



# Cosmological Neutrinos

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## **FRAMEWORK**

What can the Universe Large Scale Structure (LSS)  
tell us about cosmological neutrinos?

## QUESTIONS TO BE ADDRESSED

- 1) Can they be probed by looking at their energy density contribution?
- 2) Can they be probed by looking at their perturbations?
- 3) Have we detected departures from the standard/expected Cosmic Neutrino Background (CNB)?
- 4) Are these findings robust?
- 5) Are there perspectives of discoveries in the next few years?

# CNB in the relativistic regime

CNB predicted in 1953 by Alpher et al.

PHYSICAL REVIEW

VOLUME 92, NUMBER 6

DECEMBER 15, 1953

## Physical Conditions in the Initial Stages of the Expanding Universe\*†

RALPH A. ALPHER, JAMES W. FOLLIN, JR., AND ROBERT C. HERMAN  
*Applied Physics Laboratory, The Johns Hopkins University, Silver Spring, Maryland*

(Received September 10, 1953)

$$\omega_R = \omega_\gamma \left( 1 + N_{\text{eff}} \times \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} \right) \quad \text{with } N_{\text{eff}} = 3.046$$

in the relativistic regime

Planck (CMB) + several other combinations yield evidence of  $N_{\text{eff}} > 0$   
at a level between  $10\text{-}17\sigma$



## CNB in the non relativistic regime

$$\rightarrow \quad \omega_M = \omega_b + \omega_{\text{CDM}} + (\Sigma m_\nu) / 93.14 \text{ eV}$$

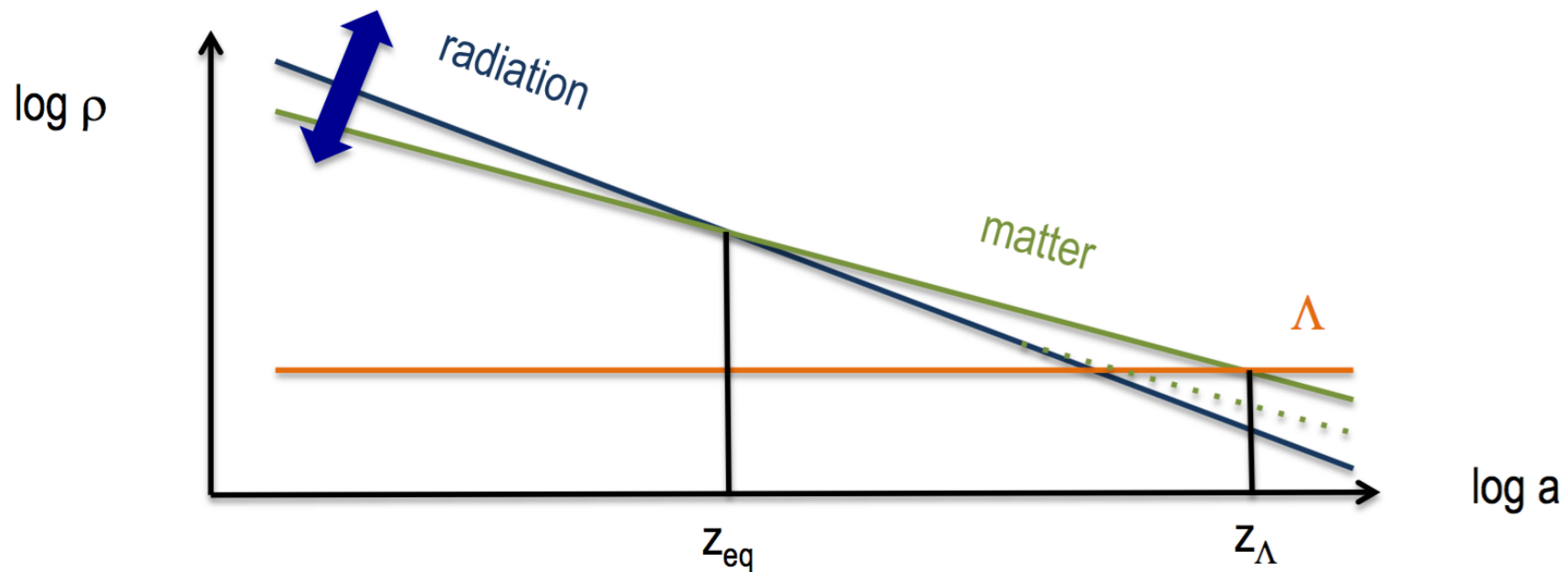
$\rightarrow$  Impact on the matter clustering through neutrino free streaming, impact on CMB statistics (angular diameter distance, Late ISW effect)

No convincing evidence for this effect, i.e. a non zero total mass

(although be aware that claims have been made)

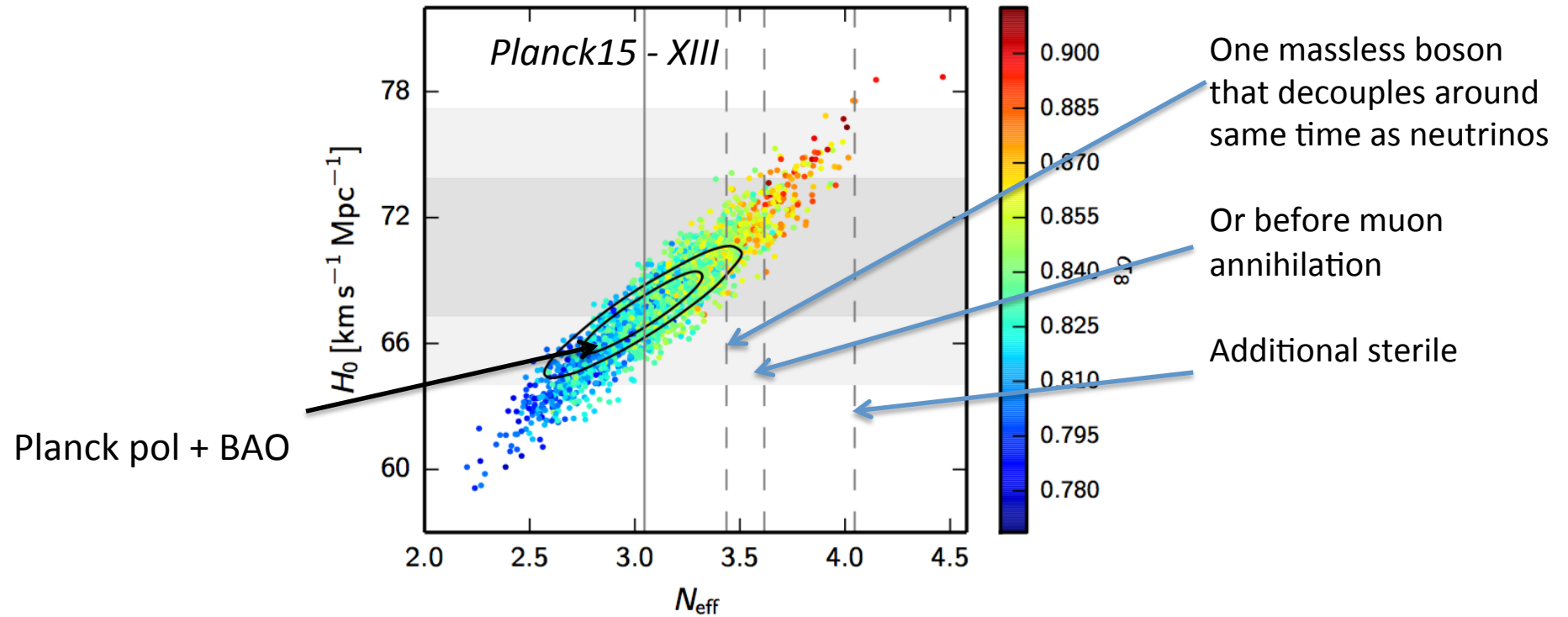
## Measuring $N_{\text{eff}}$ – CNB average density

*Key issue:* exploiting different evolution of the matter and radiation energy densities



There is an obvious degeneracy: can preserve all redshifts by increasing  $N_{\text{eff}}$ ,  $H_0$  and keeping energy densities fixed – However this will cause more damping in the CMB power spectrum.

# Measuring $N_{\text{eff}}$ - CNB average density - II



$$N_{\text{eff}} = 3.13 \pm 0.32 \quad \text{Planck TT+lowP};$$

$$N_{\text{eff}} = 3.15 \pm 0.23 \quad \text{Planck TT+lowP+BAO};$$

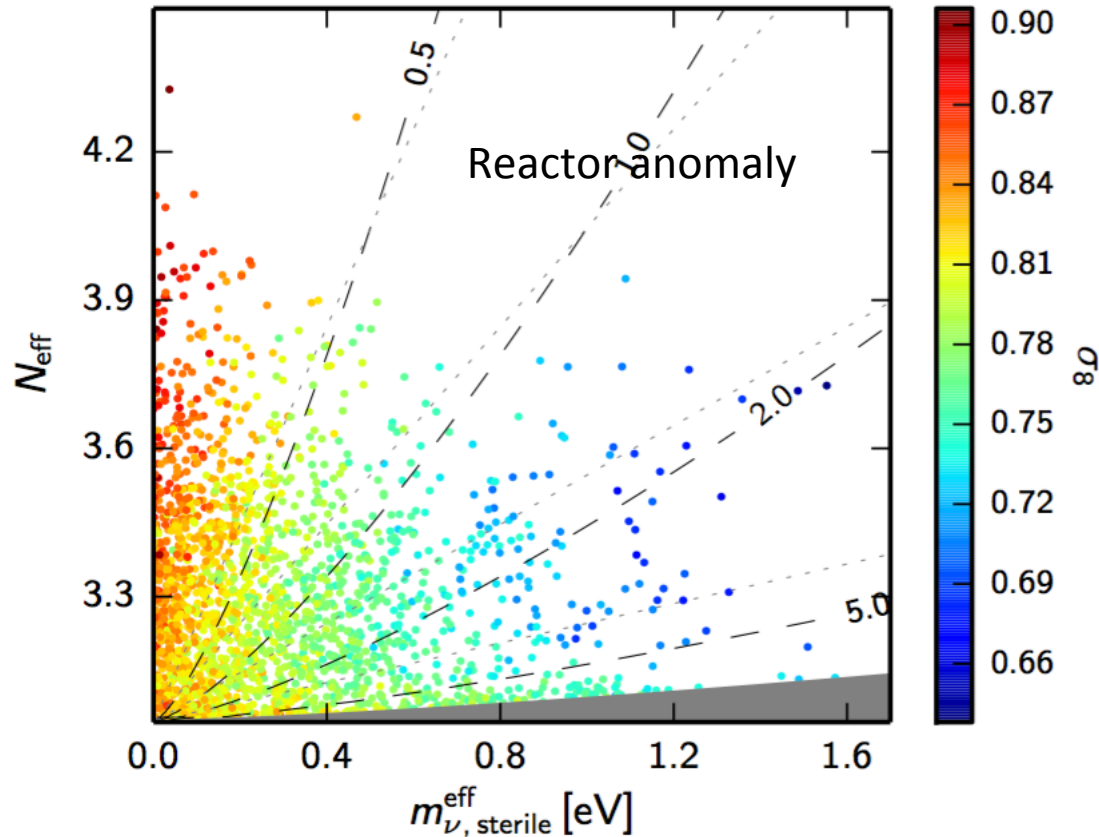
$$N_{\text{eff}} = 2.99 \pm 0.20 \quad \text{Planck TT, TE, EE+lowP};$$

$$N_{\text{eff}} = 3.04 \pm 0.18 \quad \text{Planck TT, TE, EE+lowP+BAO}.$$

In this relativistic regime, perturbations have been tested and support the view that this contribution to  $N_{\text{eff}}$  is really made by neutrinos (and not by other particles).

# Measuring $N_{\text{eff}}$ - Extra relics? Most likely not

Planck15 - XIII



Search motivated by short baseline oscillation anomaly (LSND, MiniBoone, reactor data...)

General parameterization: (one massive sterile neutrino)

$N_{\text{eff}}$ : parameter for relativistic density at early times

$m_{\text{eff}}$ : parameter for non-relativistic mass of HDM today ( $\omega_{\text{HDM}} = m_{\text{eff}} / 93.14 \text{eV}$ )

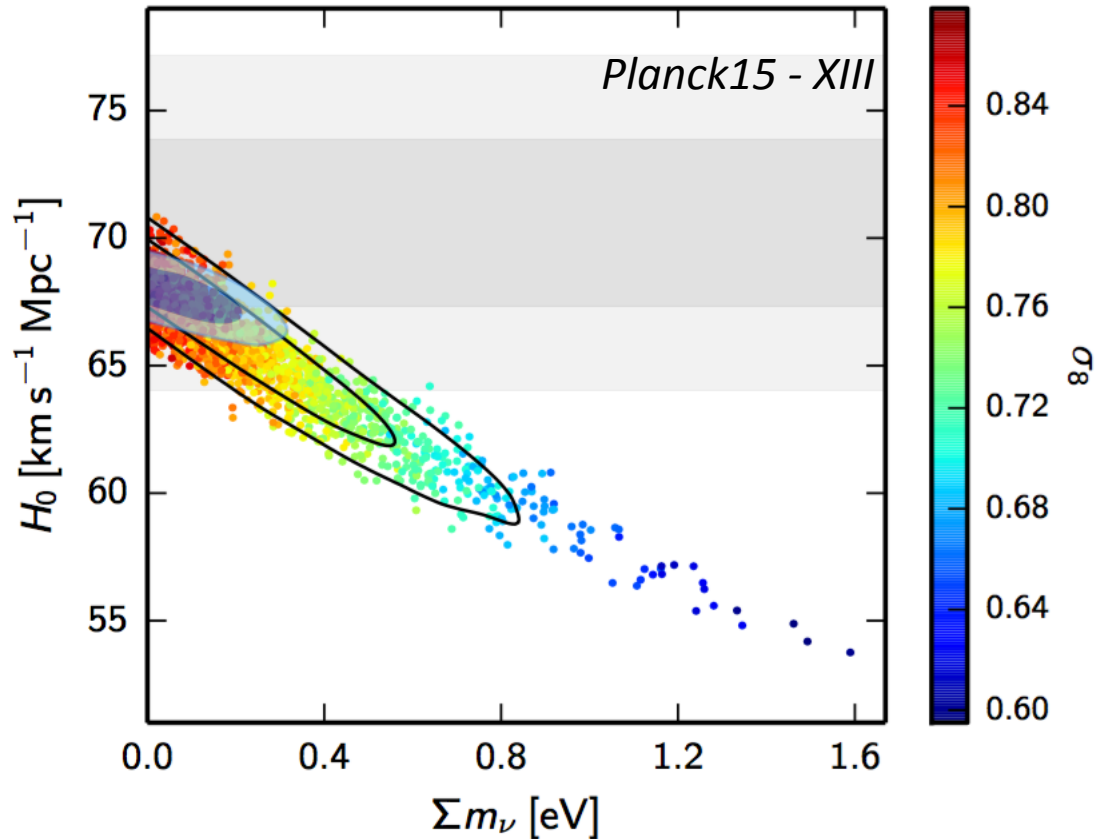
Models with  $\Delta N_{\text{eff}}=1$  highly Disfavoured by Planck

Models with  $\Delta N_{\text{eff}}=0.4$  mildly Disfavoured but require higher  $\sigma_8$  and  $H_0$

$$\left. \begin{array}{l} N_{\text{eff}} < 3.7 \\ m_{\nu, \text{sterile}}^{\text{eff}} < 0.38 \text{ eV} \end{array} \right\} 95\%, \text{ Planck TT+lowP+lensing+BAO.}$$



# Total neutrino mass from the CMB



3 key parameters: power spectrum amplitude, neutrino masses and H0

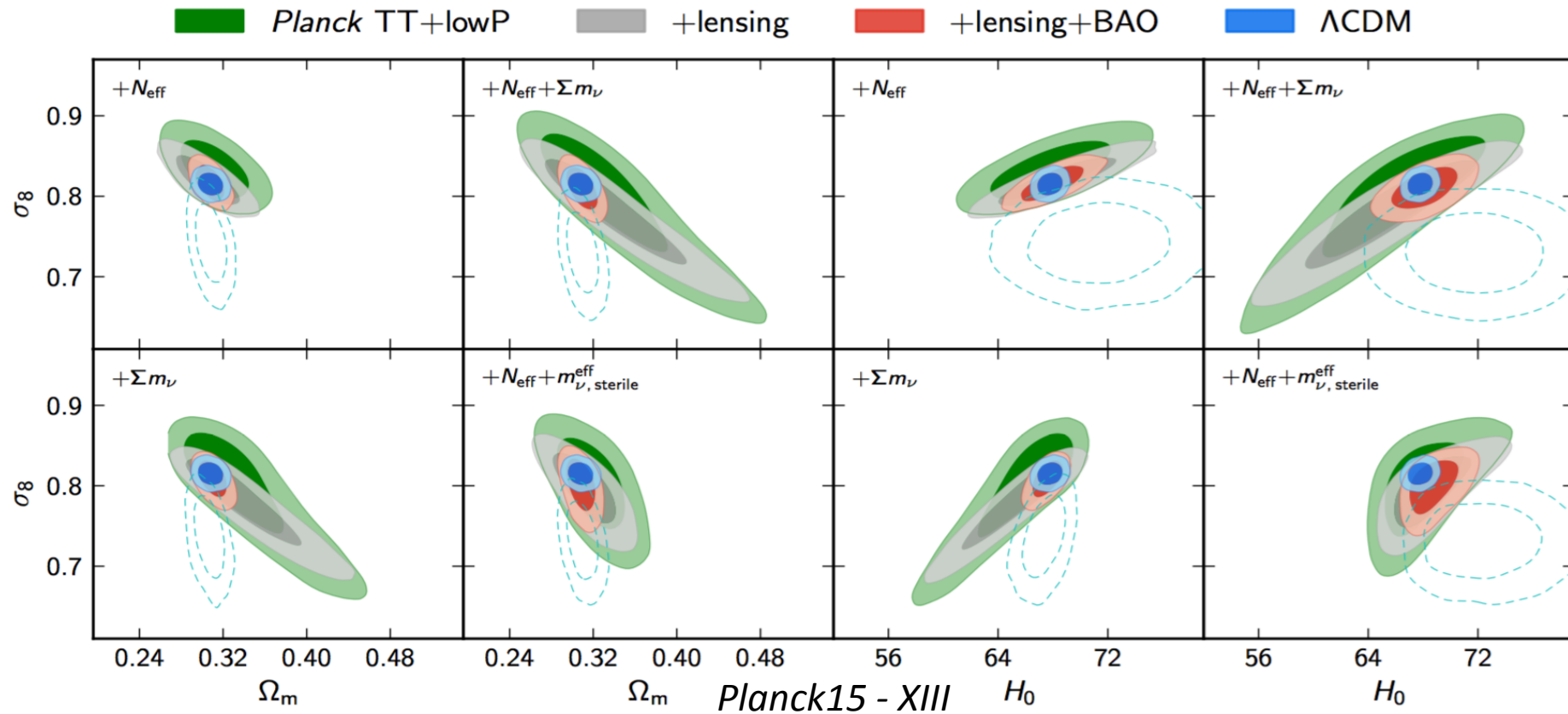
$$\sum m_\nu < 0.72 \text{ eV} \quad \text{Planck TT+lowP};$$

$$\sum m_\nu < 0.21 \text{ eV} \quad \text{Planck TT+lowP+BAO};$$

$$\sum m_\nu < 0.49 \text{ eV} \quad \text{Planck TT, TE, EE+lowP};$$

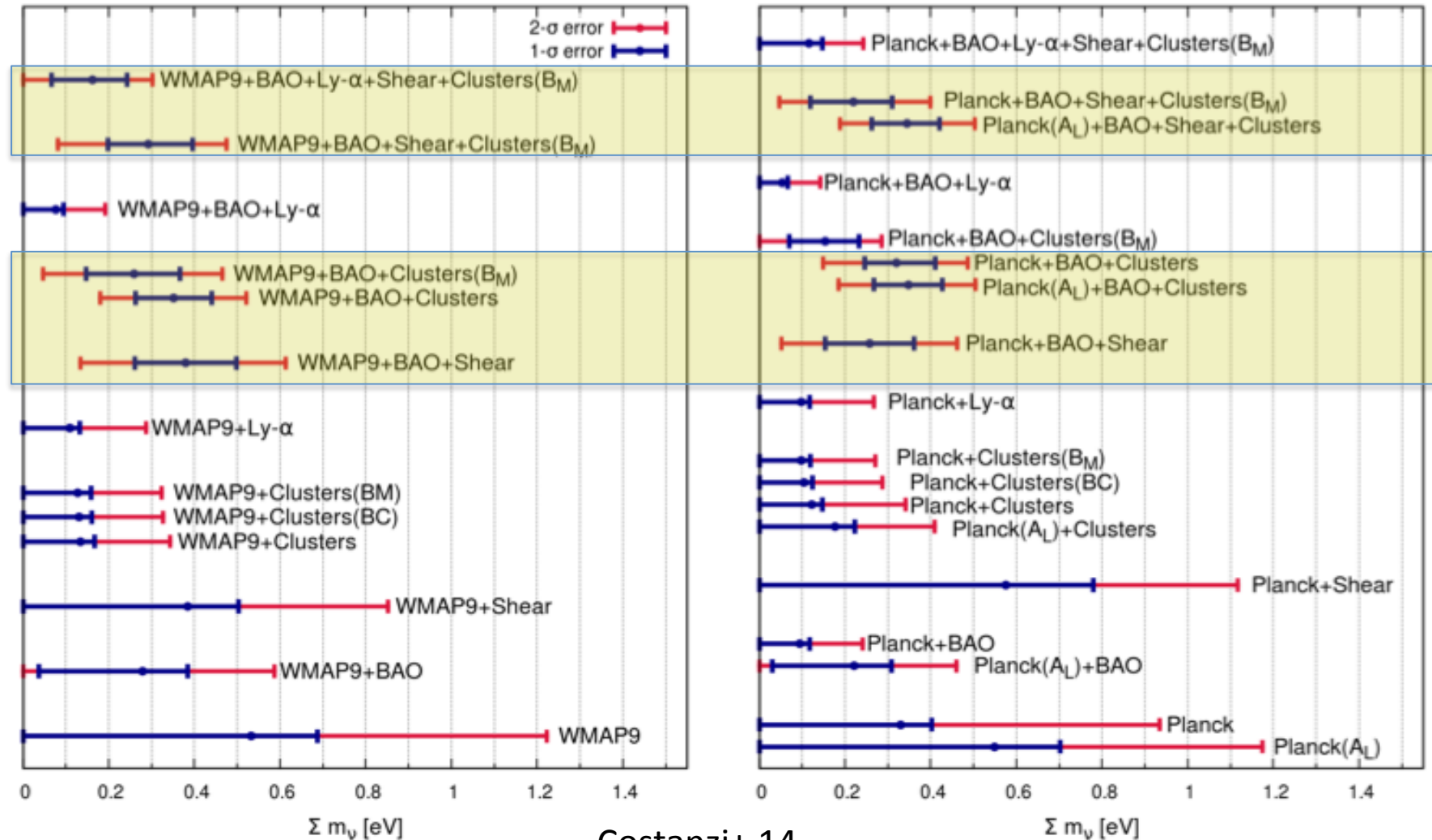
$$\sum m_\nu < 0.17 \text{ eV} \quad \text{Planck TT, TE, EE+lowP+BAO}.$$

# Departing from LCDM using neutrinos is difficult



Claims of non zero neutrino mass  $0.3 \pm 0.1$  eV appear to be a compromise to reconcile low  $\sigma_8$  values suggested by weak lensing and/or cluster number counts – some is true for the sterile sector.

# Data combination after Planck 13...



# Possible surprises/systematic effects?

*Tension with CMB data  $H_0$  value between 2 and  $3\sigma$*

## **A 2.4% Determination of the Local Value of the Hubble Constant<sup>1</sup>**

Adam G. Riess<sup>2,3</sup>, Lucas M. Macri<sup>4</sup>, Samantha L. Hoffmann<sup>4</sup>, Dan Scolnic<sup>2,5</sup>, Stefano Casertano<sup>3</sup>, Alexei V. Filippenko<sup>6</sup>, Brad E. Tucker<sup>6,7</sup>, Mark J. Reid<sup>8</sup>, David O. Jones<sup>2</sup>, Jeffrey M. Silverman<sup>9</sup>, Ryan Chornock<sup>10</sup>, Peter Challis<sup>8</sup>, Wenlong Yuan<sup>4</sup>, and Ryan J. Foley<sup>11,12</sup>

km s<sup>-1</sup> Mpc<sup>-1</sup>, respectively. Our best estimate of  $H_0 = 73.02 \pm 1.79$  km s<sup>-1</sup> Mpc<sup>-1</sup> combines the anchors NGC 4258, MW, and LMC, and includes systematic errors for a final uncertainty of 2.4%. This value is  $3.0\sigma$  higher than  $67.3 \pm 0.7$  km s<sup>-1</sup> Mpc<sup>-1</sup> predicted by  $\Lambda$ CDM with 3 neutrino flavors having a mass of 0.06 eV and the *Planck* data, but the discrepancy reduces to  $2.0\sigma$  relative to the prediction of  $69.3 \pm 0.7$  km s<sup>-1</sup> Mpc<sup>-1</sup> based on the comparably precise combination of *WMAP*+ACT+SPT+BAO observations, suggesting that systematic uncertainties in cosmic microwave background radiation measurements may play a role in the tension.

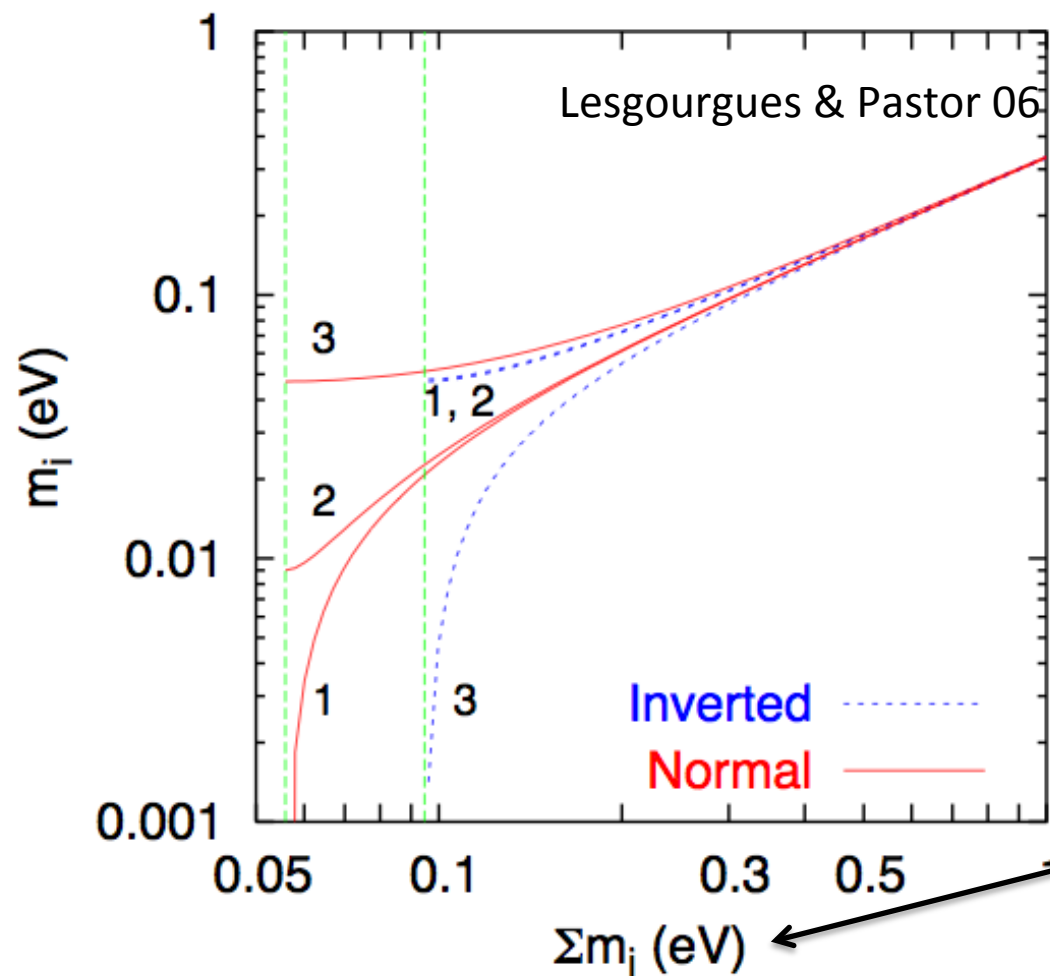
If we take the conflict between *Planck* high-redshift measurements and our local determination of  $H_0$  at face value, one plausible explanation could involve an additional source of dark radiation in the early Universe in the range of  $\Delta N_{\text{eff}} \approx 0.4 - 1$ . We

**Impact on structure formation**

**i.e. neutrino perturbations**



# COSMOLOGICAL NEUTRINOS - I: STARTING POINT



COSMOLOGY

constraints on the sum of the neutrino masses

$$0.056 \text{ (0.095) eV} \lesssim \sum_i m_i \lesssim 6 \text{ eV}$$

## COSMOLOGICAL NEUTRINOS - II: FREE-STREAMING SCALE

Neutrino thermal velocity  $v_{\text{th}} \equiv \frac{\langle p \rangle}{m} \simeq \frac{3T_\nu}{m} = \frac{3T_\nu^0}{m} \left( \frac{a_0}{a} \right) \simeq 150(1+z) \left( \frac{1 \text{ eV}}{m} \right) \text{ km s}^{-1}$

*Neutrino free-streaming scale*

*Scale of non-relativistic transition*

$$k_{FS}(t) = \left( \frac{4\pi G \bar{\rho}(t) a^2(t)}{v_{\text{th}}^2(t)} \right)^{1/2} \quad k_{\text{nr}} \simeq 0.018 \Omega_m^{1/2} \left( \frac{m}{1 \text{ eV}} \right)^{1/2} h \text{ Mpc}^{-1}$$

THREE  
COSMIC  
EPOCHS

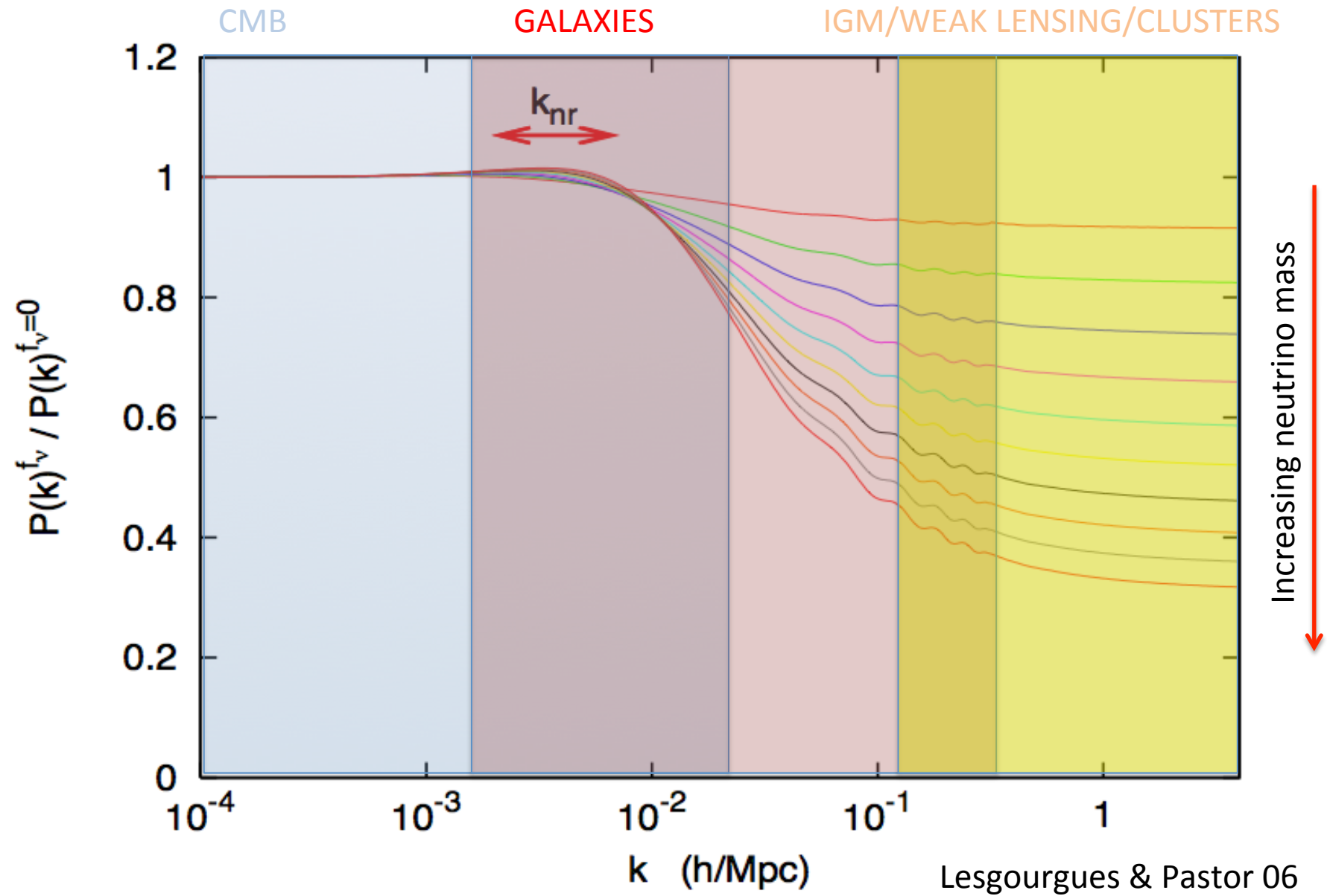
RADIATION ERA  $z > 3400$

MATTER RADIATION  $z < 3400$

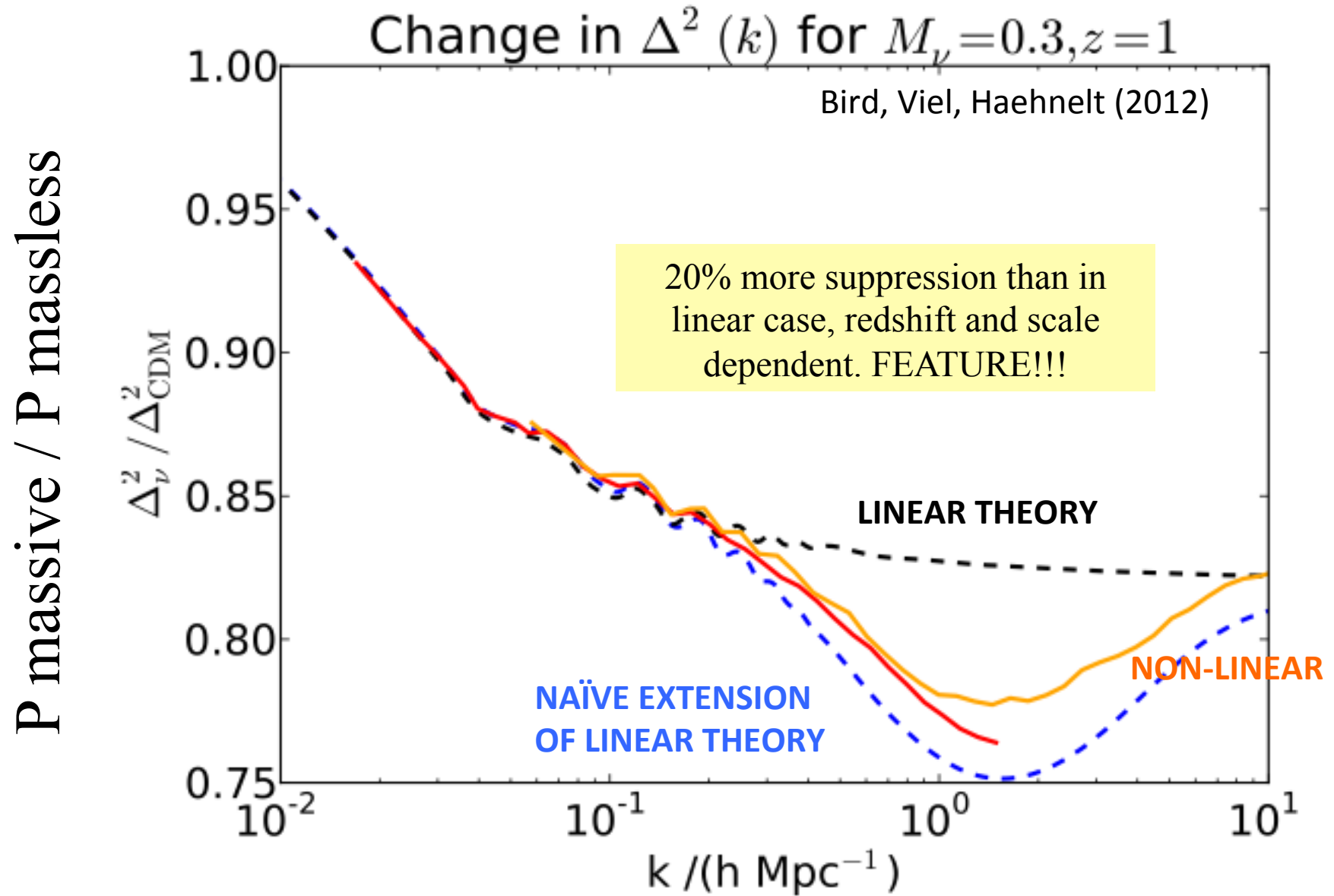
NON-RELATIVISTIC TRANSITION  $z \sim 500$

Below  $k_{\text{nr}}$  there is suppression in power at scales that are cosmologically important

# COSMOLOGICAL NEUTRINOS - III: LINEAR MATTER POWER

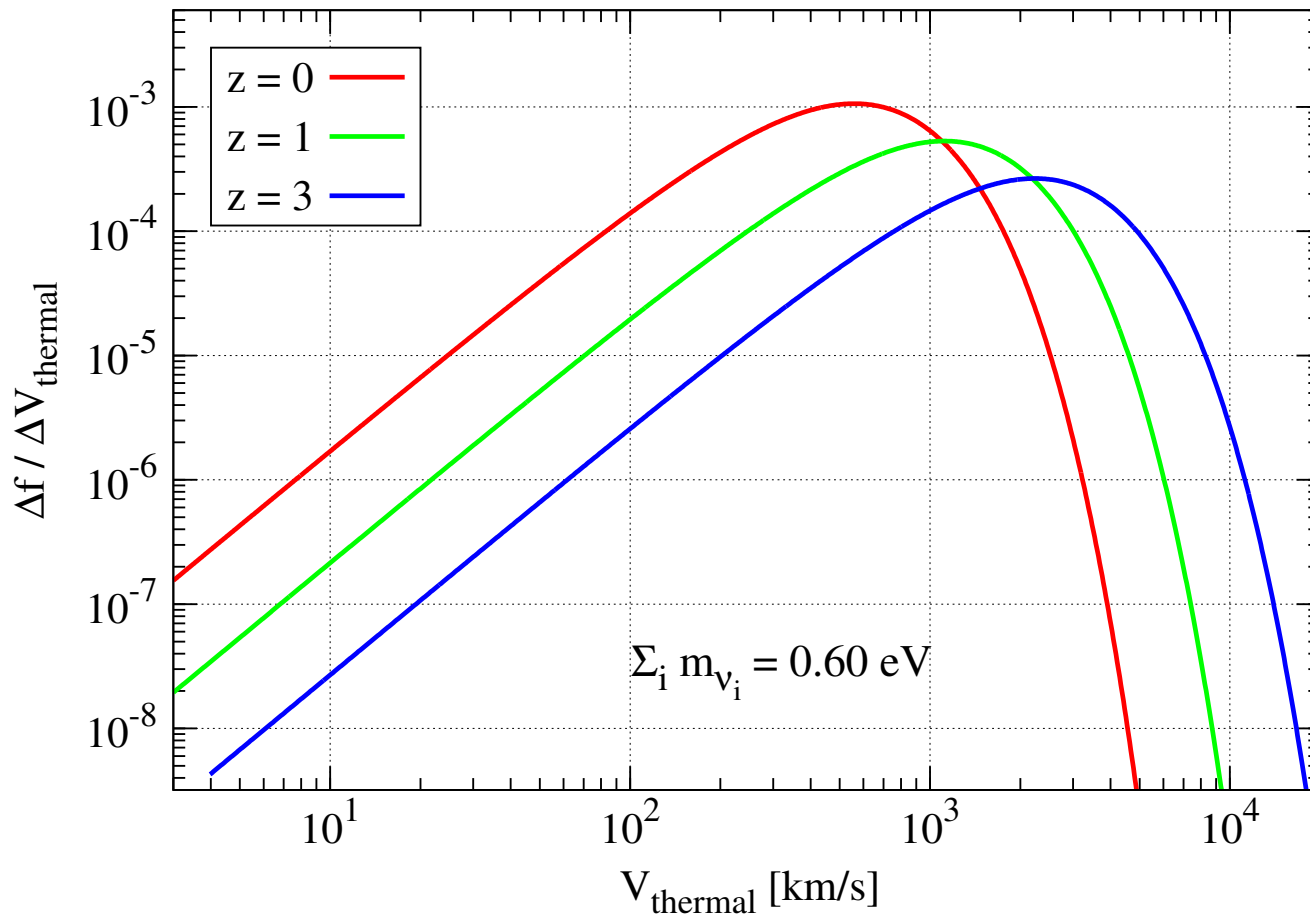


COSMOLOGICAL NEUTRINOS : NON-LINEAR MATTER POWER



# Neutrino clustering

$$n_\nu(p, z) dp \cong \frac{4\pi g_\nu}{(2\pi\hbar c)^3} \left( \frac{p^2 dp}{e^{(p/k_B T_\nu(z))} + 1} \right) \quad T_\nu(z) = 1.95(1+z) K$$



$10^{12} h^{-1} M_\odot$   $\sim 100 \text{ km/s}$

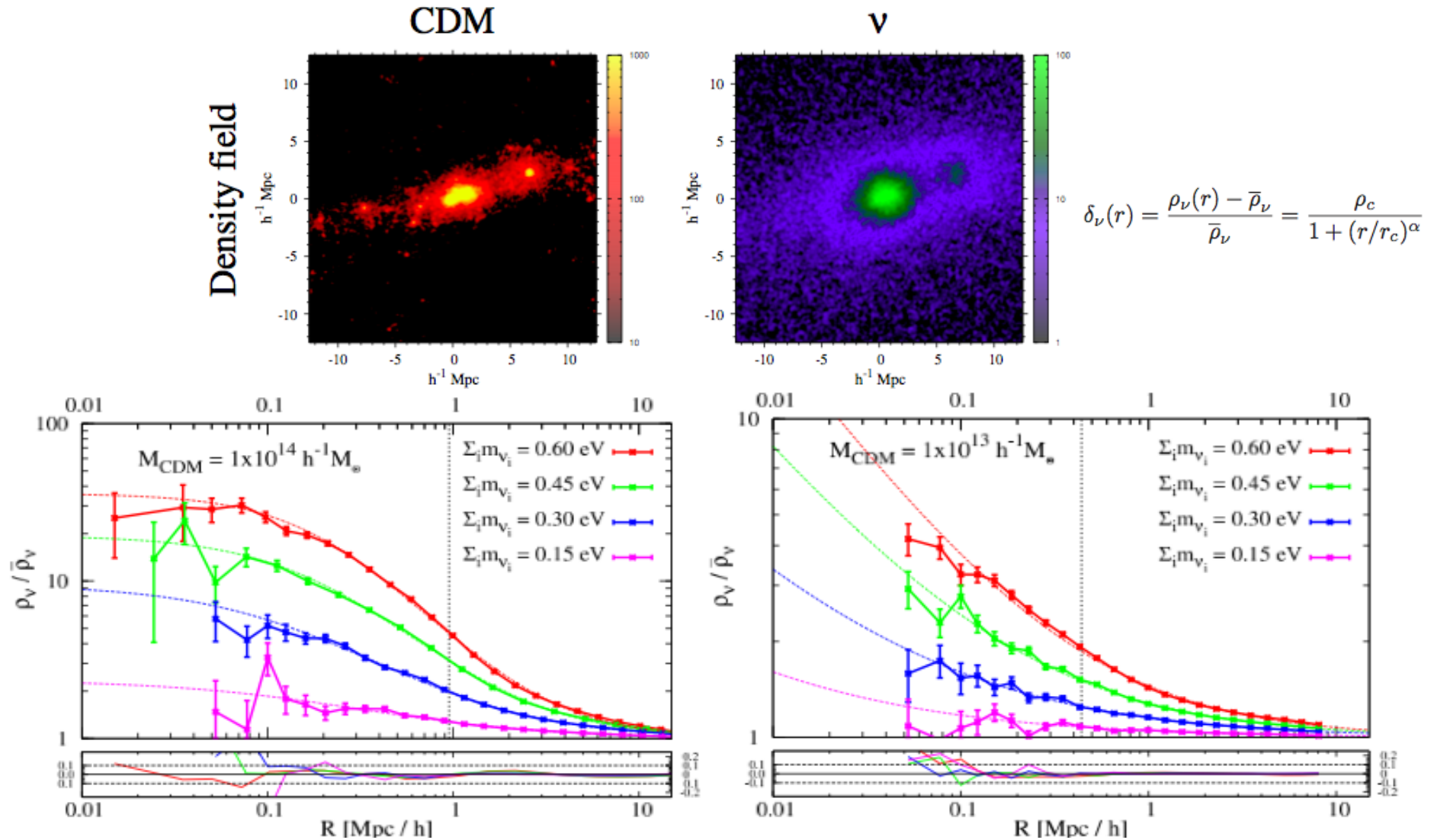
$10^{13} h^{-1} M_\odot$   $\sim 200 \text{ km/s}$

$10^{14} h^{-1} M_\odot$   $\sim 450 \text{ km/s}$

$10^{15} h^{-1} M_\odot$   $\sim 950 \text{ km/s}$



# THE NEUTRINO HALO?



Villaescusa-Navarro, Bird, Garay, Viel, 2013, JCAP, 03, 019  
 Marulli, Carbone, Viel+ 2011, MNRAS, 418, 346

# Halo mass function

Castorina, Sefussati, Sheth, FVN, Viel 2013

FoF halos :  $b=0.2$

$$\frac{dn(M, z)}{dM} = \nu f(\nu) \frac{\rho_m}{M^2} \frac{d \ln \nu}{d \ln M}$$

Universal?

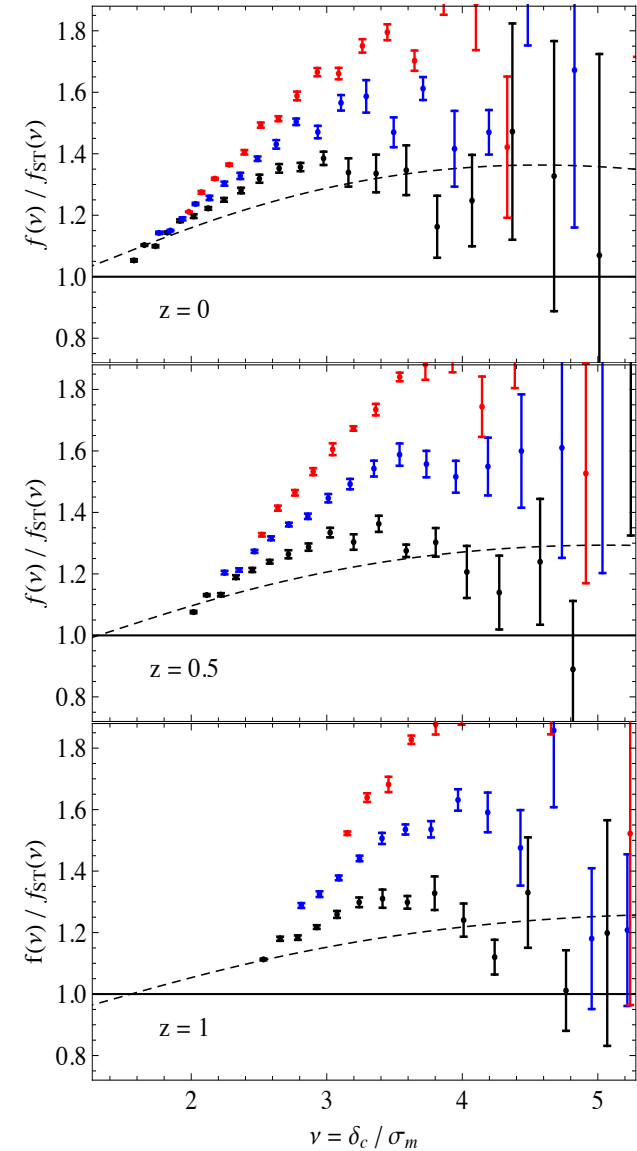
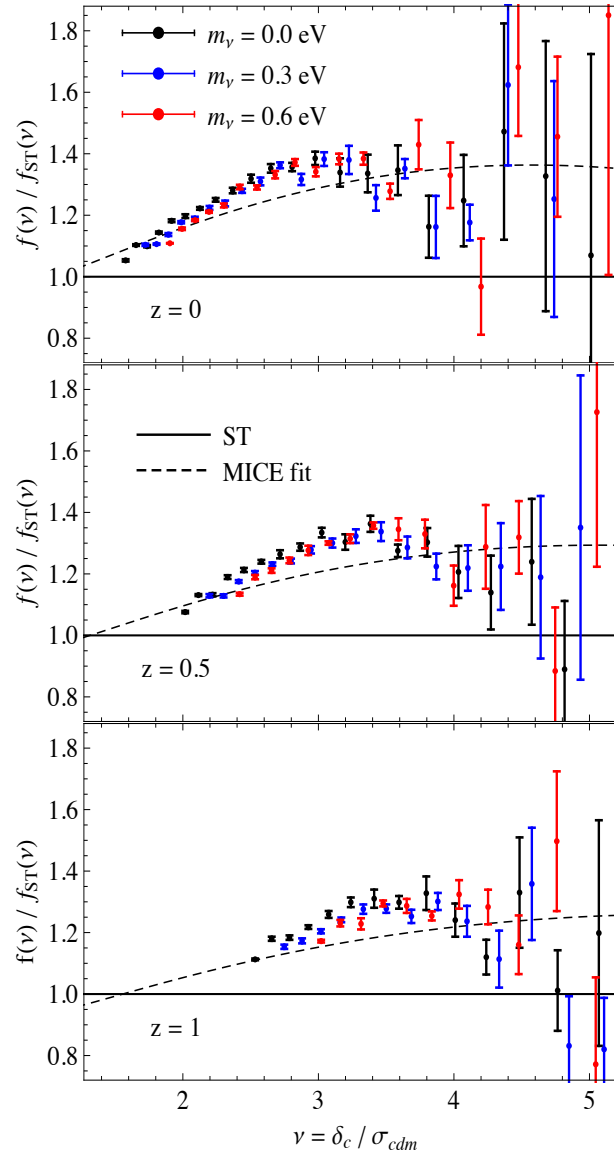
$$f(\nu) = \frac{M^2}{\rho} \frac{1}{\nu} \frac{d \ln M}{d \ln \nu} \frac{dn(M, z)}{dM}$$

~~Matter prescription~~

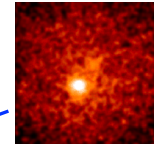
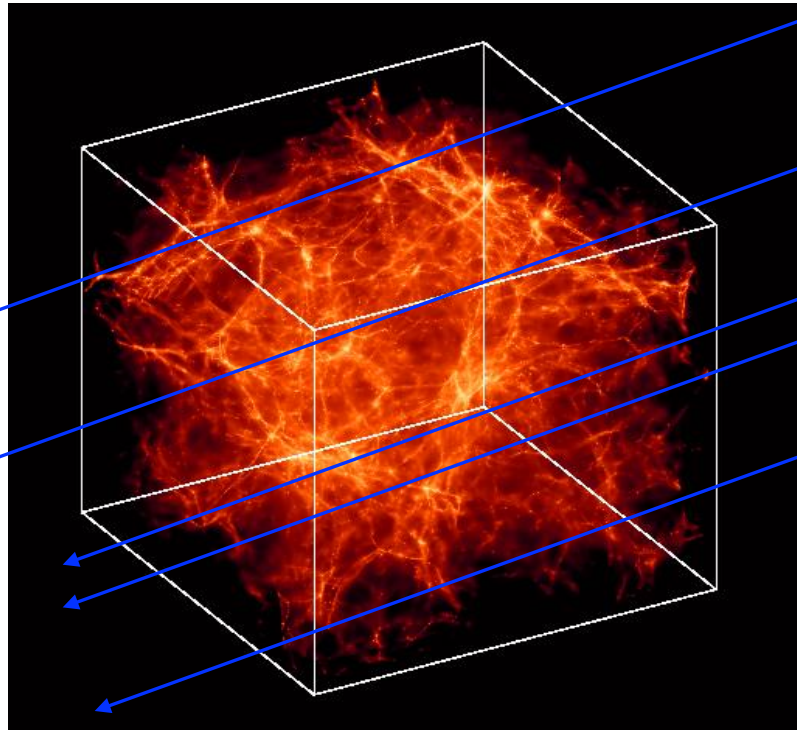
$$\rho_m \rightarrow \rho_{cdm} \quad P_m(k) \rightarrow P_m(k)$$

Cold dark matter prescription

$$\rho_m \rightarrow \rho_{cdm} \quad P_m(k) \rightarrow P_{cdm}(k)$$



# The Intergalactic Medium: Theory vs. Observations



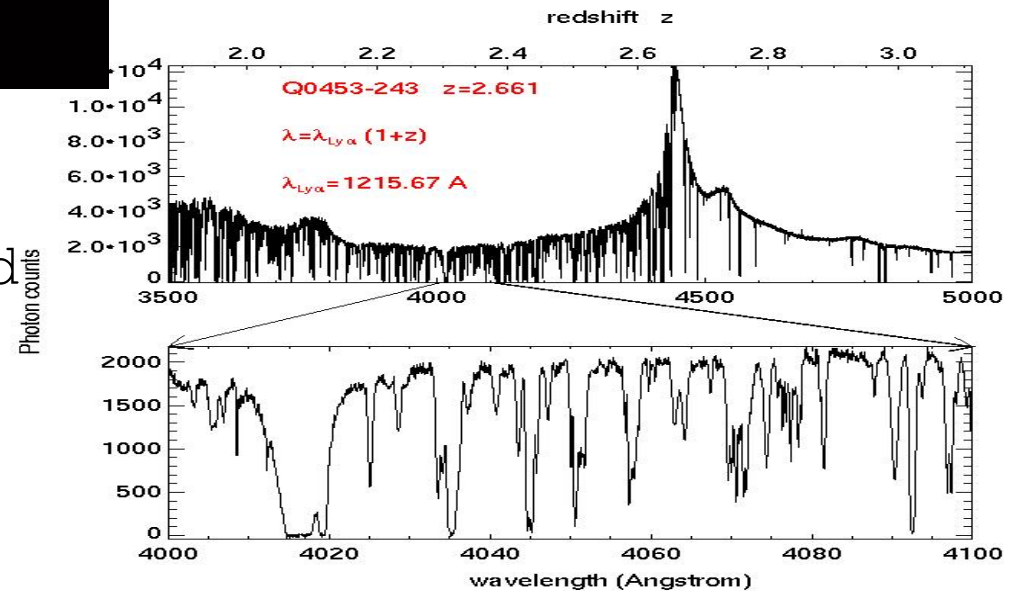
80% of the baryons at  $z=3$  are in the **Lyman- $\alpha$  forest**

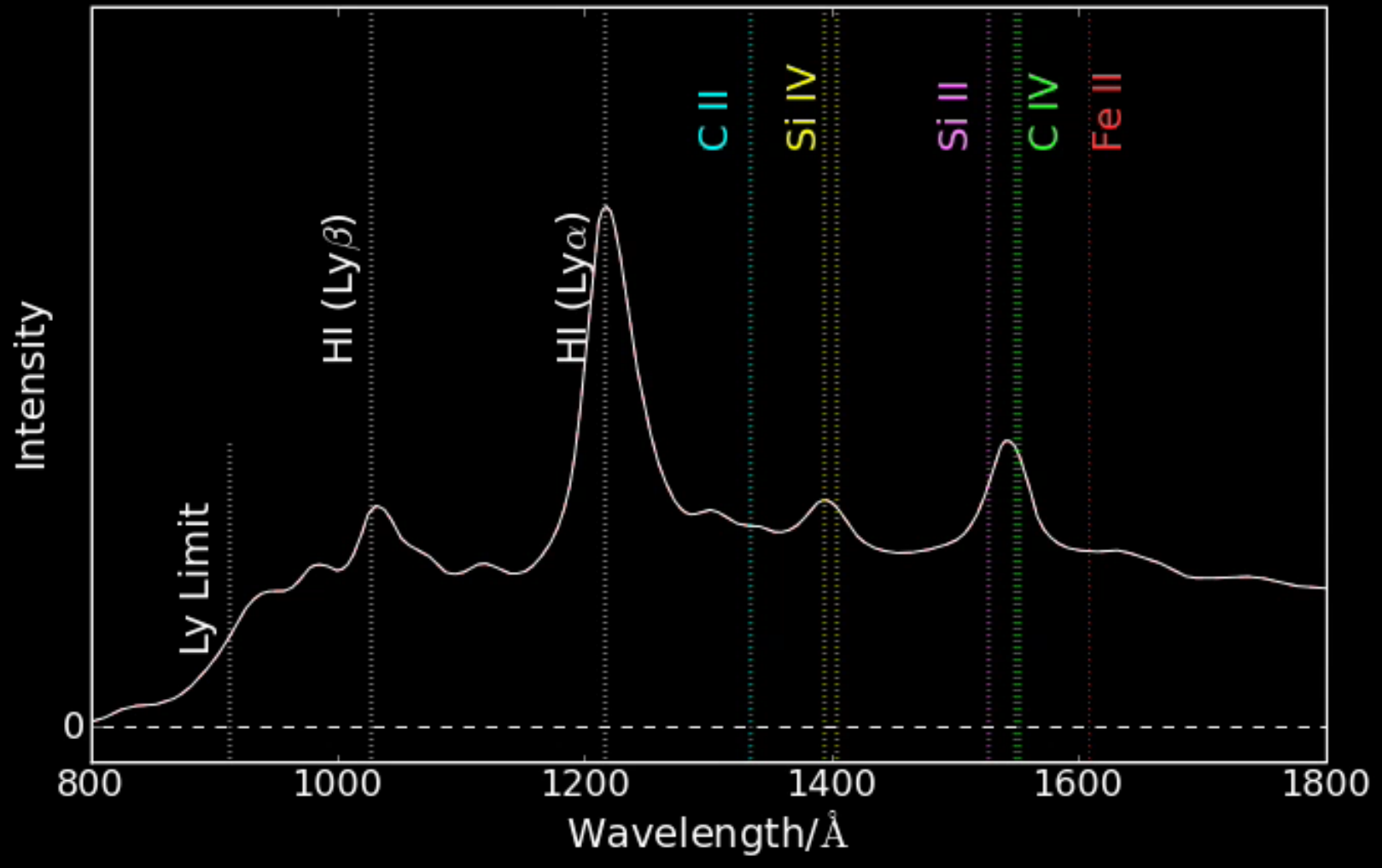
Bi & Davidsen (1997), Rauch (1998)  
Review by Meiksin (2009)



baryons as tracer of the dark matter density field  
 $\delta_{\text{IGM}} \sim \delta_{\text{DM}}$

Croft+ 99,02  
MV+ 04  
McDonald+ 01,03

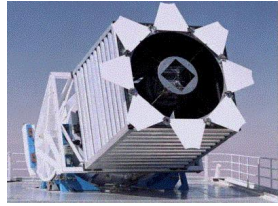




TOPIC	DATA	THEORY	RESULTS
<u>BAOs</u>	QSO Ly $\alpha$ flux and cross correlation with QSOs 3D analysis - <b>low res</b>	Mocks	Clear detection, small tension with Planck
<u>Cosmic neutrinos</u>	IGM QSO Spectra <b>low res</b> 1D flux power	N-body/hydro sims	$\Sigma m_\nu < 0.12$ eV
<u>Cold dark matter Coldness</u>	IGM QSO Spectra <b>high res</b> 1D flux Power	N-body/hydro sims	$m_{\text{WDM}} > 3.3$ keV (thermal cross. sect.)



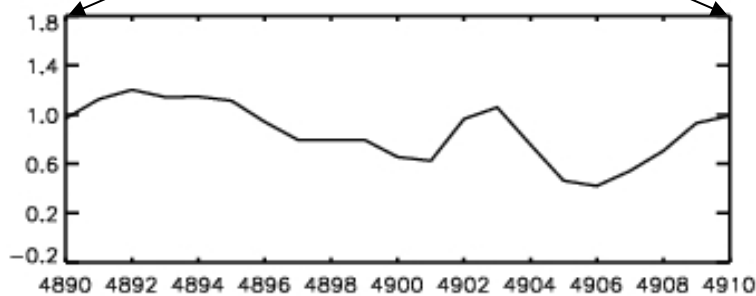
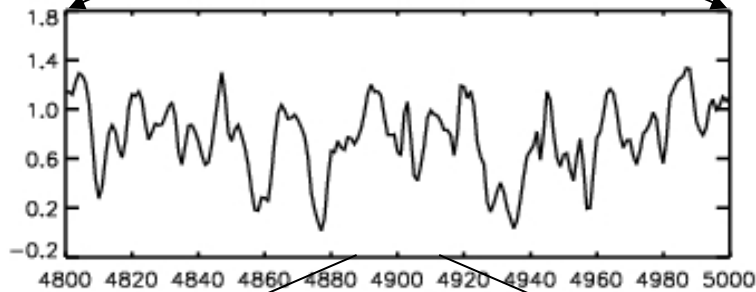
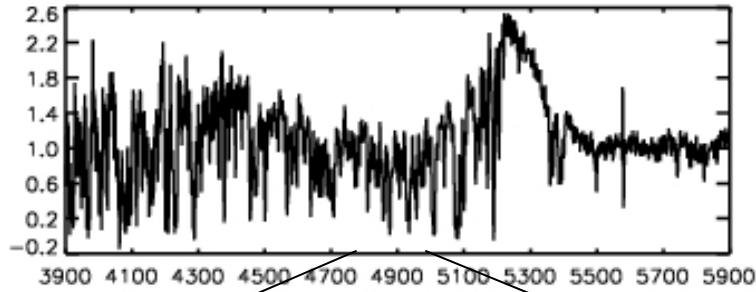
# The data sets



## SDSS vs UVES



McDonald et al. 2005

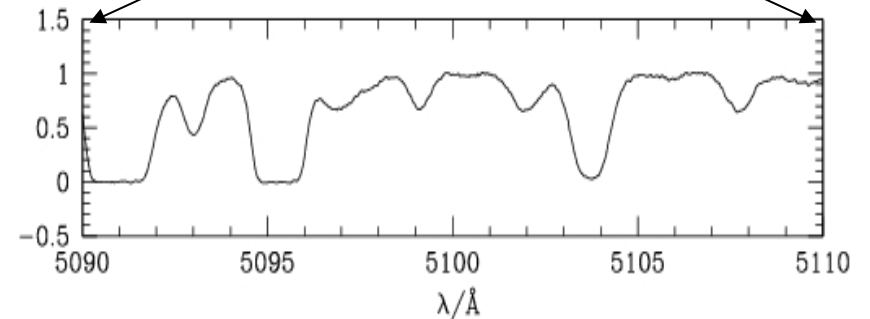
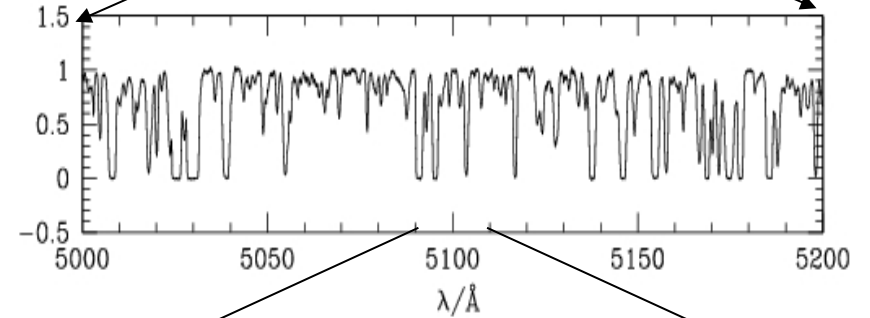
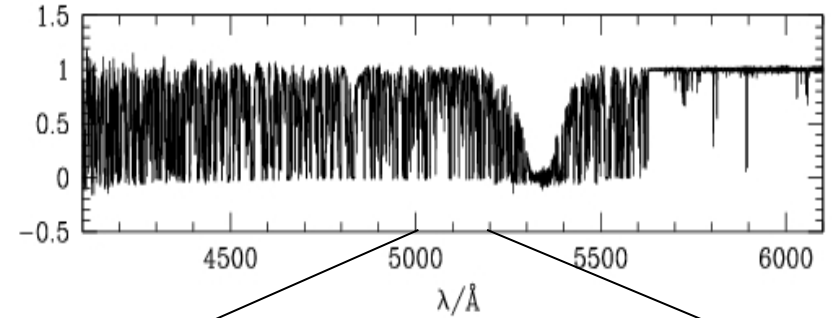


SDSS

$\sim 10^4$  LOW RESOLUTION LOW S/N

vs

Kim, MV+ 2004



UVES/KECK etc.

$\sim 10^2$  HIGH RESOLUTION HIGH S/N

## Key aspects

- High redshift (and small scales):  
possibly closer to linear behaviour

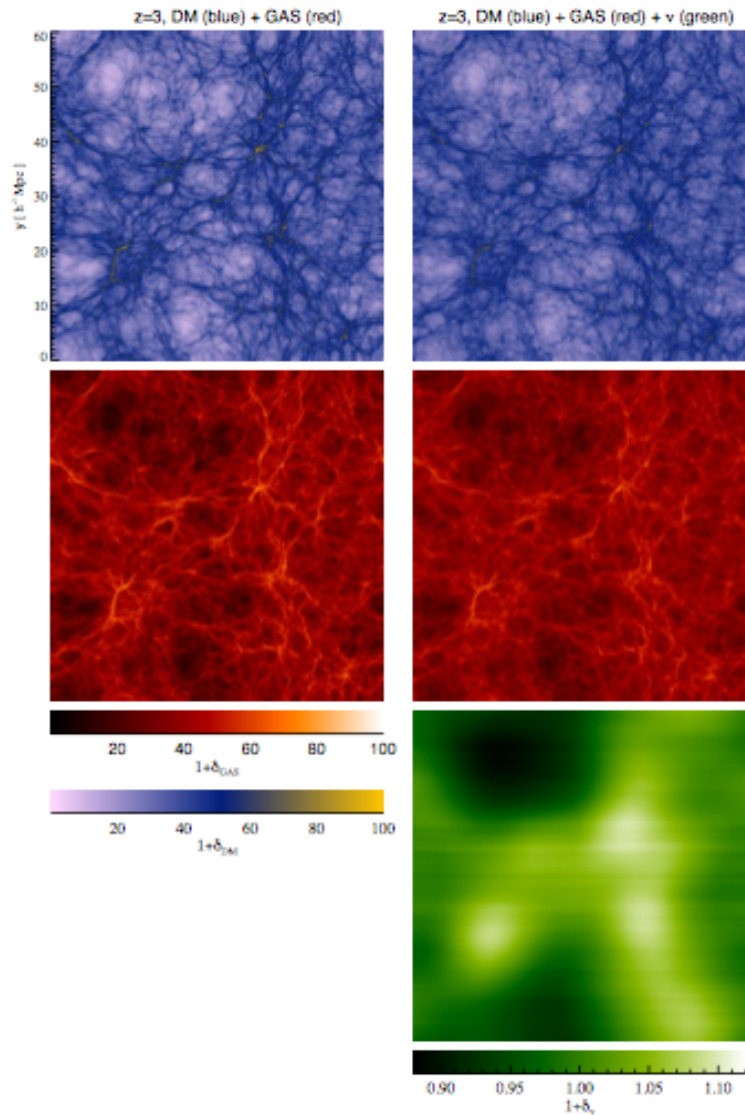
- 1D power: 
$$P_{1D}(k) = \frac{1}{2\pi} \int_k^\infty P_{3D}(x) x dx$$

- Matter probed at around the mean density

# RESULTS FROM BOSS/SDSS-III

NEUTRINOS

## NEUTRINOS IN THE IGM



N-body + hydro sims

Neutrino induced non-linear suppression understood and reproduced also with simple halo modelling (**Massara+ 15**)

Degeneracies with s8 are present

Neutrino induced effects on RSD (Marulli+11), BAOs (Peloso+15), mass functions and bias (Castorina+14) investigated

**FROM IGM ONLY:**

$$\Sigma m_{\nu} < 0.9 \text{ eV} (2\sigma)$$

## METHOD

*DATA*: thousands of low-res. Spectra for neutrino constraints. Few tens for cold dark matter coldness

*SIMULATIONS*: Gadget-III runs: 20 and 60 Mpc/h and  $(512^3, 786^3, 896^3)$

Cosmology parameters:  $\sigma_8, n_s, \Omega_m, H_0, m_{\text{WDM}}$ , + neutrino mass

Astrophysical parameters:  $z_{\text{reio}}, \text{UV fluctuations}, T_0, \gamma, \langle F \rangle$

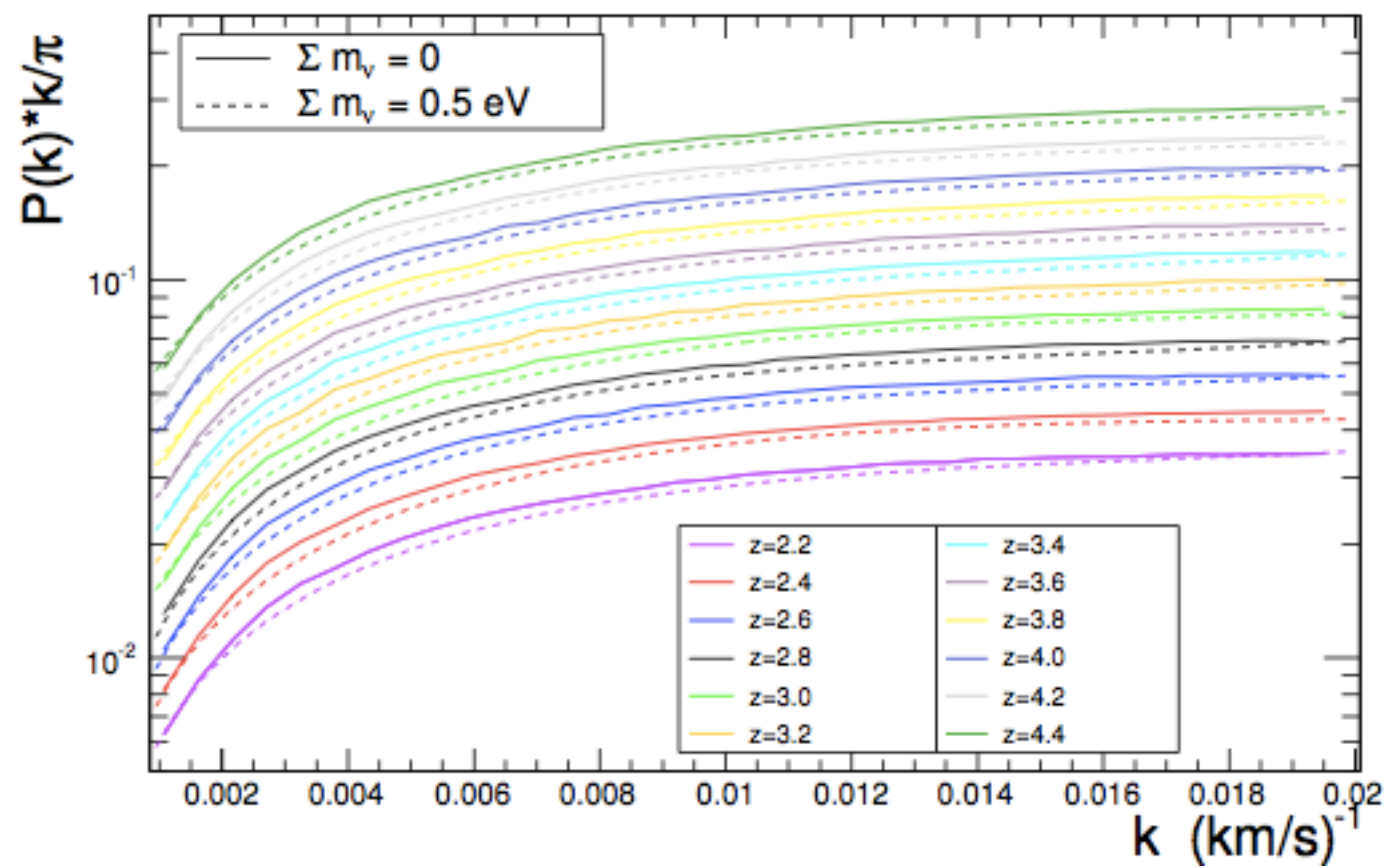
Nuisance: resolution, S/N, metals

*METHOD*: Monte Carlo Markov Chains likelihood estimator  
+ **very conservative assumptions** for the continuum fitting and error bars on the data

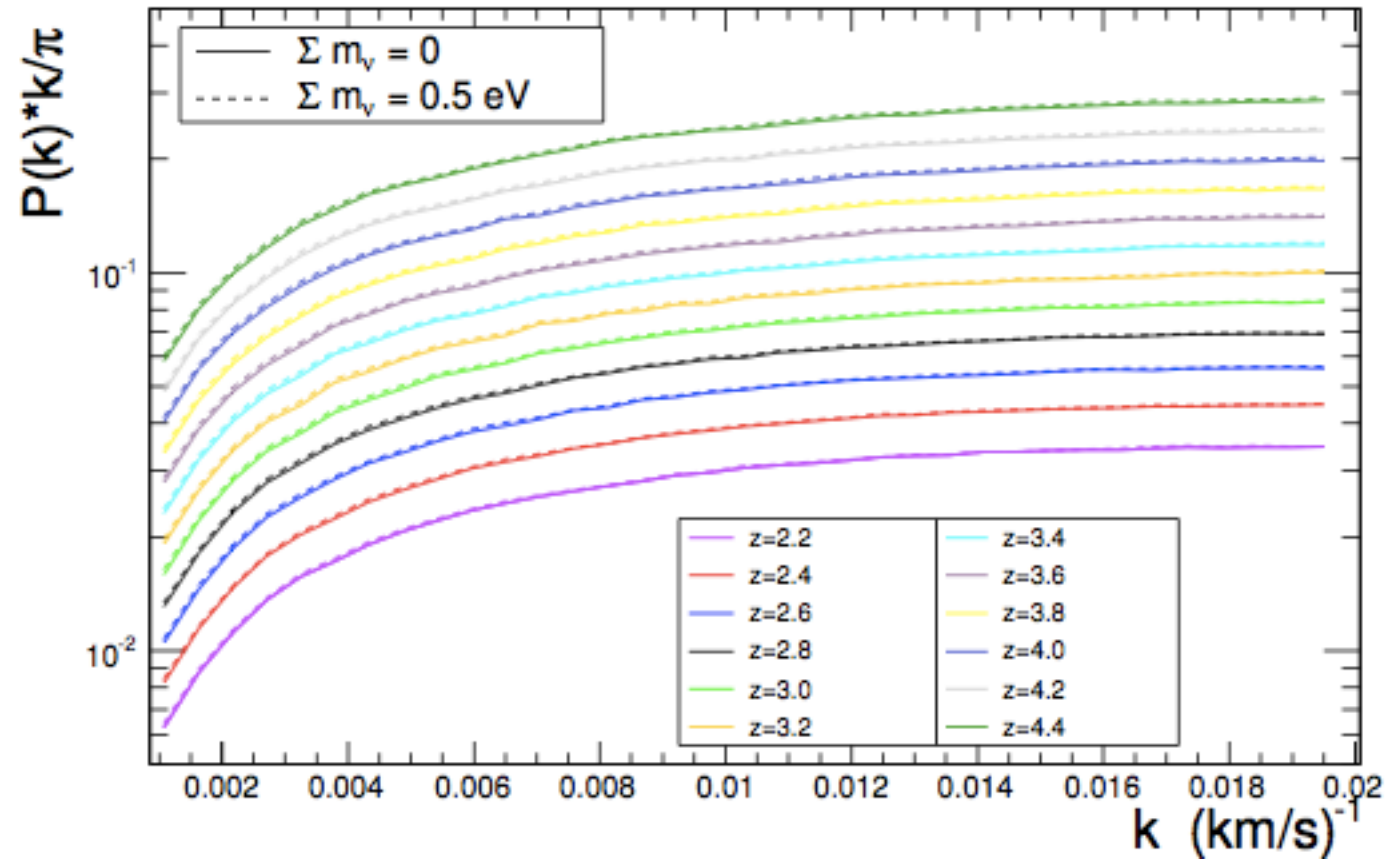
Parameter space: second order Taylor expansion of the flux power

$$P_F(k, z; \mathbf{p}) = P_F(k, z; \mathbf{p}^0) + \sum_i^N \left. \frac{\partial P_F(k, z; p_i)}{\partial p_i} \right|_{\mathbf{p}=\mathbf{p}^0} (p_i - p_i^0) + \text{second order}$$

## NEUTRINO IMPACT - I



## NEUTRINO IMPACT - II



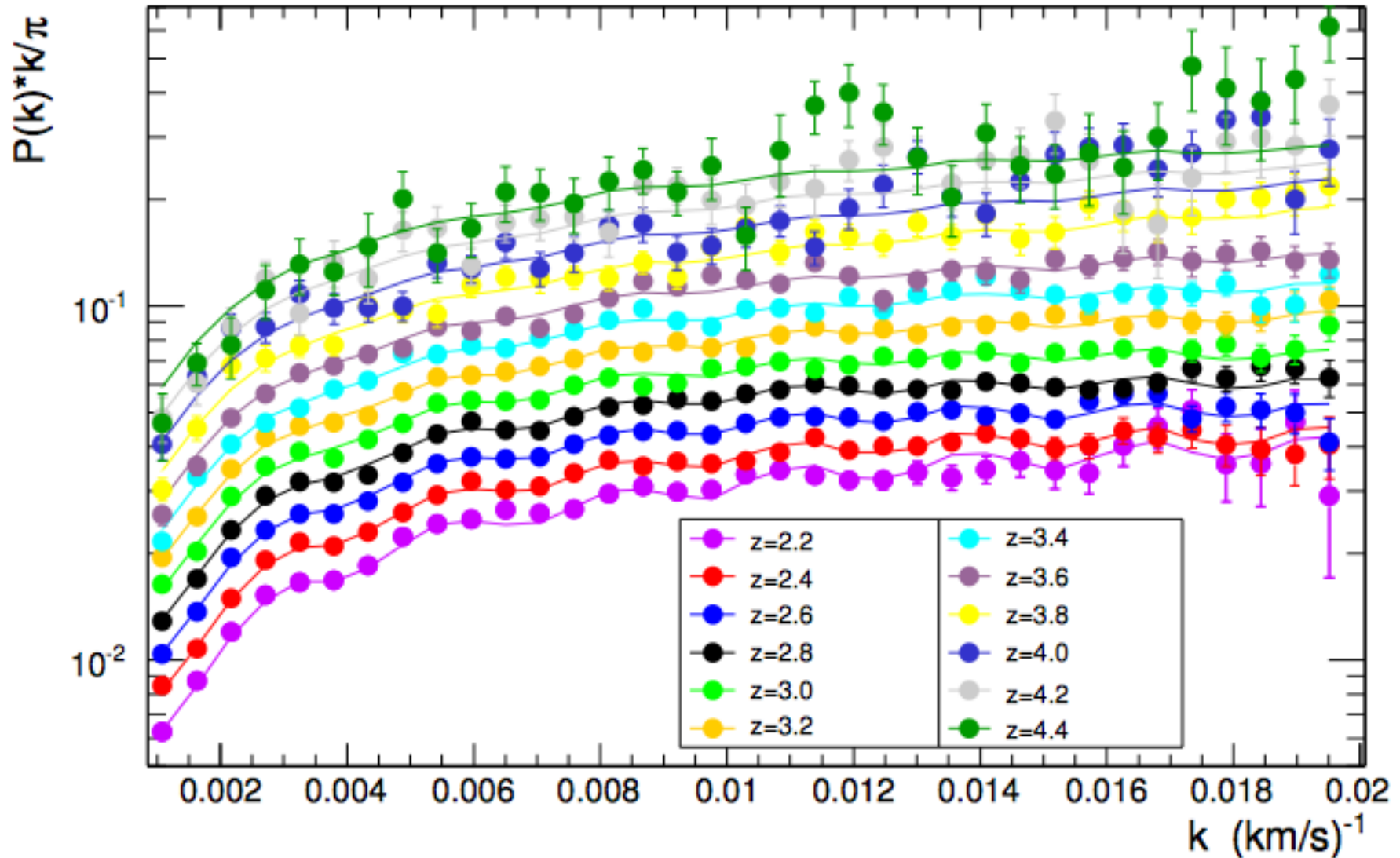


# GROWTH OF STRUCTURES AT HIGH REDSHIFT

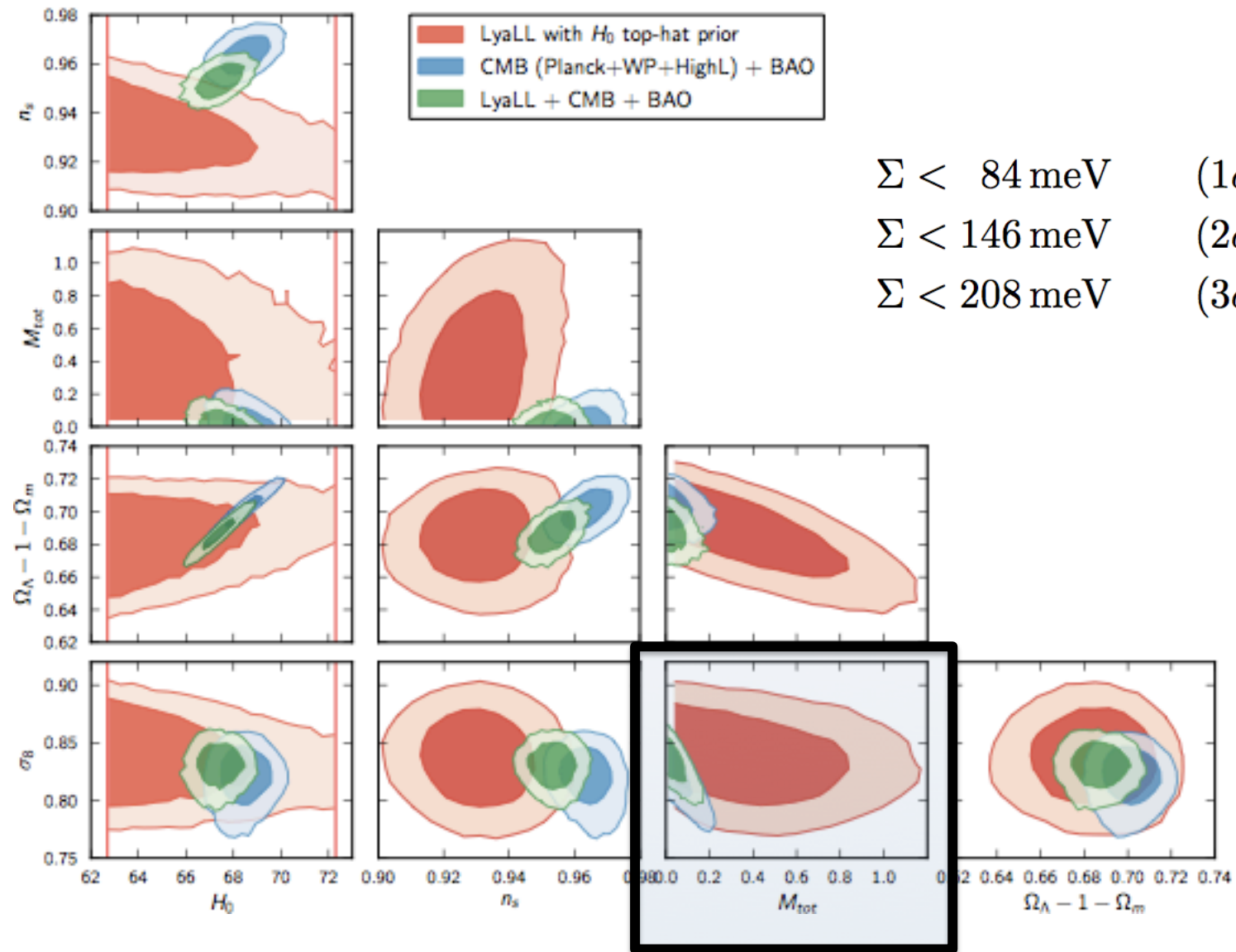
Constraint on neutrino masses from SDSS-III/BOSS Ly $\alpha$  forest and other cosmological probes

1D Flux power spectrum evolution

Nathalie Palanque-Delabrouille,<sup>a,b</sup> Christophe Yèche,<sup>a</sup> Julien Lesgourgues,<sup>c,d,e</sup> Graziano Rossi,<sup>a,f</sup> Arnaud Borde,<sup>a</sup> Matteo Viel,<sup>g,h</sup> Eric Aubourg,<sup>i</sup> David Kirkby,<sup>j</sup> Jean-Marc LeGoff,<sup>a</sup> James Rich,<sup>a</sup> Natalie Roe,<sup>b</sup> Nicholas P. Ross,<sup>k</sup> Donald P. Schneider,<sup>l,m</sup> David Weinberg<sup>n</sup>



# BAYESIAN ANALYSIS



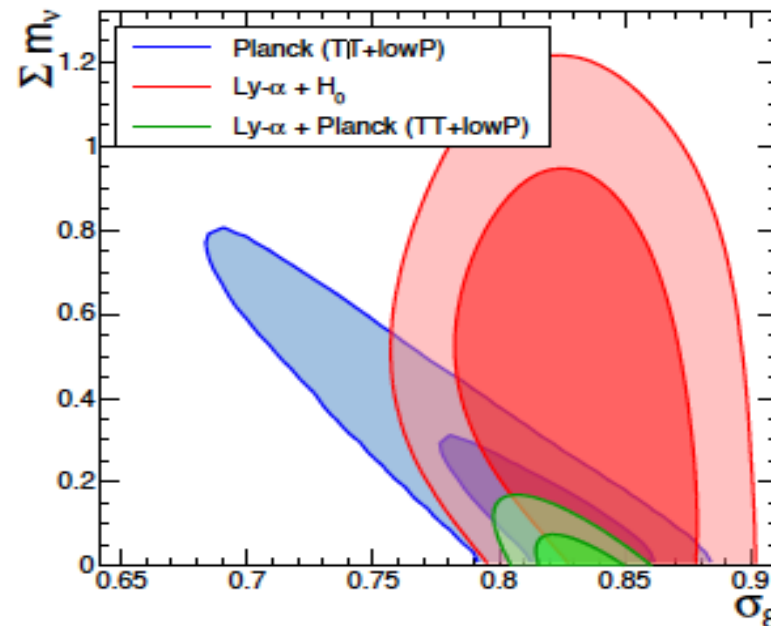
## FINAL NUMBERS

Parameter	$\text{Ly}\alpha + H_0^{\text{tophat}}$ ( $62.5 \leq H_0 < 72.5$ )	$\text{Ly}\alpha + \text{CMB}$	$\text{Ly}\alpha + \text{CMB}$ + BAO	$\text{Ly}\alpha + \text{CMB}(A_L)$
$10^9 A_s$	$3.2^{+0.5}_{-0.7}$	$2.20^{+0.05}_{-0.06}$	$2.20^{+0.05}_{-0.06}$	$2.18^{+0.05}_{-0.06}$
$10^2 \omega_b$	(fixed to 2.22)	$2.20 \pm 0.02$	$2.20 \pm 0.02$	$2.22 \pm 0.03$
$\omega_{\text{cdm}}$	$0.110^{+0.008}_{-0.013}$	$0.1200^{+0.0019}_{-0.0018}$	$0.1196^{+0.0015}_{-0.0014}$	$0.1191 \pm 0.002$
$\tau_{\text{reio}}$	(irrelevant)	$0.091^{+0.012}_{-0.013}$	$0.091^{+0.011}_{-0.013}$	$0.0871^{+0.012}_{-0.013}$
$n_s$	$0.931 \pm 0.012$	$0.953 \pm 0.005$	$0.953 \pm 0.005$	$0.955^{+0.005}_{-0.006}$
$H_0$	$< 70.9$ (95%)	$67.2^{+0.8}_{-0.9}$	$67.4 \pm 0.7$	$67.5^{+1.0}_{-1.1}$
$\sum m_\nu$ (eV)	$< 0.98$ (95%)	$< 0.16$ (95%)	$< 0.14$ (95%)	$< 0.21$ (95%)
$A_L$	(fixed to 1)	(fixed to 1)	(fixed to 1)	$1.12 \pm 0.10$
$\sigma_8$	$0.84 \pm 0.03$	$0.830^{+0.017}_{-0.013}$	$0.830^{+0.016}_{-0.012}$	$0.818^{+0.021}_{-0.014}$
$\Omega_m$	$0.316^{+0.018}_{-0.021}$	$0.316 \pm 0.012$	$0.313 \pm 0.009$	$0.312 \pm 0.013$

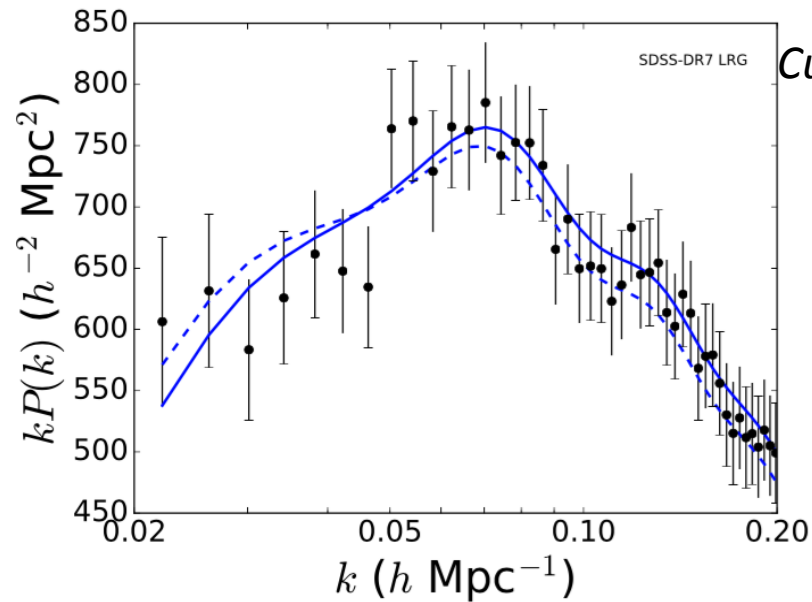
UPDATE using Planck 15

Palanque-Delabrouille+ 2015

Parameter	(1) Ly $\alpha$ + $H_0^{\text{Gaussian}}$ ( $H_0 = 67.3 \pm 1.0$ )	(2) Ly $\alpha$ + Planck TT+lowP	(3) Ly $\alpha$ + Planck TT+lowP + BAO	(4) Ly $\alpha$ + Planck TT+TE+EE+lowP + BAO
$\sigma_8$	$0.831 \pm 0.031$	$0.833 \pm 0.011$	$0.845 \pm 0.010$	$0.842 \pm 0.014$
$n_s$	$0.938 \pm 0.010$	$0.960 \pm 0.005$	$0.959 \pm 0.004$	$0.960 \pm 0.004$
$\Omega_m$	$0.293 \pm 0.014$	$0.302 \pm 0.014$	$0.311 \pm 0.014$	$0.311 \pm 0.007$
$H_0$ (km s $^{-1}$ Mpc $^{-1}$ )	$67.3 \pm 1.0$	$68.1 \pm 0.9$	$67.7 \pm 1.1$	$67.7 \pm 0.6$
$\Sigma m_\nu$ (eV)	$< 1.1$ (95% CL)	<b><math>&lt; 0.12</math> (95% CL)</b>	$< 0.13$ (95% CL)	$< 0.12$ (95% CL)
Reduced $\chi^2$	0.99	1.04	1.05	1.05

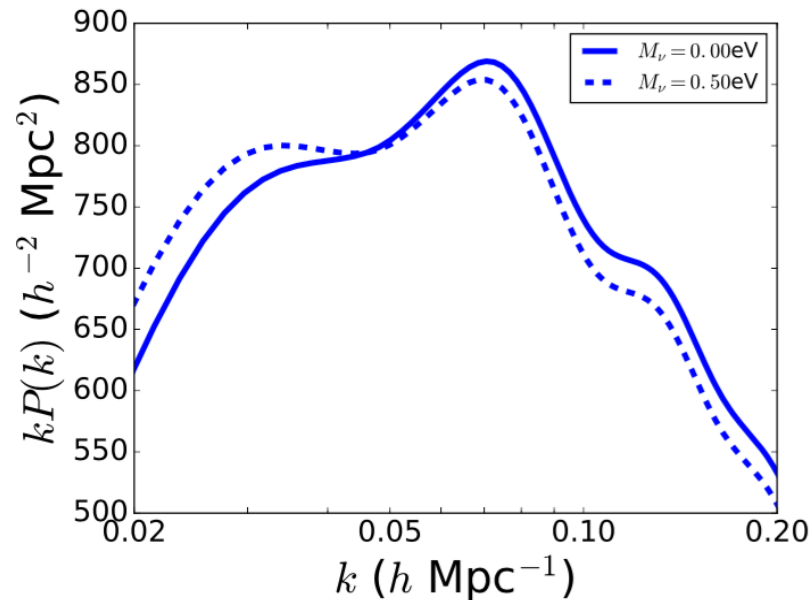


# Constraints from galaxy clustering



Cuesta+16

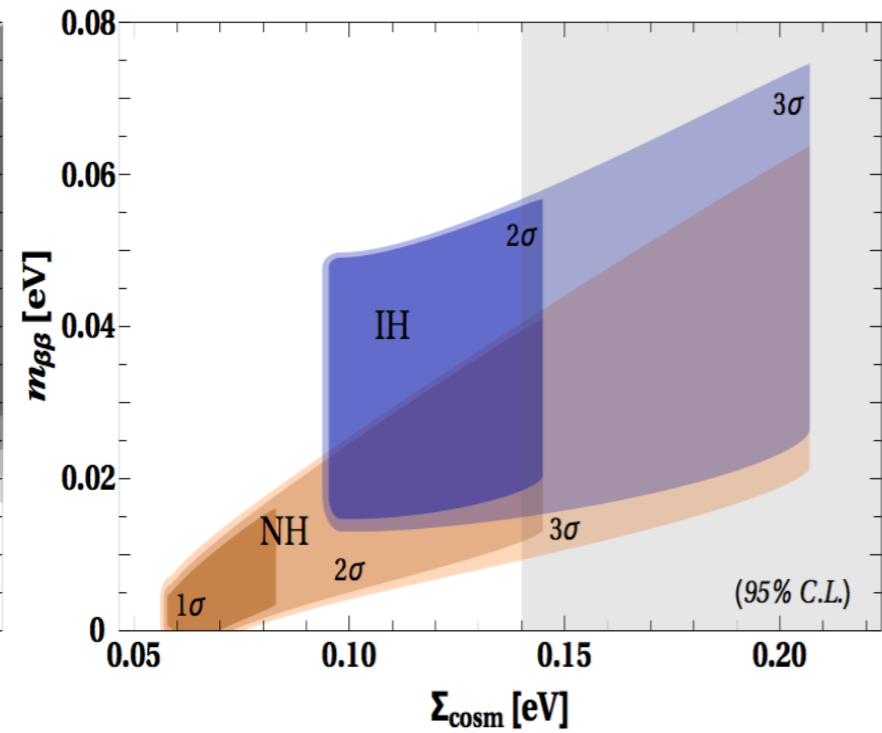
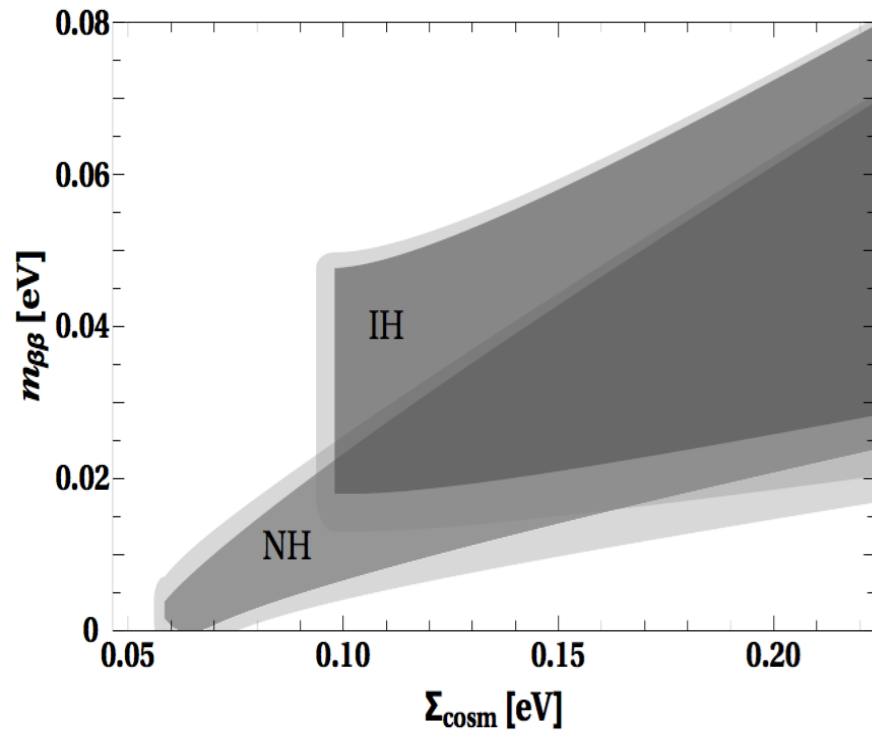
- Galaxy clustering offers independent constraints that mainly exploit the shape
- Notice: galaxy bias  $P_{gal} = b^2 \times P_{matter}$  marginalized over but some assumptions on the bias  $b(k, z)$  model must be made



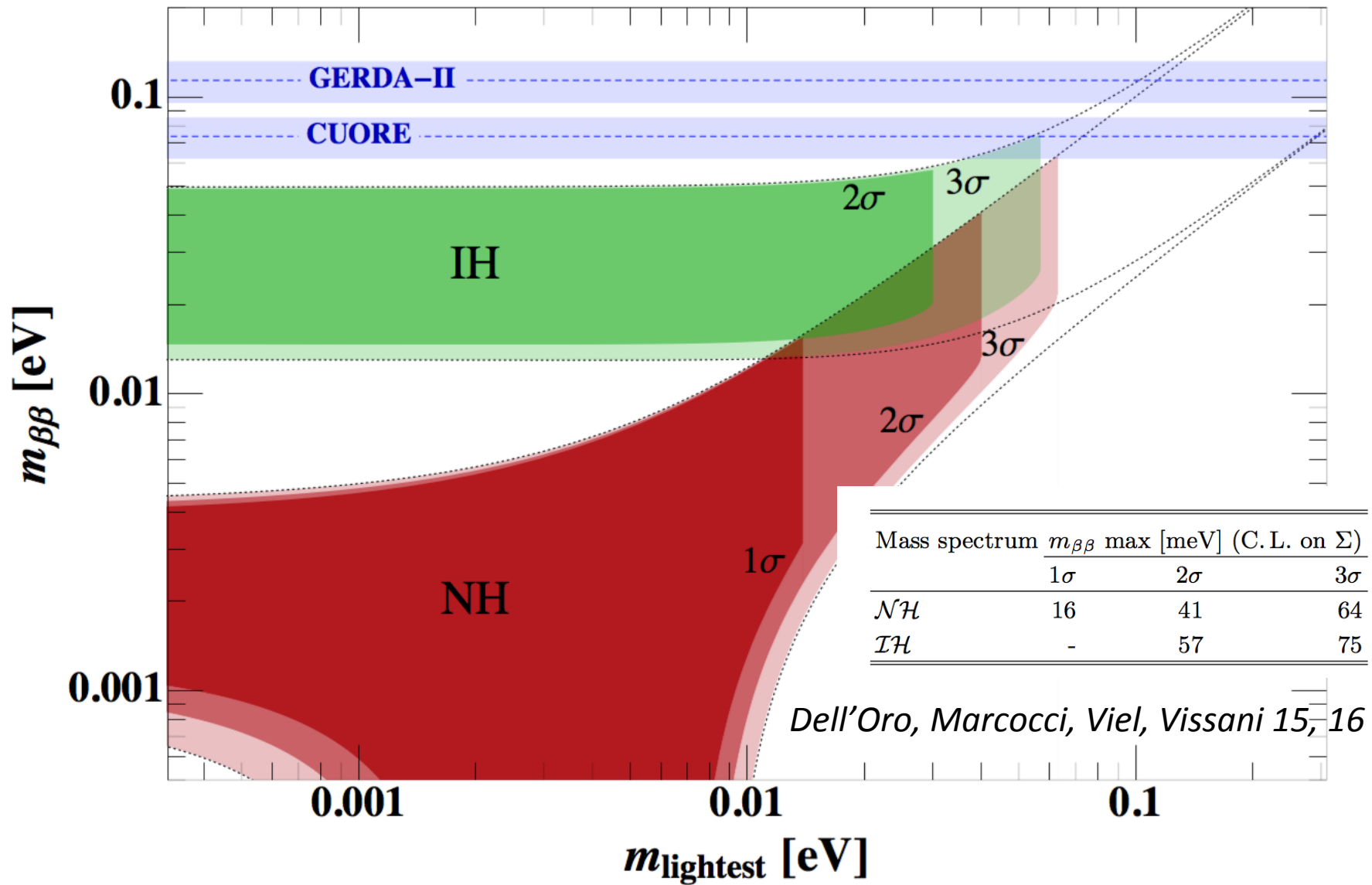
Parameter	CMB15+LRG+BAO
$100 \omega_b$	$2.236^{+0.014}_{-0.014}$
$\omega_{\text{cdm}}$	$0.1183^{+0.0012}_{-0.0011}$
$n_s$	$0.9677^{+0.0042}_{-0.0045}$
$\tau_{\text{reio}}$	$0.083^{+0.016}_{-0.017}$
$\ln(10^{10} A_s)$	$3.097^{+0.031}_{-0.034}$
$H_0$	$68.06^{+0.55}_{-0.55}$
$\sigma_8$	$0.831^{+0.016}_{-0.015}$
$M_\nu$ [eV]	$< 0.13$

# Implications for neutrinoless double beta decay - I

*Dell'Oro, Marcocci, Viel, Vissani 15,16*



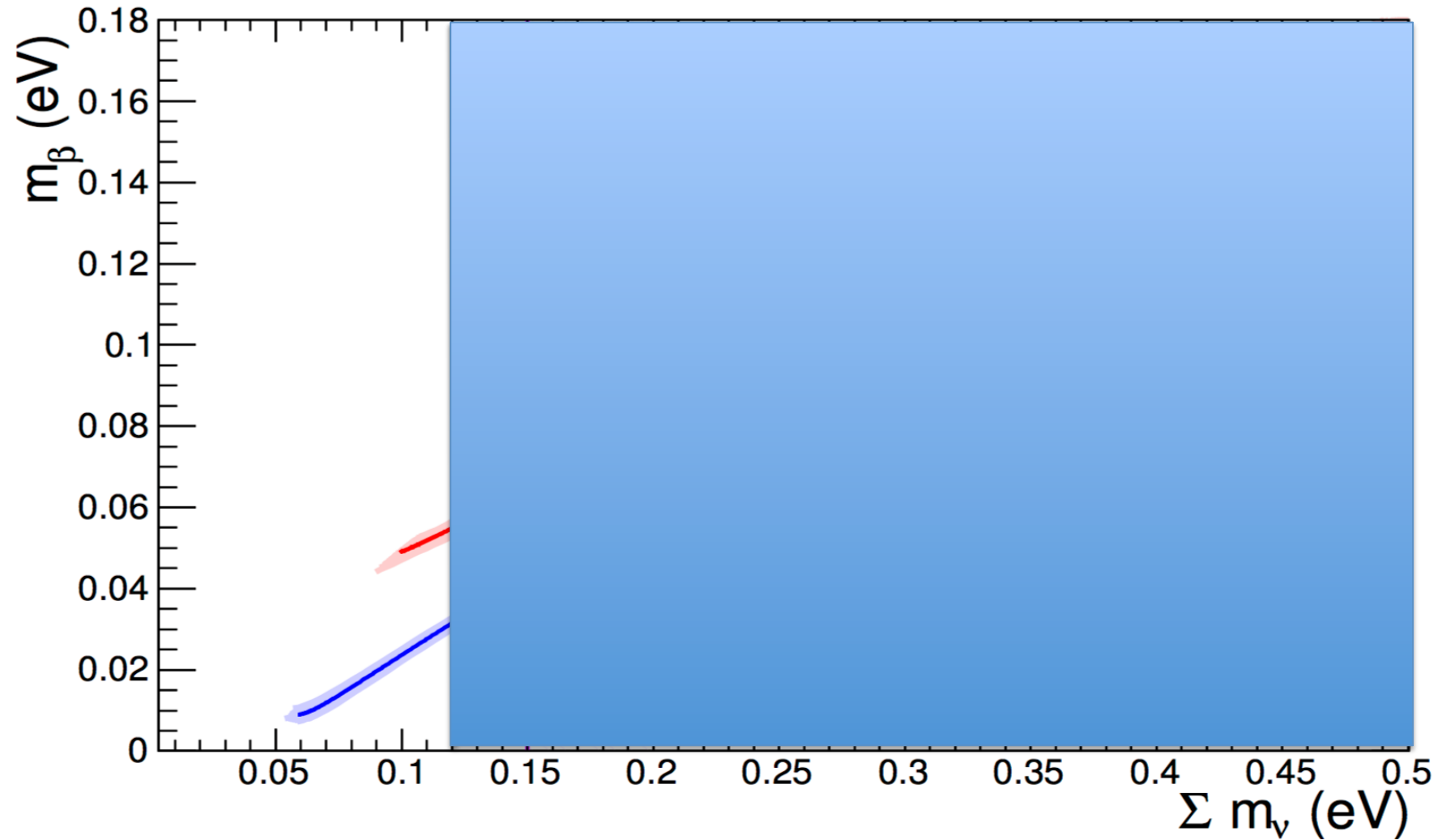
# Implications for neutrinoless double beta decay - II



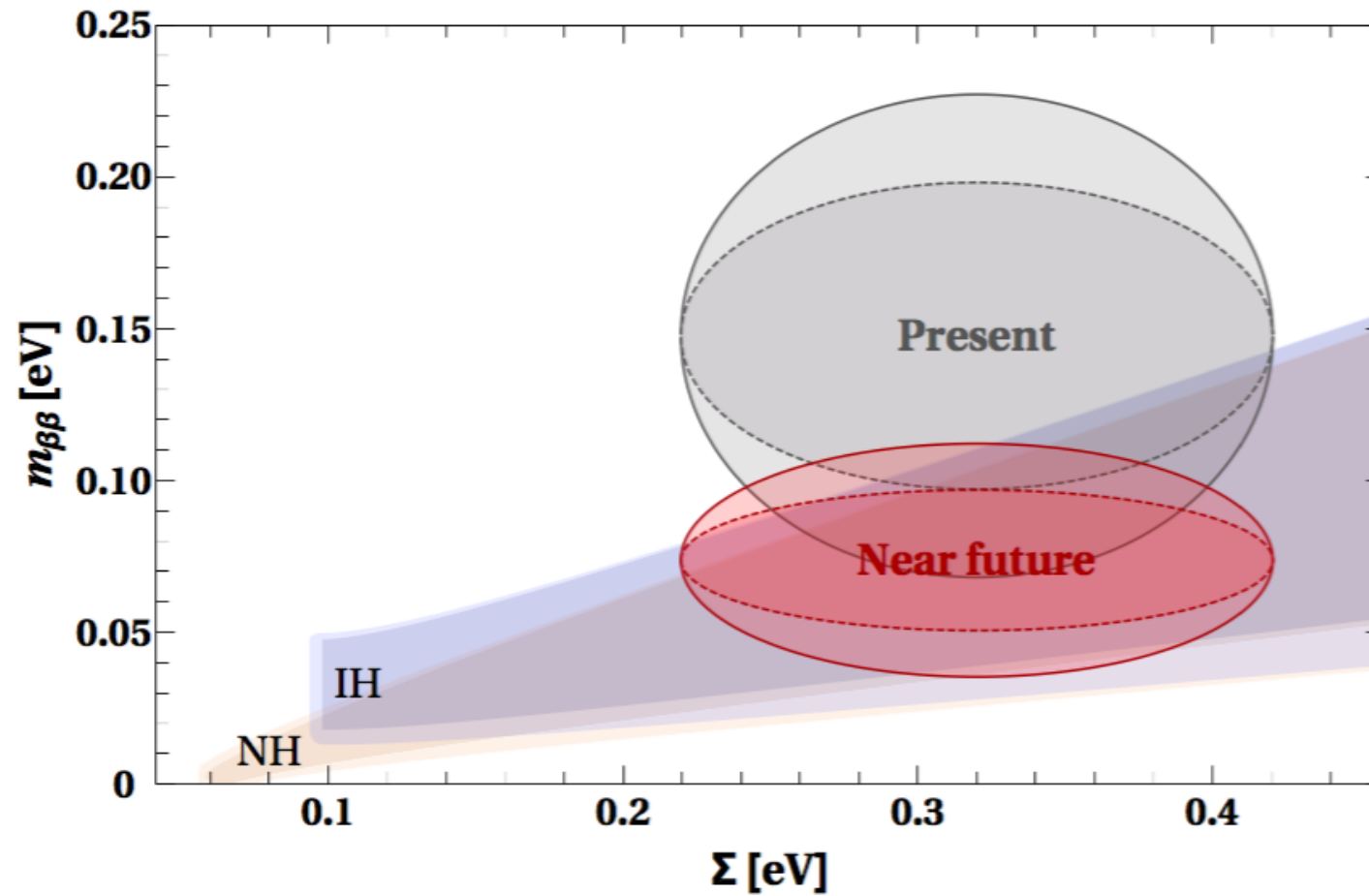


## Implications for Tritium beta decay

$$m_\beta = \left( \sum_i |U_{ei}|^2 m_i^2 \right)^{\frac{1}{2}} = \left( c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2 \right)^{\frac{1}{2}}$$



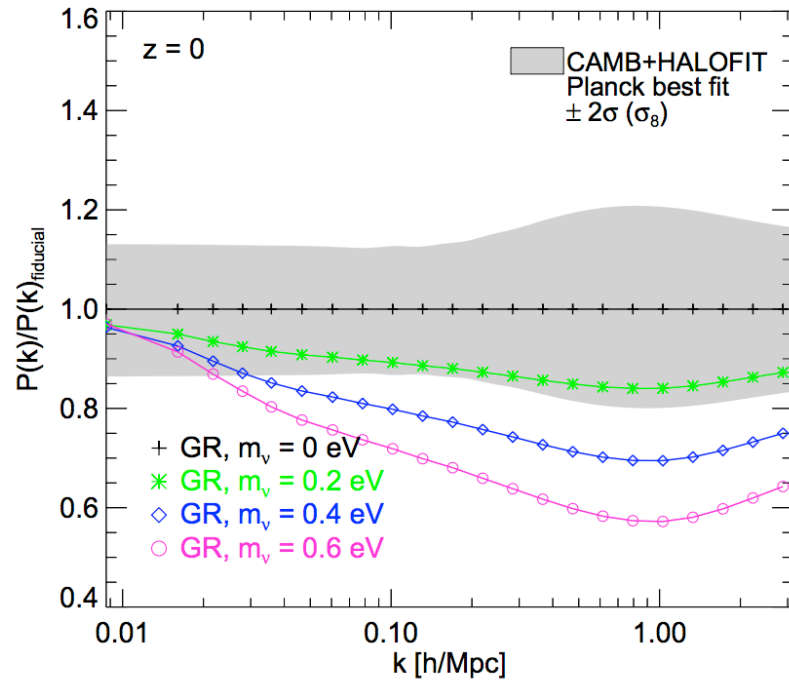
What if ... non-zero neutrino claims are correct?



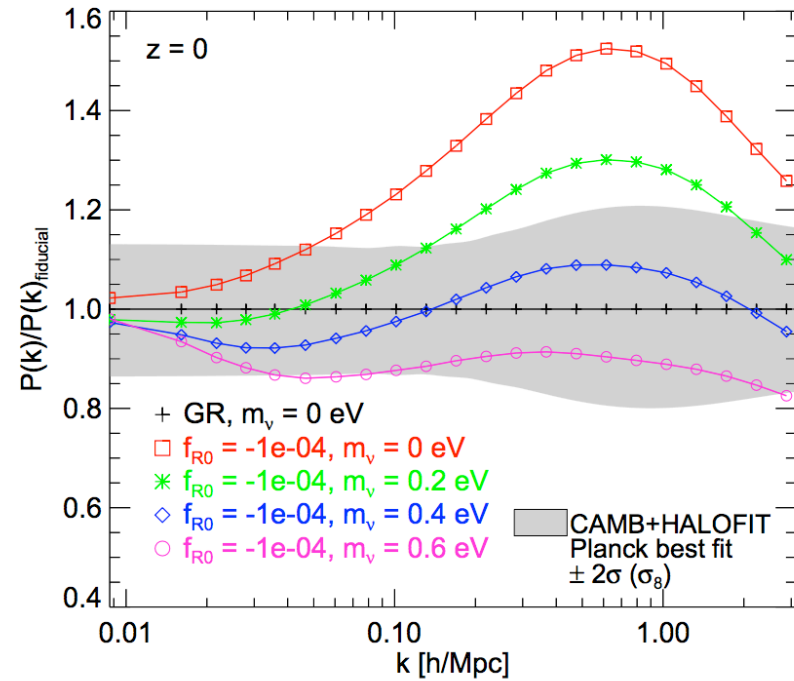
# What if ... large non-zero neutrino mass found?

Baldi, Villaescusa-Navarro, Viel, Puchwein, Springel, Moscardini, 2014

## General Relativity + massive neutrinos



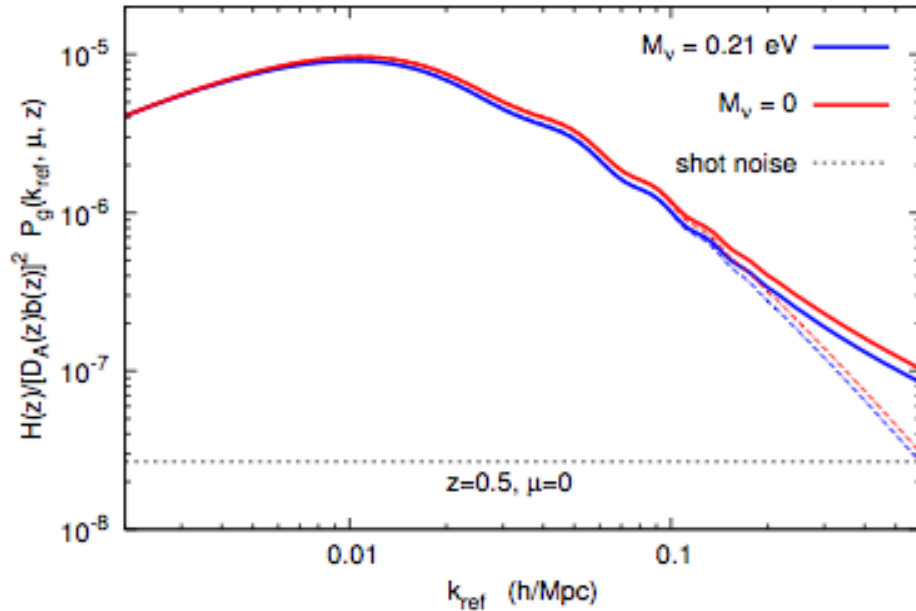
## Modified gravity + massive neutrinos



# FORECASTS

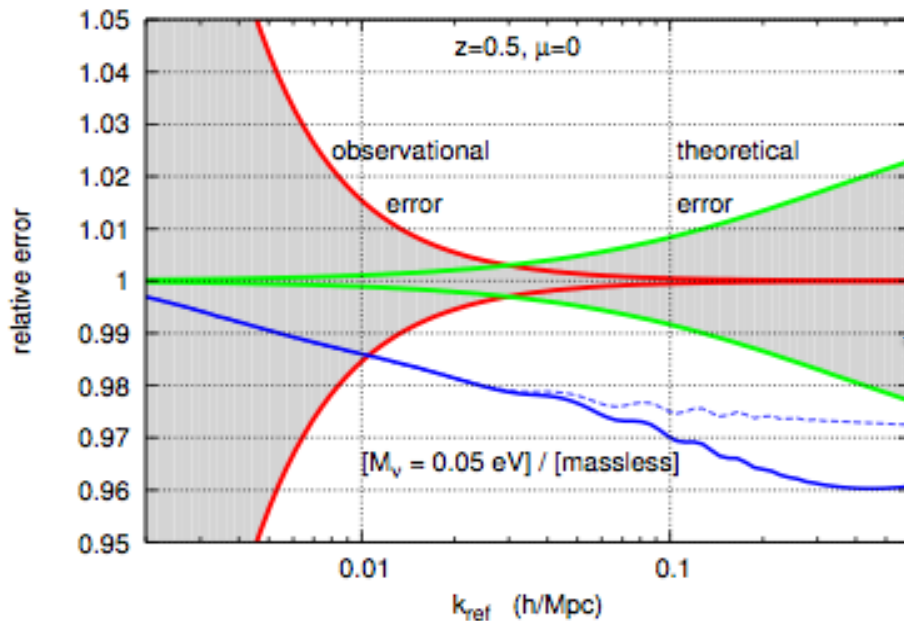
# MASSIVE NEUTRINO FORECASTS for Euclid

Audren, Lesgourgues, Bird, Haehnelt, MV 2013



Non-linearities

- $\sigma(M_\nu) = 18 \text{ meV} \rightarrow 5 \text{ meV}$  when going from 0.1 to 0.6 h/Mpc
- with conservative errors the improvement is modest
- with realistic error could be 20%

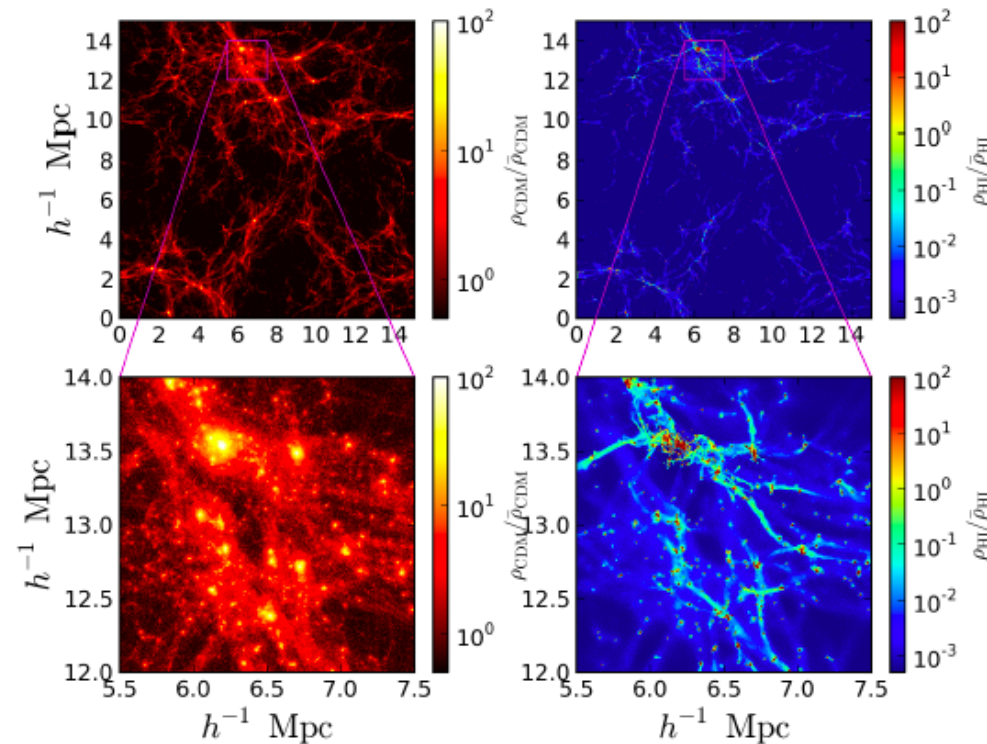


Need to be modelled accurately

See also Costanzi et al. 2013 for clusters

$k_{\max}$ ( $h/\text{Mpc}$ )	un. err.	co. err.	$10^4\omega_b$	$10^4\omega_c$	$10^3n_s$	$10^{11}A_s$	$10^3h$	$z_{\text{reio}}$	$3m_\nu = M_\nu$ (meV)
0.1	–	–	1.2	6.2	2.8	3.0	4.1	0.38	18
0.1	1/10	–	1.2	6.9	2.8	3.1	4.5	0.39	18
0.1	1/2	–	1.3	9.5	3.2	3.5	6.1	0.39	23
0.1	•	–	1.3	11	3.4	3.6	6.7	0.40	25
0.1	•	•	1.3	11	3.4	3.6	6.7	0.40	25
0.6	–	–	0.86	2.1	0.37	1.2	0.40	0.23	5.9
0.6	1/10	–	1.1	4.8	2.5	2.7	3.0	0.37	14
0.6	1/2	–	1.2	8.6	3.2	3.4	5.7	0.39	22
0.6	•	–	1.3	10	3.4	3.6	6.7	0.39	25
0.6	•	•	1.3	10	3.4	3.6	6.7	0.39	25

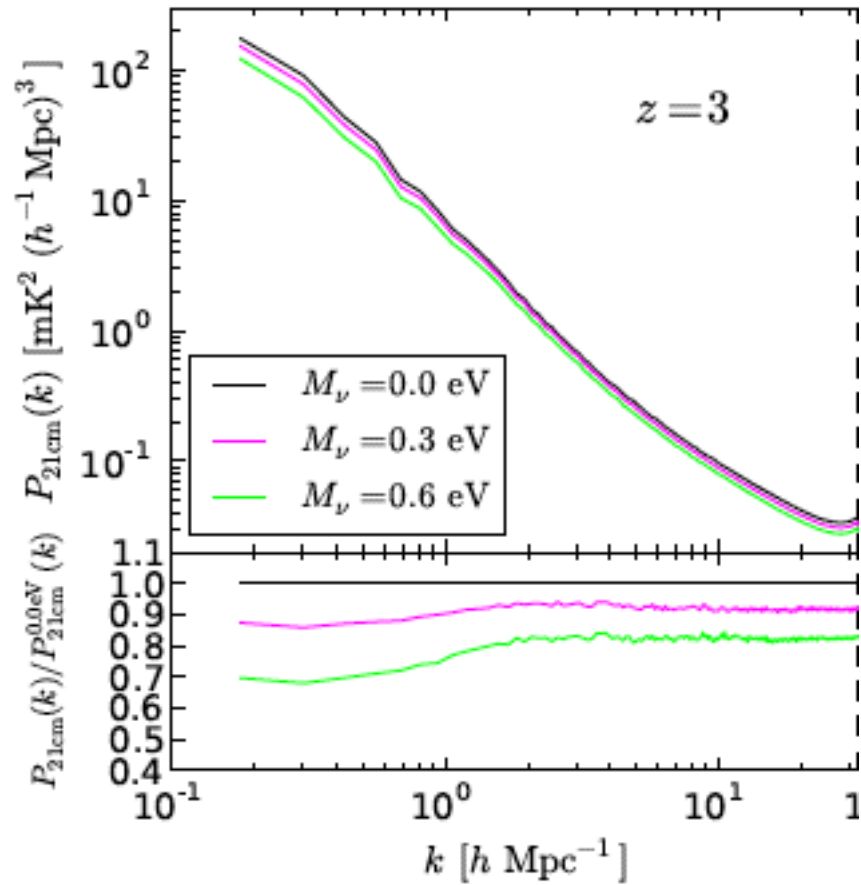
HI halo model	
Linear matter power spectrum	$P_m(k, z)$
Halo mass function	$n(M, z)$
Halo bias	$b(M, z)$
HI mass in halos	$M_{HI}(M, z)$
HI density profile in halos	$\rho_{HI}(r   M, z)$



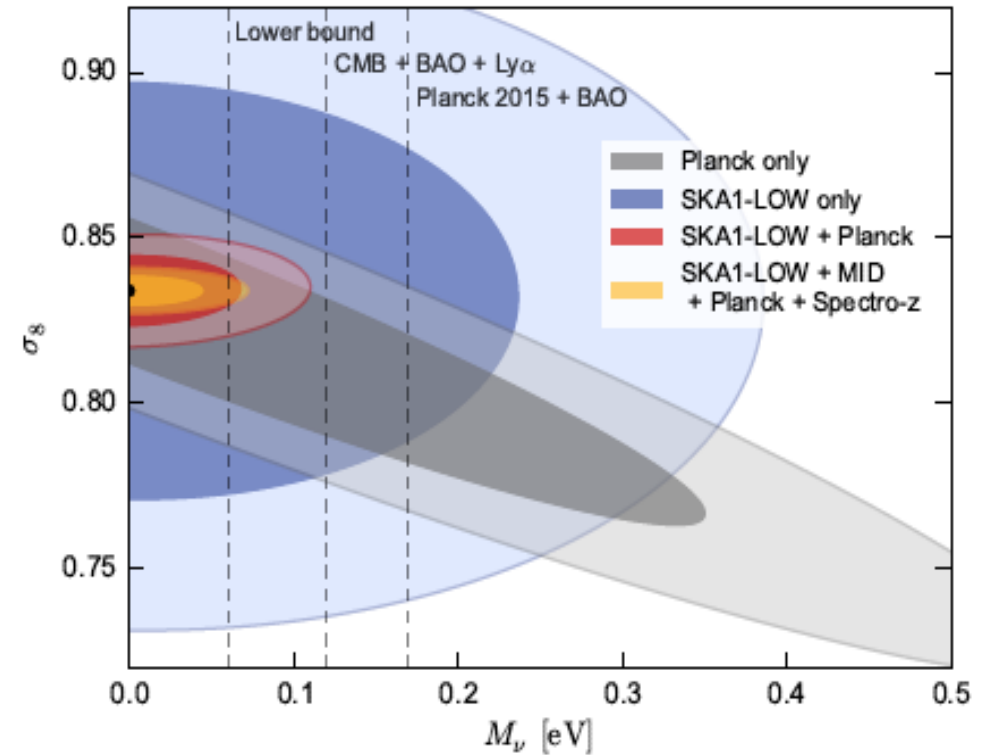


**FROM ABSORPTION TO EMISSION:  
NEUTRINOS in 21cm INTENSITY MAPPING with SKA**

Villaescusa-Navarro, Bull, MV, arXiv: 1507.05102



$\sigma(M_\nu) = 0.06 \text{ eV}$  ( $2\sigma$  error bar)



## CONCLUSIONS

- From CMB data  $\Delta N_{\text{eff}}$  constrained to be  $< 0.2$
- Limits on total neutrino mass  $0.17-0.2$  eV (2s C.L.)
- Adding Large Scale Structure data could provide hints for detection or tighten limits further depending on the data set used. Some recent WL and Cluster analysis are however in agreement with Planck
- Lyman-alpha forest data + CMB or galaxy clustering +CMB are the most constraining combination  $< 0.12-13$  eV
- Implications for neutrinoless double beta decay and Tritium beta decay are important
- Non-linear window on neutrino CNB is now open