

# Dark matter in stars

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MPI Heidelberg - Online - December 6 2020



# Dark Matter in the Sun

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arXiv:1311.2074 / JCAP/04019 (ACV, P. Scott)

Thermal conduction by dark matter with velocity and momentum-dependent cross-sections

arXiv:1411.6626/ PRL 114.081302 (ACV, P. Scott, A. Serenelli)

Possible Indication of Momentum-Dependent Asymmetric Dark Matter in the Sun

arXiv:1504.04378/ JCAP 1508 (2015) 08, 040 (ACV, Scott, Serenelli)

Generalised form factor dark matter in the Sun

arXiv:1605.06502 /JCAP1611 (2016) 007 (ACV, Scott, Serenelli)

Updated constraints on velocity and momentum- dependent asymmetric dark matter

arXiv:1610.06737/JCAP03(2017)029 (B. Geytenbeek, S. Roa, P. Scott, A. Serenelli, ACV, M. White, A. Williams)

Effect of electromagnetic dipole dark matter on energy transport in the solar interior

arXiv:1703.07784/JCAP 1710 (2017)10 037: G.Busoni, A. de Simone, P. Scott, ACV

Generalised solar capture and evaporation of DM

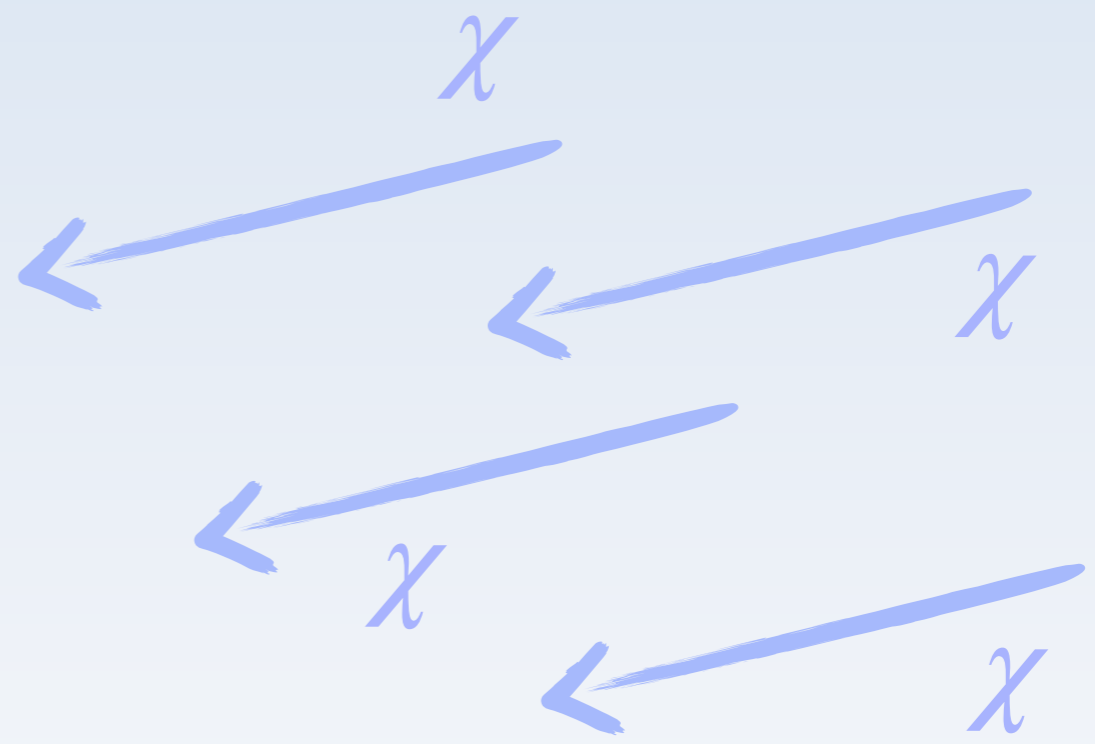
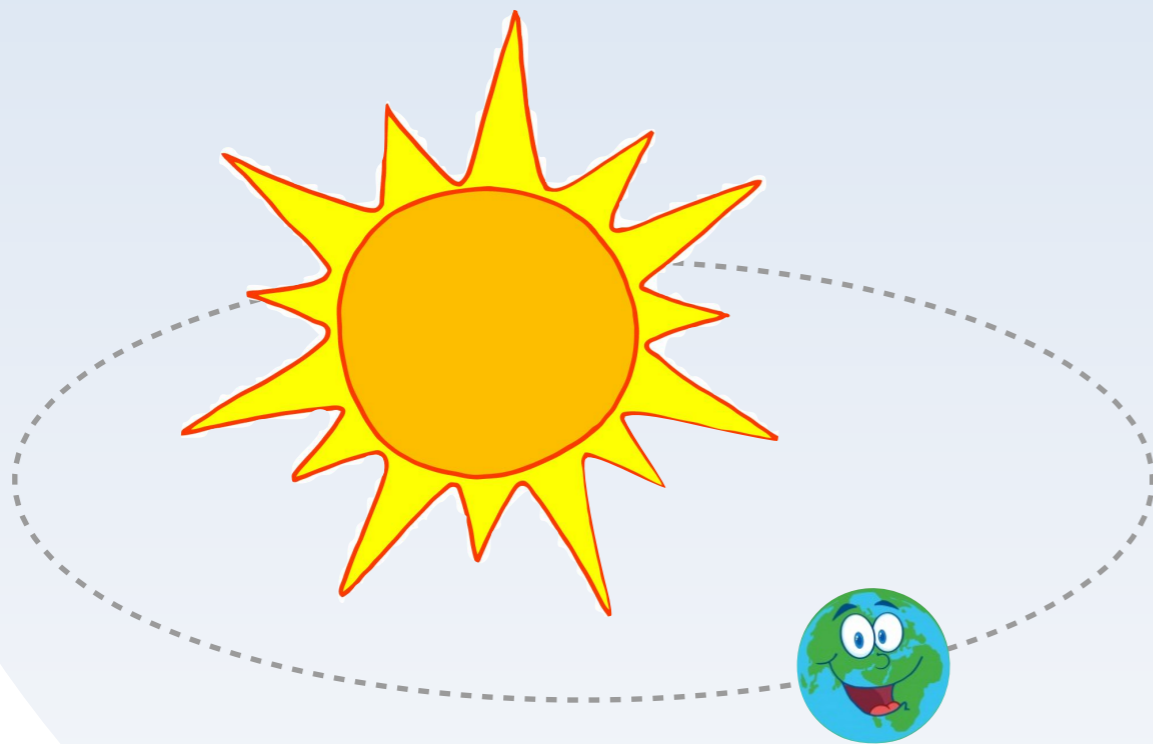
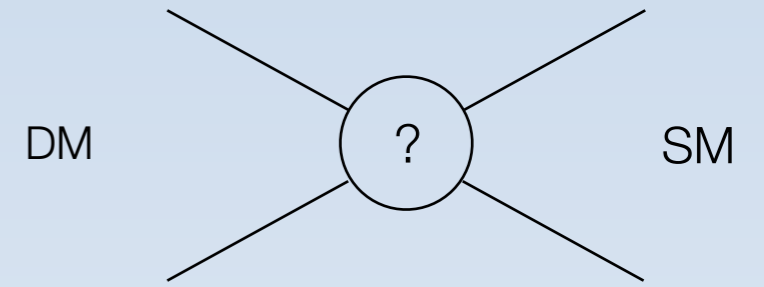
++ work in progress w/ Hannah Banks, Siyam Ansari (Imperial), Neal Kozar (Queen's)

# Overview

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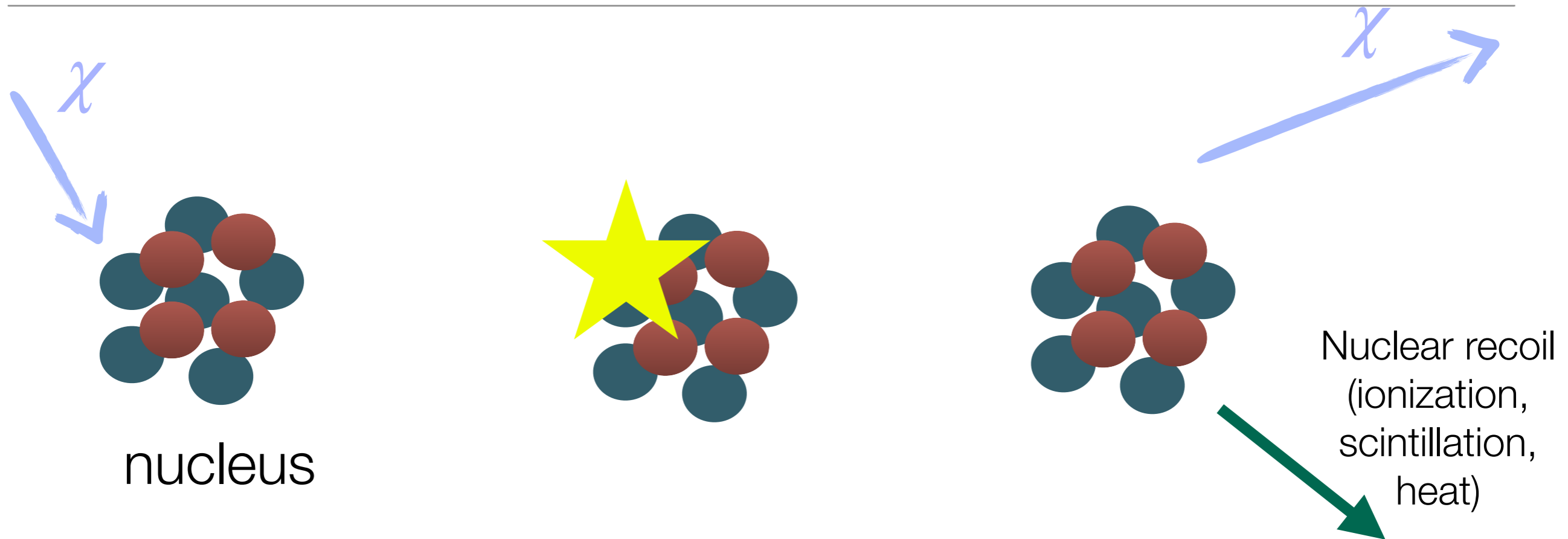
- 1. Dark matter capture in the Sun**
2. Asymmetric dark matter
3. Beyond the Sun — the Danger zone

# Direct detection





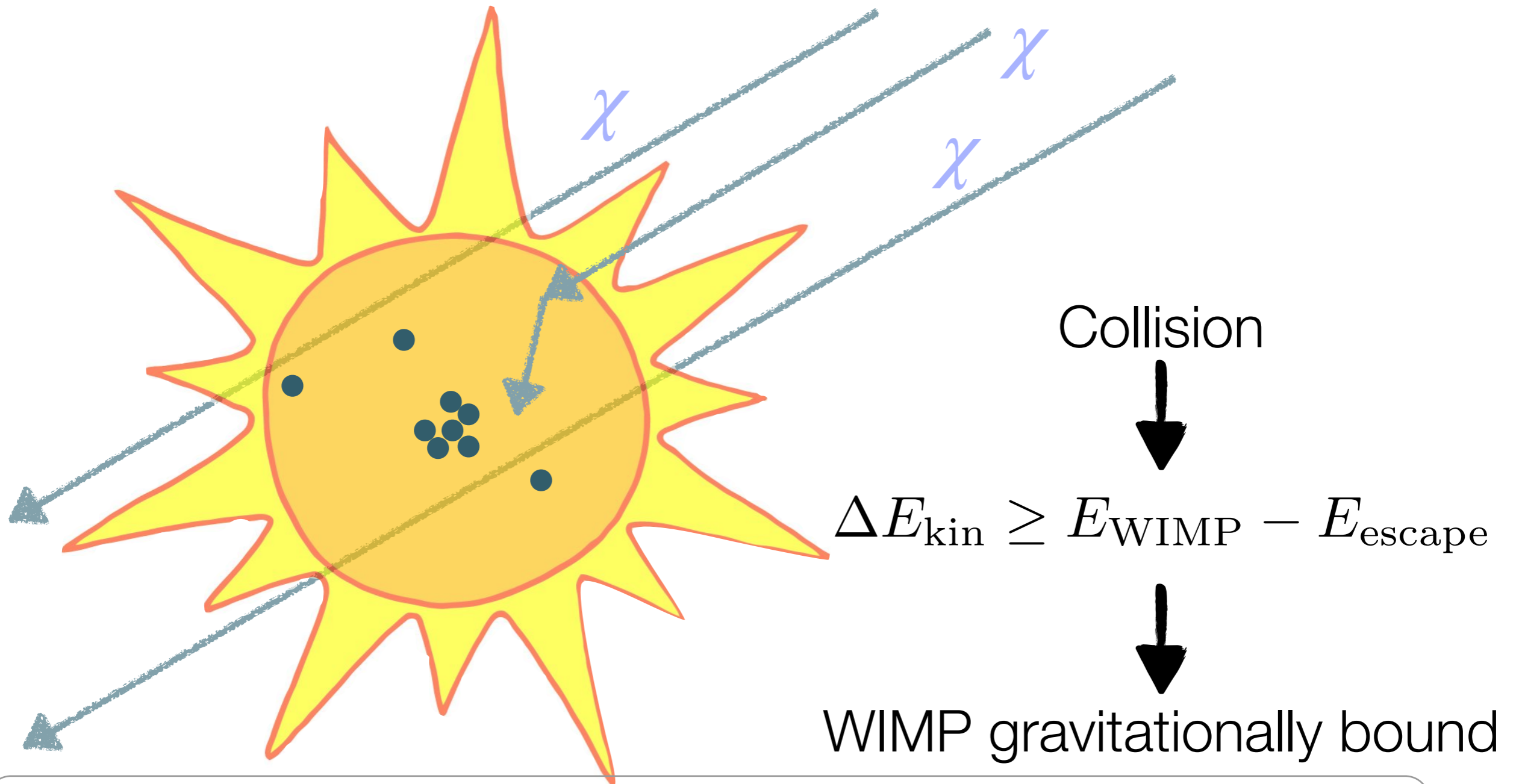
# Direct detection



Most sensitive to **heavy, fast** particles  $\rightarrow$  larger recoil signal

$$R = \int_{E_T}^{\infty} dE_R \frac{\rho_0}{m_N m_\chi} \int_{v_{min}}^{\infty} v f(v) \frac{d\sigma_{WN}}{dE_R}(v, E_R) dv$$

# The sun is a direct detection experiment



Population:

$$\frac{dN_{\chi}}{dt} = C(t) - 2A(t) - E(t)$$

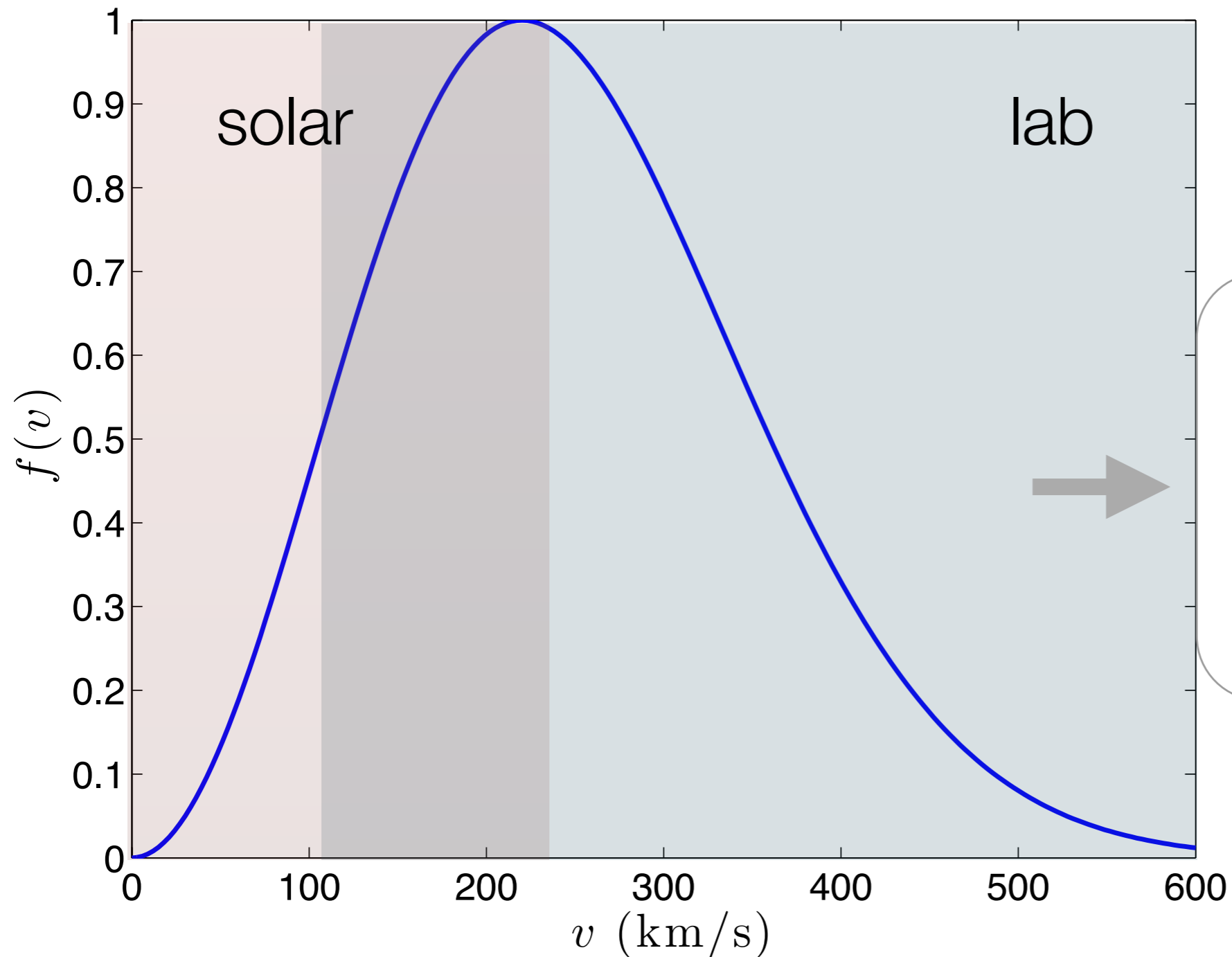
Population: 
$$\frac{dN_\chi}{dt} = C(t) - 2A(t) - E(t)$$

$C(t)$  Capture rate  $\propto \frac{\rho_\odot}{m_\chi} \int dV_\odot \int dv \frac{f(v)}{v} \sigma$

$A(t)$  Annihilation rate  $\propto N_\chi^2$

$E(t)$  Evaporation rate ( $m \lesssim 4$  GeV)  $\propto N_\chi$   
(see Busoni, de Simone, Scott, AV  
1703.07784)

# Differences with earth-based detection



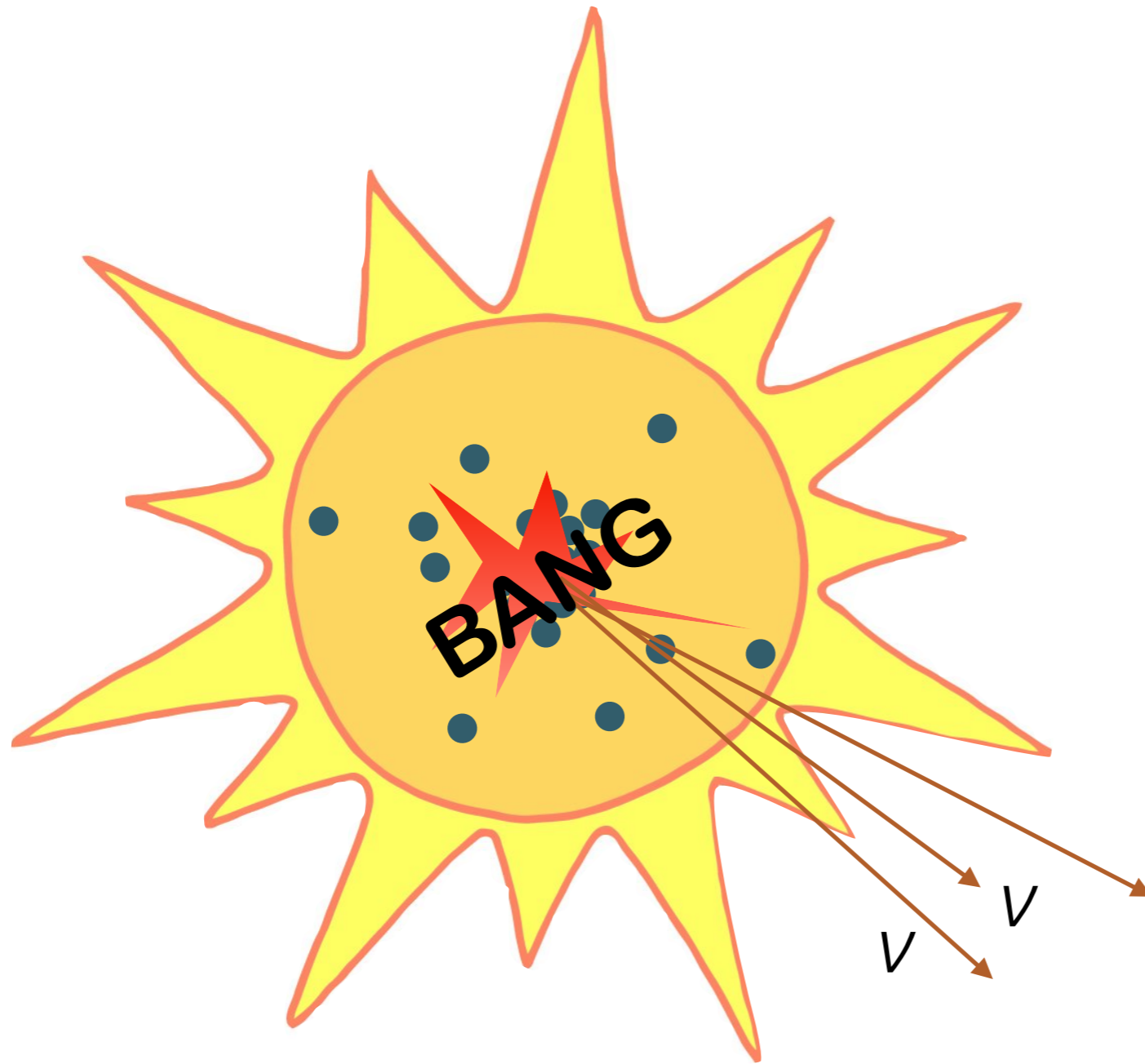
More sensitive to  
lighter DM

Different particle  
couplings



# If DM annihilates: look for neutrinos

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Actually, you reach a steady state:  
 $C(t) = A(t)$

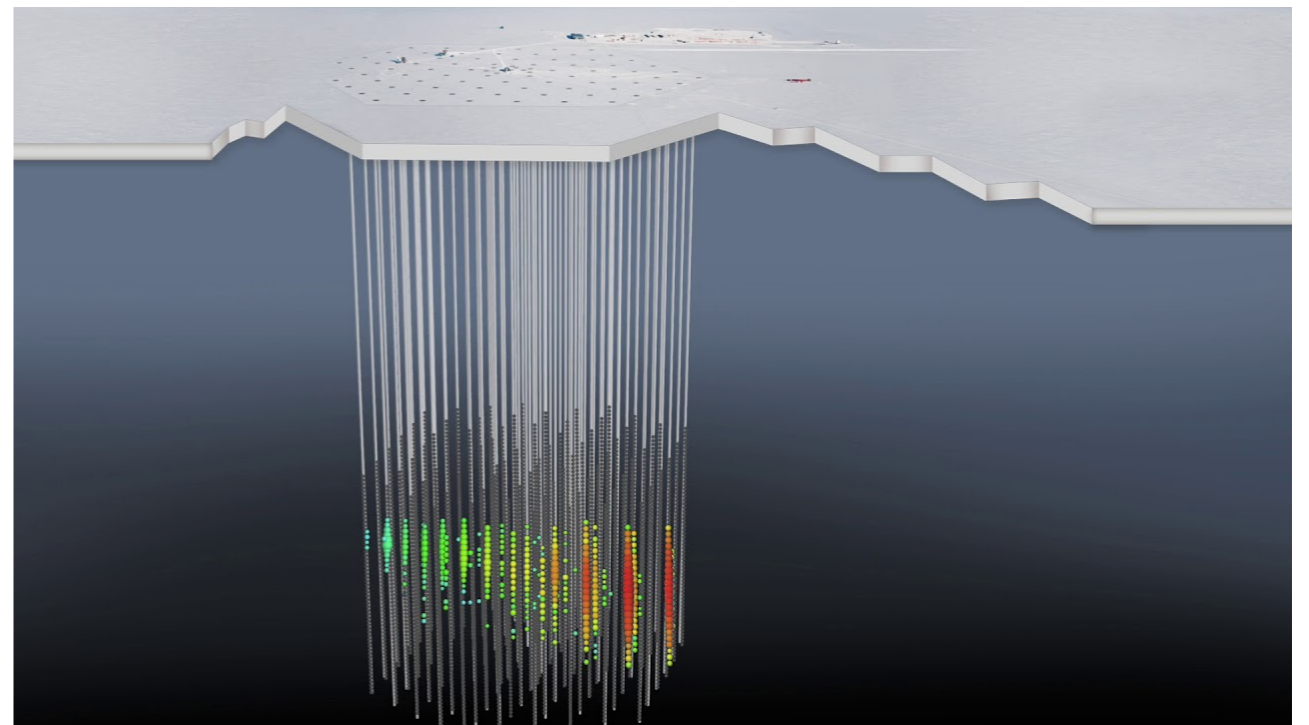
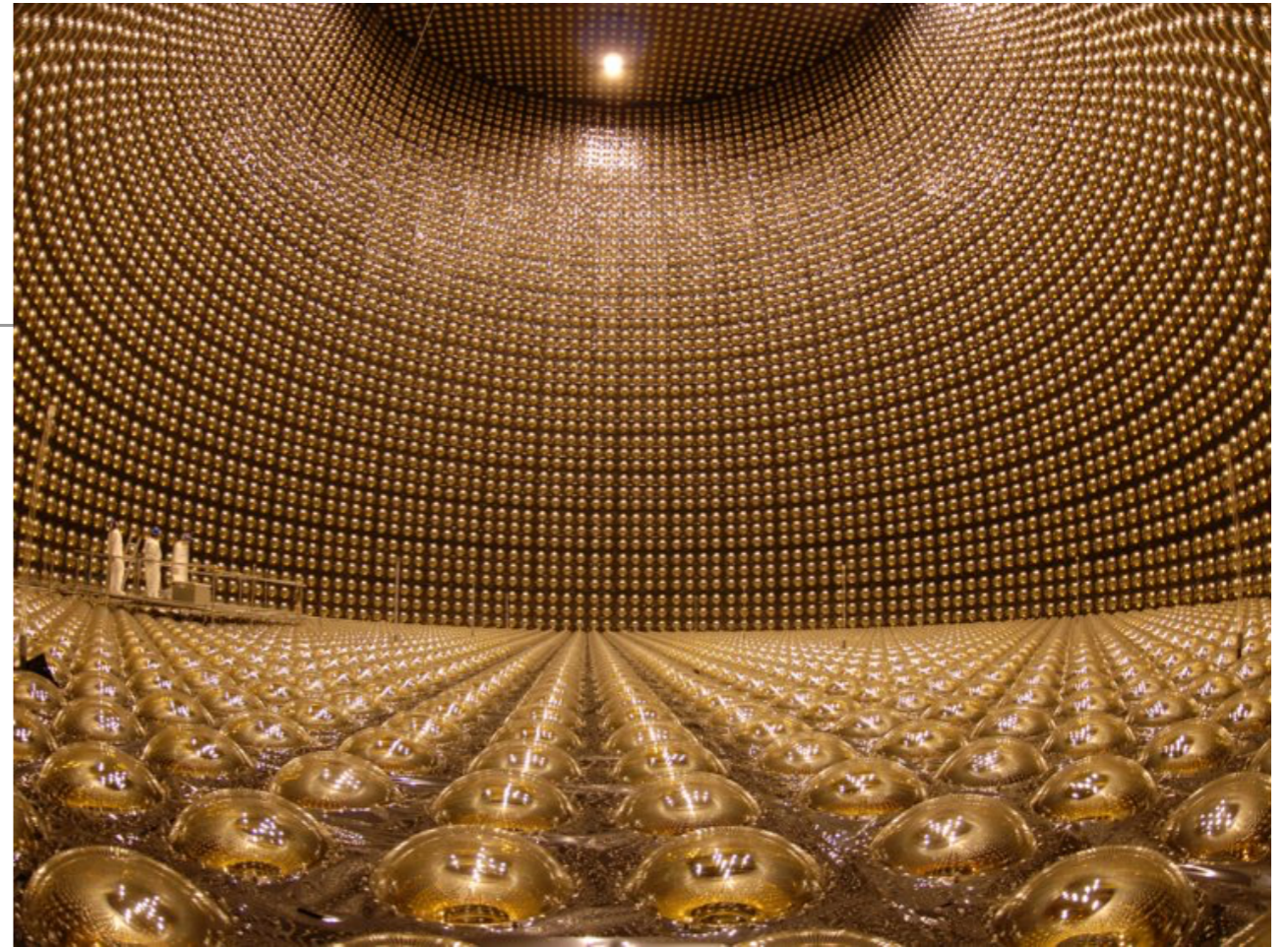


# Neutrinos at Earth

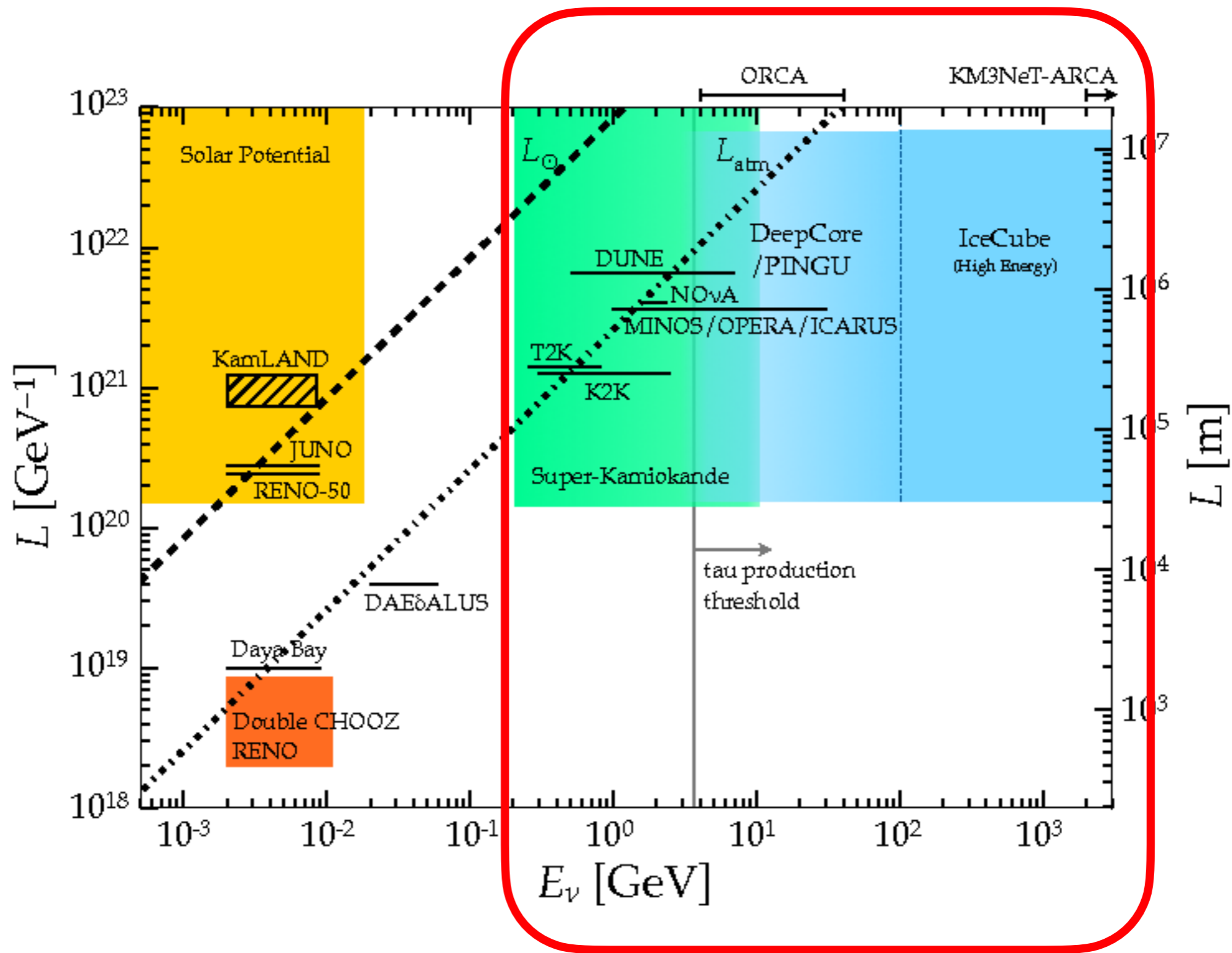
$$E_\nu \simeq m_\chi / f$$

$f$  is a number of O(1-10)

Solar neutrinos (the ones from nuclear fusion) produce  $< 10$  MeV scale neutrinos. This means that **GeV or higher neutrino** signals from the solar core are a **smoking gun for new physics**.\*

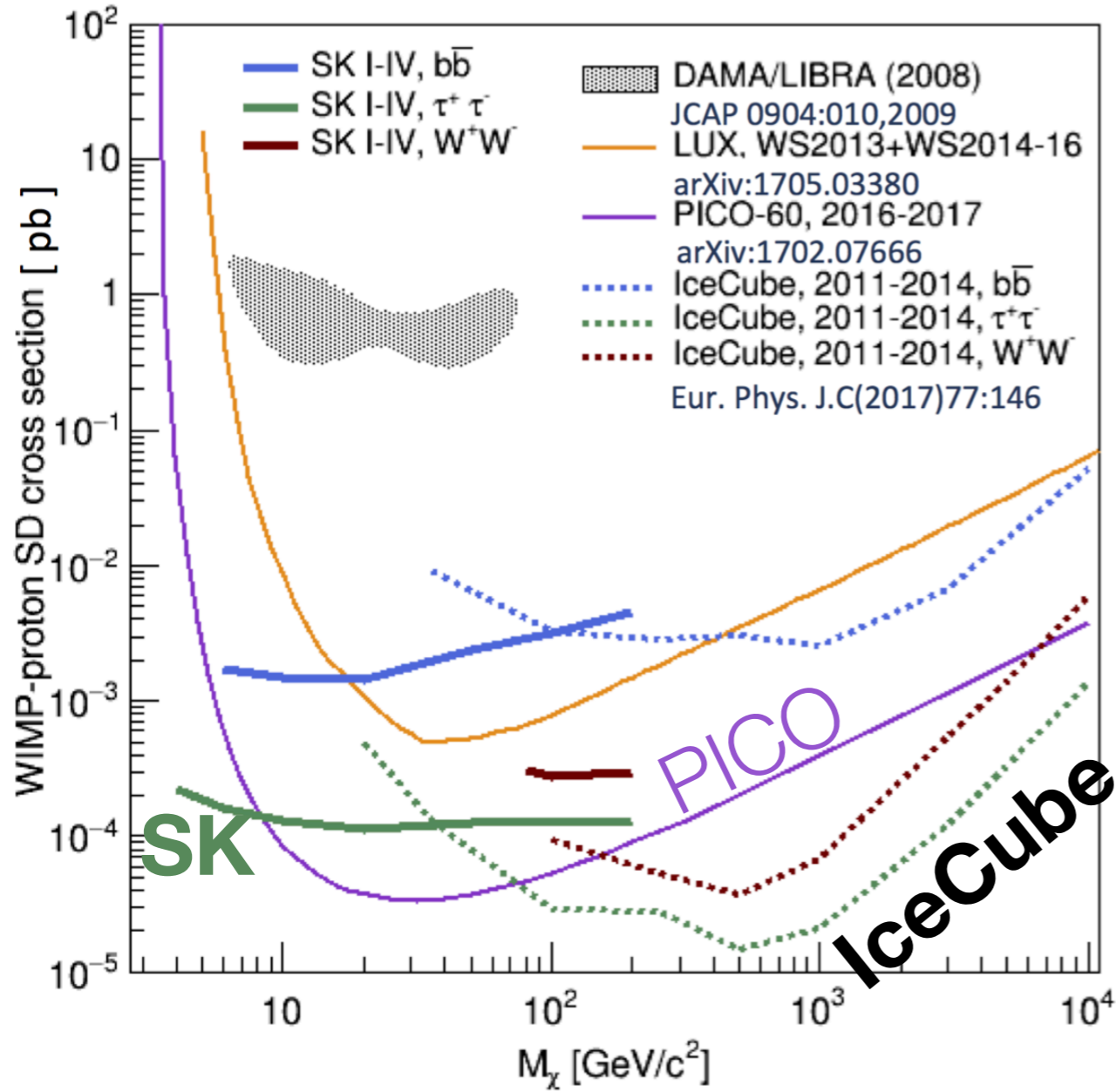


\*except for solar atmospheric neutrinos shh<sup>10</sup>

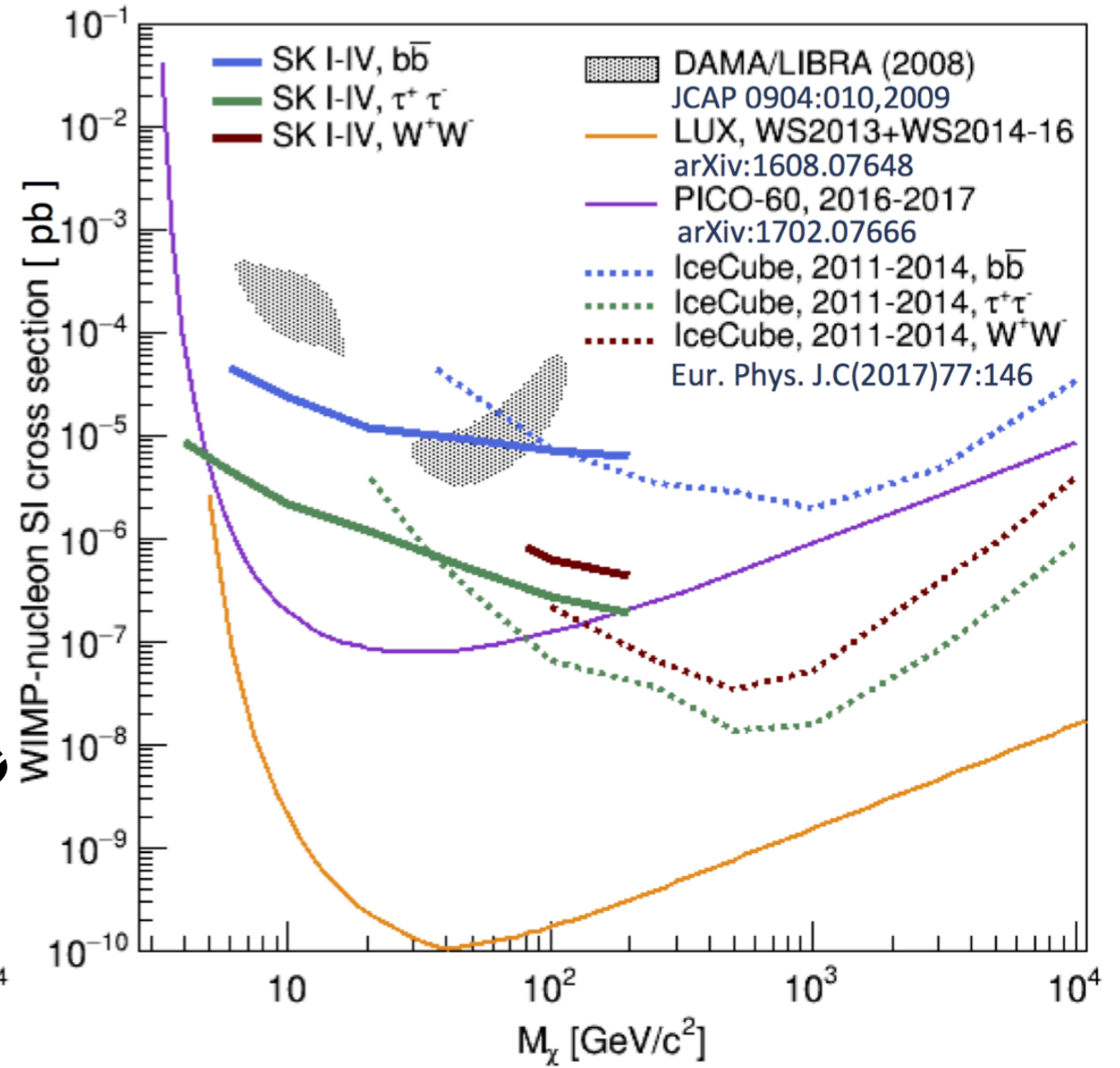




(a) spin dependent interactions



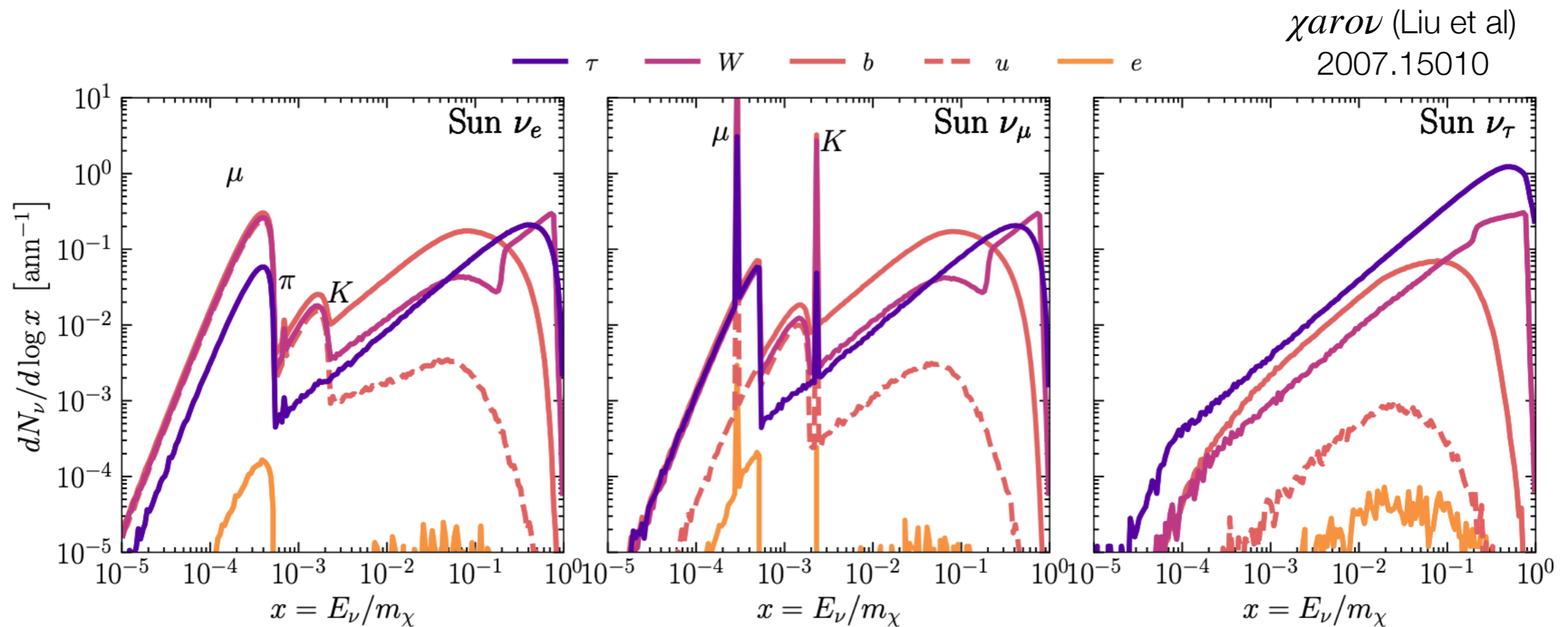
(b) spin independent interactions





# Stopped mesons

Monoenergetic neutrinos from stopped meson ( $\pi$ ,  $K$ ) decay can provide complementary constraints at low mass

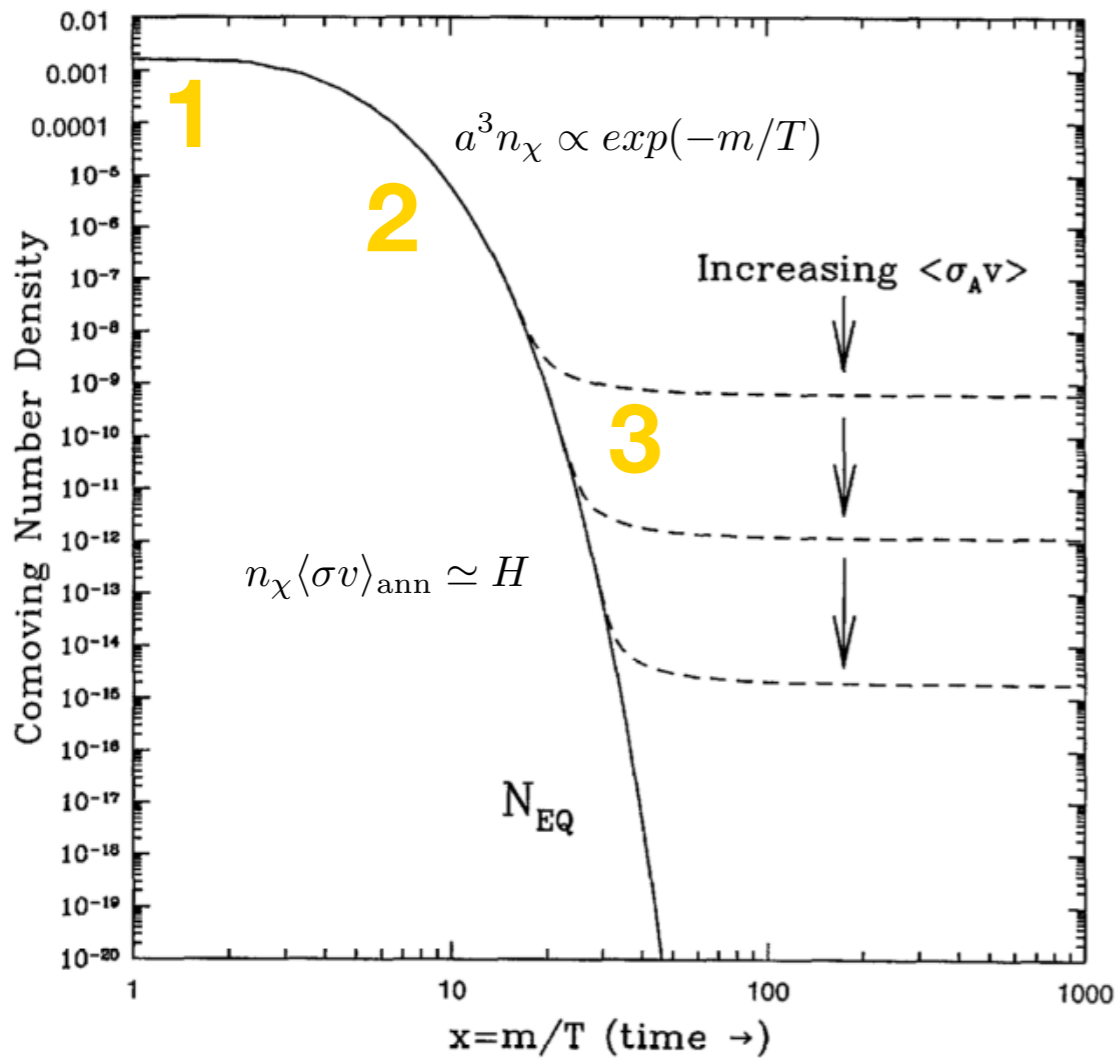


<https://github.com/IceCubeOpenSource/charon>

See also Rott et al 1609.04876

1. Dark matter capture in the Sun
- 2. Asymmetric dark matter**
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# “WIMP miracle”



“Weak scale” cross section

$$m_{DM} \gtrsim 100 \text{ GeV} \quad \Omega_{DM} h^2 \sim 0.1$$

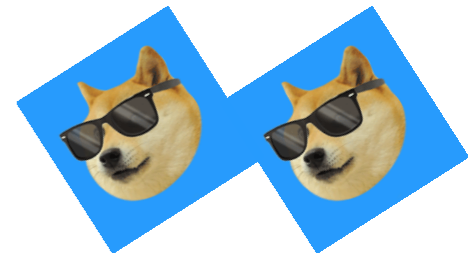


# If we try with SM

Similar approach with **Neutrinos**  
(keeping in mind  $m \ll T$ )

$$\Omega_{\nu,FO} = \Omega_{\nu,obs}$$

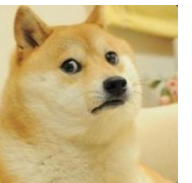
$$(N_{\nu,eff} = 3.046)$$



## Baryons?

Annihilation of a symmetric baryon component:

$$\Omega_{B,FO} \sim 10^{-10}$$



“baryon disaster” (Sarkar)

Require an **initial asymmetry**

Starting over:

$$\text{Require } \eta_b = \frac{n_B - \bar{n}_B}{n_\gamma} \sim 10^{-9}$$

$$\text{Note } \Omega_{DM} \sim 5\Omega_b$$

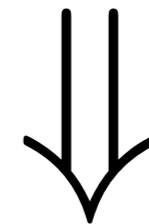
So if we start with an initial (shared) asymmetry such that

$$n_b \sim n_{DM}$$

$$\Rightarrow m_{DM} \sim 5m_b$$

Observed abundance  $\rightarrow$   
prediction of a mass scale

If asymmetry is generated before thermal freeze-out



Exponential Boltzmann suppression means

$$\langle \sigma v \rangle_{ann} \gtrsim \text{few} \times \langle \sigma v \rangle_{WIMP}$$

Mass-asymmetry relation:

$$\frac{m_{DM}}{m_p} \frac{\eta_D/q}{\eta_B} = \frac{1 - r_\infty}{1 + r_\infty} \frac{\Omega_{DM}}{\Omega_b}$$

Reviews

Petraki & Volkas 1305.4939

Zurek 1308.0338



Population:  $\frac{dN_\chi}{dt} = C(t) - 2A(t) - E(t)$

$C(t)$  Capture rate

~~$A(t)$  Annihilation rate~~

~~$E(t)$  Evaporation rate (low m)~~

No anti-DM leftover in the universe:  
asymmetric dark matter

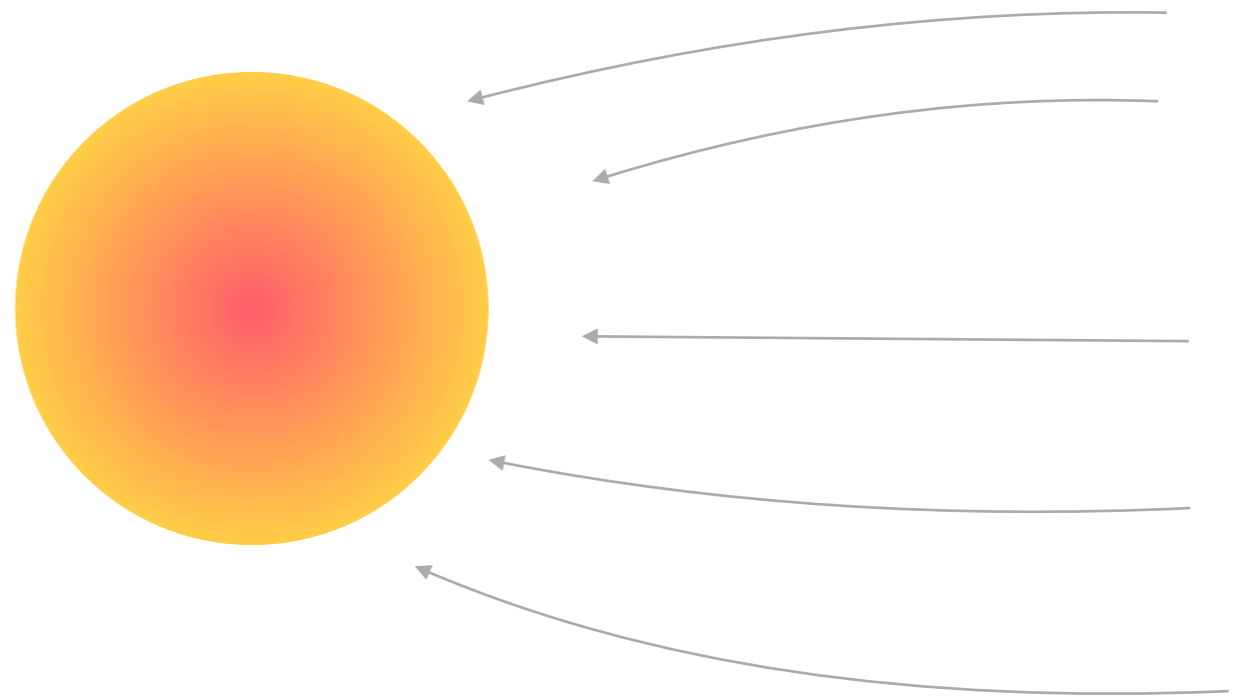
# Suppressing annihilation (Asymmetric DM)

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No annihilation: DM just accumulates...

Can accumulate a lot of DM

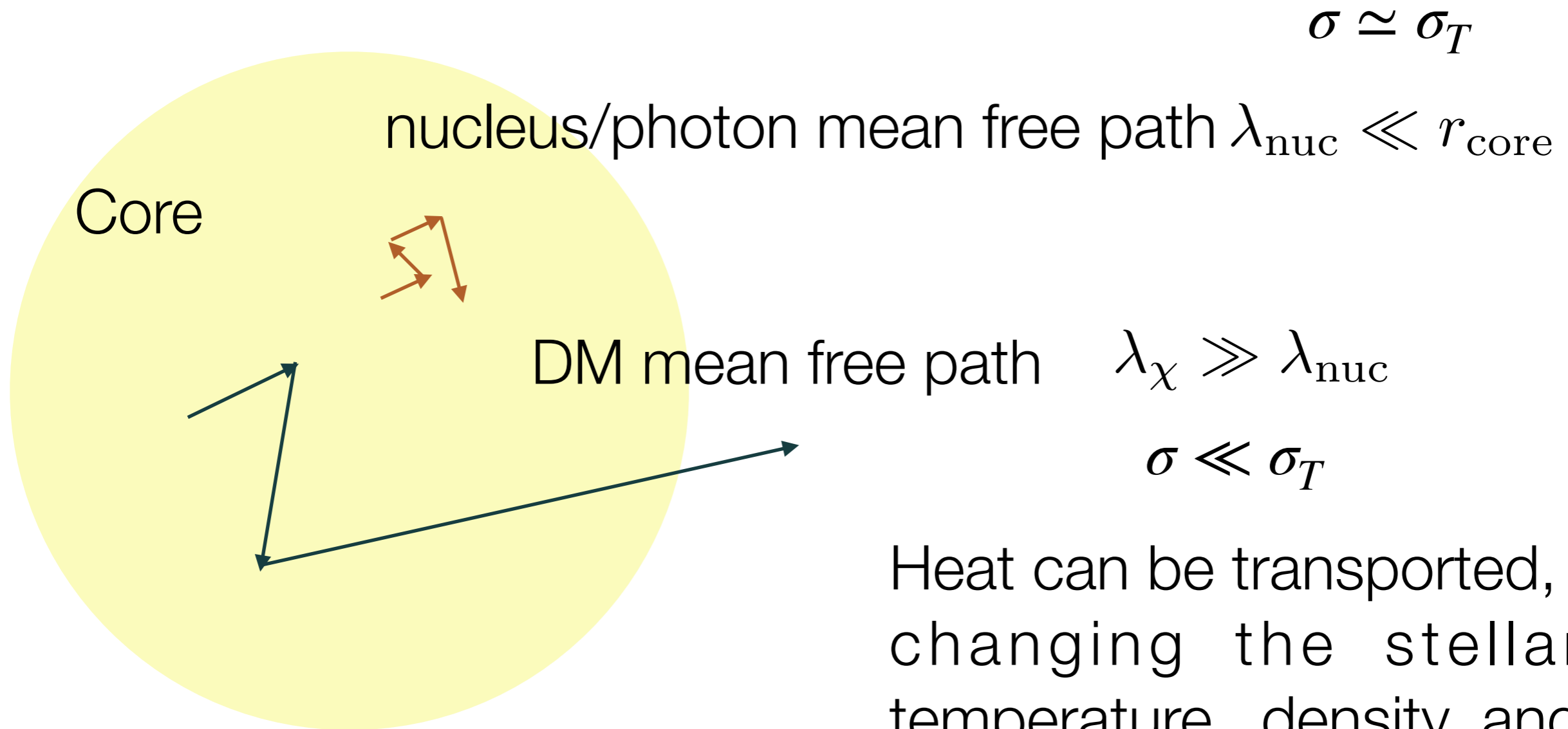
$$N_\chi \lesssim 2\pi R_\odot^2 (\rho_\chi / m_\chi) v_\odot T_\odot$$
$$\simeq 10^{-10} n_p \sim 10^{46}$$



(impact parameter a little bigger than  $R_\odot$  thanks to gravity)

# Asymmetric DM in stars

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Heat can be transported, changing the stellar temperature, density and pressure profiles

**Can this be observed?**

# Probes of Solar structure

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## Obvious

Mass, age, radius, luminosity are extremely well-measured and are the first thing any solar model must satisfy.

## Neutrinos\*

$pp$  constrained by overall luminosity, but other byproducts of  $pp$  chain extremely sensitive

to  $T$ . e.g.  $\phi_{\nu, ^8B} \propto T_c^{25}$

\*actually this mechanism was first studied as part of the solar neutrino problem: lower than expected solar core  $T \rightarrow$  fewer neutrinos

## Helioseismology?



No, it's because neutrinos change flavour as they propagate to Earth

Art McDonald (Queen's)

Nobel Prize

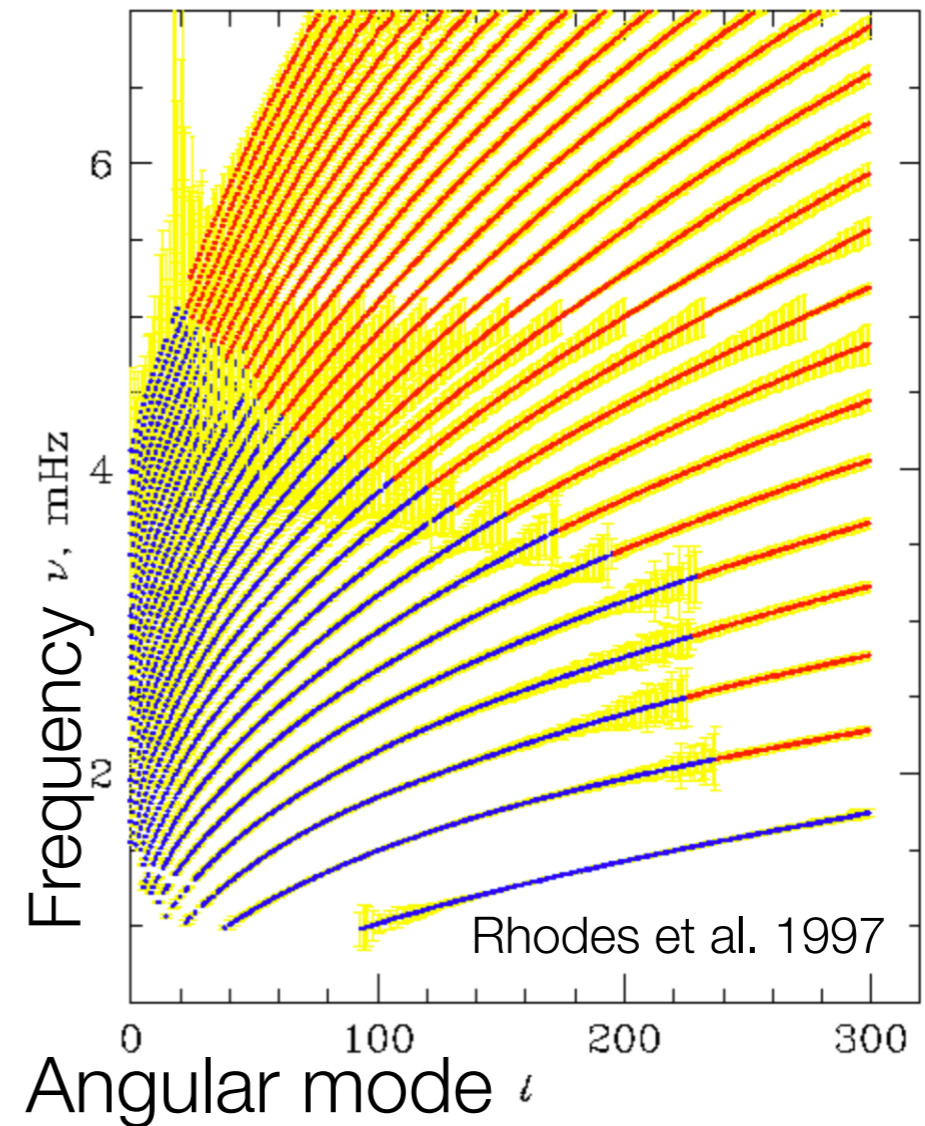
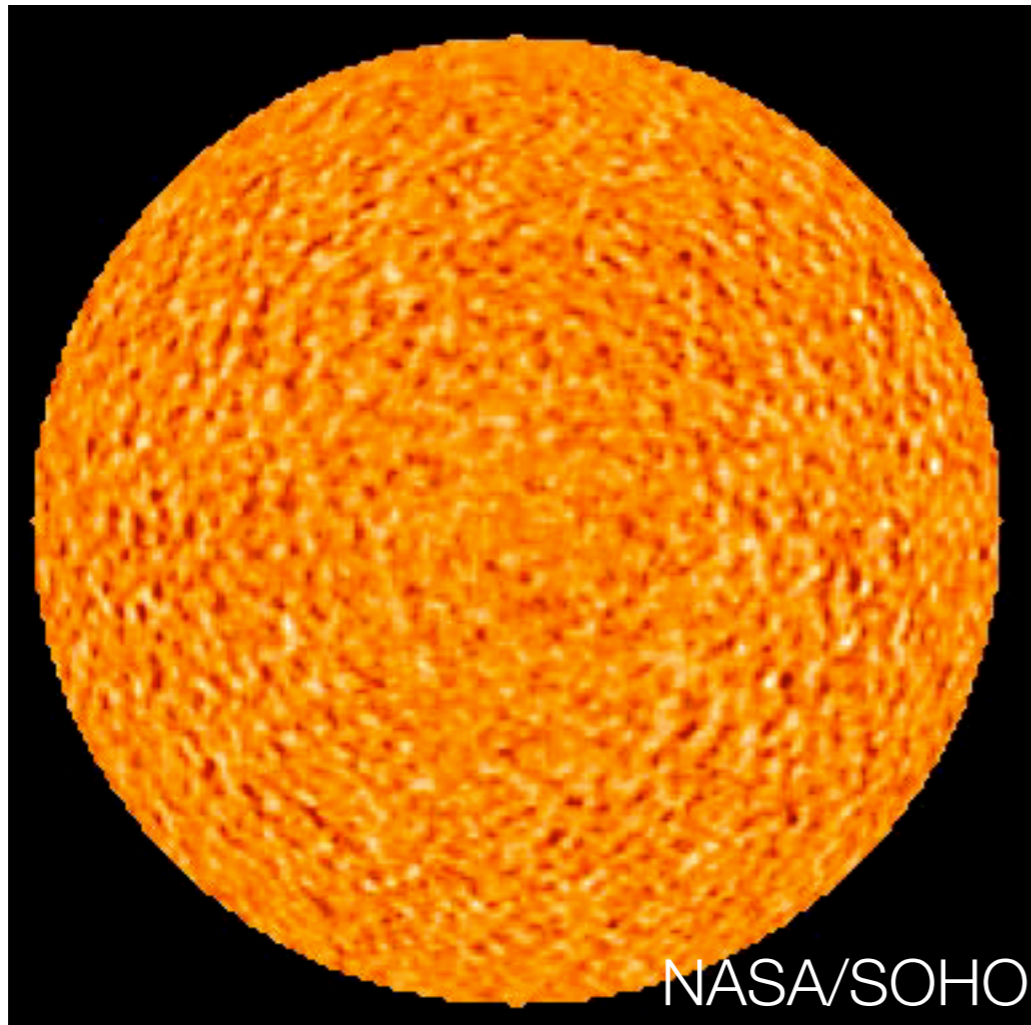


# Development

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- the 80's & the first solar crisis: Nauenberg, Press & Spergel, Gould & Raffelt
- The renaissance: Lopes/Bertone/Silk astro-ph/0205066++, Scott et al 0809.1871++
- The post-modern era (second solar crisis): Frandsen & Sarkar 1003.4505; Cumberbatch et al 1005.5102; Taoso et al 1005.5711; Lopes, Silk, Casanellas (+ many papers), ACV, Scott, Serenelli, Busoni (many papers)
- Other stars: Casanellas ++ 1212.2985 & a few more
- And a lot more...

# Helioseismology



The **frequencies** of these **eigenmodes** should be predictable from:

-**density**

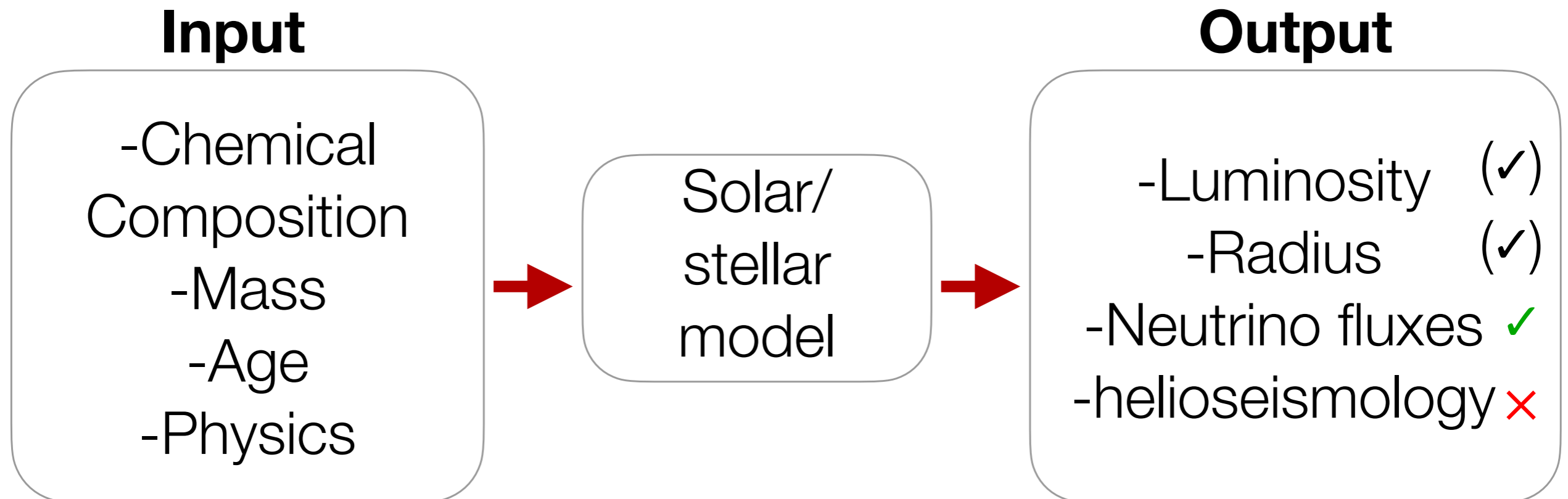
-**sound speed**

-molecular weight (i.e. **elemental composition**)

-**convective zone radius**

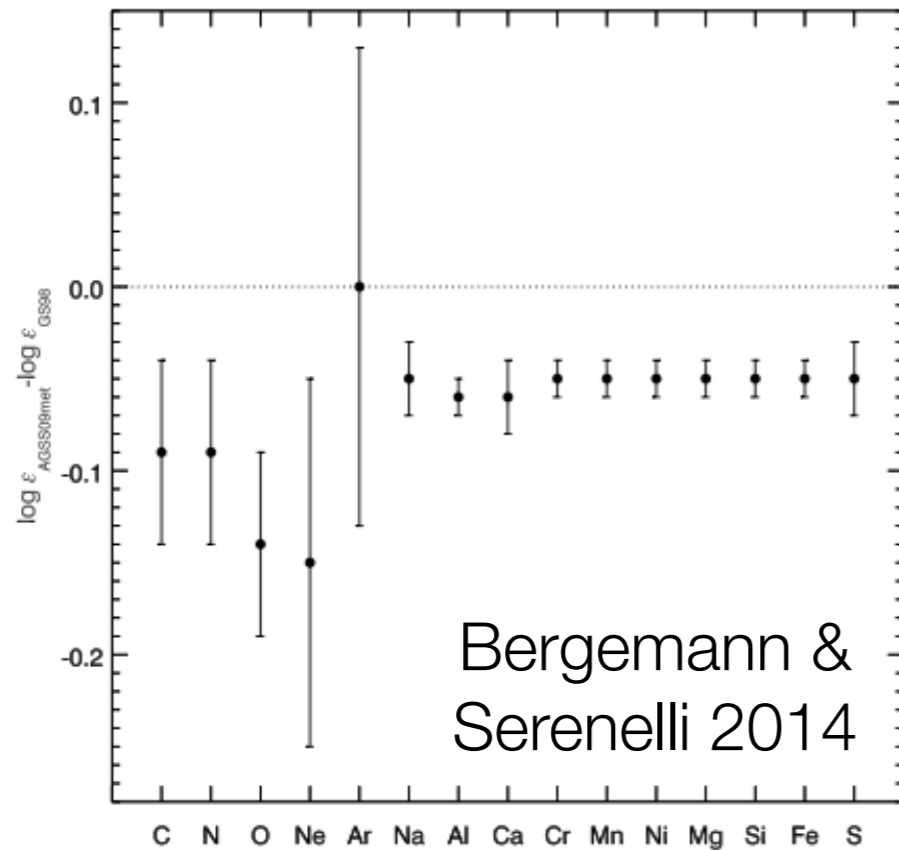
# Standard Solar Model (since 1970s)

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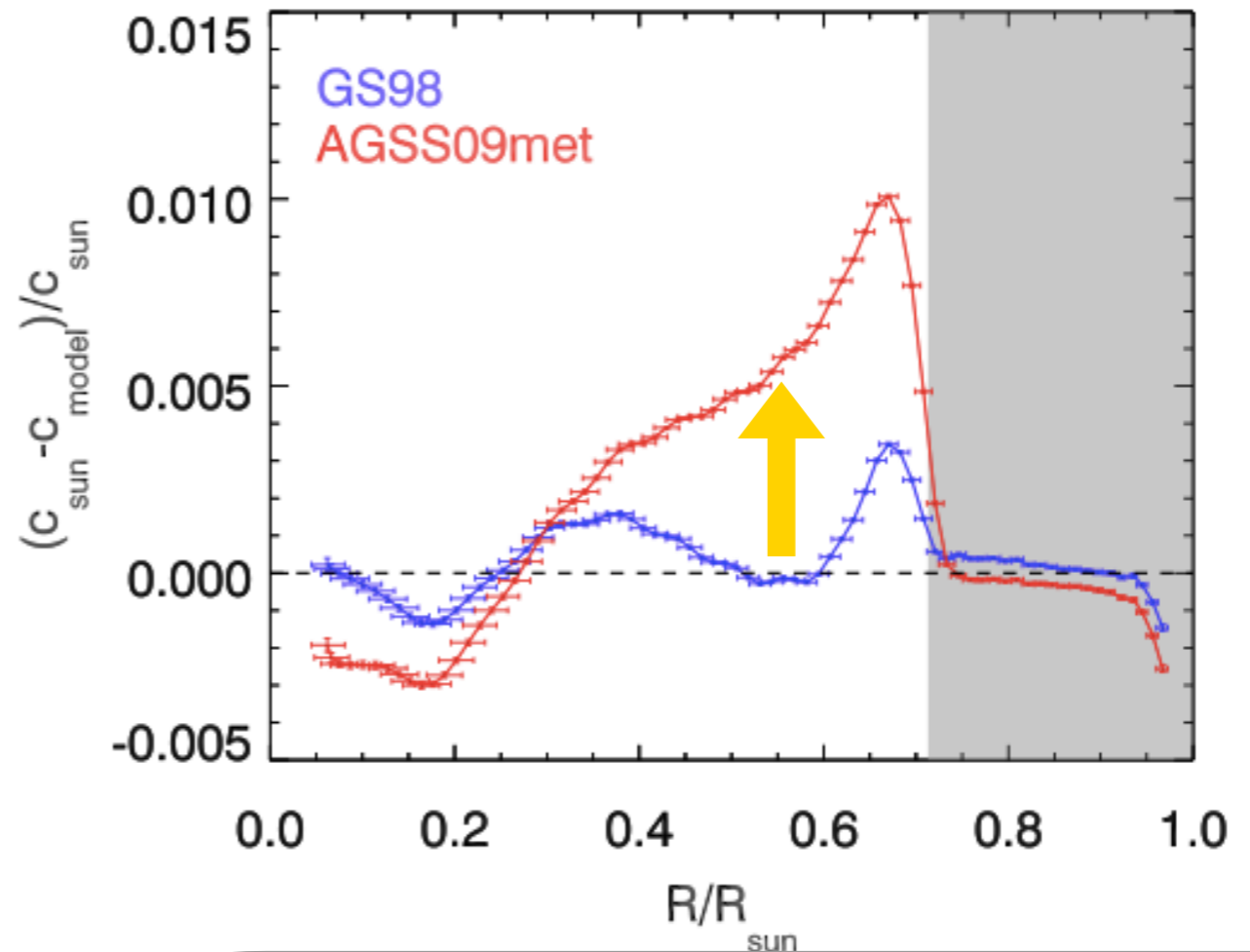


Known problem since 2004: still no solution!

# Solar composition problem



**revised - old abundances**



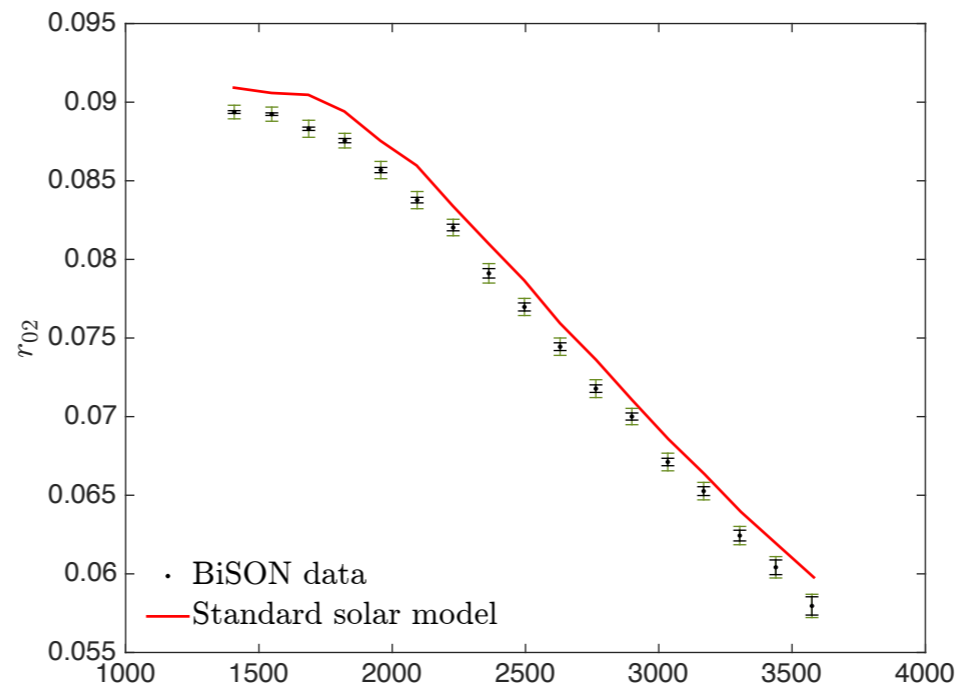
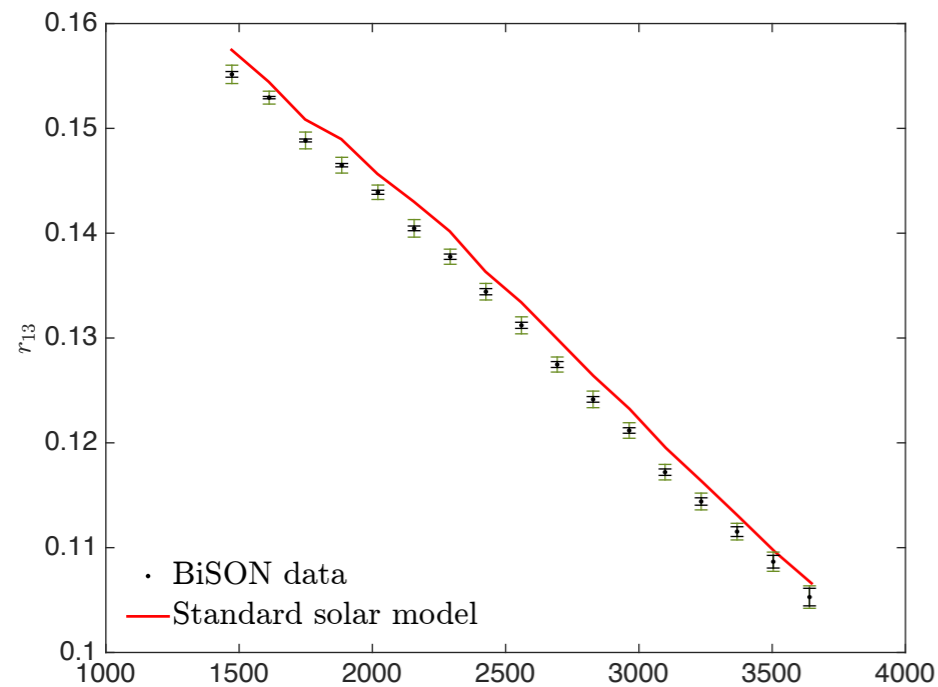
$$R_{CZ,\odot} = 0.713 \pm 0.001 R_{\odot}$$

$$R_{CZ,SSM} = 0.722 \pm 0.004 R_{\odot}$$

Mainly: smaller mean molecular weight, which shifts temperature, pressure, density gradients

# Solar composition problem

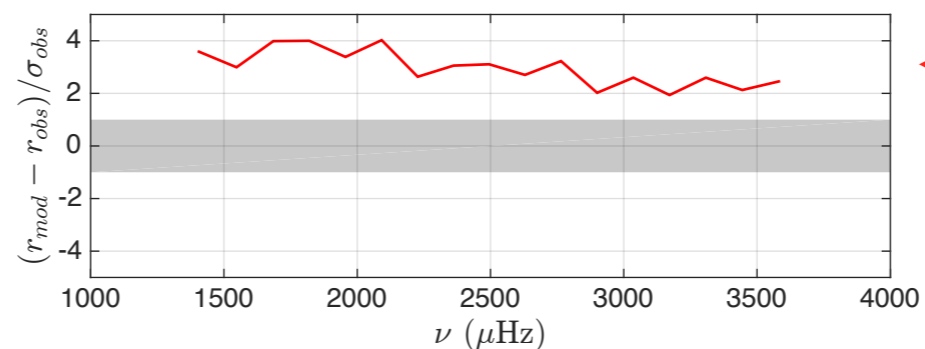
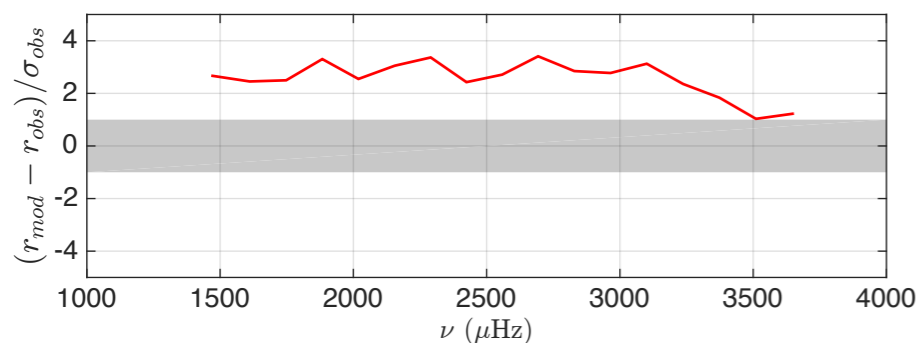
## Small frequency separations: a probe of the core



$$\Delta_l(n) \equiv \nu_{n,l} - \nu_{n-1,l}$$

$$d_{l,l+2}(n) \equiv \nu_{n,l} - \nu_{n-1,l+2}$$

$$\simeq -(4l + 6) \frac{\Delta_l(n)}{4\pi^2 \nu_{n,l}} \int_0^{R_\odot} \frac{dc_s}{dr} \frac{dr}{r}$$



← SSM describes the core **very badly**

$$r_{02}(n) = \frac{d_{02}(n)}{\Delta_1(n)}$$

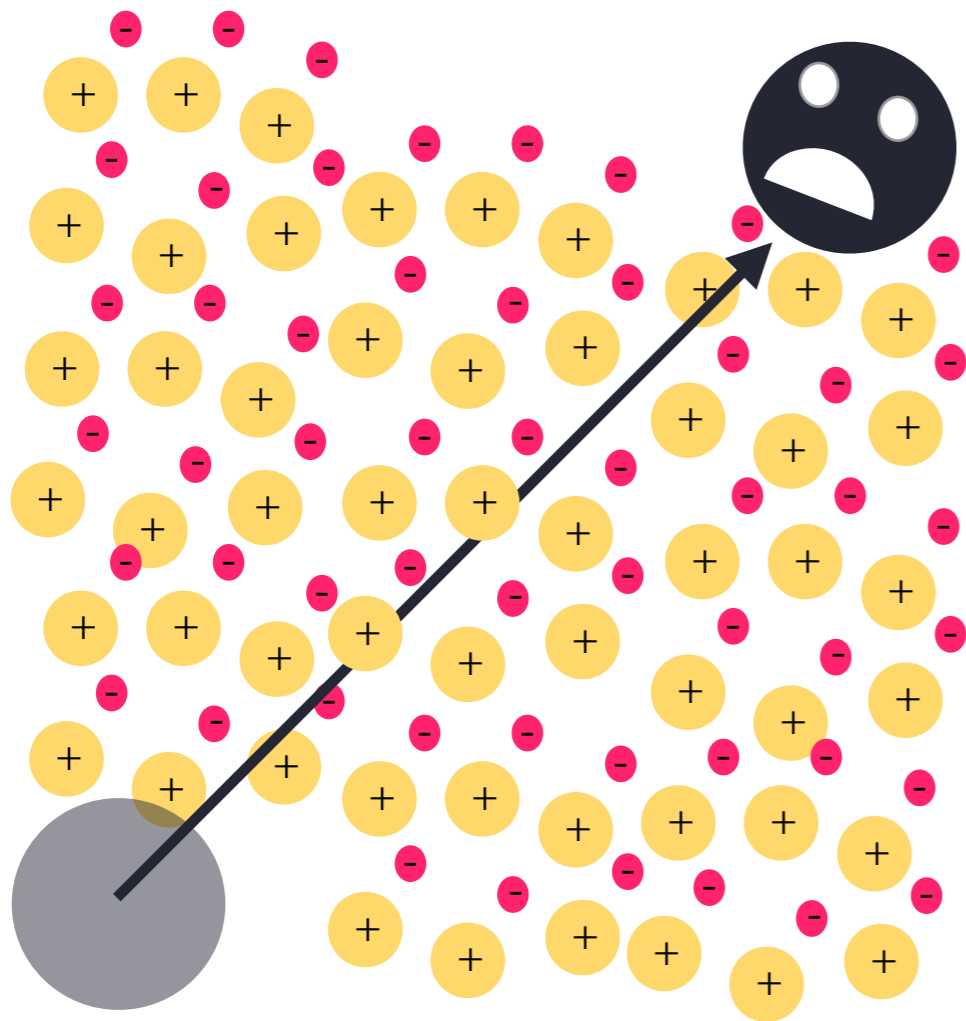
$$r_{13}(n) = \frac{d_{13}(n)}{\Delta_0(n+1)}$$



# Heat transport: two regimes

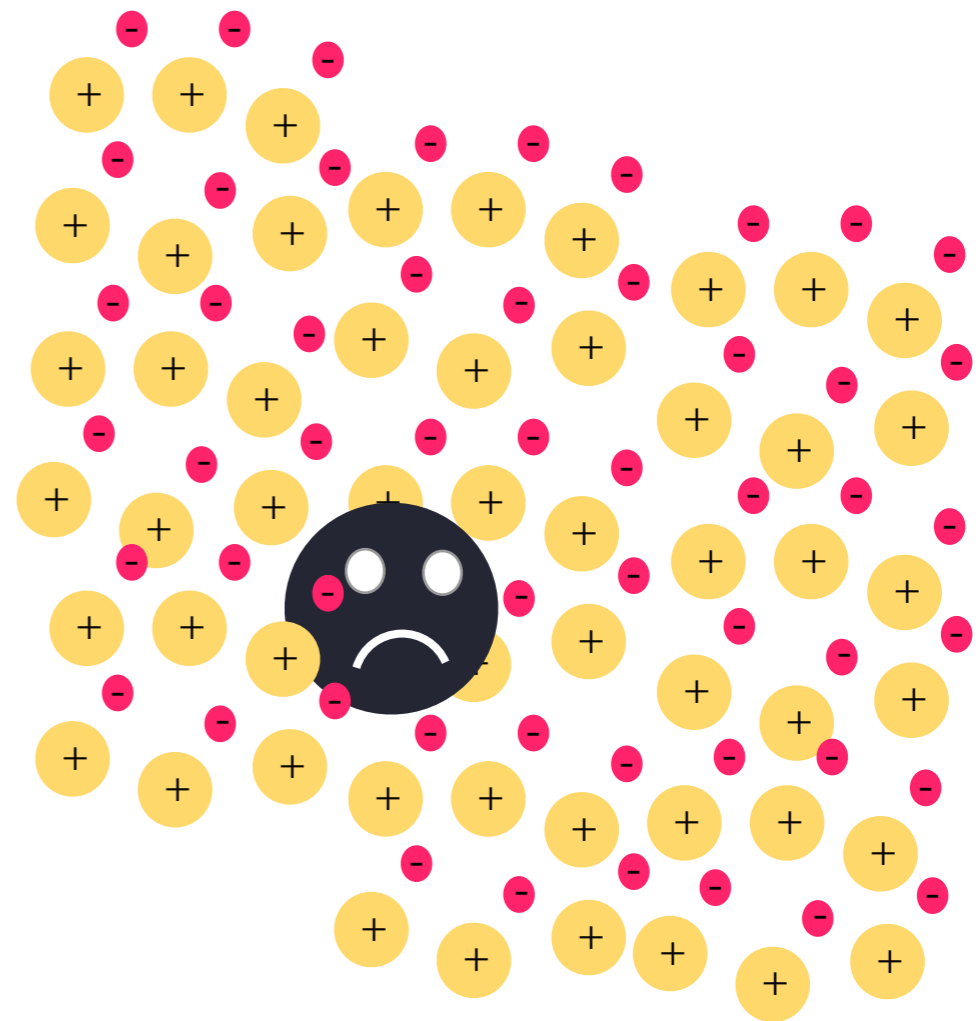
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Interactions too weak

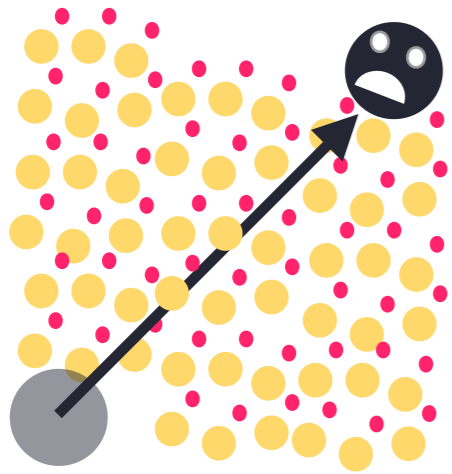


DM goes far but cannot efficiently transfer momentum

Interactions too strong



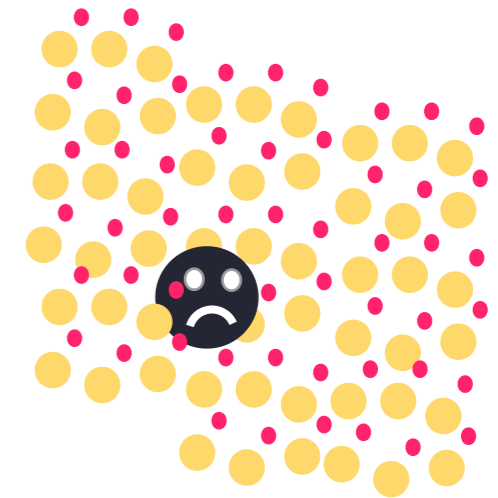
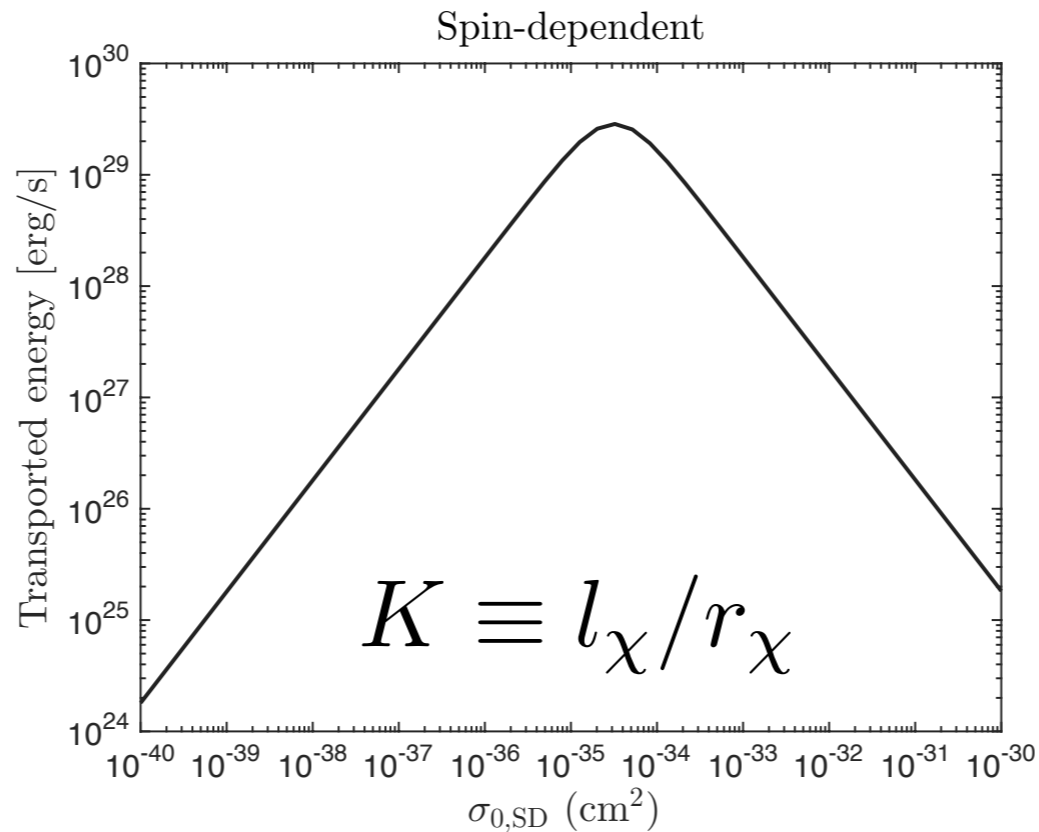
Efficient momentum transfer but DM is "stuck"



**Knudsen**  
(non-local)

$$K \gtrsim 1$$

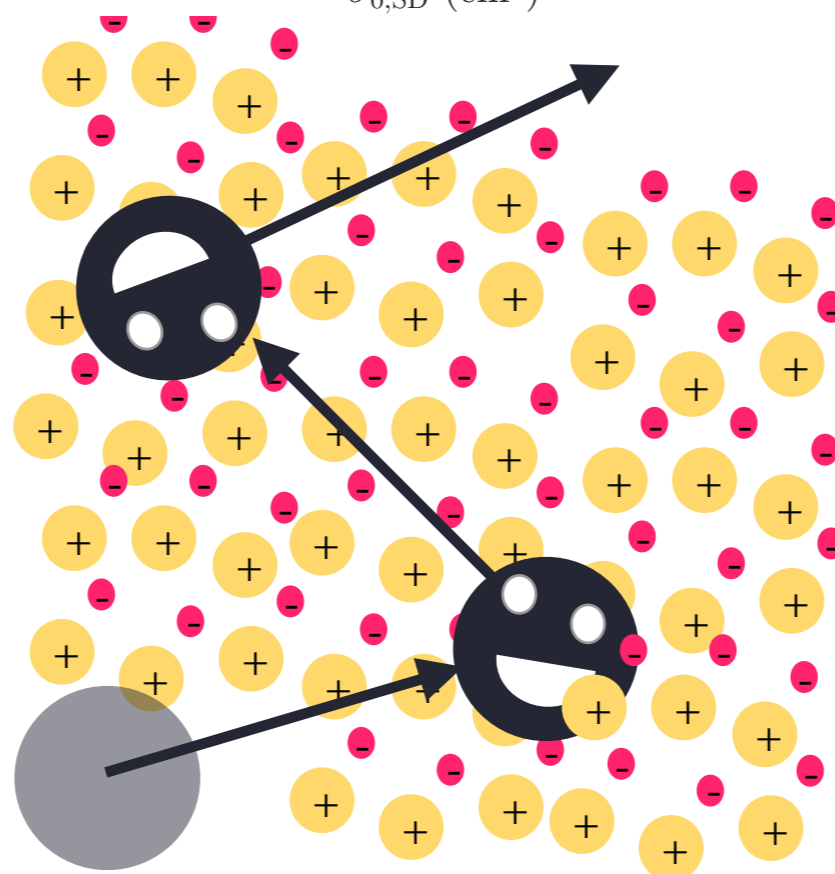
Calculable  
(but wrong)



**LTE**

$$K < 1$$

Somewhat  
calculable  
but unstable



optimal heat transport:  
"Knudsen Peak"

not calculable

# Stitching together: Monte Carlo (the “most correct” approach)

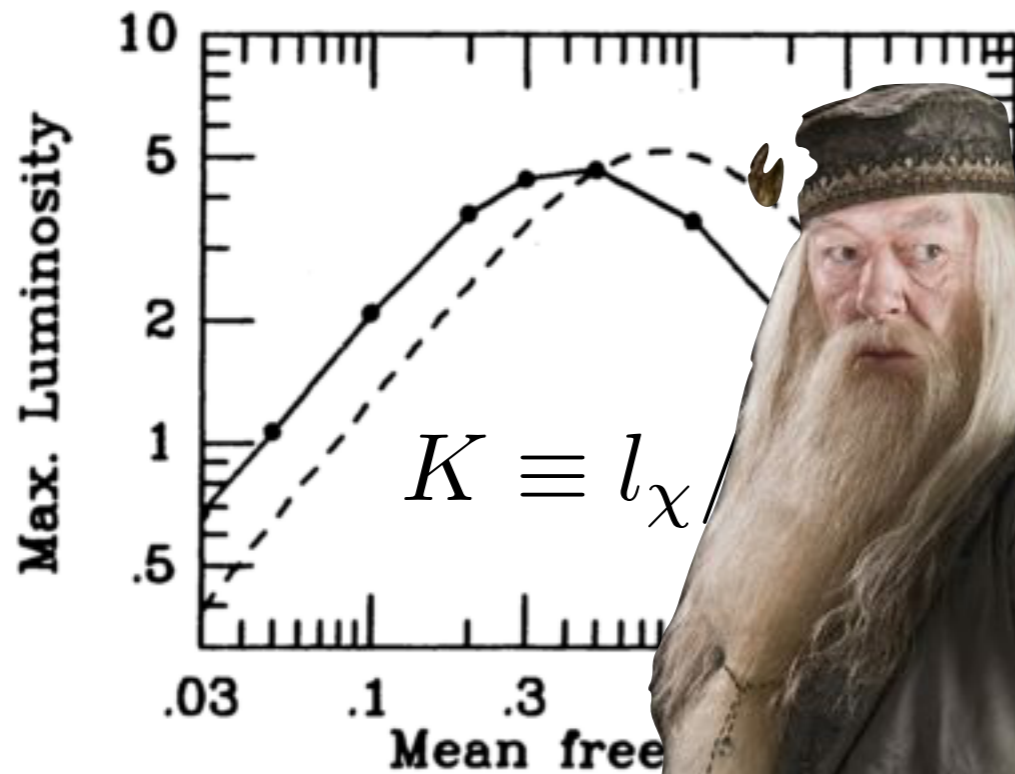


FIG. 11.—Maximum luminosity carried by model described in Fig. 8. The maximum refers to the corresponding curves for other mean free path values. The maximum value corresponds to a Monte Carlo run for that value. The formula used by Gilliland *et al.* (1986) in their model for transport in the Sun.

Gould & Ford



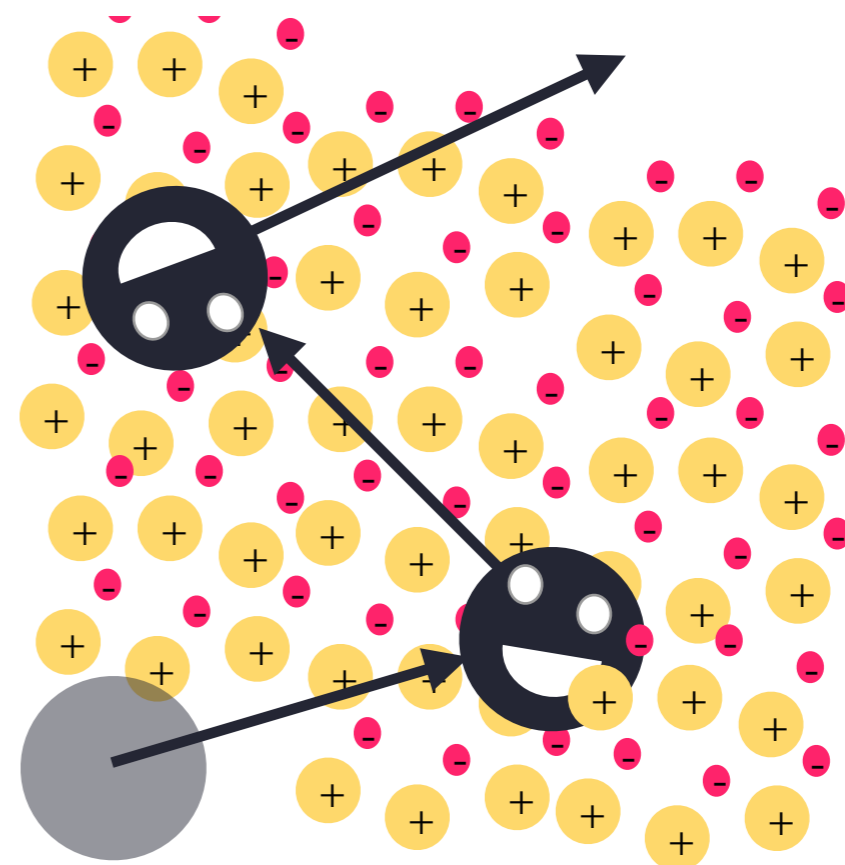
$$n_{\chi}(r) = \boxed{\text{Local}} f(K)n_{\chi,\text{LTE}} + \boxed{\text{nonlocal}} [1 - f(K)] n_{\chi,\text{iso}},$$

$$L_{\chi,\text{total}}(r, t) = f(K)h(r, t)L_{\chi,\text{LTE}}(r, t).$$

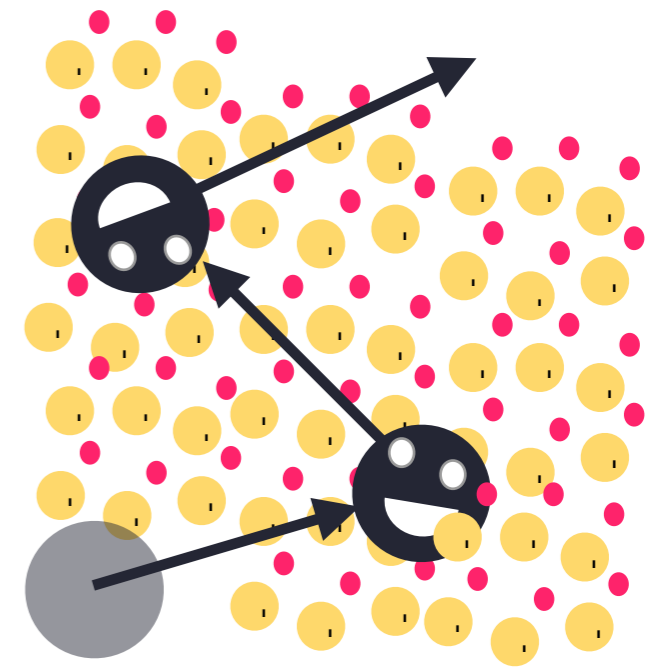
$$h(r) = \left( \frac{r - r_{\chi}}{r_{\chi}} \right)^3 + 1,$$

$$f(K) = \frac{1}{1 + \left( \frac{K}{K_0} \right)^{1/\tau}},$$

interpolating  
fcs

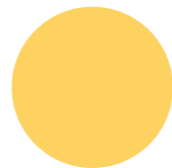


Knudsen peak depends sensitively on the microphysical interaction (i.e. the structure of the cross section)



**E.g. “billiard ball”**

**1/r force**



# Systematic parametrization: NR EFT/ NREO

$$\begin{aligned}
 \mathcal{O}_1 & 1_\chi 1_N \\
 \mathcal{O}_2 & (\vec{v}^\perp)^2 \\
 \mathcal{O}_3 & i\vec{S}_N \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp\right) \\
 \mathcal{O}_4 & \vec{S}_\chi \cdot \vec{S}_N \\
 \mathcal{O}_5 & i\vec{S}_\chi \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp\right) \\
 \mathcal{O}_6 & \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_N\right) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi\right) \\
 \mathcal{O}_7 & \vec{S}_N \cdot \vec{v}^\perp \\
 \mathcal{O}_8 & \vec{S}_\chi \cdot \vec{v}^\perp \\
 \mathcal{O}_9 & i\vec{S}_\chi \cdot \left(\vec{S}_N \times \frac{\vec{q}}{m_N}\right) \\
 \mathcal{O}_{10} & i\frac{\vec{q}}{m_N} \cdot \vec{S}_N \\
 \mathcal{O}_{11} & i\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi \\
 \mathcal{O}_{12} & \vec{S}_\chi \cdot \left(\vec{S}_N \times \vec{v}^\perp\right) \\
 \mathcal{O}_{13} & i(\vec{S}_\chi \cdot \vec{v}^\perp) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_N\right) \\
 \mathcal{O}_{14} & i(\vec{S}_N \cdot \vec{v}^\perp) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi\right) \\
 \mathcal{O}_{15} & -\left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N}\right) \left(\left(\vec{S}_N \times \vec{v}^\perp\right) \cdot \frac{\vec{q}}{m_N}\right)
 \end{aligned}$$

Theories of particle interactions can give scattering cross sections that depend on the kinematical quantities.

In the non-relativistic limit

$v_{rel}$  Relative velocity

$q$  Exchanged momentum (scattering angle)

$S_\chi$  Dark matter spin

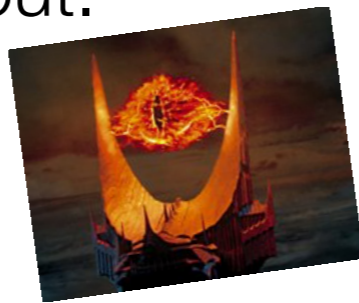
$S_N$  Nuclear spin

In the Sun: expect very different sensitivity vs direct detection experiments.



# What are we looking for?

Some models will **suppress neutrino** fluxes and/or mess up **helioseismology**: we can use this to constrain them rule them out.



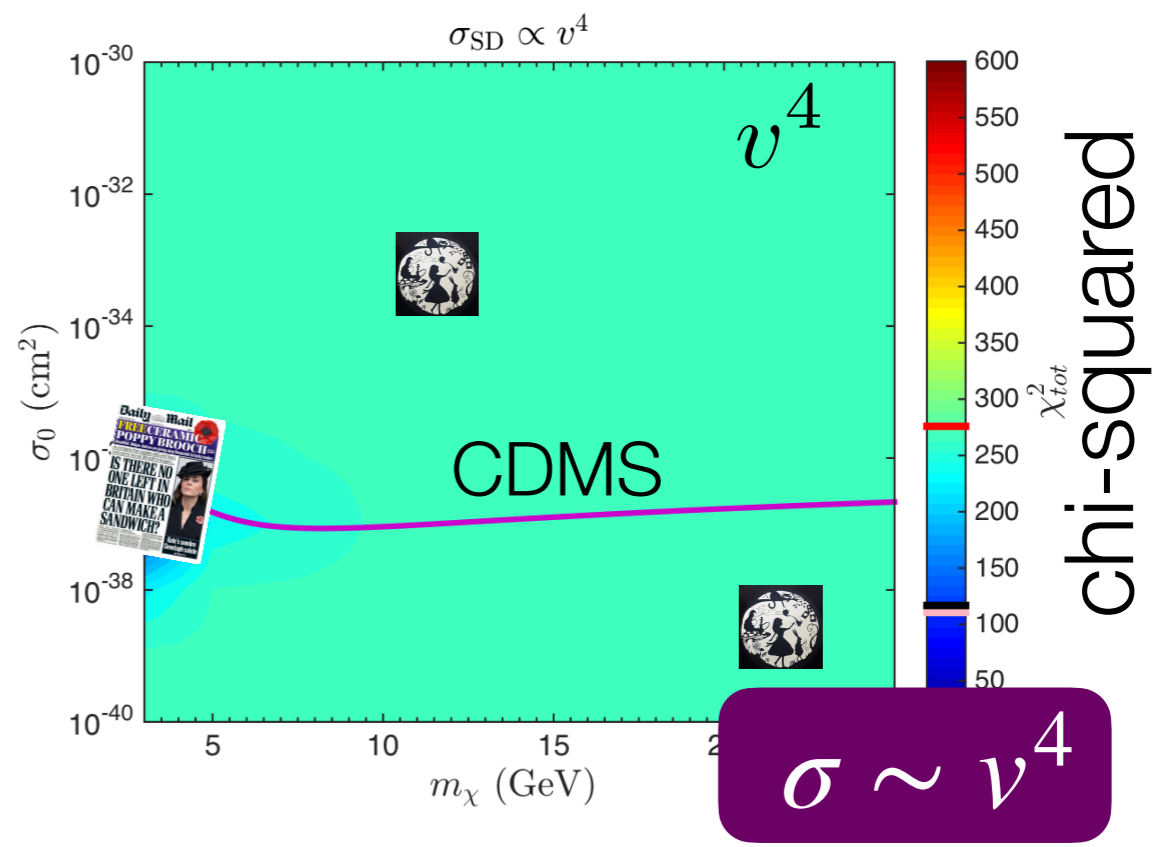
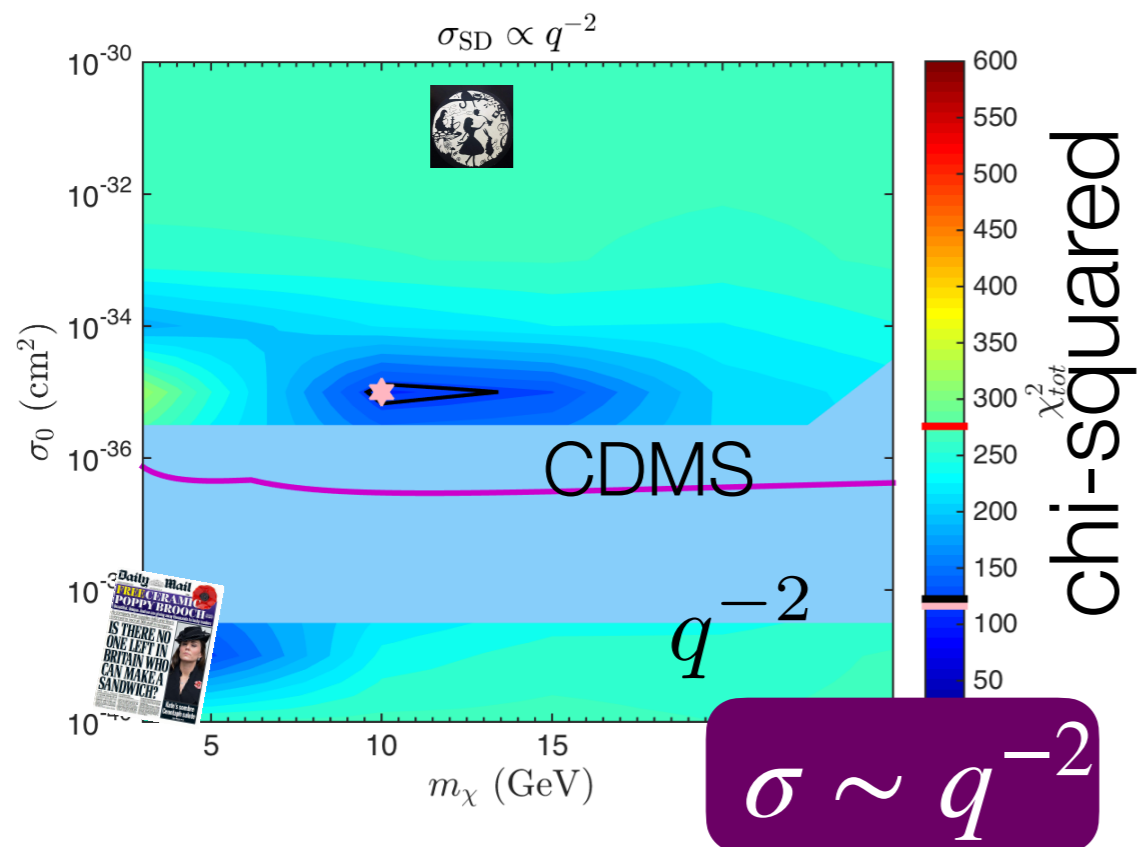
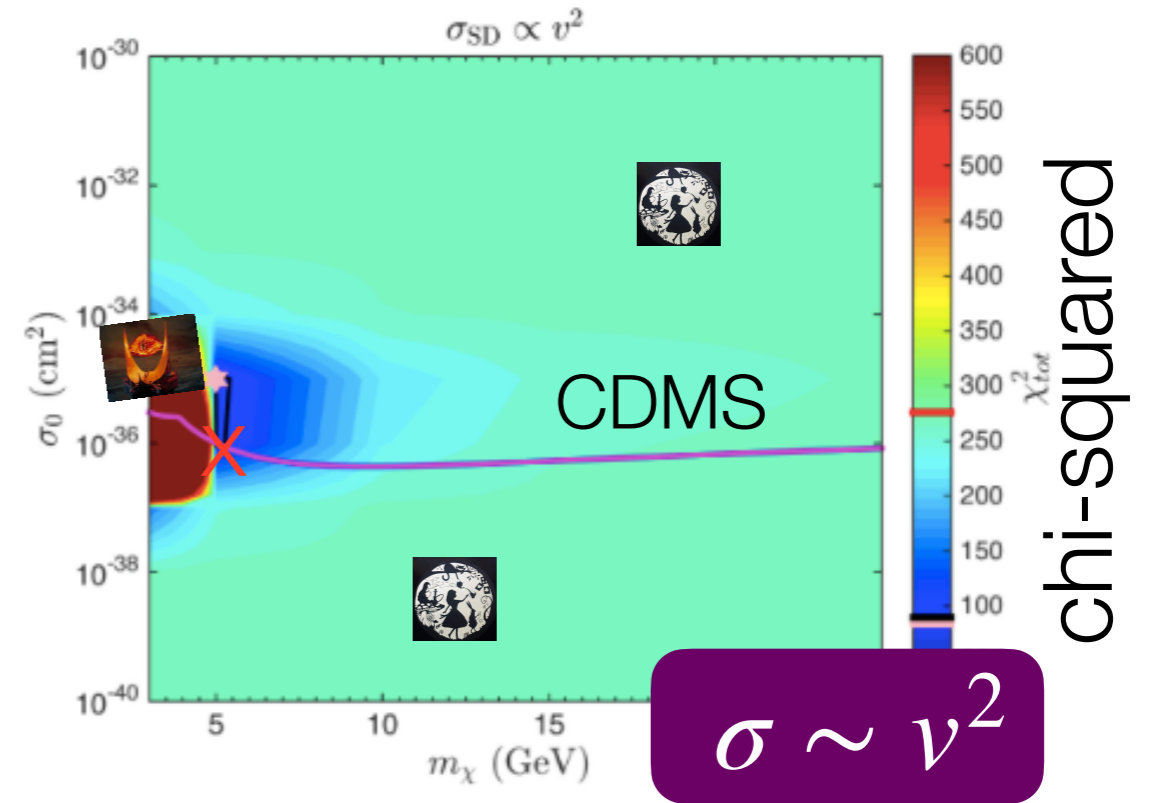
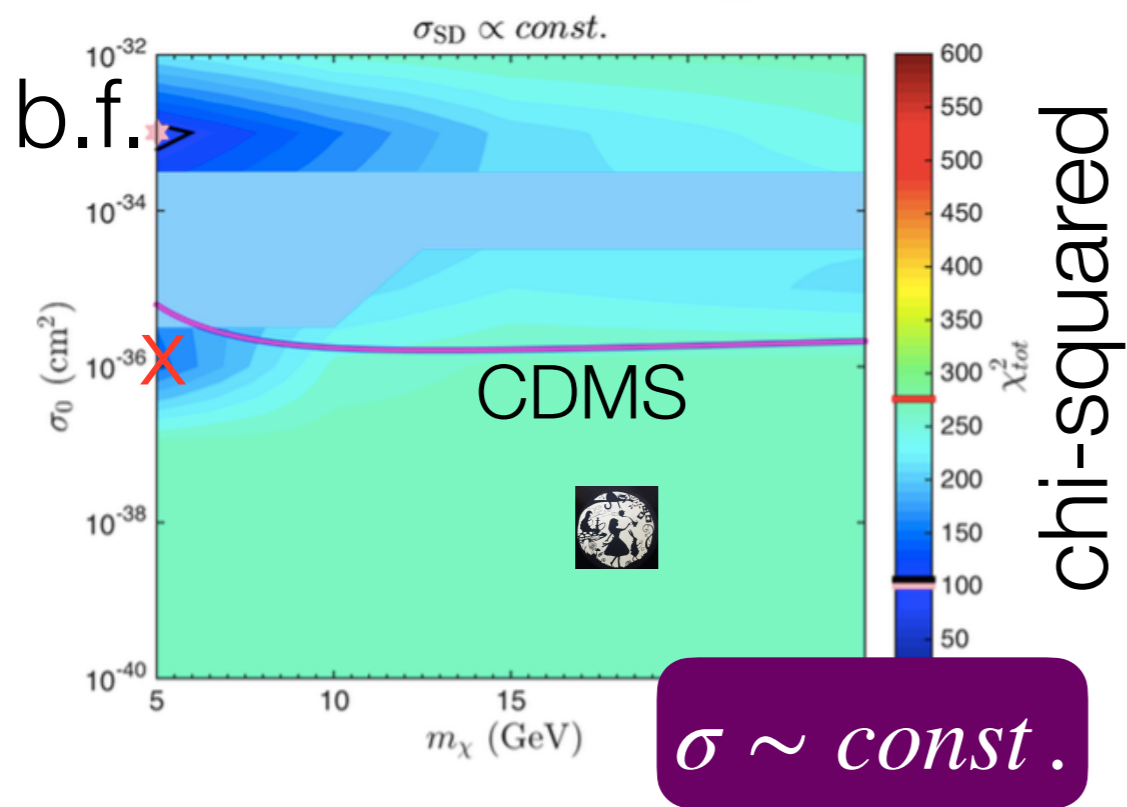
Some models will affect helioseismology enough to reconcile the SSM with observations. These will lead to happy editors and articles about us in the Daily Mail



Some models will do nothing at all



# Spin-dependent scenarios (ACV, Scott, Serenelli)



— SSM

— Within 3 sigma of BF

X Allowed



## Is dark matter lurking inside the SUN? Mysterious particles may be reducing the star's core temperature

- Durham University scientists have proposed a new model for the sun
- They say that dark matter may be transferring heat around its interior
- This would help explain how pressure waves move around the sun
- Current models are insufficient to account for how they move
- The dark matter could be originating in the galactic halo of the Milky Way

By JONATHAN O'CALLAGHAN FOR MAILONLINE

PUBLISHED: 13:57, 2 March 2015 | UPDATED: 07:28, 3 March 2015

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Scientists have discovered that there might be dark matter trapped inside the sun - and it could be the solar interior.

The bold new theory suggests that a form of the mysterious particle - which has yet to be directly observed - is absorbed by the sun from the centre of our galaxy.

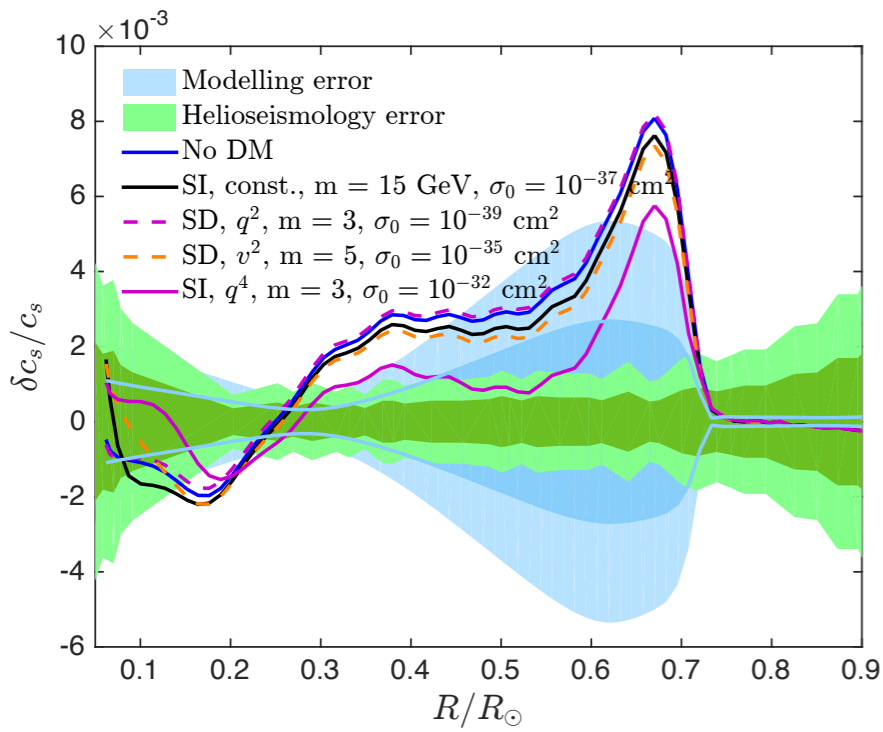
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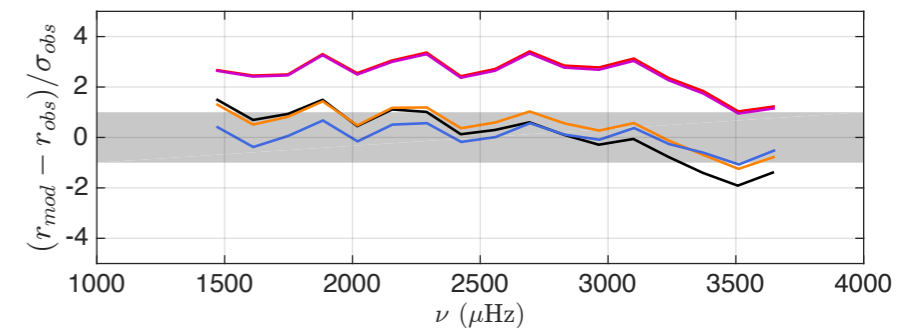
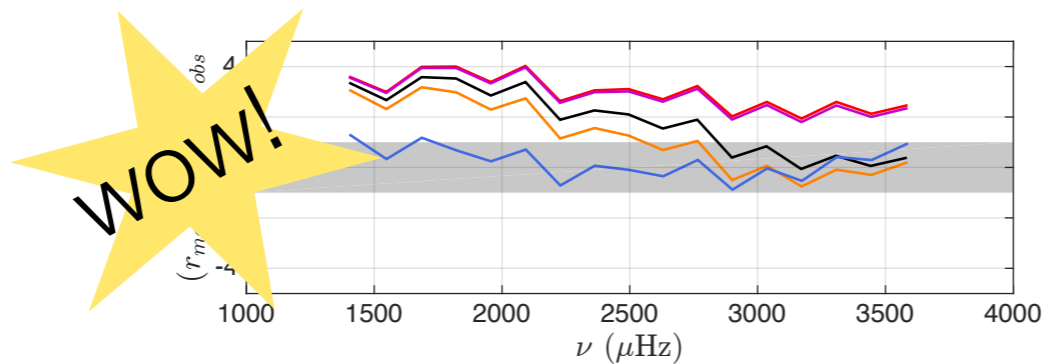
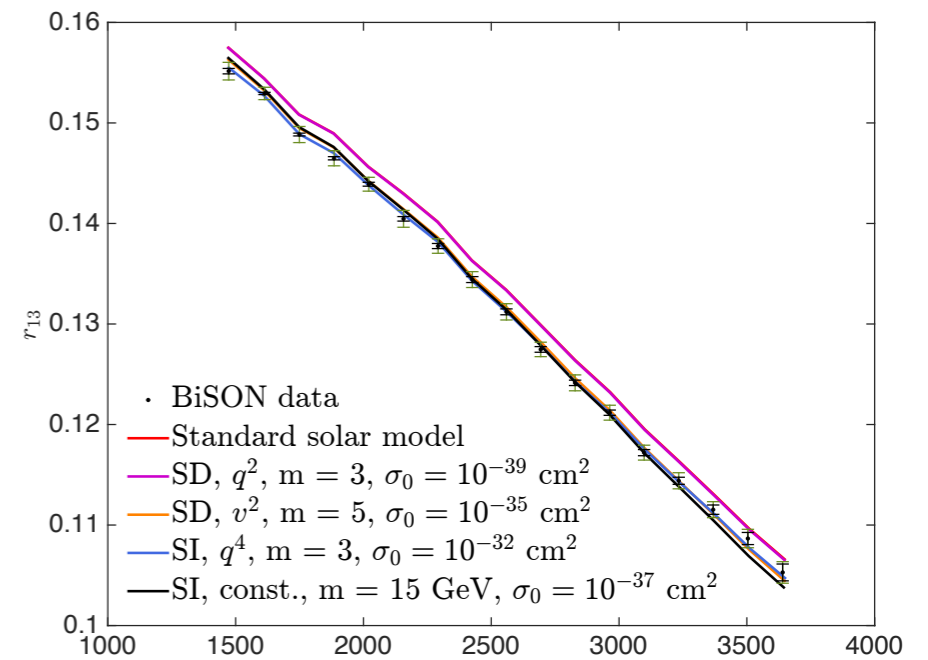
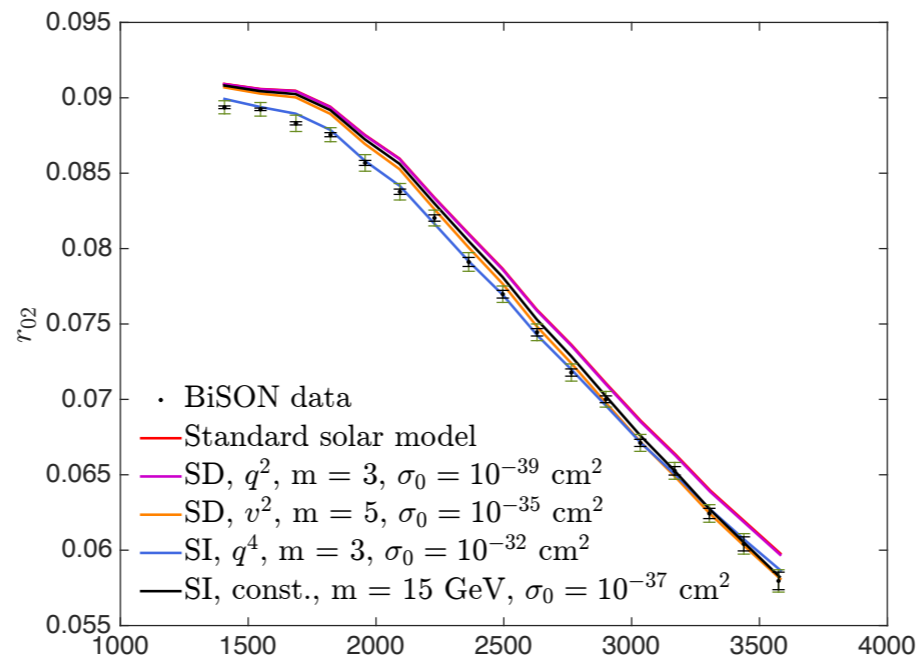
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# Sound speed

# Core

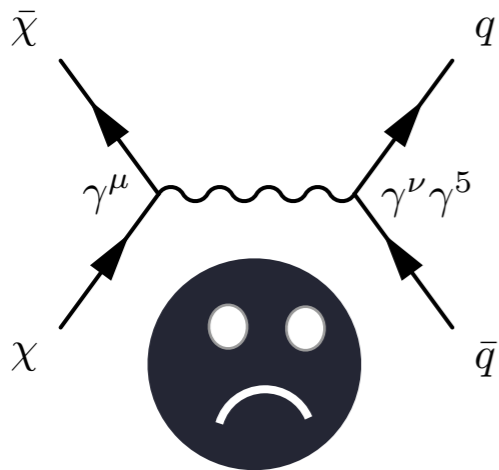




# What could these successful models be?

All spin-dependent (to evade DD constraints)

$$\sigma_{\chi-n} \propto v^2$$



...but also leads to a larger  $q^2$  coupling that is ruled out

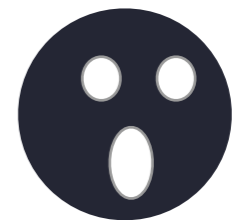
$$\sigma_{\chi-n} \propto q^{-2}$$

Simplified models don't produce this, but long-range forces? Light mediator?

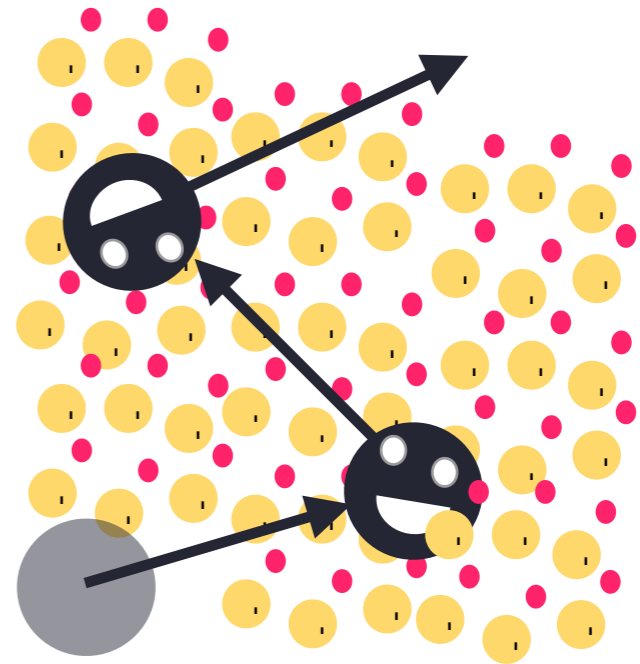
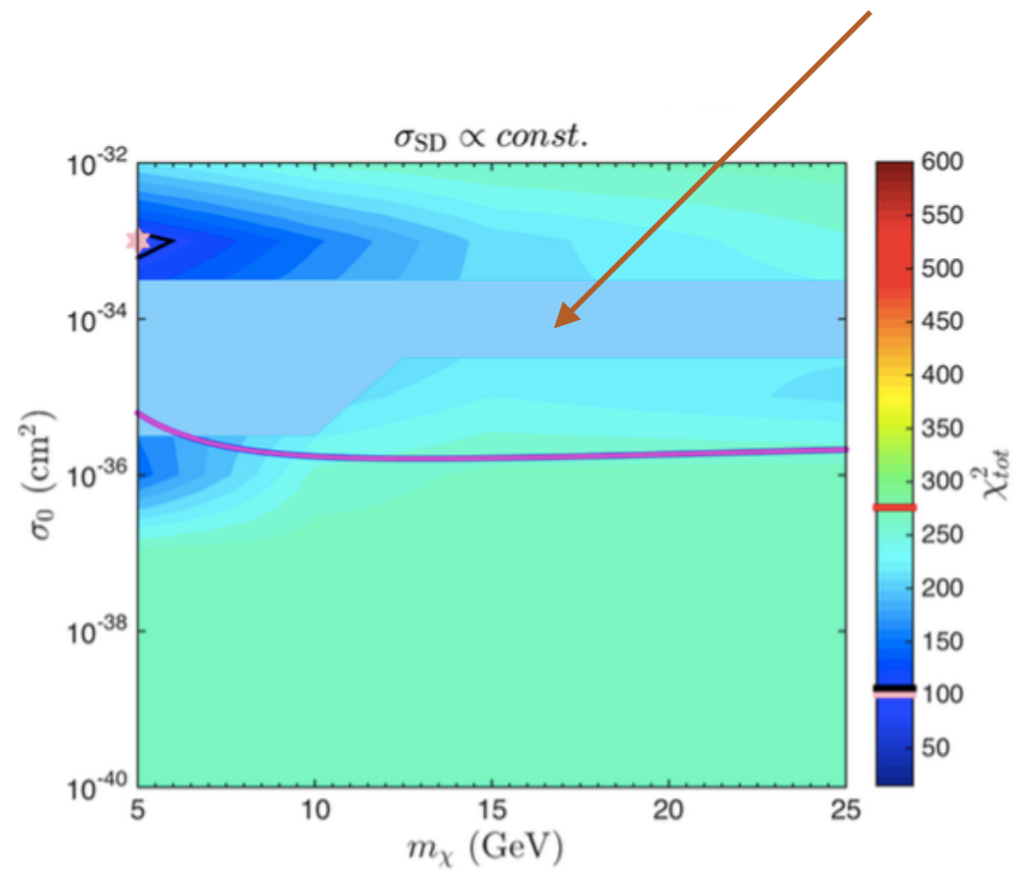


$$\sigma_{\chi-n} \propto v^4$$

???

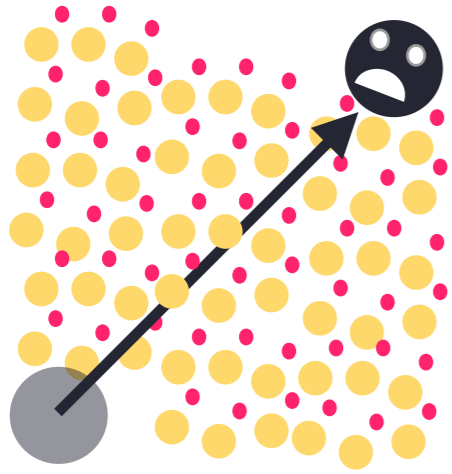


What's going on here?



1. Dark matter capture in the Sun
2. Asymmetric dark matter
- 3. Beyond the Sun — the Danger zone**





## Knudsen

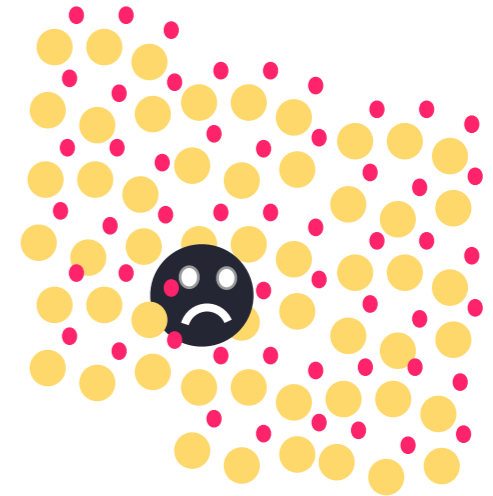
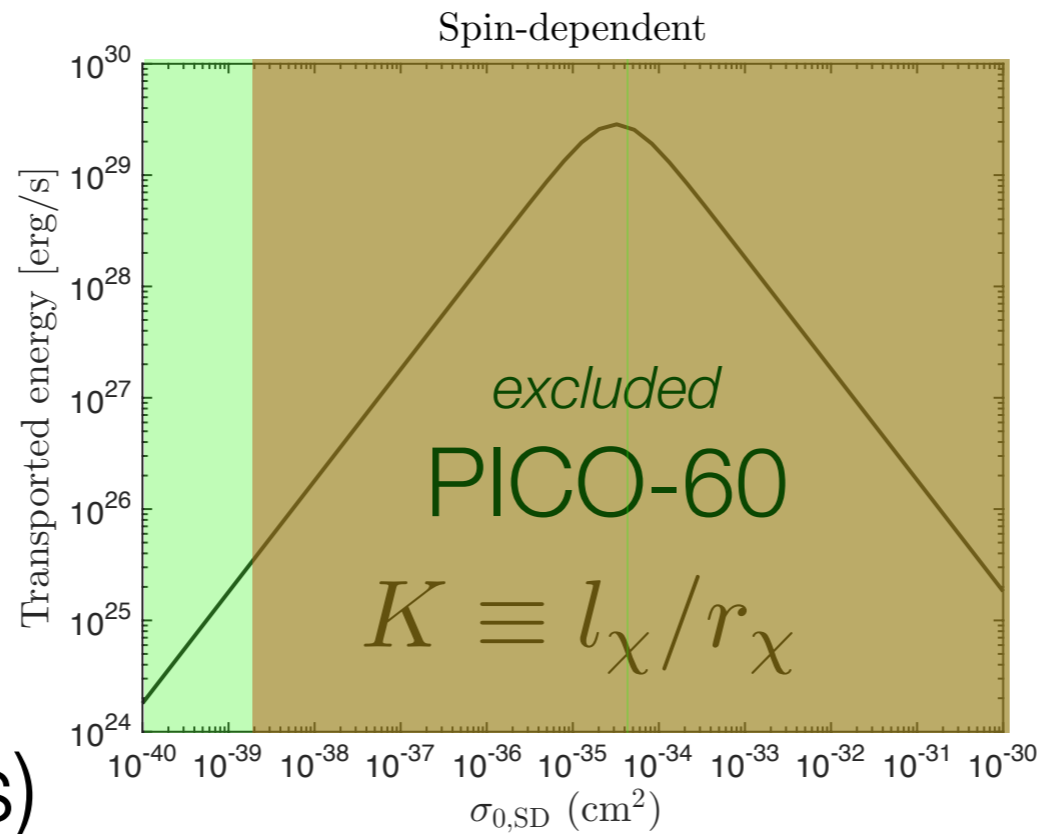
(non-local)

Small cross section

$$K \gtrsim 1$$

“easy” calculation  
(Spergel and Press)

**disagrees  
with Monte Carlo  
Simulation**



## LTE

large cross section

$$K < 1$$

Difficult calculation  
Gould and Raffelt

**“corrected”  
approach  
agrees with Monte  
Carlo everywhere**

## **For small couplings we have:**

- A corrected large-coupling solution
- or
- An incorrect small-coupling solution



# Why Spergel and Press is wrong

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Boltzmann:  $DF = l_{\chi}^{-1} CF$

Liouville operator:  $D(\vec{u}, \vec{r}, t) = \partial_t + \vec{u} \cdot \nabla_{\vec{r}} + \vec{g}(\vec{r}) \cdot \nabla_{\vec{u}}$

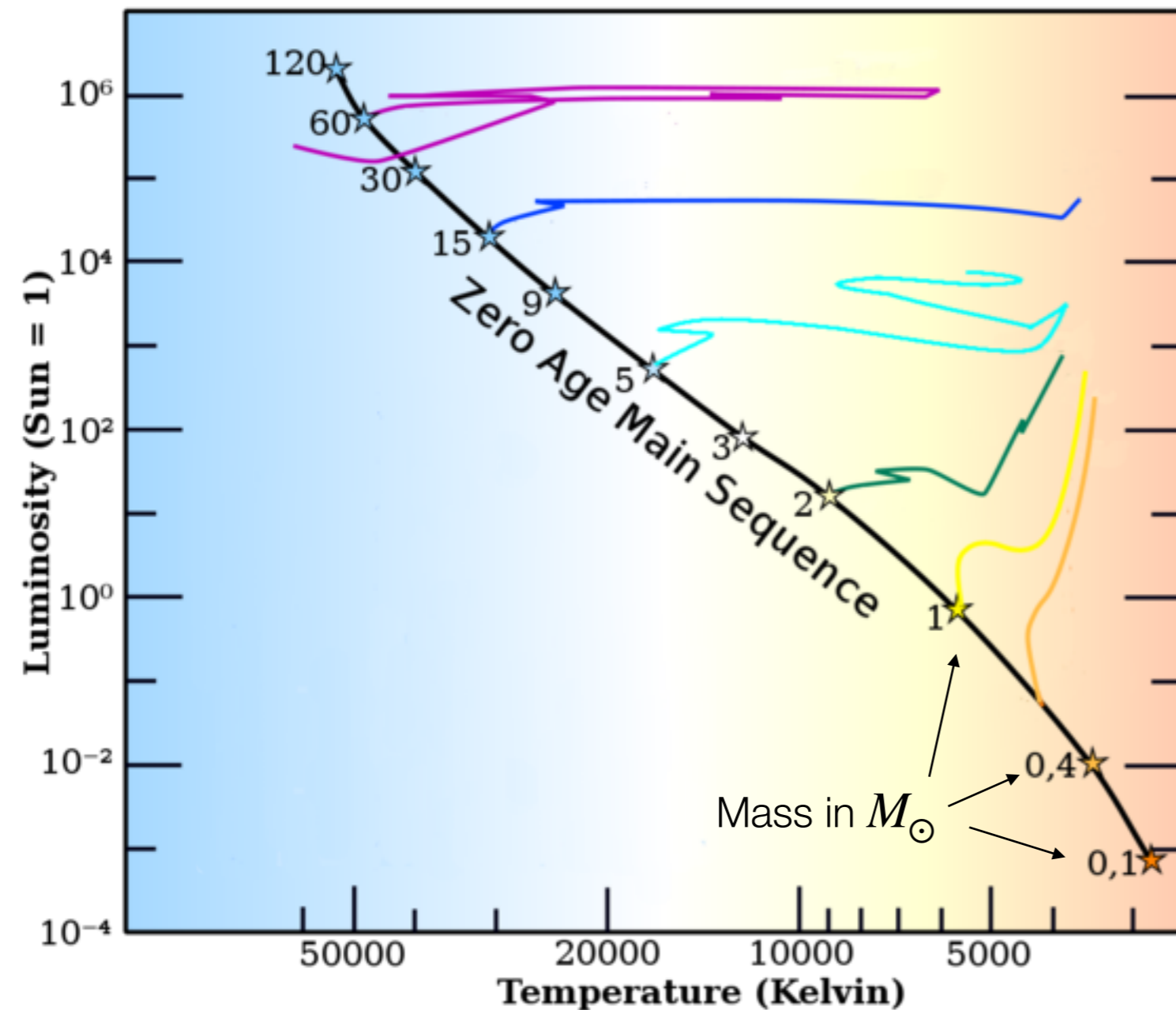
DM distribution:  $F(\vec{u}, \vec{r}, t)$

Collision rate  
with nuclei:  $l_{\chi}^{-1}(\vec{u}, \vec{r}, t) C(\vec{u}, \vec{r}, t)$

Assume  $DF = 0 \rightarrow$  Isothermal solution

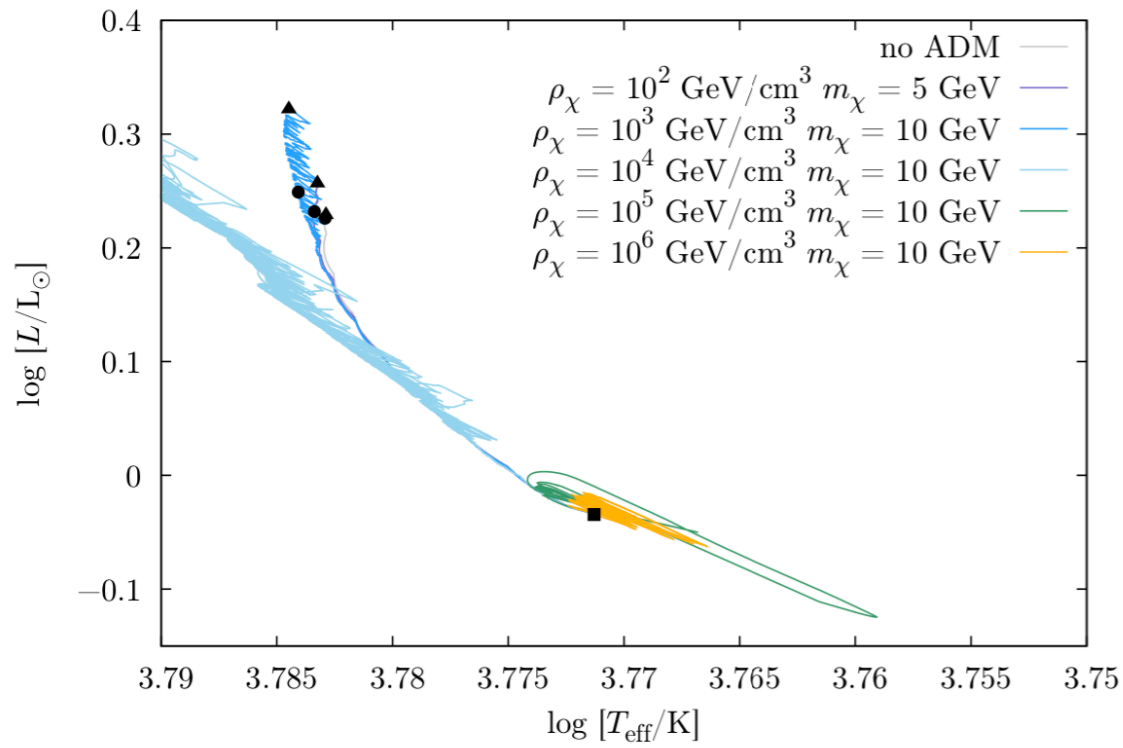
Then solve for heat exchanged with heat bath of the Sun:  
not self-consistent.

# Main sequence stars near the galactic centre

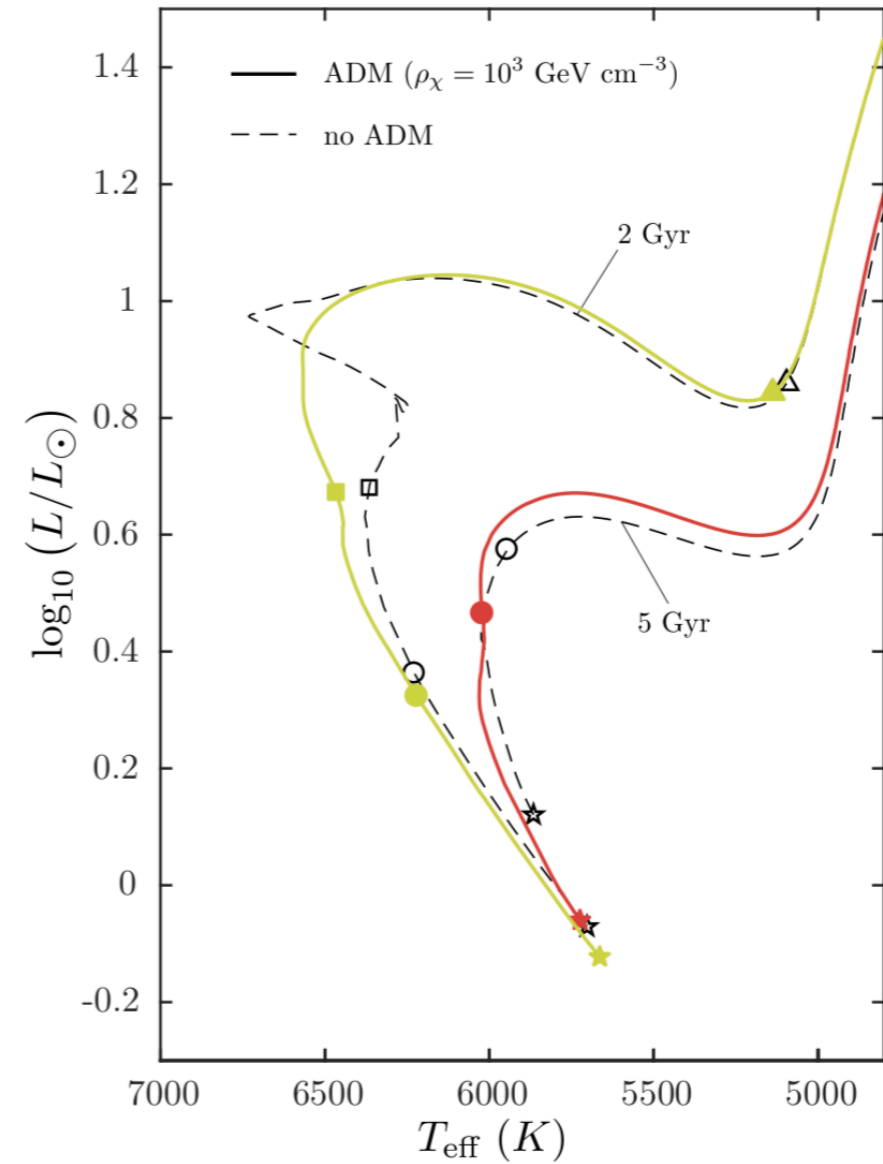


Time spent on the Main Sequence: how fast do you burn your nuclear fuel (hydrogen)?

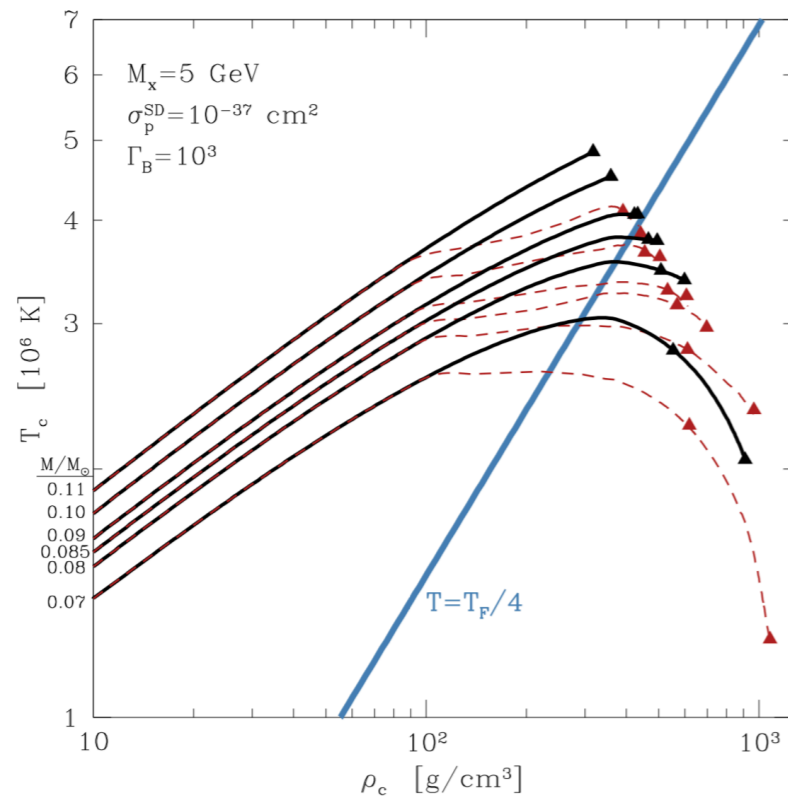
Heat transport by DM: Core temperature can go up or down, changing stellar luminosity and fuel consumption rate?



Lopés and Lopés (2019)  
use Spergel & Press transport



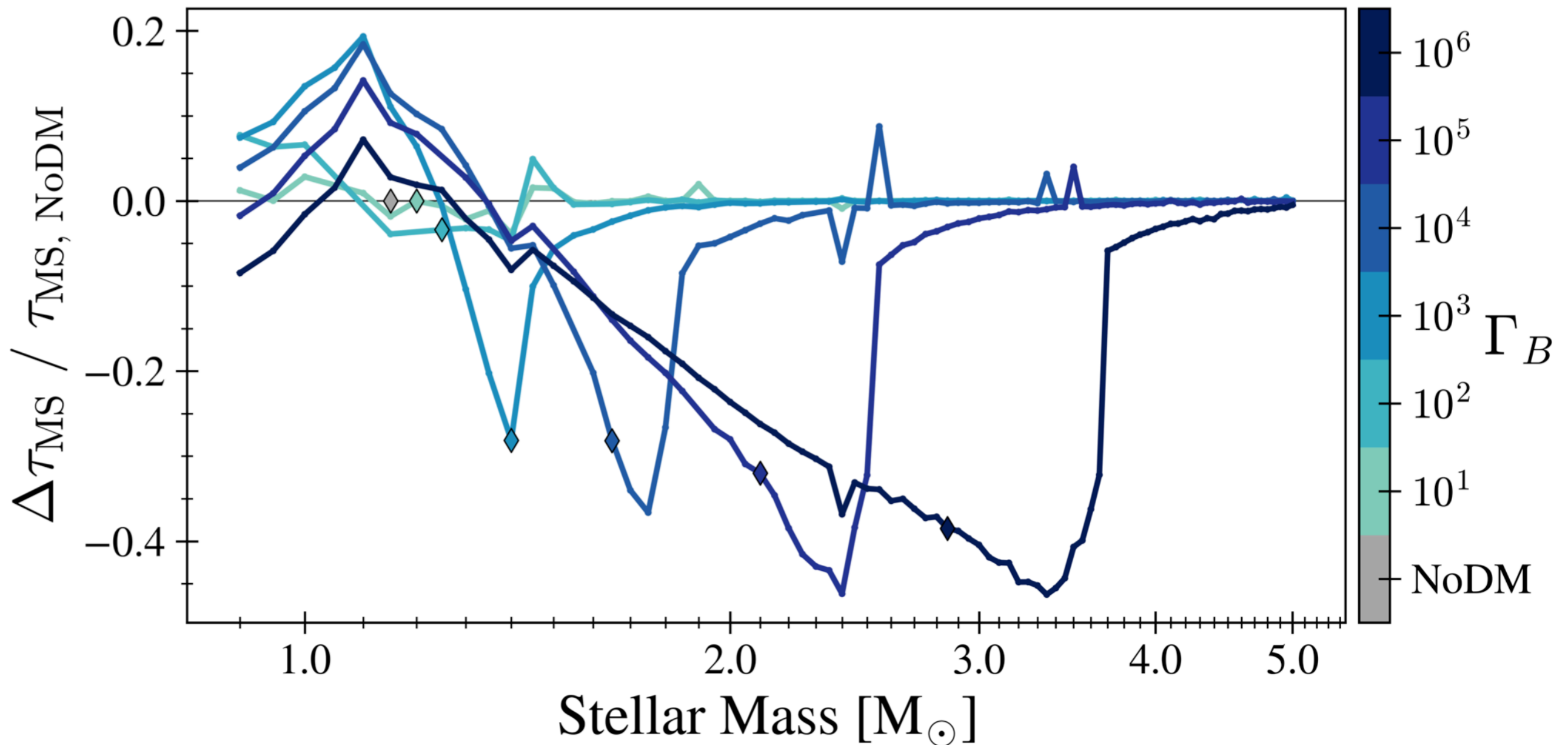
locco et al. 1201.5387  
Dangerous instabilities



Hurst & Zentner  
2011: Spergel &  
Press transport,  
some iffy  
approximations

# The Effects of Asymmetric Dark Matter on Stellar Evolution I: Spin-Dependent Scattering

Troy J. Raen,<sup>1\*</sup> Héctor Martínez-Rodríguez<sup>1</sup>, Travis J. Hurst<sup>2</sup>, Andrew R. Zentner<sup>1</sup>,  
and Carles Badenes<sup>1</sup>,



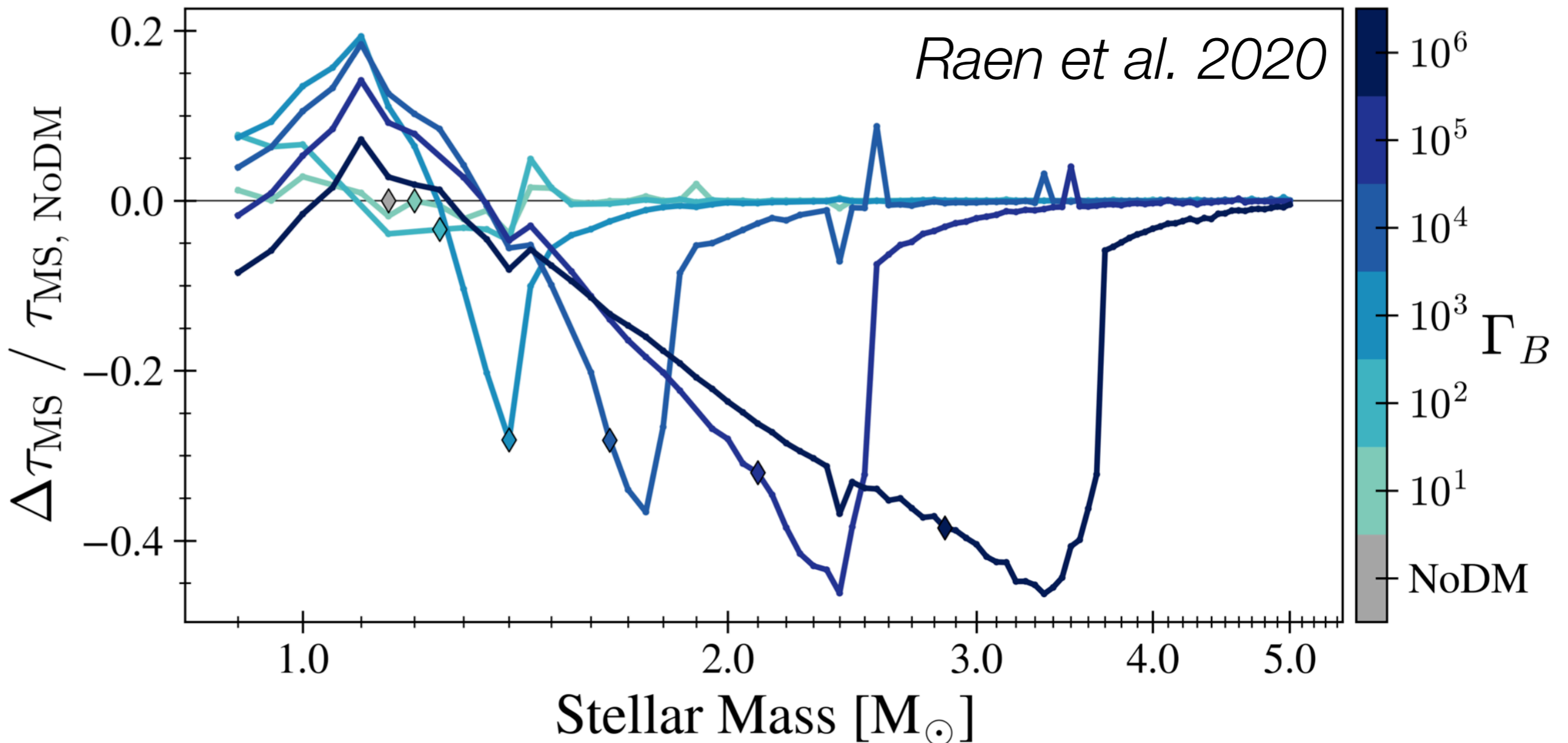


### Low mass stars:

ADM removes heat from center, leading to less fusion in the center, but heats up higher radii, allowing access to more fuel overall

### Higher mass stars:

ADM suppresses the formation of a convective core\*: H fuel is not replenished. Core is compressed, leading to higher burning rates and lower lifetime.



\*see also work by Casanellas, Lopes

All of these use Spergel and Press (isothermal)

How do we properly compute heat transport  
in the non-local regime?

Post Main-Sequence: even harder.

# Conclusions

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There may be a connection between the solar composition and asymmetric dark matter

Can we see DM in distant stars? What happens when they stop burning hydrogen? More work needed!

We still don't understand DM heat transport in the correct regime. Clever work required.

Public code: **Capt'n' General**. Computes capture rates for DM with general  $q^n$  and  $v^n$  cross sections. NREFT operators available soon.

<https://github.com/aaronvincent/captngen>



