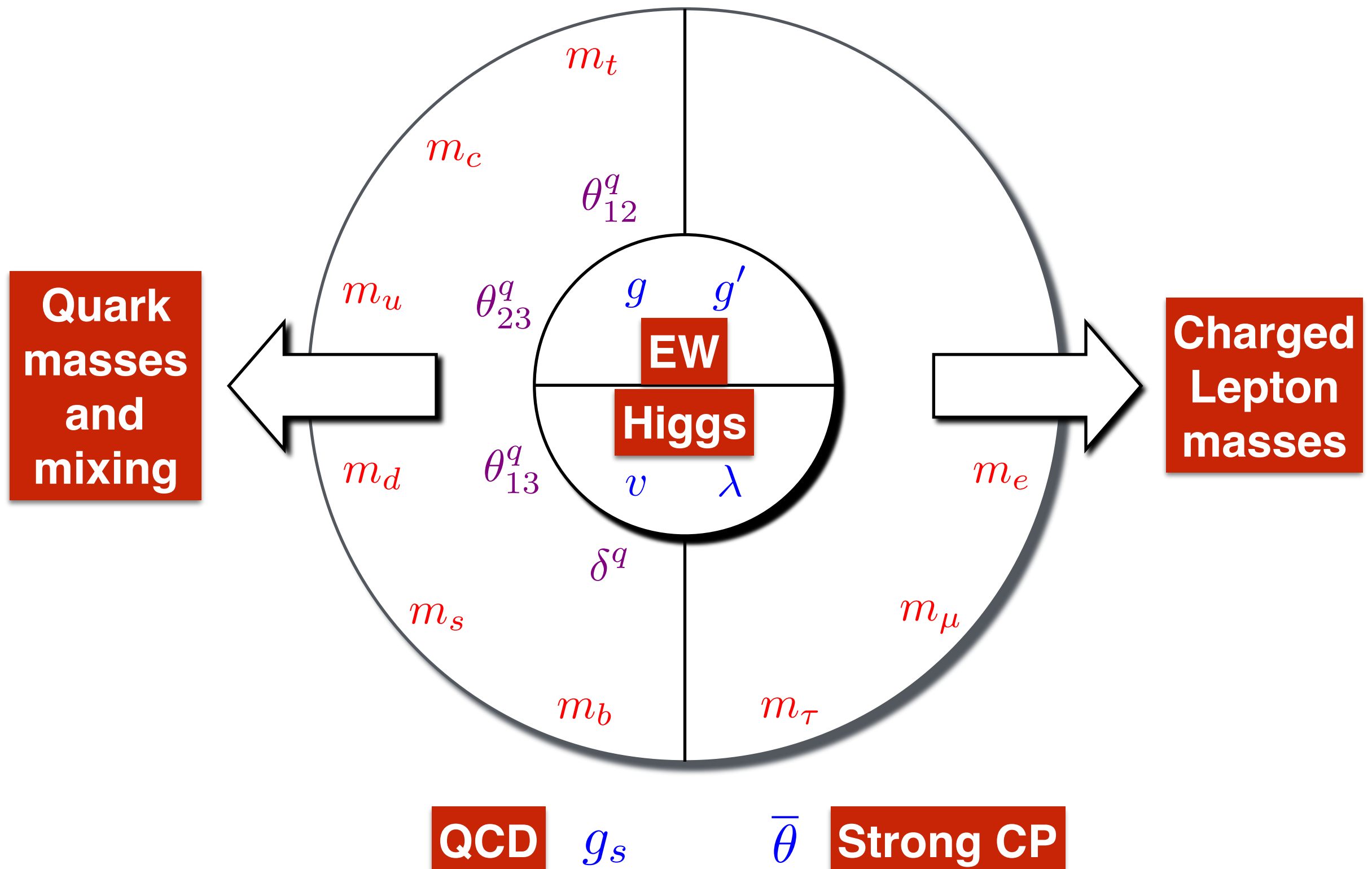


Outline

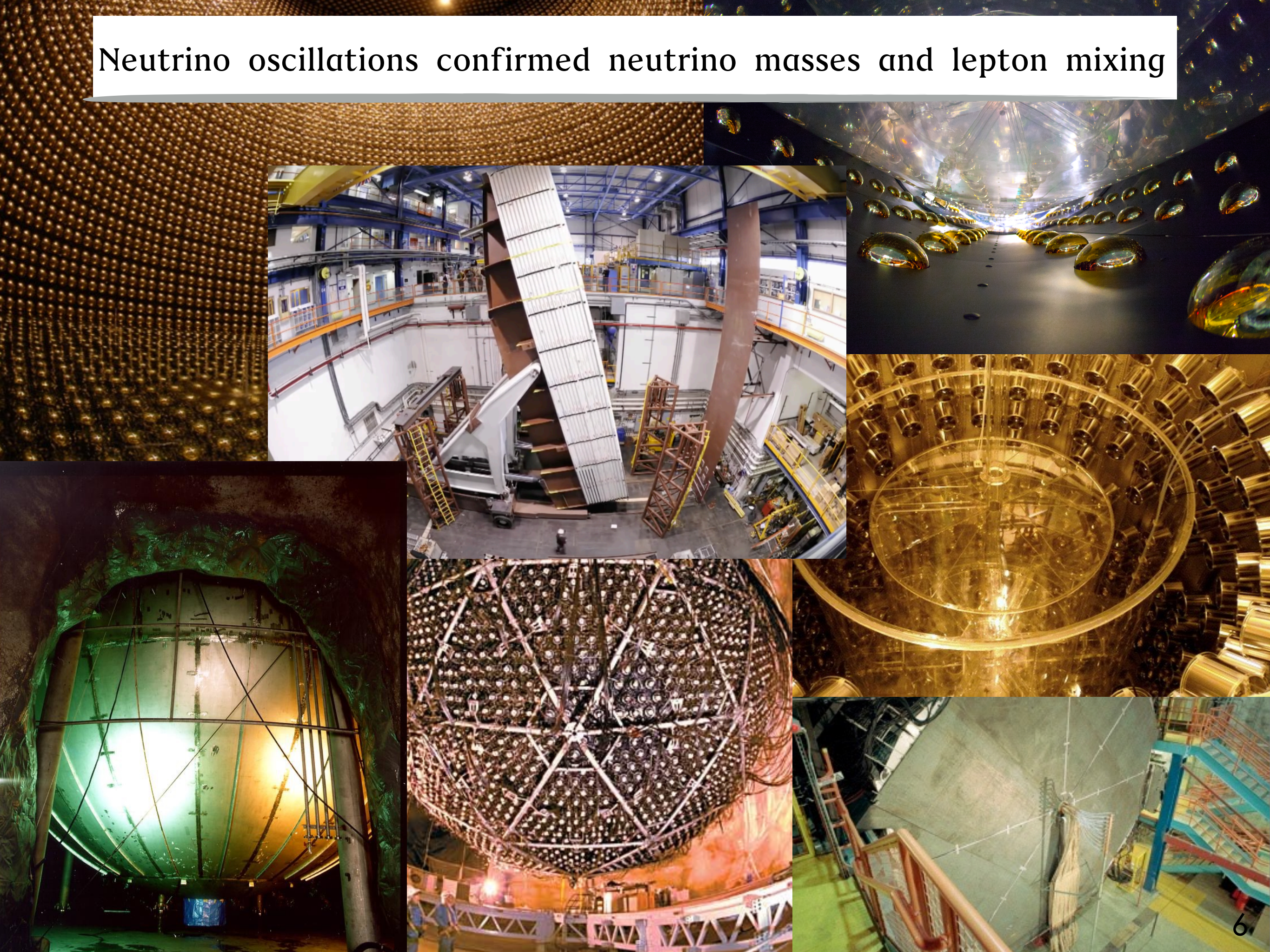
- *Review of neutrino mass and mixing*
 - —motivation of spacetime-varying Weinberg operator
- *Leptogenesis via phase transition*
 - —intuitive picture based on semi-classical approach
 - —quantitative result based on closed-time-path approach

SM (massless neutrinos)

17+2 free parameters



Neutrino oscillations confirmed neutrino masses and lepton mixing



Neutrino masses and lepton mixing

$$|\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle$$

Flavour eigenstates **Mass eigenstates**

$$m_1, m_2, m_3$$

$$\Delta m_{21}^2 = m_2^2 - m_1^2 \quad \Delta m_{31}^2 = m_3^2 - m_1^2$$

Pontecorvo–Maki–Nakagawa–Sakata (PMNS) matrix

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & & \\ & e^{i\frac{\alpha_{21}}{2}} & \\ & & e^{i\frac{\alpha_{31}}{2}} \end{pmatrix}$$

Atmospheric

Reactor

Solar

Majorana

Mixing angles

$$\theta_{12}, \theta_{23}, \theta_{13}$$

$$c_{ij} = \cos \theta_{ij}, \quad s_{ij} = \sin \theta_{ij}$$

CP-violating phases

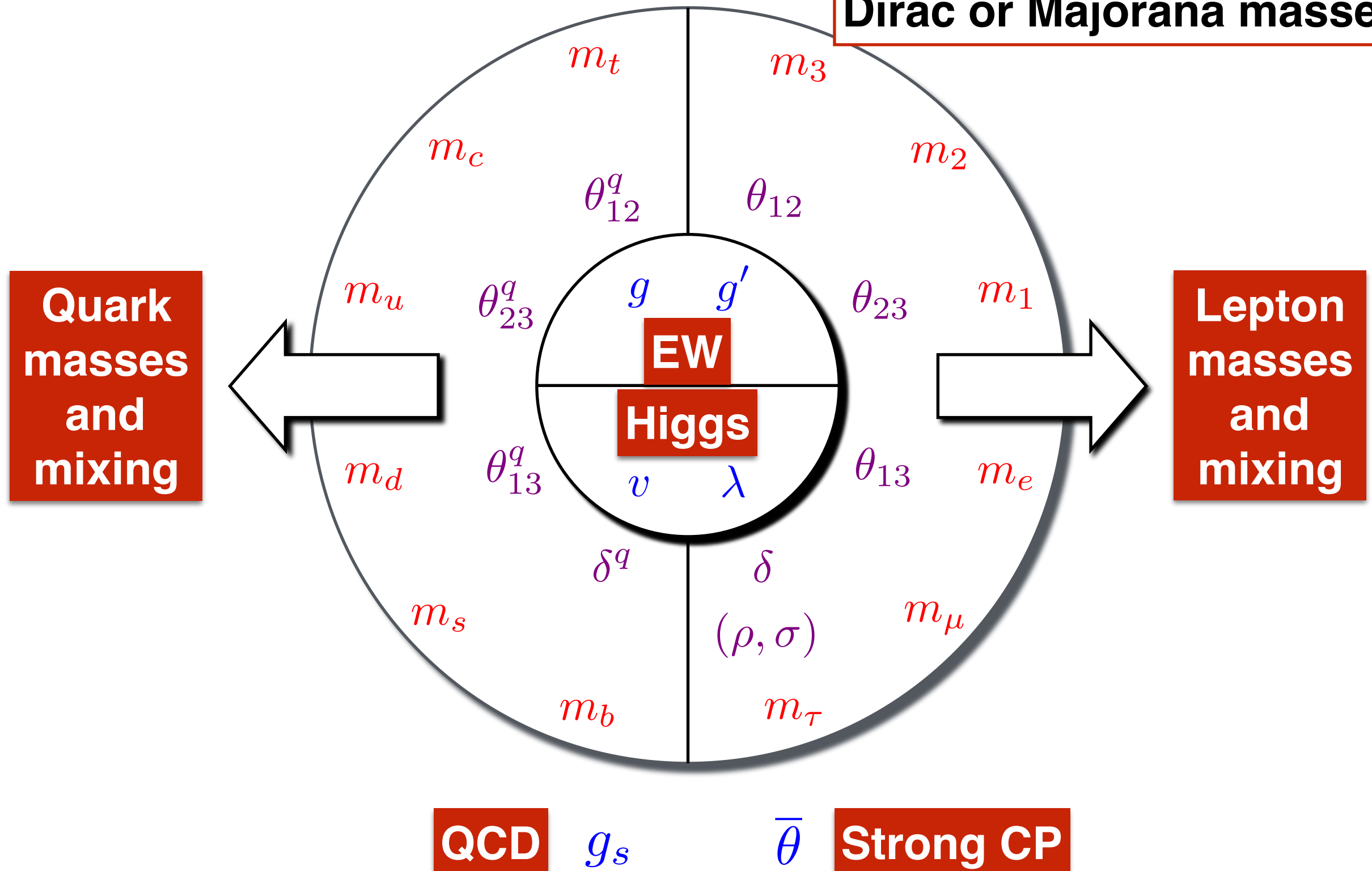
Dirac-type δ

Majorana-type α_{21}, α_{31}

SM + massive neutrinos

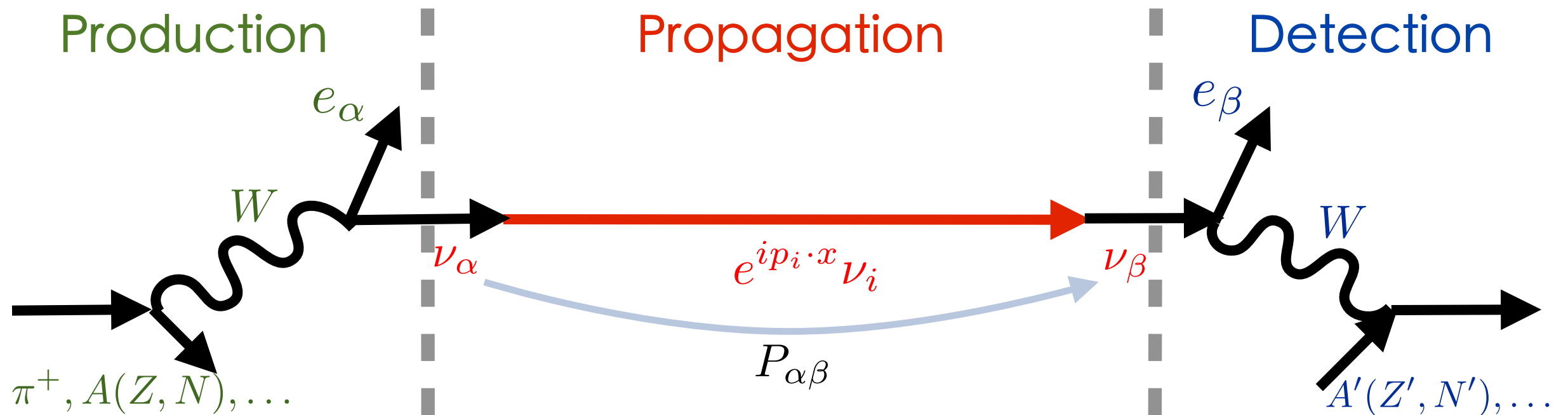
24(26)+2 free parameters

Neutrinos may take
Dirac or Majorana masses



Neutrino oscillations

Active neutrino oscillation in neutrino oscillation experiments



$$|\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle \quad |\nu_\alpha(x)\rangle = \sum_i U_{\alpha i}^* e^{ip_i \cdot x} |\nu_i\rangle \quad \langle \nu_\beta | \nu_\alpha(x) \rangle = \sum_i U_{\alpha i}^* U_{\beta i} e^{ip_i \cdot x}$$

probability

$$P(\nu_\alpha \rightarrow \nu_\beta) = |\langle \nu_\beta | \nu_\alpha(x) \rangle|^2$$

$$P(\nu_\alpha \rightarrow \nu_\beta) - P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta) =$$

CP asymmetry

$$\sum_{i \neq j} \text{Im} \left\{ \exp \left(-i \int_0^t \frac{\Delta m_{ij}^2}{2E} dt \right) \right\} \times \text{Im} \{ U_{\alpha i} U_{\beta i}^* U_{\alpha j}^* U_{\beta j} \}$$

$$\alpha \neq \beta$$

Kinetic contribution

Interaction contribution

Neutrino oscillations

NuFIT 4.1 (2019)

		Normal Ordering (best fit)		Inverted Ordering ($\Delta\chi^2 = 6.2$)	
		bfp $\pm 1\sigma$	3σ range	bfp $\pm 1\sigma$	3σ range
without SK atmospheric data	$\sin^2 \theta_{12}$	$0.310^{+0.013}_{-0.012}$	$0.275 \rightarrow 0.350$	$0.310^{+0.013}_{-0.012}$	$0.275 \rightarrow 0.350$
	$\theta_{12}/^\circ$	$33.82^{+0.78}_{-0.76}$	$31.61 \rightarrow 36.27$	$33.82^{+0.78}_{-0.76}$	$31.61 \rightarrow 36.27$
	$\sin^2 \theta_{23}$	$0.558^{+0.020}_{-0.033}$	$0.427 \rightarrow 0.609$	$0.563^{+0.019}_{-0.026}$	$0.430 \rightarrow 0.612$
	$\theta_{23}/^\circ$	$48.3^{+1.1}_{-1.9}$	$40.8 \rightarrow 51.3$	$48.6^{+1.1}_{-1.5}$	$41.0 \rightarrow 51.5$
	$\sin^2 \theta_{13}$	$0.02241^{+0.00066}_{-0.00065}$	$0.02046 \rightarrow 0.02440$	$0.02261^{+0.00067}_{-0.00064}$	$0.02066 \rightarrow 0.02461$
	$\theta_{13}/^\circ$	$8.61^{+0.13}_{-0.13}$	$8.22 \rightarrow 8.99$	$8.65^{+0.13}_{-0.12}$	$8.26 \rightarrow 9.02$
	$\delta_{CP}/^\circ$	222^{+38}_{-28}	$141 \rightarrow 370$	285^{+24}_{-26}	$205 \rightarrow 354$
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.39^{+0.21}_{-0.20}$	$6.79 \rightarrow 8.01$	$7.39^{+0.21}_{-0.20}$	$6.79 \rightarrow 8.01$
	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.523^{+0.032}_{-0.030}$	$+2.432 \rightarrow +2.618$	$-2.509^{+0.032}_{-0.030}$	$-2.603 \rightarrow -2.416$

Origin of neutrino masses

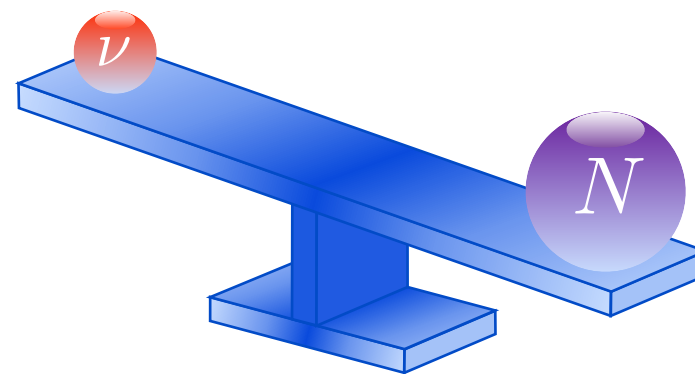
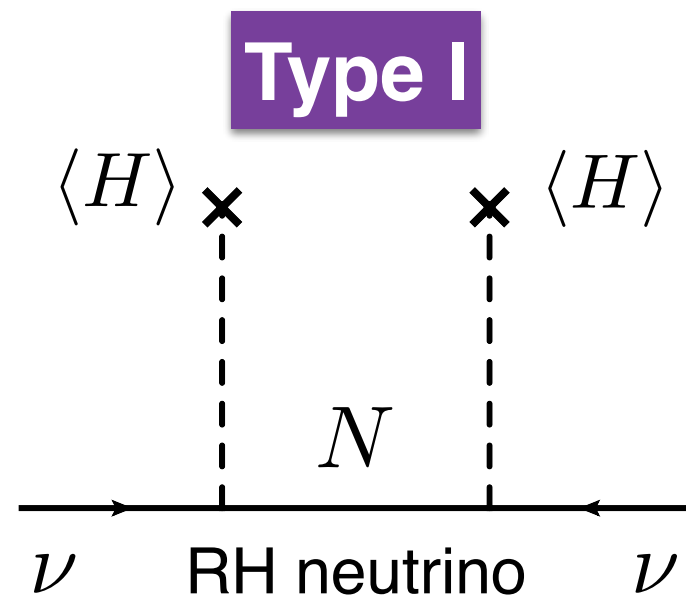
- Weinberg Operator

$$\mathcal{L}_W = \frac{\lambda_{\alpha\beta}}{\Lambda} \ell_{\alpha L} H C \ell_{\beta L} H + \text{h.c.}$$

Lepton number violation

Majorana masses

- Seesaw mechanism

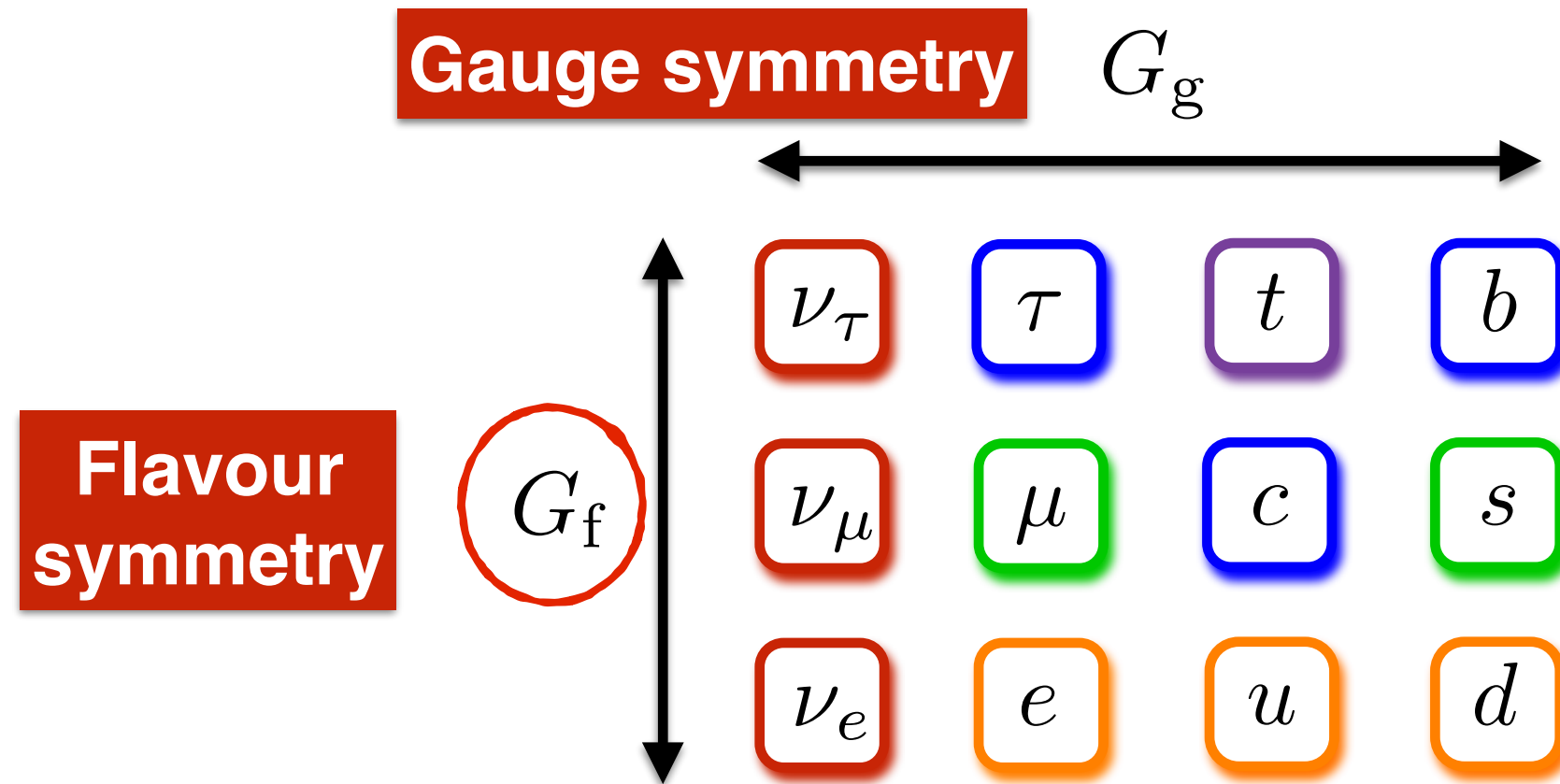


$$-\mathcal{L} = y \bar{\ell} H N + \frac{1}{2} m_N \bar{N}^c N + \text{h.c.}$$

$$m_D = y \langle H \rangle \quad m_\nu = -\frac{m_D^2}{m_N}$$

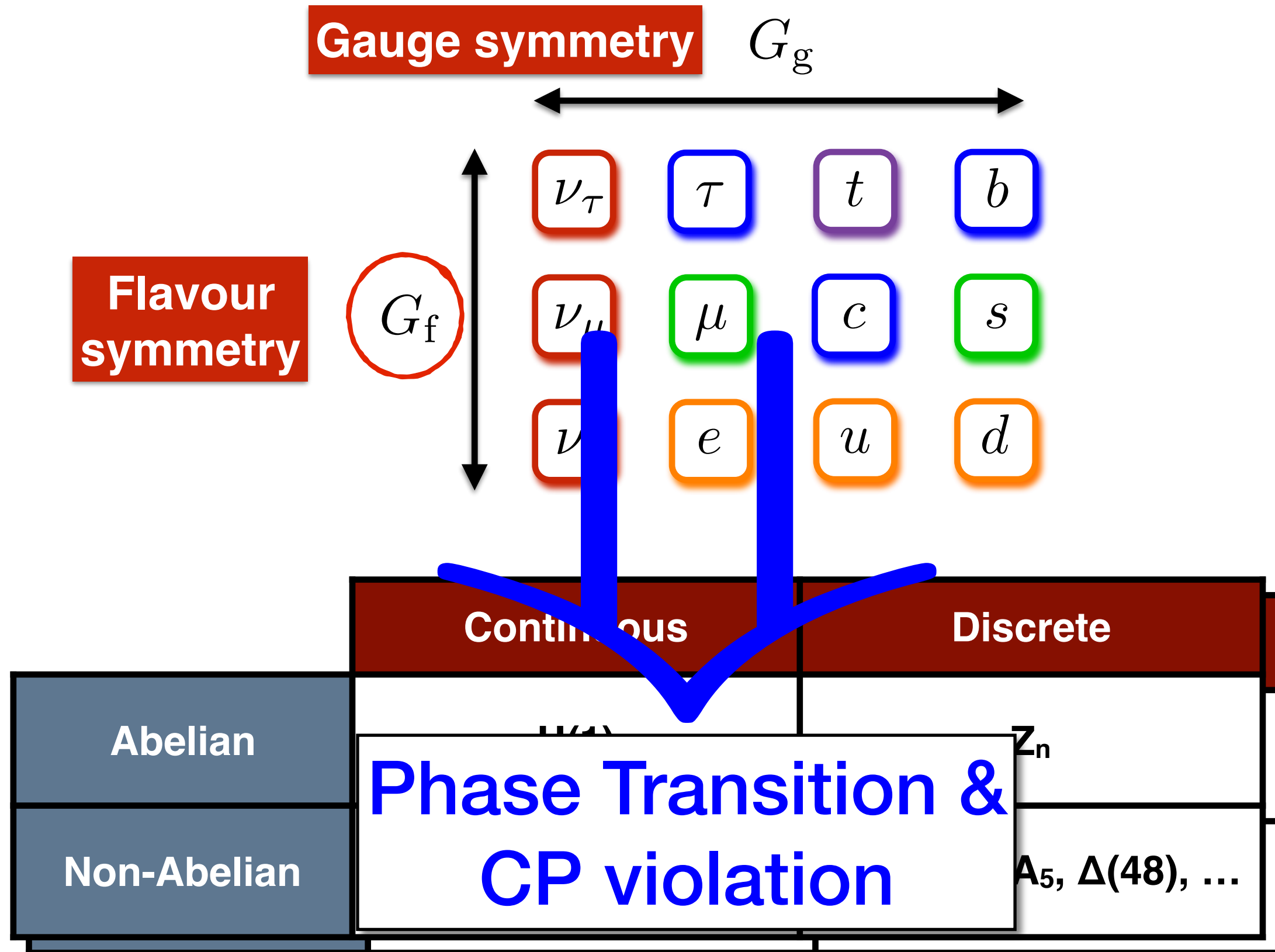
- $U(1)_{B-L}$, Left Right Symm Model, GUT, ...

Origin of lepton flavour mixing



	Continuous	Discrete
Abelian	$U(1)$	Z_n
Non-Abelian	$SU(3), SO(3), \dots$	$A_4, S_4, T', A_5, \Delta(48), \dots$

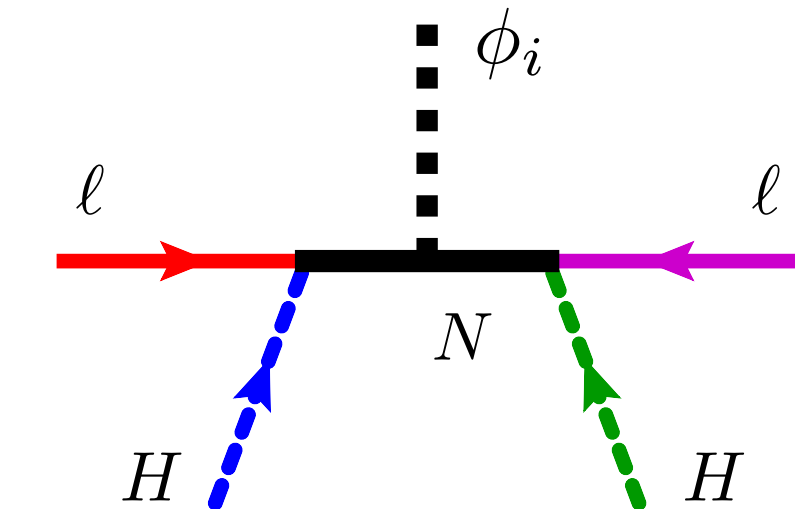
Origin of lepton flavour mixing



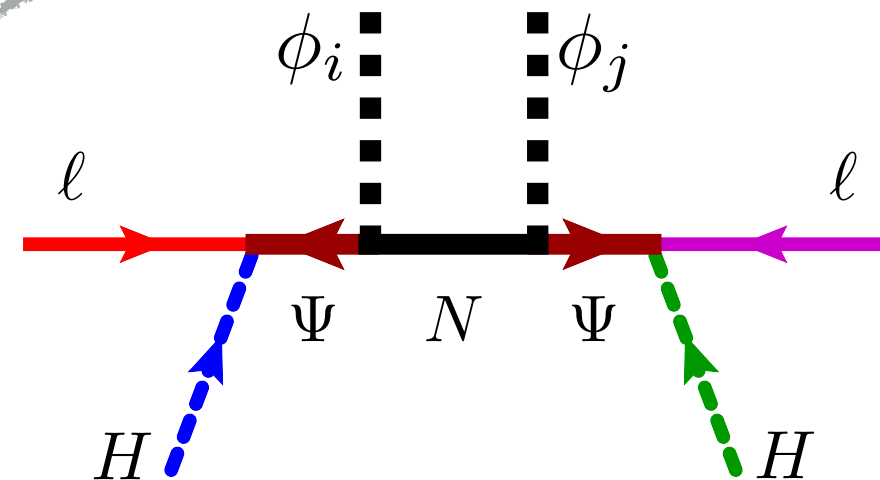
Spacetime-varying Weinberg operator

- UV completion

Option 1:
varying RH neutrino mass



Option 2:
varying Yukawa coupling



Ψ : vector-like fermion

- After the decouple of heavy fermions

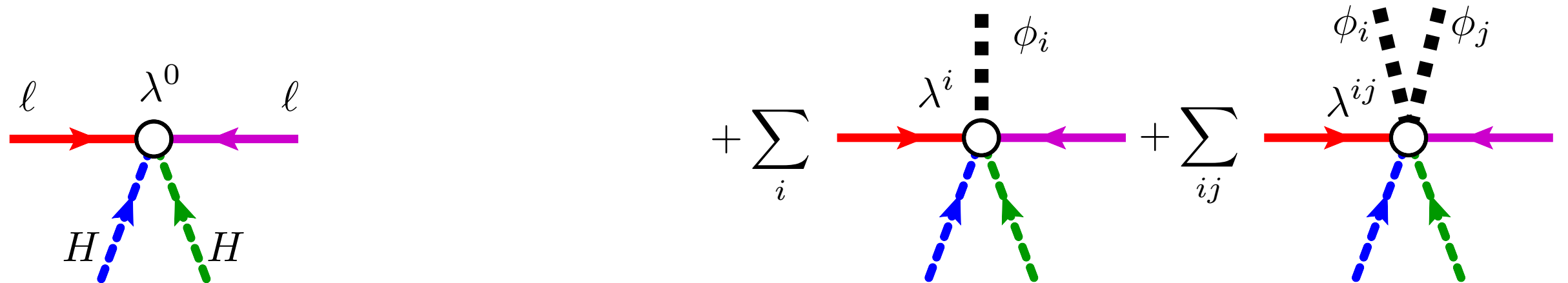
$$\mathcal{L}_W = \frac{\lambda_{\alpha\beta}}{\Lambda} \ell_{\alpha L} H C \ell_{\beta L} H + \frac{\lambda_{\alpha\beta}^*}{\Lambda} \overline{\ell_{\alpha L}} H^* C \overline{\ell_{\beta L}} H^*,$$

$$\lambda_{\alpha\beta} = \lambda_{\alpha\beta}^0 + \sum_{i=1}^n \lambda_{\alpha\beta}^i \frac{\phi_i}{v_{\phi_i}} + \sum_{i,j=1}^n \lambda_{\alpha\beta}^{ij} \frac{\phi_i}{v_{\phi_i}} \frac{\phi_j}{v_{\phi_j}} + \dots$$

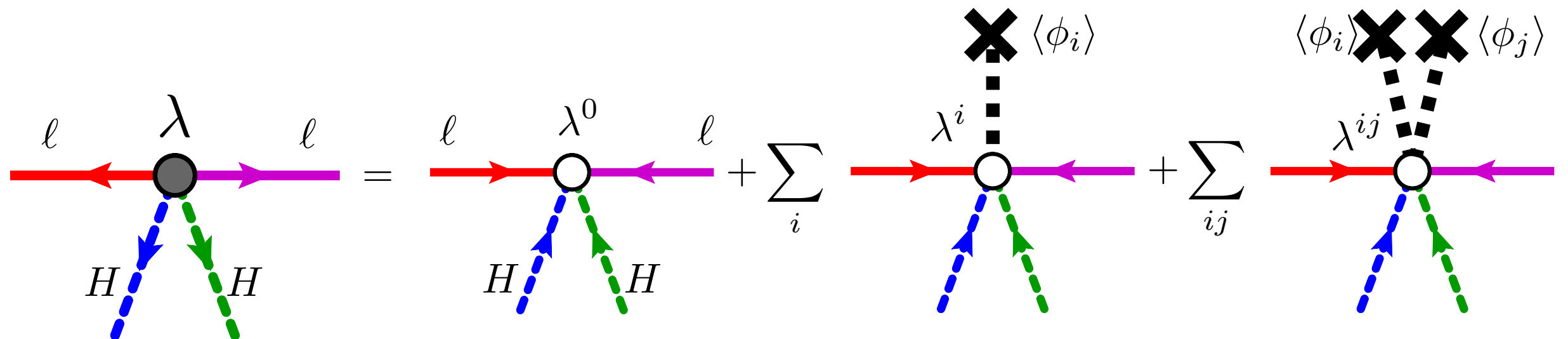
Assuming phase
transition temperature
lower than the mass
scale of heavy fermions

Spacetime-varying Weinberg operator

- Weinberg operator before phase transition



- Weinberg operator after phase transition

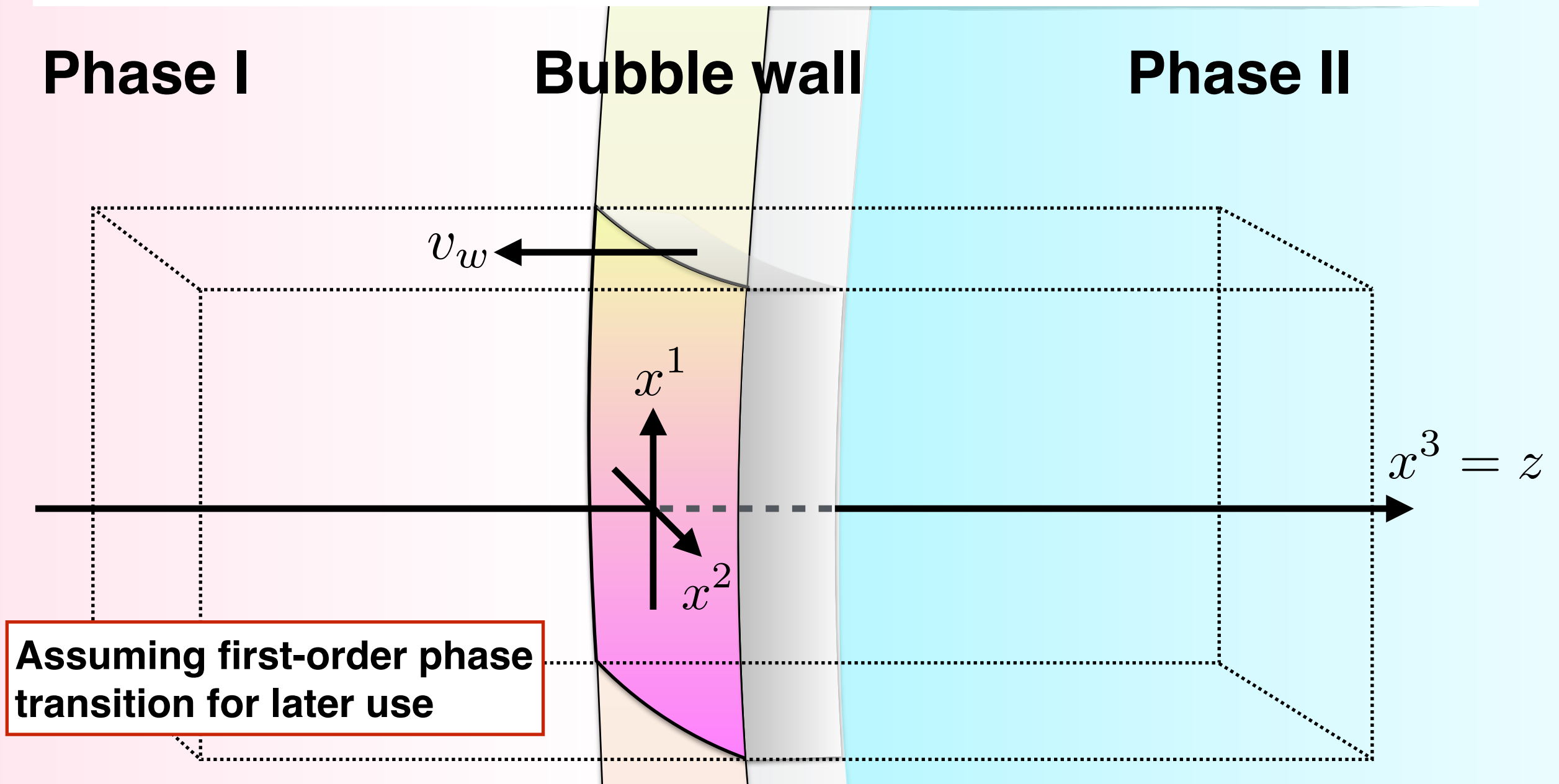


Spacetime-varying Weinberg operator

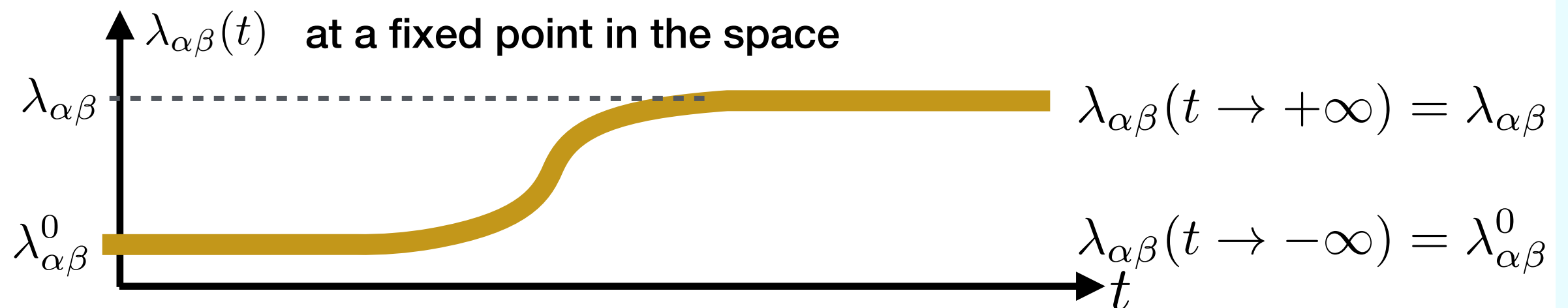
Phase I

Bubble wall

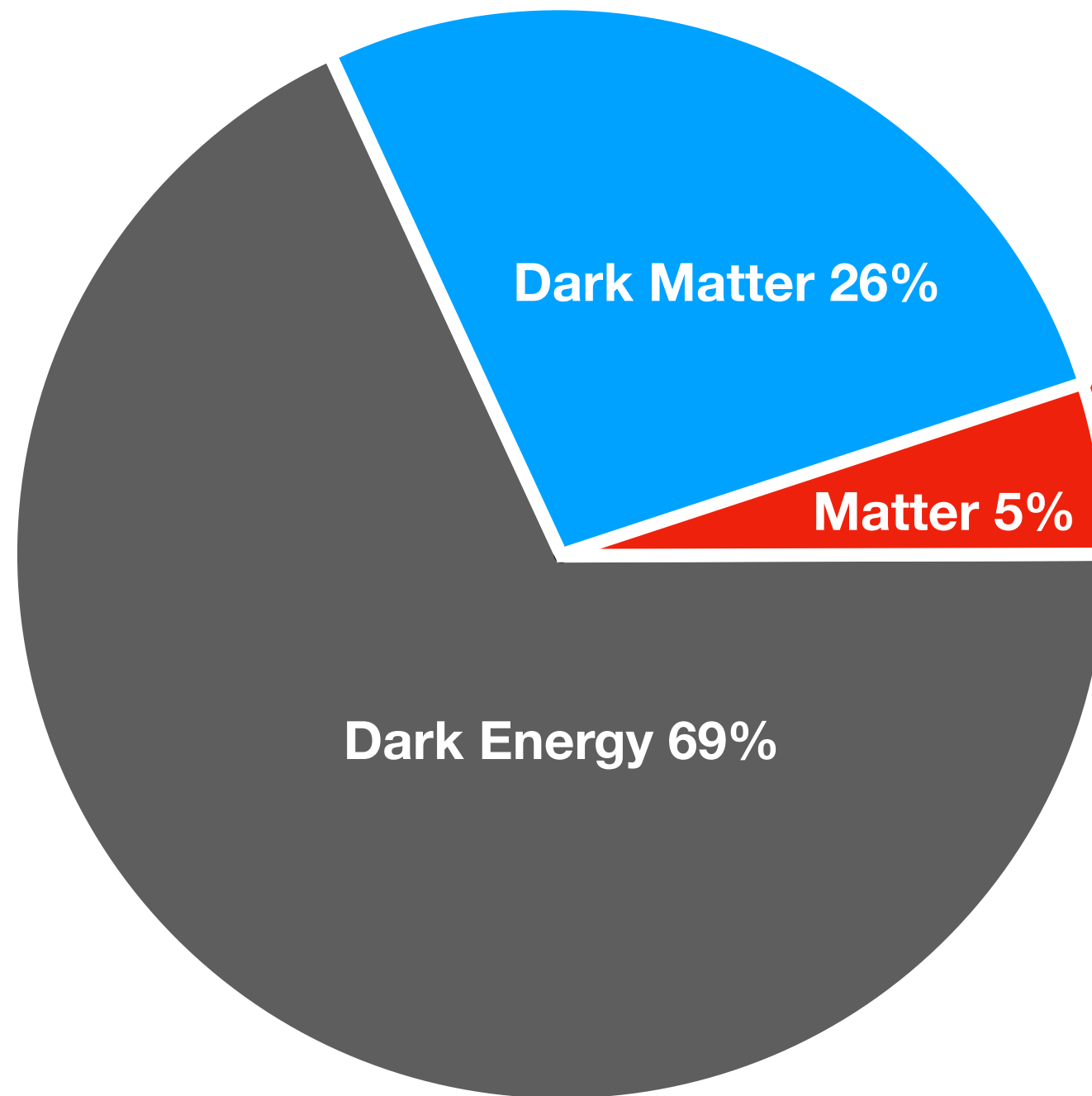
Phase II



$\lambda_{\alpha\beta}(t)$ at a fixed point in the space



Baryon-antibaryon asymmetry



Most matter is formed by baryon, not anti-baryon.

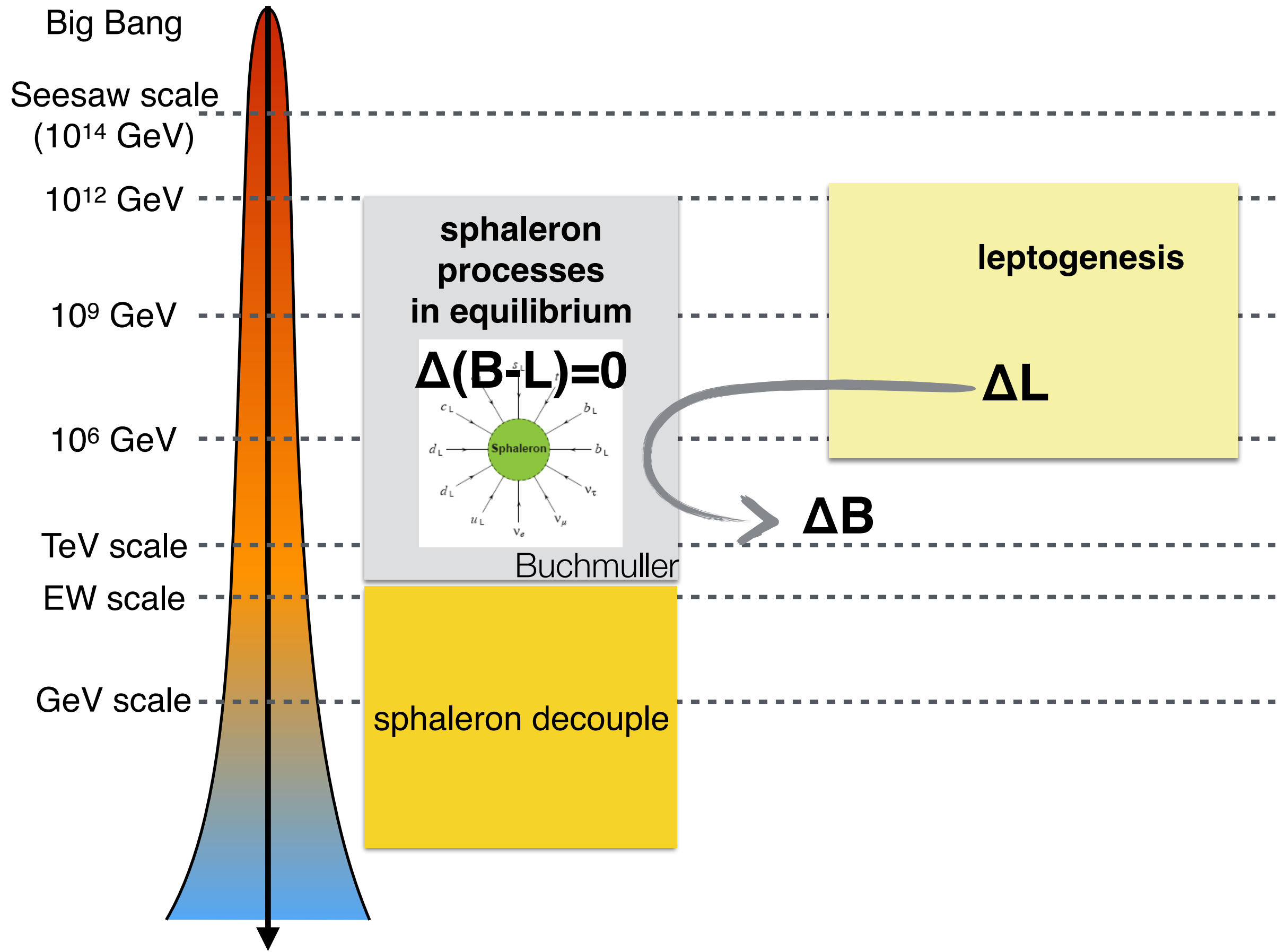
$$\eta_B \equiv \frac{n_B - n_{\bar{B}}}{n_\gamma} = (6.12 \pm 0.04) \times 10^{-10}$$

Planck 2018

The SM cannot provide strong out-of-equilibrium dynamics and enough CP violation.

Parameter(s)	$\Omega_b h^2$	$\Omega_c h^2$	$100\theta_{MC}$	H_0	n_s	$\ln(10^{10} A_s)$
Base Λ CDM	0.02237 ± 0.00015	0.1200 ± 0.0012	1.04092 ± 0.00031	67.36 ± 0.54	0.9649 ± 0.0042	3.044 ± 0.014
r	0.02237 ± 0.00014	0.1199 ± 0.0012	1.04092 ± 0.00031	67.40 ± 0.54	0.9659 ± 0.0041	3.044 ± 0.014
$dn_s/d \ln k$	0.02240 ± 0.00015	0.1200 ± 0.0012	1.04092 ± 0.00031	67.36 ± 0.53	0.9641 ± 0.0044	3.047 ± 0.015
$dn_s/d \ln k, r$	0.02243 ± 0.00015	0.1199 ± 0.0012	1.04093 ± 0.00030	67.44 ± 0.54	0.9647 ± 0.0044	3.049 ± 0.015
$d^2 n_s/d \ln k^2, dn_s/d \ln k$	0.02237 ± 0.00016	0.1202 ± 0.0012	1.04090 ± 0.00030	67.28 ± 0.56	0.9625 ± 0.0048	3.049 ± 0.015
N_{eff}	0.02224 ± 0.00022	0.1179 ± 0.0028	1.04116 ± 0.00043	66.3 ± 1.4	0.9589 ± 0.0084	3.036 ± 0.017

Baryogenesis via leptogenesis



Sakharov conditions for leptogenesis

B violation $\Rightarrow$ **SM L/B-L violation**

(sphaleron processes)

C/CP violation

Out of equilibrium dynamics

Leptogenesis via RH neutrinos

- Classical thermal leptogenesis (in type-I seesaw)

RH neutrino N

Complex Yukawa couplings

Decay of lightest N

- Lepton asymmetry

$$\Delta f_{\ell_\alpha} \equiv f_{\ell_\alpha} - f_{\bar{\ell}_\alpha}$$

$$\Delta f_{\ell_\alpha} \propto \text{Im} \left\{ \begin{array}{c} \text{Diagram 1: } N_1 \text{ line with } L_\alpha \text{ and } H \text{ vertices} \\ \times \left(\text{Diagram 2: Triangle loop with } N_1, N_j, L_\beta \text{ and } H \text{ vertices} \right. \\ \left. + \text{Diagram 3: Self-energy loop with } N_1, N_j \text{ and } L_\beta \text{ vertices} \right) \end{array} \right\}$$

$$\propto \text{Im} \{ Y_{\alpha I} (Y^\dagger Y)_{IJ} Y_{J\alpha}^\dagger \} \times \frac{M_N}{16\pi} \dots$$

CP
asymmetry

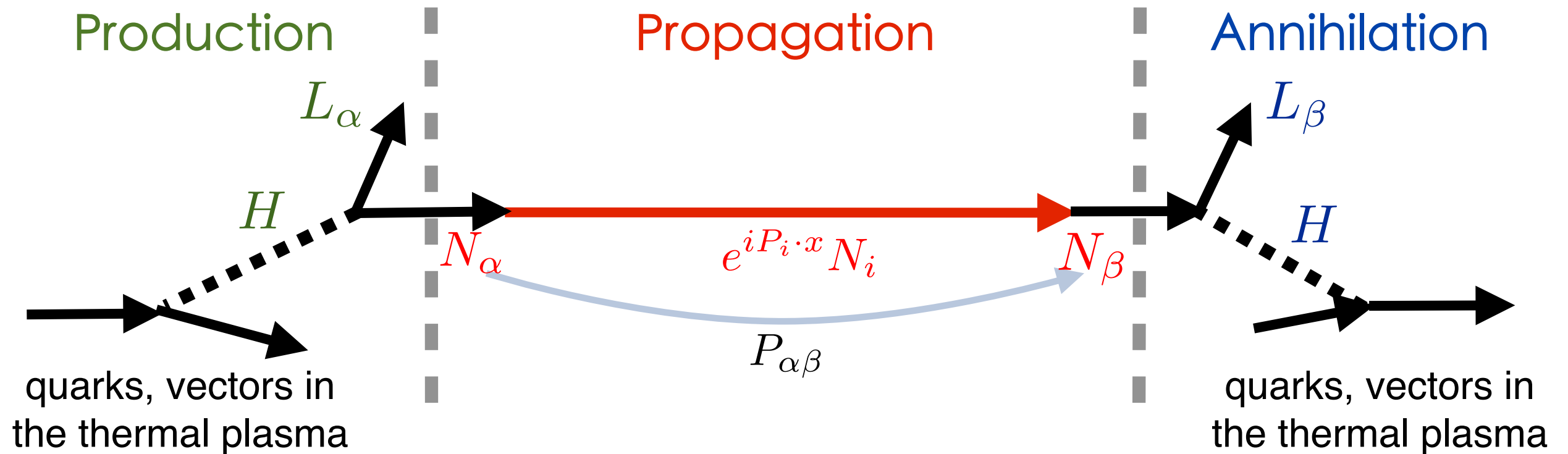
[Fukugita, Yanagida, 1986]

- Flavour effects, Resonant leptogenesis, N_2 decay
leptogenesis, ...

Pilaftsis, hep-ph/9702393, hep-ph/9707235; Pilaftsis, Underwood, hep-ph/0309342; Barbieri, Creminelli, Strumia, Tetradis, hep-ph/9911315; Vives, hep-ph/0512160; Nardi, Nir, Roulet, Racker, hep-ph/0601084; Abada, Davidson, Josse-Michaux, Losada, Riotto, hep-ph/0601083; Blanchet, Di Bari, hep-ph/0607330,

Leptogenesis via RH neutrinos

Sterile neutrino oscillation in early Universe



The “generalised” lepton number $\mathbf{L} = L + L_N$ is conserved.

$$\Delta_{\alpha\alpha} \propto \sum_{\beta} P(N_\beta \rightarrow N_\alpha) - P(\bar{N}_\beta \rightarrow \bar{N}_\alpha) - P(N_\alpha \rightarrow N_\beta) + P(\bar{N}_\alpha \rightarrow \bar{N}_\beta)$$

CP asymmetry $\propto \text{Im}\left\{\exp\left(-i \int_0^t \frac{\Delta M_{IJ}^2}{2E} dt\right)\right\} \times \text{Im}\{Y_{\alpha I} (Y^\dagger Y)_{IJ} Y_{J\alpha}^\dagger\}$

Akhmedov, Rubakov, Smirnov, hep-ph/9803255

Asaka and Shaposhnikov, hep-ph/0505013; Drewes, et al, 1606.06690, 1609.09069;
Hernández, et al, 1606.06719; Drewes et al, 1711.02862,

Leptogenesis via leptonic phase transition



Weinberg operator + leptonic phase transition

1. Baryogenesis via leptonic CP-violating phase transition
S Pascoli, J Turner, **YLZ**, [arXiv:1609.07969](https://arxiv.org/abs/1609.07969)
2. Leptogenesis via Varying Weinberg Operator: the Closed-Time-Path Approach,
J Turner, **YLZ**, [arXiv:1808.00470](https://arxiv.org/abs/1808.00470)
3. Leptogenesis via Varying Weinberg Operator: a Semi-Classical Approach
S Pascoli, J Turner, **YLZ**, [arXiv:1808.00475](https://arxiv.org/abs/1808.00475)

Role of Weinberg operator

A consistent Weinberg operator provides two Sakharov conditions

- The Weinberg operator violates lepton number and leads to LNV processes in the thermal universe.

$$H^*H^* \leftrightarrow \ell\ell, \quad \bar{\ell}H^* \leftrightarrow \ell H, \quad \bar{\ell}H^*H^* \leftrightarrow \ell, \quad \text{and their CP-conjugate processes}$$
$$\bar{\ell} \leftrightarrow \ell HH, \quad H^* \leftrightarrow \ell\ell H, \quad 0 \leftrightarrow \ell\ell HH$$

- The Weinberg operator is very weak and can directly provide out of equilibrium dynamics in the early Universe.

$$\Gamma_W \sim \langle \sigma n \rangle \sim \frac{3}{(4\pi)^3} \frac{\lambda^2}{\Lambda^2} T^3 \sim \frac{3}{(4\pi)^3} \frac{m_\nu^2 T^3}{v_H^4}$$

$$T < 10^{12} \text{ GeV}$$

<

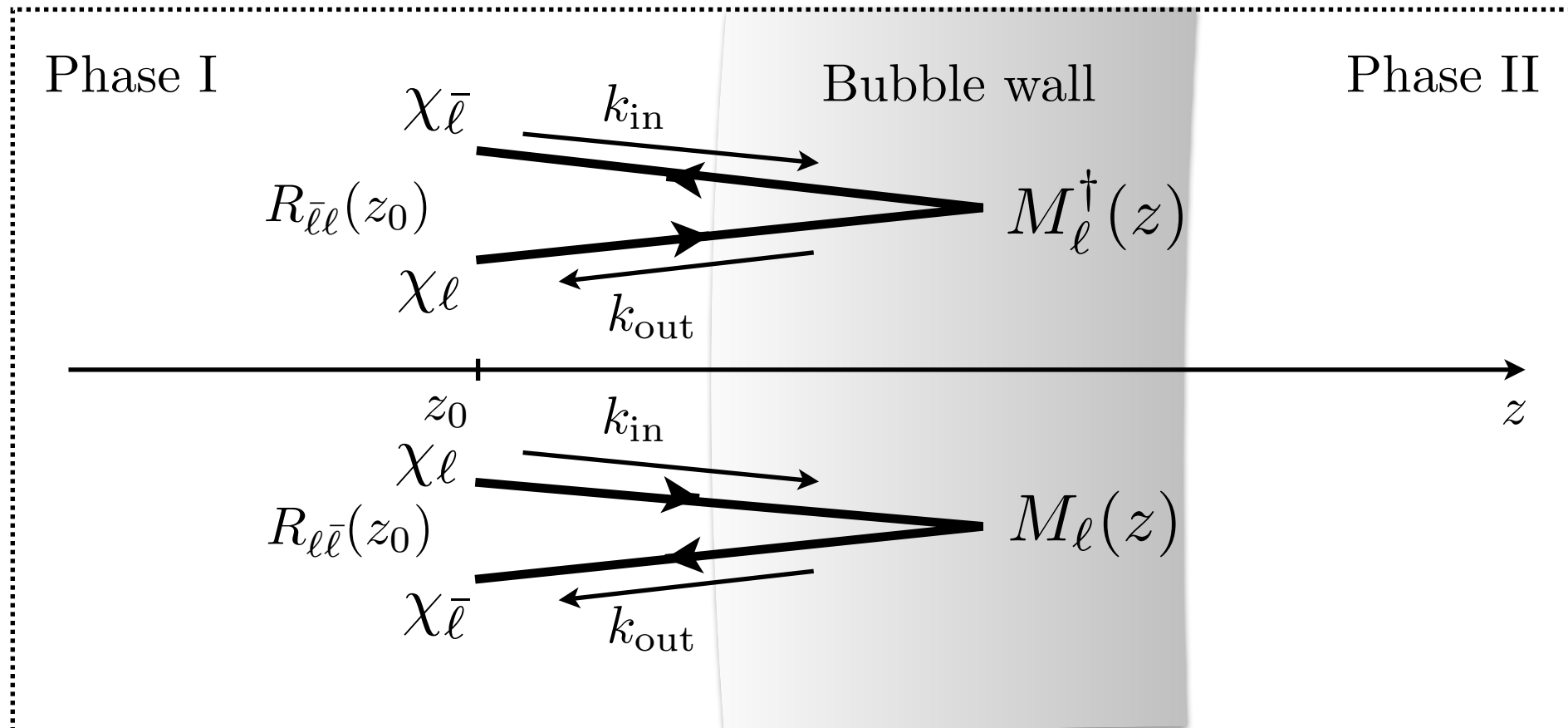
$$H_u \sim 10 \frac{T^2}{m_{\text{pl}}}$$

No washout

if there are no other LNV sources.

Lepton asymmetry in Semi-classical approach

In the rest wall frame



**wave functions
of lepton and
anti lepton**

$$\chi_{\bar{\ell}}(x) = \begin{pmatrix} -\chi_{\bar{\nu}}(x) \\ \chi_{\bar{l}}(x) \end{pmatrix}$$

$$\chi_{\ell}(x) = \begin{pmatrix} \chi_{\nu}(x) \\ \chi_l(x) \end{pmatrix}$$

**Majorana-like
mass matrix**

$$M_{\ell}^{\dagger}(x) = \frac{\lambda(x)}{\Lambda} \begin{pmatrix} 2 [H^0(x)]^2 & -2H^0(x)H^+(x) \\ -2H^0(x)H^+(x) & 2 [H^+(x)]^2 \end{pmatrix}$$

- We treating the Higgs as a background field in the thermal bath

$$\langle H^{0*} H^0 \rangle = \langle H^{+*} H^+ \rangle = \frac{1}{2} \langle H^{\dagger} H \rangle = 2 \int \frac{d^3 k}{(2\pi)^3} \frac{1}{2\omega} \frac{1}{e^{\beta\omega} - 1} = \frac{T^2}{12},$$

Lepton asymmetry in Semi-classical approach

- The “EOM” of lepton and antilepton

$$i\partial\ell_L + M_\ell C \overline{\ell}_L^T = 0$$

- We further include the decoherence effect is included by replacing the incoming and outgoing momentums

$$\ell_L = \begin{pmatrix} \exp[-i(\omega t - k_{\text{in}}z)]\chi_{1\ell}(z) \\ \exp[-i(\omega t + k_{\text{out}}z)]\chi_{2\ell}(z) \\ 0 \\ 0 \end{pmatrix}$$

$$\overline{\ell}_L^T = \begin{pmatrix} 0 \\ 0 \\ \exp[+i(\omega t - k_{\text{in}}z)]\chi_{1\bar{\ell}}(z) \\ \exp[+i(\omega t + k_{\text{out}}z)]\chi_{2\bar{\ell}}(z) \end{pmatrix}$$

$$k_{\text{in}} \rightarrow K_{\text{in}} = k_{\text{in}} + \frac{i}{2L}, \quad k_{\text{out}} \rightarrow K_{\text{out}} = k_{\text{out}} - \frac{i}{2L}$$

$$L = \frac{1}{6\gamma} \text{ decoherence length, avoiding interference between infinite distance}$$

- EOM of lepton-antilepton propagating along the z direction is given by

$$\left[(-i\partial_z + \omega) \mathbb{1}_2 - \begin{pmatrix} -K_{\text{in}} & M_\ell^\dagger(z) \\ -M_\ell(z) & -K_{\text{out}} \end{pmatrix} \right] \begin{pmatrix} \chi_{1\ell}(z) \\ \chi_{2\bar{\ell}}(z) \end{pmatrix} = 0$$

$$j_z = +\frac{1}{2}$$

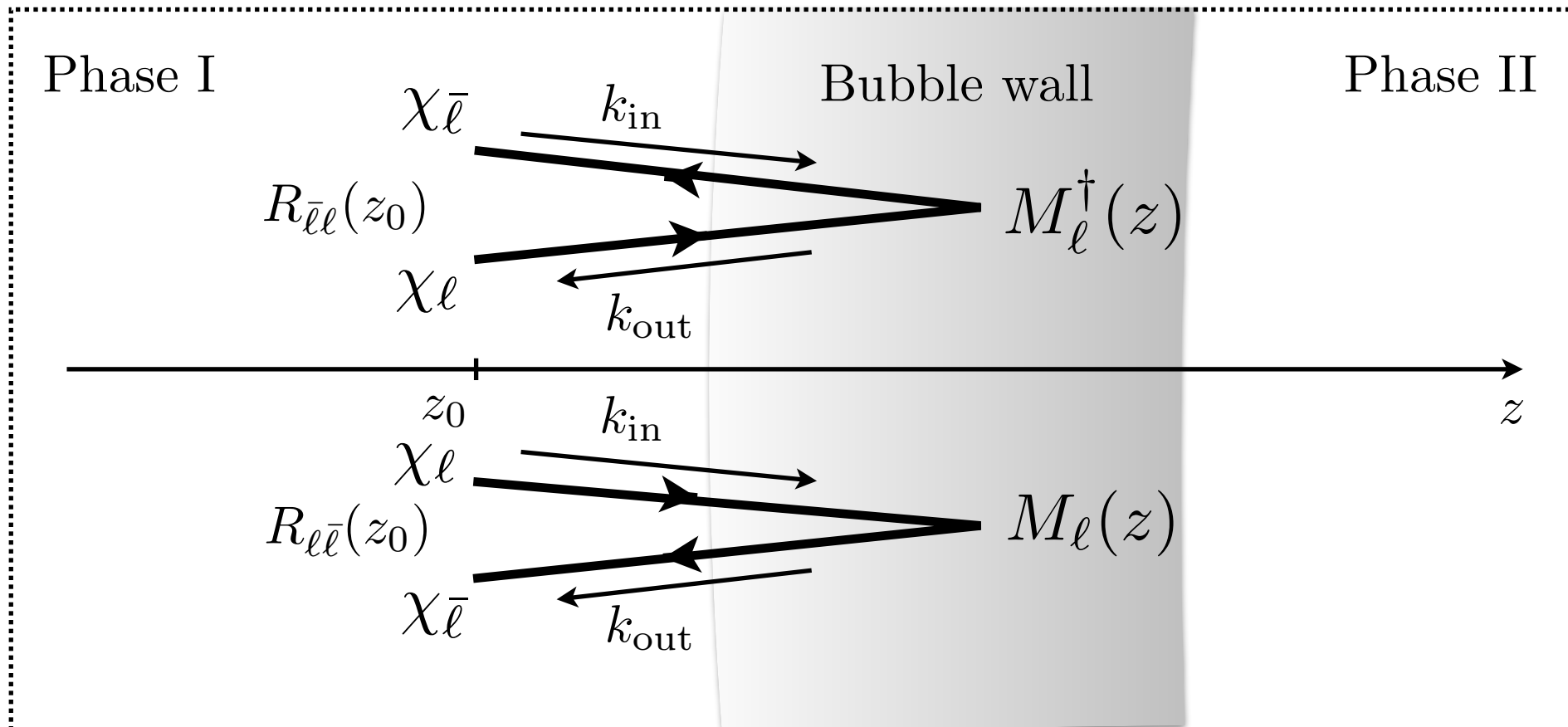
$$\left[(-i\partial_z - \omega) \mathbb{1}_2 - \begin{pmatrix} K_{\text{in}} & -M_\ell(z) \\ M_\ell^\dagger(z) & K_{\text{out}} \end{pmatrix} \right] \begin{pmatrix} \chi_{1\bar{\ell}}(z) \\ \chi_{2\ell}(z) \end{pmatrix} = 0$$

$$j_z = -\frac{1}{2}$$

The semi-classical approximation follows the technique of varying mass for left-right chirality transition developed for electroweak baryogenesis in Huet, Sather, hep-ph/9404302

Lepton asymmetry in Semi-classical approach

In the rest wall frame



$$\chi_{\bar{\ell}}(x) = \begin{pmatrix} -\chi_{\bar{\nu}}(x) \\ \chi_{\bar{l}}(x) \end{pmatrix}$$

$$\chi_{\ell}(x) = \begin{pmatrix} \chi_{\nu}(x) \\ \chi_l(x) \end{pmatrix}$$

$$z_1 = z - z_0$$

antilepton to lepton $R_{\bar{\ell}\ell}(z_0) = i \int_0^{+\infty} dz_1 e^{-z_1/L} e^{ik_{\text{out}}z_1} M_{\ell}^{\dagger}(z_0 + z_1) e^{-ik_{\text{in}}z_1}$

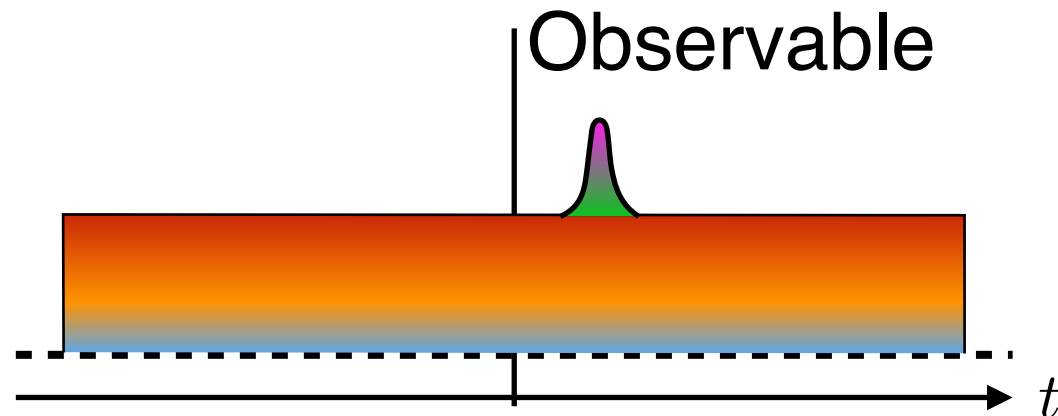
lepton to antilepton $R_{\ell\bar{\ell}}(z_0) = i \int_0^{+\infty} dz_1 e^{-z_1/L} e^{ik_{\text{out}}z_1} M_{\ell}(z_0 + z_1) e^{-ik_{\text{in}}z_1}$

$$\Delta_{CP}(z_0) \equiv |R_{\bar{\ell}\ell}(z_0)|^2 - |R_{\ell\bar{\ell}}(z_0)|^2 = 2 \int_0^{+\infty} dz_1 dz_2 e^{-(z_1+z_2)/L} \sin[(k_{\text{out}} - k_{\text{in}})(z_1 - z_2)] \times \text{Im}[M_{\ell}(z_0 + z_1) M_{\ell}^{\dagger}(z_0 + z_2)]$$

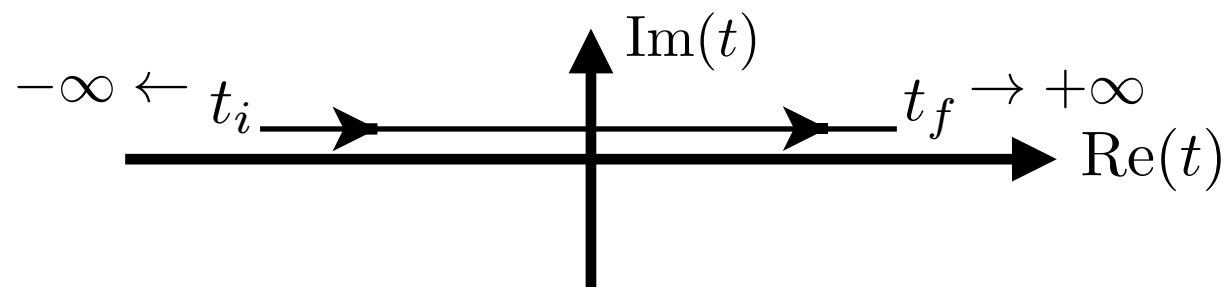
Asymmetry

The closed-time-path approach

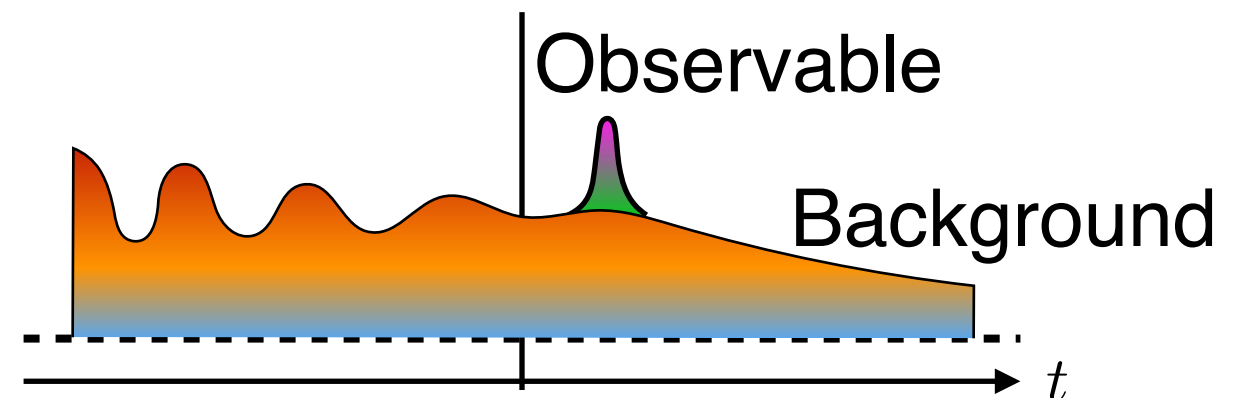
- Classical QFT
at zero temperature,
or thermal equilibrium



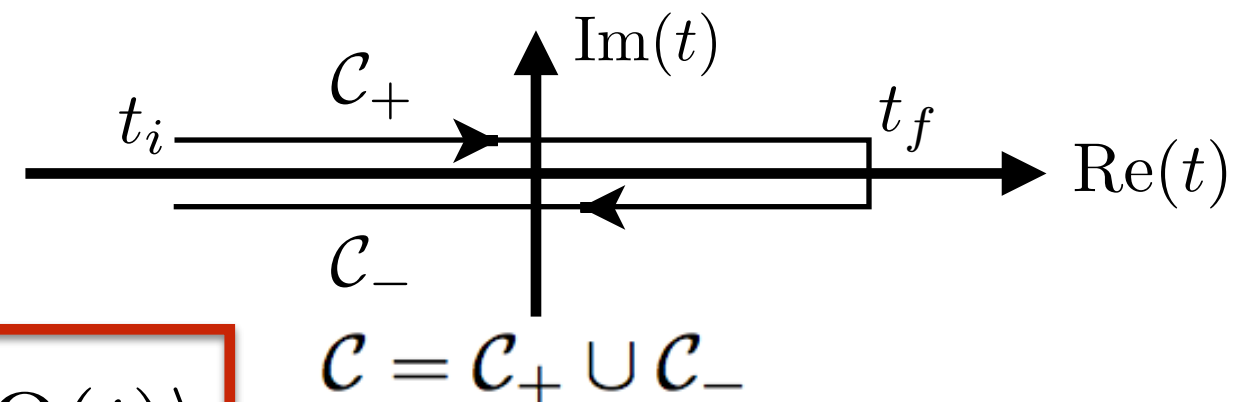
Vacuum/background is in thermal equilibrium, time-dependent



- QFT in non-equilibrium case



Background is time-dependent.
We have to specify a time.



$$\langle \Omega(t) | \mathcal{O} | \Omega(t) \rangle$$

**In-out
formalism**

$$\langle \Omega(t_f) | \mathcal{O} | \Omega(t_i) \rangle$$

**In-in
formalism**

$$\langle \Omega(t_i) | \mathcal{O} | \Omega(t_i) \rangle$$

The closed-time-path approach

• Propagators

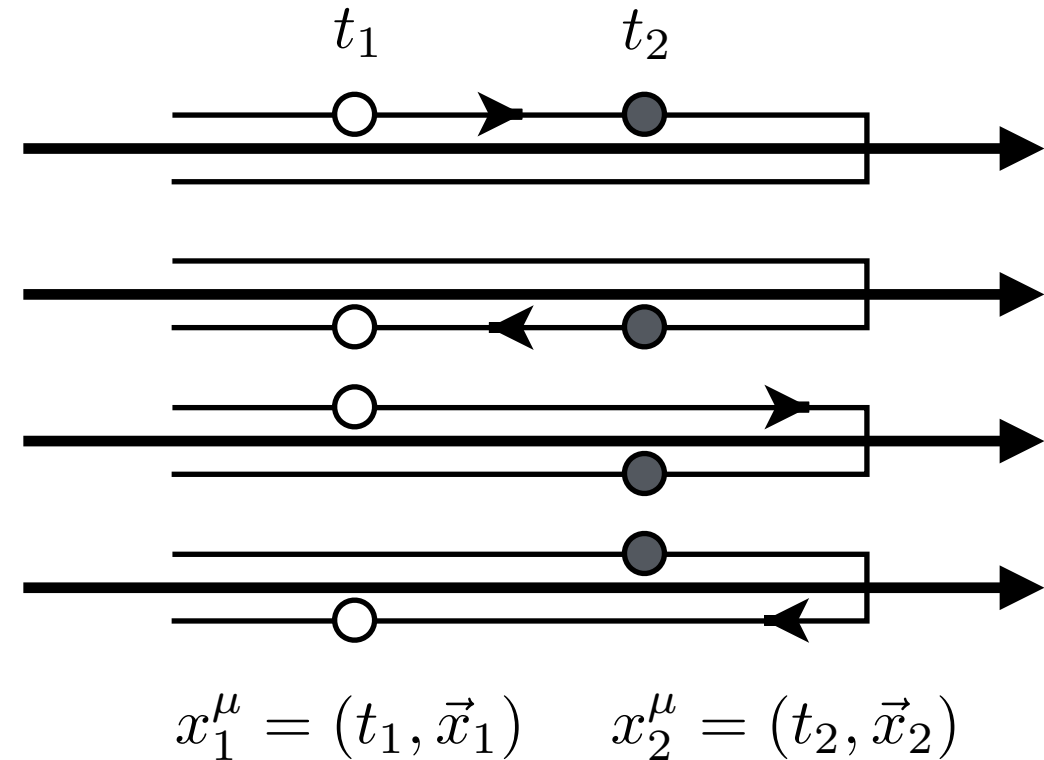
Feynman $S_{\alpha\beta}^T(x_1, x_2) = \langle T[\ell_\alpha(x_1)\bar{\ell}_\beta(x_2)] \rangle$

Dyson $S_{\alpha\beta}^{\bar{T}}(x_1, x_2) = \langle \bar{T}[\ell_\alpha(x_1)\bar{\ell}_\beta(x_2)] \rangle$

Wightman

$$S_{\alpha\beta}^<(x_1, x_2) = -\langle \bar{\ell}_\beta(x_2)\ell_\alpha(x_1) \rangle$$

$$S_{\alpha\beta}^>(x_1, x_2) = \langle \ell_\alpha(x_1)\bar{\ell}_\beta(x_2) \rangle$$



• Kadanoff-Baym equation

$$i\partial S^{<, >} - \Sigma^H \odot S^{<, >} - \Sigma^{<, >} \odot S^H = \frac{1}{2} [\Sigma^> \odot S^< - \Sigma^< \odot S^>]$$

**Lepton
asymmetry**

**Self energy
correction**

**Dispersion
relations**

Collision term

$$\Delta n_{\ell\alpha}(x) = -\frac{1}{2}\text{tr}\left\{\gamma^0[S_{\alpha\alpha}^<(x, x) + S_{\alpha\alpha}^>(x, x)]\right\}$$

$$\Delta f_{\ell\alpha}(k) = -\int_{t_i}^{t_f} dt_1 \partial_{t_1} \text{tr}[\gamma_0 S_{\vec{k}}^<(t_1, t_1) + \gamma_0 S_{\vec{k}}^>(t_1, t_1)]$$

$$S^H = S^T - \frac{1}{2}(S^> + S^<)$$

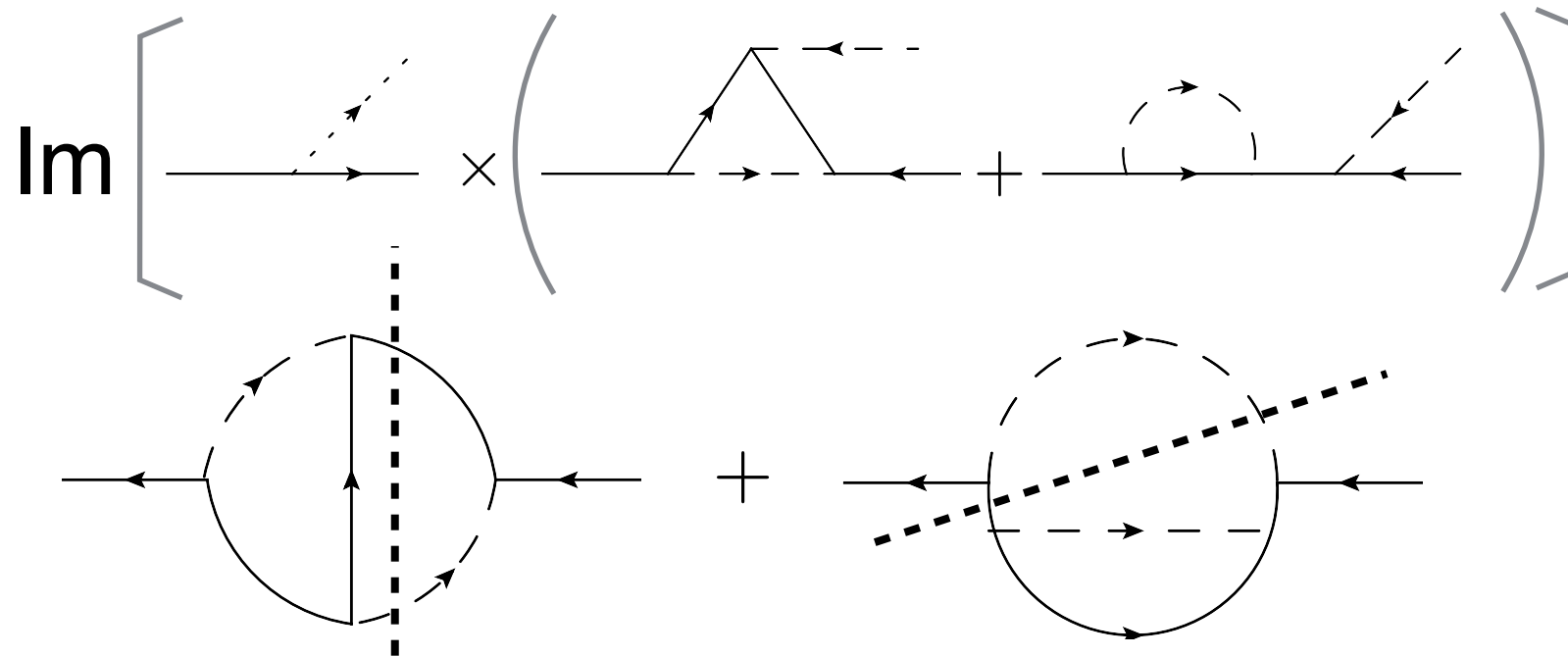
$$\Sigma^H = \Sigma^T - \frac{1}{2}(\Sigma^> + \Sigma^<)$$

CPV source

Classical QFT vs CTP formalism

- Leptogenesis via RH neutrino decay

e.g., Anisimov, Buchmuller, Drewes, Mendizabal, 1012.5821

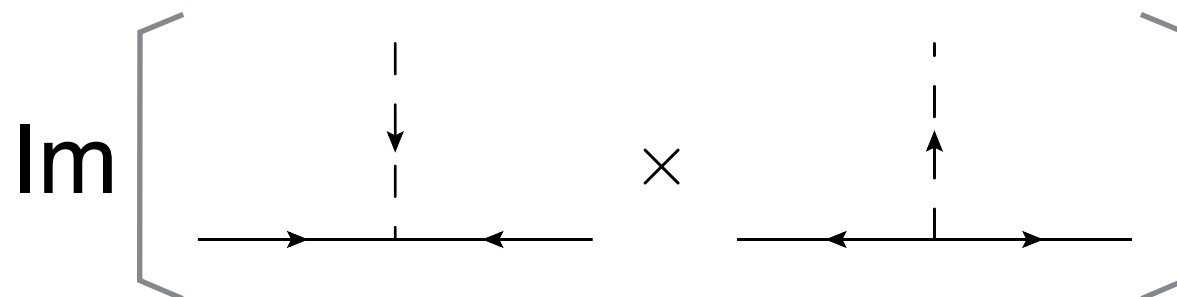


CPV source in classical formalism

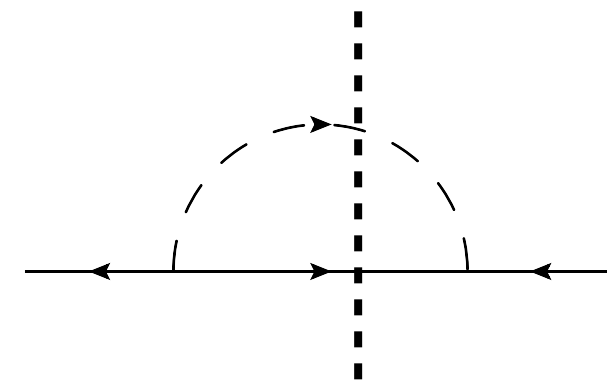
Self energies including CPV source in CTP formalism

- Leptogenesis via RH neutrino oscillation

Drewes, et al, 1711.02862

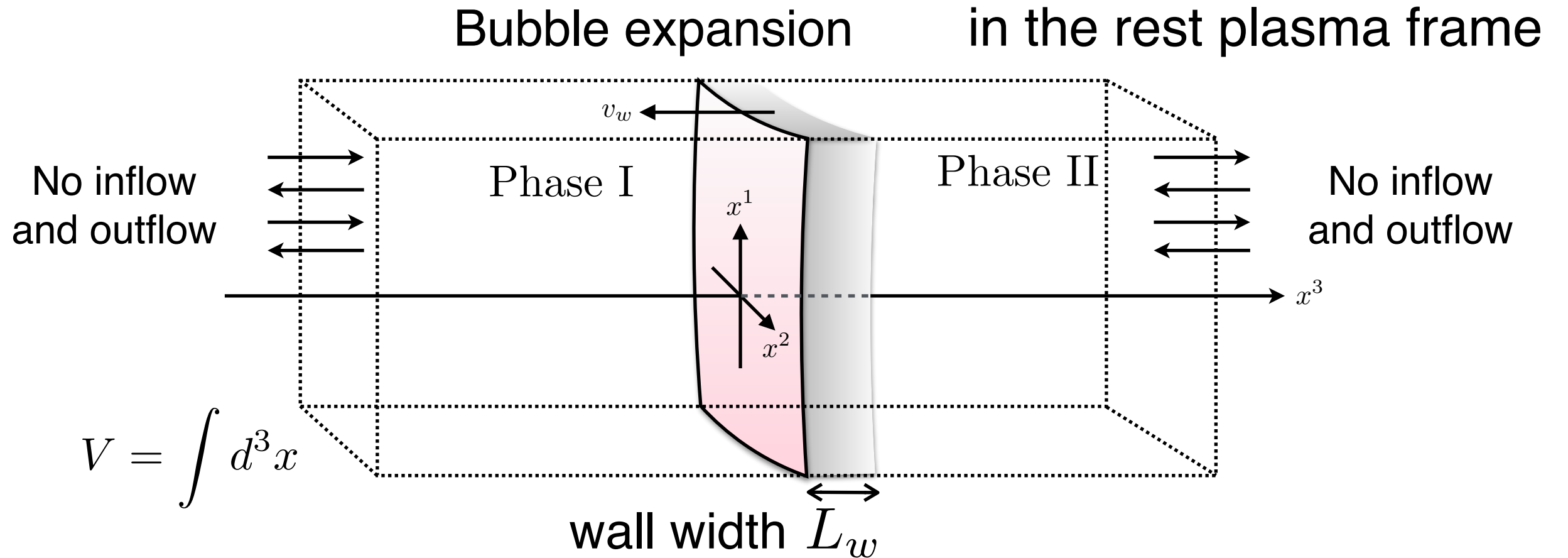


CPV source in classical formalism



Self energy including CPV source in CTP formalism

Lepton asymmetry in CTP approach



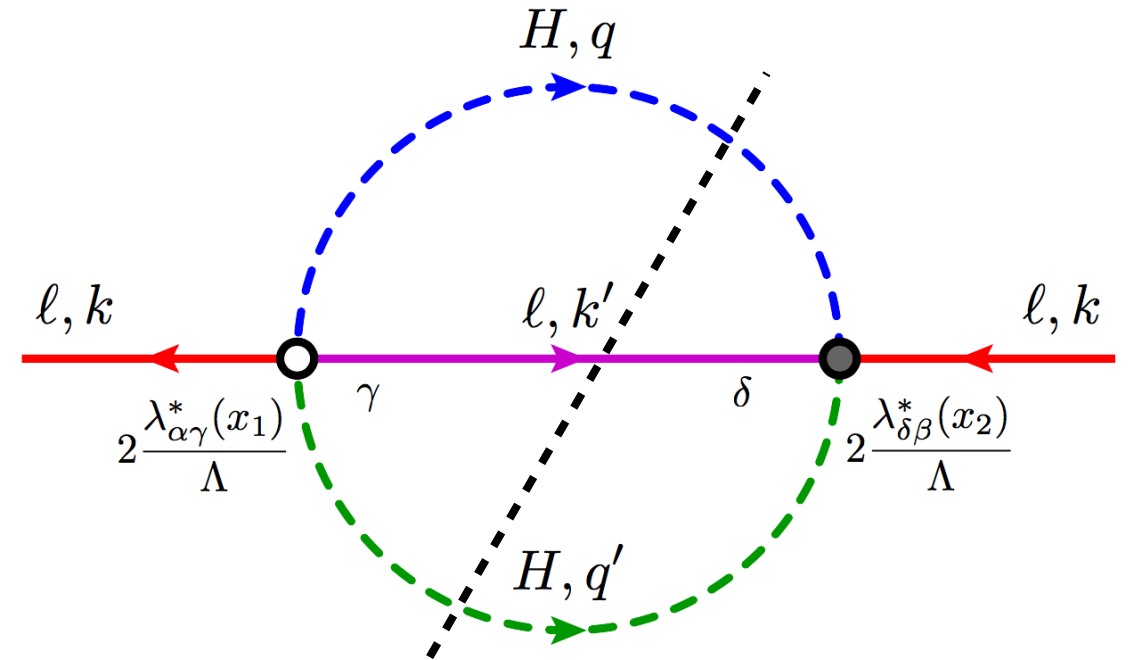
$$\begin{aligned} \Delta N_\ell &= N_\ell - N_{\bar{\ell}} = - \int \frac{d^4x_1 d^4k}{(2\pi)^4} \text{tr} \left[\gamma^\mu i \frac{\partial}{\partial x_1^\mu} (S_k^<(x_1) + S_k^>(x_1)) \right] \\ &= - \int \underline{d^4x d^4r} \text{tr} \left[\Sigma^>(x_1, x_2) S^<(x_2, x_1) - \Sigma^<(x_1, x_2) S^>(x_2, x_1) \right] . \end{aligned}$$

$$x = \frac{1}{2}(x_1 + x_2) \quad r = x_1 - x_2$$

Lepton asymmetry in CTP approach

- CP-violating self energy**

$$\Sigma_{\alpha\beta}^{<, >}(x_1, x_2) = 3 \times \frac{4}{\Lambda^2} \sum_{\gamma\delta} \lambda_{\alpha\gamma}^*(x_1) \lambda_{\delta\beta}(x_2) \times \Delta^{>, <}(x_2, x_1) \Delta^{>, <}(x_2, x_1) S_{\gamma\delta}^{>, <}(x_2, x_1),$$



- Lepton asymmetry**

$$\Delta N_\ell = -\frac{12}{\Lambda^2} \int d^4x d^4r (-i) \text{tr}[\lambda^*(x_1) \lambda(x_2)] \mathcal{M}.$$

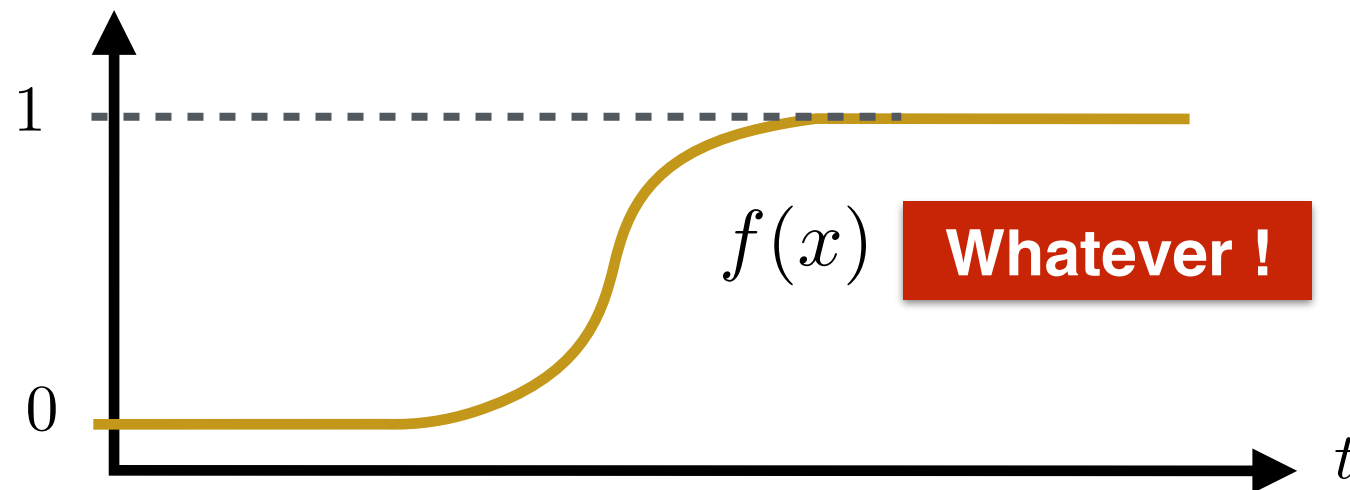
$$\mathcal{M} = i \int \frac{d^4k}{(2\pi)^4} \frac{d^4k'}{(2\pi)^4} \frac{d^4q}{(2\pi)^4} \frac{d^4q'}{(2\pi)^4} e^{iK \cdot (-r)} \left\{ \Delta_q^<(x) \Delta_{q'}^<(x) \text{tr}[S_k^<(x) S_{k'}^<(x)] - \Delta_q^>(x) \Delta_{q'}^>(x) \text{tr}[S_k^>(x) S_{k'}^>(x)] \right\}$$

The final lepton asymmetry is determined by **the behaviour of Weinberg operator during the phase transition** and **thermal properties of leptons and the Higgs**.

Influence of phase transition

- Single-scalar phase transition**

$$\lambda(x) = \lambda^0 + \lambda^1 f(x) \quad f(x) \equiv \frac{\langle \phi(x) \rangle}{v_\phi}$$



$$m_\nu^0 = \lambda^0 \frac{v_H^2}{\Lambda}$$

$$m_\nu = \lambda \frac{v_H^2}{\Lambda}$$

$$\int d^4x \text{Im}\{\text{tr}[\lambda^*(x_1)\lambda(x_2)]\} = \text{Im}\{\text{tr}[\lambda^0\lambda^*]\} \left(r^0 - \frac{r^3}{v_w}\right) V$$

$$\Delta n_\ell^{\text{I}} = -\frac{12}{\Lambda^2} \text{Im}\{\text{tr}[\lambda^0\lambda^*]\} \int d^4r r^0 \mathcal{M} \quad \text{time-dependent integration}$$

$$\Delta n_\ell^{\text{II}} = \frac{12}{v_w \Lambda^2} \text{Im}\{\text{tr}[\lambda^0\lambda^*]\} \int d^4r r^3 \mathcal{M} \quad \text{space-dependent integration}$$

$$\Delta n_\ell = \Delta n_\ell^{\text{I}} + \Delta n_\ell^{\text{II}}$$

Influence of phase transition

- **Multi-scalar phase transition (in the thick-wall limit)**

e.g., $\lambda(x) = \lambda^0 + \lambda^1 f_1(x) + \lambda^2 f_2(x)$

$$\begin{aligned} \text{Im}\{\text{tr}[\lambda^*(x_1)\lambda(x_2)]\} &= \text{Im}\{\text{tr}[\lambda^0\lambda^{1*}]\}[f_1(x_1) - f_1(x_2)] + \text{Im}\{\text{tr}[\lambda^0\lambda^{2*}]\}[f_2(x_1) - f_2(x_2)] \\ &\quad + \text{Im}\{\text{tr}[\lambda^{1*}\lambda^2]\}[f_1(x_1)f_2(x_2) - f_1(x_2)f_2(x_1)] \end{aligned}$$

Interferences of different scalar VEVs cannot be neglected.

$$\begin{aligned} \int d^4r \text{Im}\{\text{tr}[\lambda^*(x_1)\lambda(x_2)]\} \mathcal{M} &= \int d^4r \text{Im}\{\text{tr}[\lambda^*(x + r/2)\lambda(x - r/2)]\} \mathcal{M} \\ &\approx \text{Im}\{\text{tr}[\lambda^*(x)\partial_\mu\lambda(x)]\} \int d^4r r^\mu \mathcal{M}. \end{aligned}$$

$$\begin{aligned} \Delta n_\ell^{\text{I}} &\propto \text{Im}\{\text{tr}[\lambda^*(x)\partial_t\lambda(x)]\} \int d^4r r^0 \mathcal{M} && \text{time-dependent integration} \\ \Delta n_\ell^{\text{II}} &\propto \text{Im}\{\text{tr}[\lambda^*(x)\partial_z\lambda(x)]\} \int d^4r r^3 \mathcal{M} && \text{space-dependent integration} \end{aligned}$$

Time derivative/spatial gradient

Influence of thermal effects

Thermal effects influence the time- and space-dependent integration.

$$\int d^4r r^0 \mathcal{M}$$

$$\int d^4r r^3 \mathcal{M}$$

$$\mathcal{M} = i \int \frac{d^4k}{(2\pi)^4} \frac{d^4k'}{(2\pi)^4} \frac{d^4q}{(2\pi)^4} \frac{d^4q'}{(2\pi)^4} e^{iK \cdot (-r)} \left\{ \Delta_q^<(x) \Delta_{q'}^<(x) \text{tr}[S_k^<(x) S_{k'}^<(x)] - \Delta_q^>(x) \Delta_{q'}^>(x) \text{tr}[S_k^>(x) S_{k'}^>(x)] \right\}$$

• Resummed propagators of the Higgs and leptons

$$\Delta_q^{<,>} = \frac{-2\varepsilon(q^0) \text{Im}\Pi_q^R}{[q^2 + \text{Re}\Pi_q^R]^2 + [\text{Im}\Pi_q^R]^2} \left\{ \vartheta(\mp q^0) + f_{B,|q^0|}(x) \right\},$$

$$S_k^{<,>} = \frac{-2\varepsilon(k^0) \text{Im}\Sigma_k^{R2}}{[k^2 + \text{Re}\Sigma_k^{R2}]^2 + [\text{Im}\Sigma_k^{R2}]^2} \left\{ \vartheta(\mp k^0) - f_{F,|k^0|}(x) \right\} P_L \not{k} P_R,$$

thermal equilibrium

$$f_{B,|q^0|} \equiv \frac{1}{e^{\beta|q^0|} - 1},$$

$$f_{F,|k^0|} \equiv \frac{1}{e^{\beta|k^0|} + 1},$$

thermal mass

$$m_{\text{th},H}^2 = \text{Re}\Pi$$

$$m_{\text{th},\ell} = \text{Re}\Sigma$$

thermal width

$$\gamma_H = \frac{\text{Im}\Pi}{2m_{\text{th},H}}$$

$$\gamma_\ell = \frac{\text{Im}\Sigma^2}{2m_{\text{th},\ell}}$$

$$\gamma = 6/L$$

By assuming thermal equilibrium in the rest frame of plasma, the space-dependent integration is zero.

$\mathcal{M}$ is invariant under parity transformation
 $r \rightarrow r^P = (r^0, -\mathbf{r}), \quad k_n \rightarrow k_n^P = (k_n^0, -\mathbf{k}_n)$

$$\Rightarrow \int d^4r r^3 \mathcal{M} = 0$$

Influence of thermal effects

- Performing the time-dependent integration

From 4D momentum space to 3D momentum space + 1D time

$$\Delta_{\mathbf{q}}^{<, >}(t_1, t_2) = \int \frac{dq^0}{2\pi} e^{-iq^0 y} \Delta_{\mathbf{q}}^{<, >} = \frac{\cos(\omega_{\mathbf{q}} y^{\mp})}{2\omega_{\mathbf{q}} \sinh(\omega_{\mathbf{q}} \beta/2)} e^{-\gamma_{H, \mathbf{q}} |y|}, \quad y = r^0$$

$$S_{\mathbf{k}}^{<, >}(t_1, t_2) = \int \frac{dk^0}{2\pi} e^{-ik^0 y} S_{\mathbf{k}}^{<, >} = -P_L \frac{\gamma^0 \cos(\omega_{\mathbf{k}} y^{\mp}) + i\vec{\gamma} \cdot \hat{\mathbf{k}} \sin(\omega_{\mathbf{k}} y^{\mp})}{2 \cosh(\omega_{\mathbf{k}} \beta/2)} e^{-\gamma_{\ell, \mathbf{k}} |y|}, \quad y^- = y - i\beta/2$$

Integrating out the time

$$\omega_{\mathbf{q}} = \sqrt{m_{H, \text{th}}^2 + \mathbf{q}^2}, \quad \omega_{\mathbf{k}} = \sqrt{m_{\ell, \text{th}}^2 + \mathbf{k}^2} \quad \text{and} \quad \hat{\mathbf{k}} \equiv \mathbf{k}/\omega_{\mathbf{k}}$$

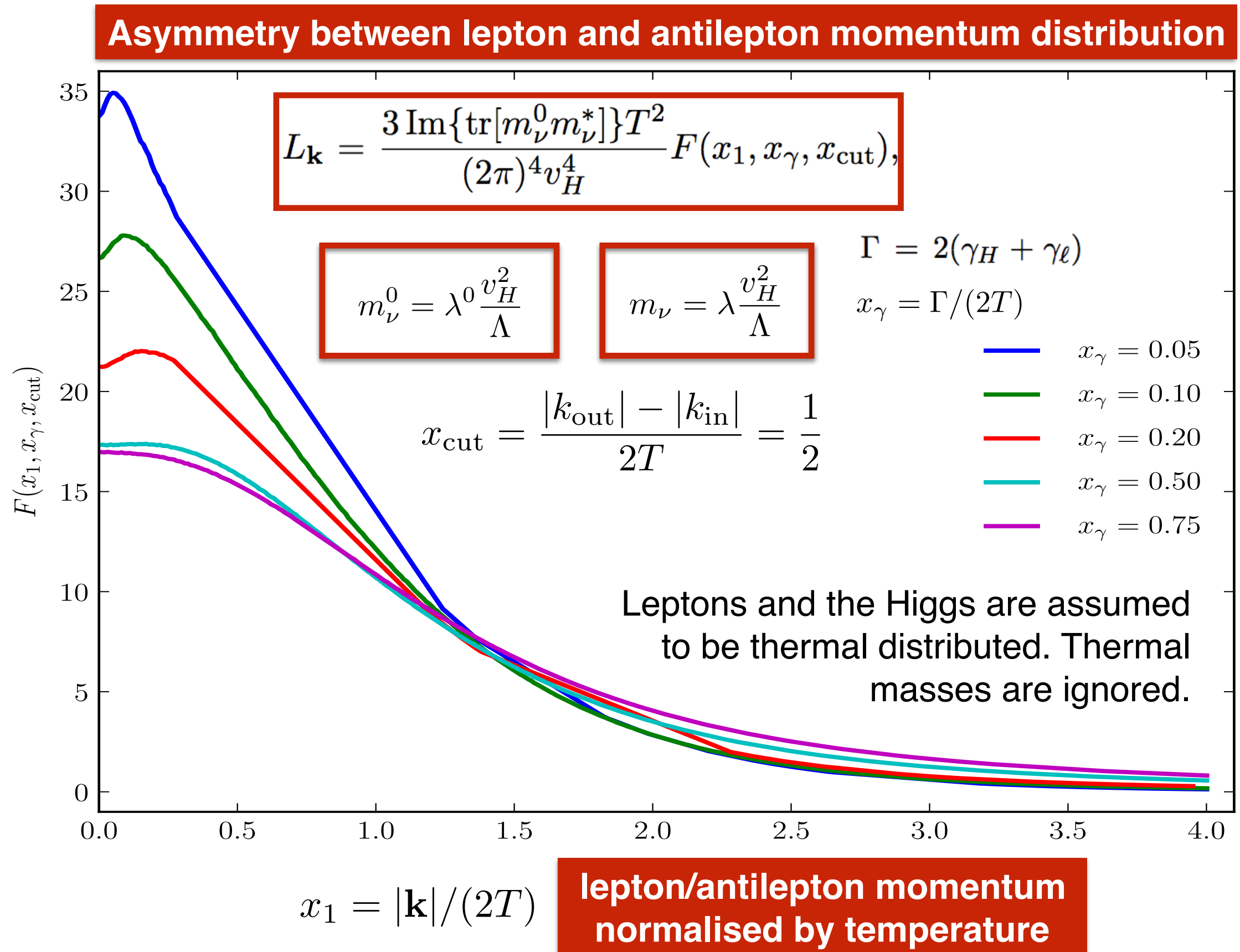
$$\int d^4 r \, y \mathcal{M} = 2 \int \frac{d^3 \mathbf{k}}{(2\pi)^3} \frac{d^3 \mathbf{q}}{(2\pi)^3} \frac{d^3 \mathbf{q}'}{(2\pi)^3} \int dy \, y M,$$

$$\int_{-\infty}^{+\infty} dy \, y M = 2 \int_0^{+\infty} dy \, y M \quad \Gamma = 2(\gamma_H + \gamma_{\ell})$$

$$= 2 \int_0^{+\infty} dy \, y \frac{\text{Im}\{\cos(\omega_{\mathbf{q}} y^-) \cos(\omega_{\mathbf{q}'} y^-) [\cos(\omega_{\mathbf{k}} y^-) \cos(\omega_{\mathbf{k}'} y^-) + \hat{\mathbf{k}} \cdot \hat{\mathbf{k}'} \sin(\omega_{\mathbf{k}} y^-) \sin(\omega_{\mathbf{k}'} y^-)]\}}{8\omega_{\mathbf{q}} \omega_{\mathbf{q}'} \sinh(\omega_{\mathbf{q}} \beta/2) \sinh(\omega_{\mathbf{q}'} \beta/2) \cosh(\omega_{\mathbf{k}} \beta/2) \cosh(\omega_{\mathbf{k}'} \beta/2)} e^{-\Gamma y}$$

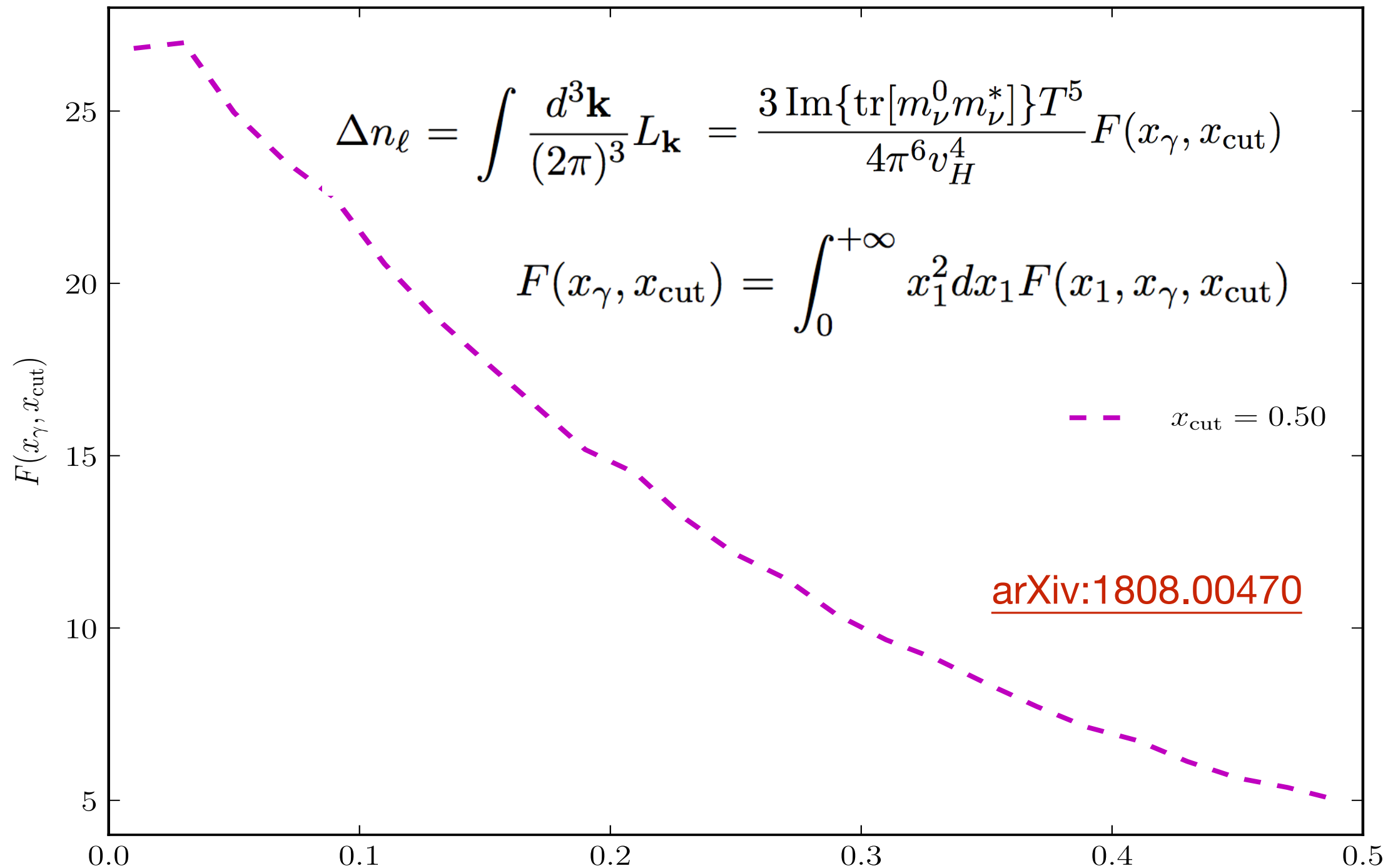
$$= - \sum_{\eta_2, \eta_3, \eta_4 = \pm 1} \frac{\Omega_{\eta_2 \eta_3 \eta_4} \Gamma \sinh(\beta \Omega_{\eta_2 \eta_3 \eta_4} / 2) [1 - \eta_2 \hat{\mathbf{k}} \cdot \hat{\mathbf{k}'}]}{32\omega_{\mathbf{q}} \omega_{\mathbf{q}'} (\Omega_{\eta_2 \eta_3 \eta_4}^2 + \Gamma^2)^2 \sinh(\omega_{\mathbf{q}} \beta/2) \sinh(\omega_{\mathbf{q}'} \beta/2) \cosh(\omega_{\mathbf{k}} \beta/2) \cosh(\omega_{\mathbf{k}'} \beta/2)}$$

Influence of thermal effects



Leptogenesis via Weinberg operator (in CTP approach)

Asymmetry between lepton and antilepton number density



$$x_\gamma = \Gamma / (2T)$$

**Damping rate normalised
by temperature**

Lepton models vs neutrino experiments

- In the single-scalar case

$$\Delta n_\ell = \frac{3 \operatorname{Im}\{\operatorname{tr}[m_\nu^0 m_\nu^*]\} T^5}{4\pi^6 v_H^4} F(x_\gamma, x_{\text{cut}})$$

$$M_\nu^0 = \frac{\lambda^0}{\Lambda} v_H^2$$

Effective nu mass before PT

Depend on lepton model

determined by symmetries
(Discrete, U(1), SO(3), SO(10)...) and order of scalars getting vevs

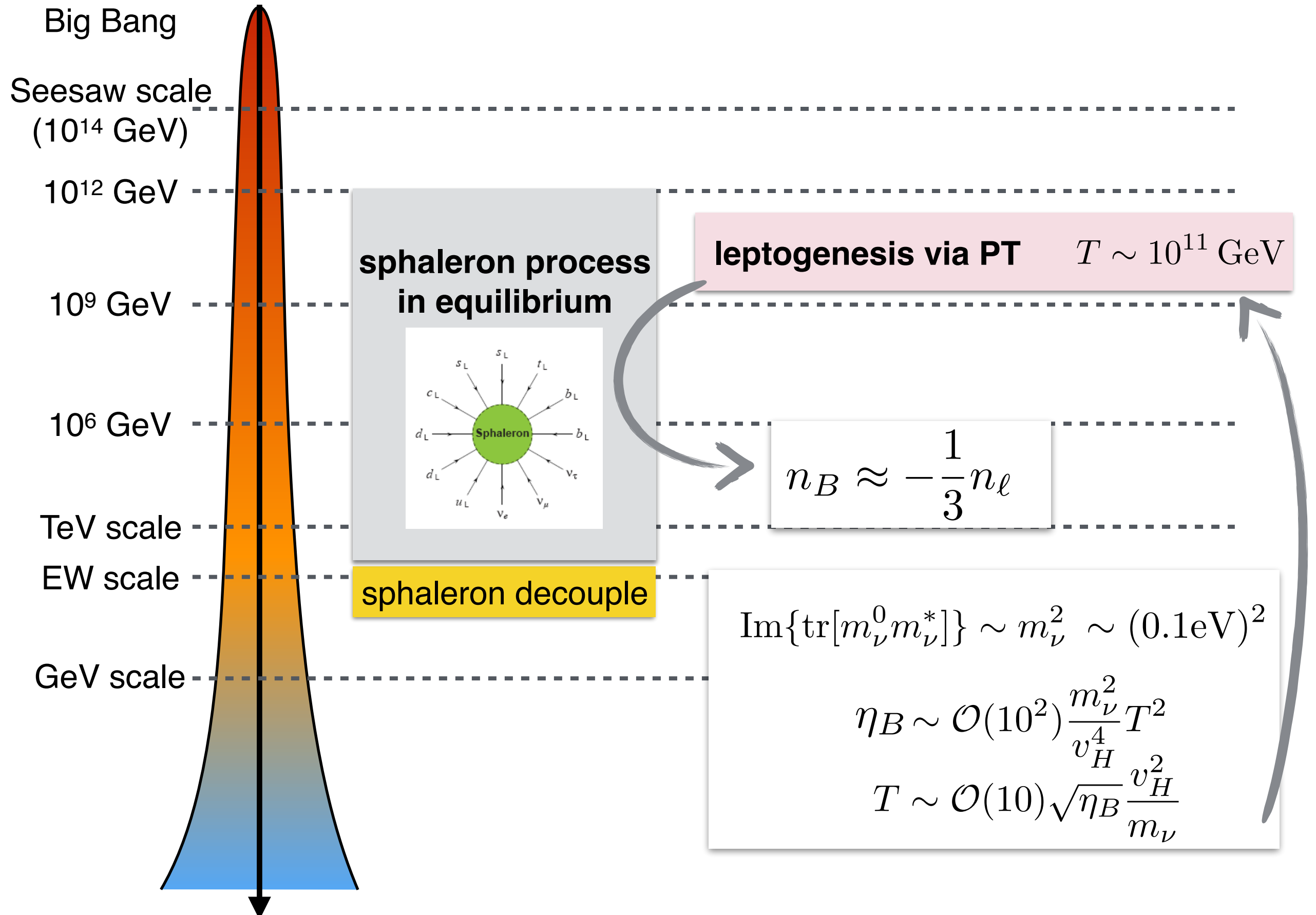
$$M_\nu = \frac{\lambda}{\Lambda} v_H^2$$

Effective nu mass after PT

Measured by nu experiment

nu oscillation exp: DUNE, T2HK, ...
0ν2β exp: Gerda, EXO-200, KamLAND-Zen

Temperature for phase transition



Summary

- I give a brief review of neutrino mass and mixing. Models related to these issues usually introduces new symmetries, which may result in a spacetime-varying Weinberg operator.
- I introduce a novel mechanism of leptogenesis via phase transition. No explicit new particles are required, but just a spacetime-varying Weinberg operator.
- In order to generate enough baryon-antibaryon asymmetry, the temperature for phase transition is roughly around 10^{11} GeV.

Thank you very much!