Lepton mixing from Lepton mixing from Lepton sector





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magnituae High scale seesaw Quark- lepton symmetry /analogy GUT



Spurious scale?

Electroweak -LHC

Looking under the lamp



Low scale seesaw, radiative mechanisms, RPV, high dimensional operators

Scale of neutrino masses themselves Relation to dark energy, MAVAN?

Neutrino mass itself is the fundamental scale of new physics





No convincing understanding of mass and mixing pattern although some constructions may have connection to reality.

The problem is to identify correct ones among hundreds ideas, approaches, models

with scepticism: no explanation of quark masses and mixing

Back to bottom

Back to data, search for hints, indications. Look for connection to other sectors, e.g. Dark sector of the Universe

May be

Solutions of problems of visible sector in the Hidden sector







Daya Bay Collaboration (An, F.P. et al.) arXiv:1505.03456 [hep-ex]









M.C. Gonzalez-Garcia, M. Maltoni, T. Schwetz, JHEP 1411 (2014) 052,1409.5439 [hep-ph]

2-3 mixing:

asymmetric for NO and IO NO: $sin^2\theta_{23}$ = 0.45, IO: 0.58

Small preference IO and 2nd quadrant

Data confirm prediction $\theta_{13} \sim \sqrt{\frac{1}{2}} \theta_c$ $\sin^2 \theta_{13} \sim \frac{1}{2} \sin^2 \theta_c$



Phenomenological level

C. Giunti, M. Tanimoto



From QLC (Quark-Lepton Complementarity) H. Minakata, A Y S



From TBM-Cabibbo scheme

S. F. King et al

Now accuracy of measurements permits detailed comparison



can be always written

Deeper sense: reflects/indicates certain theoretical framework



Two types of new physics and partial relations

CIXM type new physics

Neutrino new physics

Framework and prediction

$$L_{PMNS} = U_{CKM}^{+} U_{X}$$

$$U_{PMNS} = U_{CKM}^{+} U_{X}$$
where $U_{CKM} \sim V_{CKM}$
has similar hierarchical structure
determined (as in Wolfenstein
parametrization) by powers of
 $\lambda = \sin \theta_{c}$

$$A = \sin \theta_{c}$$

$$A = \sin \theta_{c}$$

$$A = \sin \theta_{c}$$

$$C = Gunti, M. Tanimoto
H. Minakata, A Y S
S - Z. Xing
Harada
S - Antusch, S. F. King
Y Farzan, A Y S
M Picariello, etc.
$$U_{X} = U_{23}(\pi/4) U_{12}$$
arbitrary;
no 1-3 rotation
(or very small)$$

$$U_{PMNS} = U_{CKM}^{+} U_{23}(\pi/4) U_{12}$$

In the first approximation ~ $U_{12} (\theta_c)^{+} U_{23}(\pi/4) U_{12}$

permutation - to reduce the lepton mixing matrix to the standard form

$$\sin \theta_{13} \sim \sqrt{\frac{1}{2}} \sin \theta_C$$

CKM corrections

take whole V_{CKM} with small elements V_{td} , V_{cb} , etc. \rightarrow this will give also corrections to 2-3 mixing

take in general, non-maximal rotation $U_{23}(\theta_{23}^{*})$: $U_{X} = \Gamma(\alpha) U_{23}(\theta_{23}^{*}) U_{12}(\theta_{12}^{*}) \Gamma(\alpha) = \text{diag}(1, 1, e^{i\alpha})$ phase matrix

$$\sin^2 \theta_{13} = \sin^2 \theta_{23} \sin^2 \theta_c \Big(1 - 2\cot \theta_{23}^2 \cos (\alpha - \phi_{td}) |V_{td}| / |V_{cd}| \Big)$$

where $\phi_{td} = \text{Arg V}_{td}$ In Wolfenstein parametrization

$$\sin^2 \theta_{13} = \sin^2 \theta_{23} \lambda^2 \Big(1 - 2A\lambda^2 [(1 - \rho)^2 + \eta^2]^{1/2} \cot^2 \theta_{23} \cos(\alpha - \phi_{td}) \Big)$$

$$\frac{\tan^2 \theta_{23} = \tan^2 \theta_{23}^{*} (1 - \lambda^2) \left[1 - 2A\lambda^2 [(1 - \rho)^2 + \eta^2]^{1/2} \sin^{-1} 2\theta_{23}^{*} \cos \alpha \right]}{\tan^2 \theta_{23}^{*} = \tan^2 \theta_{23}^{*} \kappa (\alpha) \qquad \kappa = (1 - \lambda^2) \left[1 - 4A\lambda^2 [(1 - \rho)^2 + \eta^2]^{1/2} \cos \alpha \right]}$$

Excluding $\theta_{23}^{*} \sin^2 \theta_{13}^{*} = f(\theta_{23}, \alpha)$





a) CKM -corrections; $\sin^2\theta_{23}^{*} = 0.50$ b) No CKM corrections, $\sin^2\theta_{23}^{*} = 0.45$ ($\sin^2\theta_{23}^{*} = 0.40$) c) CKM-corrections, $\sin^2\theta_{23}^{*} = 0.47$ ($\sin^2\theta_{23}^{*} = 0.42$) cos ($\alpha - \phi_{td}^{*}$) = 1

What does this mean?



Quarks and leptons know about each other,
 Q L unification, GUT
 Common flavor symmetries
 Some additional physics is involved in the lepton sector which explains smallness of neutrino mass and difference of the quark and lepton mixing patterns



Indicates SO(10)

Two types of new physics

CKM











IMPORTANT:

 M_R can be related to GUT / Planck scale

Framework and Seesaw mechanism

Natural and simplest realization of the framework is the seesaw type I

 $\mathbf{m}_{v} = -\mathbf{m}_{D} (\mathbf{M}_{R})^{-1} \mathbf{m}_{D}^{T} \qquad \mathbf{m}_{D} = U_{L} (\mathbf{m}_{D}^{\text{diag}}) U_{R}^{+} \qquad B \text{ Dasgupta A.S}$

In the simplest SO(10): $U_L = V_{CKM}^*$

then U_x is the matrix which diagonalizes

 $M_X = -m_D^{diag} U_R^+ (M_R)^{-1} U_R^* m_D^{diag}$

that is

$$M_X = U_X M_X^{diag} U_X^T = U_X m_v^{diag} U_X^T \sim m_{TBM}$$

$$M_R = - m_D^{diag} (m_{TBM})^{-1} m_D^{diag}$$

very hierarchical, Generated by seesaw itself?
→ Double seesaw

Scale of seesaw

$$M_{\rm R} = -m_{\rm D}^{\rm T} \frac{1}{m_{\rm v}} m_{\rm D}$$

q - 1 similarity: $m_D \sim m_q \sim m_1$ for one third generations $M_R \sim 2 \ 10^{14} \ GeV$

$$M_{R} \sim - \begin{cases} M_{GUT} \sim 10^{16} \text{ GeV} \\ 10^{8} - 10^{14} \text{ GeV} \\ 10^{16} - 10^{17} \text{ GeV} \end{cases}$$

for the heaviest in the presence of mixing $\frac{M_{GUT}^2}{M_{Pl}}$ double seesaw many heavy singlets (RH neutrinos) ...string theory N ~ 10²

also in favor of high scale:

Gauge coupling unification Leptogenesis





Three additional singlets S which couple with RH neutrinos

Can realize scenario with two types of new physics involved



- 1. Complete screening of the Dirac structure
 - $m_D = A M_D$ as a consequence of symmetry $A = v_{EW}/V_{GUT}$

$$d = A I \implies m_v = A^2 M_s$$

Light neutrino mass matrix is determined by the heaviest one M_s

2. Partial screening of the Dirac structure

$$m_D, M_D = diag$$
 $d = diagonal e.g. d = diag(a, 1, 1)$
 $d = U_{23}^{max}$ or U_{ω}

S belong to Hidden sector









singlet of the SM symmetry group, also invisible

Populated by new

fermions – sterile neutrinos, etc scalar bosons – axions, majorons, flavons Gauge bosons – dark photons, etc,

Fill in

The Dark universe

> DM DE BAU

Responsible for Anomalies

LSND/MiniBooNE Reactor Gallum 3.5 keV line? explains Neutrino masses and mixing

It looks like, The Problems are in the Visible sector Solutions - in the Hidden one



SO(10) GUT + hidden sector + flavor symmetries

RH-neutrino

Double seesaw \rightarrow smallness of neutrino mass

Can realize framework $U_{PMNS} = U_{CKM}^+ U_X$

Flavor symmetries at very high scales, above GUT Symmetries in S-sector



Schemes and Symmetries





SO(10) and double seesaw Patrick Lud A.S



In general Υ ~ y (<φ> /Λ)ⁿ

For third generation we take n = 0 i.e. the mass is generated at the renormalizable level

No mixing is generated by F-F at this level Allow to separate CKM and Neutrino new physics



Although mixing is not generated, masses are generated by the F-F term

Information about states with definite masses should be communicated to the Hidden sector



(0, 0), (1,1), (1,0)(1, 1), (0,0), (0,1)(1, 0), (0.1), (0.0) (other assignments lead to the same results)

assignment

Matrix of charges

of F-F couplings

Both distinguishes states and makes couplings diagonal

(1, 0), (0,1), (1,1) with nontrivial charges fixes 3 generations

Scenarios and realizations Patrick Lud A.S.

F-F and F-S couplings are diagonal in the same basis $m_D \sim M_D = diag$ So, essentially we construct M_X Mixing is produced by S-S coupling i.e. in M_S





S as mediators which propagate info from visible to hidden sectors

 $G_{\text{basis}} = Z_2 \times Z_2$ $G_{\text{aux}} = Z_3$ $\omega = e^{i2\pi/3}$ to avoid NR couplings of 1_{H} with 16_{F}

	16 _F	1 ₅	1 _H	10 _H	16 _н
$Z_2 \times Z_2$	(1, 0) (0,1) (0,0)	(1, 0) (0,1) (0,0)	(0,1) (0,0)	(0,0)	(0,0)
Z ₃	ω	ω	ω	ω	ω

the same charges

 $m_{D} = \langle 10_{H} \rangle \operatorname{diag}(Y_{1}, Y_{2}, Y_{3})$ $M_{D} = \langle 16_{H} \rangle \operatorname{diag}(Y'_{1}, Y'_{2}, Y'_{3})$

for third generation renormalizable coupling with , $Y_3 = 1$, $Y'_3 = 1$

Hierarchy of masses due to $Y_1 \leftrightarrow Y_2 \leftrightarrow Y_3$, $Y'_1 \leftrightarrow Y'_2 \leftrightarrow Y'_3$

Due to identical flavor charges of interaction one may expect that $y_i \sim y'_i$ This might be residual of some further unification 16 and 1



Screening matrix: $d = M_D^{-1} m_D = (\langle 10_H \rangle / \langle 16_H \rangle) diag(Y_1/Y_1, Y_2/Y_2, Y_3/Y_3)$

Mixing originates from S-S interactions provided that the scalars 1_H have non-trivial $Z_2 \times Z_2$ charges

Z₂ xZ₂ charges of F-F, F-S and S-S terms

Due to $G_{aux} = Z_3$

With charge assignment (0,1), (0,0) for 1_H (0, 0), (1,1), (1,0)(1, 1), (0,0), (0,1)(1, 0), (0.1), (0.0)

- 1_H do not couple with FxF and FxS
 →only diagonal terms are allowed
- bare mass terms in SxS are forbidden

$$M_{5} = \begin{pmatrix} x & 0 & 0 \\ 0 & x & x \\ 0 & x & x \end{pmatrix}$$

Elements 1-2 and 1-3 can be produced with additional (1,0), (1,1) flavons or due to interactions with other hidden fermions



Putting things together

 $M_X = d^T M_S d$ should be of m_{TBM} form

For all parameters of the same order produces large mixings Enough parameters, further model building is needed

Interesting possibilities: M_{S} has slightly smaller 1-2 and 2-3 elements d = diag(a, 1, 1) a < 1 can produce TBM mass matrix

d = AI
$$M_X = M_S$$

There is an accidental (?) 2-3 permutation symmetry



16_H as mediators

 $G_{\text{basis}} = Z_2 \times Z_2 \times Z_4$

	16 _F	16 _H i	10 _H	1 ₅	1 _H
$Z_2 \times Z_2$	(1, 0) (0,1) (0,0)	(1, 0) (0,1) (0,0)	1	1	1
Z ₄	1	(i, 1, -1)	1	(-i, 1, -1)	(-1, i, -i)
Z ₃	ω	ω	ω	ω	ω

 1_{s} are singlet of $Z_2 \times Z_2$

Additional Z_4 to fix basis and communicate info to the hidden sector Three 16_{H^i} charged with respect to both groups play role of mediators

 $Y_{i} 16_{F^{i}} 16_{F^{i}} 10_{H} + Y_{i}' 16_{F^{i}} 1_{S^{i}} 16_{H^{i}} + h_{ijk} 1_{S^{i}} 1_{S^{j}} 1_{H^{k}}$

 $m_{D} = \langle 10_{H} \rangle diag (Y_{1}, Y_{2}, Y_{3})$

 $M_{D} = diag(Y'_{1} < 16_{H}^{1}), Y'_{2} < 16_{H}^{2}), Y'_{3} < 16_{H}^{3})$



Here more flexibility in construction of M_S

 Z_4 charges of 1_5 (3,0,2) This implies of charges of 16_{H^i} (1,0,2)

The matrix of Z₄ charges of S-S coupling terms

with Z_4 charges of 1_H (2, 1, 3) Produces the mass matrix $\begin{pmatrix} a & c & d \\ ... & 0 & b \\ ... & ... & 0 \end{pmatrix}$

Correspond to quasi-degenerate Spectrum (a = b)

For c ~ d it has approximate 2-3 permutation symmetry which gives maximal 2-3 mixing and zero 1-3 mixing



Another possibility $G_{\text{basis}} = Z_2 \times Z_2 \times Z_7$

The matrix of Z_4 charges of S-S coupling terms

Produces the mass matrix

 Z_7 charges of 1_5 (0, 2, 3) (this implies of charges of 16_{H^i} (0, 5, 4)

$$\begin{pmatrix} 0 & 2 & 3 \\ ... & 4 & 5 \\ ... & ... & 6 \end{pmatrix}$$
$$M_{SS} = \begin{pmatrix} 0 & 0 & 0 \\ ... & a & b \\ ... & ... & c \end{pmatrix}$$

with dominant 2-3 block \rightarrow hierarchical mass spectrum maximal 2-3 mixing and zero 1-3 mixing

Small elements can be generated by additional flavons or higher dimension operators with product of 2 flavons



Three 16_Hⁱ can be substituted

 $16_{H^{i}} \rightarrow 16_{H} (1_{\eta^{i}}/\Lambda)$

16_H and 1_{η}^{i} transform as (- 1, -1) with respect to new connecting group Z_2

All other fields are singlets of this group

<1 $_{\eta}^{i}$ > ~ M_{GUT} < 16_H > ~ Λ ~ M_{PI}

To avoid large effects of higher dimension operators

SO(10) is broken near M_{PI}

CKM physics 105

- hierarchy of Yuakawas Y_i, Y'_i
 CKM mixing
 difference of masses of upper and down quarks
 - difference of masses of down guarks and charged leptons

Related to breaking of S(10)

Framework allows to disentangle the CKM physics and neutrino physics

Hierarchy of masses

due to hierarchy of couplings: $Y_1 \leftrightarrow Y_2 \leftrightarrow Y_3$, $Y'_1 \leftrightarrow Y'_2 \leftrightarrow Y'_3$

 \rightarrow in turn, due to operators of different order:

3rd generation renormalizable coupling with , $Y_3 = 1$, $Y'_3 = 1$

2nd generation:

1st generation: $y \sim y (\langle \phi \rangle / \Lambda)^2$



new flavon Scheme with 16_Hⁱ mediator all other fields are singlets $16_{\rm F}^{\rm i}$ 16_Hⁱ $1_{\rm y}$ powers of $e^{i2\pi/5}$ Z_5 (1, 3, 0)(1, 3, 0) 4 $Y_1 = y_1 (< 1_y > / \Lambda)^2$ produces geometric hierarchy of masses of the upper component $y_2 = y_2 (< 1_y > / \Lambda)$ $Y_3 = y_3$

Scheme with 1_sⁱ mediator

without non-renormalizable terms

	16 _F	1 _F i	1 _y	1 _H (0, 1)	1 _H (0, 0)	1 _H (0, 0)
Z ₅	(1, 3, 0)	(1, 3, 0)	4	2	4	0

allows to get dominant 2-3 block in M_s but now CKM and Nu physics are entangled

 $Z_2 \times Z_2$

One or more additional 10_H

CKM Mixing

Different 10_H give masses for upper and down fermion components (ensures different mass hierarchies)

CKM mixing originates from the down sector: 10_{H}^{d} interactions

additional G'_{aux}= Z'₂ can be introduced to distinguish them

additional higgs singlets 1_{ξ^i} with $Z'_2 = -1$

With of $Z_2 \times Z_2$ charge assignment (0,0), (0,1), (0,1) for 1_{ξ^i} : Alternatively - several 10_H^d with $Z_2 \times Z_2$ charges

$$10_{H^{u}} \quad \text{with } v_{d} = 0 + 10_{H^{d}} \quad \text{with } v_{u} = 0 - 10_{H^{d}} + 10_{H^{d}} +$$

Z

$$10_{H^d} \rightarrow 10_{H^d} (1_{\xi^i}/\Lambda)$$



Non-abelian discrete symmetries

Approximate non-abelian symmetries from interactions with many singlets and decoupling of heavy degrees of freedom

 $S_2 - S_3$ permutation symmetry gives equality of 12- and 13elements as well as 22- and 33- elements of the matrix M_{SS} This permutation $G_{perm} = Z_2$ is not consistent with basis symmetry $Z_2 \times Z_2$ since S_2 and S_3 have different $Z_2 \times Z_2$ charges.

The violation is explicit in F-S interactions However , these interactions are at GUT energies, and therefore their effect on M_{SS} is very small

One can consider semi-direct product of G_{perm} and $G_{basis} = Z_2$ and embed them in a single non-abelian group. This group can be spontaneously broken in the F-S sector, which however requires substantial complication of the model.







DeepCore





Hopeless?

Nothing should be observed at LHC which is responsible for neutrino masses If something is observed against (excludes) framework Special value of CP-phases Light sterile neutrinos Dark mater Inflation Leptogenesis



Implications

If the phase δ_{CP} deviates substantially from 0 or π , new sources of CPV beyond CKM

New sources may have specific symmetries which lead to particular values of δ_{CP} e.g. $-\pi$ /2



neglecting terms of the order ~ λ^3

 $\sin \delta_{CP} = s_{13}^{-1} \left[\sin(\alpha_{\mu} + \delta_{X}) V_{ud} | X_{e3} | - \sin \alpha_{e} | V_{cd} | X_{\mu 3} \right]$

here α_{μ} , δ_{X} and α_{e} are $% \beta_{\mu}$ parameters of U_{X}

Some special values of δ_{CP} can be obtained under certain assumptions

- if $X_{e3} = 0$ we have $\sin \delta_{CP} \sim -\sin \alpha_e$
- if $\alpha_e = \pi / 2$ $\delta_{CP} \sim 3\pi / 2$

One can find structure of the RH sector which lead to these conditions



WDN from Hidden sector



The blue point: the best-fit value from M31 (Andromeda galaxy). Thick error bars are $\pm 1\sigma$ limits on the flux. Thin error bars correspond to the uncertainty in the DM distribution in the center of M31.

A Boyarsky et al, 1402.4119



 $\delta m \sim \theta_{aS}^2 m \sim (1 - 2) \, 10^{-7} \, eV$

- below any relevant scale in the neutrino mass matrix $\sim 10^{-3} \mbox{ eV}$

 \rightarrow does not participate in neutrino mass generation

 \rightarrow is not RH, but some singlet from HS beside 3 v_R

 \rightarrow high mass scales are involved



$$\begin{split} & \mathcal{M} \sim \mathcal{M}_{GUT} \sim 10^{16} \text{ GeV} \\ & m_D \sim m \sim 10^2 \text{ GeV} \\ & m_{aS} \sim m m_D / \mathcal{M} \quad \sim 10^{-3} \text{ eV} \quad \text{Required mixing parameter} \end{split}$$

meV sterile neutrino

 $m_0 \sim 0.003 \text{ eV}$



For solar nu: $\sin^2 2\alpha \sim 10^{-3}$

For dark radiation



Motivated by

Solar neutrino data - absence of upturn of spectrum - additional radiation in the Universe if mixed in v_3 no problem with LSS bound on neutrino mass **Origins**: M^2 m_0 M ~ 2 - 3 TeV $\alpha, \beta \sim v / M$ In the Hidden sector?





Data support relation between I- and q- mixings $U_{PMNS} = V_{CKM}^+ U_X$ Smallness of neutrino mass due to GUT-Planck scale physics still appealing possibility

This implies unification of quarks and leptons and existence of new sector of theory which is responsible for smallness of neutrino mass and striking difference of mixing patterns. This sector may have certain symmetries

> The framework which allow to realise such a possibility considered and its properties are explored

The main elements of the framework:

- SO(10) type of Grand Unification,
- existence of the Hidden (singlet sector)
- Double (multiple) see-saw mechanism
- complete or partial screening on the Dirac structures
- existence of symmetries which ensure communication between hidden and visible sectors

- additional symmetries in the hidden sector

Hidden sector may contain many fermions and bosons which have their own symmetries as well as "basis fixing symmetry" which communicate information from hidden to visible sector in certain way. Basis fixing symmetry select only some components of the Hidden sector which immediately couple with visible one.

Certain features can appear due to involvement of many Components in hidden sector. Basis symmetry select only some of them

The framework allows to disentangle physics responsible for CKM and the one -- for special neutrino properties

Other manifestations of the Hidden sector can be

- sterile neutrinos
- certain values of CP phases
- dark matter

It can be related to leptogenesis , inflation, etc.