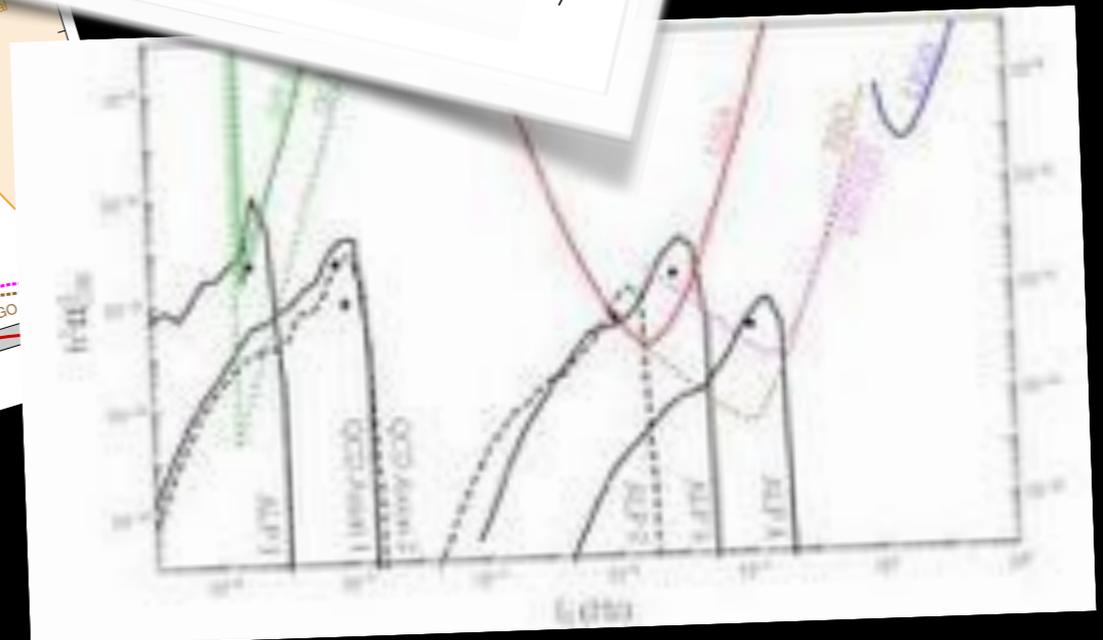
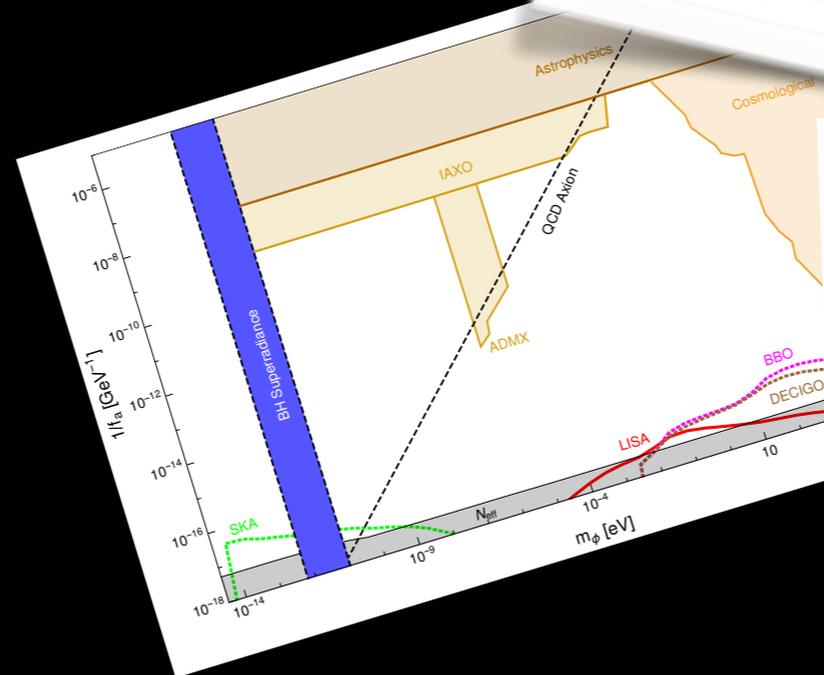
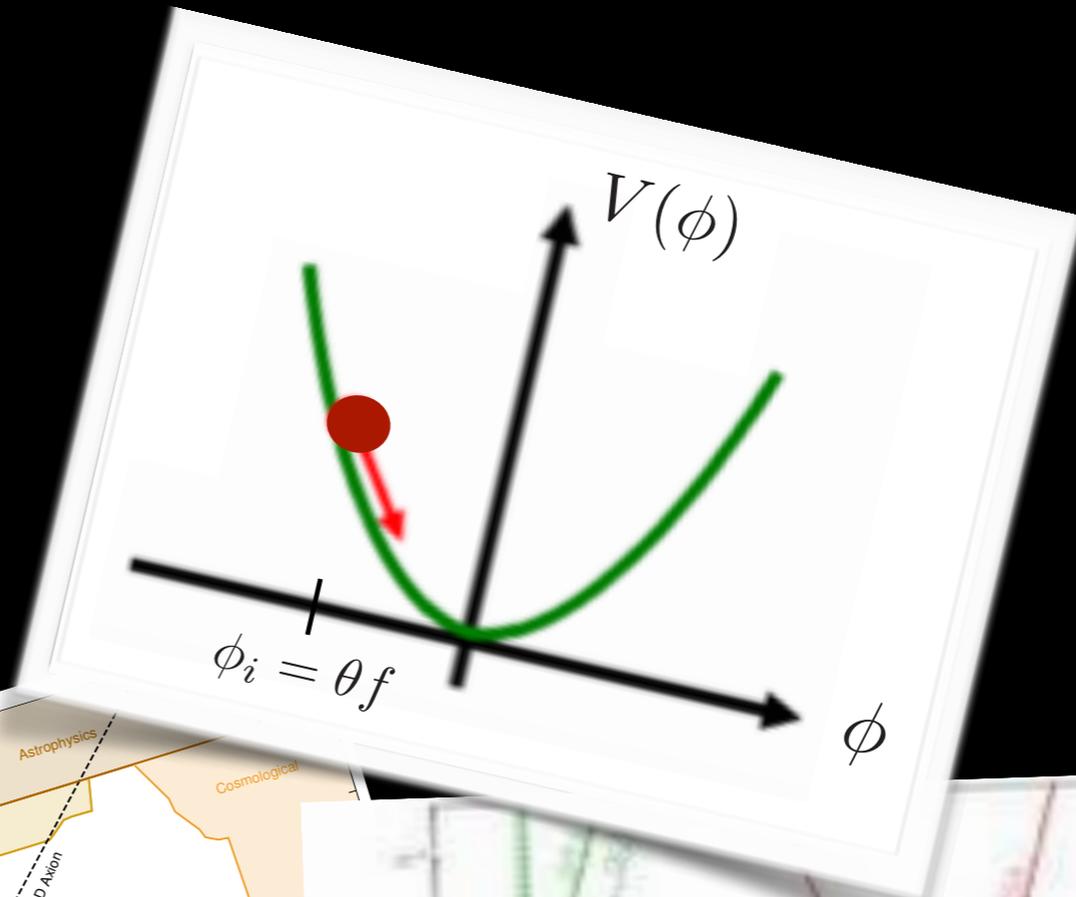


Audible Axions

Particle & Astroparticle Theory
Seminar

MPIK Heidelberg
November 25, 2019

Pedro Schwaller
(JGU Mainz)



- The early Universe and new physics
- Gravitational waves as windows into the early Universe
- Axions, strong CP problem, and dark matter
- Probing axions with GWs

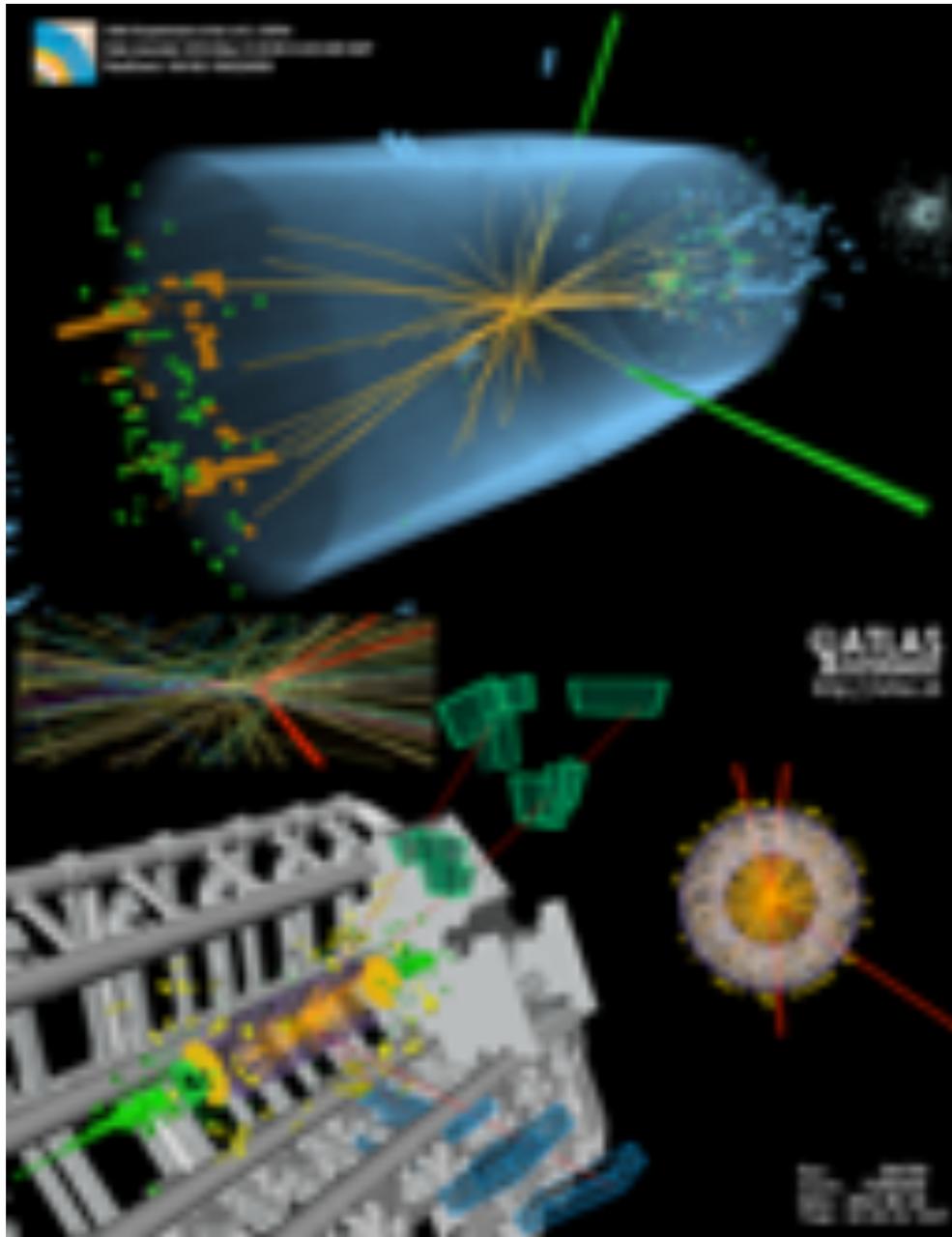
The Standard Model (of particle physics)

Matter



Forces

Discovery 2012 by ATLAS & CMS



The Nobel Prize in Physics 2013



Photo: A. Mahmoud
François Englert
Prize share: 1/2



Photo: A. Mahmoud
Peter W. Higgs
Prize share: 1/2

"for the **theoretical discovery of a mechanism that contributes to our understanding of the origin of mass of subatomic particles**, and which recently was **confirmed through the discovery** of the predicted fundamental particle, by the ATLAS and CMS experiments at CERN's Large Hadron Collider"

- Curiosity!
 - Is there something else?

- Origin of Matter
- Nature of Dark Matter

Can not be explained within SM

Requires new Physics!!!

- Quark and Lepton Flavour puzzles
- Strong CP problem

Parameterised but not explained in SM

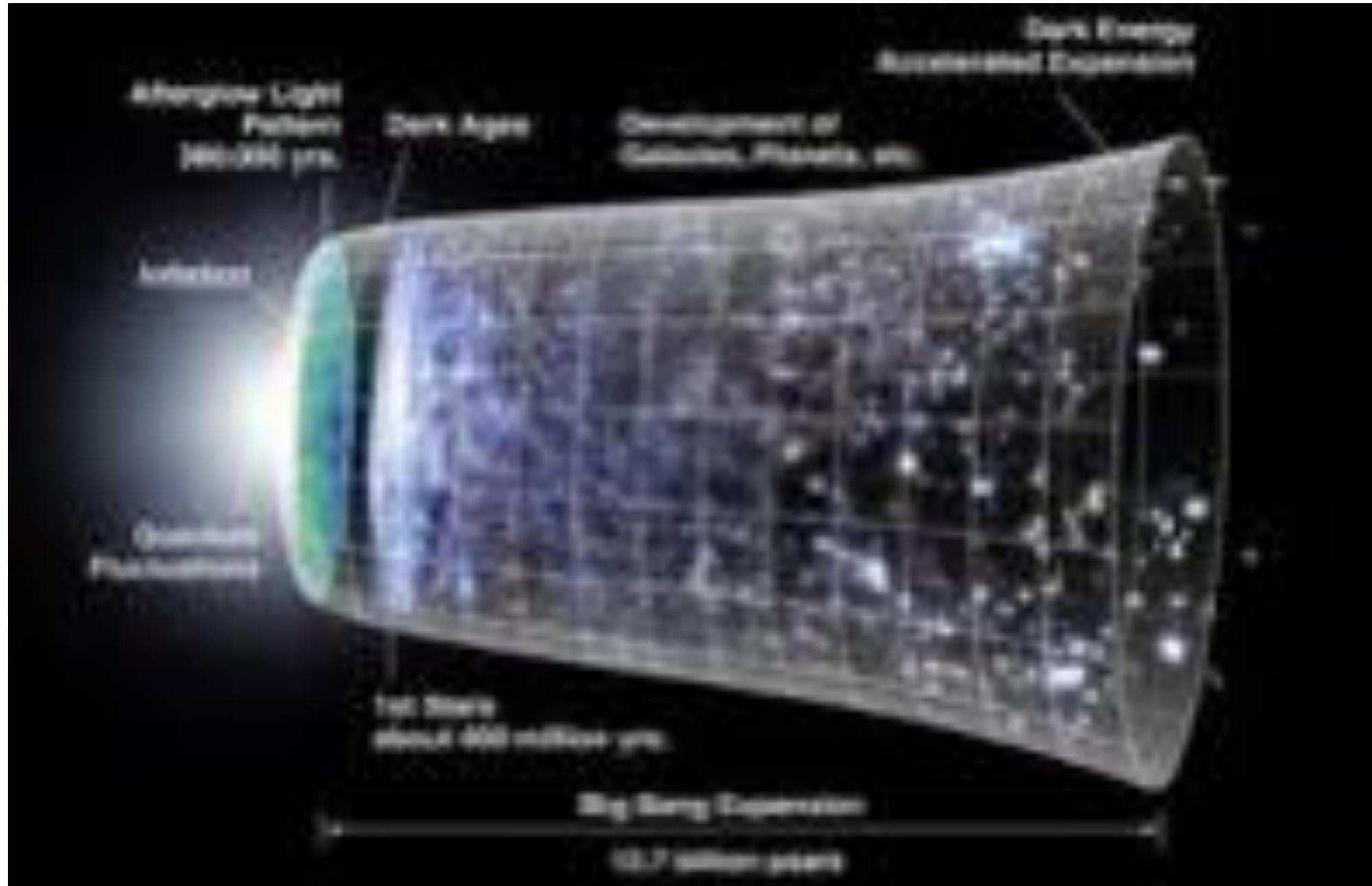
Hints for new Physics

- Inflation, Dark Energy, Reheating...

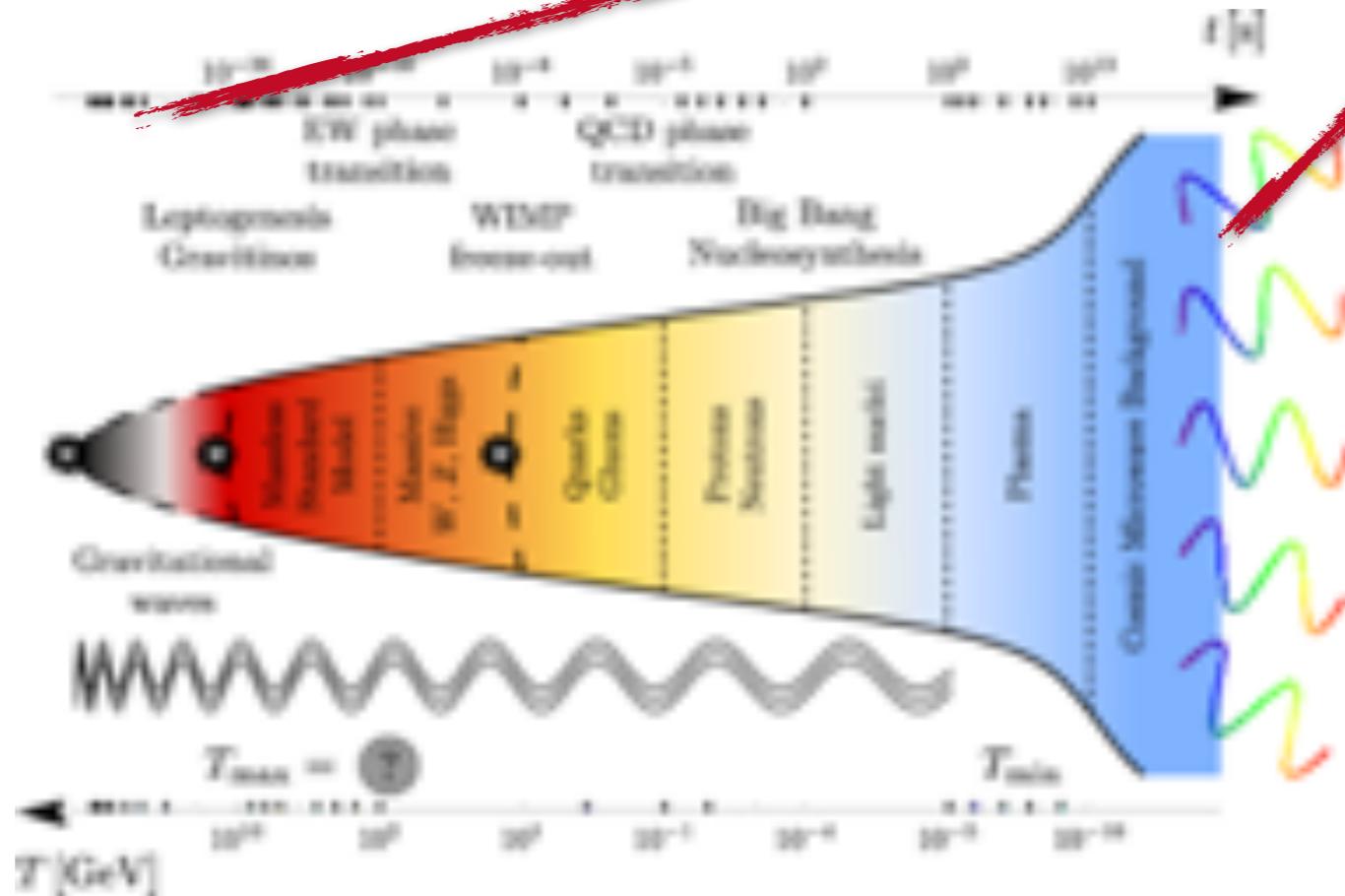
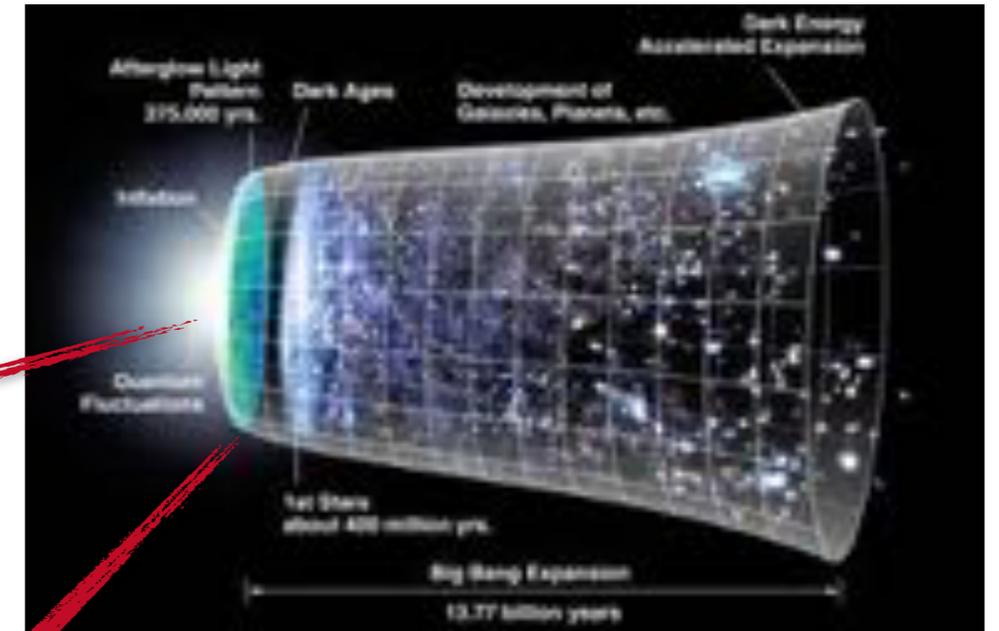
- Curiosity!
 - Is there something else?
- Origin of Matter
- Nature of Dark Matter
- Quark and Lepton Flavour puzzles ?
- Strong CP problem
- Inflation, Dark Energy, Reheating...

Connected with
Cosmology/early
Universe

What do we know about
the early Universe?



- First direct observation in 2016
- New window into early universe



- e.g.
- Electroweak symmetry breaking
 - Baryogenesis
 - Dark matter production

Physics Highlight 2016



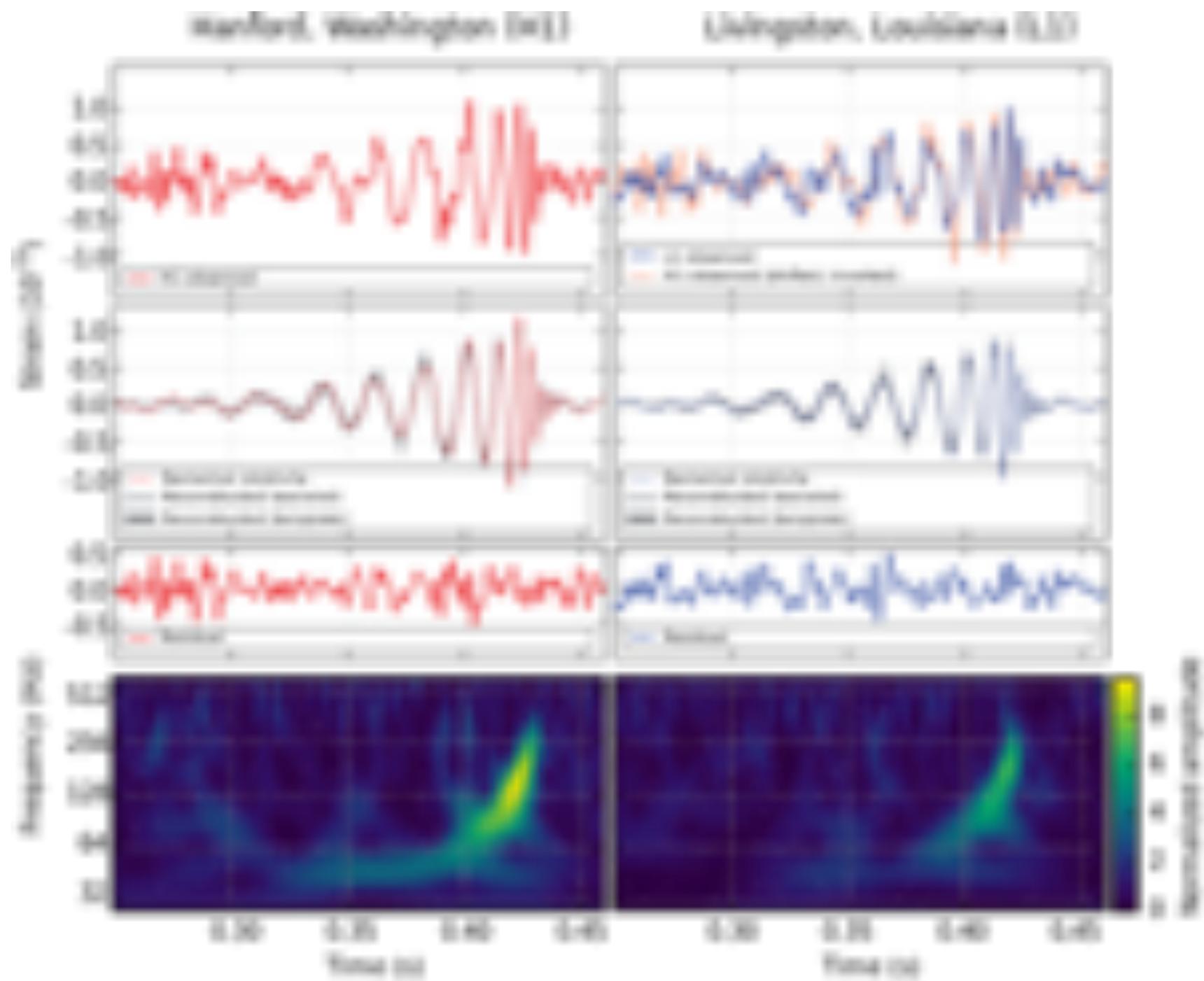
LIGO



Hanford, Washington, USA

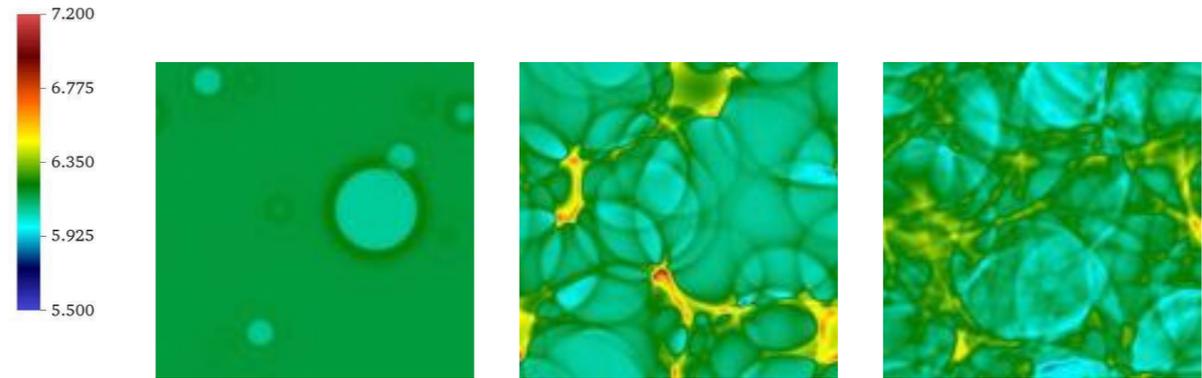


Signal



- CMB encodes information about the state of the universe at the time of its emission
 - Densities of matter, radiation, dark matter
 - Fluctuations (seeds for galaxy formation)
 - Hubble rate (interesting discrepancy!)
- GWs could do the same
 - For earlier (and different) times
 - Need a strong source (CMB photons are just there!)

- First order phase transitions (symmetry breaking)

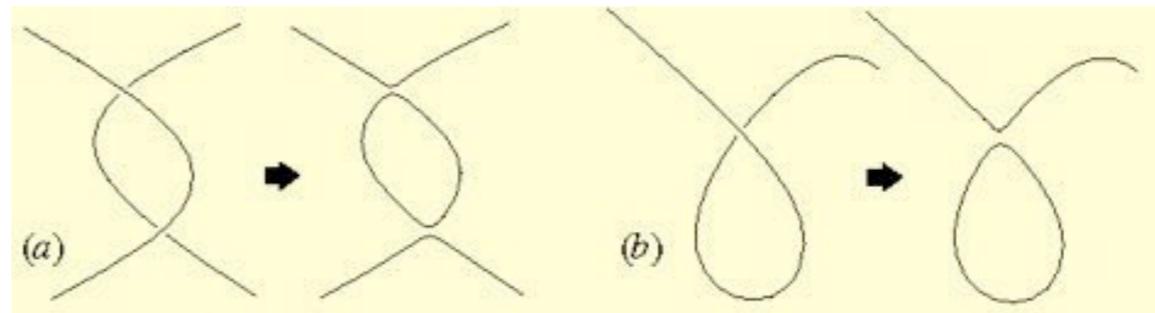
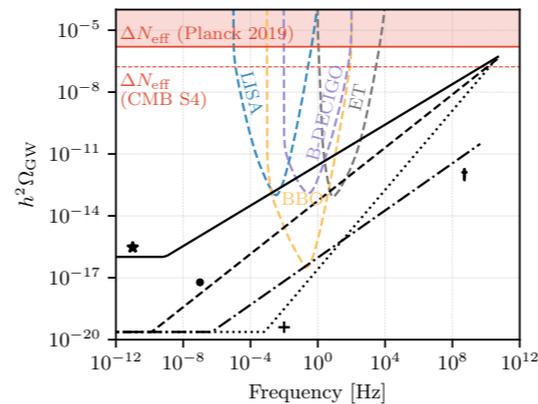


from Hindmarsh et al

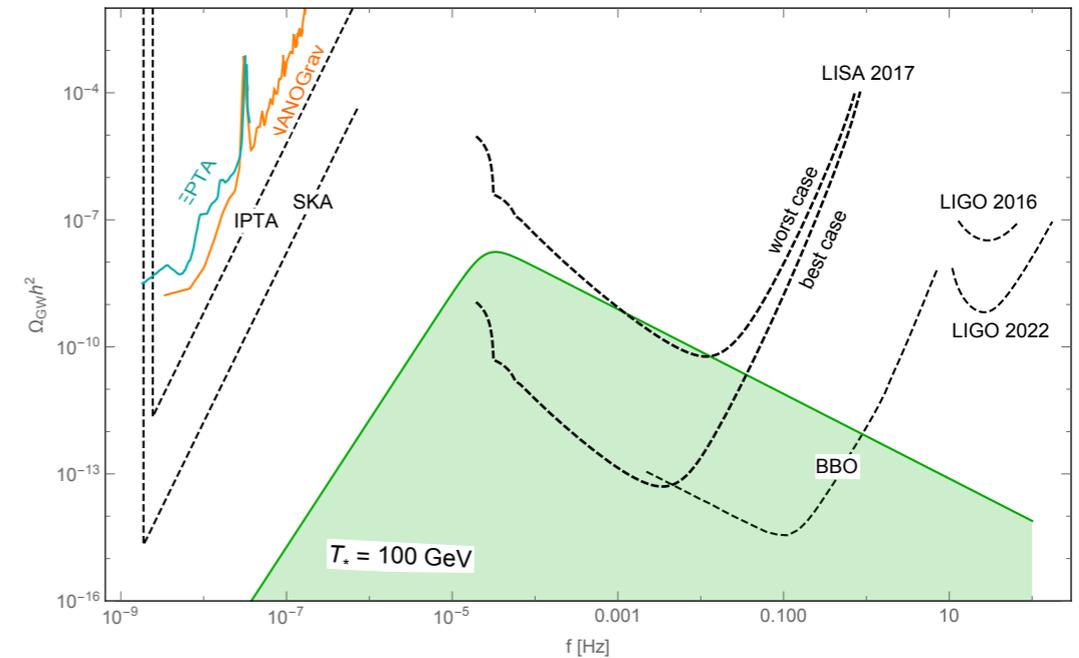
- Inflation/Reheating

- Cosmic strings

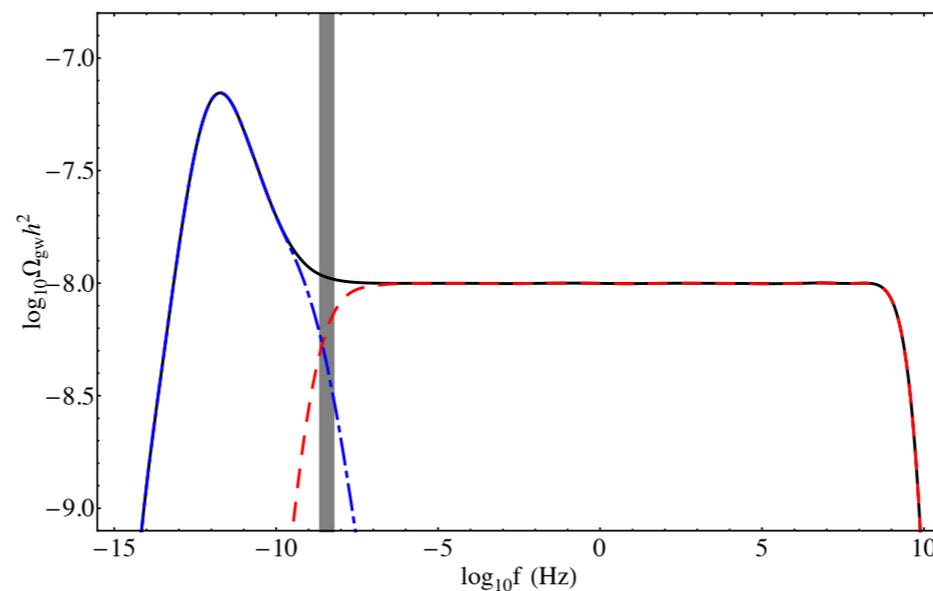
- and now... Axions!



- Characteristic for source, e.g.
- Phase transition, peak location depends on T_{nuc}

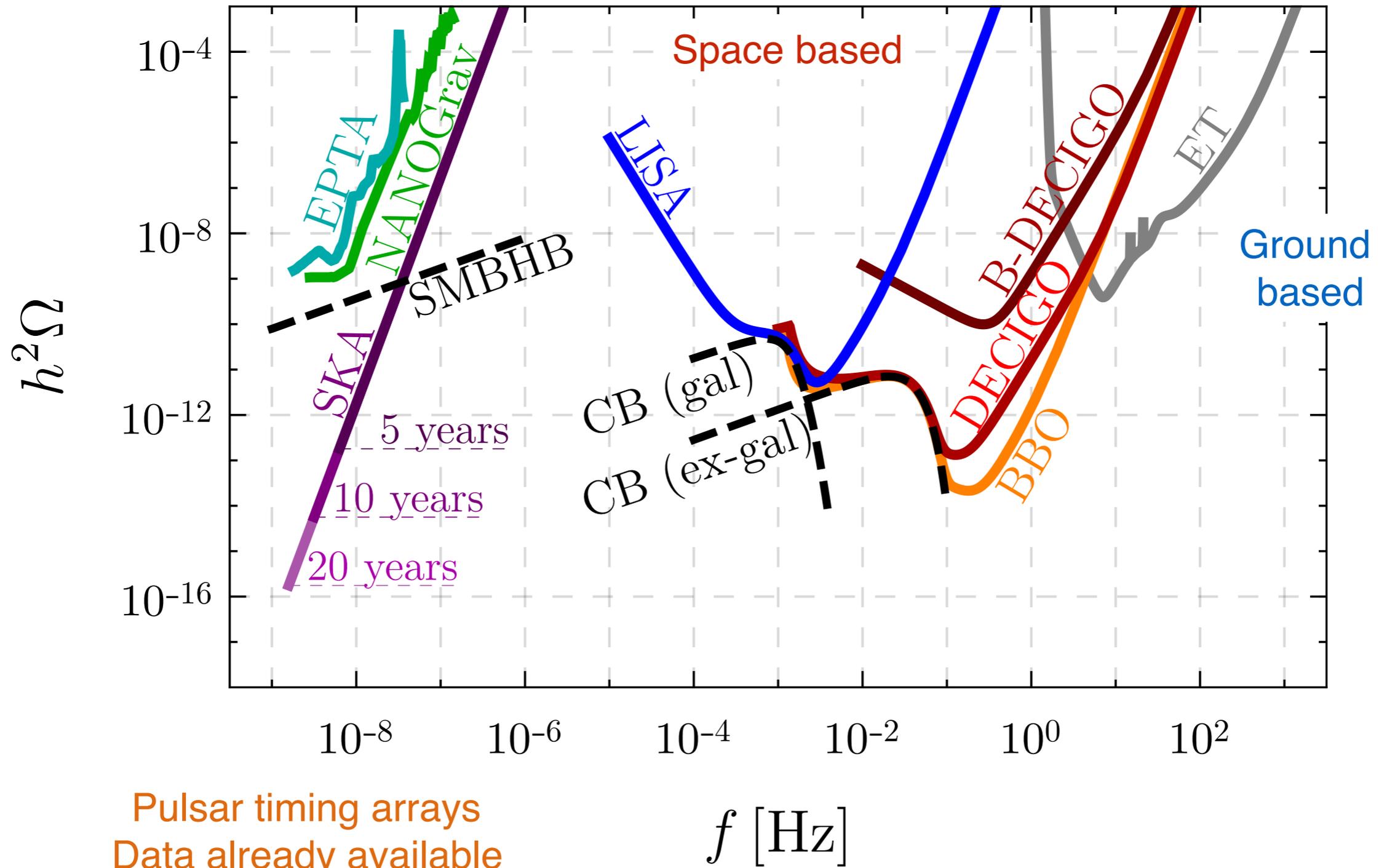


- Cosmic strings



Sanidas,
Battye,
Stappers,
2012

Frequency ranges



Pulsar timing arrays
Data already available

Axions?

- Strong CP problem

$$\mathcal{L}_{\text{QCD}} \supset \theta \frac{g_s^2}{32\pi^2} G\tilde{G}$$

with $\theta \sim 1$

- Neutron EDM: $|d_n| \lesssim 10^{-26} \text{ e cm} \implies \theta < 10^{-10}$

- Axion is dynamical solution

$$\mathcal{L}_{\text{QCD}} \supset \left(\theta + \frac{a}{f_a} \right) \frac{g_s^2}{32\pi^2} G\tilde{G}$$

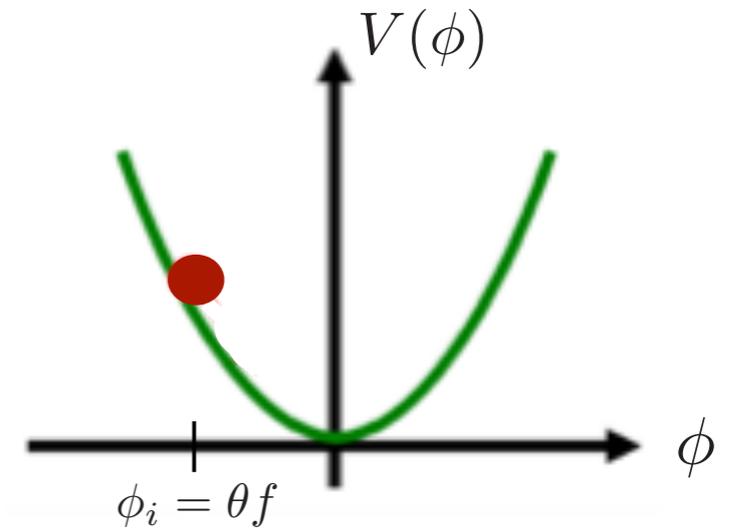
- Ground state has $\theta \sim 0$

symmetry breaking scale,
suppresses couplings to SM

- Axion EOM

$$\phi'' + 2aH\phi' + a^2 m_\phi^2 \phi = 0$$

- Starts rolling when $H \sim m_\phi$

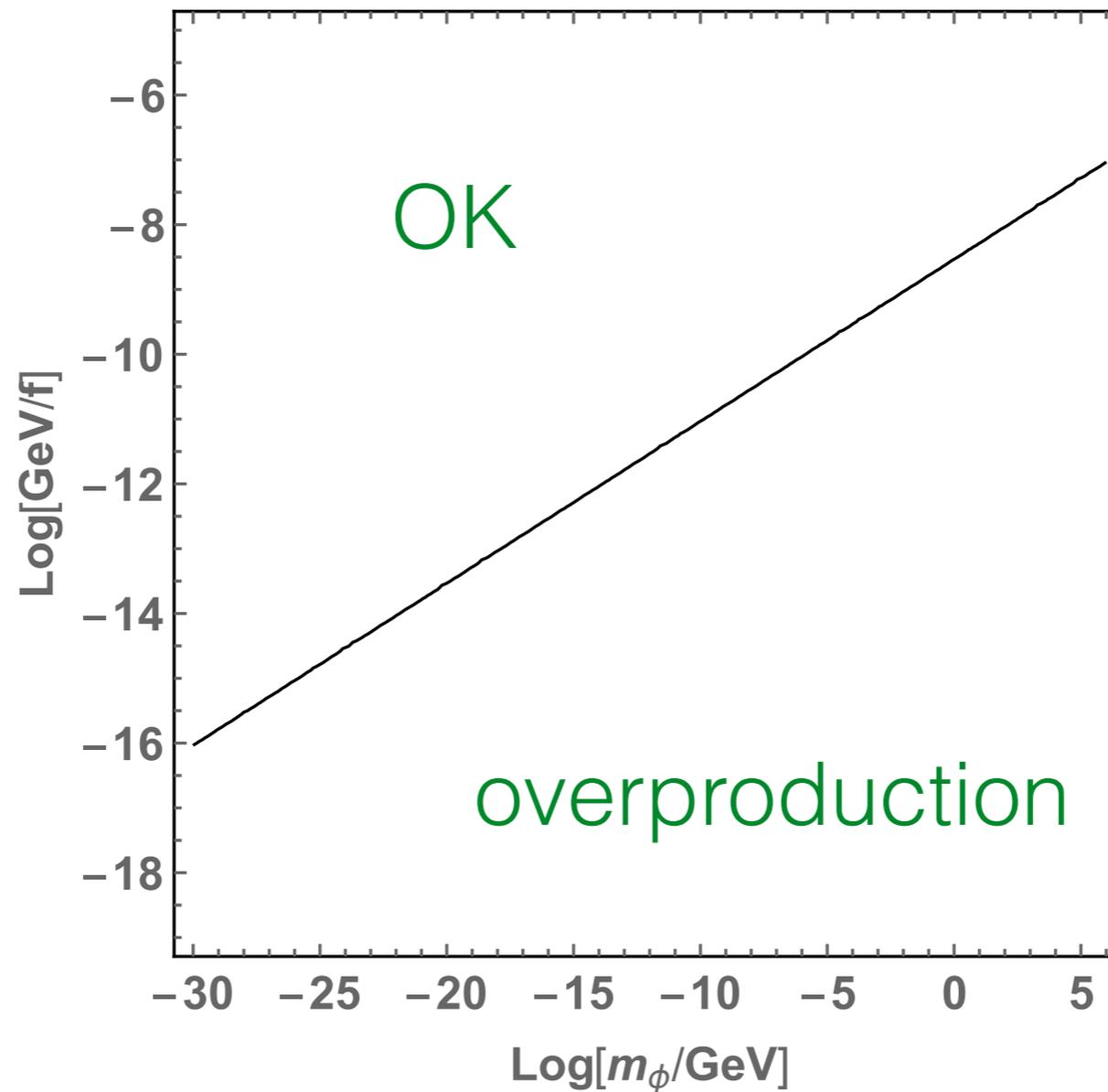


- Redshifts with a^{-3} , i.e. like non-relativistic matter

- Candidate for non-particle dark matter

- Energy density $\rho_\phi = \frac{1}{2} m_\phi^2 \theta^2 f^2$
- Hubble $m_\phi \sim H_{\text{osc}} \sim \frac{T_{\text{osc}}^2}{M_P}$
- Energy fraction $\frac{\rho_\phi}{\rho_{\text{rad}}} \sim \frac{m_\phi^2 \theta^2 f^2}{T_{\text{osc}}^4} \sim \frac{\theta^2 f^2}{M_P^2}$
- Increases due to redshift $\frac{a_{\text{osc}}}{a_{\text{eq}}} \sim \frac{\sqrt{m_\phi M_P}}{\text{eV}}$

$$\Omega_{\text{today}} \sim \theta^2 f^2 \frac{m_\phi^{1/2}}{M_P^{3/2} \text{eV}} \quad \Omega_{\text{observed}} \approx 0.12$$



- We consider the following effective field theory consisting of an axion-like particle (ALP) ϕ and a massless dark photon X_μ

$$\mathcal{S} = \int d^4x \sqrt{-g} \left[\frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) - \frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{\alpha}{4f} \phi X_{\mu\nu} \tilde{X}^{\mu\nu} \right]$$

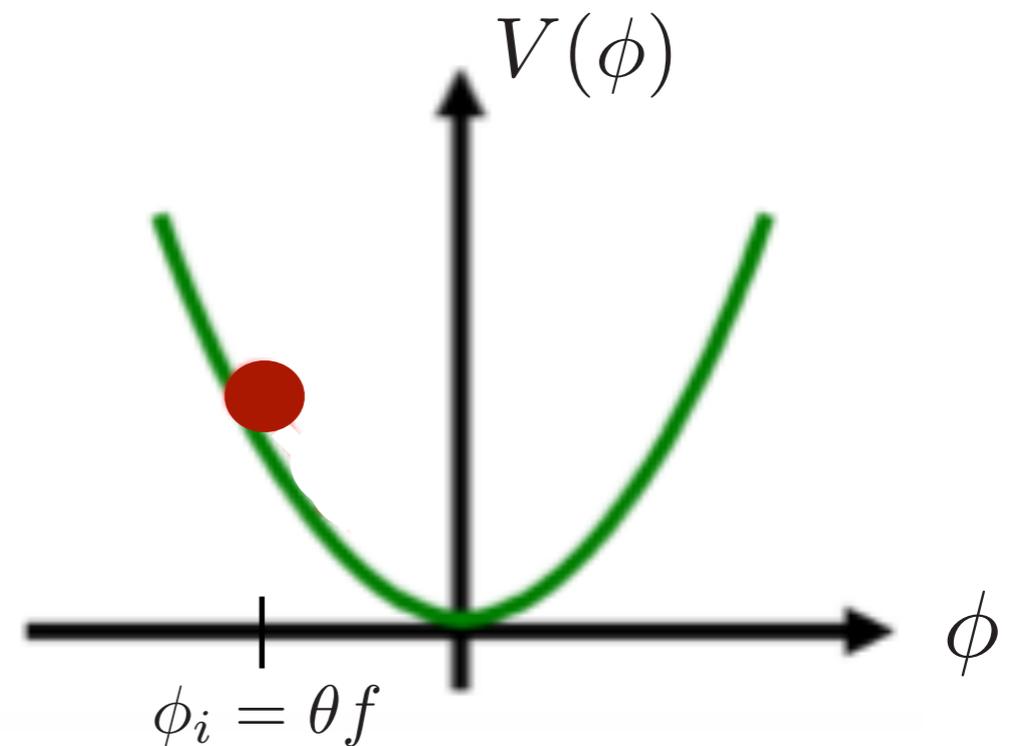
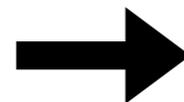
- We assume some explicit breaking of the global symmetry at the scale $\Lambda = \sqrt{mf}$, which generates a mass for the ALP

$$V(\phi) = m^2 f^2 \left[1 - \cos \left(\frac{\phi}{f} \right) \right]$$

$$\phi_i = \theta f, \quad \phi'_i \approx 0, \quad \theta \sim \mathcal{O}(1)$$

- Since the ALP has no reason to be near the minimum of the potential when it tilts, we generically expect initial conditions of the form

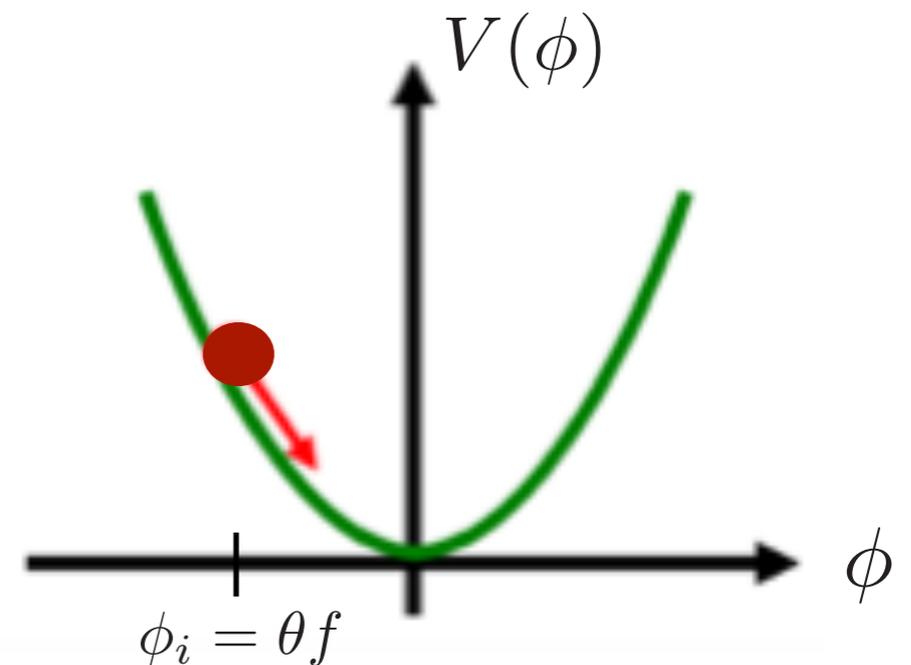
$$\phi_i = \theta f, \quad \phi'_i \approx 0, \quad \theta \sim \mathcal{O}(1)$$



- The ALP begins to oscillate when the Hubble rate drops below the ALP mass

$$H_{\text{osc}} \sim m, \quad \rho_{\phi}^{\text{osc}} \sim \frac{1}{2} m^2 \phi_i^2$$

$$\Omega_{\phi}^{\text{osc}} = \frac{\rho_{\phi}^{\text{osc}}}{\rho_{\text{tot}}^{\text{osc}}} \approx \frac{m^2 \theta^2 f^2 / 2}{3 M_P^2 H_{\text{osc}}^2} \approx \left(\frac{\theta f}{M_P} \right)^2$$



- Dark Photon EOM

$$\left(\frac{\partial^2}{\partial \tau^2} - \nabla^2 \right) \vec{X} = \alpha \frac{\phi'}{f} \vec{\nabla} \times \vec{X}, \quad \vec{\nabla} \cdot \vec{X} = 0.$$

Source for dark photons
(while ALP rolls)

We quantize the dark photon field as Circular pols. ($\mathbf{k} \times \boldsymbol{\varepsilon}_{\pm} = \mp ik \boldsymbol{\varepsilon}_{\pm}$)

$$\hat{X}^i(\mathbf{x}, \tau) = \sum_{\lambda=\pm} \int \frac{d^3k}{(2\pi)^3} v_{\lambda}(k, \tau) \boldsymbol{\varepsilon}_{\lambda}^i(\mathbf{k}) \hat{a}_{\lambda}(\mathbf{k}) e^{i\mathbf{k}\cdot\mathbf{x}} + \text{h.c.}$$

which leads to the following equation for the mode functions

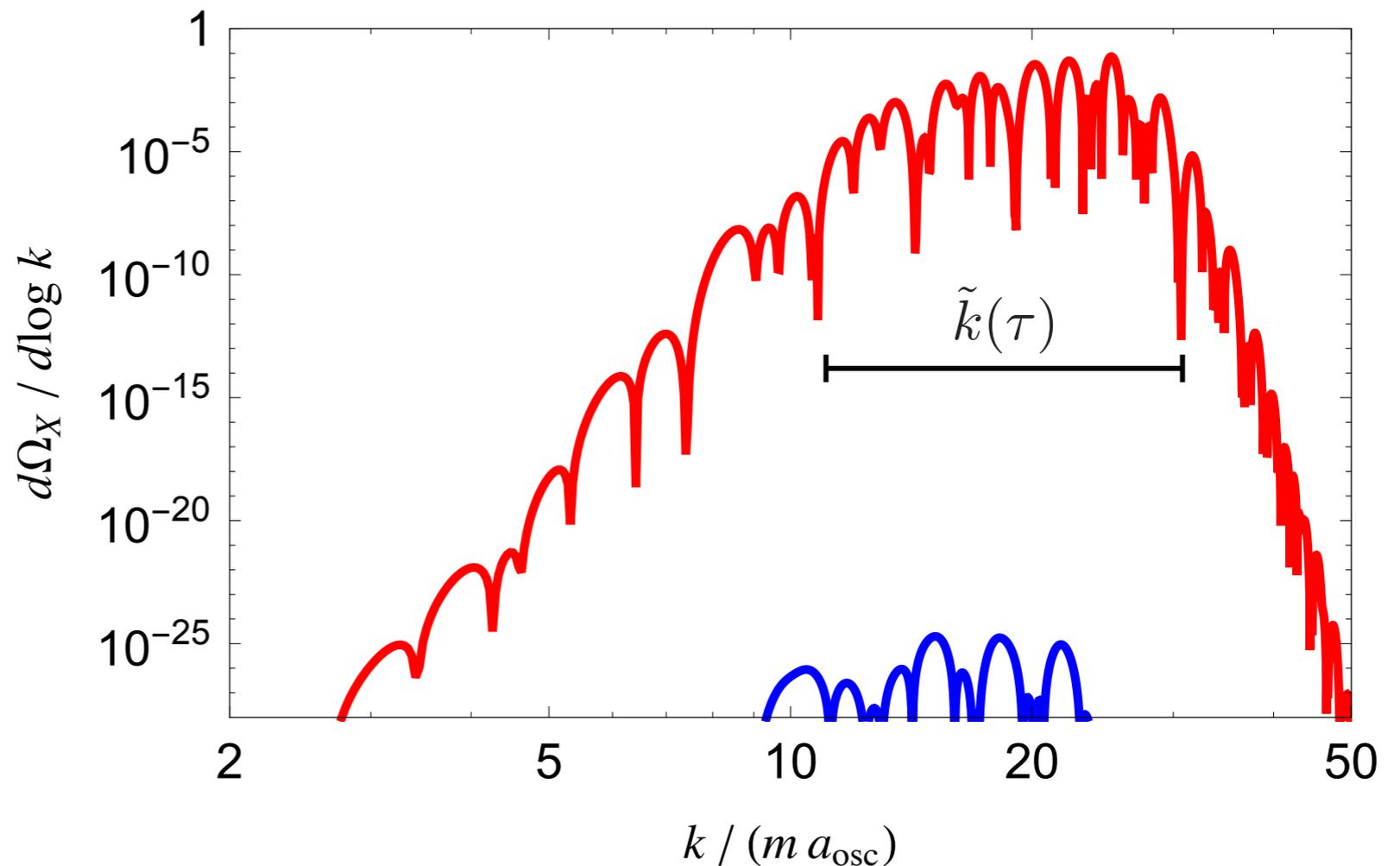
$$v_{\pm}'' + \omega_{\pm}^2(\tau) v_{\pm} = 0, \quad \omega_{\pm}^2(\tau) = k^2 \mp k \frac{\alpha}{f} \phi'$$

As the ALP rolls, there exist momenta for which ω_{\pm}^2 is negative. The corresponding modes are tachyonic and grow exponentially:

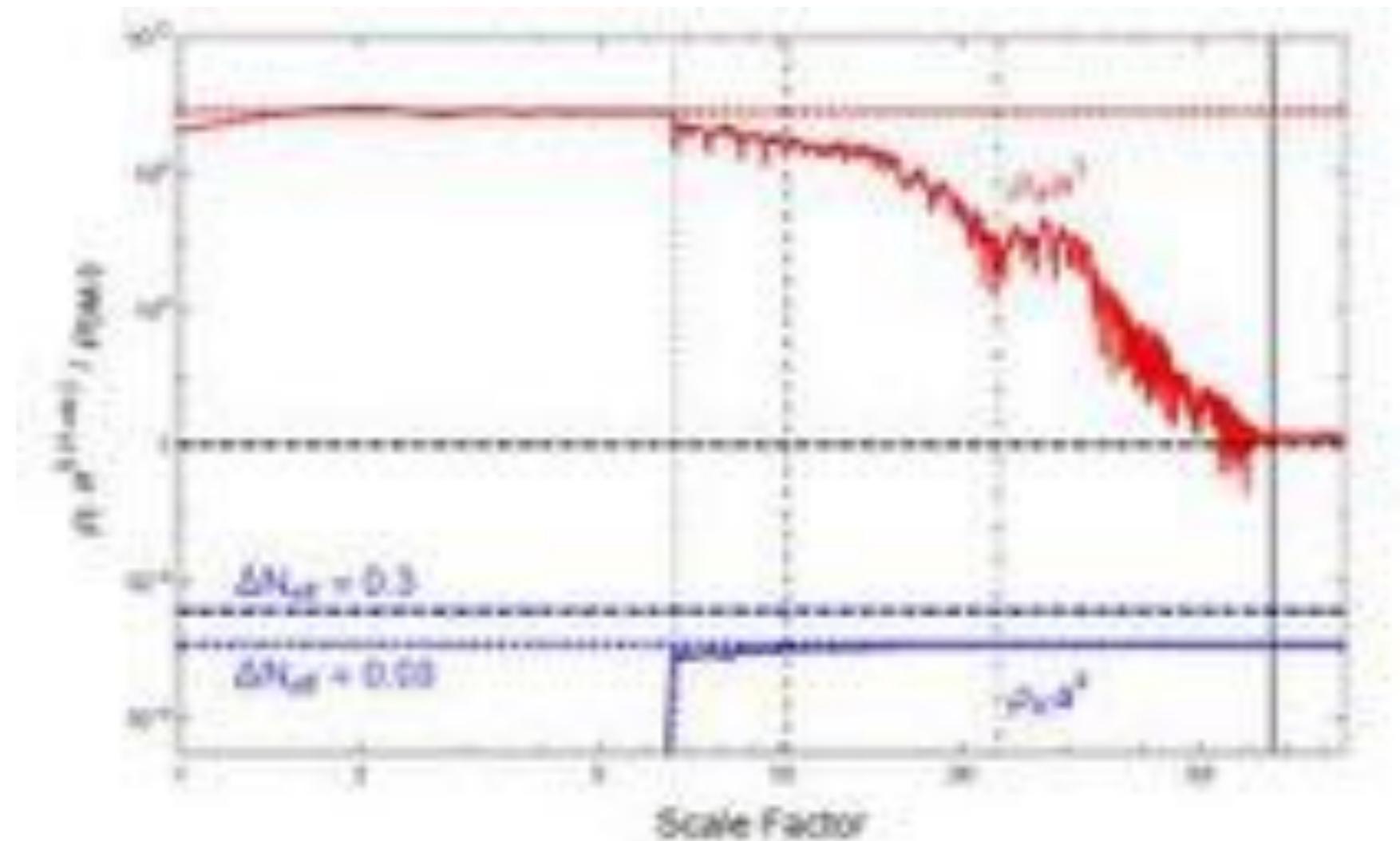
$$v_{\pm}(k, \tau) \sim e^{|\omega_{\pm}|\tau}$$

- Initial condition violates parity (field rolls to the left or to the right)
- One dark photon helicity dominates
- A certain range of modes undergoes tachyonic growth

$$0 < k < \frac{\alpha\phi'}{f}, \quad \frac{k}{m} \lesssim \alpha\theta$$



- Tachyonic dark photon production
- + parametric resonance
- efficient energy transfer away from axion
- N_{eff} constraint on dark photon abundance



Dark photon modes in the range $0 < k < \theta \alpha m$ which were initially in vacuum grow exponentially when the axion begins to oscillate

$$v_{\pm}(k, \tau \ll \tau_{\text{osc}}) = \frac{1}{\sqrt{2k}} e^{-ik\tau} \quad \xrightarrow{\omega_{\pm}^2 < 0} \quad v_{\pm}(k, \tau) \sim e^{|\omega_{\pm}|\tau}$$

These rapidly growing modes amplify quantum fluctuations of the dark photon into a time-varying, anisotropic classical energy distribution which sources gravitational waves

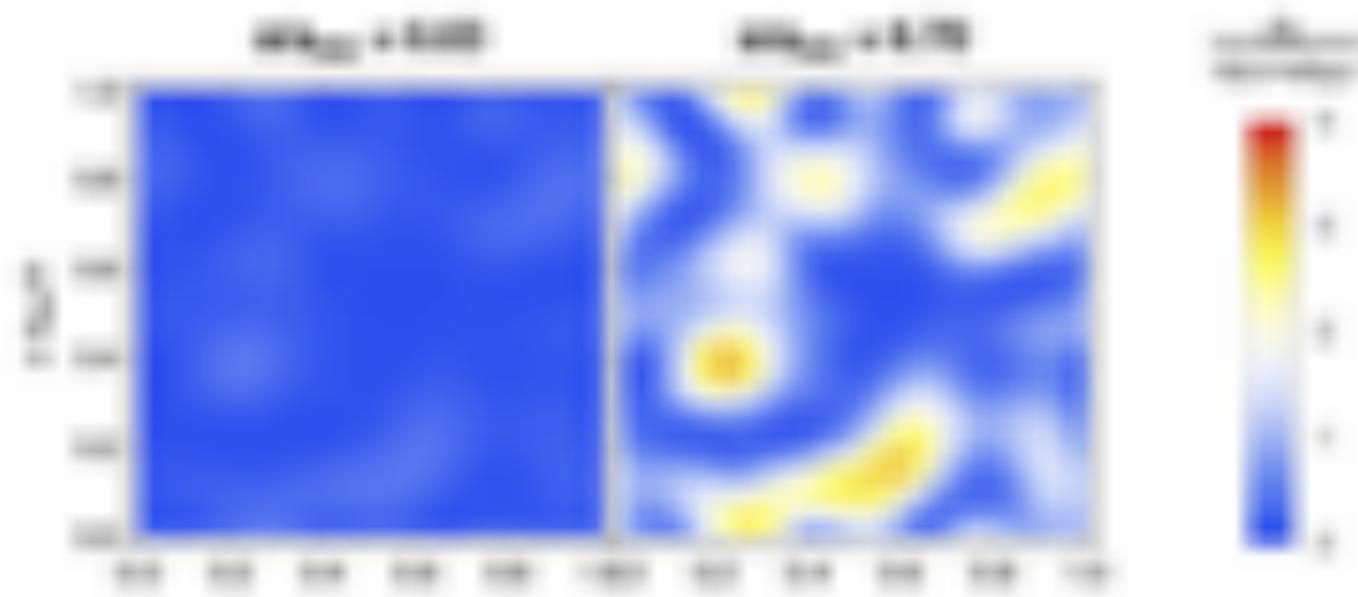
Gravity Waves

$$h''_{ij}(\mathbf{k}, \tau) + k^2 h_{ij}(\mathbf{k}, \tau) = \frac{2}{M_P^2} \Pi_{ij}(\mathbf{k}, \tau),$$

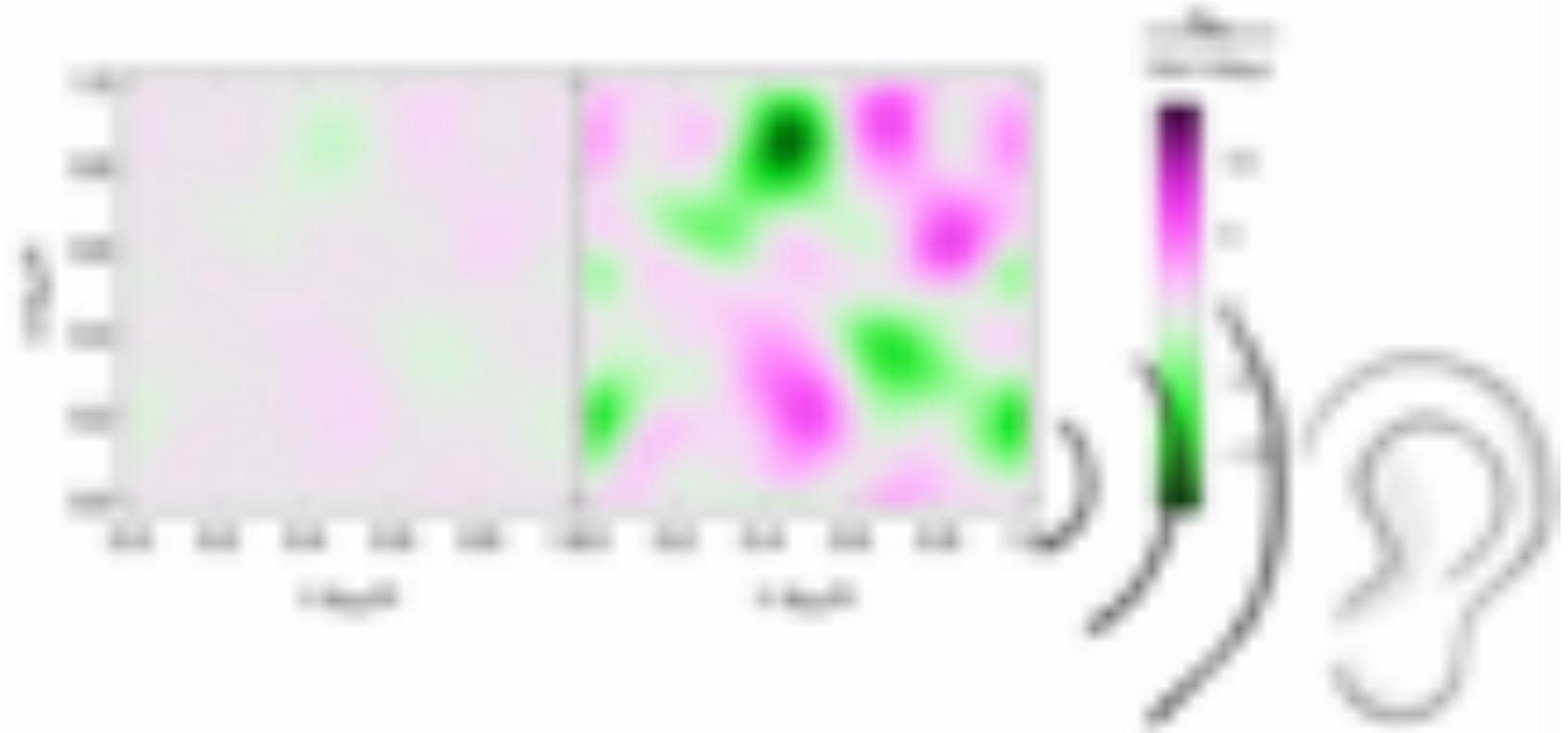
Anisotropic stress

$$\hat{\Pi}_{ij}(\mathbf{k}, \tau) = \frac{\Lambda_{ij}^{kl}}{a^2} \int \frac{d^3q}{(2\pi)^3} \left[\hat{E}_k(\mathbf{q}, \tau) \hat{E}_l(\mathbf{k} - \mathbf{q}, \tau) + \hat{B}_k(\mathbf{q}, \tau) \hat{B}_l(\mathbf{k} - \mathbf{q}, \tau) \right].$$

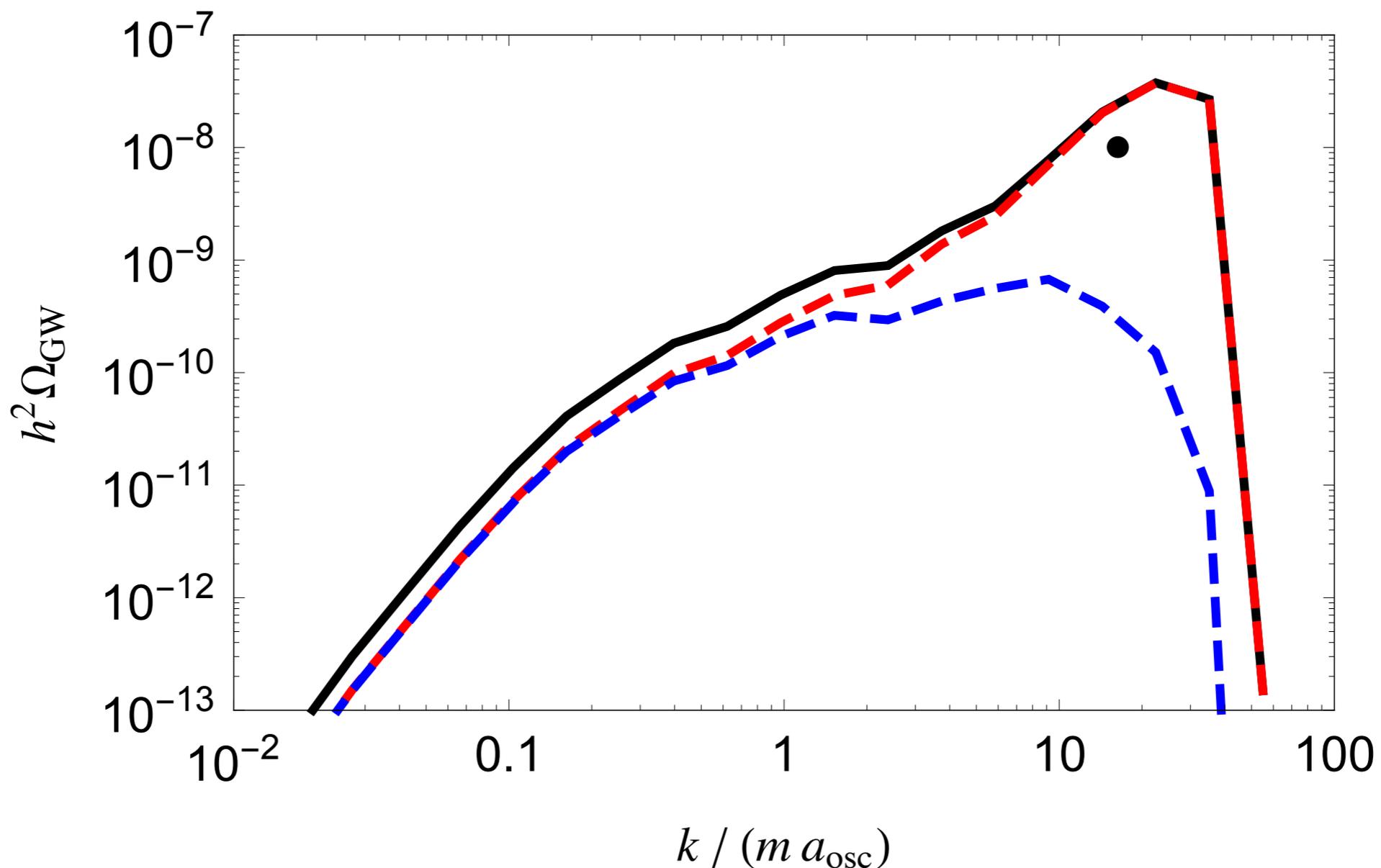
Energy Density of Dark Photon

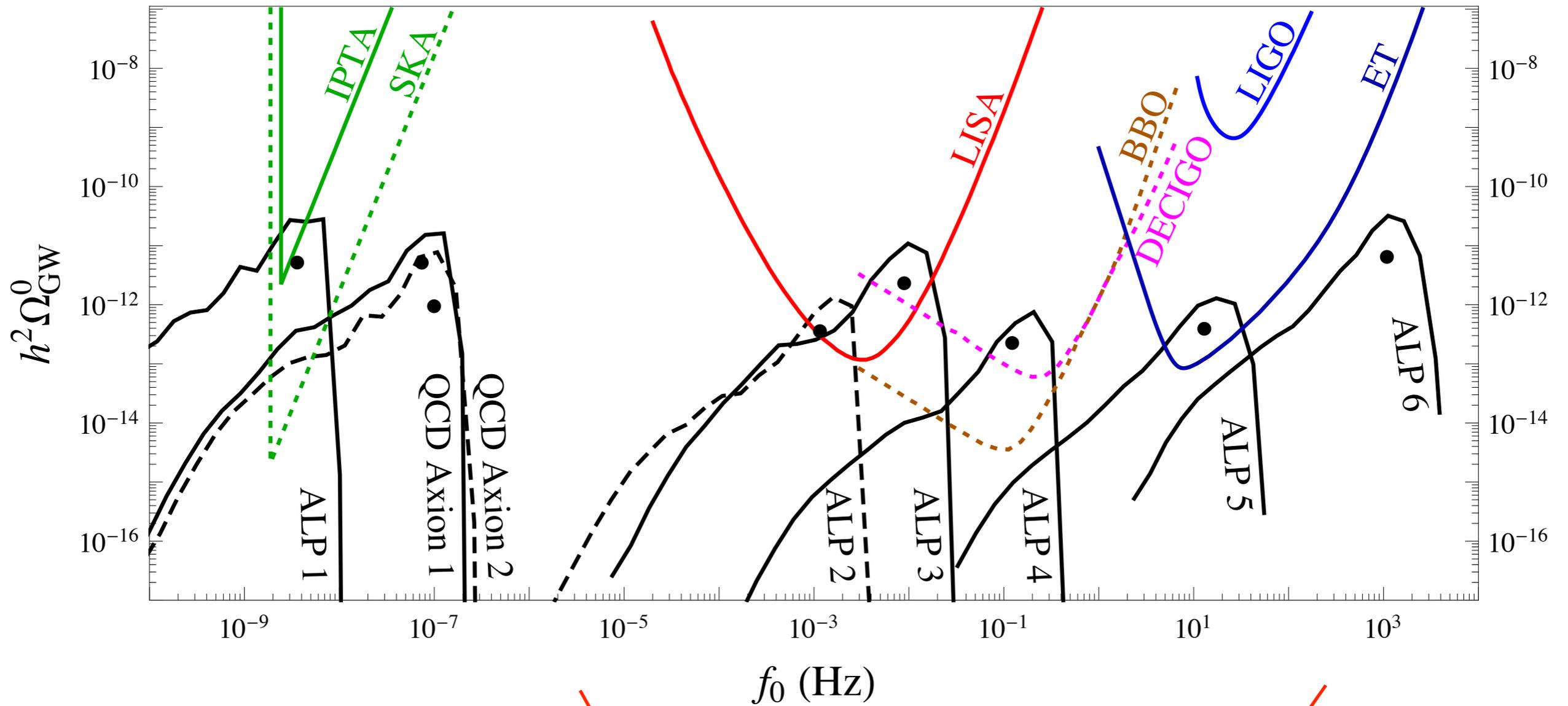


Anisotropic Stress



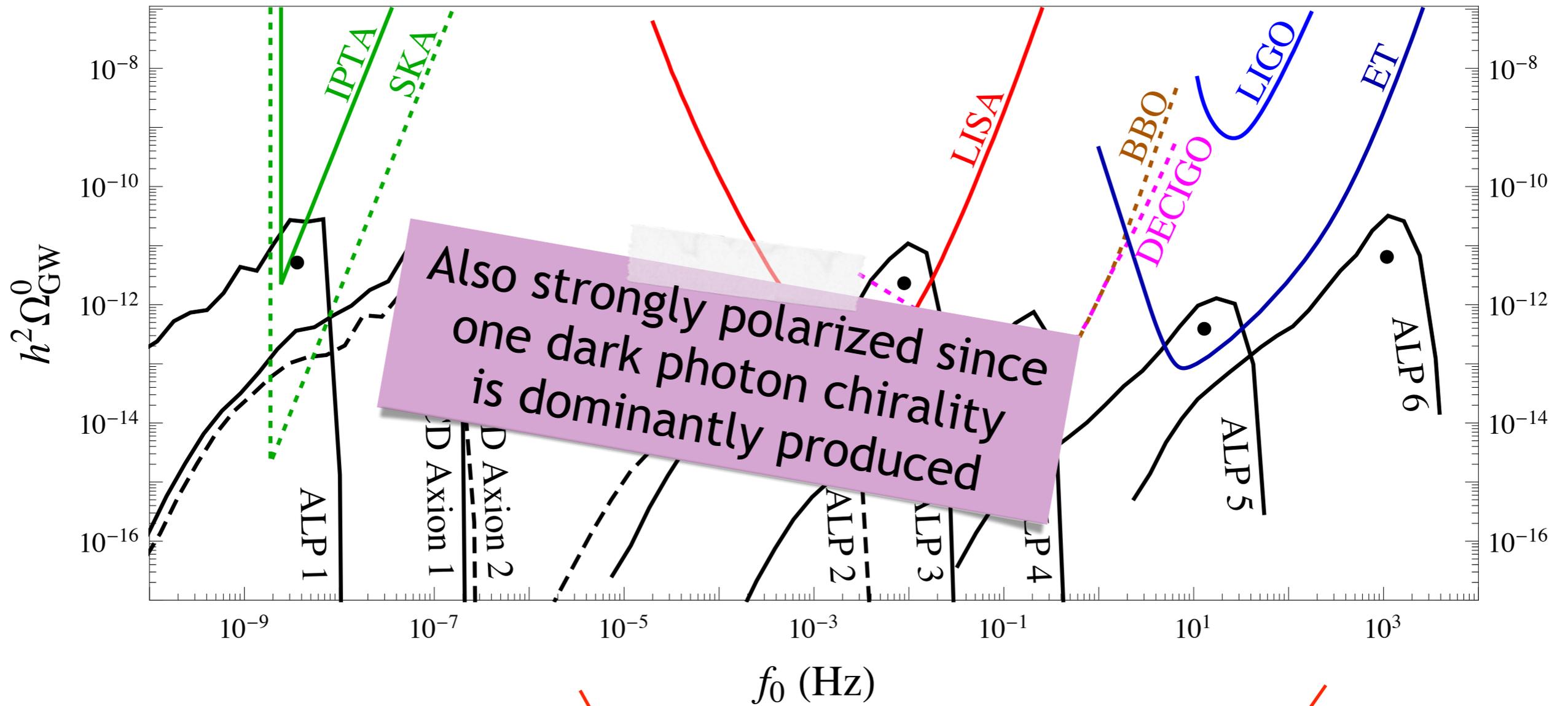
$$k_{\text{peak}} \approx (\alpha\theta)^{2/3} m, \quad \Omega_{\text{GW}}(k_{\text{peak}}) \approx \left(\frac{f}{M_P}\right)^4 \left(\frac{\theta^2}{\alpha}\right)^{4/3}$$





$$f_0 \approx m \left(\frac{T_0}{T_*} \right) (\alpha\theta)^{2/3} = \sqrt{\frac{m}{M_P}} T_0 (\alpha\theta)^{2/3},$$

$$\Omega_{\text{GW}}^0 \approx \Omega_\gamma^0 \left(\frac{f}{M_P} \right)^4 \left(\frac{\theta^2}{\alpha} \right)^{4/3}$$

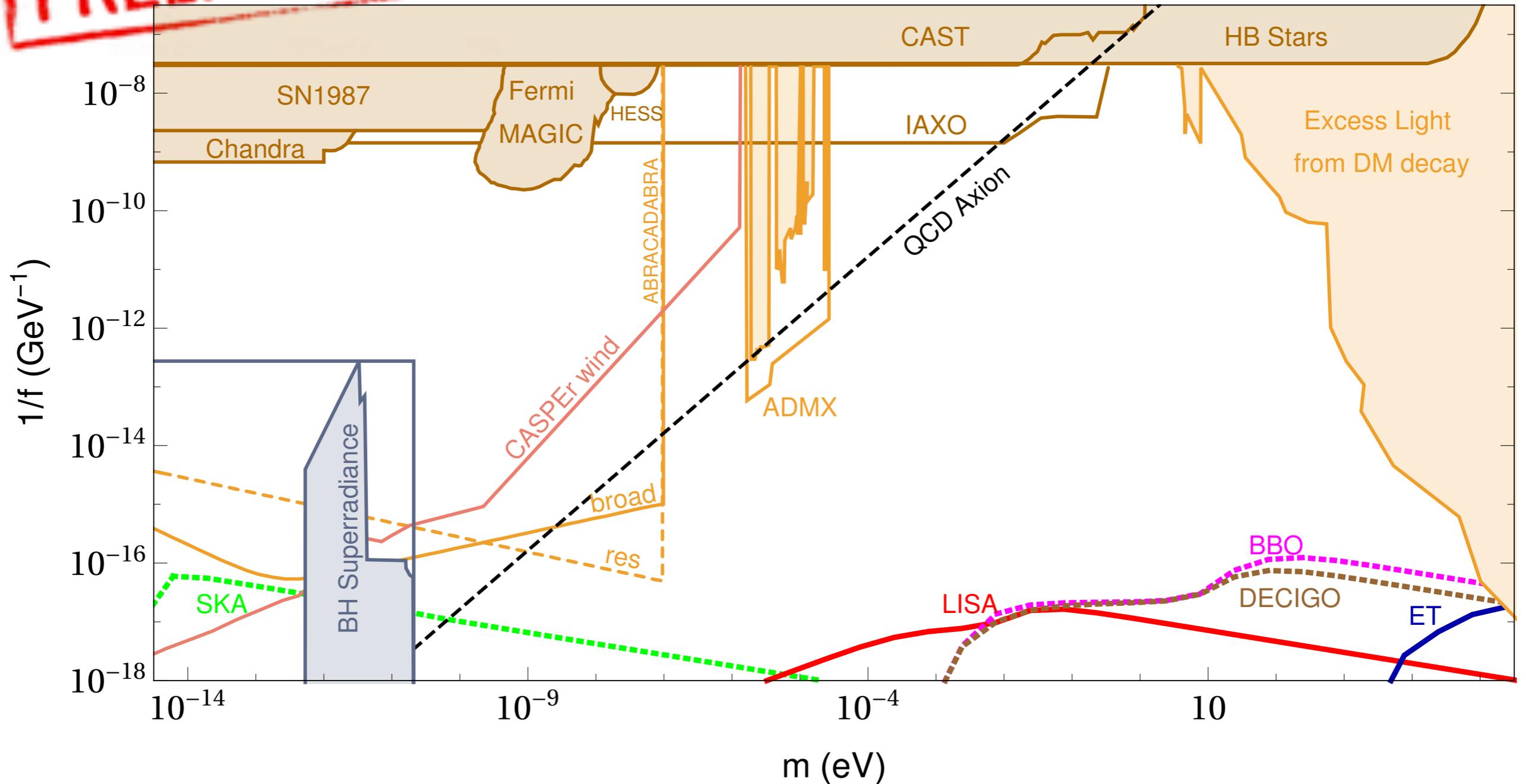


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$$\Omega_{\text{GW}}^0 \approx \Omega_\gamma^0 \left(\frac{f}{M_P} \right)^4 \left(\frac{\theta^2}{\alpha} \right)^{4/3}$$

Constraints on ALP plane

PRELIMINARY



Machado, Ratzinger, PS, Stefanek, 2019 (to appear)

From Wolframs talk @
GW4FP Amsterdam



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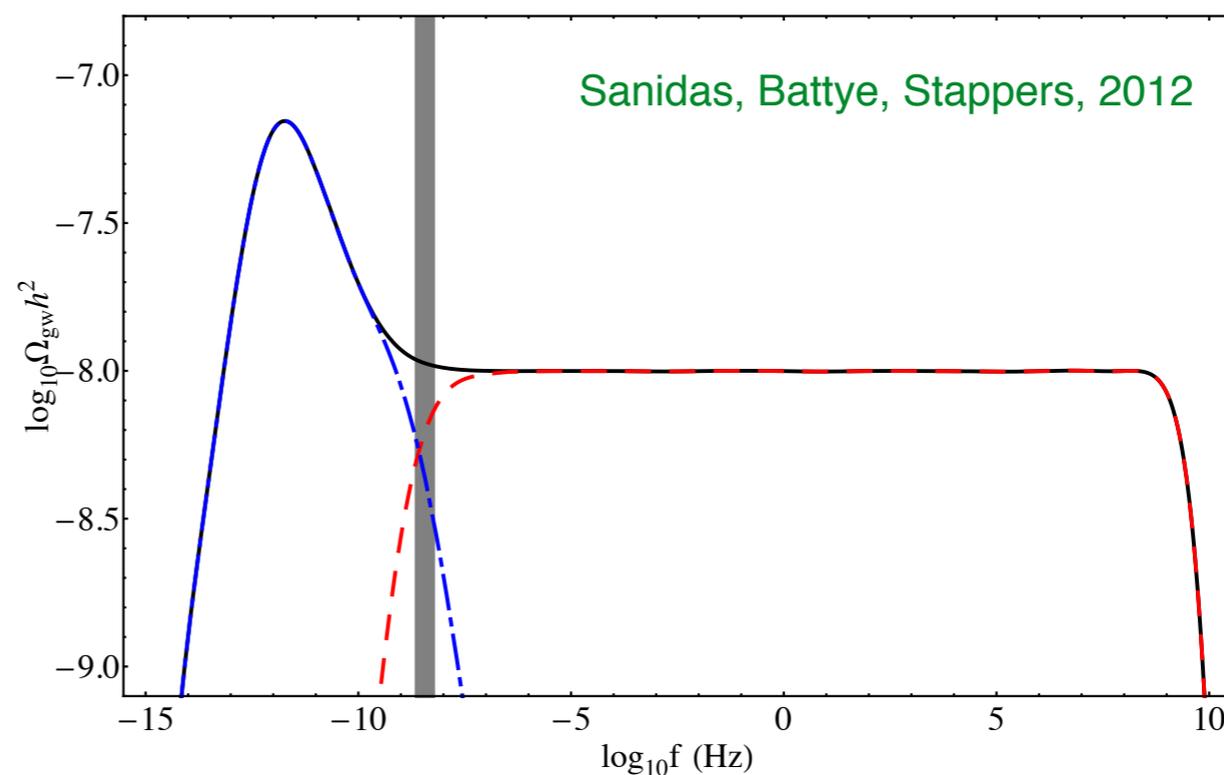
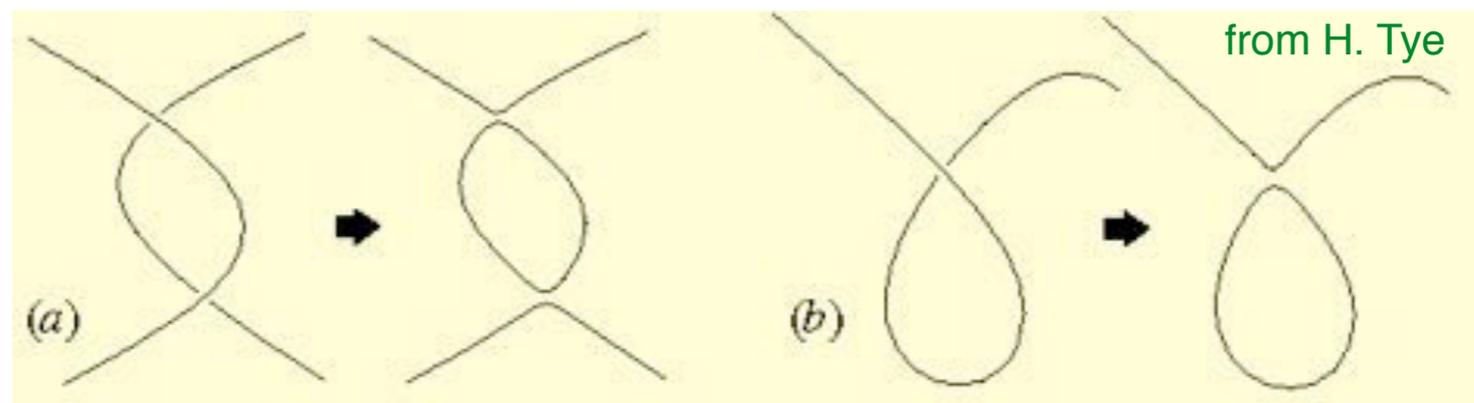


- Gravitational waves offer unique window into the early universe
- Can hope to observe GWs from a strong EWPT
- Could be first (or only) way to obtain signals from a strongly coupled hidden sector
- New way to probe axions/ALPs
- Lots of room for new ideas!

Cosmic strings

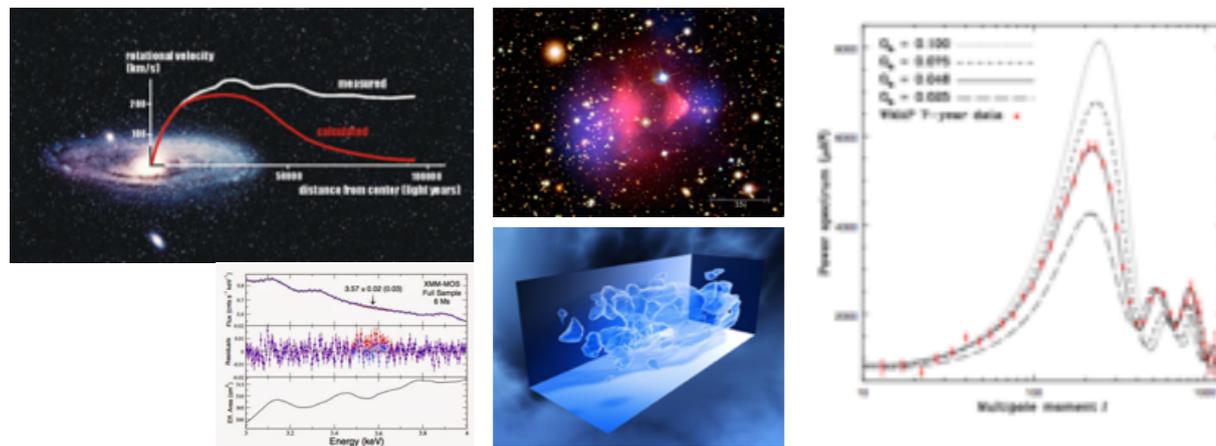
See also talk by
W. Buchmüller

- Topological defects or stretched superstrings
- Formed after inflation or in PTs
- Interact and form loops
- Loops loose energy by GW radiation

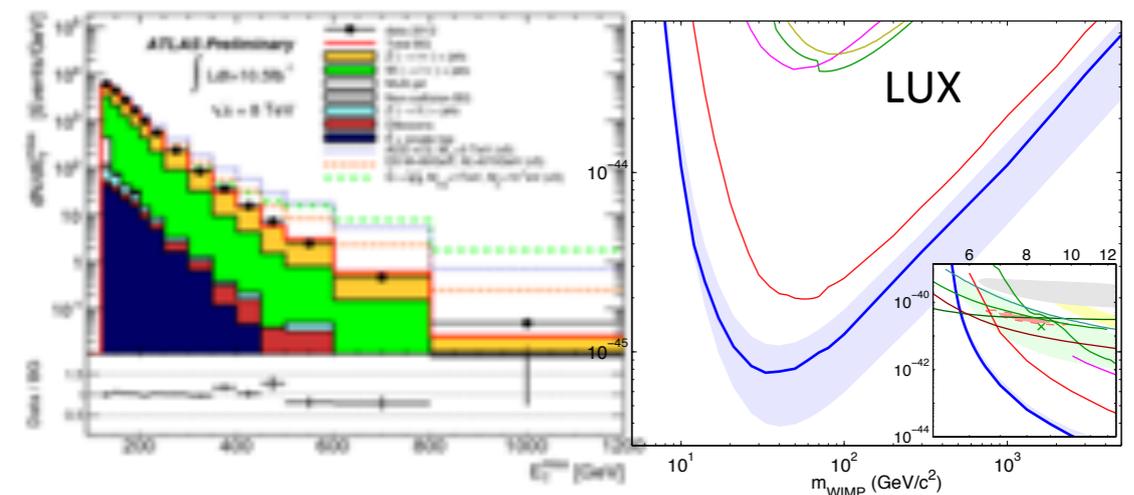


Dark Matter

We have seen DM in the sky:



But no direct observation



Maybe DM is just part of a larger dark sector

- Example: Proton is massive, stable, composite state
- DM self interactions solve structure formation problems
- New signals, new search strategies!

DM Motivation

- New mechanisms for relic density, extend mass range:
 - ▶ Asymmetric DM - GeV-TeV scale
 - ▶ Strong Annihilation - 100 TeV scale
 - ▶ SIMP - MeV scale
Hochberg, Kuflik, Volansky, Wacker, 2014; + Murayama, 2015
- Advantages of Composite
 - ▶ DM mass scale and stability
 - ▶ Fast annihilation for ADM
 - ▶ Self-interactions for structure formation

GW spectra

- Lot of work on GW from 1st order PT
 - Still difficult to simulate or model
- Here in addition:
 - Transition is non-perturbative
 - Parameters not known - take an optimistic guess

See talks by
Hindmarsh, Weir
for more details

$$\beta/H_* = 1 - 100$$

$$v = 1$$

$$\frac{\kappa\alpha}{1 + \alpha} = 0.1$$

SU(N) - PT 2

- One more parameter: Θ angle
- Effect on PT not well studied
- N_d, n_f dependence of PT strength?
- Finite density/chemical potentials?

M. Anber, 2013
Garcia-Garcia, Lasenby, March-Russell, 2015

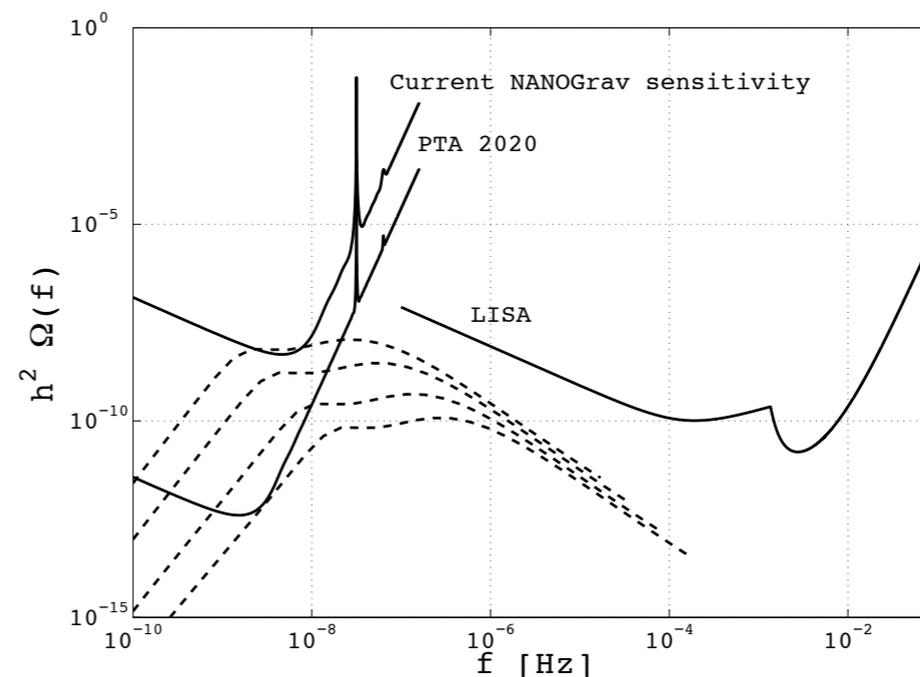
Panero, 2009

- ▶ QCD FOPT?

Schwarz, Stuke, 2009

- ▶ GW signal:

Caprini, Durrer, Siemens, 2009

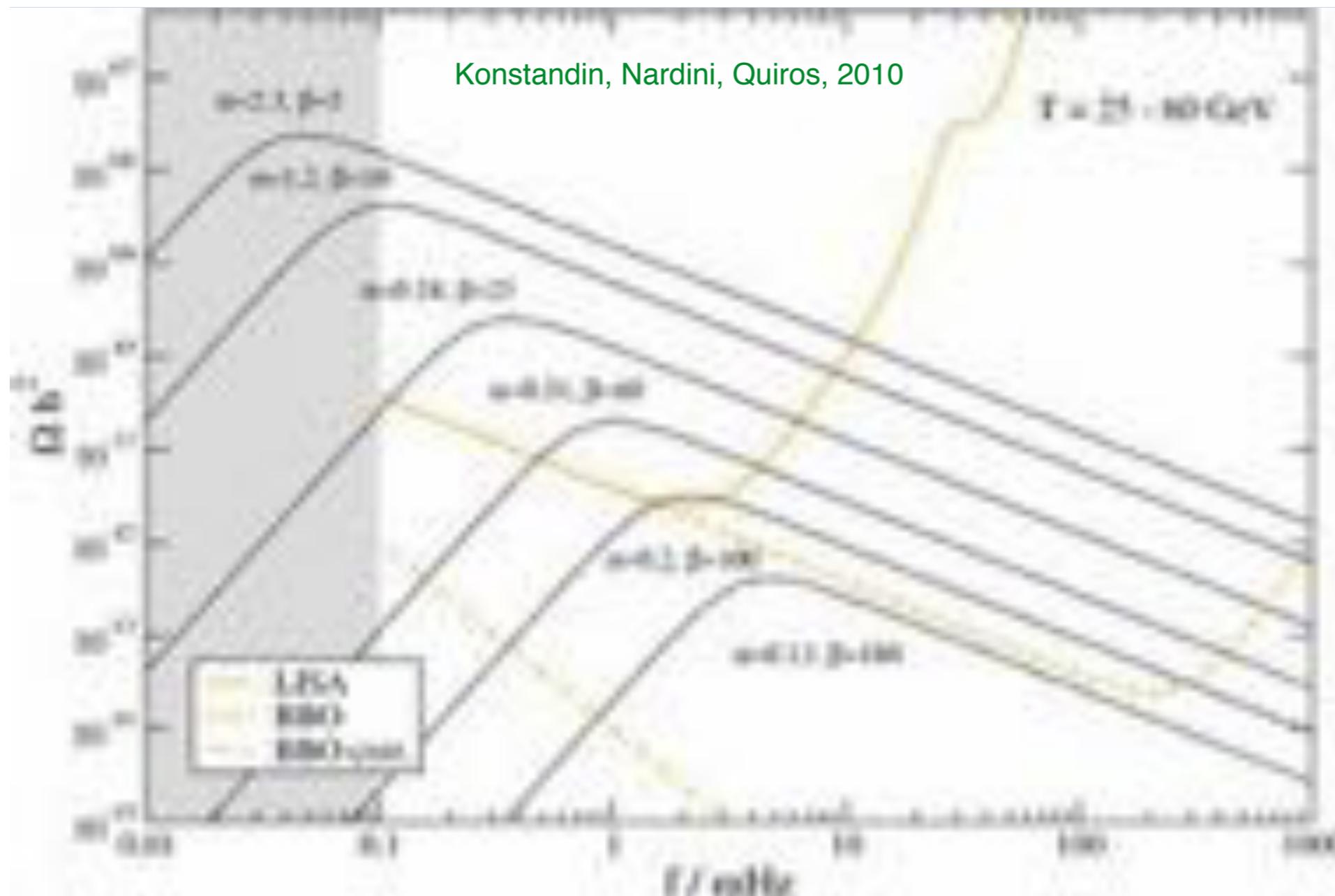


Electroweak Baryogenesis

- Baryogenesis requires departure from thermal equilibrium
- EWPT also provides B and CP violation, but no first order transition
- Strong motivation to study BSM scenarios with a strong EWPT. Examples:
 - ▶ Modified Higgs self-coupling
 - ▶ Extended scalar sectors
 - ▶ Radion in warped extra dimensions

For more details,
see talks by Geraldine,
Michael, Jeremy

Example: Radion in RS



Example: Strong EWPT

