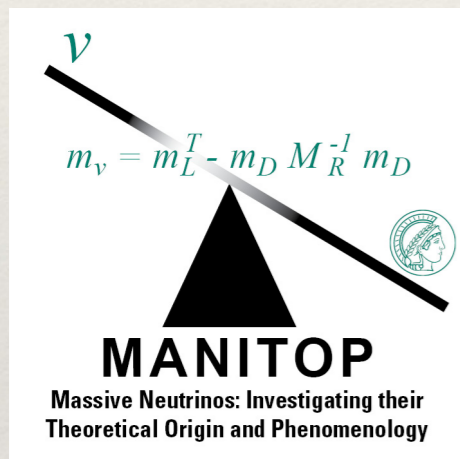


How to tell if a particle is its own antiparticle

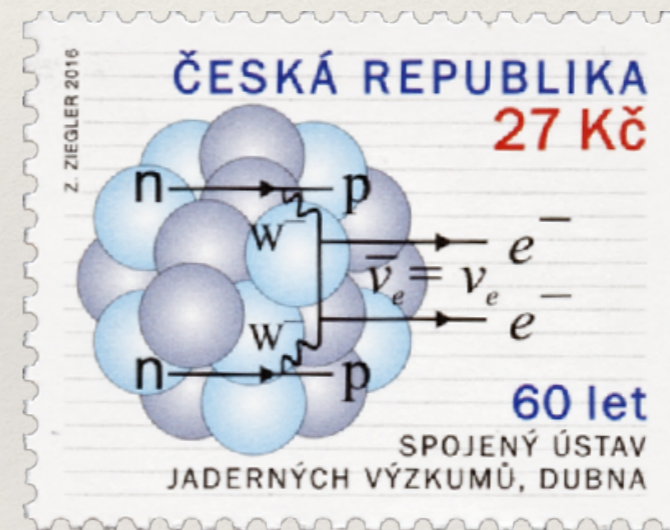


Werner Rodejohann (MPIK)
26/01/22



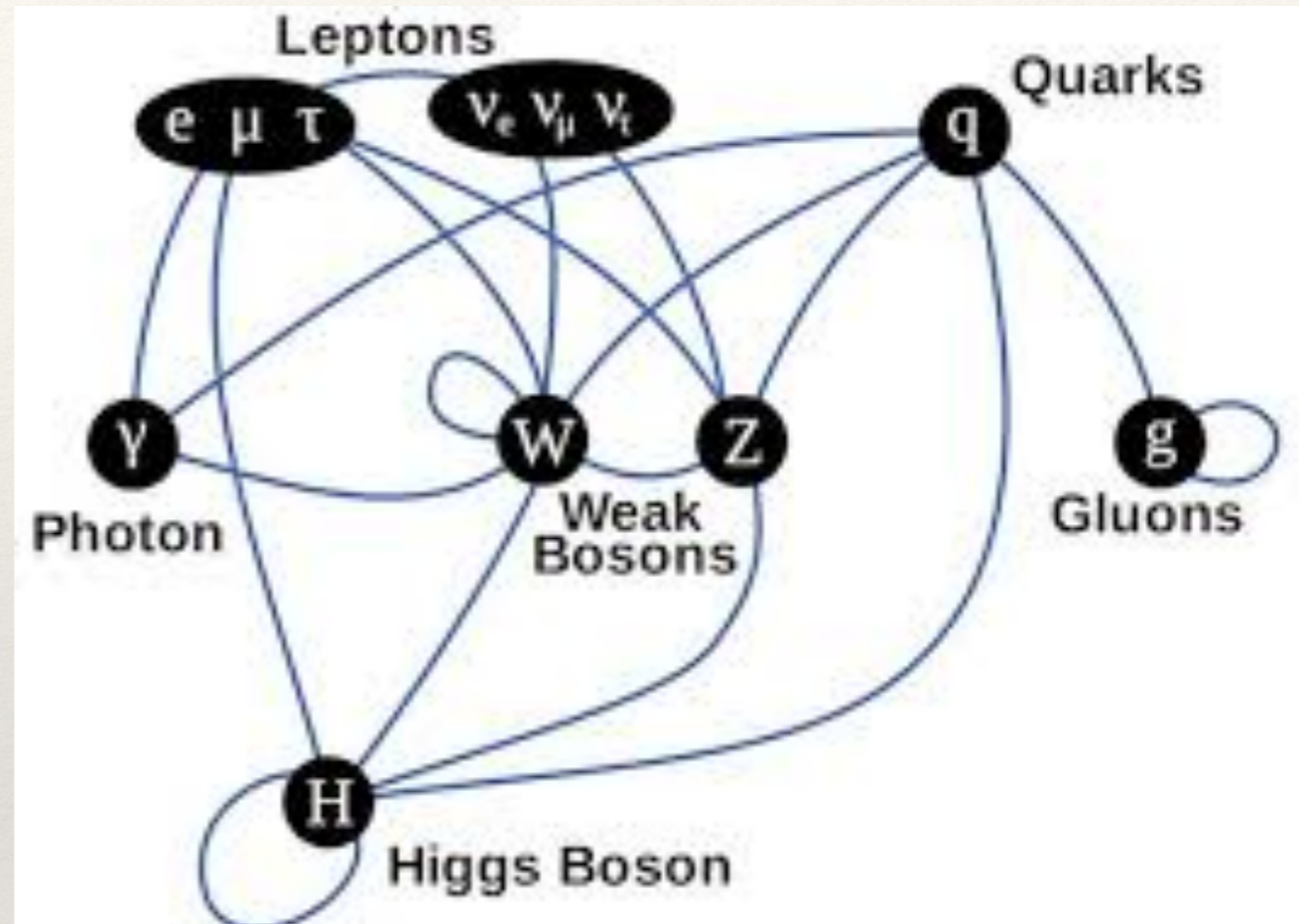
Outline

- ❖ Lepton Number Violation: Why look for it?
- ❖ Neutrinoless Double Beta Decay $(A,Z) \rightarrow (A,Z+2) + 2 e^-$:
 - Standard Interpretation
 - Non-Standard Interpretations
- ❖ $\Delta L = 2$ versus $\Delta L = 4$
- ❖ Self-conjugacy of dark matter



The Standard Model

	mass →	charge →	spin →							
QUARKS	$\approx 2.3 \text{ MeV}/c^2$	$2/3$	$1/2$	u	up	$\approx 1.275 \text{ GeV}/c^2$	$2/3$	$1/2$	c	charm
						$\approx 173.07 \text{ GeV}/c^2$	$2/3$	$1/2$	t	top
						0	0	1	g	gluon
									H	Higgs boson
LEPTONS	$\approx 4.8 \text{ MeV}/c^2$	$-1/3$	$1/2$	d	down	$\approx 95 \text{ MeV}/c^2$	$-1/3$	$1/2$	s	strange
						$\approx 4.18 \text{ GeV}/c^2$	$-1/3$	$1/2$	b	bottom
						0	0	1	γ	photon
GAUGE BOSONS	$0.511 \text{ MeV}/c^2$	-1	$1/2$	e	electron	$105.7 \text{ MeV}/c^2$	-1	$1/2$	μ	muon
						$1.777 \text{ GeV}/c^2$	-1	$1/2$	τ	tau
						$91.2 \text{ GeV}/c^2$	0	1	Z	Z boson
LEPTONS	$< 2.2 \text{ eV}/c^2$	0	$1/2$	ν_e	electron neutrino	$< 0.17 \text{ MeV}/c^2$	0	$1/2$	ν_μ	muon neutrino
						$< 15.5 \text{ MeV}/c^2$	0	$1/2$	ν_τ	tau neutrino
						$80.4 \text{ GeV}/c^2$	± 1	1	W	W boson



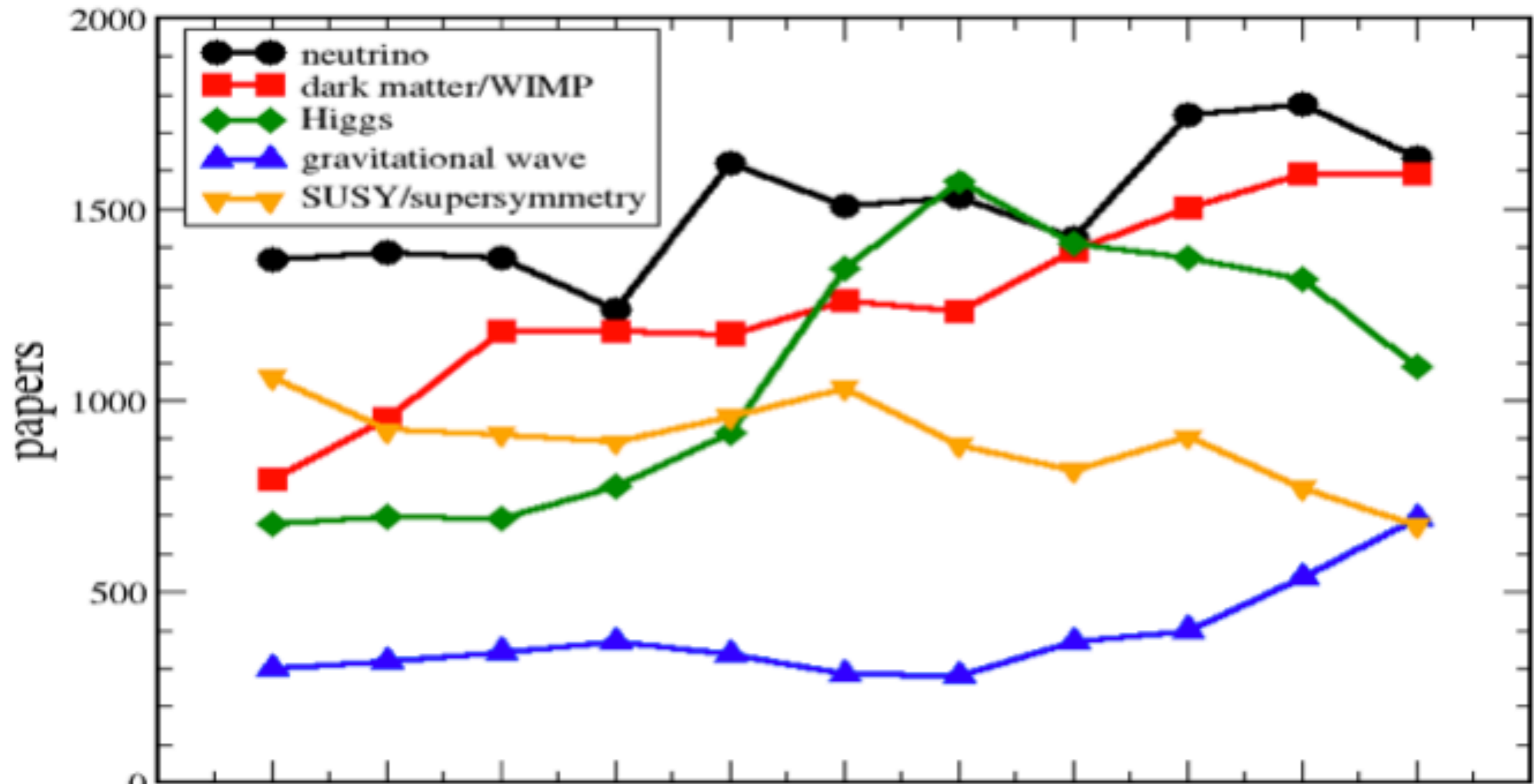
Single energy scale!

Interactions fixed by mathematical structure (gauge symmetry)
and symmetry breaking (Higgs): Confirmed!

Contains 19 free parameters, leaves unexplained many observational facts,...

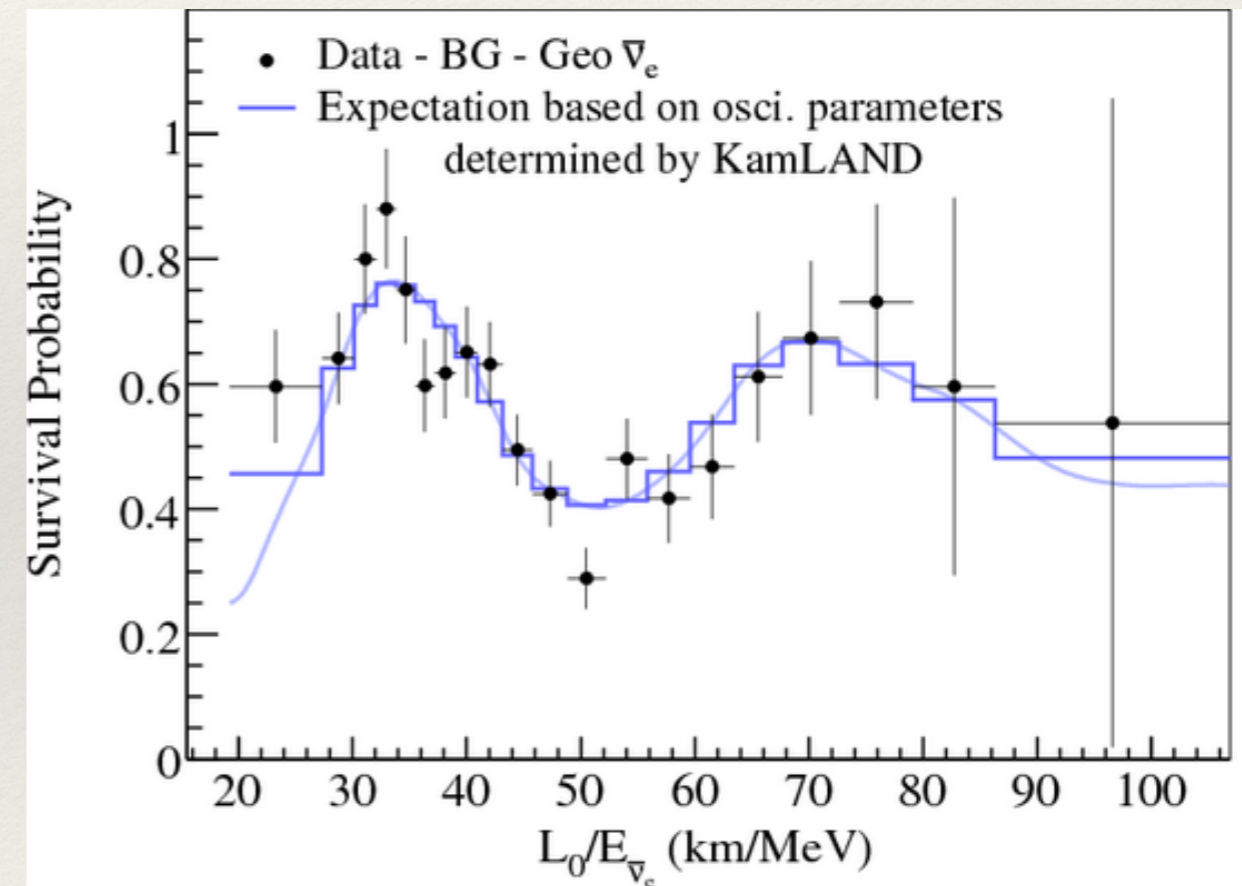
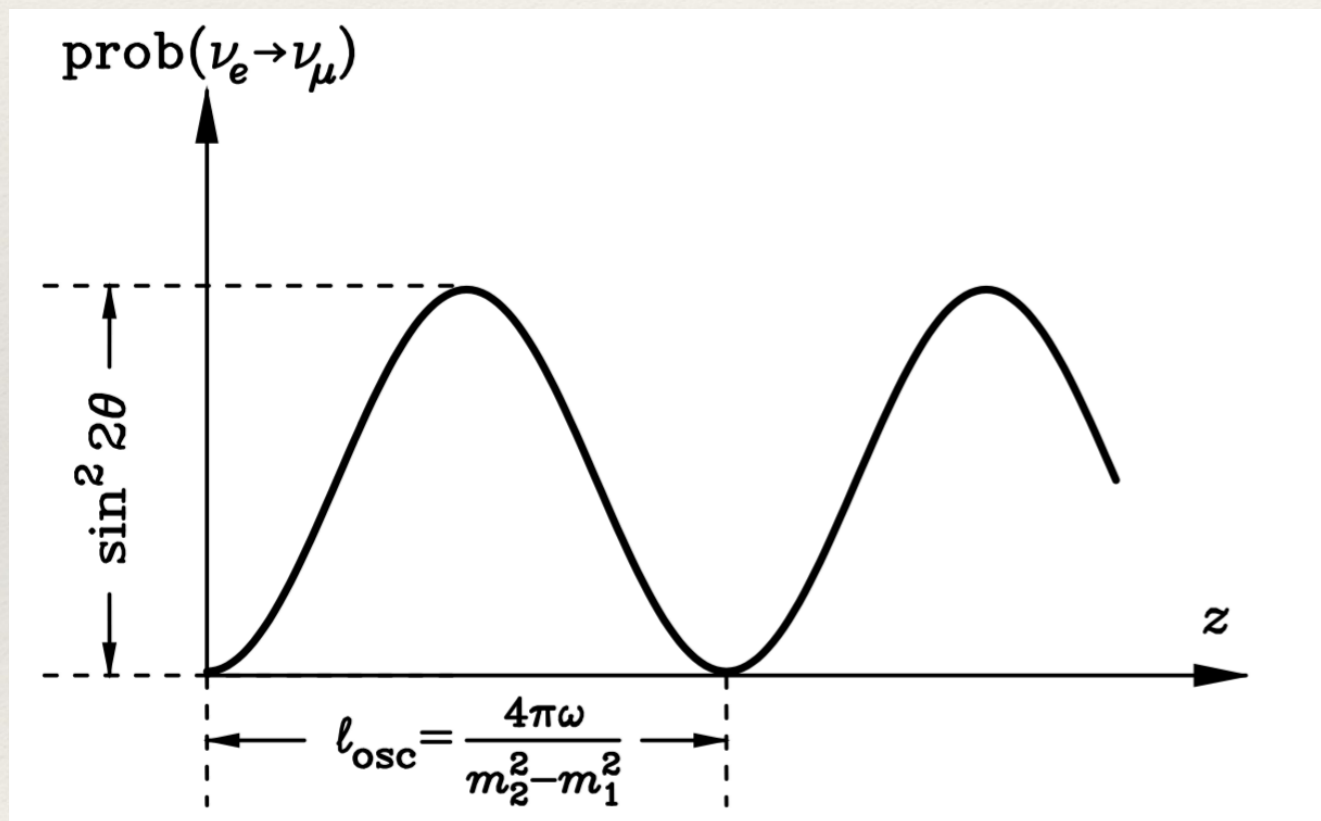
Neutrinos

INSPIRE: find title x and date y



Neutrinos do have mass!

$$P_{\alpha \rightarrow \beta, \alpha \neq \beta} = \sin^2(2\theta) \sin^2 \left(1.27 \frac{\Delta m^2 L [\text{eV}^2] [\text{km}]}{E [\text{GeV}]} \right).$$



Note: only mass (squared) differences can be measured!

Puzzles

- neutrino mass much much smaller than all other masses
- lepton mixing completely different from quark mixing (CKM)

Puzzles

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- ~~lepton mixing completely different from quark mixing (CKM)~~

Origin of Neutrino Mass

- ❖ Most straightforward possibility: add N_R and obtain Dirac mass:

$$\overline{L} \Phi N_R \rightarrow m_D \overline{\nu}_L N_R$$

- ❖ Gauge invariance allows Majorana mass

$$M_R N_R N_R^c$$

- ❖ in total Majorana mass for SM neutrinos:

$$m_\nu \nu_L^c \nu_L \text{ with } m_\nu = m_D^2 / M_R = m_D \varepsilon \text{ with } \varepsilon = m_D / M_R = m_{SM} / M_R$$

violates lepton number
by two units: $\Delta L=2$



m_ν inversely
proportional to
scale of origin!

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- mass term links LH and RH projection
- here RH projection is LH^c
- thus: $\text{nu} = LH + RH = LH + LH^c$
- and thus: $\text{nu}^c = LH^c + LH = \text{nu}$
- is its own antiparticle!

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New energy scale beyond SM

- ❖ in total Majorana mass for SM neutrinos:

$m_\nu \nu_L^c \nu_L$ with $m_\nu \propto \frac{m_{SM}}{M_R}$

New concept: lepton number violation

violates lepton number by two units: $\Delta L=2$



m_ν inversely proportional to scale of origin!

Origin of Neutrino Mass

- ❖ N_R could be TeV: colliders!
- ❖ N_R could be keV: dark matter!
- ❖ N_R could decay in early Universe: baryon asymmetry!
- ❖ N_R couples to Higgs: vacuum stability, hierarchy problem!
- ❖ N_R couples to lepton doublets: lepton flavor violation!

==> Use this to distinguish the many (many!) mechanisms for neutrino mass

Why look for Lepton Number Violation?

- ❖ L and B accidentally conserved in SM
- ❖ $\mathcal{L} = \mathcal{L}_{\text{SM}} + 1/\Lambda \mathcal{L}_5 + 1/\Lambda^2 \mathcal{L}_6 + \dots$,
with $\mathcal{L}_5 = L^c \phi \phi L \rightarrow m_\nu \nu_L^c \nu_L$
- ❖ Baryogenesis: B is violated
- ❖ B, L often connected in BSM, GUTs
- ❖ GUTs have seesaw and Majorana neutrinos
- ❖ (B and L non-perturbatively violated by 3 units in SM...)

Why look for Lepton Number Violation?

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❖ $\mathcal{L} = \mathcal{L}_{\text{SM}} + 1/\Lambda \mathcal{L}_5 + 1/\Lambda^2 \mathcal{L}_6 + \dots,$

with **Lepton Number as important as Baryon Number**

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❖ B, L often connected in BSM, GUTs

❖ GUTs have seesaw and Majorana neutrinos

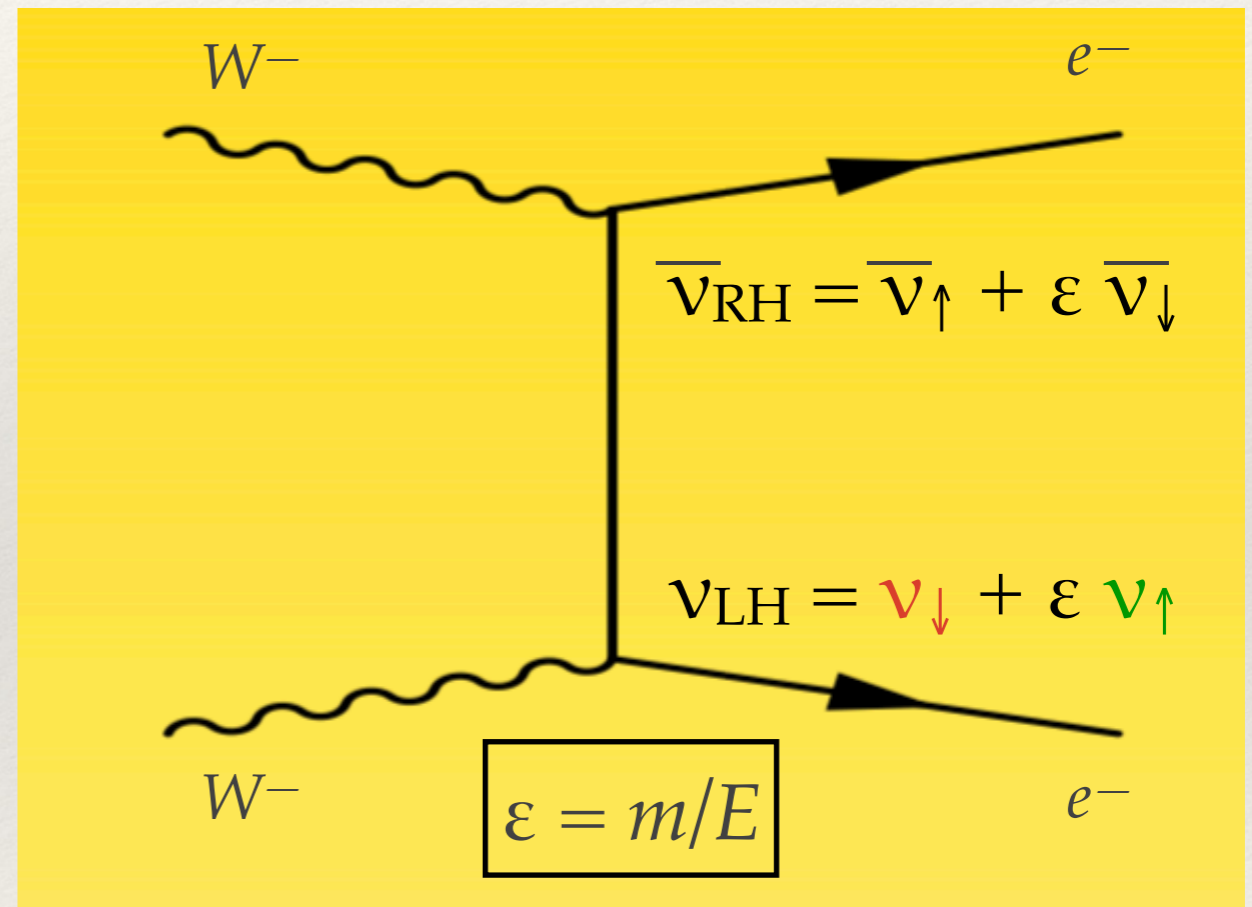
❖ (B and L non-perturbatively violated by 3 units in SM...)

Lepton Number Conservation?

- ❖ accidental lepton number conservation difficult in BSM...
- ❖ need a symmetry to forbid $M_R N_R N_R$
 - *can apply flavor symmetries with $(N_{R1}, N_{R2}, N_{R3}) \sim \underline{3}$, in groups that have no singlet in $\underline{3 \times 3}$ (e.g. $\Delta(27)$)*
 - *still need to explain smallness, e.g. wave-function overlap in ED, 2HDM with one vev of order eV,...*
- ❖ global $U(1)_L$ or $U(1)_{B-L}$ \rightarrow expected to be broken by quantum gravity effects
- ❖ gauge $U(1)_L$ or $U(1)_{B-L}$ without breaking? \rightarrow long range force, needs ultra-tiny charge

Why so difficult to see $\Delta L=2$?

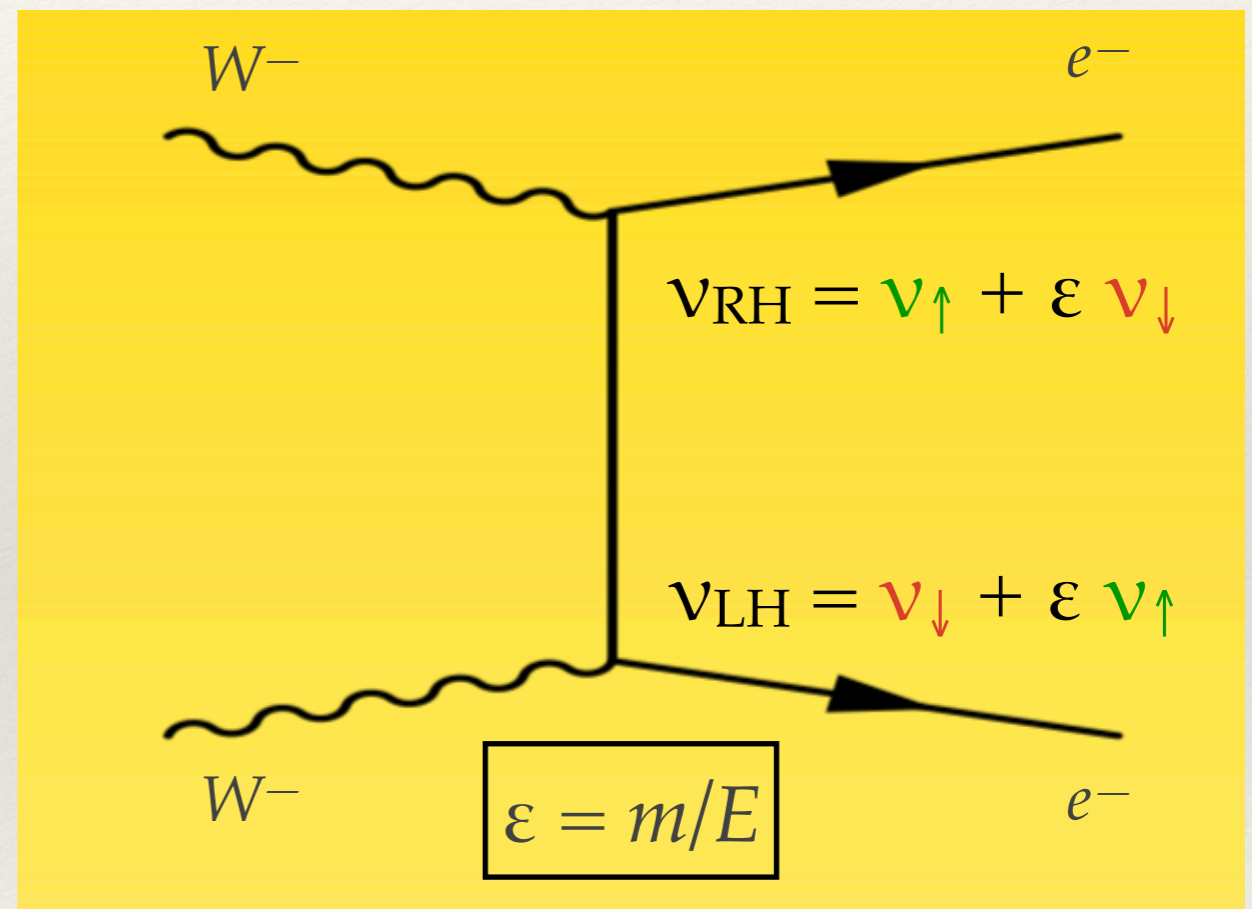
- ❖ $V-A$ makes things difficult: chirality vs. helicity
- ❖ $\mathbf{v}_D = (\mathbf{v}_{\downarrow}, \bar{\mathbf{v}}_{\downarrow}, \mathbf{v}_{\uparrow}, \bar{\mathbf{v}}_{\uparrow})$



- ❖ doesn't work

Why so difficult to see $\Delta L=2$?

- ❖ $V-A$ makes things difficult: chirality vs. helicity
- ❖ $\mathbf{v}_M = (\mathbf{v}_\downarrow, \mathbf{v}_\uparrow) = \bar{\mathbf{v}}_M$



- ❖ probability suppressed by $(m/E)^2$

Why so difficult to see $\Delta L=2$?

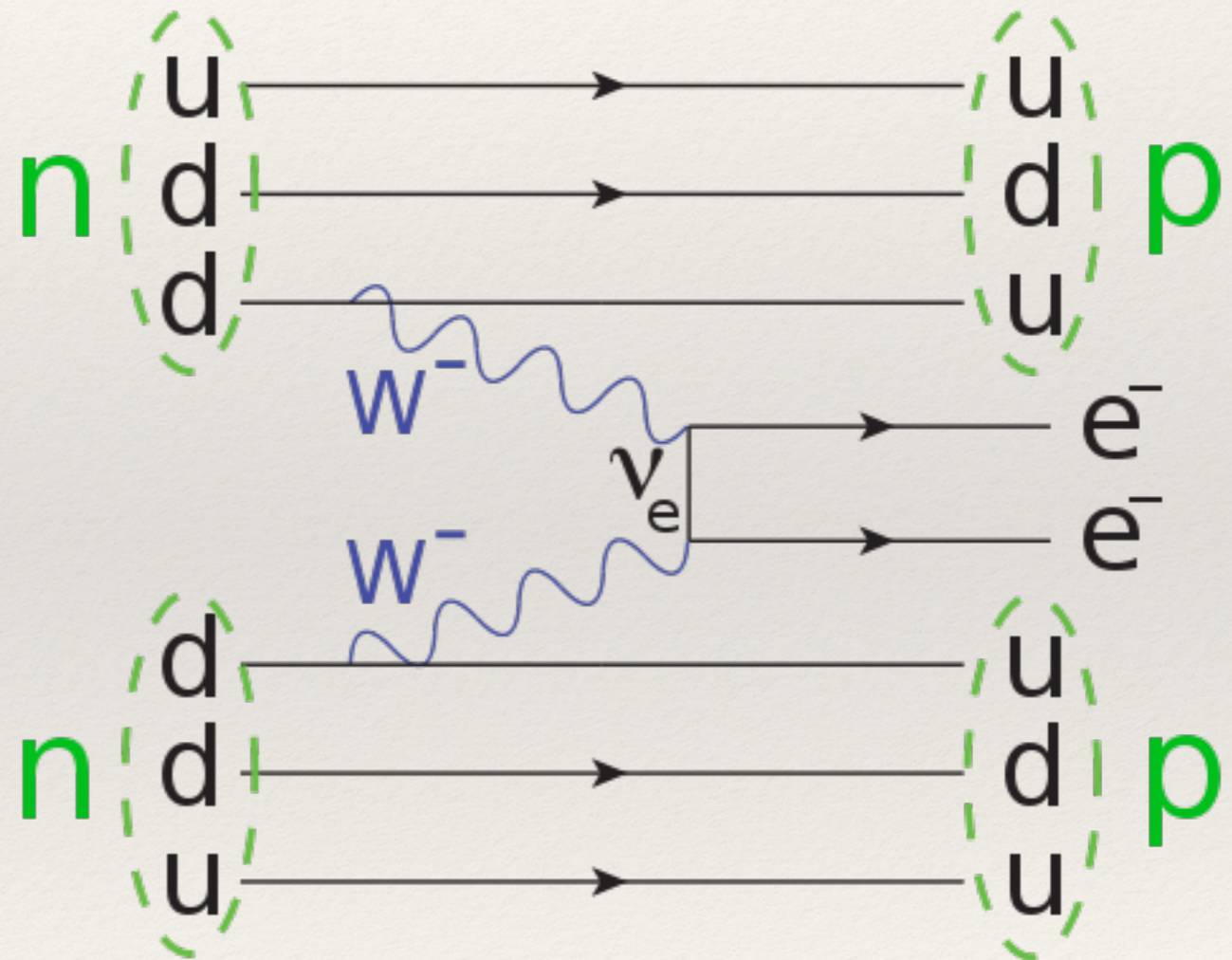
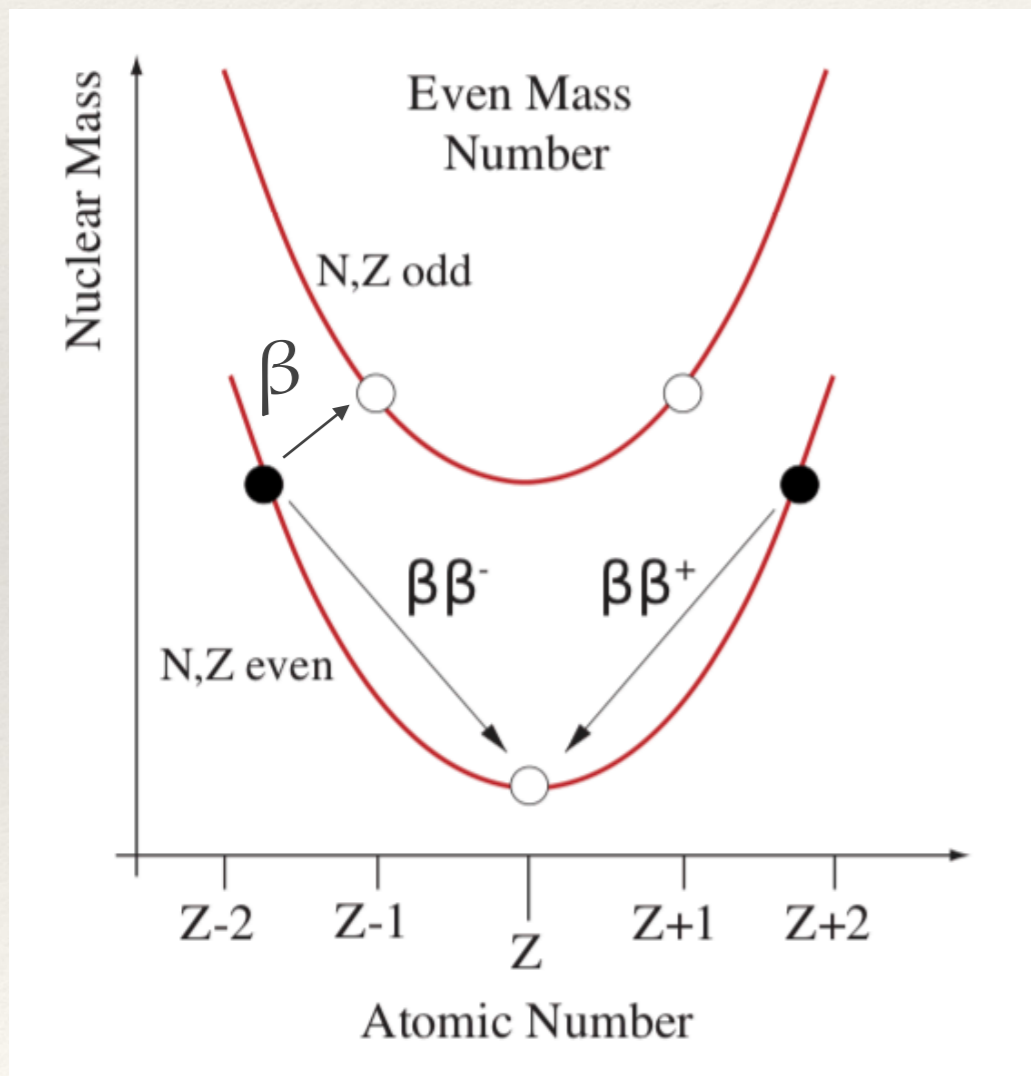
- ❖ probability suppressed by $(m/E)^2$:
 - $\Gamma(Z \rightarrow \nu_D \bar{\nu}_D) / \Gamma(Z \rightarrow \nu_M \nu_M) = 1 - 3 (m_\nu / m_Z)^2$
 - $BR(K^+ \rightarrow \pi^- e^+ \mu^+) = 10^{-30} (\langle m_{e\mu} \rangle / eV)^2$
 - $P(\nu_\alpha \rightarrow \bar{\nu}_\beta) = 1/E^2 | \sum U_{\alpha j} U_{\beta j} U_{\alpha i}^* U_{\beta i}^* m_i m_j e^{-i(E_i - E_j) t} |$
- ❖ Only way to beat m/E :

Why so difficult to see $\Delta L=2$?

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- ❖ Only way to beat m/E : Avogadro's number

Neutrinoless Double Beta Decay

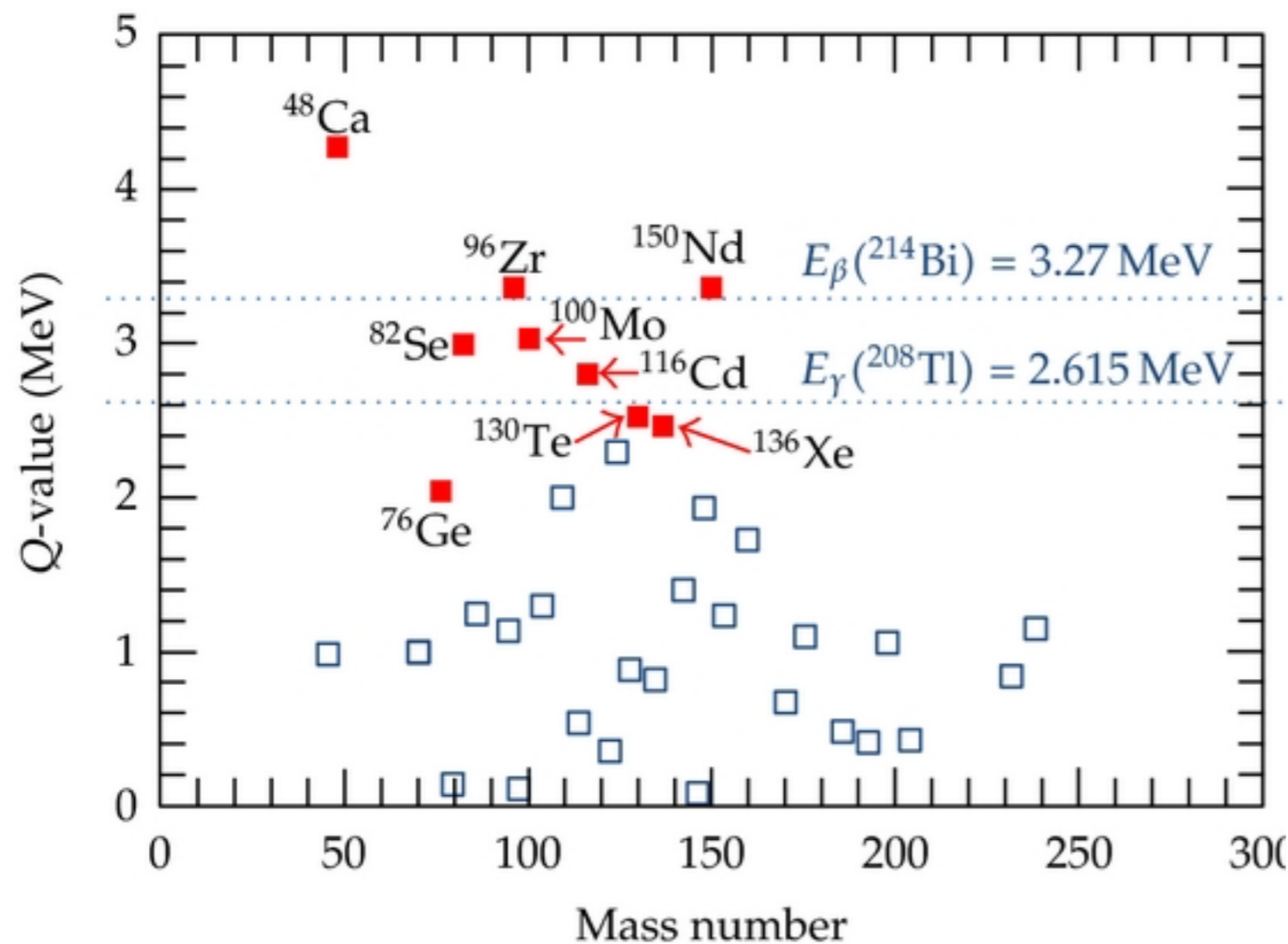
$$(A, Z) \rightarrow (A, Z+2) + 2 e^-$$



need to forbid β -decay

„creates matter!“

Neutrinoless Double Beta Decay



Isotope	$G [10^{-14} \text{ yrs}^{-1}]$	$Q [\text{keV}]$	nat. abund. [%]
^{48}Ca	6.35	4273.7	0.187
^{76}Ge	0.623	2039.1	7.8
^{82}Se	2.70	2995.5	9.2
^{96}Zr	5.63	3347.7	2.8
^{100}Mo	4.36	3035.0	9.6
^{110}Pd	1.40	2004.0	11.8
^{116}Cd	4.62	2809.1	7.6
^{124}Sn	2.55	2287.7	5.6
^{130}Te	4.09	2530.3	34.5
^{136}Xe	4.31	2461.9	8.9
^{150}Nd	19.2	3367.3	5.6

35 isotopes, 9 are useful

Current Limits

GERDA, 1909.02726

Experiment	Isotope	M_i (kmol)	FWHM (keV)	$\mathcal{L}(T_{1/2})$ (10^{25} yr)	$\mathcal{S}(T_{1/2})$ (10^{25} yr)	$m_{\beta\beta}$ (meV)
GERDA (this work)	^{76}Ge	0.41	3.3	9	11	104 - 228
Majorana [22]	^{76}Ge	0.34	2.5	2.7	4.8	157 - 346
CUPID-0 [23]	^{82}Se	0.063	23	0.24	0.23	394 - 810
CUORE [24]	^{130}Te	1.59	7.4	1.5	0.7	162 - 757
EXO-200 [25]	^{136}Xe	1.04	71	1.8	3.7	93 - 287
KamLAND-Zen [26]	^{136}Xe	2.52	270	10.7	5.6	76 - 234

reached 10^{26} years and 0.2 eV neutrino mass limits

Neutrinoless Double Beta Decay



- ❖ Master Formula: $\Gamma^{0\nu} = G_x(Q, Z) |\mathcal{M}_x(A, Z) \eta_x|^2$
- $G_x(Q, Z)$: phase space factor, $\propto Q^5$
 - $\mathcal{M}_x(A, Z)$: Nuclear Matrix Element (NME)
 - η_x : particle physics parameter

Neutrinoless Double Beta Decay



❖ Master Formula:

$$\Gamma^{0\nu} = G_x(Q, Z) |\mathcal{M}_x(A, Z) \eta_x|^2$$

- $G_x(Q, Z)$: phase space factor, $\propto Q^5$ **calculable[#]**
- $\mathcal{M}_x(A, Z)$: Nuclear Matrix Element (NME) **problematic^{*}**
- η_x : particle physics parameter **interesting**

#ignore here

**ignore here even more*

Interpretations

❖ Standard Interpretation

- Neutrinoless Double Beta Decay is mediated by light and massive Majorana neutrinos (the ones which oscillate) and all other mechanisms potentially leading to $0\nu\beta\beta$ give negligible or no contribution

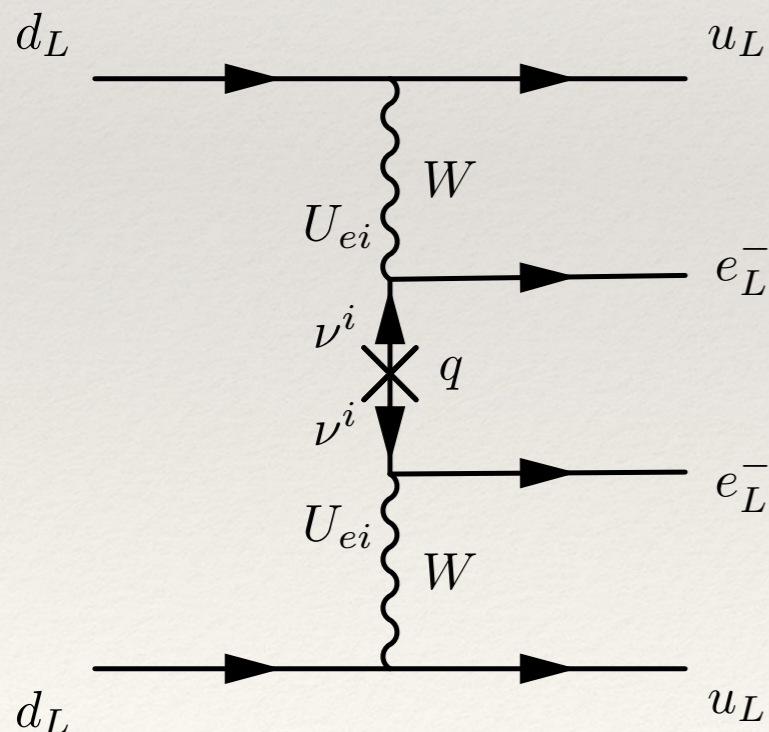
❖ Non-Standard Interpretations

- There is at least one other mechanism leading to Neutrinoless Double Beta Decay and its contribution is at least of the same order as the light neutrino exchange mechanism

WR, 1106.1334

Standard Interpretation

- ❖ Neutrinoless Double Beta Decay is mediated by light and massive Majorana neutrinos (the ones which oscillate) and all other mechanisms potentially leading to $0\nu\beta\beta$ give negligible or no contribution



amplitude proportional to „effective mass“:

$$|m_{ee}| = \left| \sum U_{ei}^2 m_i \right| = \left| U_{e1}^2 m_1 + U_{e2}^2 m_2 e^{i\alpha} + U_{e3}^2 m_3 e^{i\beta} \right|$$

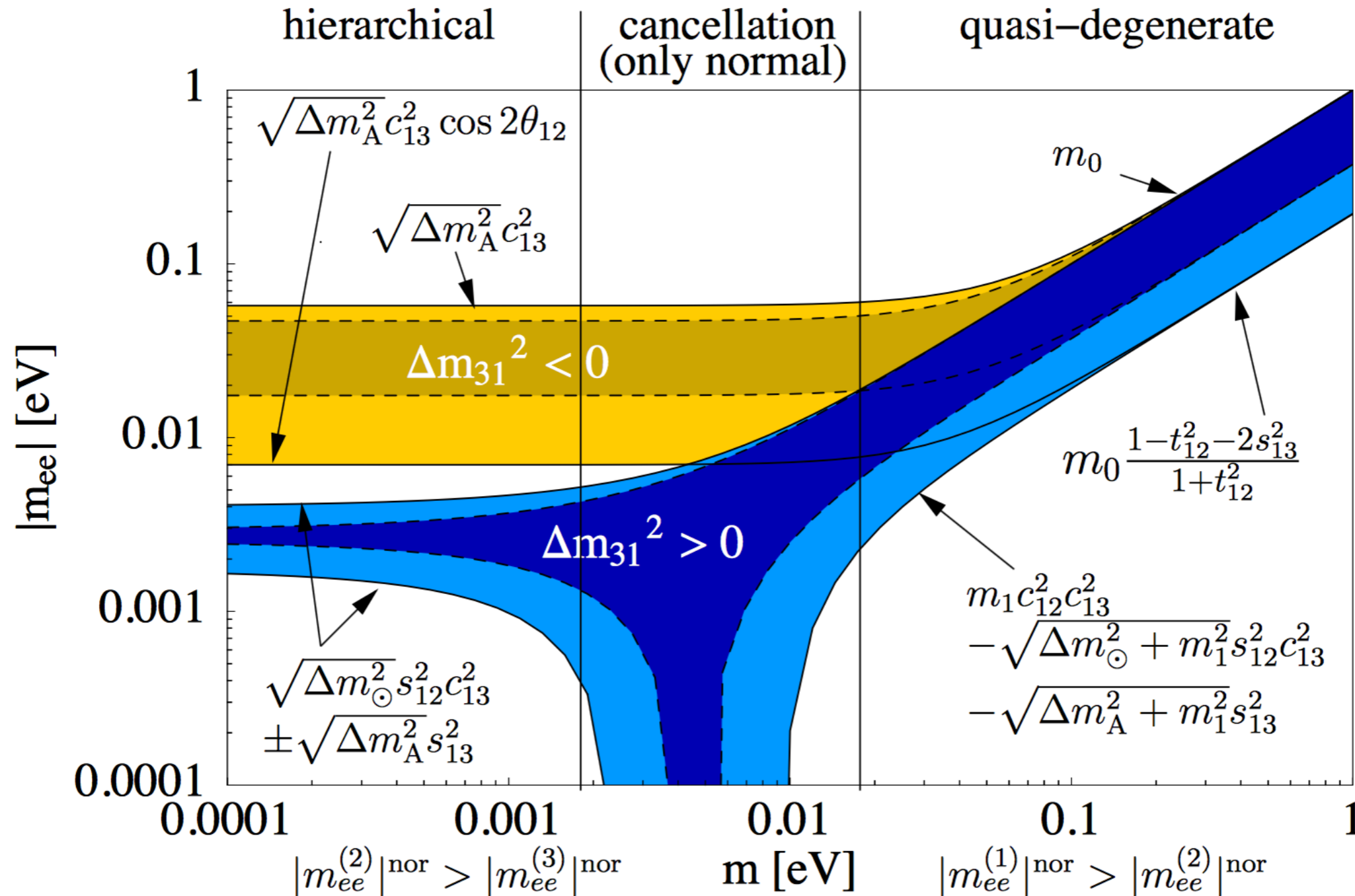
$$= f(\theta_{12}, |U_{e3}|, m_i, \text{sgn}(\Delta m_A^2), \alpha, \beta)$$

known

limits

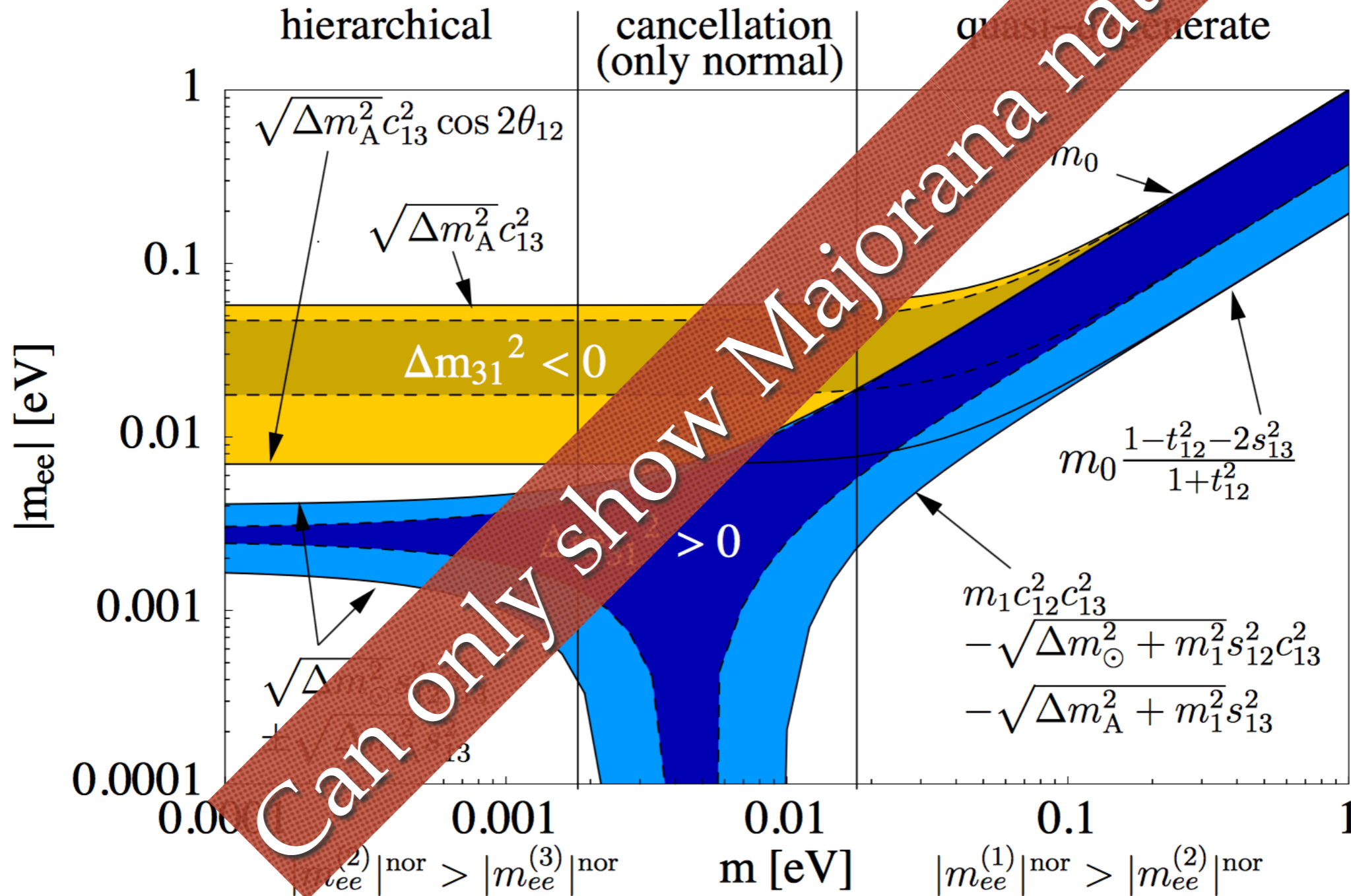
unknown

The usual plot



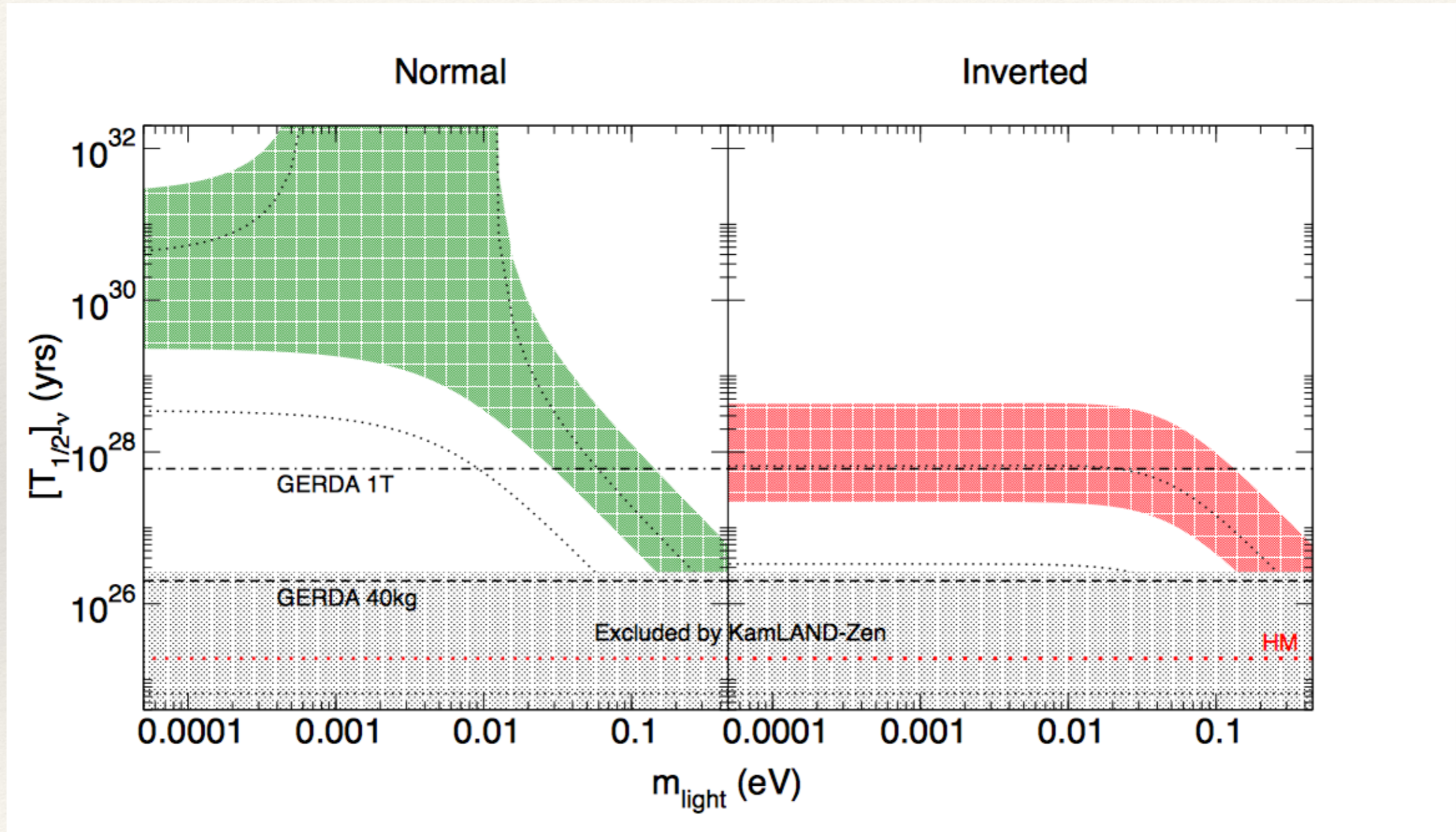
Lindner, Merle, WR, PRD73

The usual plot



Lindner, Merle, WR, PRD73

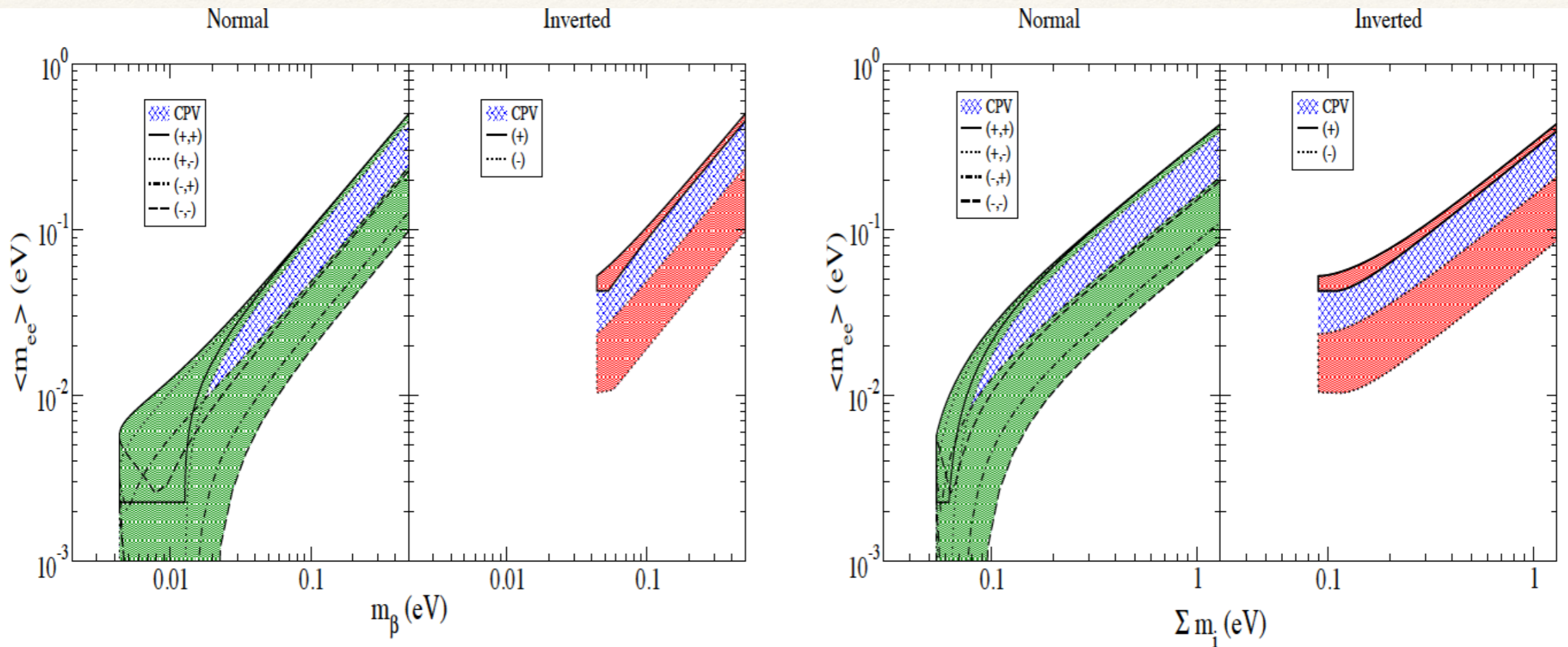
The usual plot



Neutrino Mass Observables

Method	Observable	current	near	far	pro	con
Kurie	$\sum U_{ei} ^2 m_i^2$	0.8 eV	0.3 eV	0.1 eV?	model-indep.; clean	final; weakest
cosmo	$\sum m_i$	0.5 eV	0.1 eV	0.05 eV?	best; NH/IH	model-dep.; systematics
$0\nu\beta\beta$	$\sum U_{ei}^2 m_i$	0.2 eV	0.05 eV	0.01 eV?	fundamental; NH/IH	model-dep.; NMEs

Neutrino Mass Observables



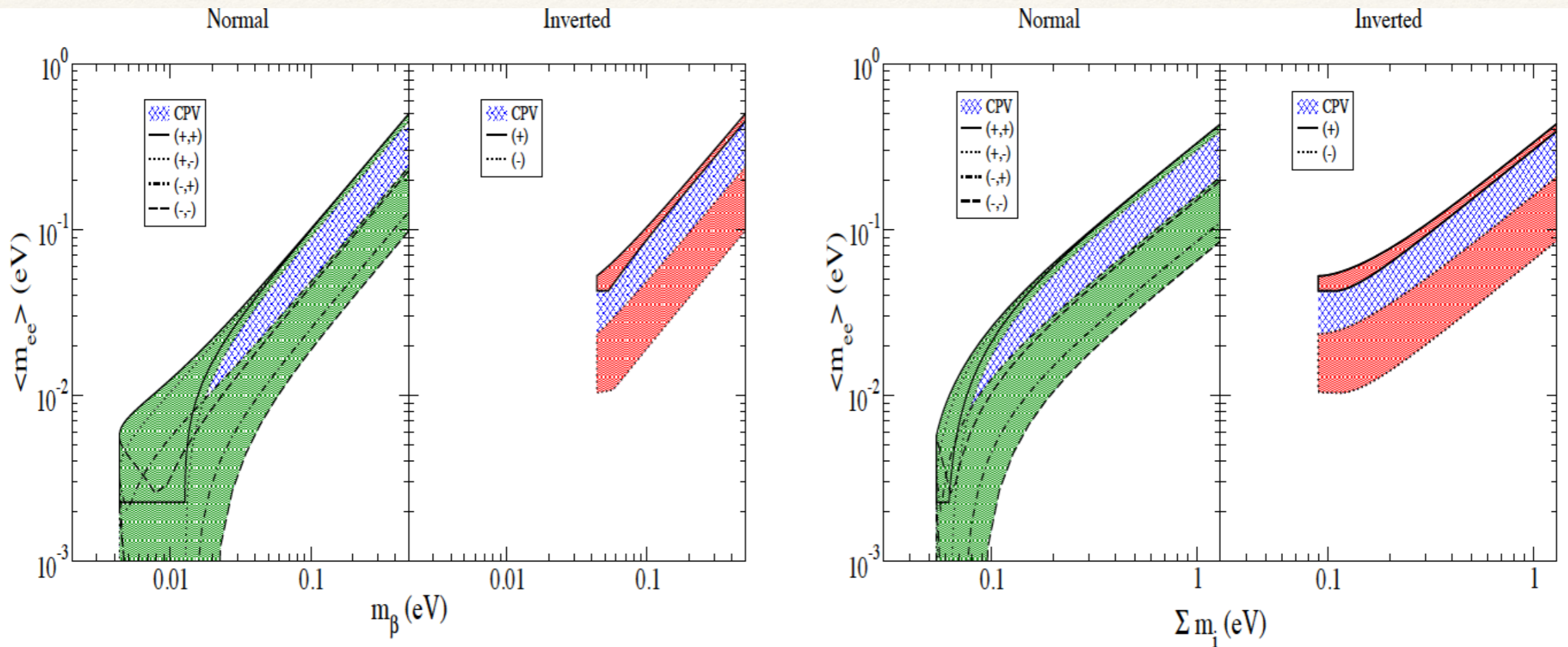
**complete complementarity
of observables**

$0\nu\beta\beta$ rules out that neutrinos saturate KATRIN-limit

$0\nu\beta\beta$ and conservative cosmology currently roughly same

cosmology strongly disfavors a signal in KATRIN

Neutrino Mass Observables

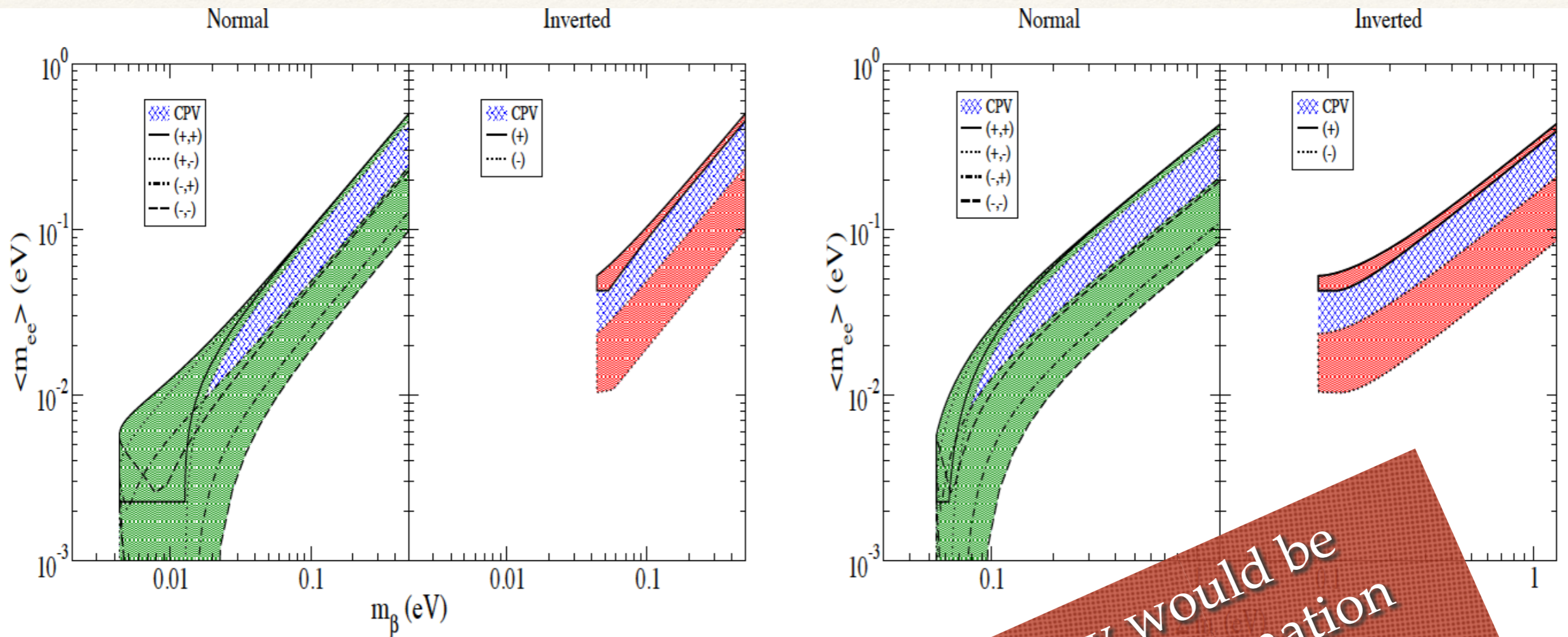


complete complementarity
of observables

- $0\nu\beta\beta$ rules out that neutrinos are degenerate at KATRIN-limit
- $0\nu\beta\beta$ and conservative cosmology currently roughly same
- cosmology strongly disfavors a signal in KATRIN

All need to be pursued!

Neutrino Mass Observables

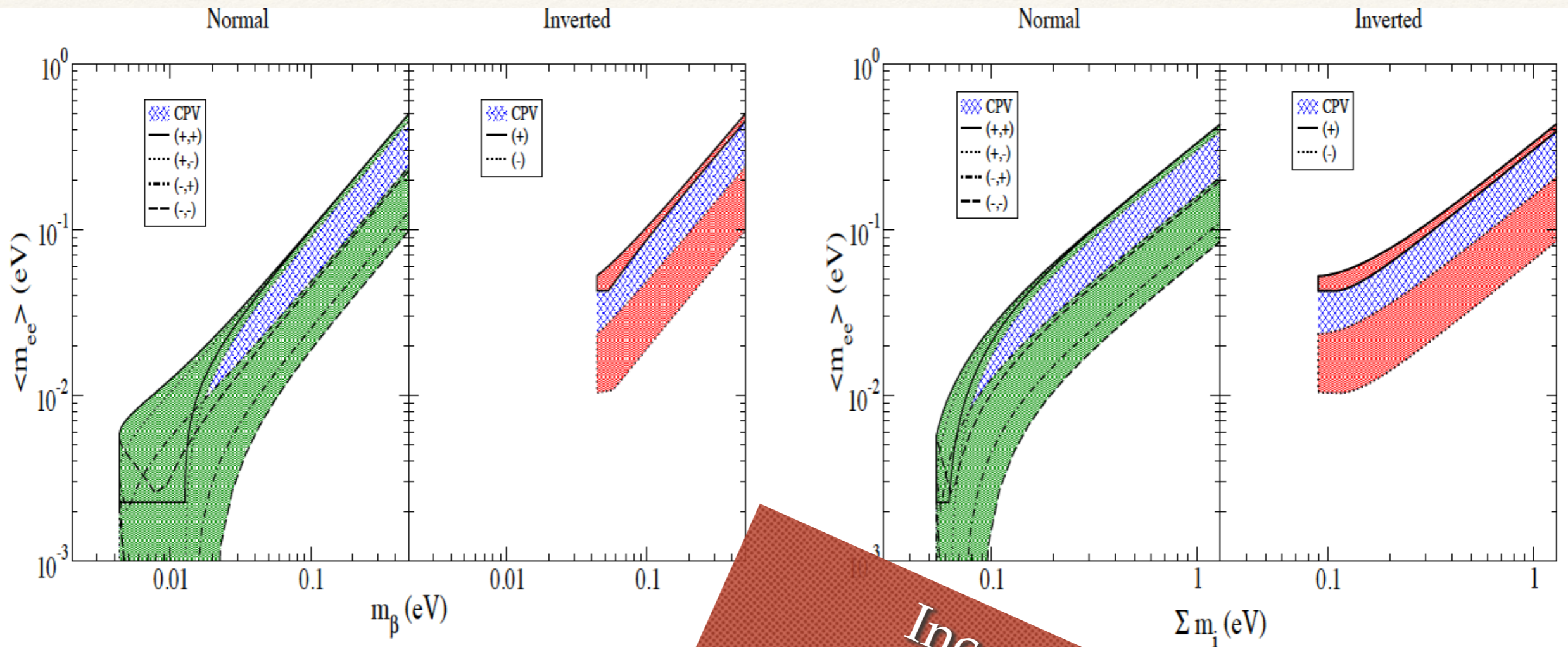


Consistency would be
 spectacular confirmation
 of 3 Majorana neutrino
 paradigm

complete complementarity
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Neutrino Mass Observables

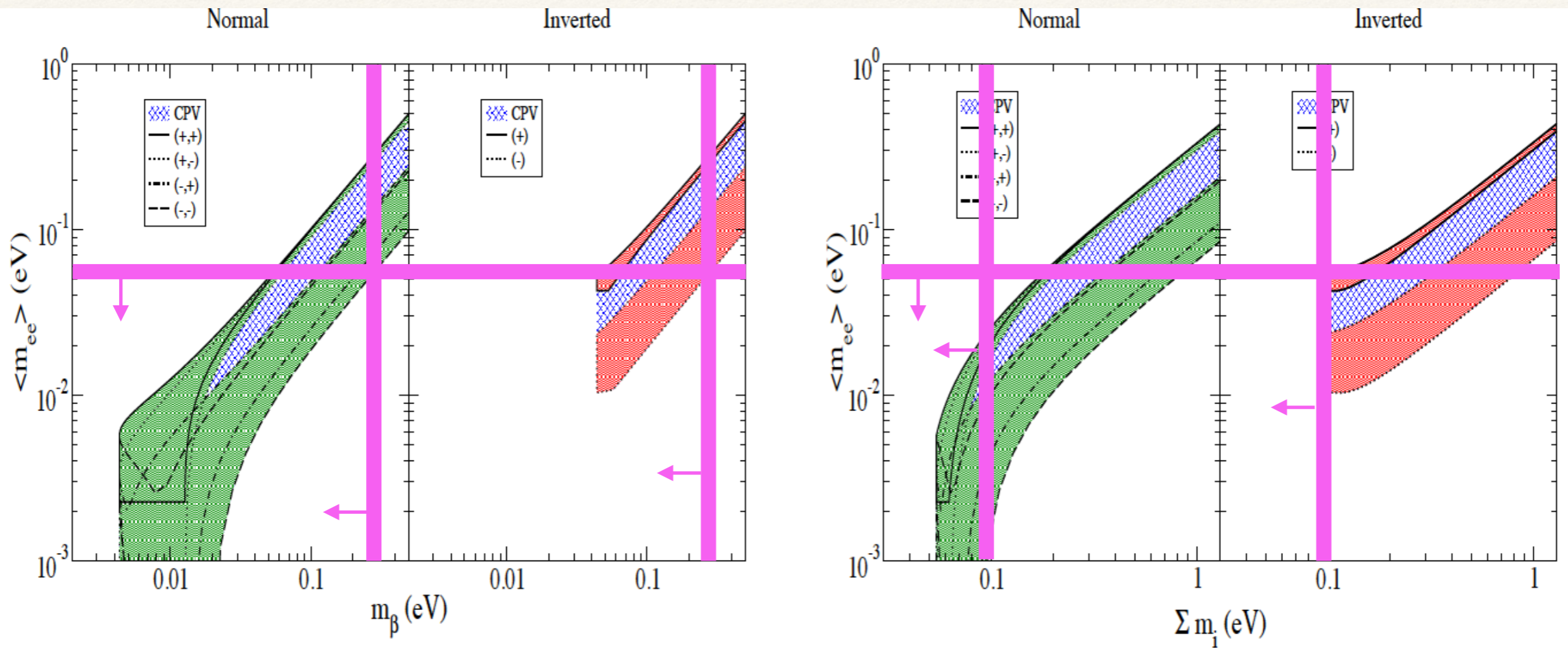


Inconsistencies would be major discovery!

complete complementarity of observables

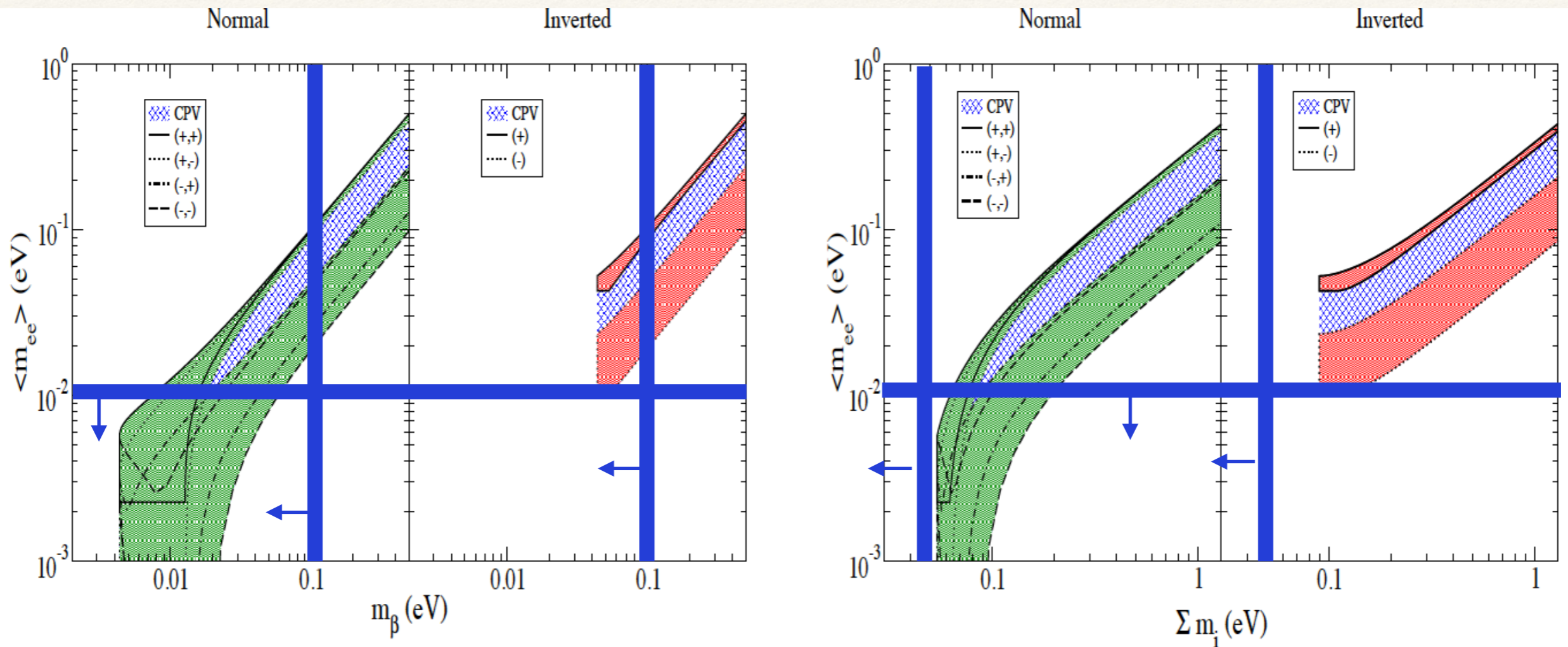
- $0\nu\beta\beta$ rule (KATRIN-limit)
- $0\nu\beta\beta$ and conservative cosmology currently roughly same
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Neutrino Mass Observables



near future

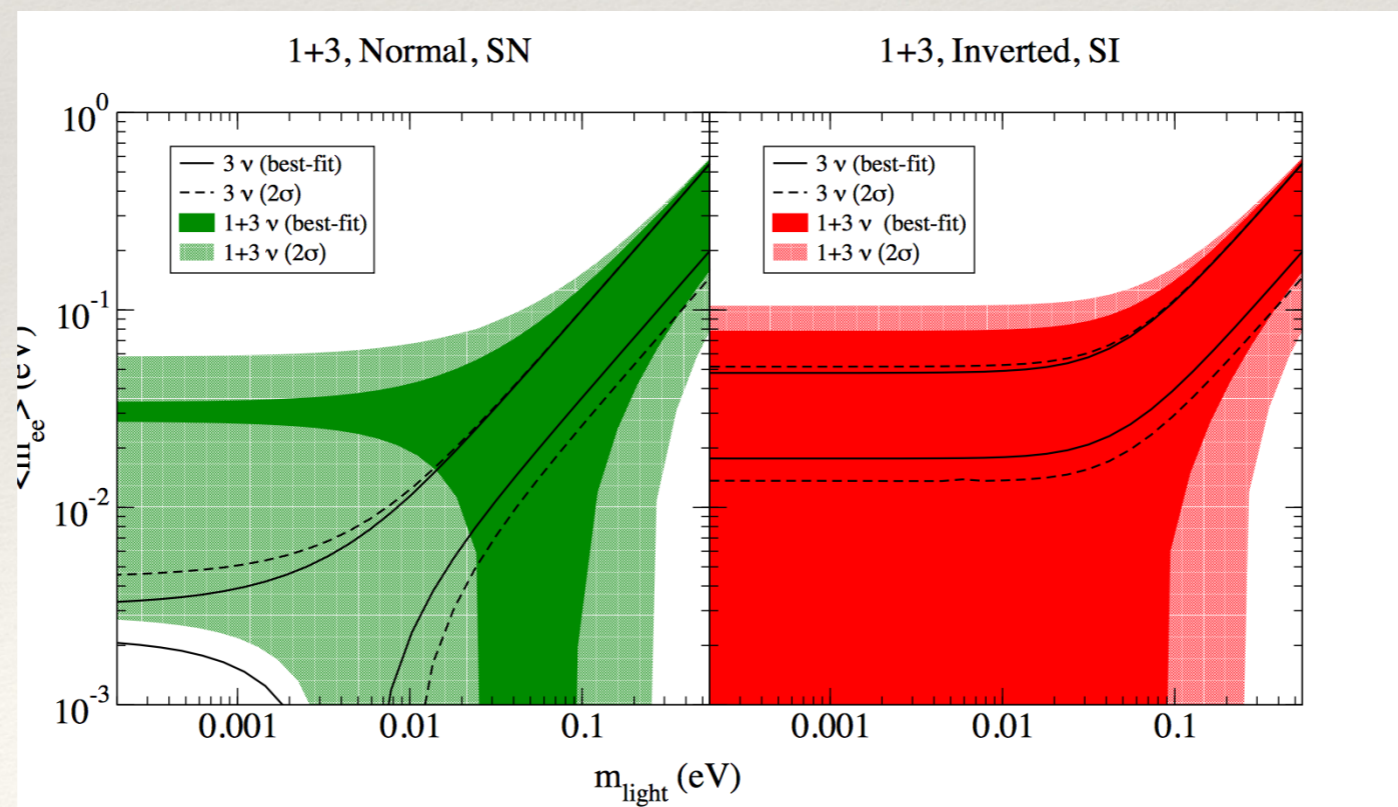
Neutrino Mass Observables



far future

Sterile Neutrinos

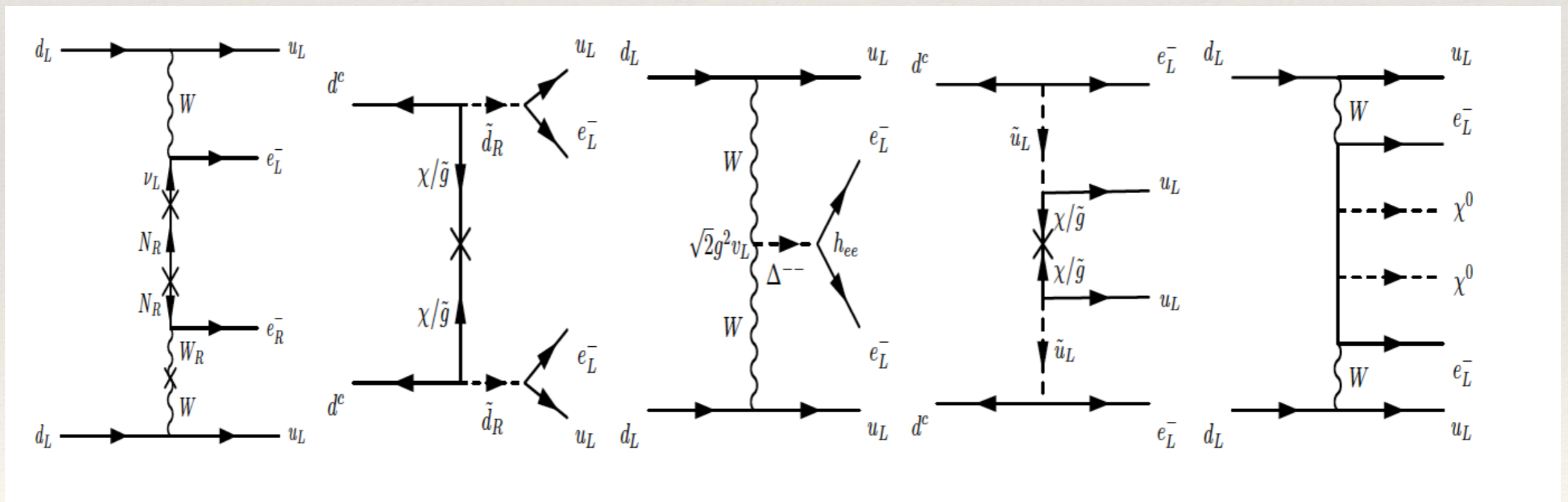
- ❖ are there sterile states (LSND / reactor / MiniBooNE, etc.) with mass $\Delta m^2 \approx \text{eV}^2$ and mixing $U_{e4} \approx 0.1$?
- ❖ would make m_{ee} sum of 4 terms with sterile contribution $|U_{e4}|^2 \sqrt{\Delta m^2}$ that can cancel almost completely contribution of IH!
- ❖ usual pheno completely turned around!



*Barry, WR, Zhang,
JHEP1107*

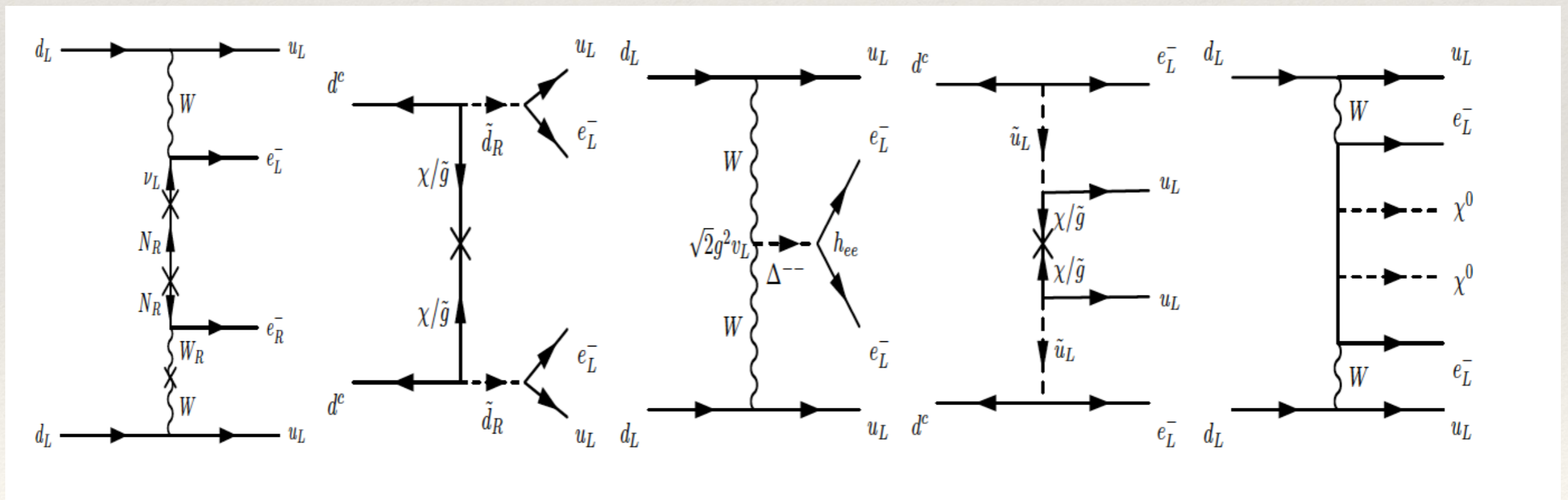
Non-Standard Interpretations

- ❖ There is at least one other mechanism leading to Neutrinoless Double Beta Decay and its contribution is at least of the same order as the light neutrino exchange mechanism



Non-Standard Interpretations

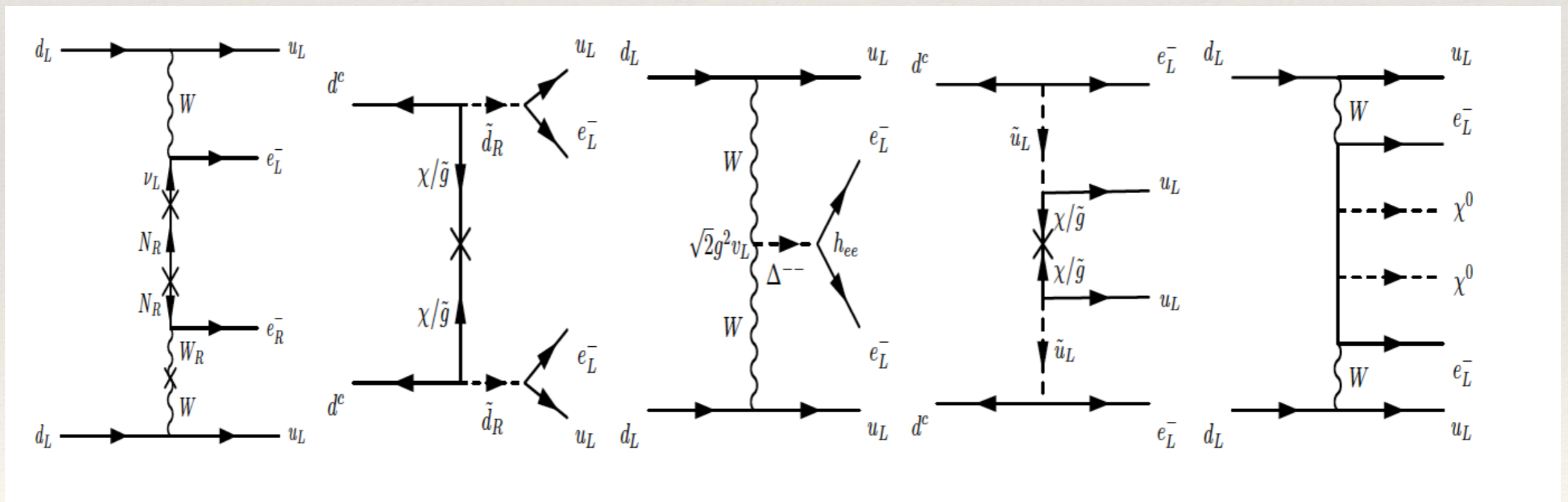
- ❖ There is at least one other mechanism leading to Neutrinoless Double Beta Decay and its contribution is at least of the same order as the light neutrino exchange mechanism



$\Rightarrow 0\nu\beta\beta$ is not a neutrino mass experiment!

Non-Standard Interpretations

- ❖ There is at least one other mechanism leading to Neutrinoless Double Beta Decay and its contribution is at least of the same order as the light neutrino exchange mechanism

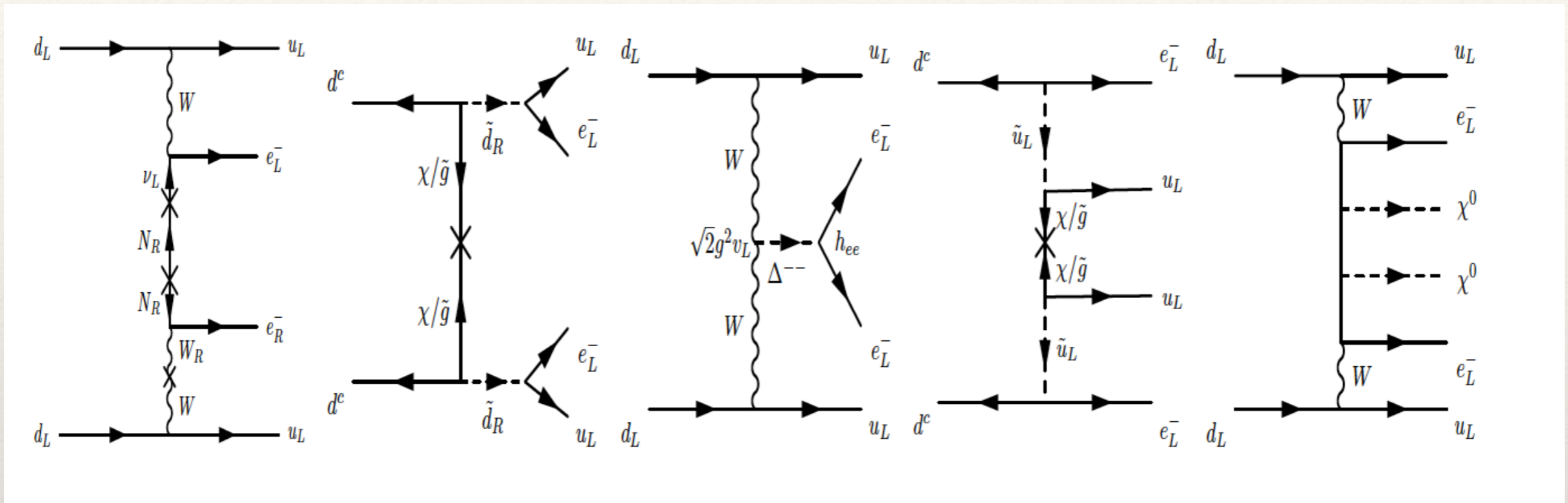


⇒ need to solve the „inverse problem“

Non-Standard Interpretations

mechanism	physics parameter	current limit	test
light neutrino exchange	$ U_{ei}^2 m_i $	0.2 eV	oscillations, cosmology, neutrino mass
heavy neutrino exchange	$\left \frac{S_{ei}^2}{M_i} \right $	$2 \times 10^{-8} \text{ GeV}^{-1}$	LFV, collider
heavy neutrino and RHC	$\left \frac{V_{ei}^2}{M_i M_{WR}^4} \right $	$4 \times 10^{-16} \text{ GeV}^{-5}$	flavor, collider
Higgs triplet and RHC	$\left \frac{(M_R)_{ee}}{m_{\Delta_R}^2 M_{WR}^4} \right $	$10^{-15} \text{ GeV}^{-1}$	flavor, collider e^- distribution
λ -mechanism with RHC	$\left \frac{U_{ei} \tilde{S}_{ei}}{M_{WR}^2} \right $	$1.4 \times 10^{-10} \text{ GeV}^{-2}$	flavor, collider, e^- distribution
η -mechanism with RHC	$\tan \zeta \left U_{ei} \tilde{S}_{ei} \right $	6×10^{-9}	flavor, collider, e^- distribution
short-range \cancel{R}	$\frac{ \lambda'_{111} ^2}{\Lambda_{\text{SUSY}}^5}$ $\Lambda_{\text{SUSY}} = f(m_{\tilde{g}}, m_{\tilde{u}_L}, m_{\tilde{d}_R}, m_{\chi_i})$	$7 \times 10^{-18} \text{ GeV}^{-5}$	collider, flavor
long-range \cancel{R}	$\left \sin 2\theta^b \lambda'_{131} \lambda'_{113} \left(\frac{1}{m_{b_1}^2} - \frac{1}{m_{b_2}^2} \right) \right $ $\sim \frac{G_F}{q} m_b \frac{ \lambda'_{131} \lambda'_{113} }{\Lambda_{\text{SUSY}}^3}$	$2 \times 10^{-13} \text{ GeV}^{-2}$ $1 \times 10^{-14} \text{ GeV}^{-3}$	flavor, collider
Majorons	$ \langle g_\chi \rangle $ or $ \langle g_\chi \rangle ^2$	$10^{-4} \dots 1$	spectrum, cosmology

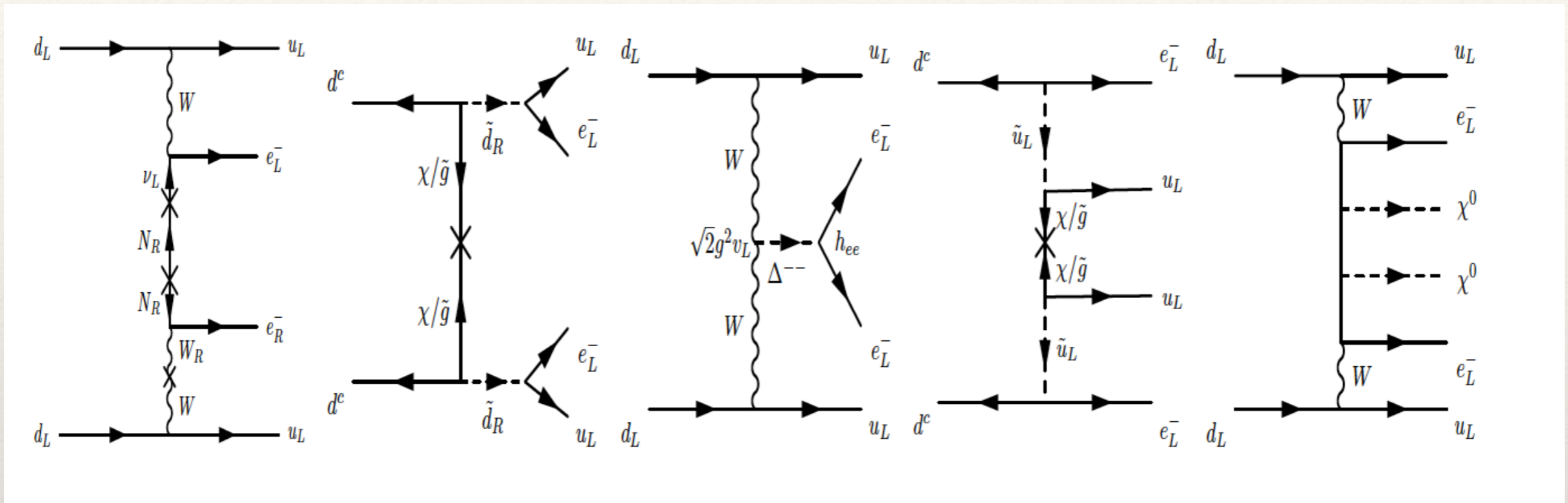
Non-Standard Interpretations



- ❖ decouples double beta decay from cosmology and KATRIN

$$\mathcal{A}_{\text{Standard}} = G_F^2 \frac{\langle m \rangle}{q^2} \quad \text{versus} \quad \mathcal{A}_{\text{Non-Standard}} = \frac{c}{M_X^5}$$

Non-Standard Interpretations

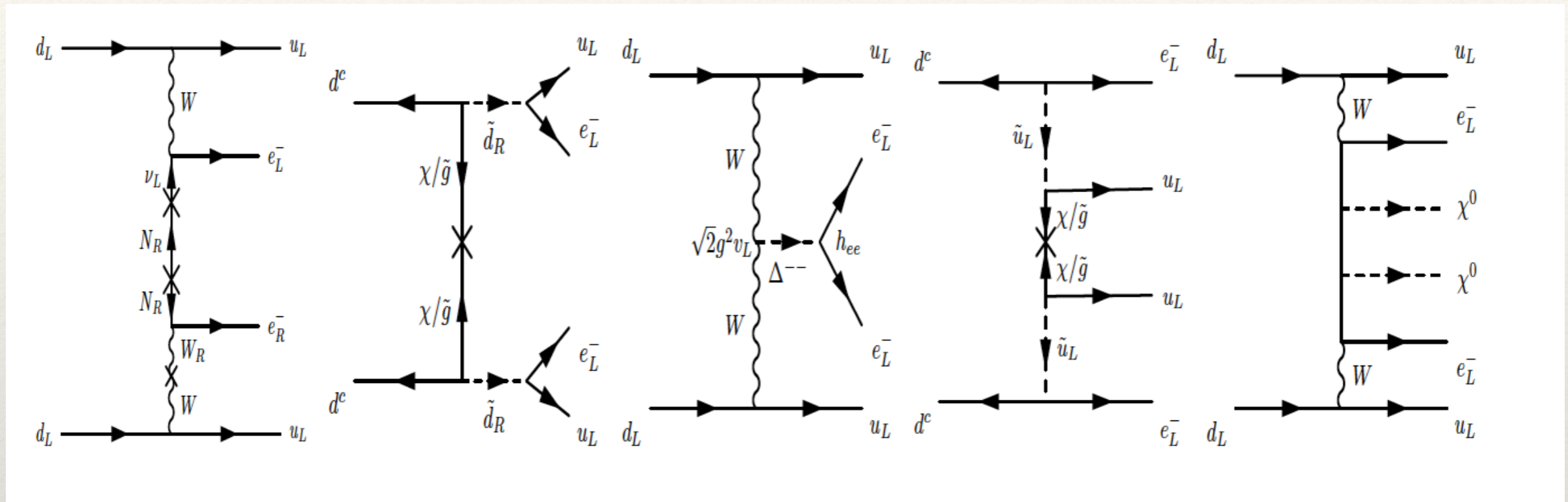


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Therefore:
 $T(\text{eV}) = T(\text{TeV})$

Non-Standard Interpretations



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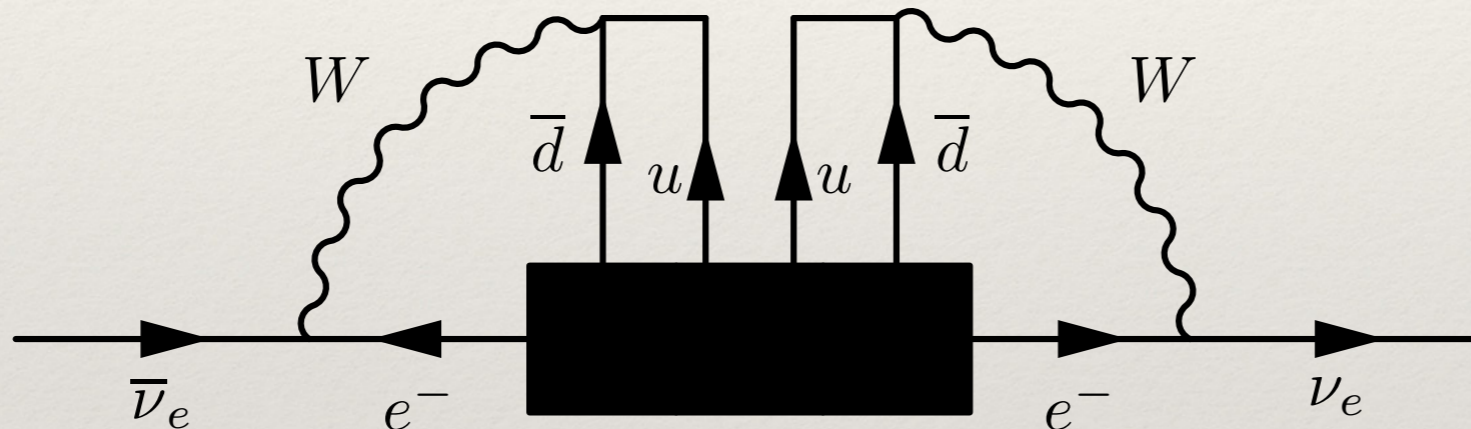
$$\mathcal{A}_{\text{Standard}} = G_F^2 \frac{\langle m \rangle}{q^2} \quad \text{versus} \quad \mathcal{A}_{\text{Non-Standard}} = \frac{c}{M_X^5}$$

Therefore:
 $T(\text{eV}) = T(\text{TeV})$

\Rightarrow Tests with LHC, LFV, etc.

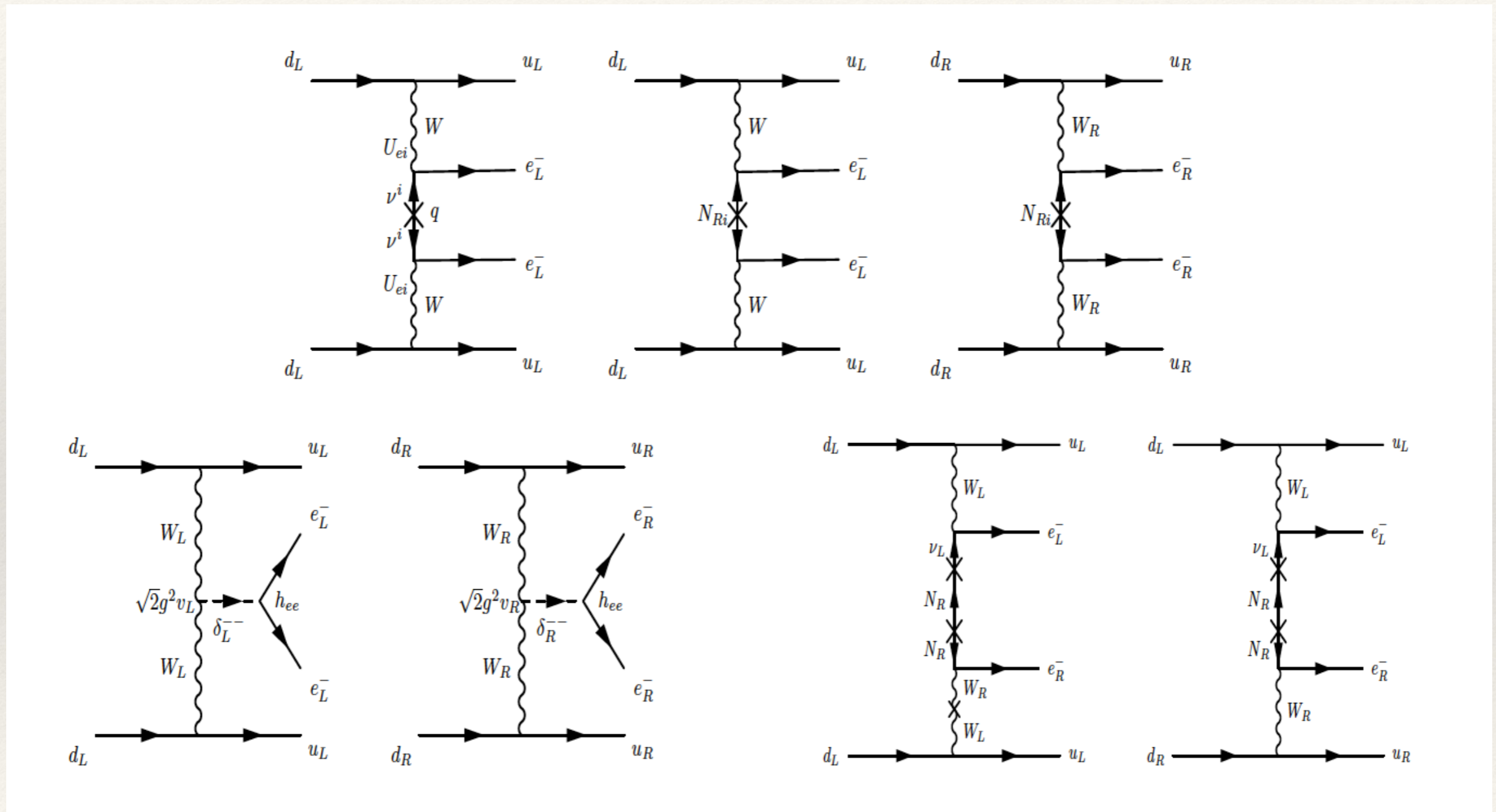
Black Box Theorem

- ❖ Whatever the mechanism, observation of $0\nu\beta\beta$ implies Majorana neutrinos (*Schechter-Valle, '82*)

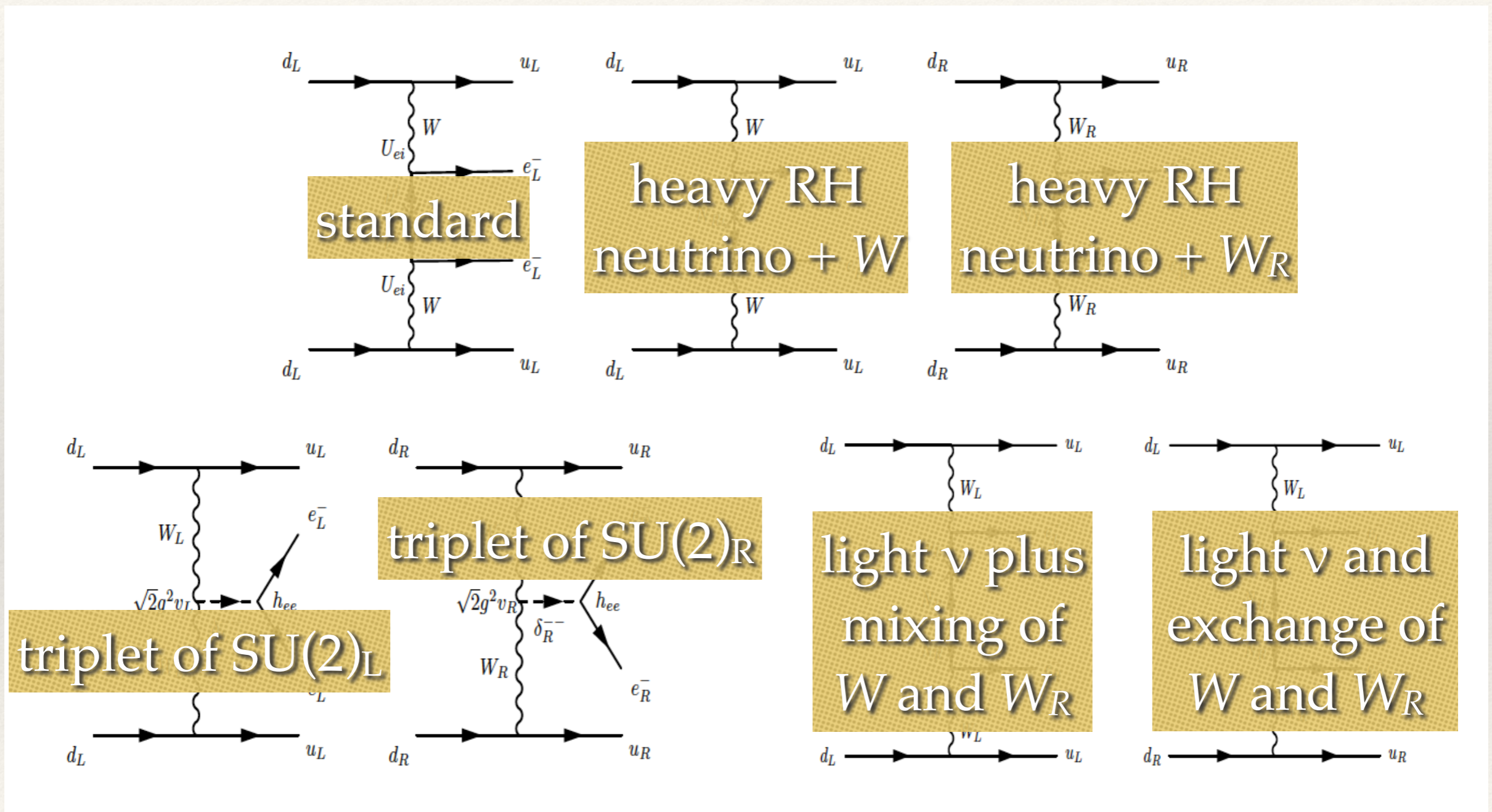


- ❖ is 4-loop diagram \Rightarrow tiny mass (*Dürr, Lindner, Merle, 1105.0901*)
- ❖ if you see $0\nu\beta\beta$: neutrinos are Majorana. If you don't, you can't tell...

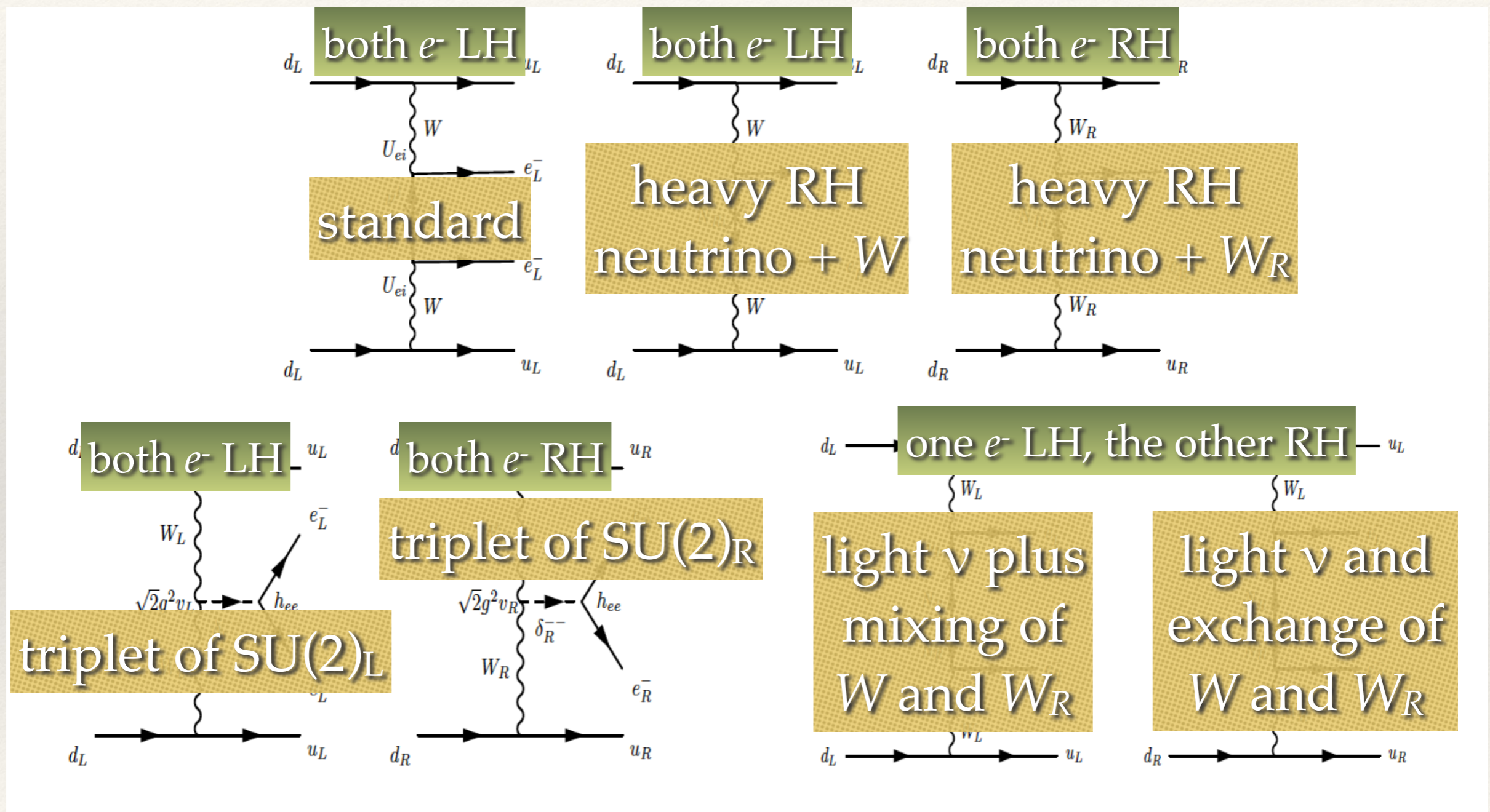
Double Beta Decay and LR-Symmetry



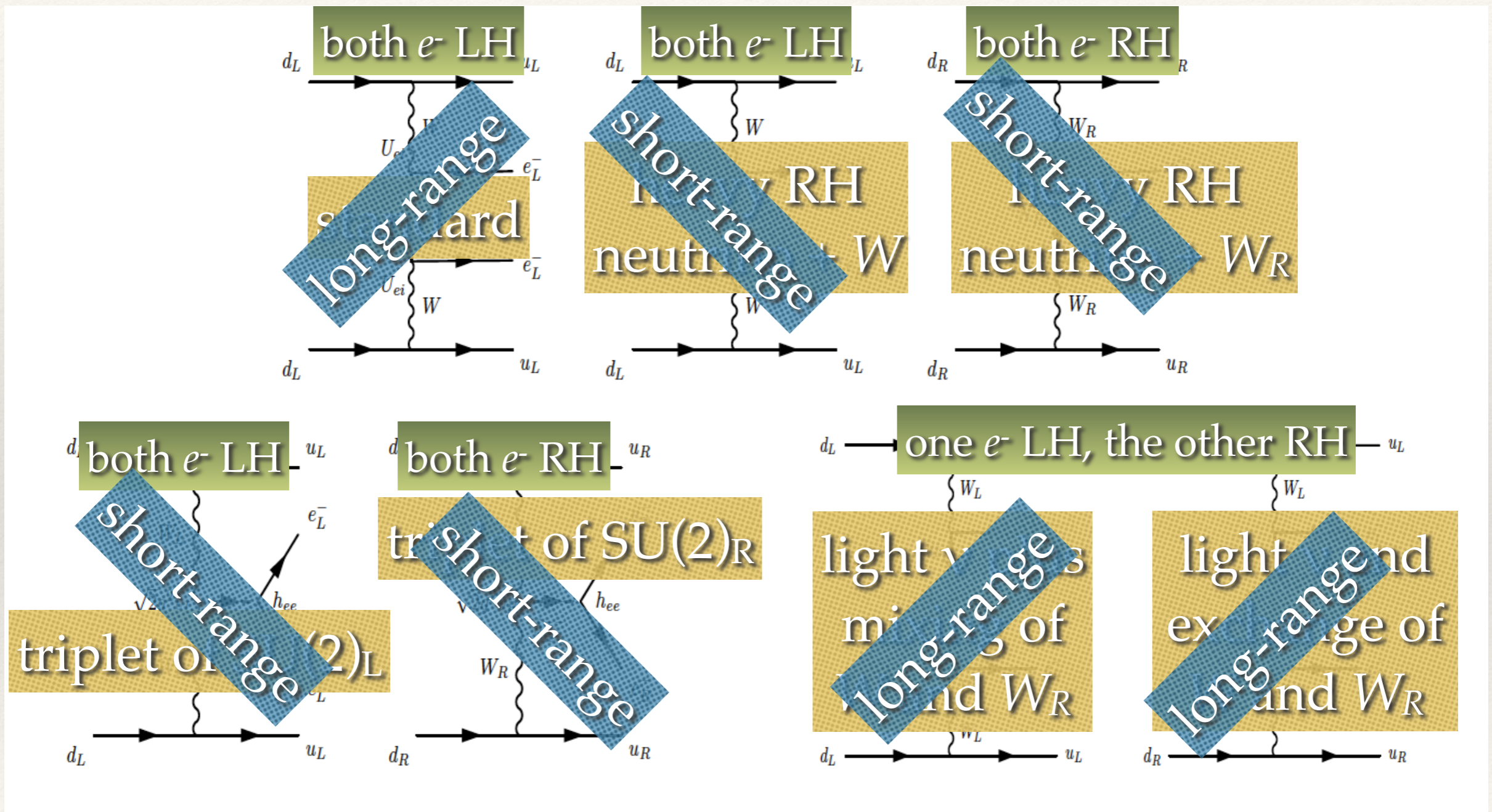
Double Beta Decay and LR-Symmetry



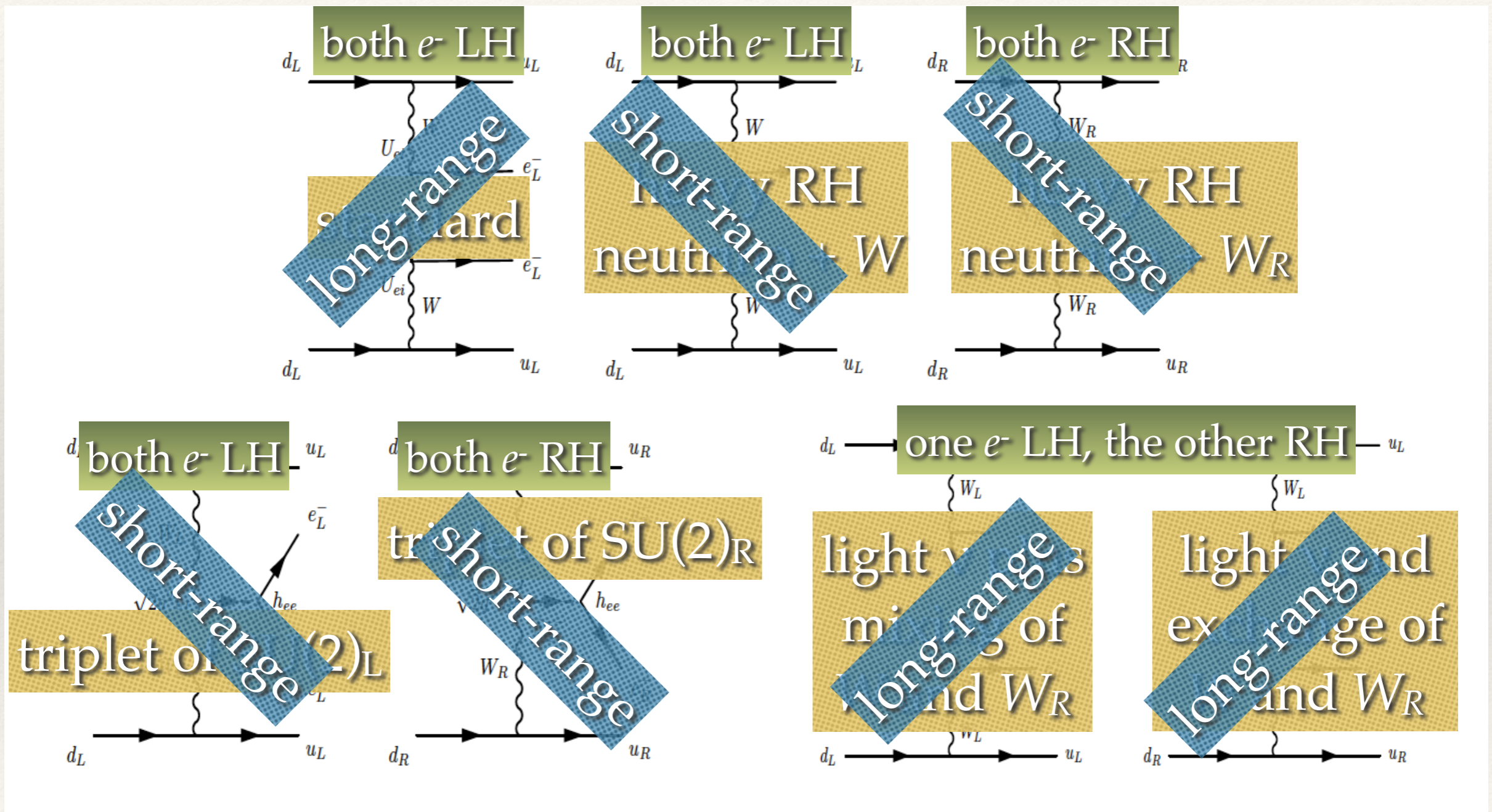
Double Beta Decay and LR-Symmetry



Double Beta Decay and LR-Symmetry



Double Beta Decay and LR-Symmetry



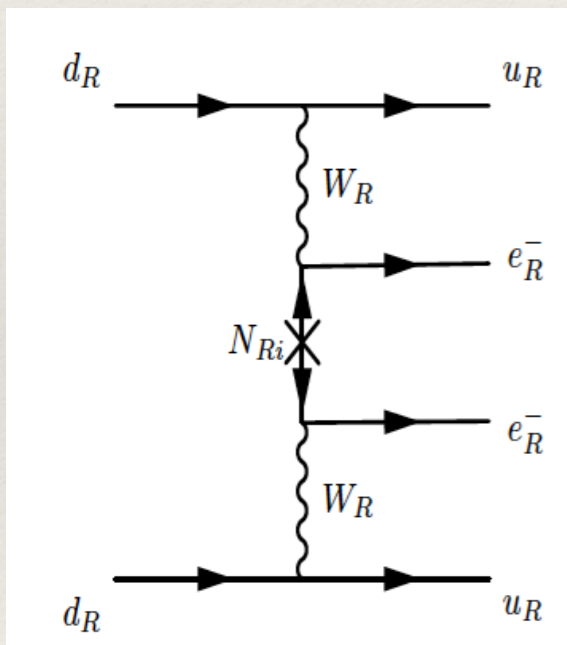
simultaneous presence / interference / ...

Double Beta Decay and LR-Symmetry

Type II dominance:

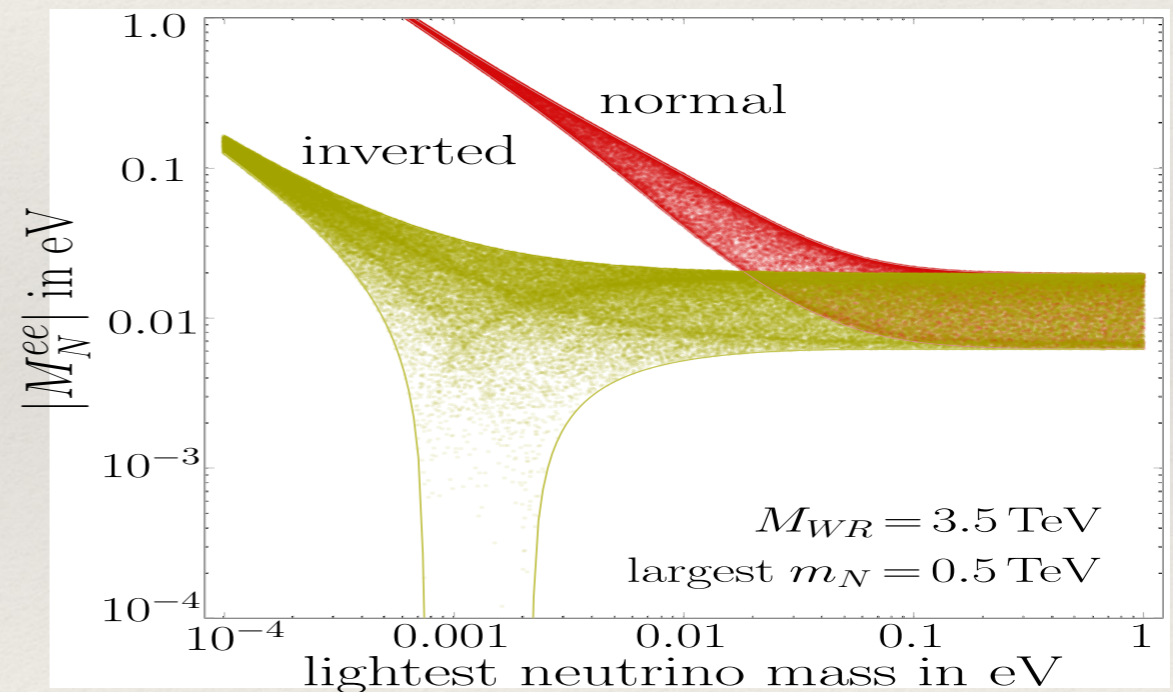
$$m_\nu = m_L - M_D^2/M_R \rightarrow m_L \text{ with } m_L \propto M_R$$

\Rightarrow right-handed neutrinos diagonalized by PMNS matrix!



$$\mathcal{A} \propto \frac{V_{ei}^2}{M_i} \propto \frac{U_{ei}^2}{m_i}$$

amplitude determined by PMNS, but $\propto 1/m_\nu$



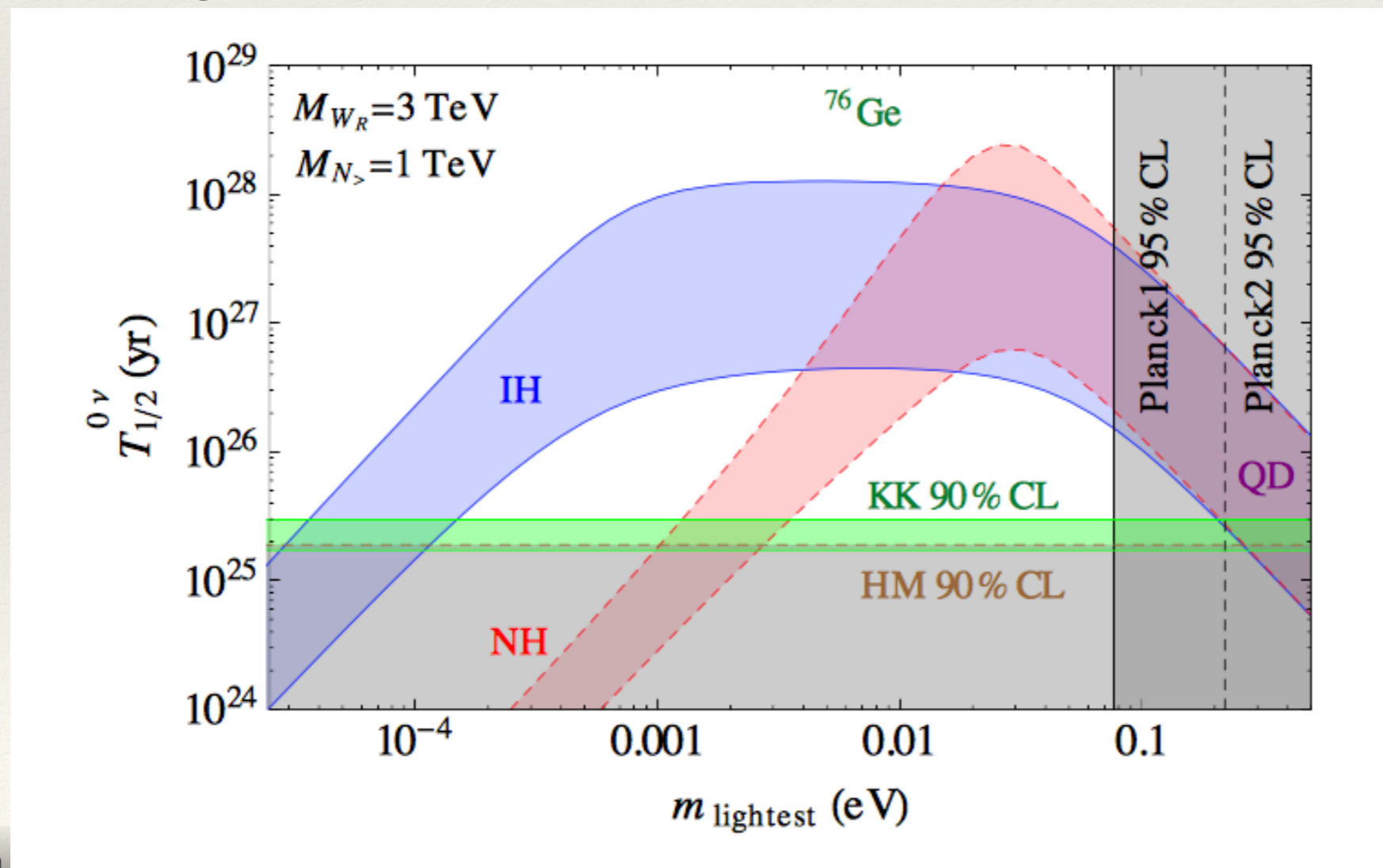
again, NH/IH turned around...

Senjanovic et al., 1011.3522

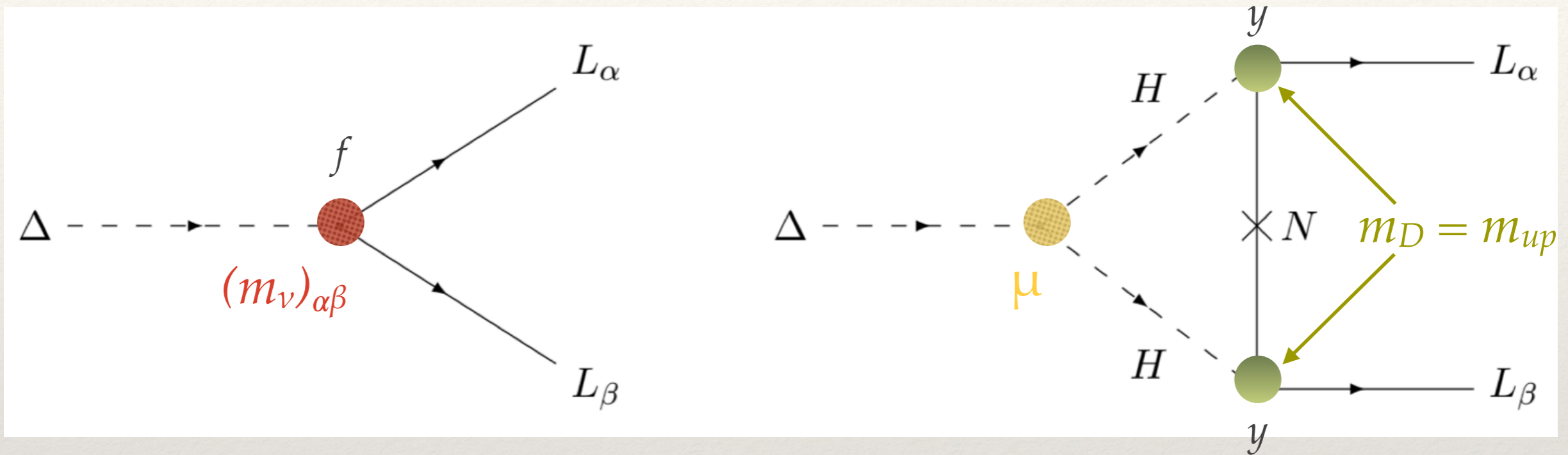
Double Beta Decay and LR-Symmetry

- ❖ add Standard and LR-diagram
- ❖ $T_{\text{St}} \propto 1/m_\nu^2$ and $T_{\text{LR}} \propto m_\nu^2$
- ❖ gives lower limit on m_ν

Barry, W.R., JHEP1309
Dev, Goswami, Mitra, WR,
PRD88



Leptogenesis



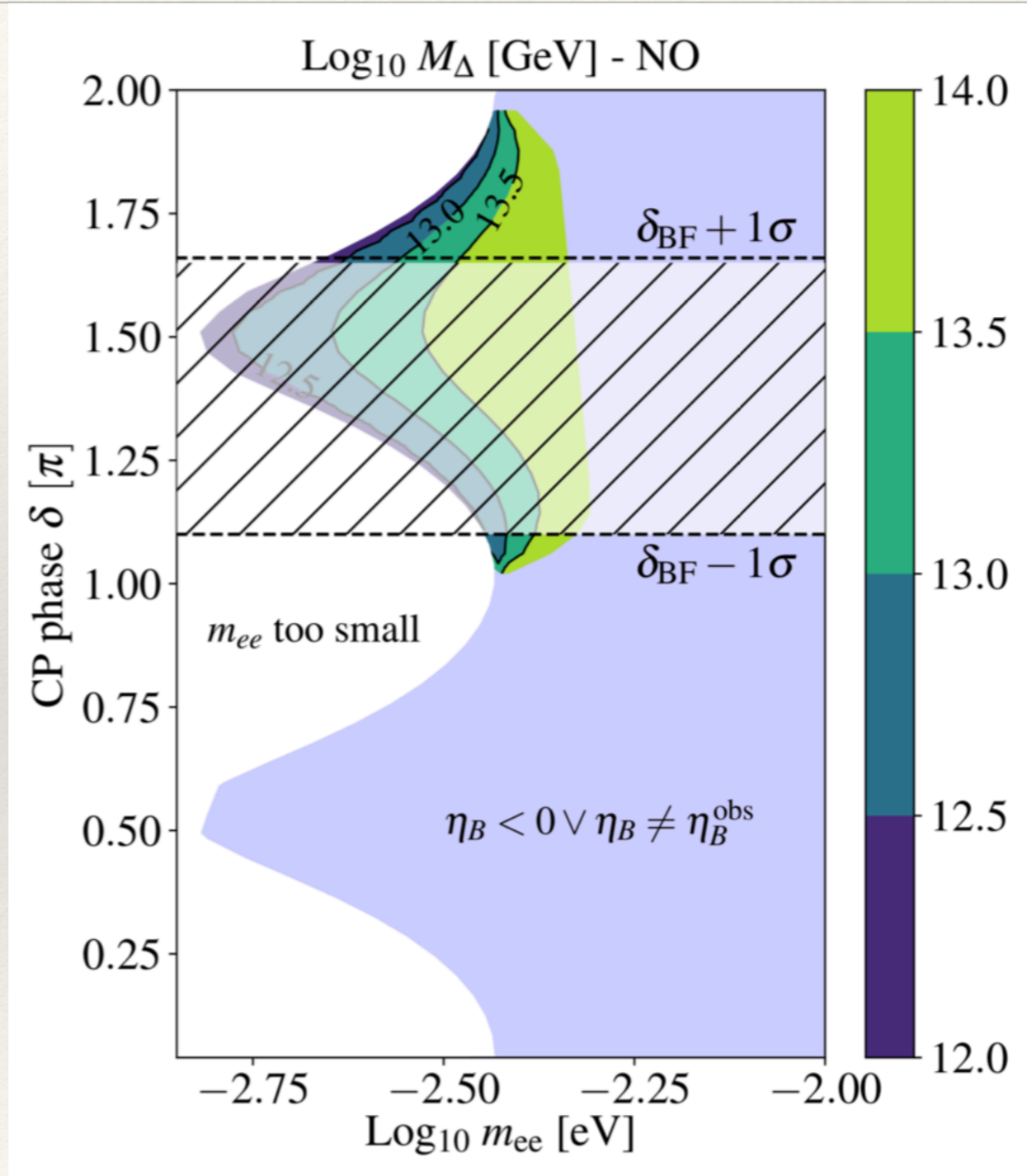
$$\epsilon_{\Delta} = -\frac{1}{8\pi} \sum_i M_i \frac{\text{Im} [\mu (y^* f y^\dagger)_{ii}]}{M_{\Delta}^2 \text{Tr} [f f^\dagger] + |\mu|^2} \ln \left(1 + \left(\frac{M_{\Delta}}{M_i} \right)^2 \right)$$

becomes proportional to:

$$\sum_{i,j} \frac{m_i}{m_j} \text{Im} \left[(U_{\tau i} U_{\tau j}^*)^2 \right]$$

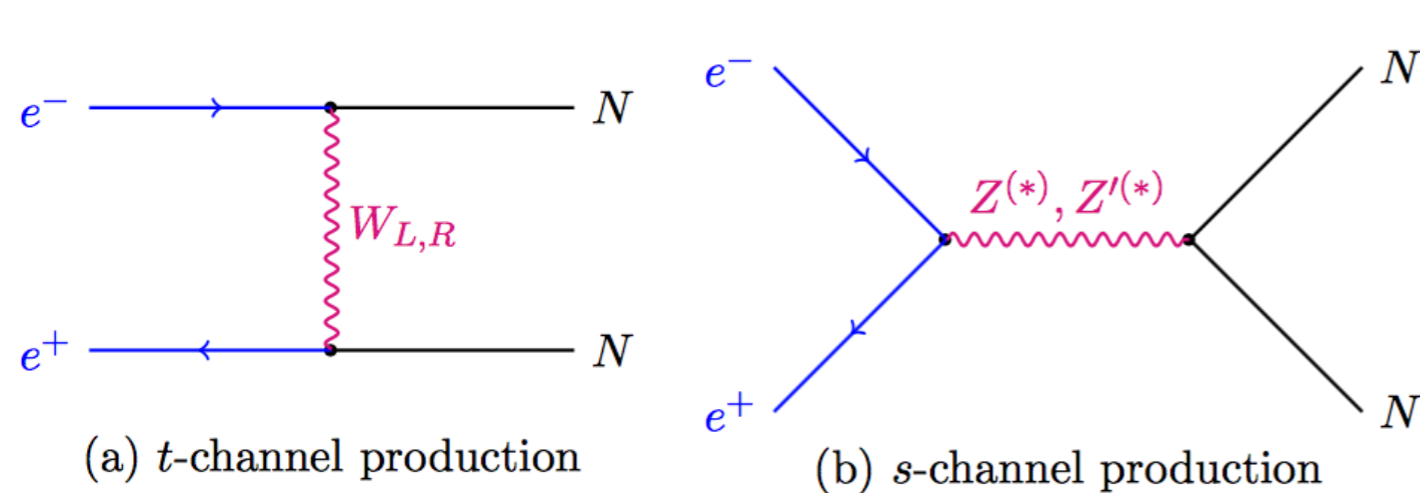
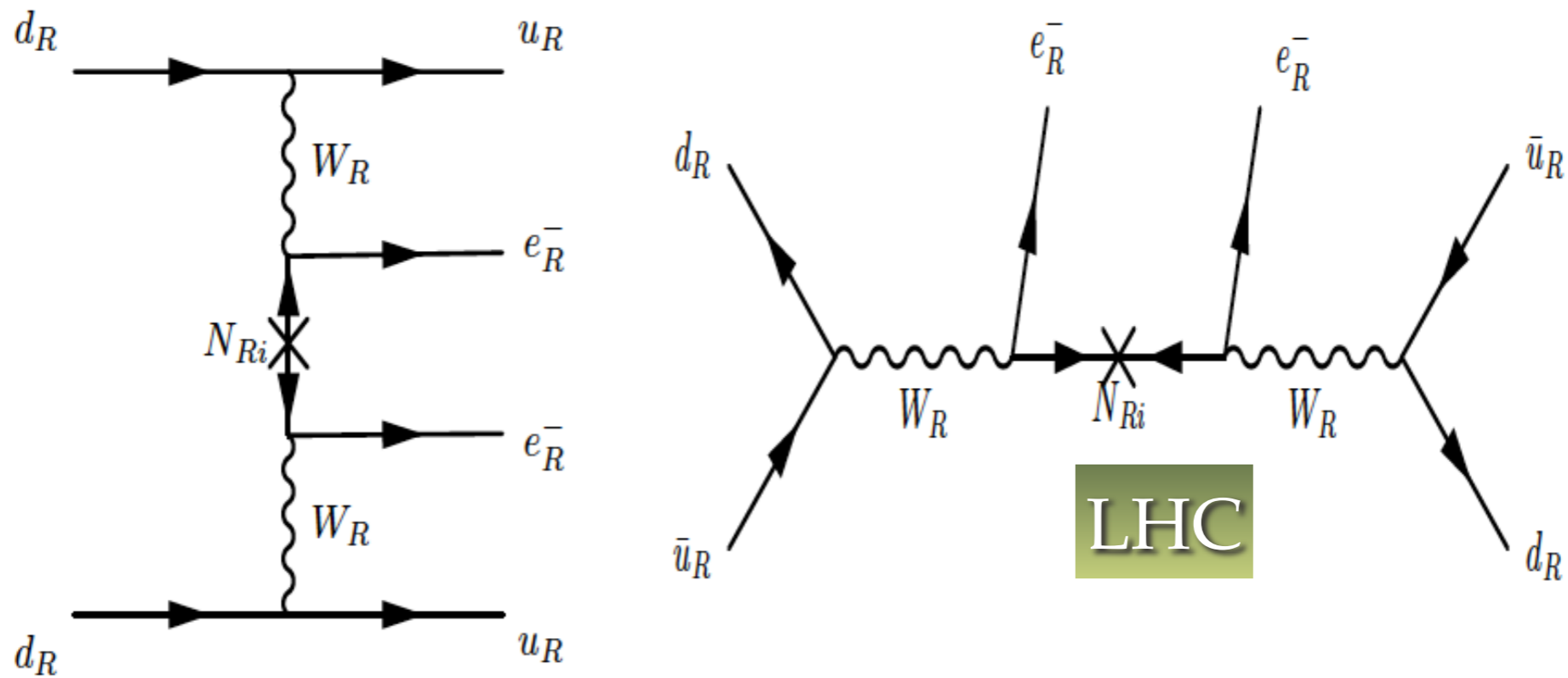
Rink, WR, Schmitz, NPB972

Leptogenesis



Rink, WR, Schmitz, NPB972

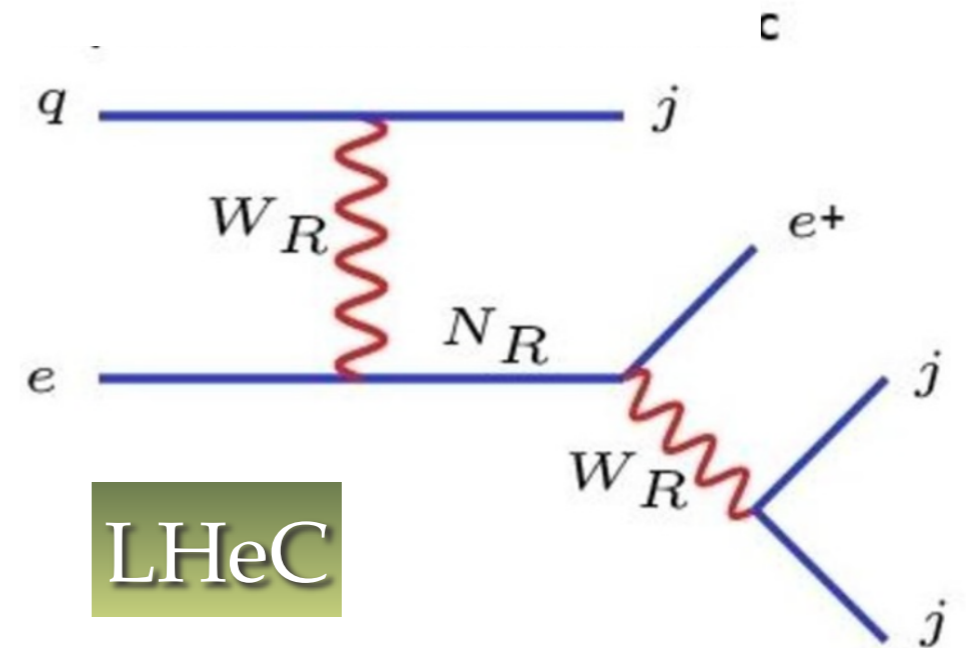
Colliders and Double Beta Decay



(a) t -channel production

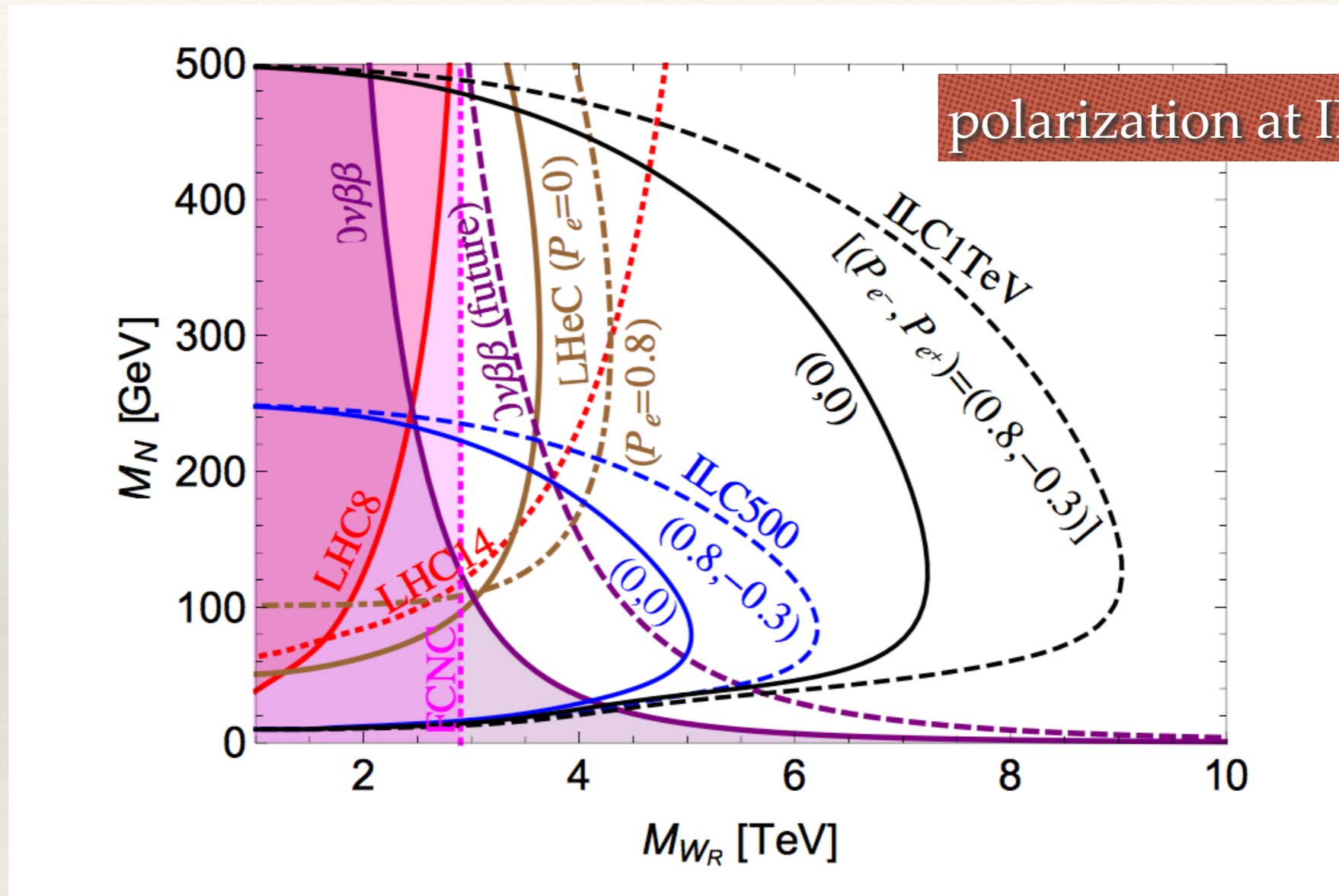
(b) s -channel production

electron-positron



LHeC

LHC and Double Beta Decay

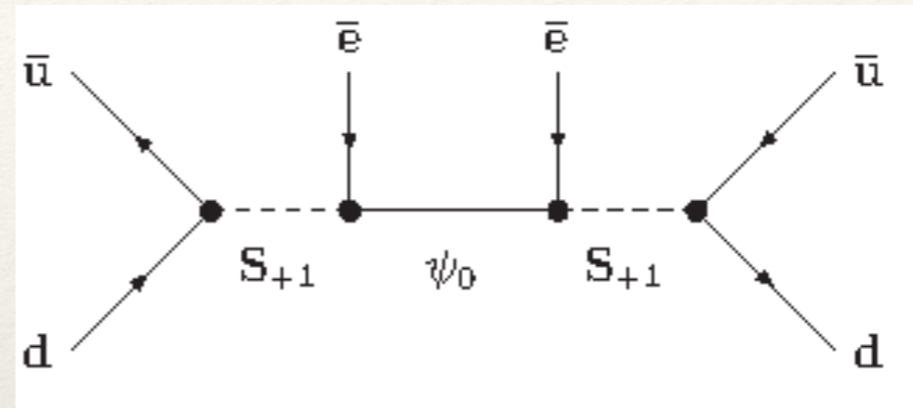
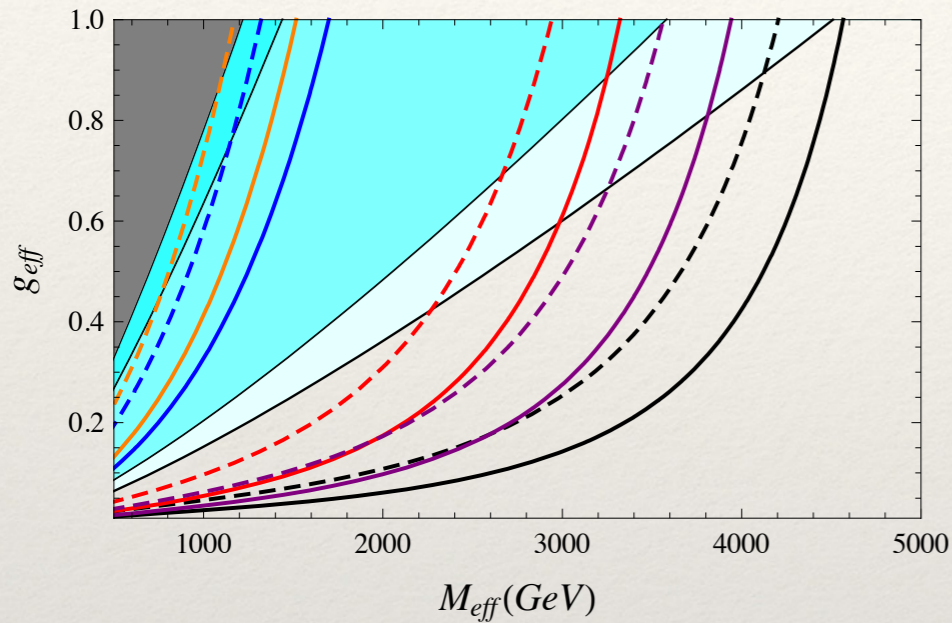


Biwal, Bhupal Dev, 1701.08751

Lindner, Queiroz, WR, Yaguna, JHEP1606

Complementarity of LHC and $0\nu\beta\beta$

Hirsch et al., 1511.03945

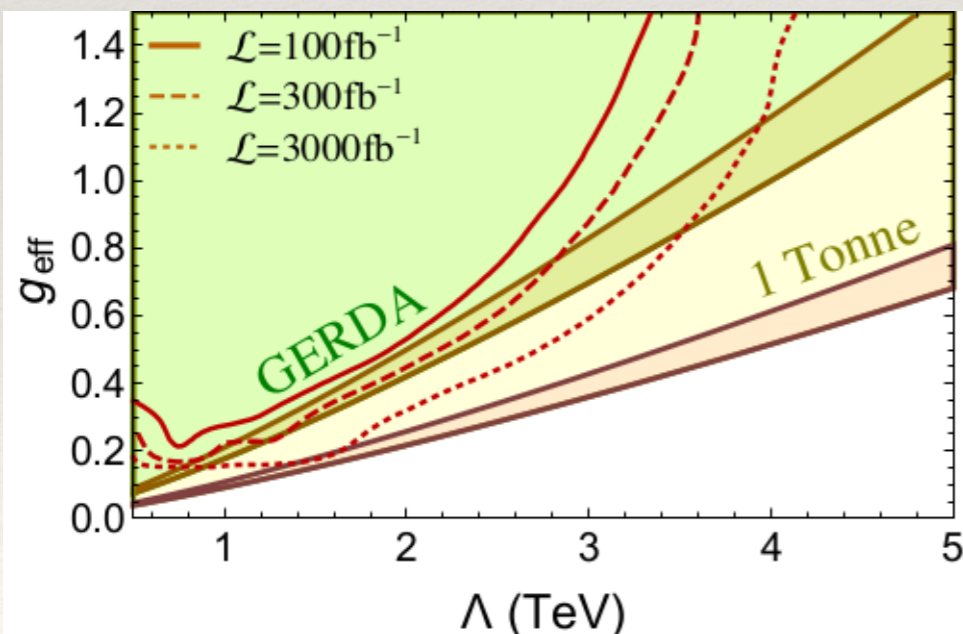


$S \sim (1, 2)$

$\psi \sim (1, 0)$

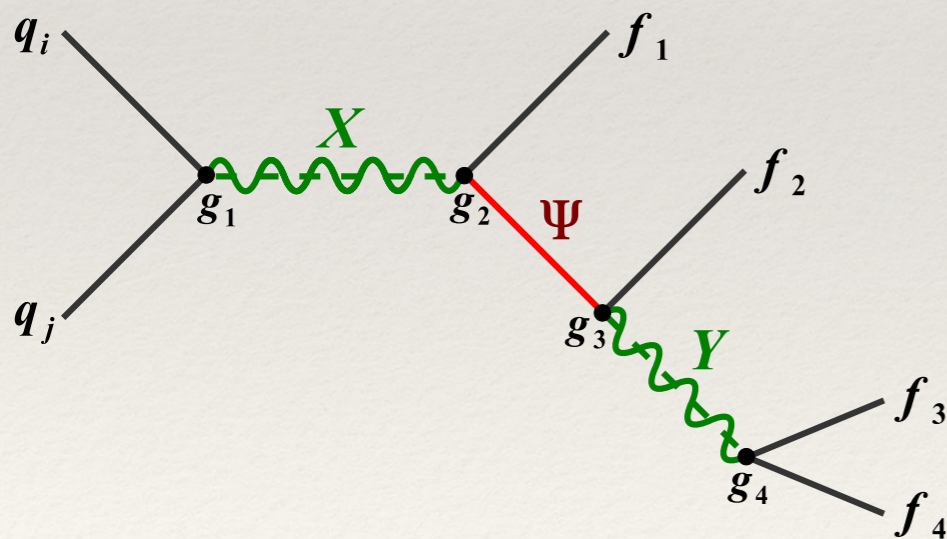
- ❖ LHC prefers $M_S > M_\psi$
- ❖ LHC has low sensitivity for small M_ψ
- ❖ include jet-fake rate, charge mis-ID, QCD corrections in $0\nu\beta\beta$, etc.
- ❖ \Rightarrow complementary

Ramsey-Musolf et al., 1508.04444



TeV-scale LNV and Baryogenesis

- ❖ Example TeV-scale W_R : leads to washout in early Universe via $e_R e_R \leftrightarrow W_R W_R$ and $e_R W_R \leftrightarrow W_R e_R$; processes stay long in equilibrium (*Frere, Hambye, Vertongen; Dev, Mohapatra; Sarkar et al.*)
- ❖ more model-independent (*Deppisch, Harz, Hirsch*):



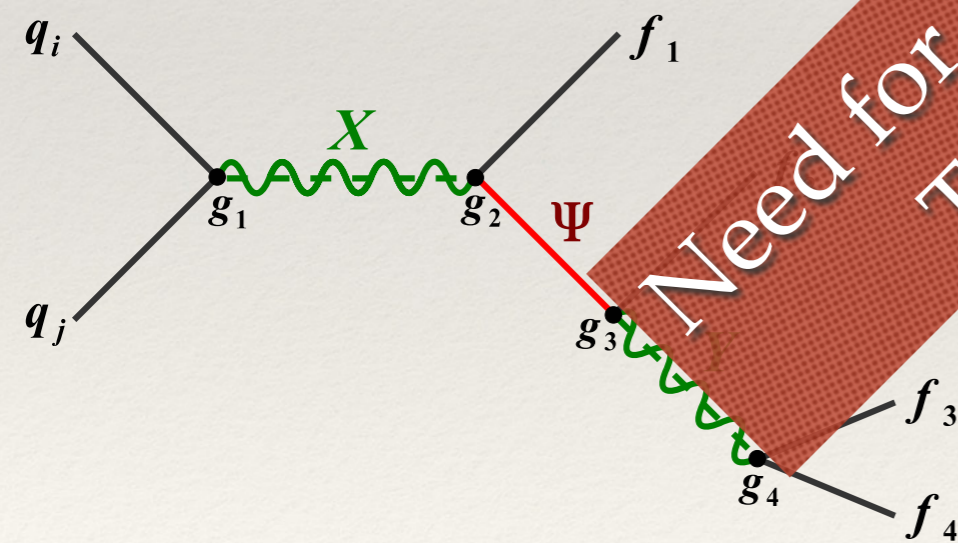
wash-out:

$$\log_{10} \frac{\Gamma_W(qq \rightarrow \ell^+ \ell^+ qq)}{H} \gtrsim 6.9 + 0.6 \left(\frac{M_X}{\text{TeV}} - 1 \right) + \log_{10} \frac{\sigma_{\text{LHC}}}{\text{fb}}$$

would need electroweak, resonant, ARS, post-sphaleron baryogenesis

TeV-scale LNV and Baryogenesis

- ❖ Example TeV-scale W_R : leads to washout in the early Universe via $e_R e_R \leftrightarrow W_R W_R$ and $W_R W_R \leftrightarrow e_R e_R$; processes stay long in equilibrium (see, e.g., *Hambye, Vertongen; Dev, Mohapatra; ...*)
- ❖ more model-independent (see, e.g., *Appelquist, Harz, Hirsch*):



Need for standard leptogenesis when TeV-scale LNV is present?

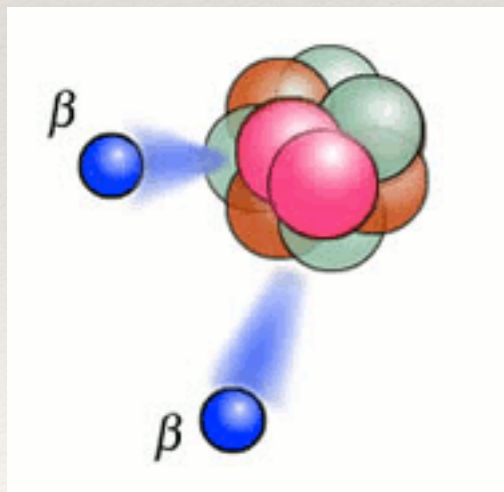
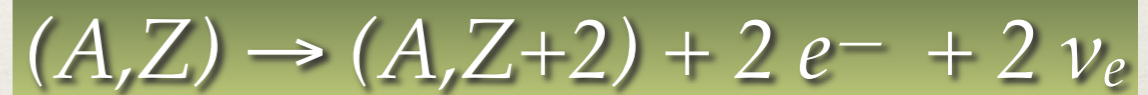
at:

$$\log_{10} \frac{\Gamma_W(qq \rightarrow \ell^+ \ell^+ qq)}{H} \gtrsim 6.9 + 0.6 \left(\frac{M_X}{\text{TeV}} - 1 \right) + \log_{10} \frac{\sigma_{\text{LHC}}}{\text{fb}}$$

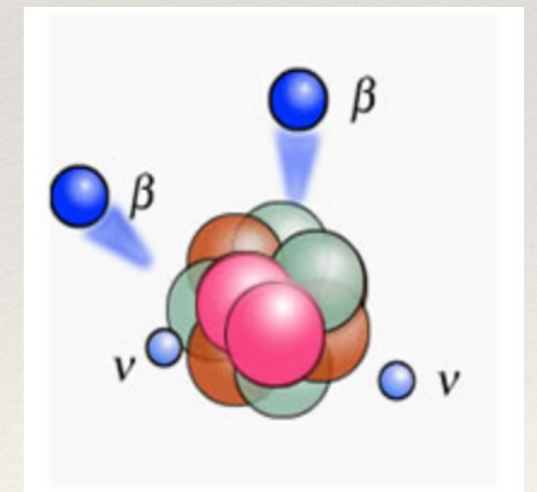
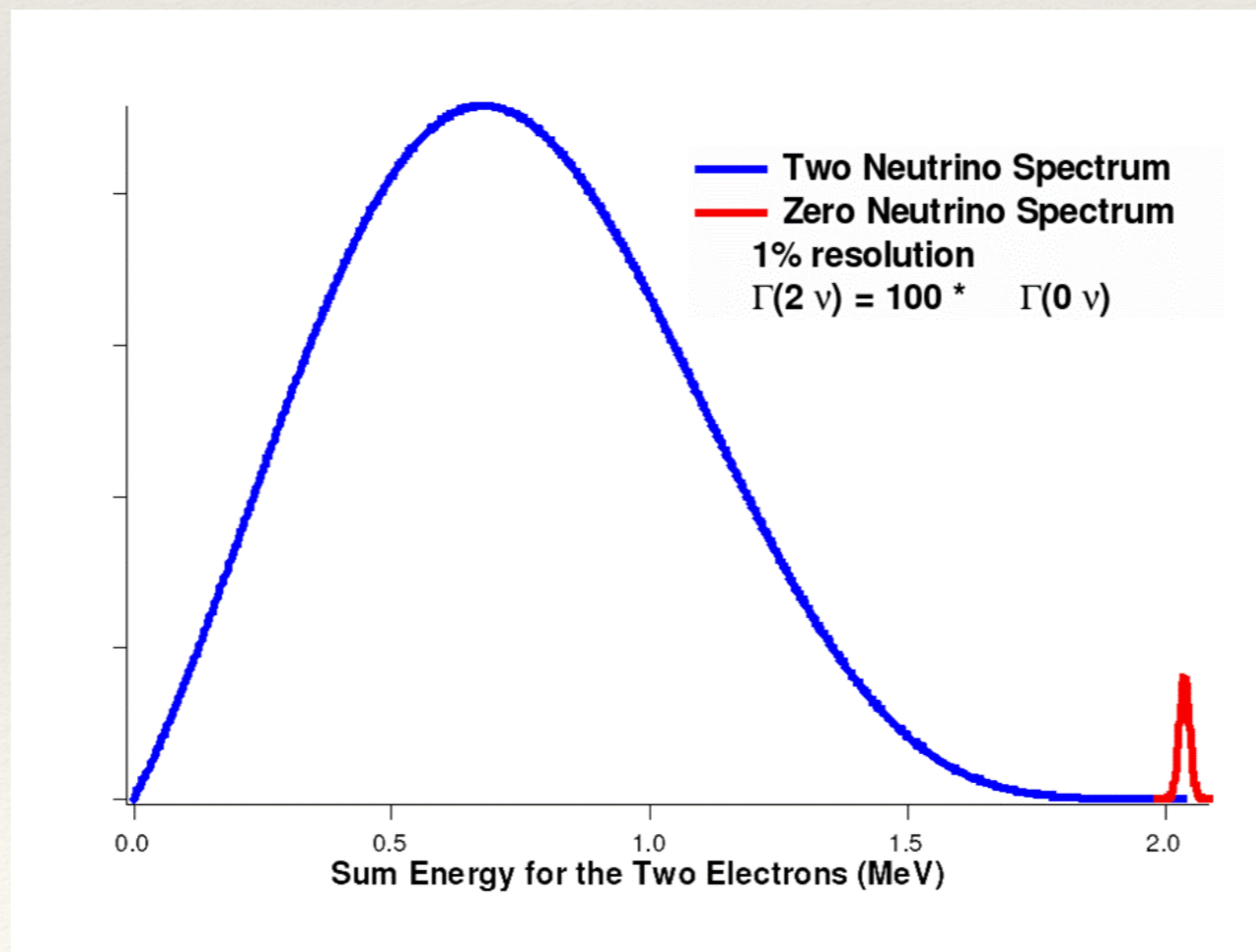
would need electroweak, resonant, ARS, post-sphaleron baryogenesis

Two Kinds of Double Beta Decay

Inevitable Background



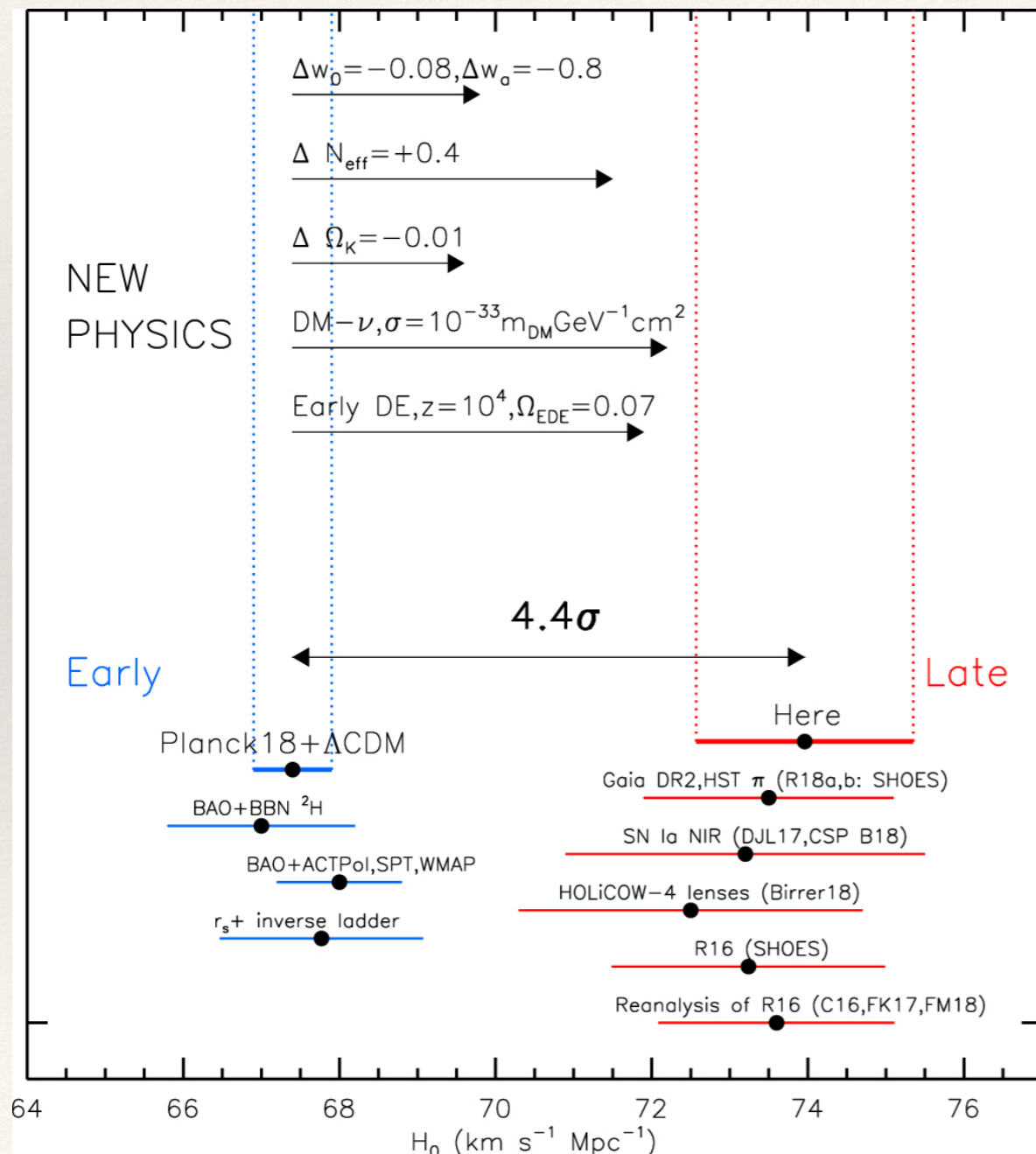
$$\Delta L = 2$$



$$\Delta L = 0$$

New Physics with $2\nu\beta\beta$

Hubble tension and new neutrino self-interactions



$$\mathcal{L}_{\nu\text{SI}}^{\text{LNC}} = G_S(\nu_e\nu_e)(\bar{\nu}_\alpha\bar{\nu}_\beta),$$

$$\mathcal{L}_{\nu\text{SI}}^{\text{LNV}} = G_S(\nu_e\nu_e)(\nu_\alpha\nu_\beta),$$

can resolve tension for strongly and „moderately“ interacting ν :

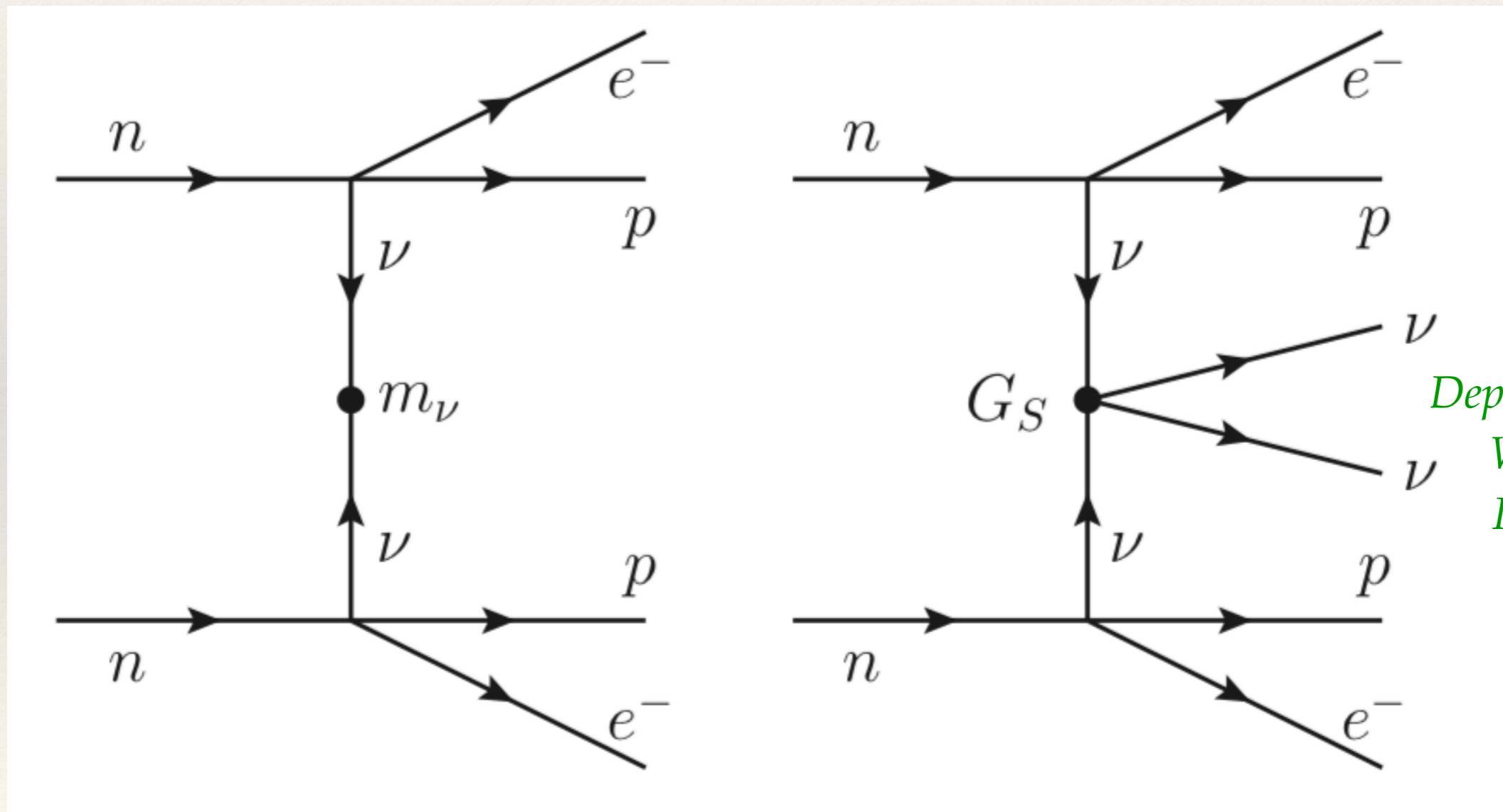
$$G_{\text{eff}} = \begin{cases} (4.7_{-0.6}^{+0.4} \text{ MeV})^{-2} & (\text{SI}\nu) \\ (89_{-61}^{+171} \text{ MeV})^{-2} & (\text{MI}\nu) \end{cases}$$

Kreisch et al., 1902.00534

(extra radiation to modify H , delays matter-radiation equality, then νSI to compensate resulting CMB modifications)

New Physics with $2\nu\beta\beta$

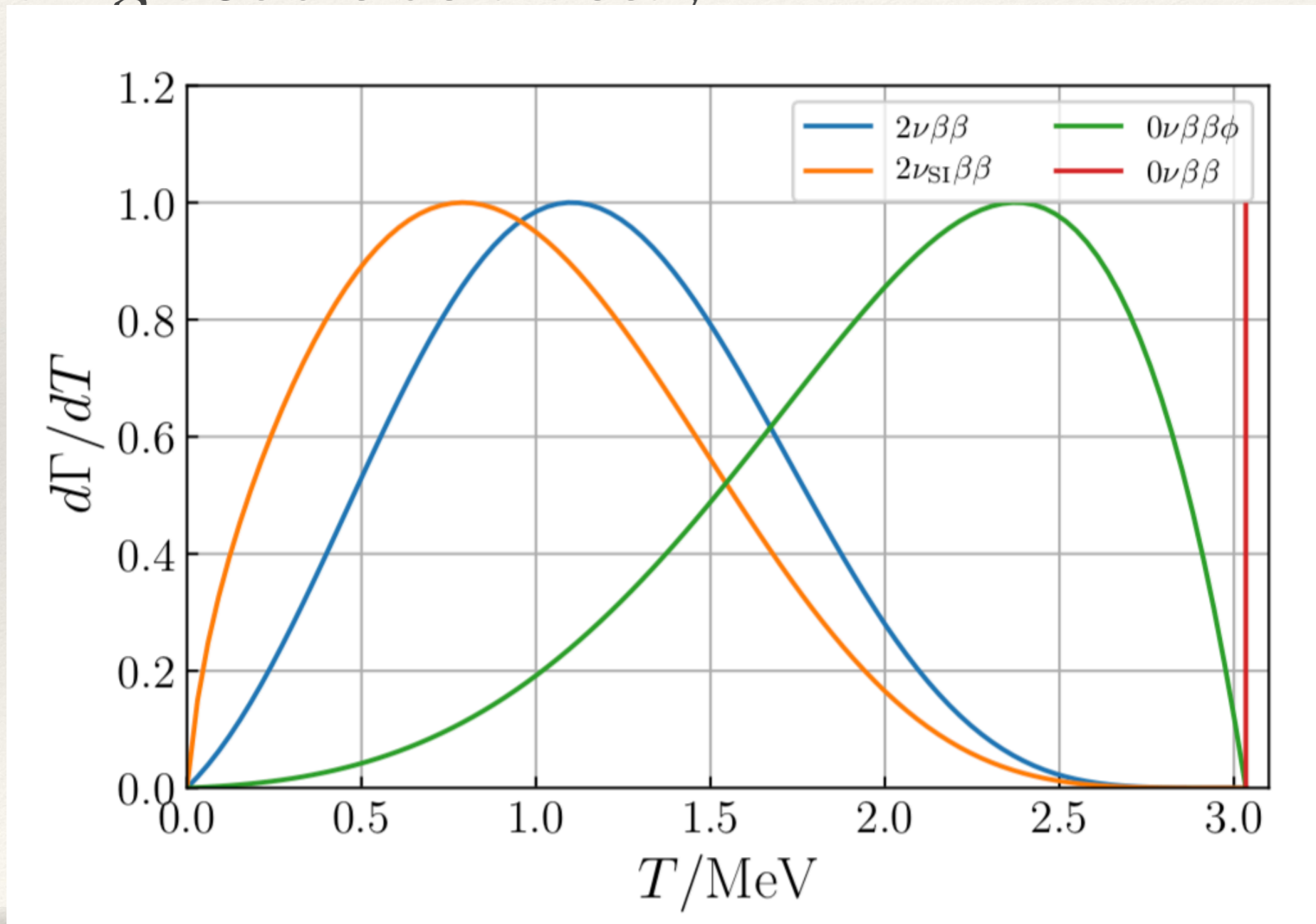
- ❖ 2-neutrino double beta decay only direct probe of 4-nu interactions:



*Deppisch, Graf,
WR, Xu,
PRD102*

New Physics with $2\nu\beta\beta$

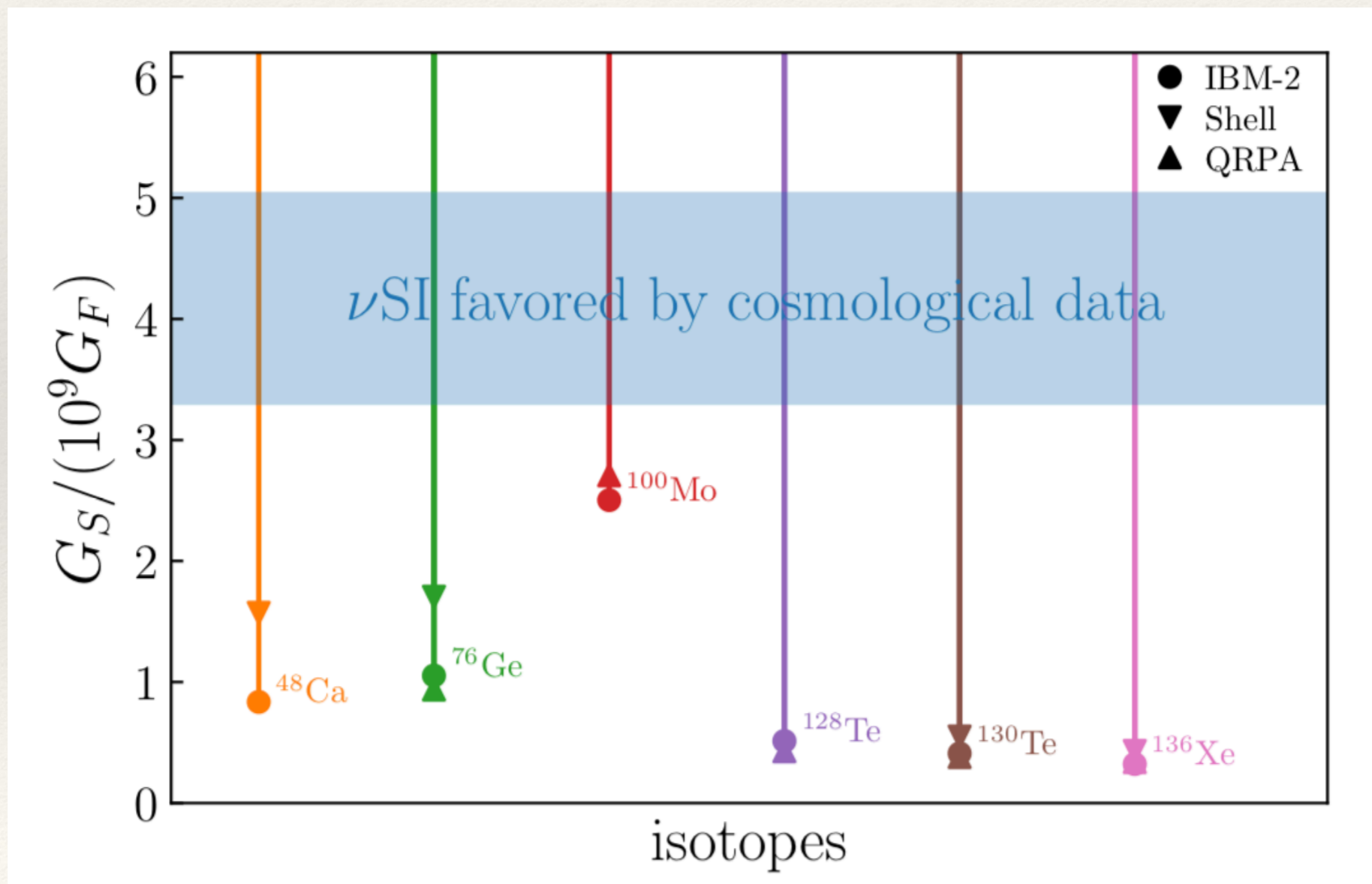
- ❖ Strong interactions ruled out by lab experiments, including double beta decay:



*Deppisch, Graf,
WR, Xu,
PRD102*

New Physics with $2\nu\beta\beta$

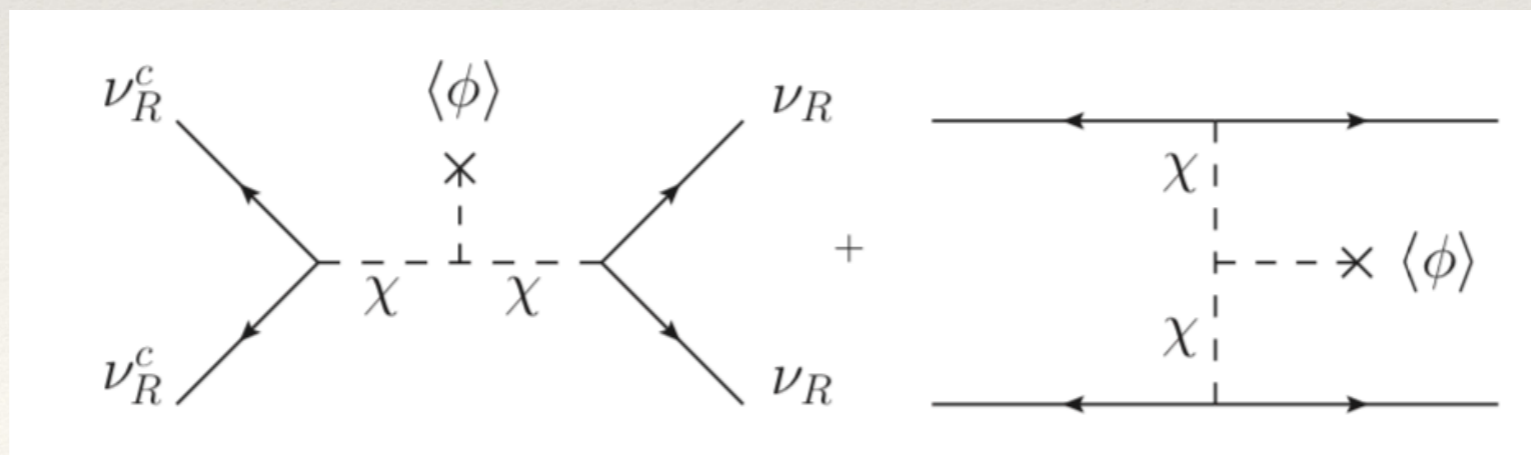
- ❖ Strong interactions ruled out by lab experiments, including double beta decay:



*Deppisch, Graf,
WR, Xu,
PRD102*

Lepton Number Violation with Dirac Neutrinos

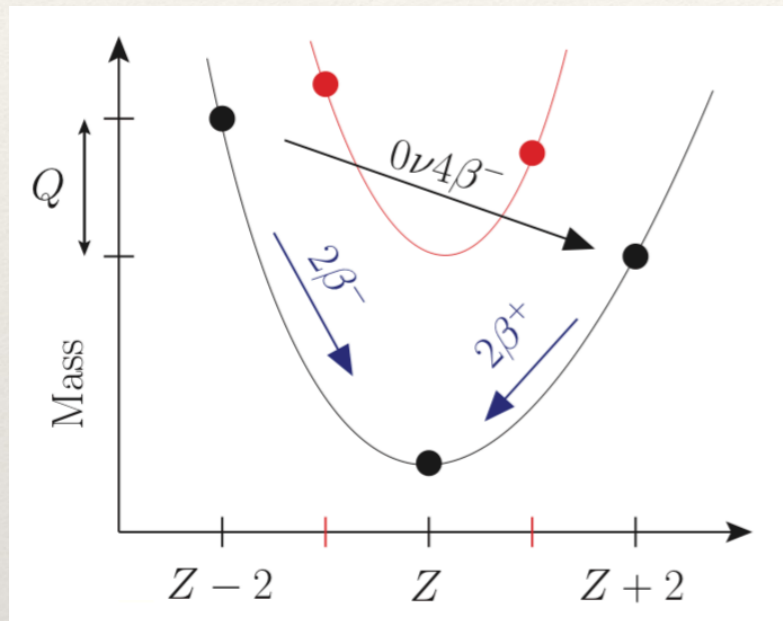
- ❖ Many models based on gauged $B-L$, broken by 2 units, hence Majorana masses and $\Delta L = 2$
- ❖ can break it also by 4 units, hence $\Delta L = 2$ forbidden, but $\Delta L = 4$ allowed!
- ❖ example: 3 RH nus with charge -1 , an inert scalar χ with charge -2 and a scalar ϕ with charge $+4$



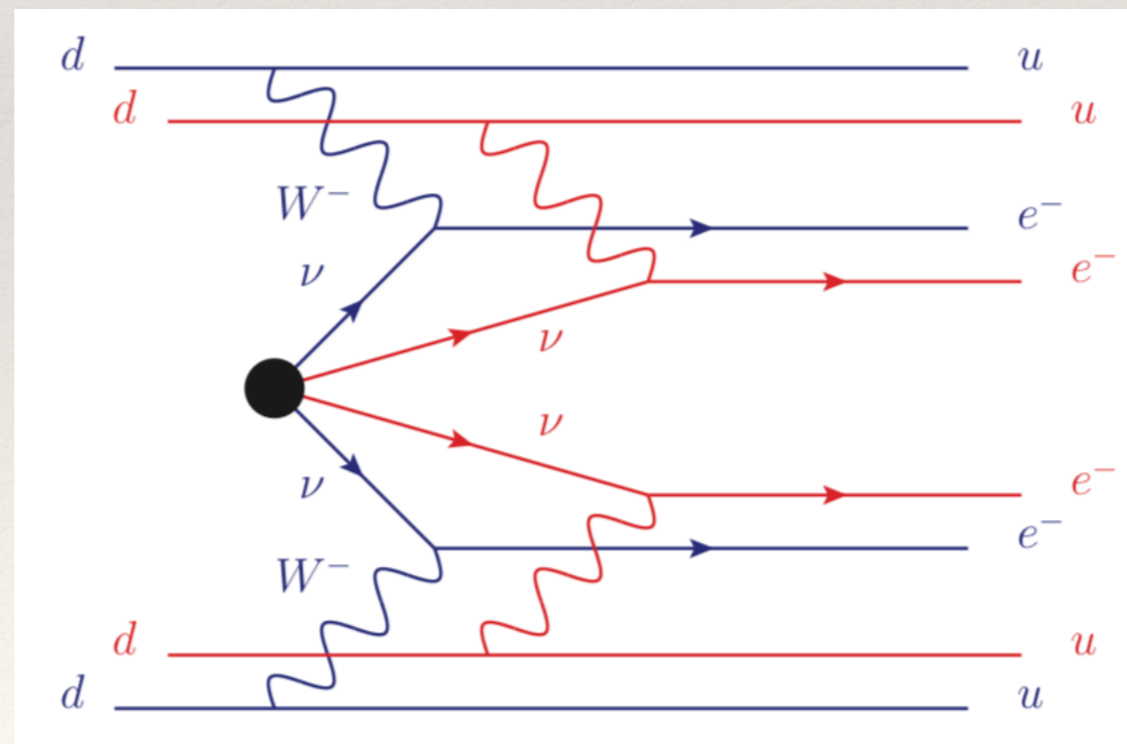
Heeck, WR, EPL103

Lepton Number Violation with Dirac Neutrinos

Phenomenology: Neutrinoless Quadruple Beta Decay $0\nu\beta\beta\beta\beta$



Candidates	$Q_{0\nu 4\beta}$	Other decays	NA
${}^{96}_{40}\text{Zr} \rightarrow {}^{96}_{44}\text{Ru}$	0.629	$\tau_{1/2}^{2\nu 2\beta} \simeq 2 \times 10^{19}$	2.8
${}^{136}_{54}\text{Xe} \rightarrow {}^{136}_{58}\text{Ce}$	0.044	$\tau_{1/2}^{2\nu 2\beta} \simeq 2 \times 10^{21}$	8.9
${}^{150}_{60}\text{Nd} \rightarrow {}^{150}_{64}\text{Gd}$	2.079	$\tau_{1/2}^{2\nu 2\beta} \simeq 7 \times 10^{18}$	5.6



Heeck, WR, EPL103

Lepton Number Violation with Dirac Neutrinos





PRL **119**, 041801 (2017)





PHYSICAL REVIEW LETTERS


week ending
28 JULY 2017





Search for Neutrinoless Quadruple- β Decay of ^{150}Nd with the NEMO-3 Detector


IOP Publishing    

 **physicsworld**  Magazine | Latest  | People 

 | particles and interactions

 **PARTICLES AND INTERACTIONS | RESEARCH UPDATE**

 **NEMO-3 hunts for ultra-rare beta decay**

 30 Jun 2017

D vs. M with general interactions

- ❖ most general neutrino charged lepton interaction:

$$\mathcal{L} \supset \frac{G_F}{\sqrt{2}} \sum_a \bar{\nu} \Gamma^a \nu [\bar{\ell} \Gamma^a (C_a + \bar{D}_a i \gamma^5) \ell]$$

Rosen, PRL48

- ❖ with usual five possible terms:

$$\Gamma^a = \left\{ I, i\gamma^5, \gamma^\mu, \gamma^\mu \gamma^5, \sigma^{\mu\nu} \equiv \frac{i}{2} [\gamma^\mu, \gamma^\nu] \right\}$$

- ❖ there can be sizable differences for Dirac and Majorana neutrinos!

D vs. M with general interactions

$$\mathcal{L} \supset \frac{G_F}{\sqrt{2}} \sum_a \bar{\nu} \Gamma^a \nu [\bar{\ell} \Gamma^a (C_a + \bar{D}_a i \gamma^5) \ell]$$

- ❖ in general, cross section for elastic neutrino electron scattering:

$$\frac{d\sigma}{dT}(\nu + \ell) = \frac{G_F^2 M}{2\pi} \left[A + 2B \left(1 - \frac{T}{E_\nu}\right) + C \left(1 - \frac{T}{E_\nu}\right)^2 \right]$$

$$T = \frac{2ME_\nu^2 c_\theta^2}{(M + E_\nu)^2 - E_\nu^2 c_\theta^2}$$

$$\frac{d\sigma}{dT}(\bar{\nu} + \ell) = \frac{G_F^2 M}{2\pi} \left[C + 2B \left(1 - \frac{T}{E_\nu}\right) + A \left(1 - \frac{T}{E_\nu}\right)^2 \right]$$

with:

$$A \equiv \frac{1}{4} (C_A - D_A + C_V - D_V)^2 + \frac{1}{2} C_P C_T + \frac{1}{8} (C_P^2 + C_S^2 + D_P^2 + D_S^2) - \frac{1}{2} C_S C_T + C_T^2 + \frac{1}{2} D_P D_T - \frac{1}{2} D_S D_T + D_T^2$$

$$B \equiv -\frac{1}{8} (C_P^2 + C_S^2 + D_P^2 + D_S^2) + C_T^2 + D_T^2,$$

$$C \equiv \frac{1}{4} (C_A + D_A - C_V - D_V)^2 - \frac{1}{2} C_P C_T + \frac{1}{8} (C_P^2 + C_S^2 + D_P^2 + D_S^2) + \frac{1}{2} C_T C_S + C_T^2 - \frac{1}{2} D_P D_T + \frac{1}{2} D_S D_T + D_T^2$$

- ❖ For Majorana neutrinos: $C_V = D_V = C_T = D_T = 0$

D vs. M with general interactions

$$\frac{d\sigma}{dT}(\nu + \ell) = \frac{G_F^2 M}{2\pi} \left[A + 2B \left(1 - \frac{T}{E_\nu}\right) + C \left(1 - \frac{T}{E_\nu}\right)^2 \right]$$

$$\frac{d\sigma}{dT}(\bar{\nu} + \ell) = \frac{G_F^2 M}{2\pi} \left[C + 2B \left(1 - \frac{T}{E_\nu}\right) + A \left(1 - \frac{T}{E_\nu}\right)^2 \right]$$

- ❖ *Rosen* introduced a measurable ratio:

$$R_\rho \equiv \frac{2(A + 2B + C)}{A + C}$$

- ❖ differs for Dirac and Majorana neutrinos!

$$0 \leq R_\rho \leq 4 \text{ (Dirac),}$$

$$0 \leq R_\rho \leq 2 \text{ (Majorana)}$$

$$(R_\rho = 2 \text{ in SM)}$$

D vs. M with general interactions

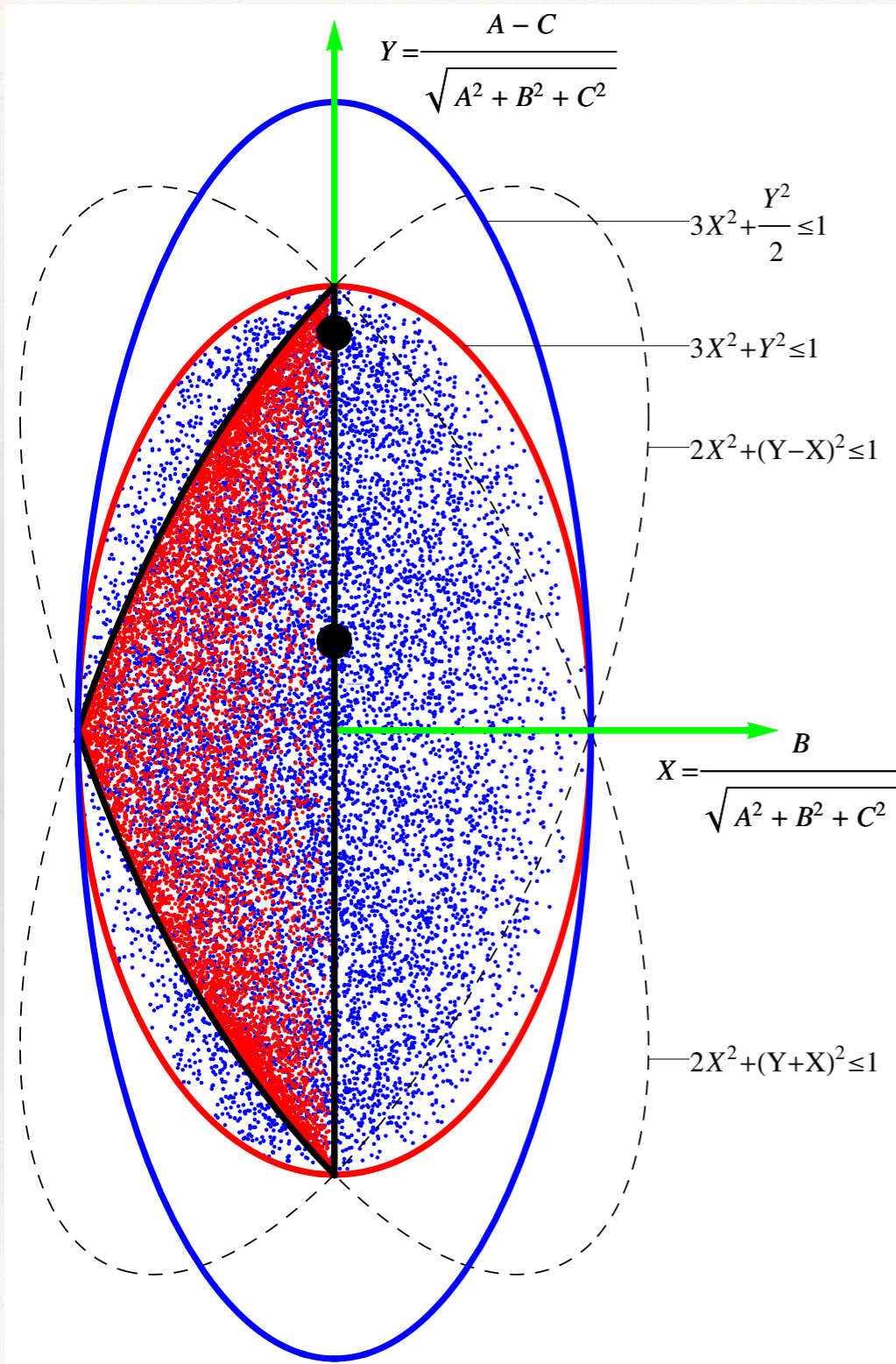
$$0 \leq R_\rho \leq 4 \text{ (Dirac),}$$

$$0 \leq R_\rho \leq 2 \text{ (Majorana)}$$

- ❖ measure between 0 and 2: can't tell
- ❖ measure between 2 and 4: Dirac!
- ❖ \Rightarrow *can only show Dirac nature!*
- ❖ actually, slightly more complicated than just R_ρ

WR, Xu, Yaguna, JHEP1705

D vs. M with general interactions



$$X \equiv \frac{B}{R}, \quad Y \equiv \frac{A - C}{R}$$

$$R \equiv \sqrt{A^2 + B^2 + C^2}$$

Dirac:

$$3X^2 + Y^2 \leq 1$$

Majorana:

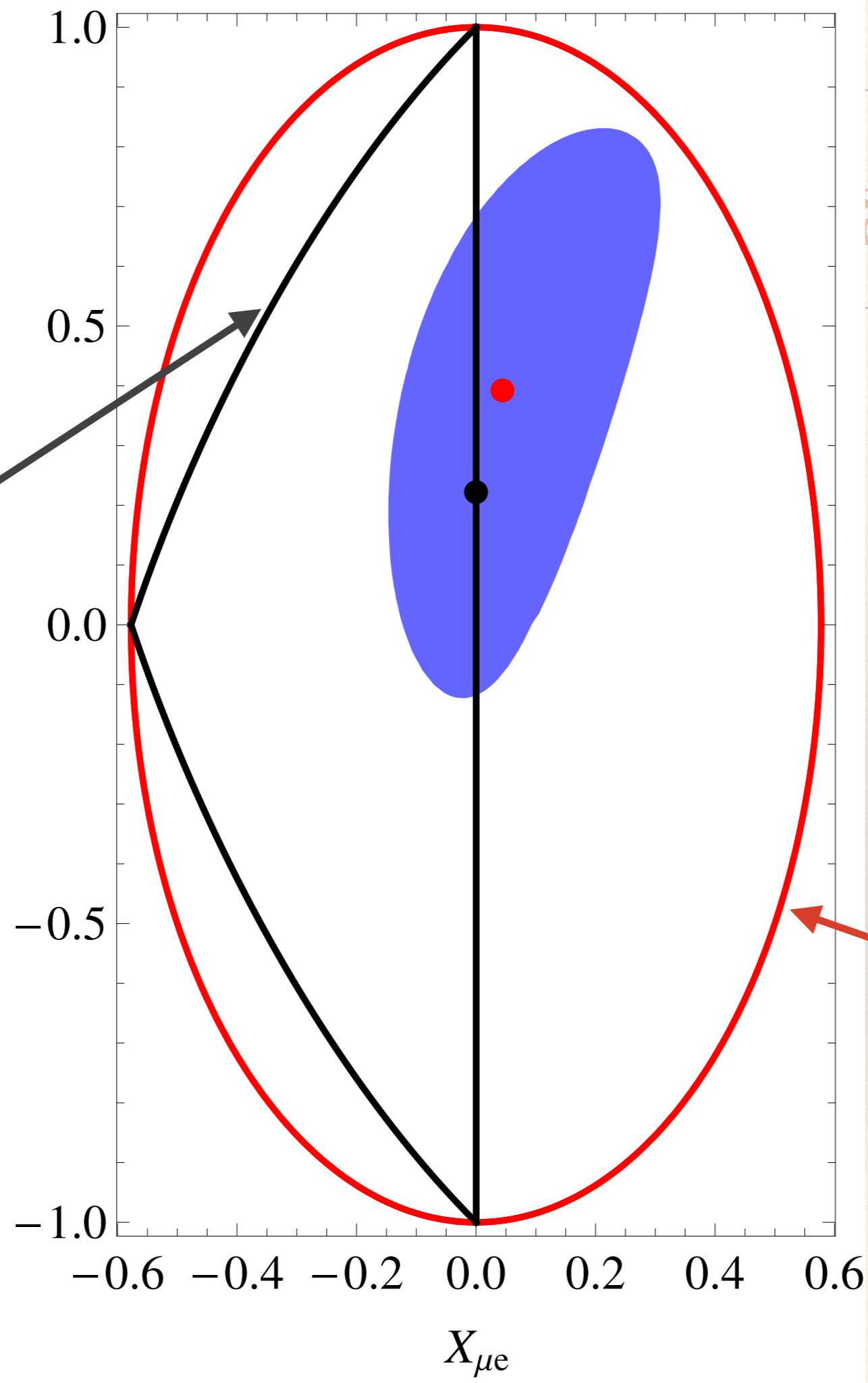
$$2X^2 + (Y \pm X)^2 \leq 1 \quad \text{and} \quad X \leq 0$$

D vs. M

actions

Majorana

$Y_{\mu e}$



CHARM-II data

Dirac

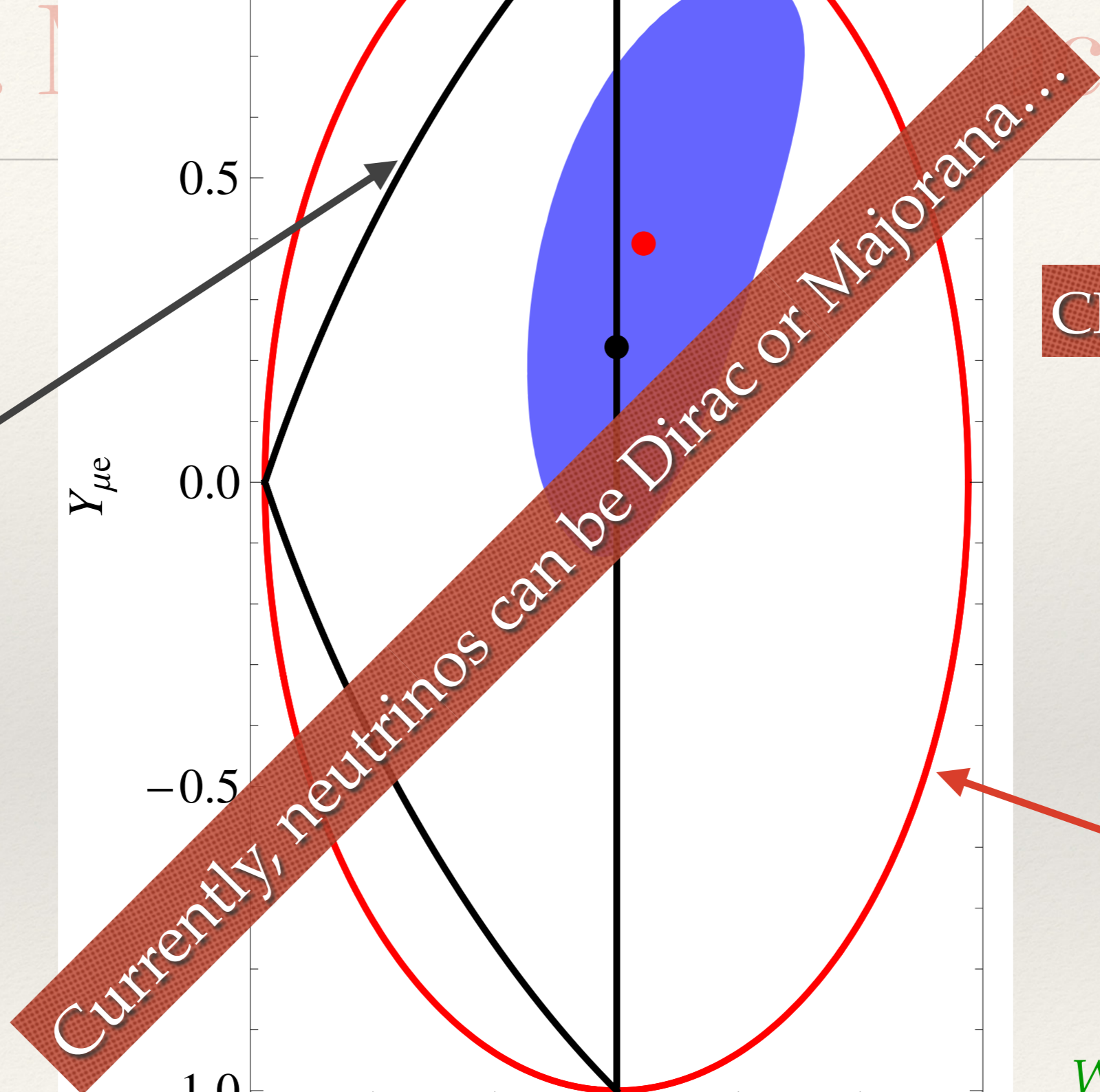
WR, Xu, Yaguna,
JHEP1705

D vs. M

stions

Majorana

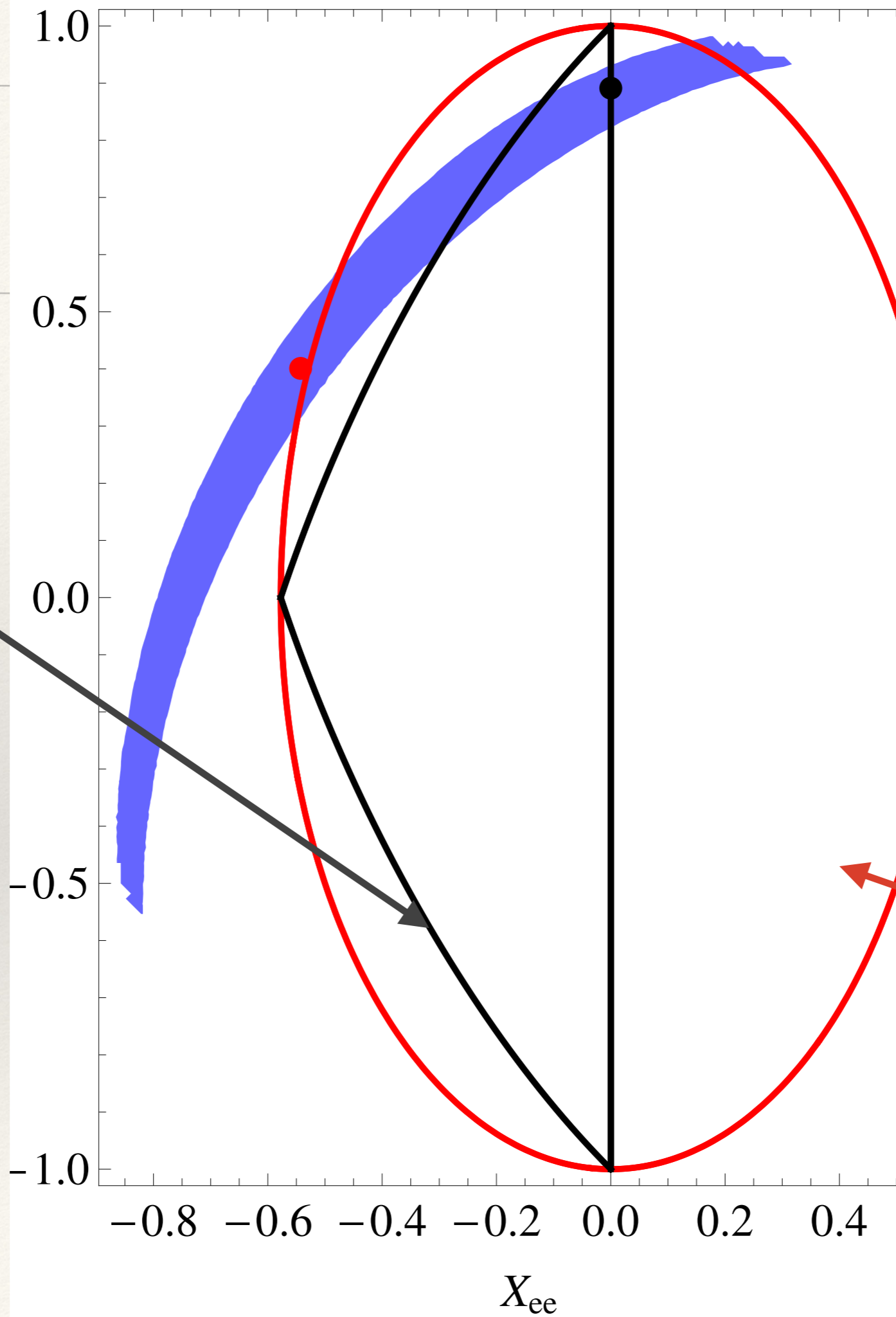
$Y_{\mu e}$



CHARM-II data

Dirac

WR, Xu, Yaguna,
JHEP1705



TEXONO data

Majorana

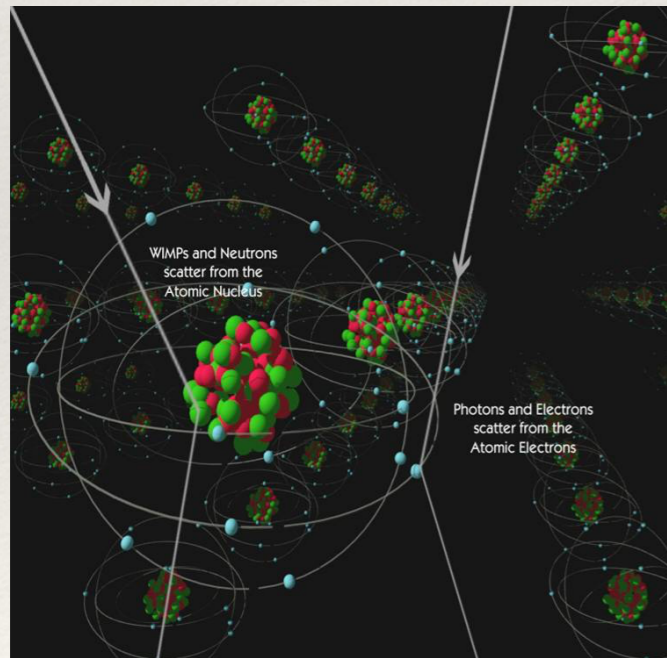
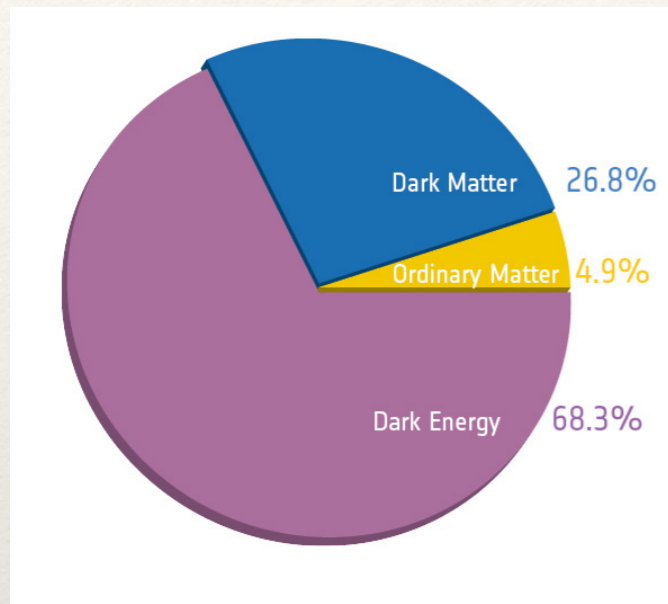
Dirac

*WR, Xu, Yaguna,
JHEP1705*

And now
for something
completely different...



Is Dark Matter its own Antiparticle?



- ❖ Dark Matter probably a particle
- ❖ natural, yet hardly asked question: *is it self-conjugate?*
- ❖ determining nature of DM particle turns out to be possible with direct detection only

(However, very difficult....)

Queiroz, WR, Yaguna, PRD95

Dirac versus Majorana DM

- ❖ difficult task, need:
 - isospin violating DM
 - non-zero coupling with p and n of DM particle and antiparticle
 - close density of DM particle and antiparticle
 - scalar **and** vector interactions
 - non-zero cross section with p and n
 - different ratio of (p,n) -coupling to DM particle and antiparticle

Queiroz, WR, Yaguna, PRD95

How it works:

- ❖ If χ is Dirac fermion: χ^D and anti- χ^D in principle both present \Rightarrow Dirac-DM has 4 possible interactions:
 - χ^D talking to p , χ^D talking to n , anti- χ^D talking to p , anti- χ^D talking to n
- ❖ If χ is Majorana fermion: $\chi^M = \text{anti-}\chi^M \Rightarrow$ Majorana-DM has 2 possible interactions:
 - χ^M talking to p , χ^M talking to n
- ❖ \Rightarrow Need to show that 4 interactions are present!
- ❖ \Rightarrow *can only show Dirac nature!*

Dirac versus Majorana DM

- ❖ most general SI interaction of fermion χ ($N = p, n$):

$$\mathcal{L}_{SI}^F = \lambda_{N,e} \bar{\psi}_\chi \psi_\chi \bar{\psi}_N \psi_N + \lambda_{N,o} \bar{\psi}_\chi \gamma_\mu \psi_\chi \bar{\psi}_N \gamma^\mu \psi_N$$

- ❖ For Majorana: no vector interactions:

$$\sigma_{SI}^M = \frac{4\mu_\chi^2}{\pi} \left[\lambda_p^M Z + \lambda_n^M (A - Z) \right]^2$$

- ❖ For Dirac: particle and antiparticle:

$$\sigma_{SI}^D = \frac{4\mu_\chi^2}{\pi} \frac{1}{2} \left(\left[\lambda_p^D Z + \lambda_n^D (A - Z) \right]^2 + \left[\lambda_p^{\bar{D}} Z + \lambda_n^{\bar{D}} (A - Z) \right]^2 \right)$$

$$\lambda_N^D \equiv (\lambda_{N,e} + \lambda_{N,o})/2 \text{ and } \lambda_N^{\bar{D}} \equiv (\lambda_{N,e} - \lambda_{N,o})/2$$

Dirac versus Majorana DM

- ❖ suppose we have measured DM cross section with isotopes X and Y . Interpreted in terms of Majorana, we have:

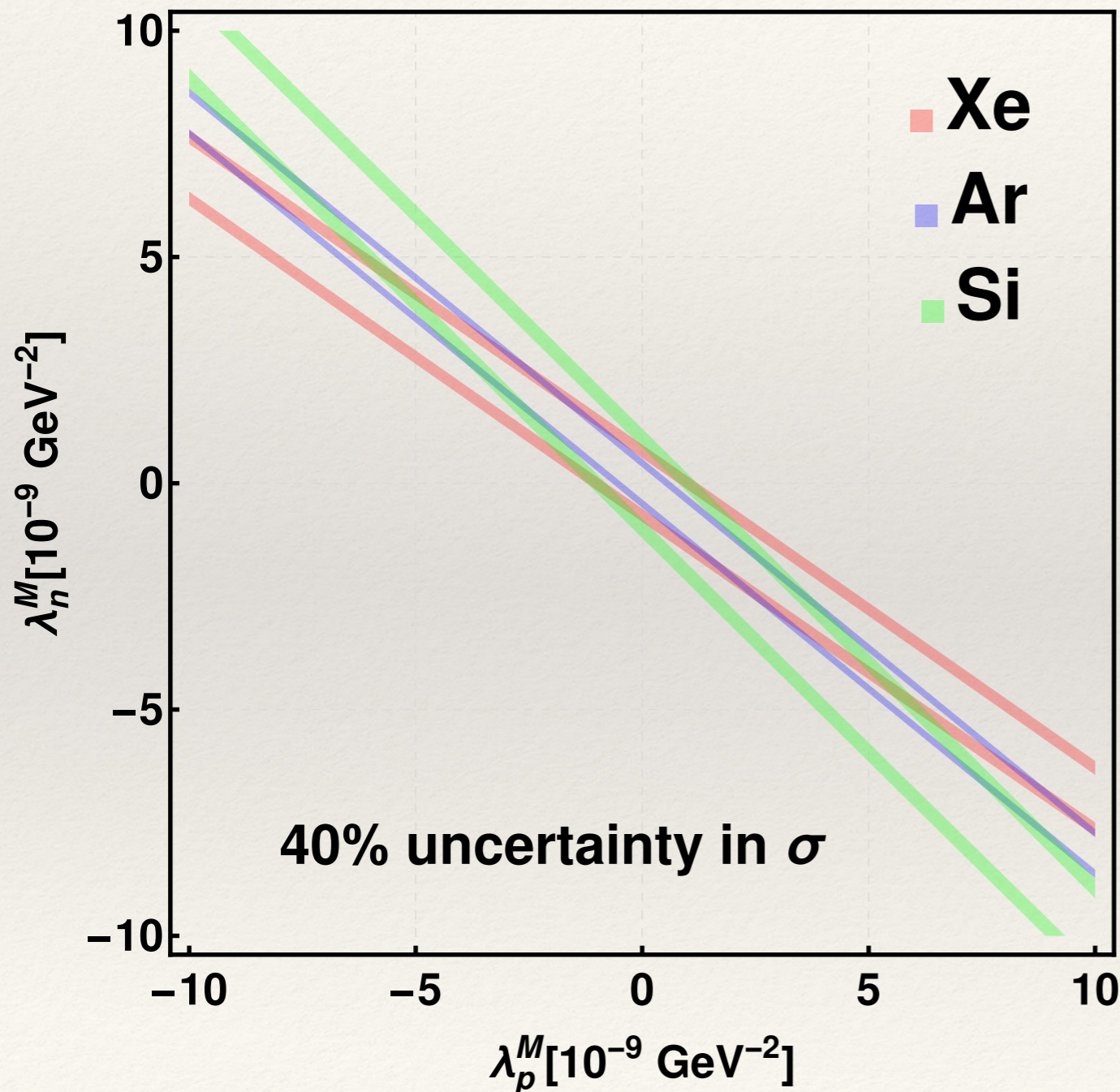
$$\left[\lambda_p^M Z_X + \lambda_n^M (A_X - Z_X) \right]^2 = \frac{\pi \tilde{\sigma}_X}{4\mu_\chi^2},$$
$$\left[\lambda_p^M Z_Y + \lambda_n^M (A_Y - Z_Y) \right]^2 = \frac{\pi \tilde{\sigma}_Y}{4\mu_\chi^2}.$$

extract $(\lambda_p^M, \lambda_n^M)$: two parallel lines each,
with slopes $m_X = Z_X/(A_X - Z_X)$ and
 $m_Y = Z_Y/(A_Y - Z_Y)$

Dirac versus Majorana DM

- ❖ suppose we have measured DM cross section with isotopes X and Y . Interpreted in terms of Majorana, extract $(\lambda_p^M, \lambda_n^M)$: two parallel lines with slopes $m_X = Z_X/(A_X - Z_X)$ and $m_Y = Z_Y/(A_Y - Z_Y)$
- ❖ if $m_X \neq m_Y$: lines intersect at 4 different points
 - \Rightarrow always consistent with Majorana case!
 - \Rightarrow need third isotope V :
 - hit one of the crossing points of X and Y : can't tell Dirac from Majorana
 - miss all crossing points of X and Y : DM is Dirac particle!

Dirac versus Majorana DM



- ❖ **red** and **blue** lines for **Xe** and **Ar**: cross each other 4 times
- ❖ **green** line for **Si**: does not cross other lines in one point
⇒ Majorana interpretation does not work
⇒ DM must be Dirac particle

Experimental Aspects

- ❖ need isotopes with different Z and $N = A - Z$
- ❖ Z/N between 0.65 and 1 for stable nuclei
- ❖ Ar, Xe, Ge too close to each other
- ❖ Ar, Xe and Si or Ca or O would be nice...

isotope	Z	N	Z/N
Ar	18	22	0.82
Xe	54	77	0.70
Ge	32	40	0.80
Si	14	14	1.00
Na	11	12	0.92
F	9	10	0.90
Ca	20	20	1.00
O	8	8	1.00
W	74	110	0.67
I	53	74	0.72

Statistical Analysis

(do „realistic“ analysis with proper event numbers, experimental details, etc.)

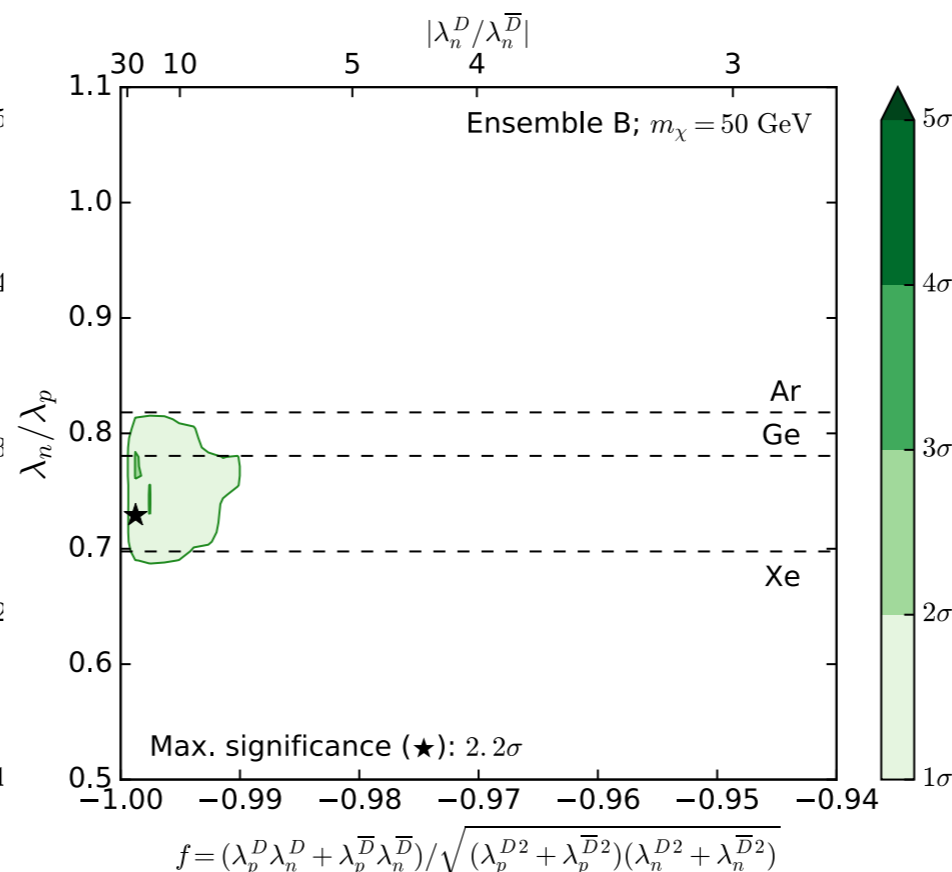
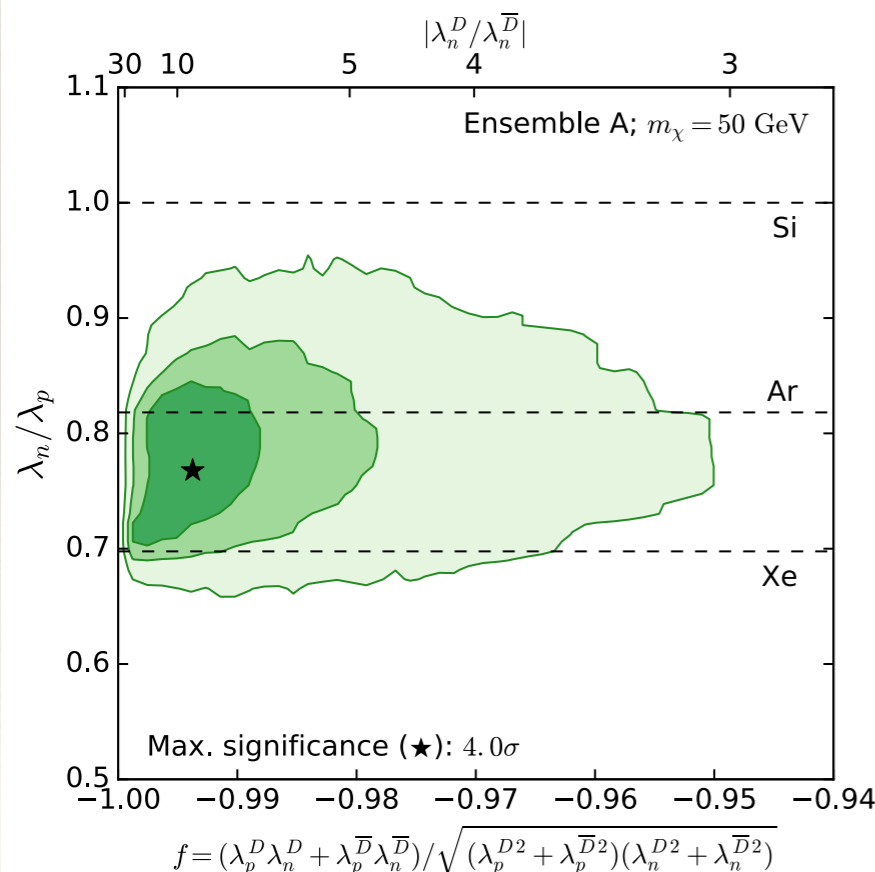
Target	E_{\min} [keV]	E_{\max} [keV]	Exposure [ton yr]
Xe	5	40	20
Ar	30	200	150
Si	7	100	3
Ge	5	100	3
CaWO ₄	10	100	3

Ensemble A: Xe + Ar + Si

Ensemble B: Xe + Ar + Ge

Ensemble C: Xe + Ar + CaWO₄

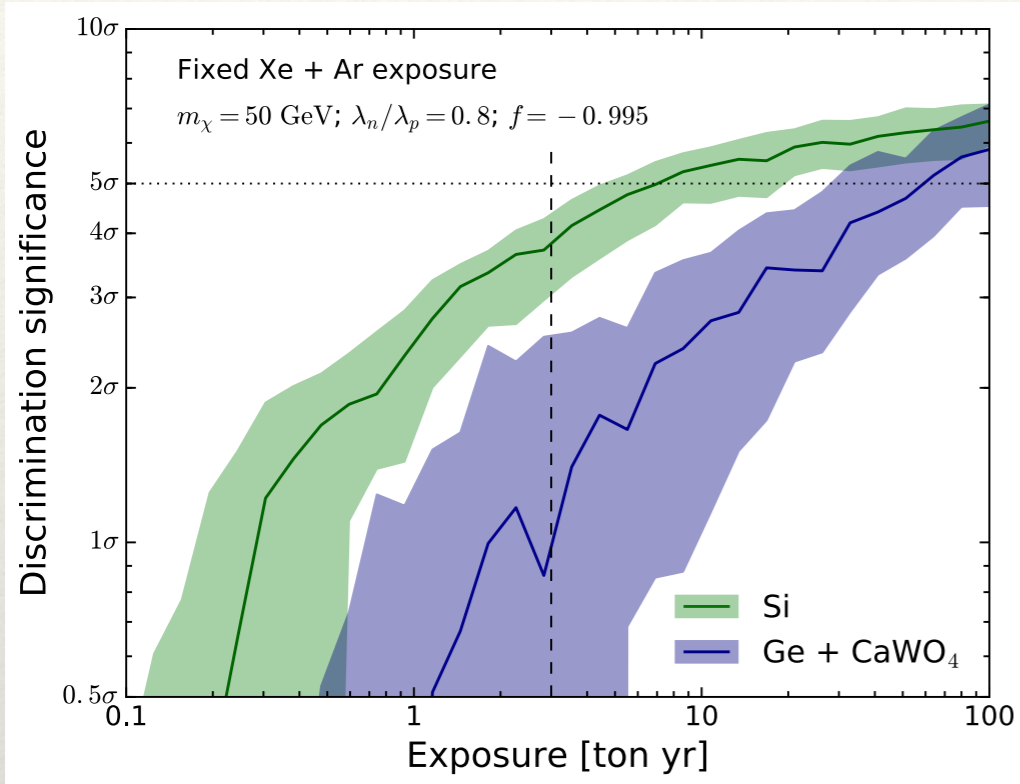
Ensemble D: Xe + Ar + 50% Ge + 50% CaWO₄



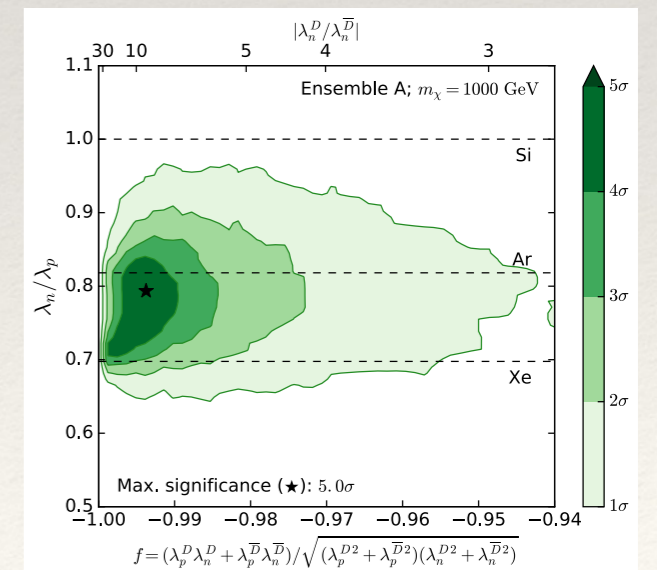
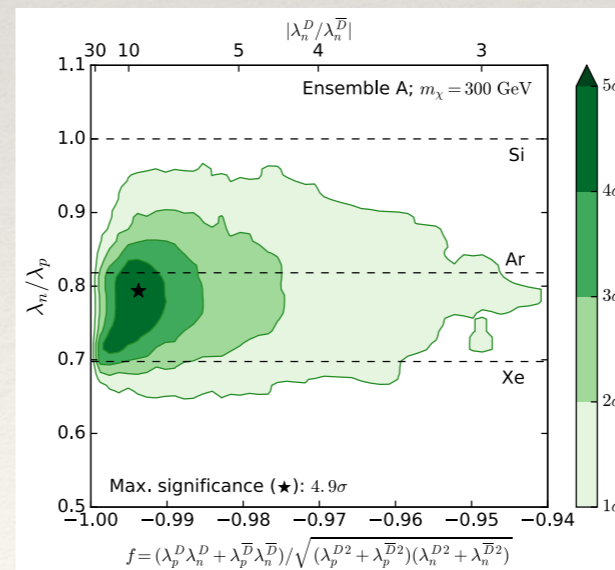
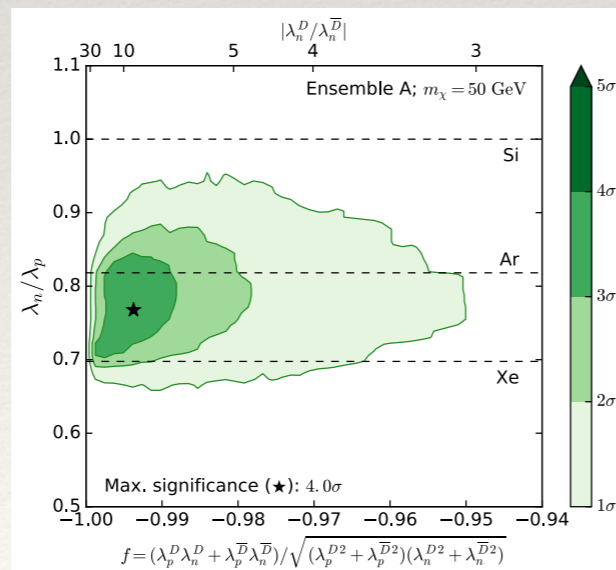
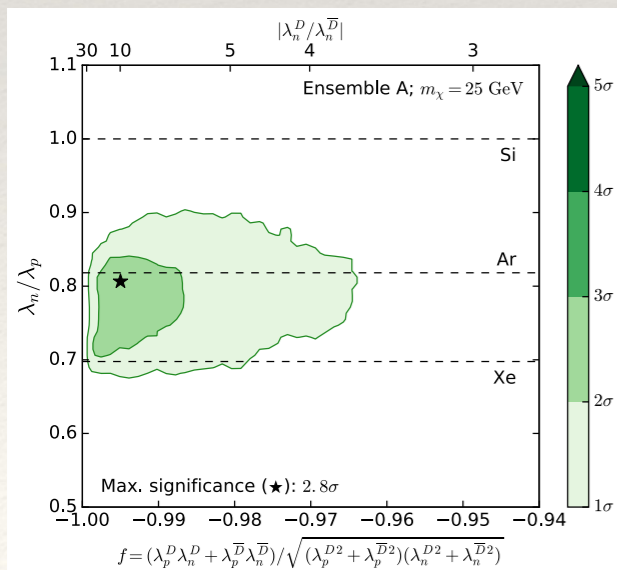
- fix event numbers for Xe
- at each mass, parameter ranges determined
- at each point, generate mock data
- fit under hypothesis D and M, respectively
- compare likelihoods

Kavanagh, Queiroz, WR, Yaguna, JHEP1710

Statistical Analysis



DM Mass [GeV]	25	50	300	1000
A (Xe+Ar+Si)	2.8 σ	4.0 σ	4.9 σ	5.0 σ
B (Xe+Ar+Ge)	1.7 σ	2.2 σ	2.7 σ	2.8 σ
C (Xe+Ar+CaWO ₄)	2.0 σ	2.4 σ	3.0 σ	2.9 σ
D (Xe+Ar+Ge/CaWO ₄)	3.2 σ	2.6 σ	2.9 σ	3.2 σ



Kavanagh, Queiroz, WR, Yaguna, JHEP1710

Scalar and Vector Dark Matter

- ❖ Scalar particle ϕ_χ also possible. If complex:

$$\begin{aligned}\mathcal{L}_{SI}^S &= 2\lambda_{N,e}M_\chi \phi_\chi^\dagger \phi_\chi \bar{\psi}_N \psi_N \\ &\quad + i\lambda_{N,o} [\phi_\chi^\dagger (\partial_\mu \phi_\chi) - (\partial_\mu \phi_\chi^\dagger) \phi_\chi] \bar{\psi}_N \gamma^\mu \psi_N\end{aligned}$$

- ❖ if real: $\lambda_{N,o} = 0$
- ❖ Again, 4 parameters for complex DM, two for real
- ❖ Works similarly with vector DM

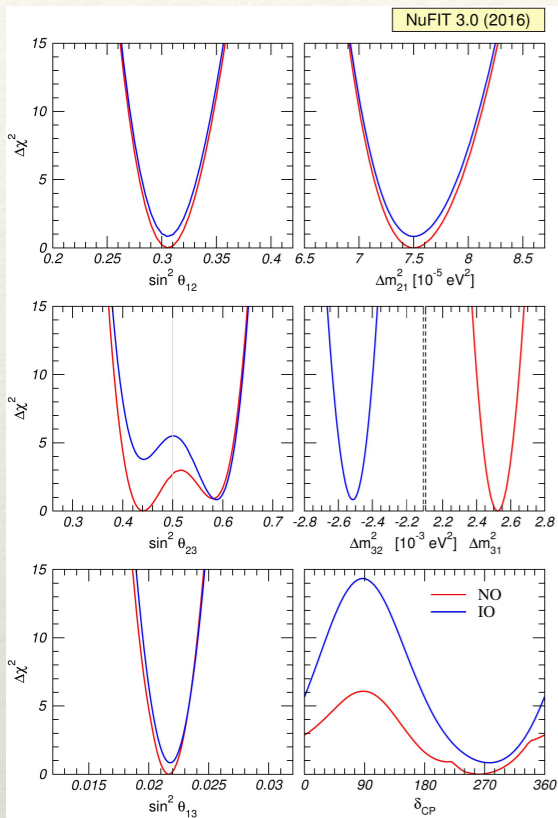
Summary

Chi l'ha visto ?



Ettore Majorana, ordinario di fisica teorica all'Università di Napoli, è misteriosamente scomparso dagli ultimi di marzo. Di anni 31, alto metri 1,70, snello, con capelli neri, occhi scuri, una lunga cicatrice sul dorso di una mano. Chi ne sapesse qualcosa è pregato di scrivere al R. P. E. Maria-necci, Viale Regina Margherita 66 - Roma.

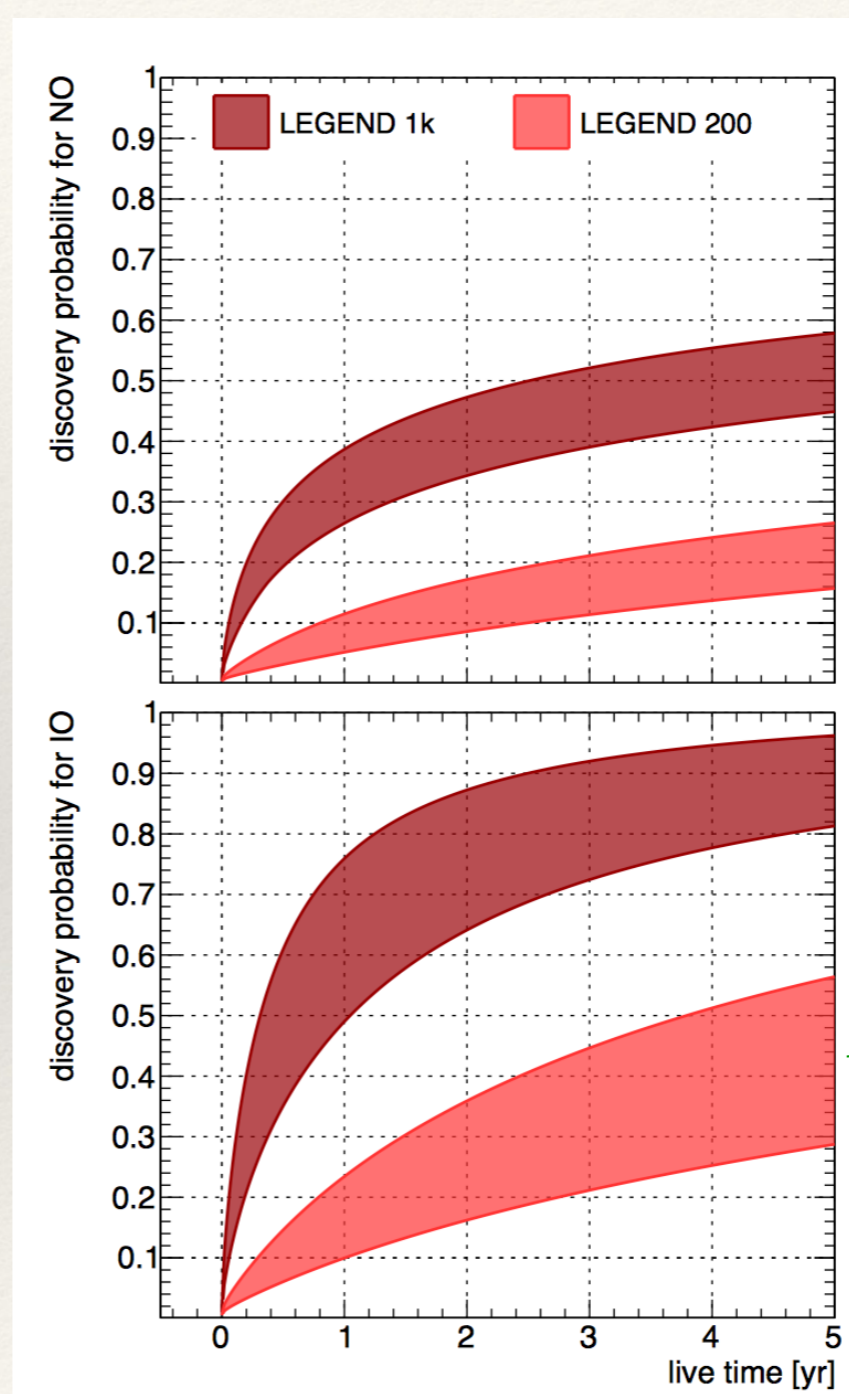
Expectations of lifetimes



Oscillation fits
 expt. sensitiv.

+

Experiment	Iso.	Iso. Mass [kg _{iso}]	σ [keV]	ROI [σ]	ϵ_{FV} [%]	ϵ_{sig} [%]	\mathcal{E} [kg _{iso} yr / yr]	B [cts / kg _{iso} ROI yr]	3σ disc. sens.		Required Improvement		
									$\hat{T}_{1/2}$ [yr]	$\hat{m}_{\beta\beta}$ [meV]	Bkg	σ	Iso. Mass
LEGEND 200 [61, 62]	⁷⁶ Ge	175	1.3	[-2, 2]	93	77	119	$1.7 \cdot 10^{-3}$	$8.4 \cdot 10^{26}$	40-73	3	1	5.7
LEGEND 1k [61, 62]	⁷⁶ Ge	873	1.3	[-2, 2]	93	77	593	$2.8 \cdot 10^{-4}$	$4.5 \cdot 10^{27}$	17-31	18	1	29
SuperNEMO [68, 69]	⁸² Se	100	51	[-4, 2]	100	16	16.5	$4.9 \cdot 10^{-2}$	$6.1 \cdot 10^{25}$	82-138	49	2	14
CUPID [58, 59, 70]	⁸² Se	336	2.1	[-2, 2]	100	69	221	$5.2 \cdot 10^{-4}$	$1.8 \cdot 10^{27}$	15-25	n/a	6	n/a
CUORE [52, 53]	¹³⁰ Te	206	2.1	[-1.4, 1.4]	100	81	141	$3.1 \cdot 10^{-1}$	$5.4 \cdot 10^{25}$	66-164	6	1	19
CUPID [58, 59, 70]	¹³⁰ Te	543	2.1	[-2, 2]	100	81	422	$3.0 \cdot 10^{-4}$	$2.1 \cdot 10^{27}$	11-26	3000	1	50
SNO+ Phase I [66, 71]	¹³⁰ Te	1357	82	[-0.5, 1.5]	20	97	164	$8.2 \cdot 10^{-2}$	$1.1 \cdot 10^{26}$	46-115	n/a	n/a	n/a
SNO+ Phase II [67]	¹³⁰ Te	7960	57	[-0.5, 1.5]	28	97	1326	$3.6 \cdot 10^{-2}$	$4.8 \cdot 10^{26}$	22-54	n/a	n/a	n/a
KamLAND-Zen 800 [60]	¹³⁶ Xe	750	114	[0, 1.4]	64	97	194	$3.9 \cdot 10^{-2}$	$1.6 \cdot 10^{26}$	47-108	1.5	1	2.1
KamLAND2-Zen [60]	¹³⁶ Xe	1000	60	[0, 1.4]	80	97	325	$2.1 \cdot 10^{-3}$	$8.0 \cdot 10^{26}$	21-49	15	2	2.9
nEXO [72]	¹³⁶ Xe	4507	25	[-1.2, 1.2]	60	85	1741	$4.4 \cdot 10^{-4}$	$4.1 \cdot 10^{27}$	9-22	400	1.2	30
NEXT 100 [64, 73]	¹³⁶ Xe	91	7.8	[-1.3, 2.4]	88	37	26.5	$4.4 \cdot 10^{-2}$	$5.3 \cdot 10^{25}$	82-189	n/a	1	20
NEXT 1.5k [74]	¹³⁶ Xe	1367	5.2	[-1.3, 2.4]	88	37	398	$2.9 \cdot 10^{-3}$	$7.9 \cdot 10^{26}$	21-49	n/a	1	300
PandaX-III 200 [65]	¹³⁶ Xe	180	31	[-2, 2]	100	35	60.2	$4.2 \cdot 10^{-2}$	$8.3 \cdot 10^{25}$	65-150	n/a	n/a	n/a
PandaX-III 1k [65]	¹³⁶ Xe	901	10	[-2, 2]	100	35	301	$1.4 \cdot 10^{-3}$	$9.0 \cdot 10^{26}$	20-46	n/a	n/a	n/a

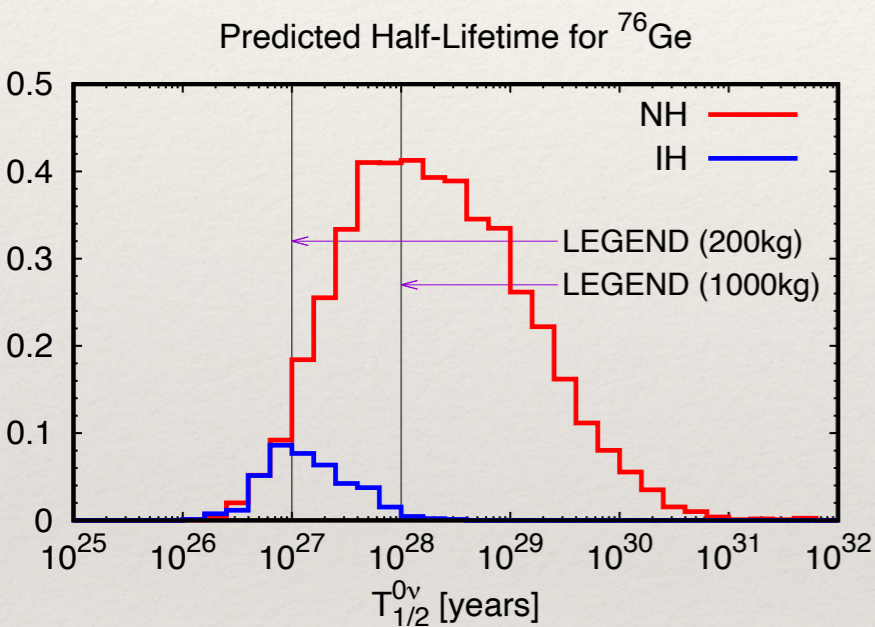


Bayesian discovery probability: discovery sensitivity (value of m_{ee} for which expt. has 50% chance to see it at 3σ) folded with probability distribution of m_{ee}

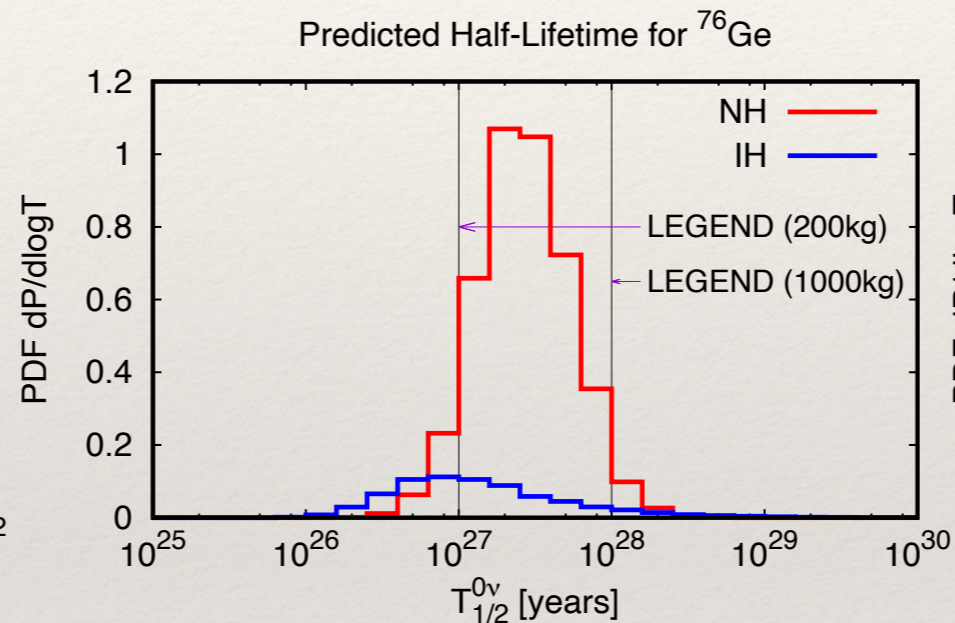
Agostini et al, 1705.02996;
 also Caldwell et al., 1705.01945;
 also Zhang, Zhou, 1508.05472

Expectations for half-lives

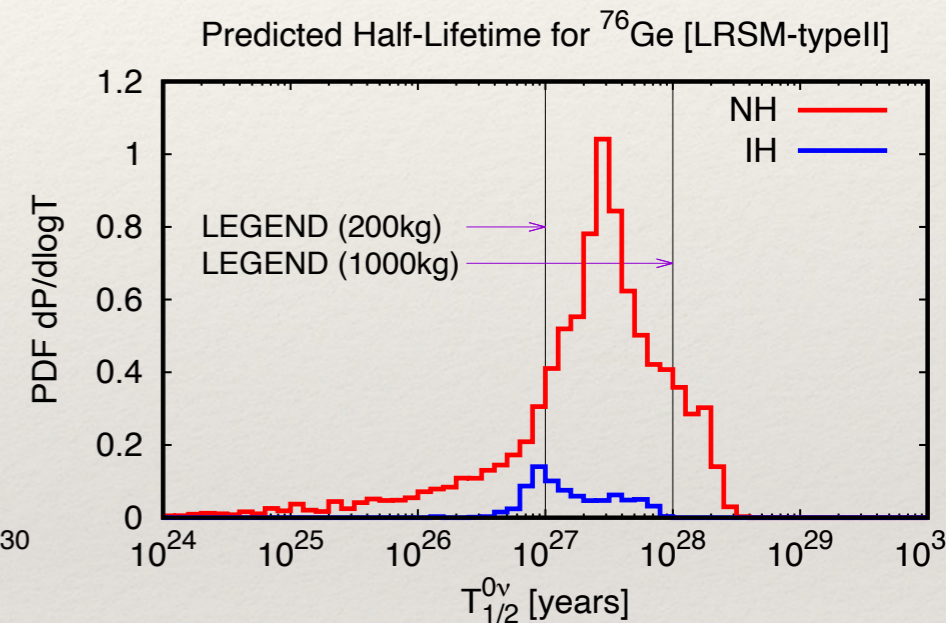
Standard



Sterile



Left-right



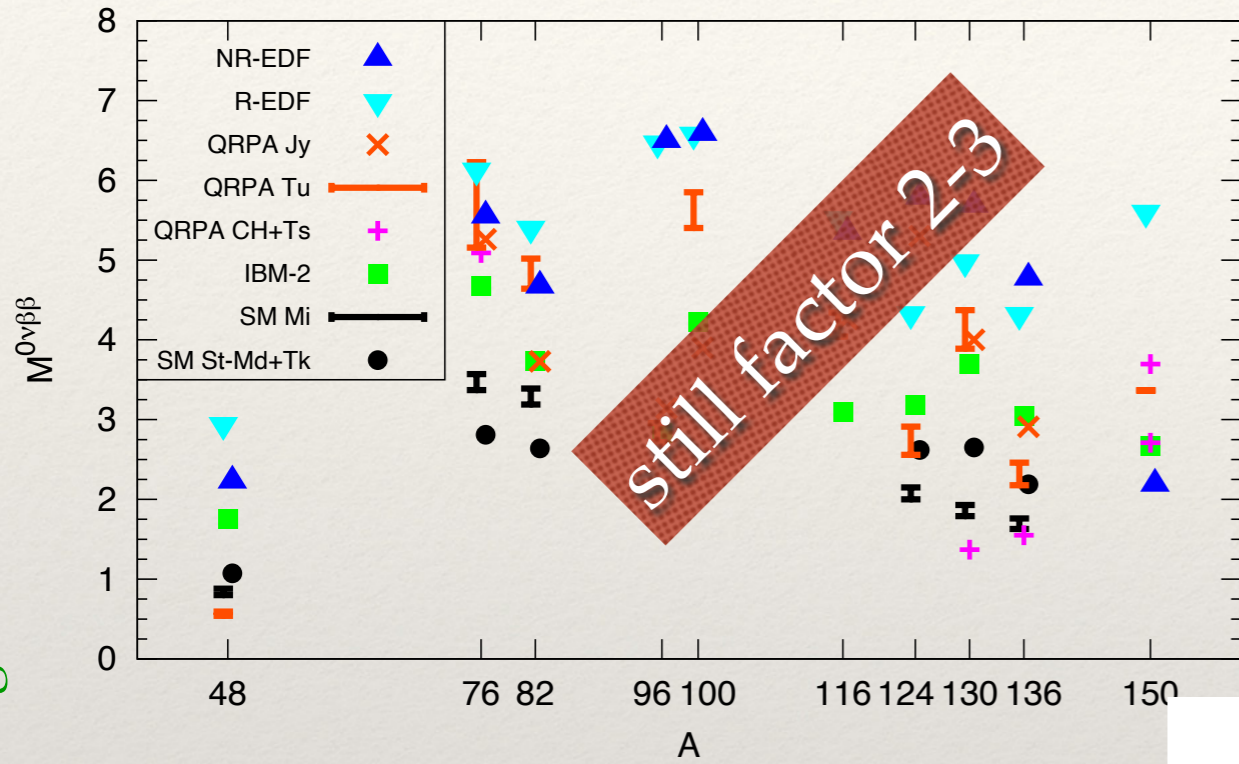
Ge, WR, Zuber, 1707.07904

However, most alternative mechanisms unrelated to neutrino parameters...

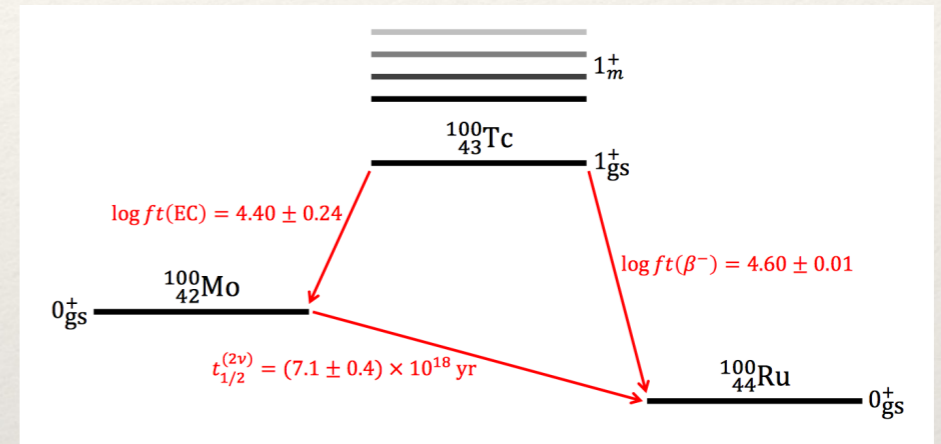
...thus decoupled from cosmology (and direct experiments)!

Nuclear Matrix Elements

Engel, Menendez, 1610.06548

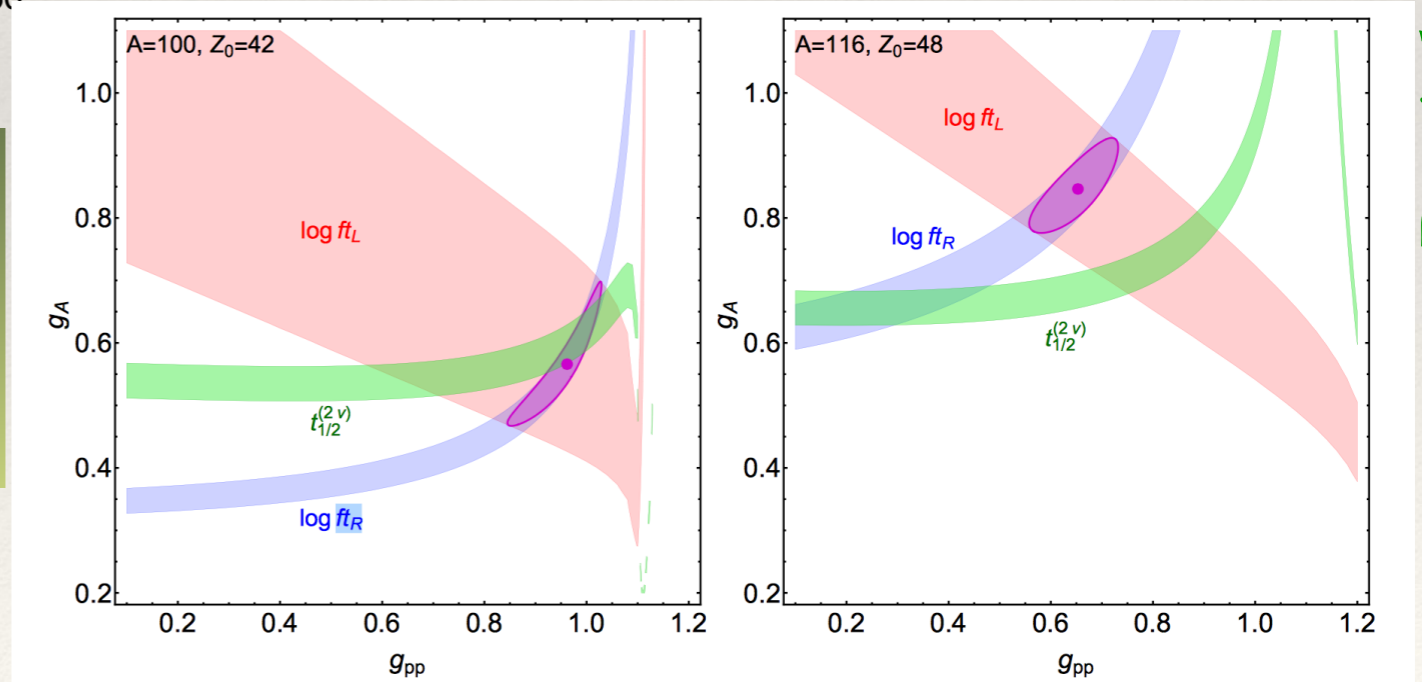


How good are the models?
Example isobaric triplets
within QRPA



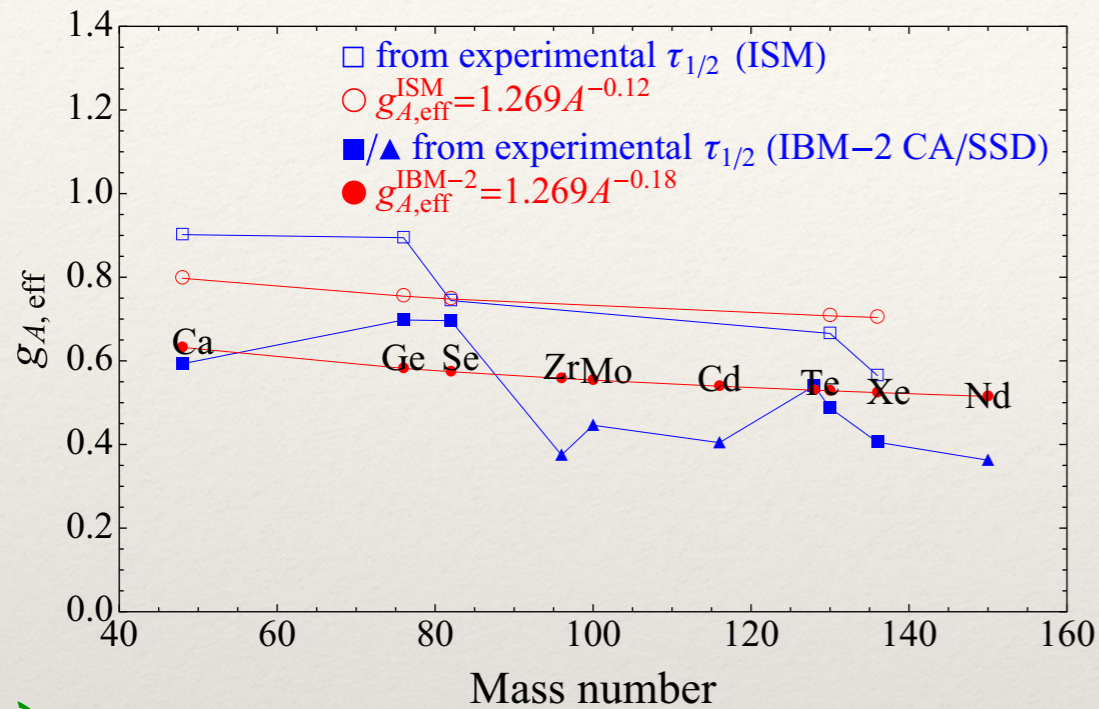
Deppisch, Suhonen, 1606.02908

⇒ Need as much experimental input (e.g. charge exchange) as possible...



Nuclear Matrix Elements

Iachello et al., 1506.08530

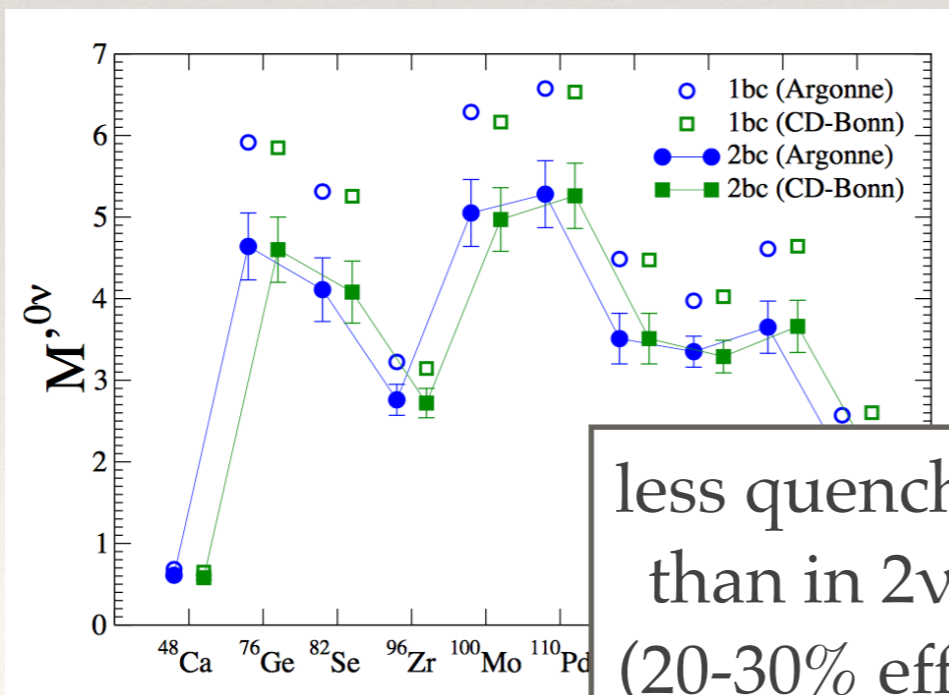


QUENCHING??

$$T_{\frac{1}{2}}^{0\nu} \propto g_A^{-4}$$

- ❖ fact in β and $2\nu\beta\beta$
- ❖ truncation of model-space?
- ❖ also in $0\nu\beta\beta$??
 - $q = 10^2$ vs. 10^0 MeV?
 - higher multipolarities?
 - two-body currents?
 - muon capture?
 - SM vs. QRPA

Menendez, Gazit, Schwenk, 1103.3622; Engel, Simkovic, Vogel, 1403.7860

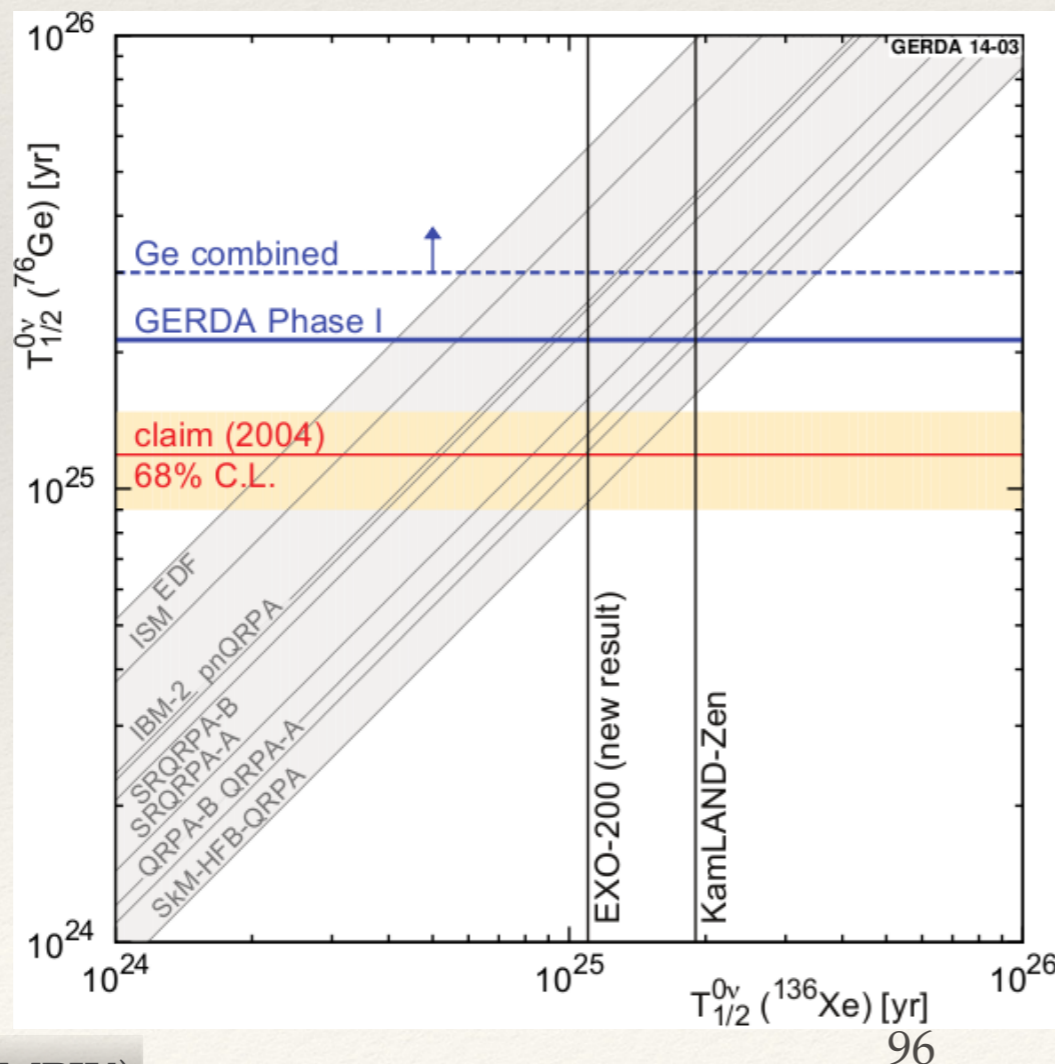


less quenching than in $2\nu\beta\beta$ (20-30% effect)

Comparison of Limits

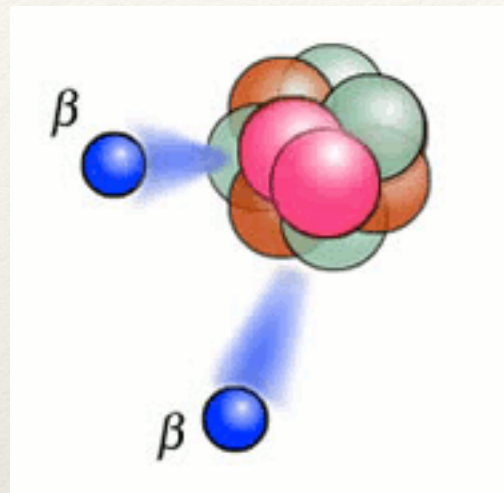
Limit from Xenon is better than limit from Germanium if:

$$T_{\text{Xe}} > T_{\text{Ge}} \frac{G_{\text{Ge}}}{G_{\text{Xe}}} \left| \frac{\mathcal{M}_{\text{Ge}}}{\mathcal{M}_{\text{Xe}}} \right|^2 \text{ yrs}$$

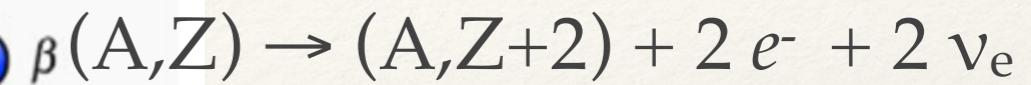
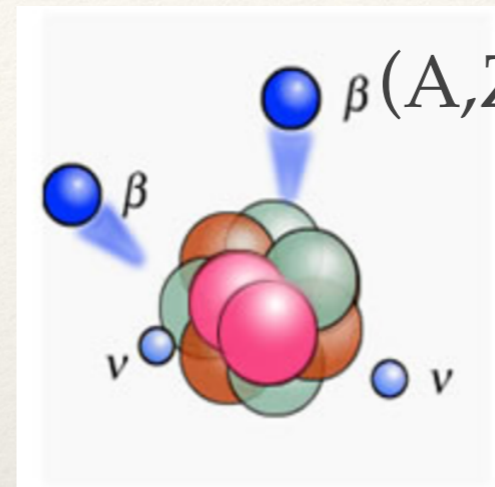


- ❖ depends on NMEs
- ❖ for most NMEs Xe better
- ❖ limit about $m_{ee} < 0.2 \text{ eV}$
- ❖ means 0.2...0.6 eV for KATRIN
- ❖ means 0.6...1.8 eV for cosmo

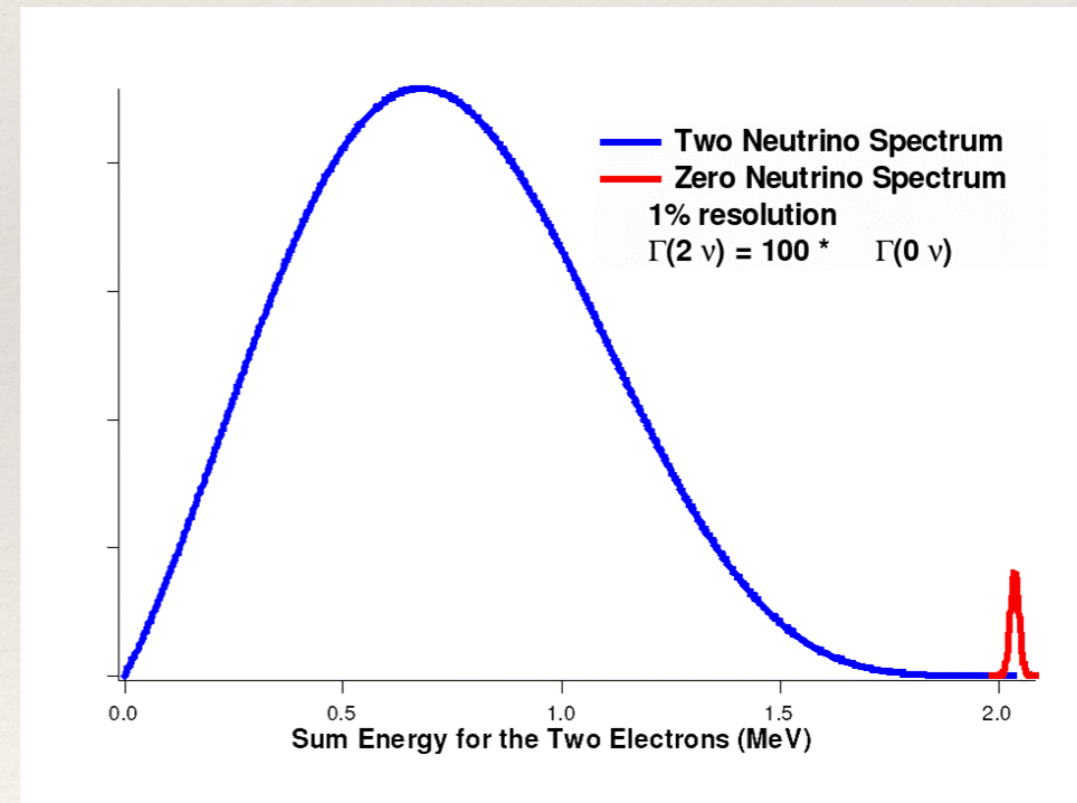
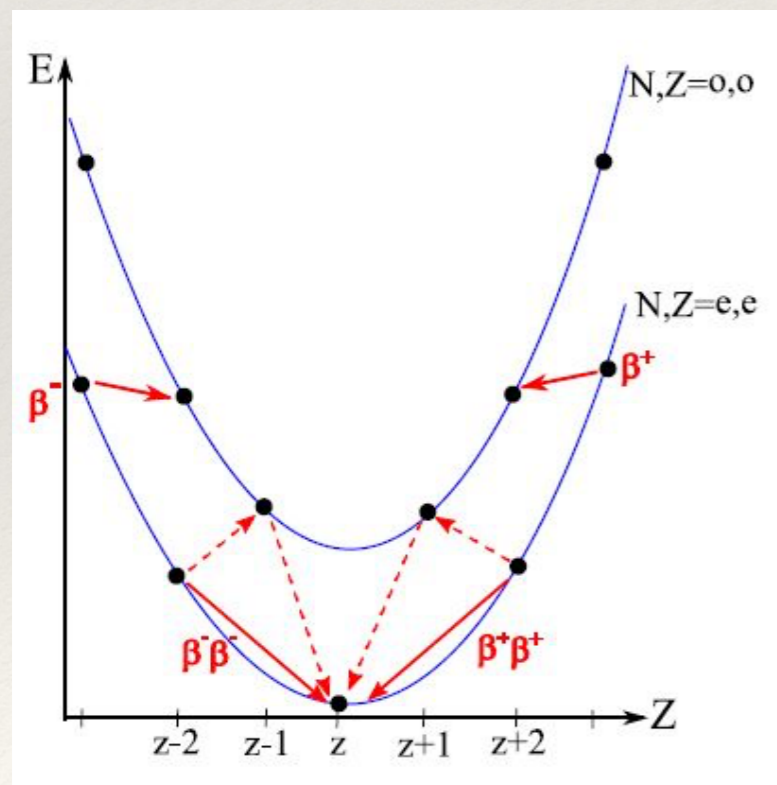
Best chance: Neutrinoless Double Beta Decay



$$\Delta L = 2$$



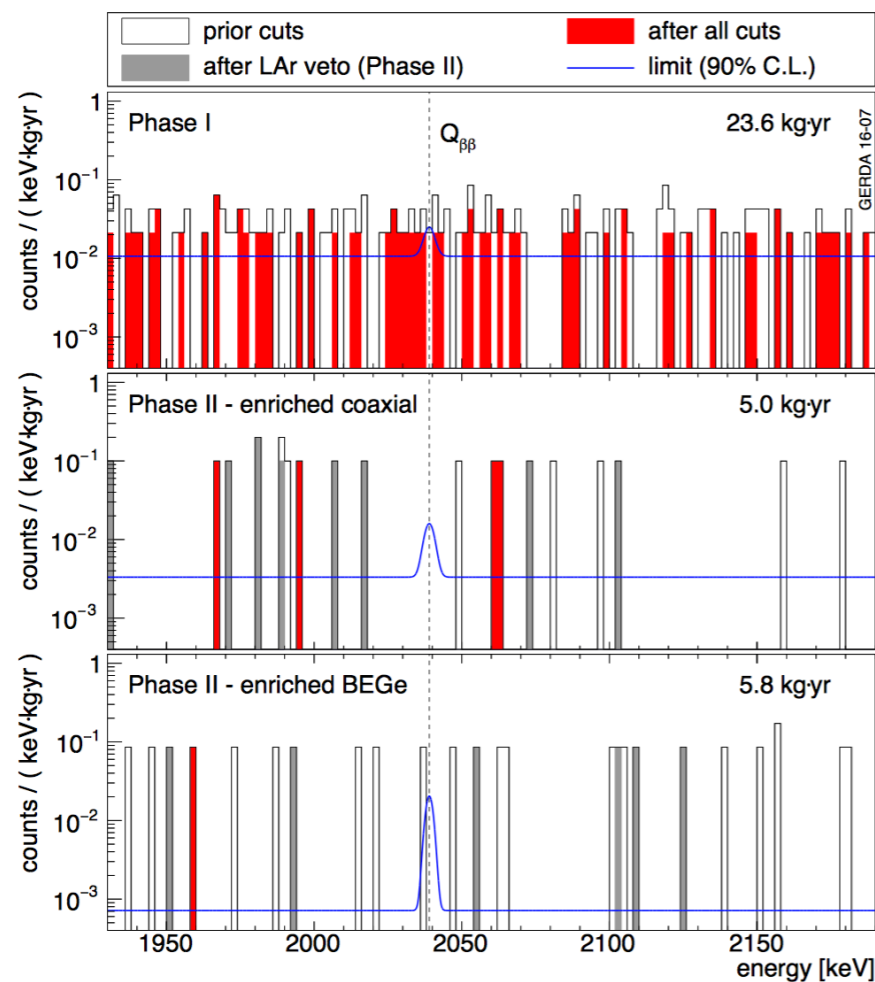
$$\Delta L = 0$$



Neutrinoless Double Beta Decay

$$(T_{1/2}^{0\nu})^{-1} \propto \begin{cases} a M \varepsilon t & \text{without background} \\ a \varepsilon \sqrt{\frac{M t}{B \Delta E}} & \text{with background} \end{cases}$$

GERDA, 1703.00570, Nature

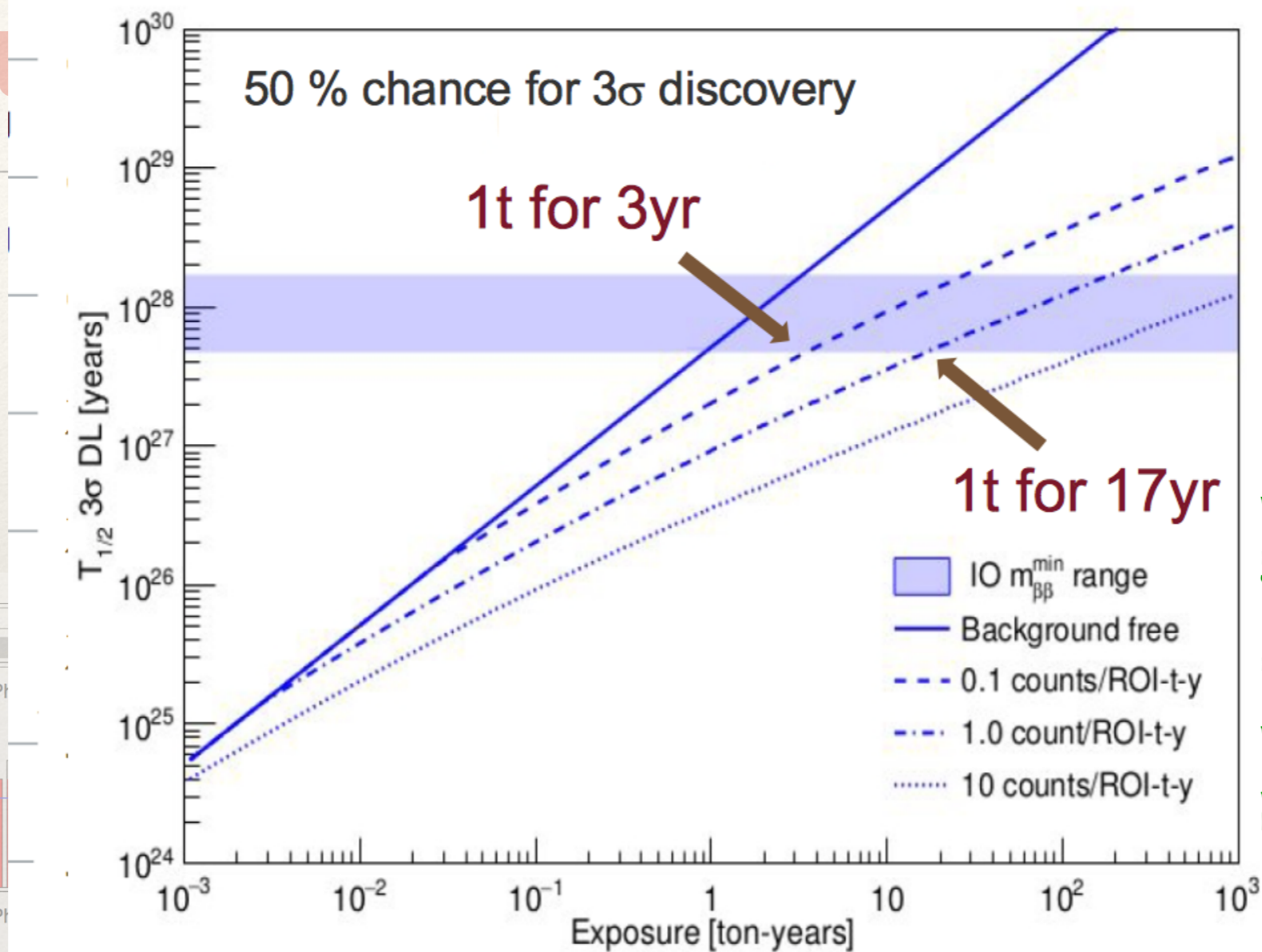


first background free result

current limits: $T_{1/2} \gtrsim 10^{26}$ years
with exposure of about 100 kg · years

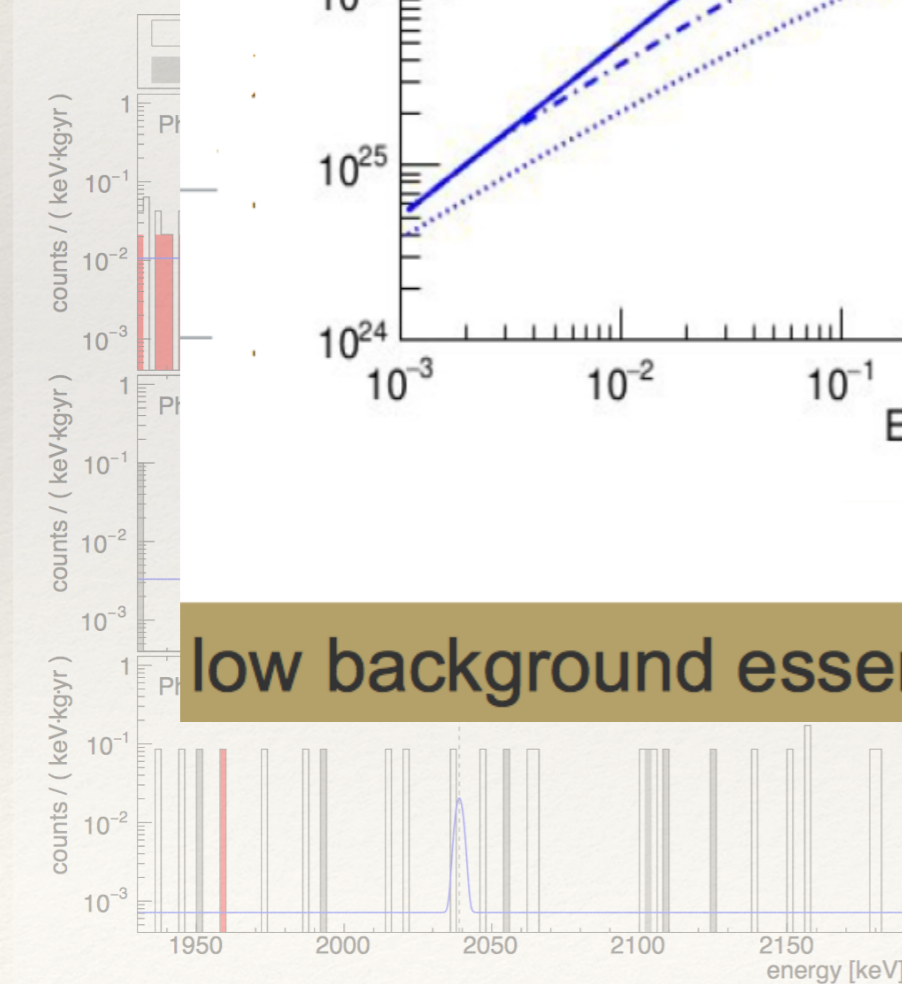
Neutrino

Decay



Plot by Josef Jochum

low background essential for discovery potential



background

free result

10²⁶ years
100 kg · years

GERDA, 1703.00570, Nature

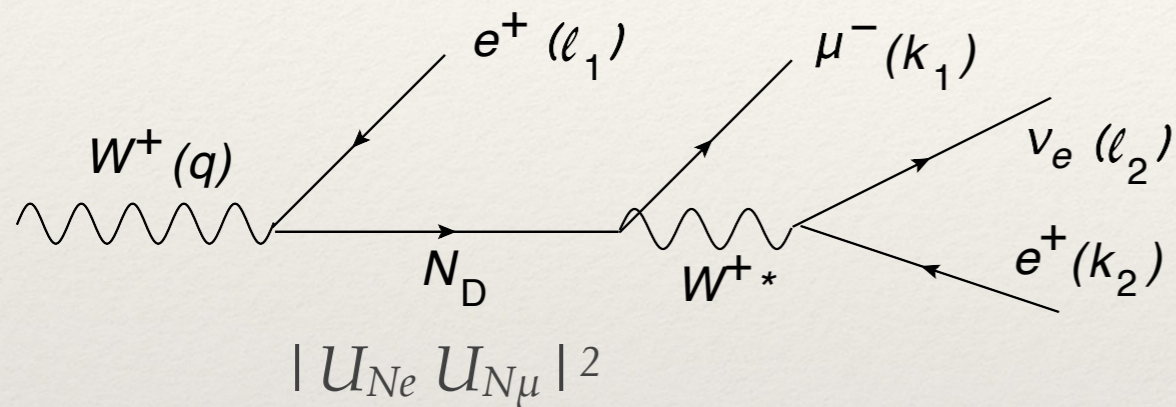
Neutrinoless Double Beta Decay

Table by Josef Jochum

			isotope mass [kg] in FV	FWHM [keV]	background [[FWHM $\epsilon t_{\text{isotope yr}}^{-1}$]	$T_{1/2}$ sensitivity after 4yr [10^{25} yr]	upper m_{β} limit [meV] (lowest NME)
Ge detectors	GERDA	Ge	27	3	5	15	190
	Majorana-D	Ge	24	3	5	15	190
	200 kg	Ge	155	3	1	100	75
	LEGEND 1000 kg	Ge	780	3	0.2	1000	24
liquid noble gas	EXO	Xe	80	88	220	6	240
	nEXO	Xe	4300	58	5	600	24
loaded liquid scintillator	400 kg	Xe	88	250	90	6	240
	KamLAND	Xe	~180	250	~10	50	90
	800 kg	Xe	~180	250	~10	50	90
	SNO+	Te	260	190	60	17	160
cryo bolometers	CUORE	Te	206	5	180	9	210

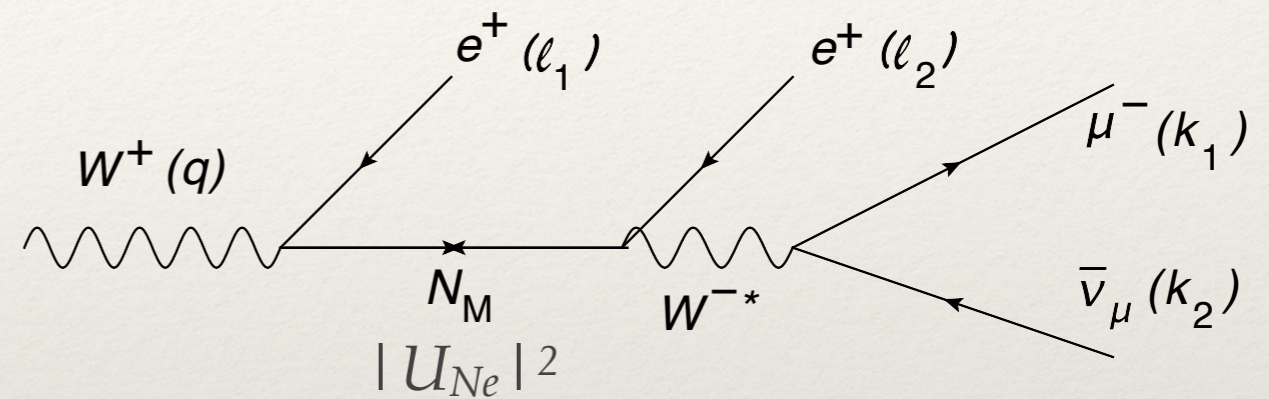
New Idea

assume RH neutrinos with mass less than m_W (*Dib, Kim, 1509.05981*):



$$W^+ \rightarrow e^+ \mu^- e^+ \nu_e$$

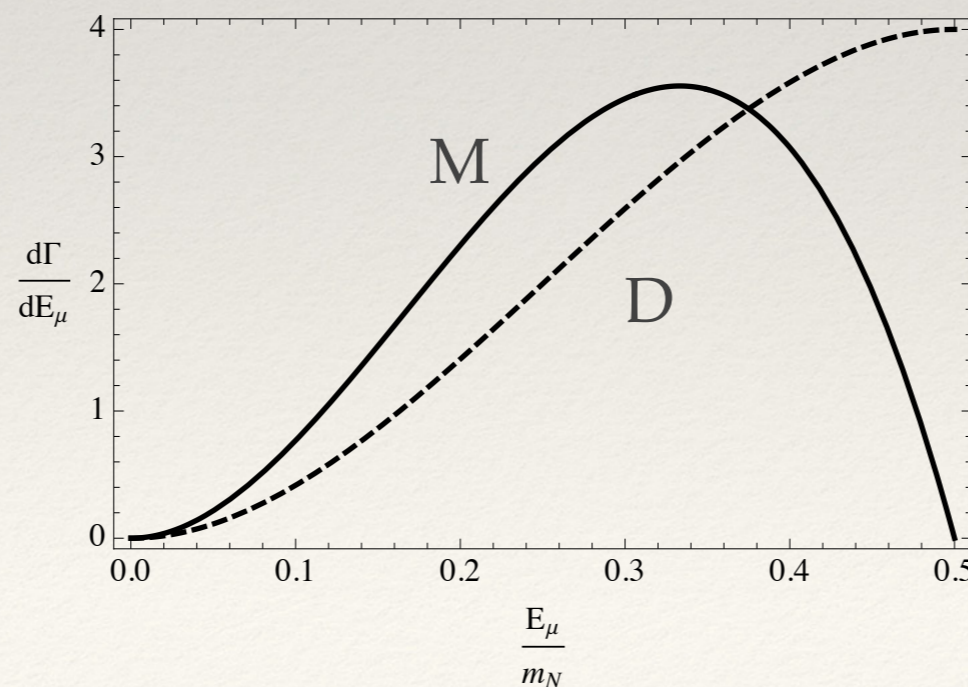
$\Delta L = 0$



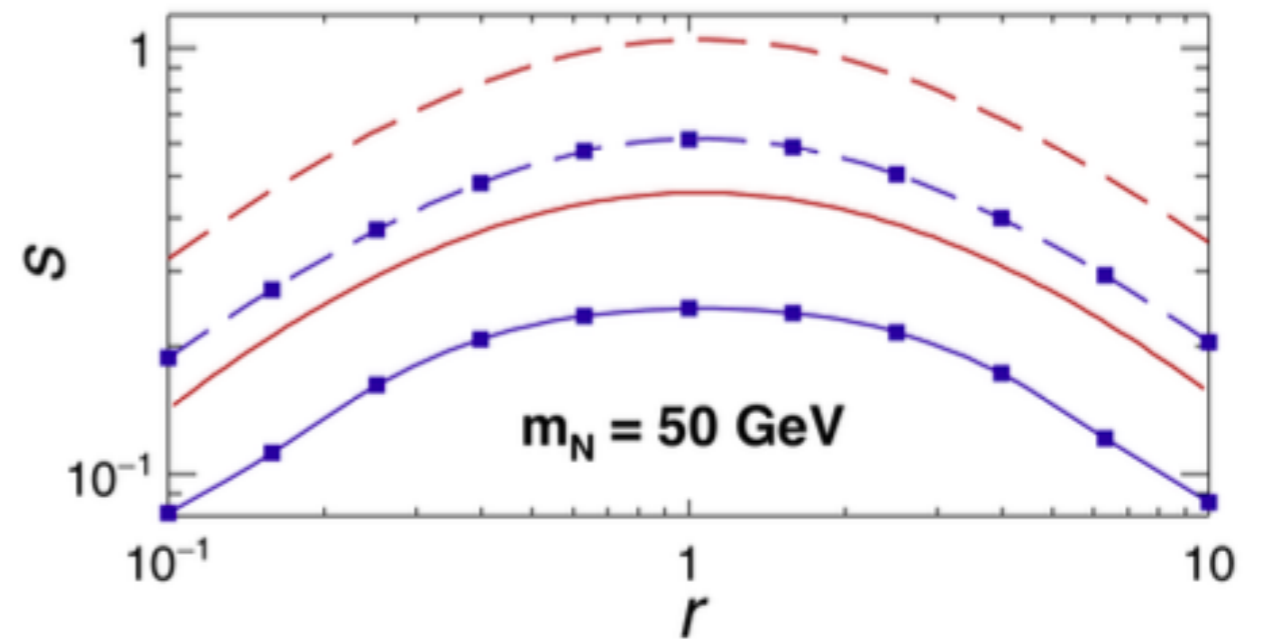
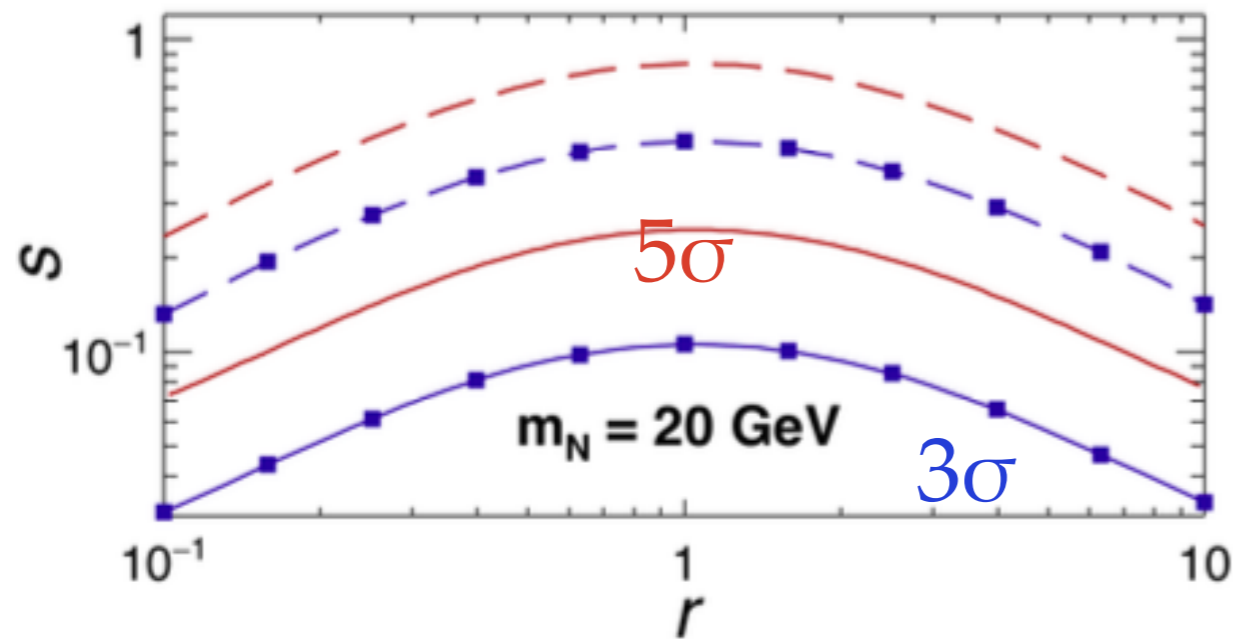
$$W^+ \rightarrow e^+ \mu^- e^+ \text{anti-}\nu_\mu$$

$\Delta L = 2$

hidden in $\nu\dots$
but μ comes from
different vertex!



New Idea



(solid is multi-variate; dashed is cut-and-count)

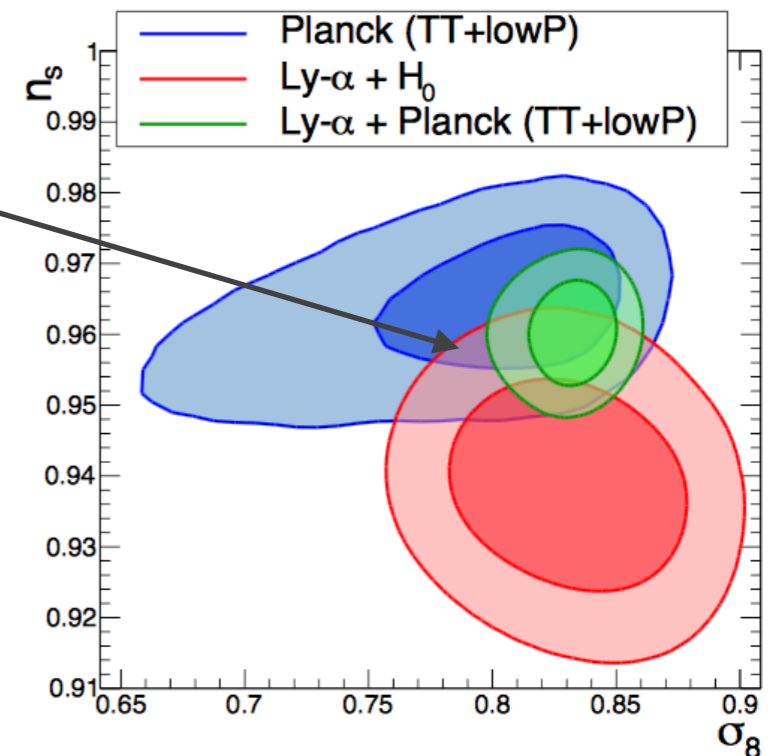
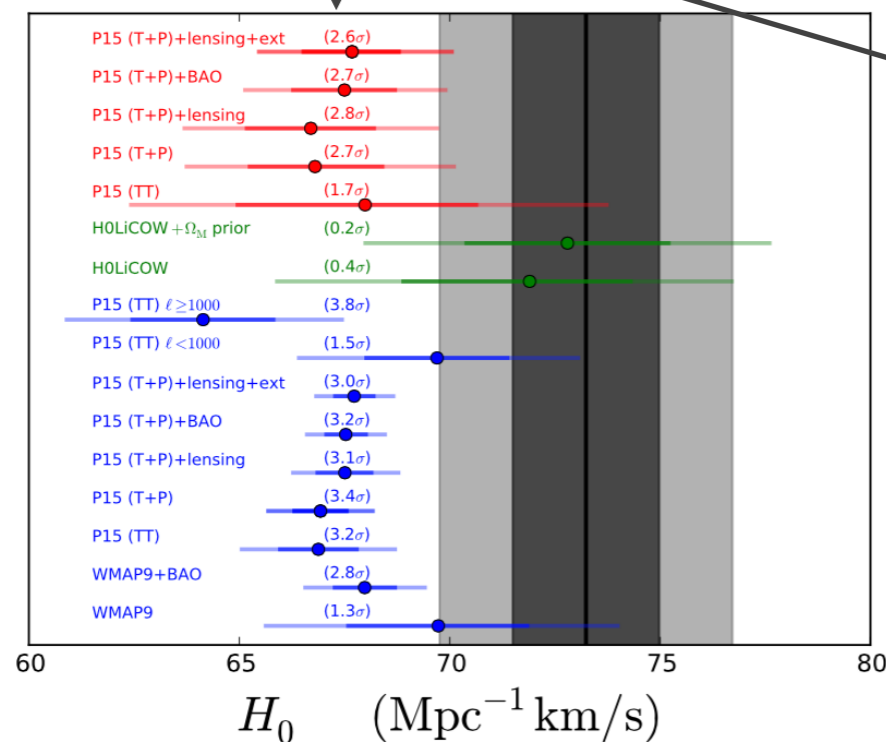
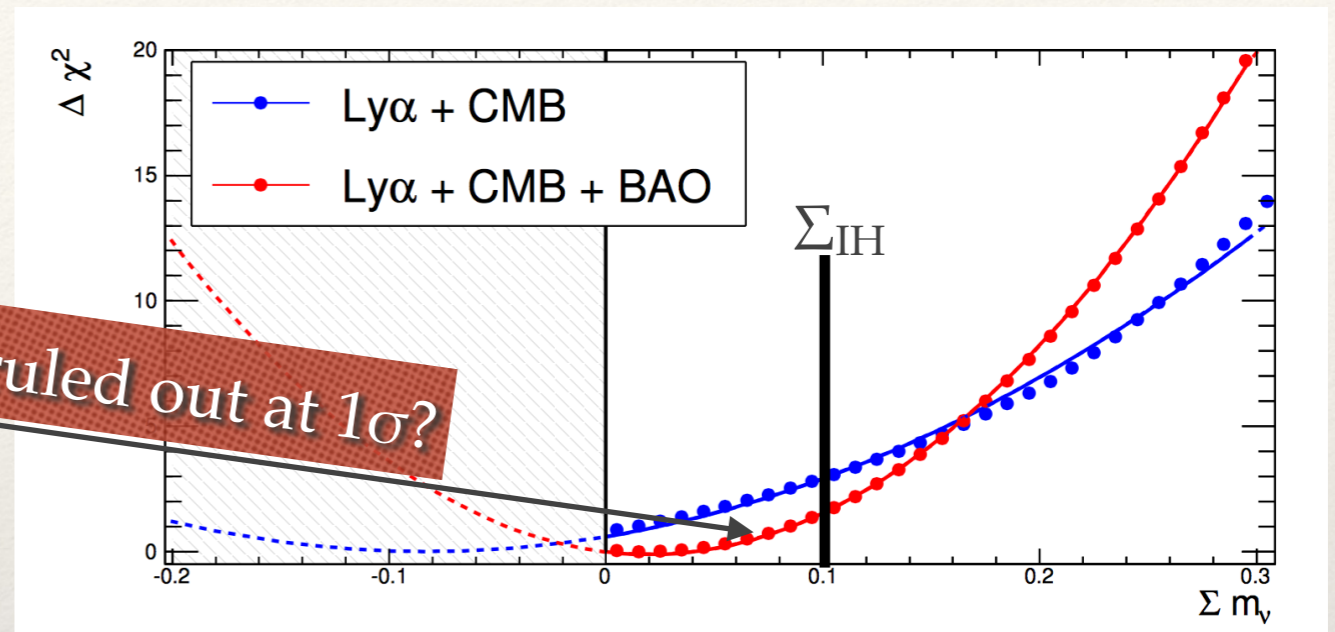
$$s \equiv 2 \times 10^6 \frac{|U_{Ne}U_{N\mu}|^2}{|U_{Ne}|^2 + |U_{N\mu}|^2}, \quad r \equiv \frac{|U_{Ne}|^2}{|U_{N\mu}|^2}.$$

Dib, Kim, Wang, 1703.01936

different vertex!

Cosmological Mass Limits

- ❖ adding more and more data sets: breaks degeneracies and improves limits
- ❖ BUT: can introduce systematics?



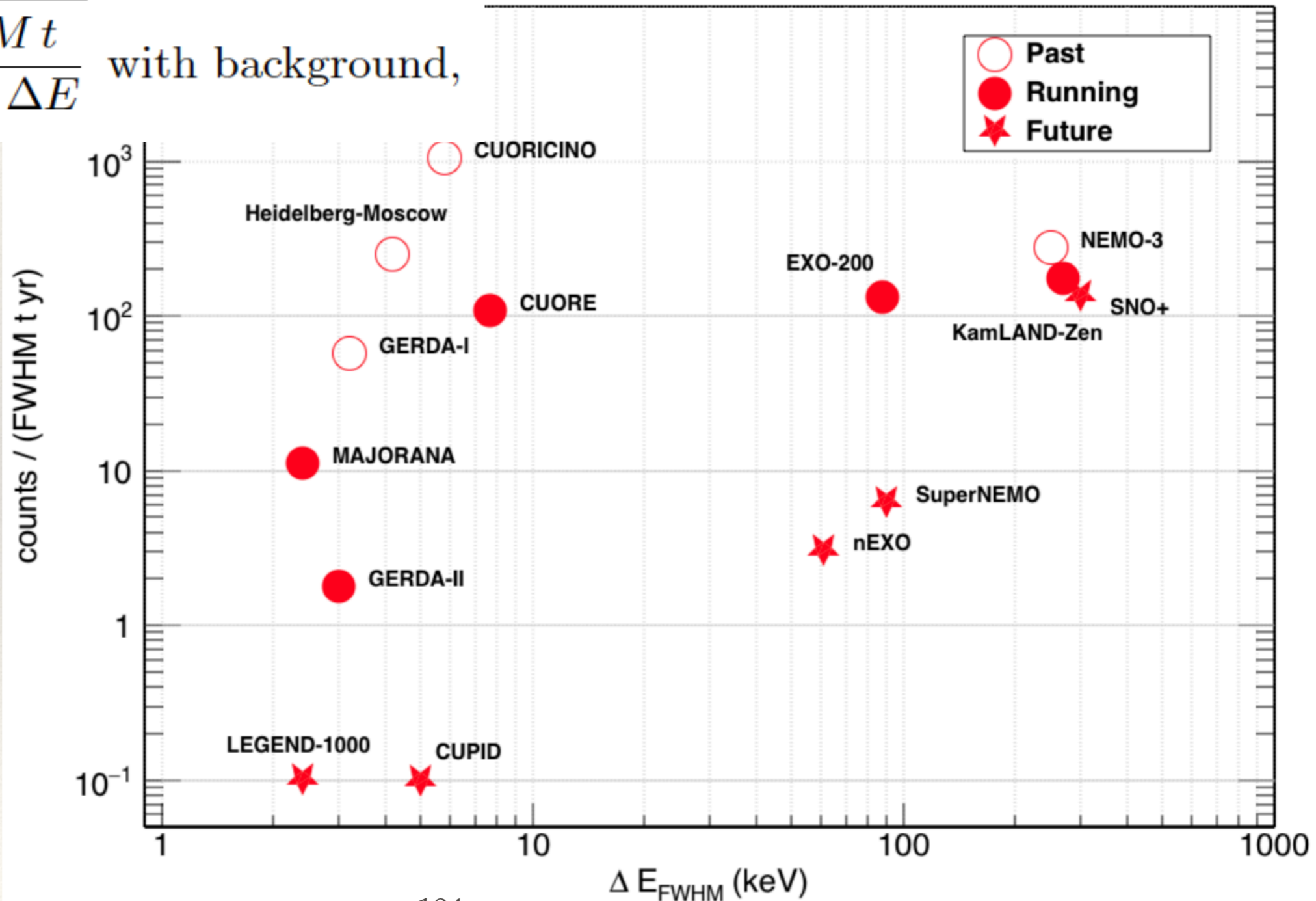
Palanque-Delabrouille et al., 1410.7244 + 1506.05976

Bernal, Verde, Riess, 1607.05617

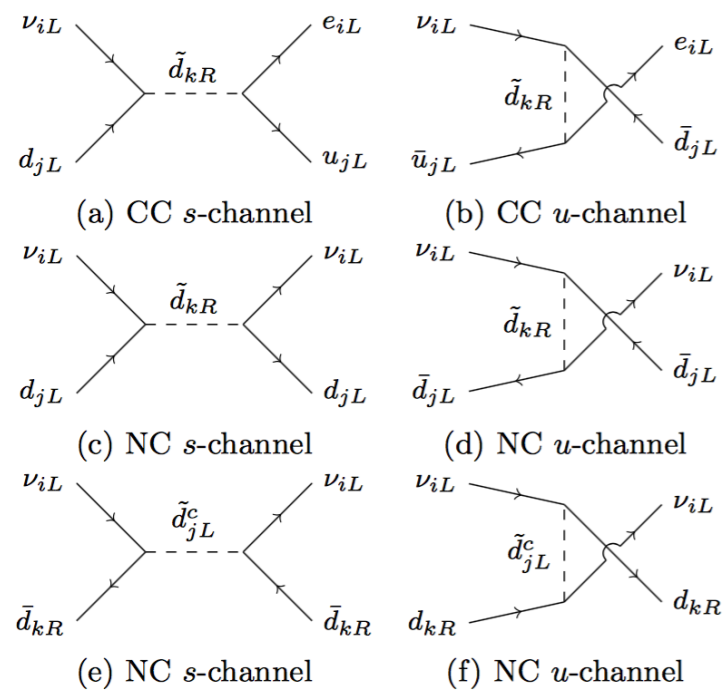
Neutrinoless Double Beta Decay

$$(T_{1/2}^{0\nu}) \propto \begin{cases} a M \varepsilon t & \text{background free,} \\ a \varepsilon \sqrt{\frac{M t}{B \Delta E}} & \text{with background,} \end{cases}$$

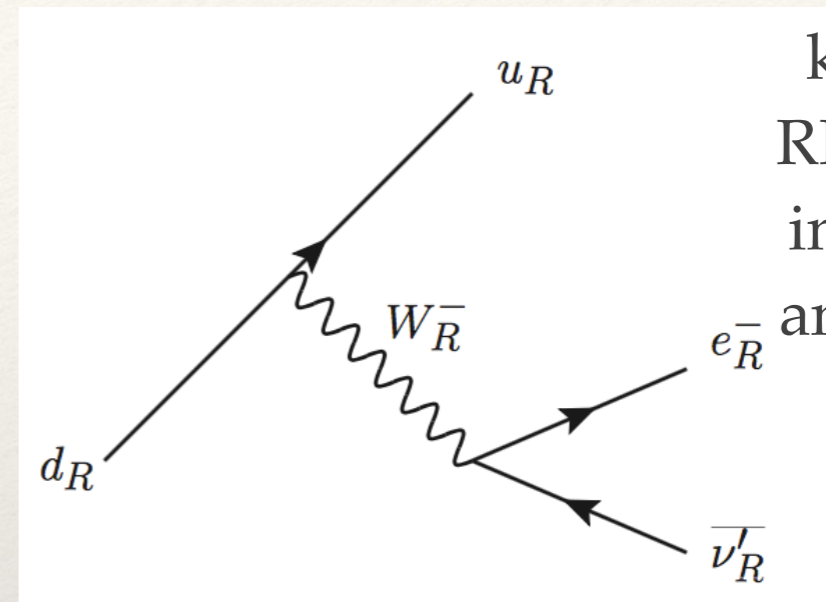
Dolinski, Poon, WR, 1902.04097



Unexpected Correlations with other Experiments



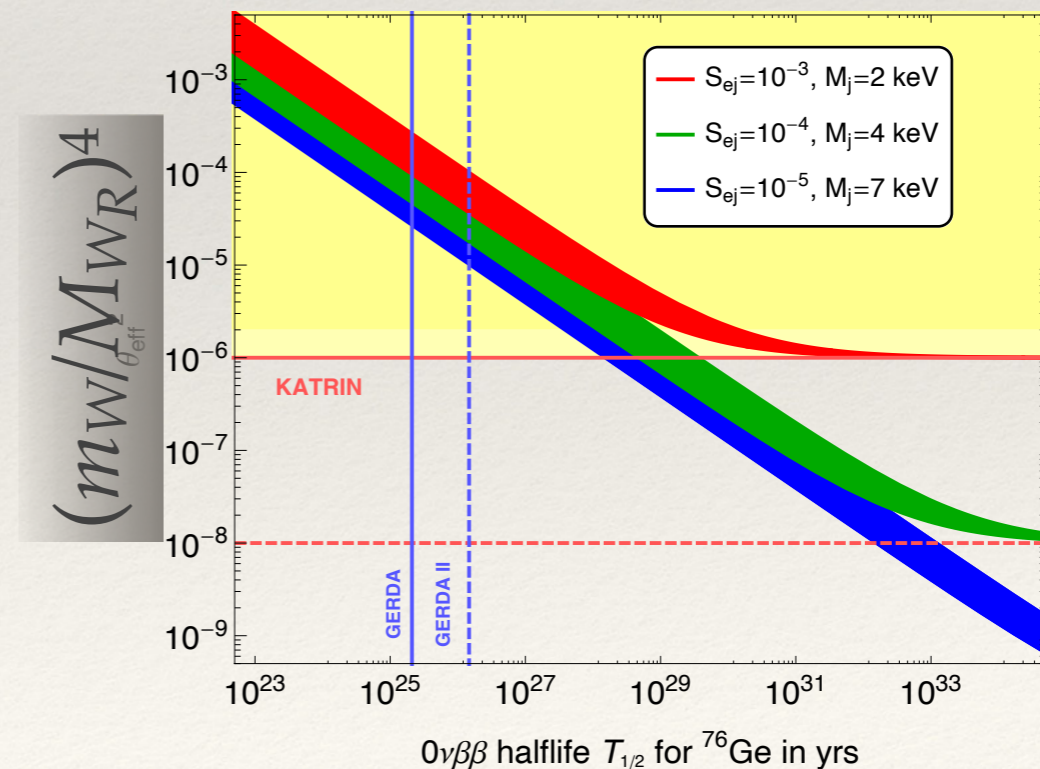
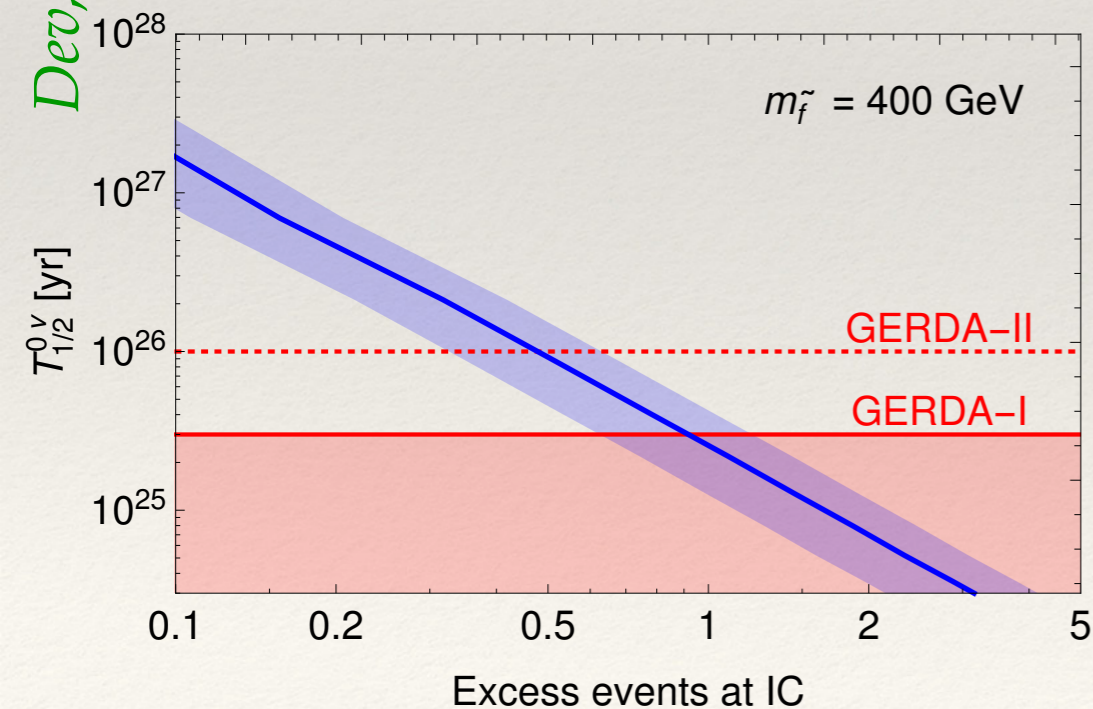
RPV SUSY
at IceCube
and in $0\nu\beta\beta$



keV ν and
RH currents
in KATRIN
and in $0\nu\beta\beta$

Barry, Heck, WR, 1404.5955

Dev, Ghosh, WR, 1605.09743



D vs. M with general interactions

$$\frac{d\sigma}{dT}(\nu + \ell) = \frac{G_F^2 M}{2\pi} \left[A + 2B \left(1 - \frac{T}{E_\nu}\right) + C \left(1 - \frac{T}{E_\nu}\right)^2 \right]$$

$$\frac{d\sigma}{dT}(\bar{\nu} + \ell) = \frac{G_F^2 M}{2\pi} \left[C + 2B \left(1 - \frac{T}{E_\nu}\right) + A \left(1 - \frac{T}{E_\nu}\right)^2 \right]$$

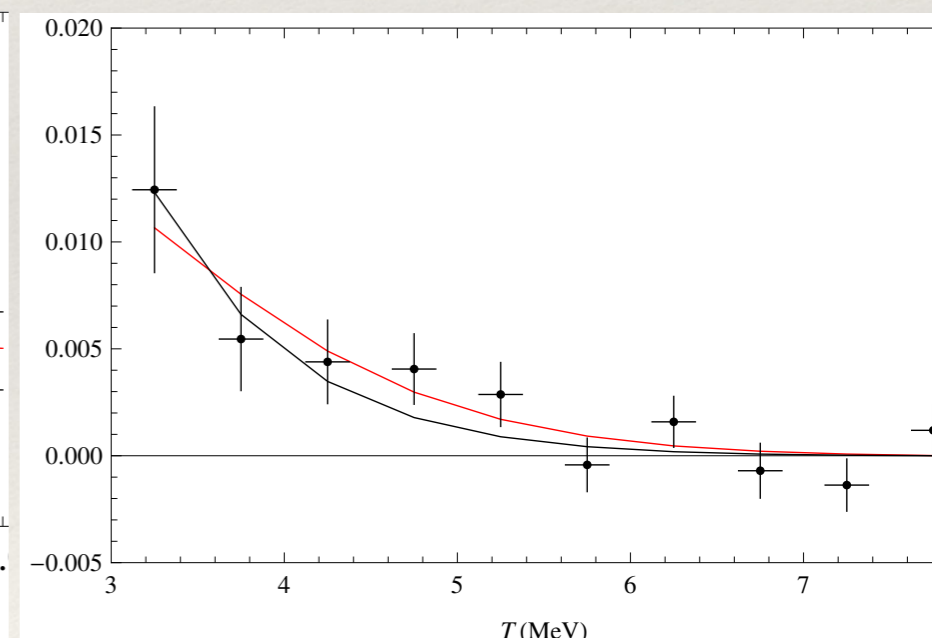
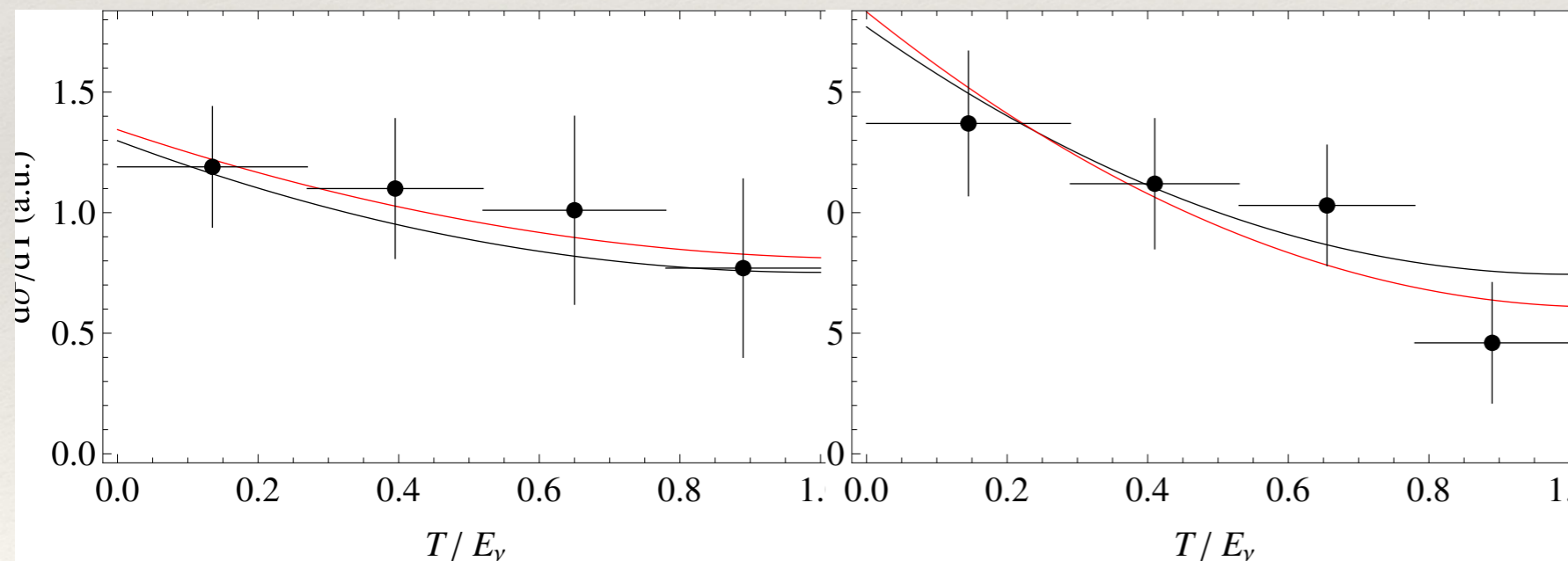
- ❖ SM: same cross sections for Dirac and Majorana

$$(A, B, C)^{\text{SM}} = \left((1 + 2s_W^2)^2, 0, 4s_W^4 \right) \text{ (NC + CC)}$$

- ❖ not the same if other interactions are present!
- ❖ can extract A, B, C due to different E -dependence
- ❖ can also combine neutrino and antineutrino data

Experimental Constraints

- ❖ Data available from CHARM, CHARM-II, LAMPF, MINER ν A, LSND, TEXONO,...
- ❖ take data from expt. with best measurement of $\sin^2 \theta_W$



CHARM-II
 $\nu_\mu e$ scattering

CHARM-II
anti- $\nu_\mu e$ scattering

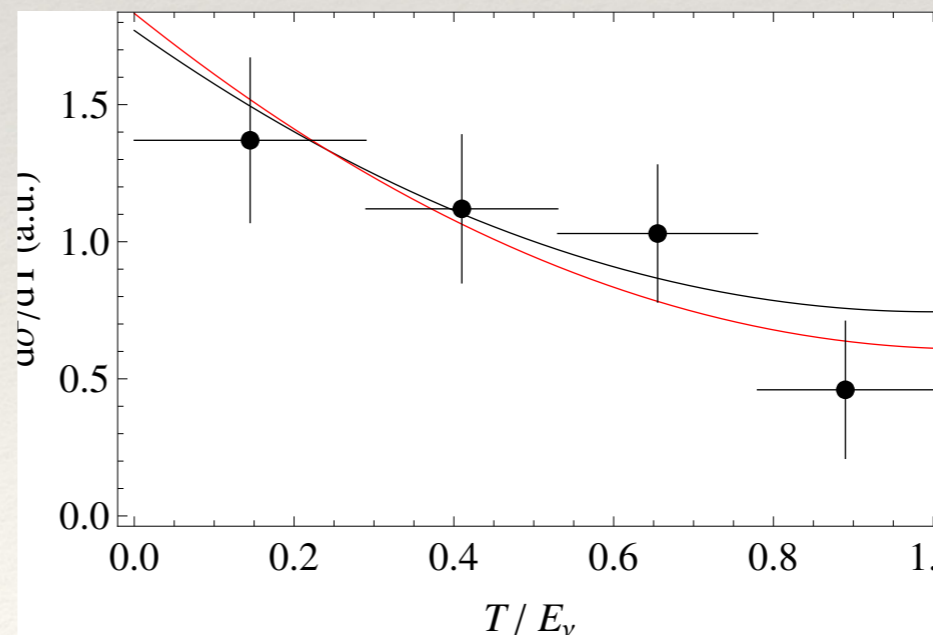
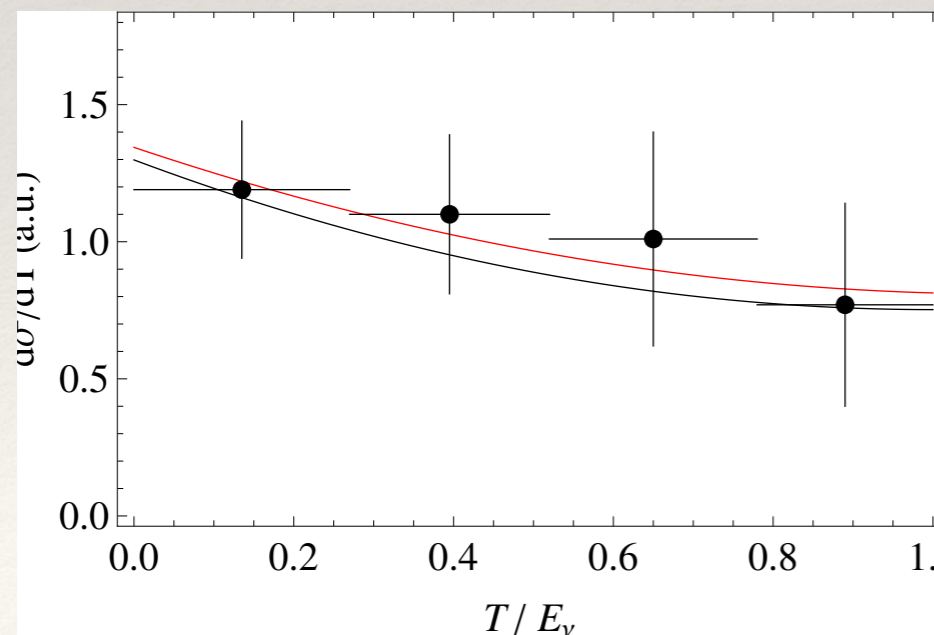
TEXONO
anti- $\nu_e e$ scattering

Experimental Constraints: CHARM-II

- ❖ CHARM-II: highly relativistic $E_\nu \approx 20$ GeV and provide unfolded differential cross sections:

$$\chi^2(A_{\mu e}, B_{\mu e}, C_{\mu e}) = \sum_{i=T \text{ bins}} \frac{\left[\left(\frac{d\sigma}{dT}\right)_i - s_i\right]^2}{\sigma_{s,i}^2} + (\nu_\mu \rightarrow \bar{\nu}_\mu)$$

- ❖ fit $A_{\mu e}, B_{\mu e}, C_{\mu e}$ and translate into $X_{\mu e}, Y_{\mu e}$ for normalization
 $R_{\mu e}$ fixed to SM-value



SM prediction
vs.
best-fit

Experimental Constraints: TEXONO

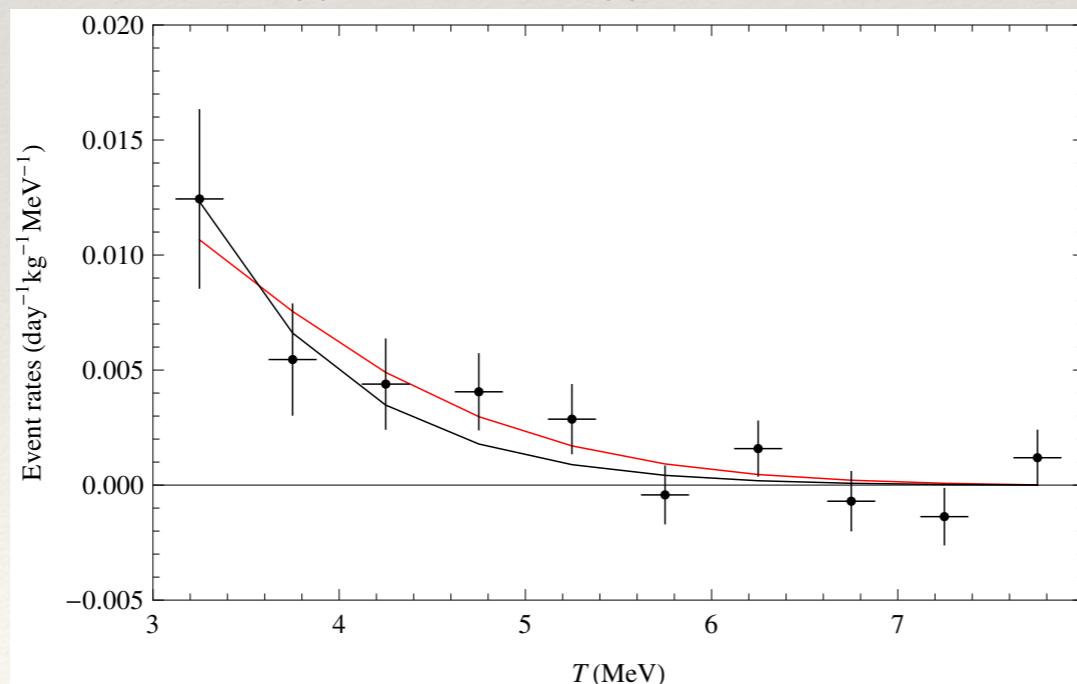
- ❖ reactor neutrinos, thus non-relativistic

- ❖ provide event numbers:

$$N_i = \int_{T_i}^{T_i + \Delta T} dT \int_0^{8 \text{ MeV}} dE_\nu \Phi(E_\nu) \frac{d\sigma}{dT}(T, E_\nu)$$

$$\chi^2(A_{ee}, B_{ee}, C_{ee}, D_{ee}) = \sum_{i=T \text{ bins}} \frac{[N_i - N_i^0]^2}{\sigma_{N,i}^2}$$

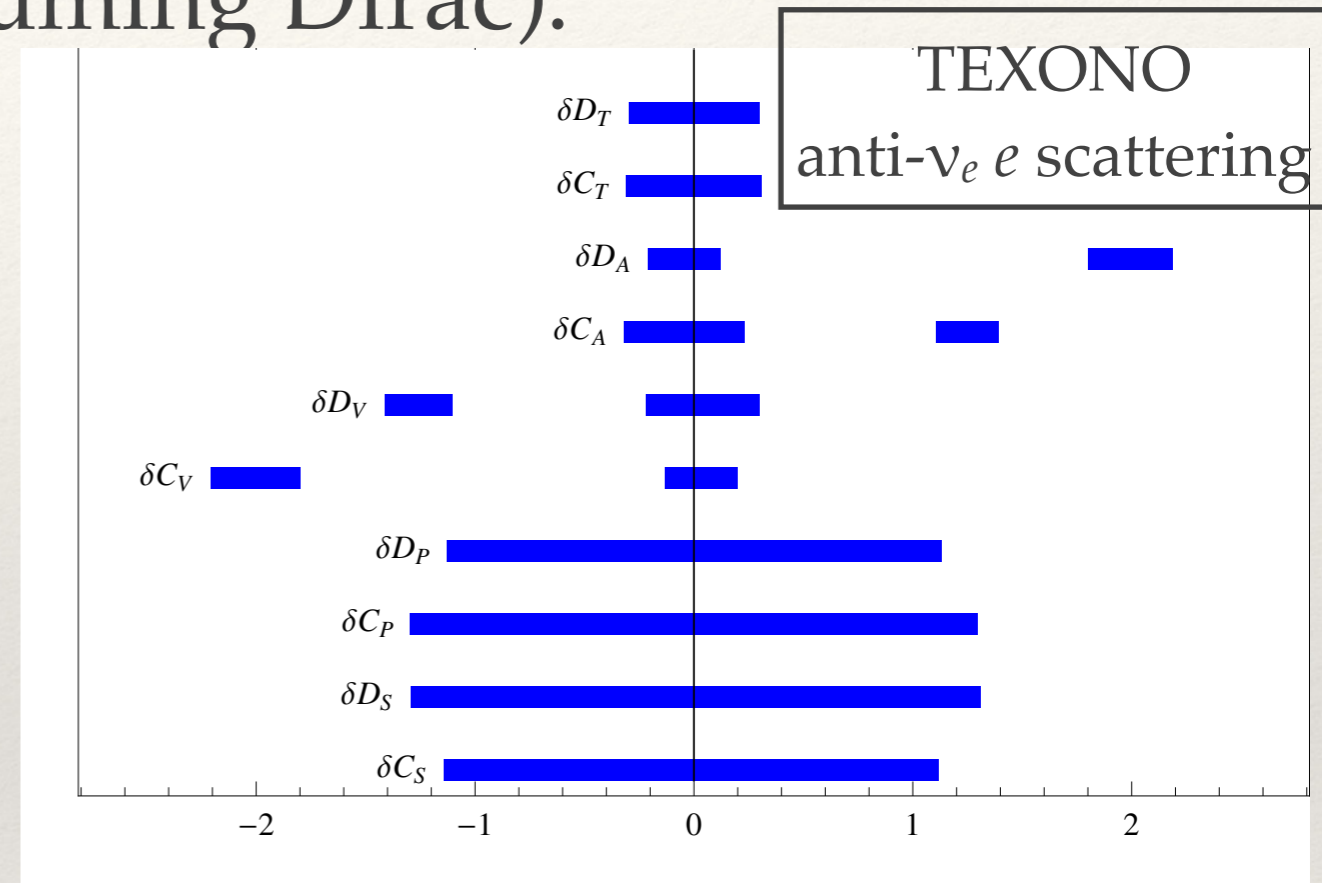
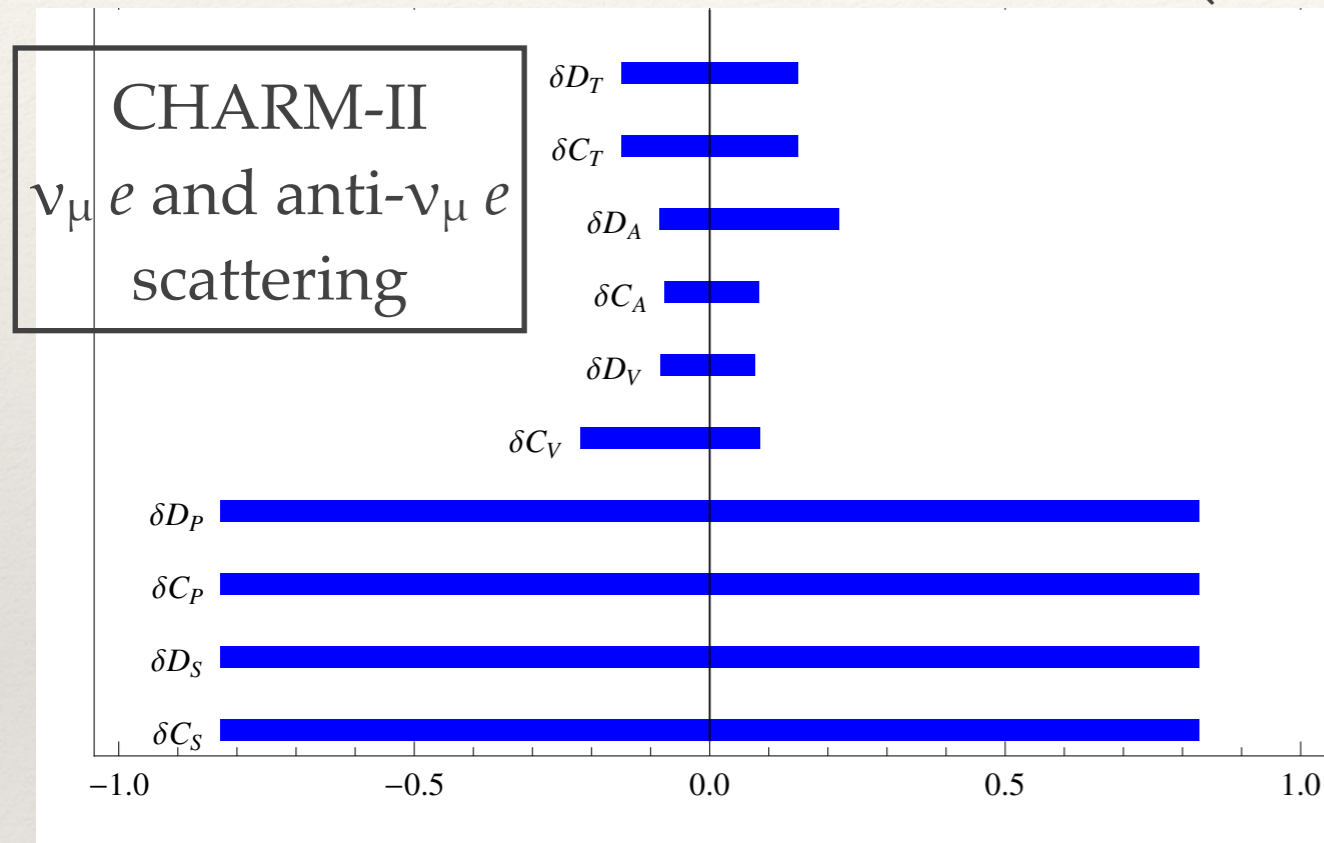
- ❖ fit $A_{ee}, B_{ee}, C_{ee}, D_{ee}$ and translate into X_{ee}, Y_{ee} for normalization R_{ee} and D_{ee} fixed to SM-value



SM prediction
vs.
best-fit

Experimental Constraints

❖ Individual Parameters (assuming Dirac):

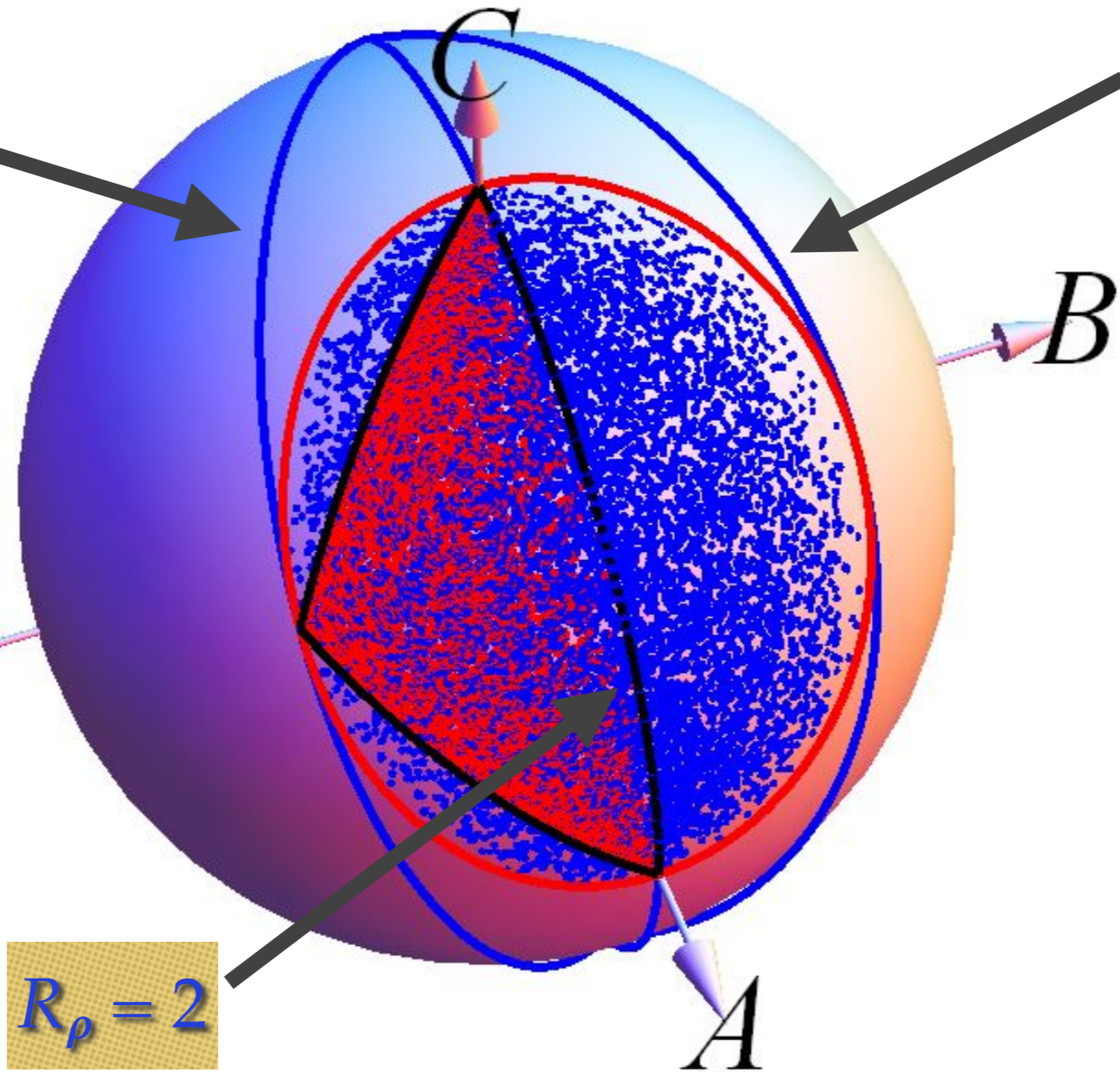


- ❖ weak limits on P and S
- ❖ T , V and A well constrained

D vs. M with general interactions

$$R_\rho = 0$$

$$R_\rho = 4$$



Dirac vs. Majorana

the ratios

$$\sqrt{B^2 + C^2}$$

- ❖ measure
- ❖ measure
- ❖ actually,

$$X \equiv \frac{B}{R}$$

- ❖ gives for

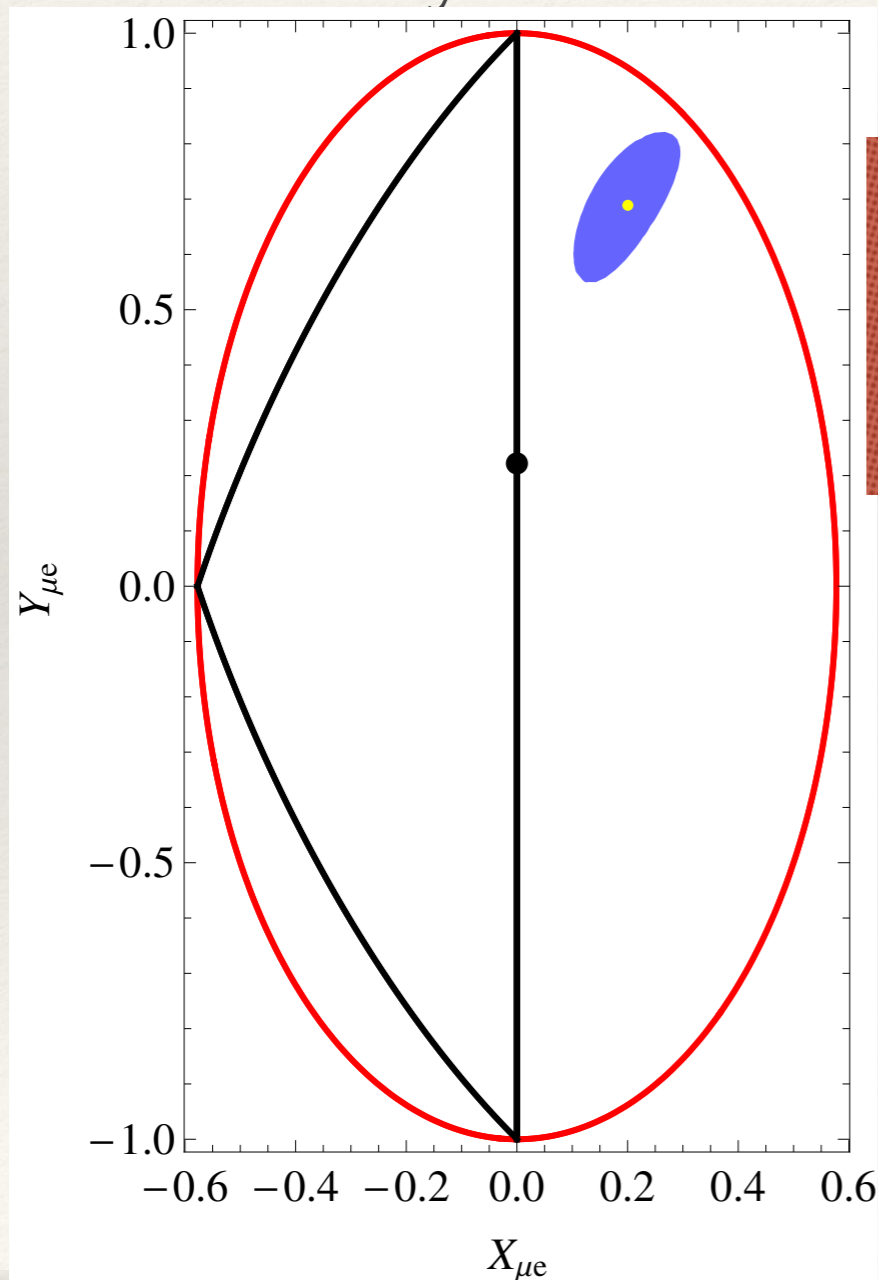
- ❖ for Majorana neutrinos:

$$2X^2 + (Y \pm X)^2 \leq 1 \quad \text{and} \quad X \leq 0$$

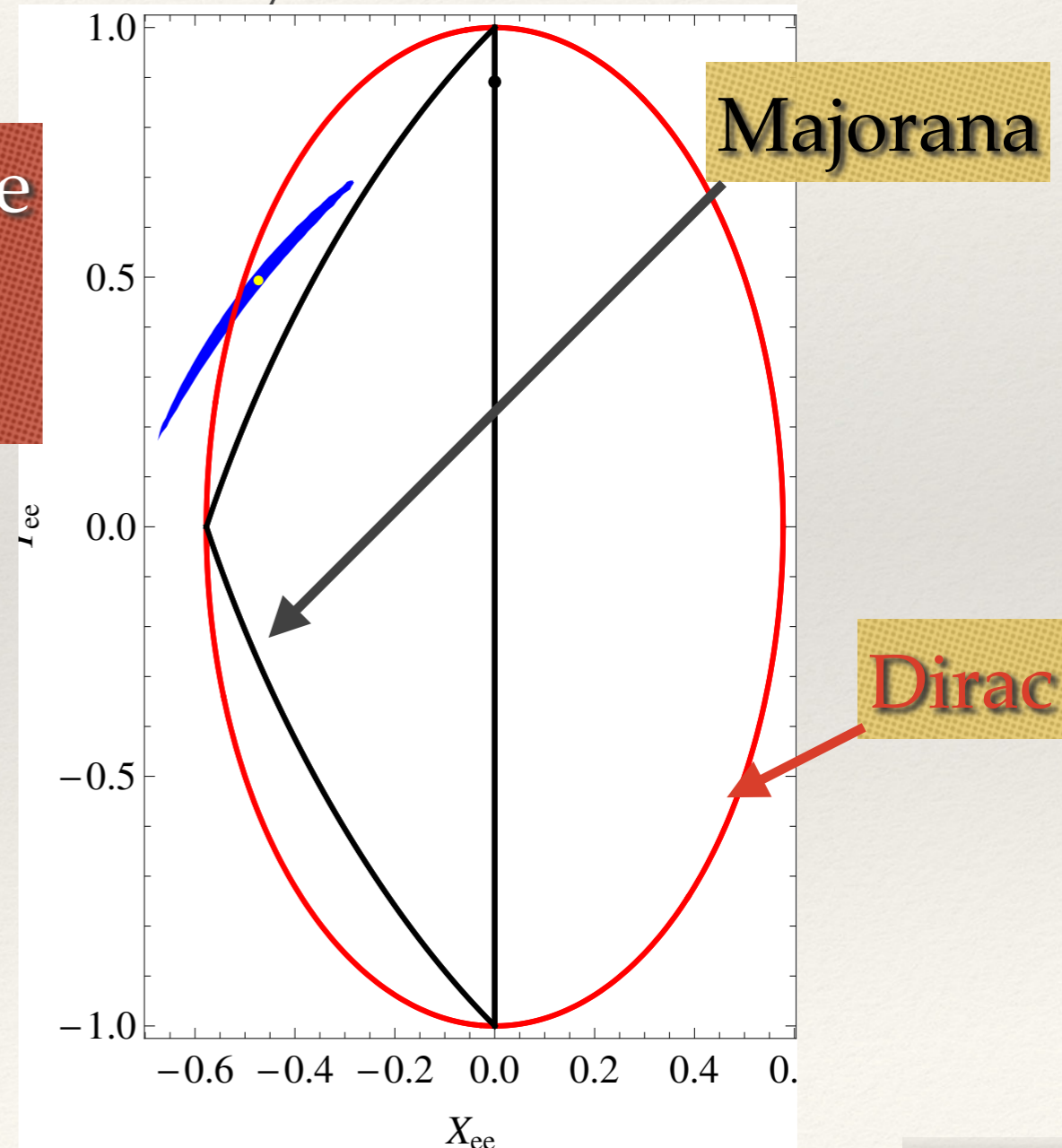
WR, Xu, Yaguna, 1702.05721

Future Constraints

- ❖ choose points in allowed 90% range, assume uncertainty reduced by factor 3 and 4, respectively:

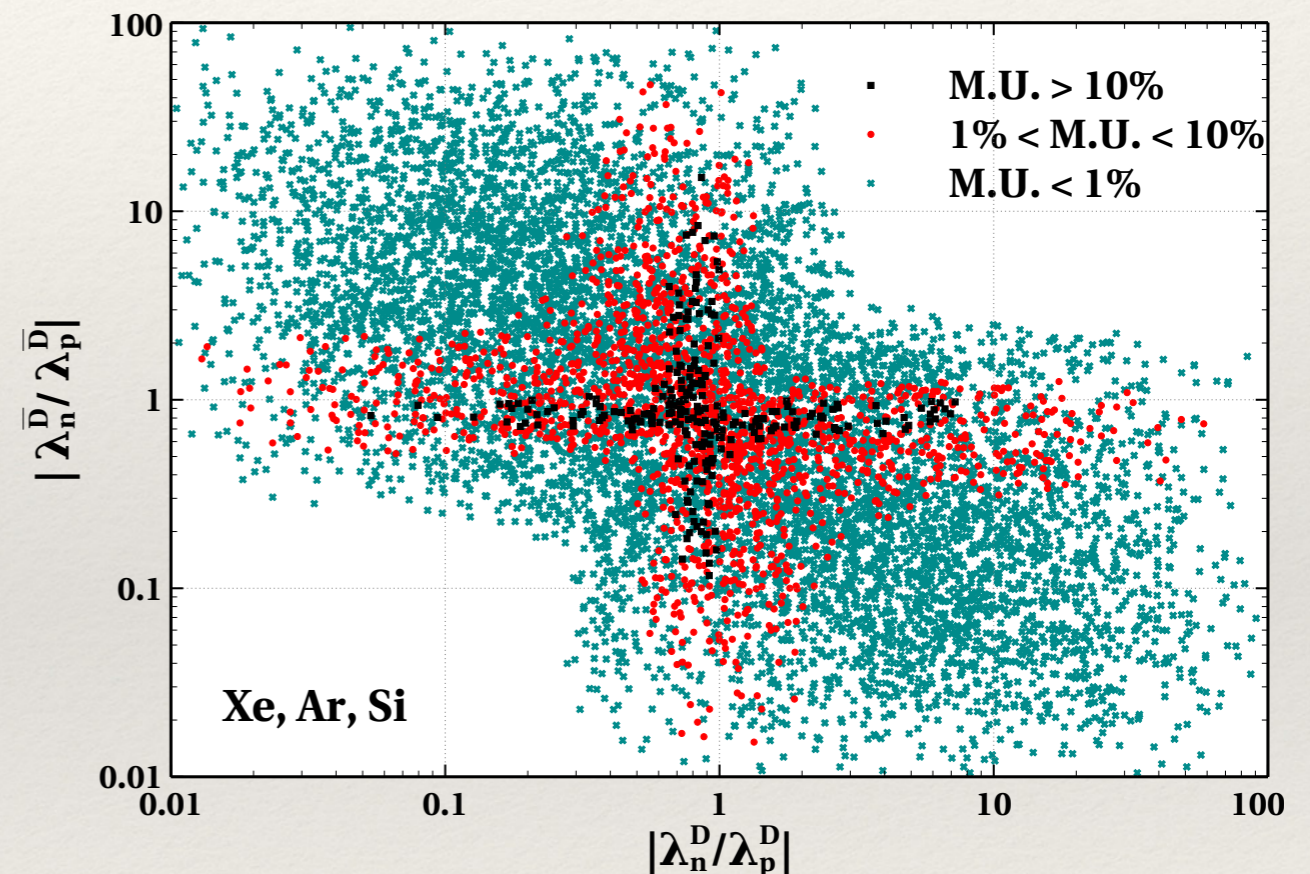
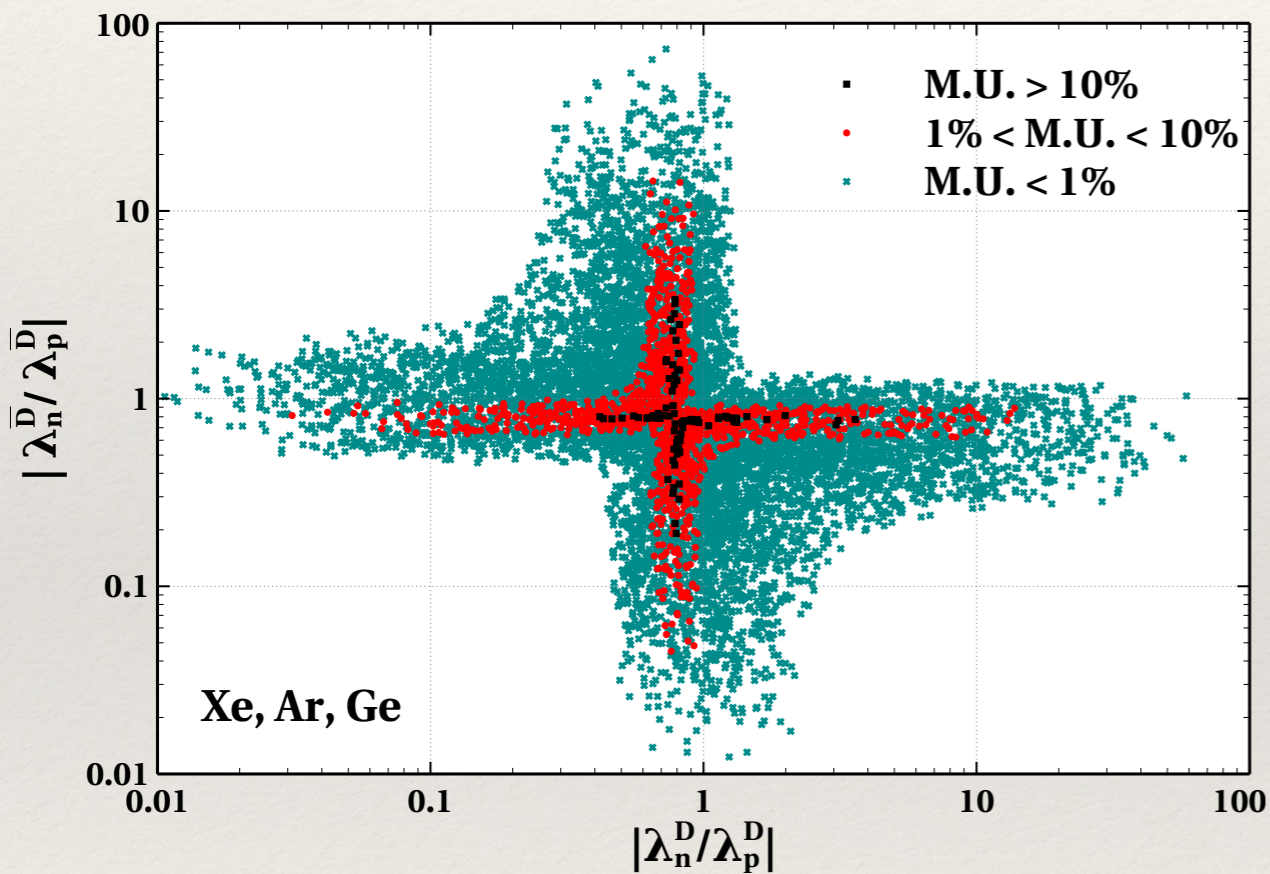


could prove
Dirac
nature!



Analysis

Assume Dirac DM and find values of the four interaction parameters such that data can not be explained in Majorana interpretation



Minimal Uncertainty to exclude Majorana particle:
larger than 10%

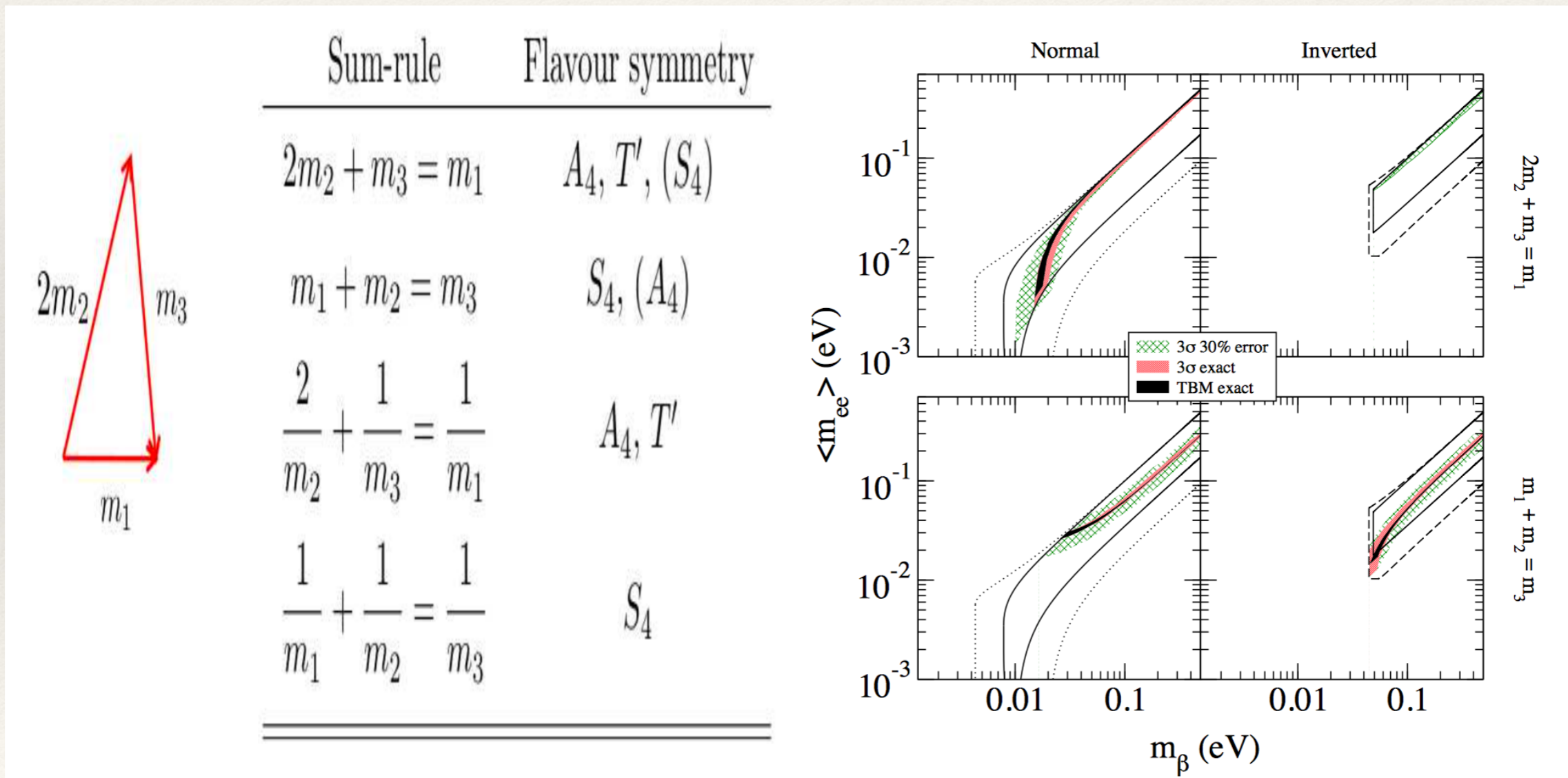
between 1% and 10%

between 0.1% and 1%

$\lambda_n^D/\lambda_p^D < 0$
 \Rightarrow need partial cancellation between
 proton and neutron contributions to σ_{tot}
 of either particle or antiparticle

Predicting the effective mass

Flavor Symmetry models can not predict masses,
but relations between them:



Barry, WR, 1007.5217

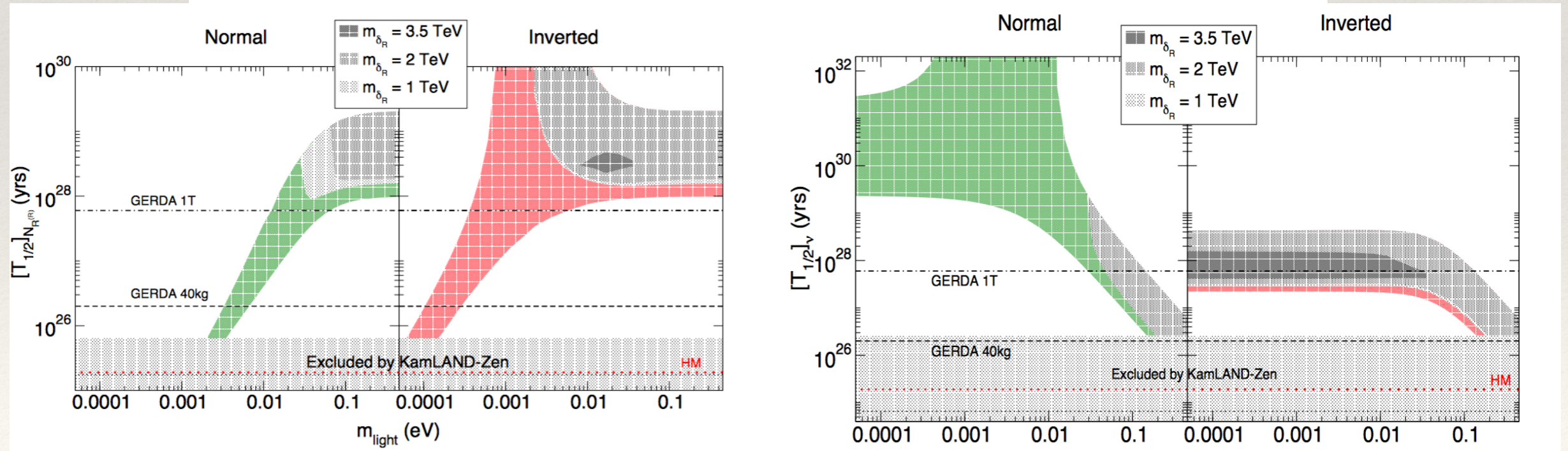
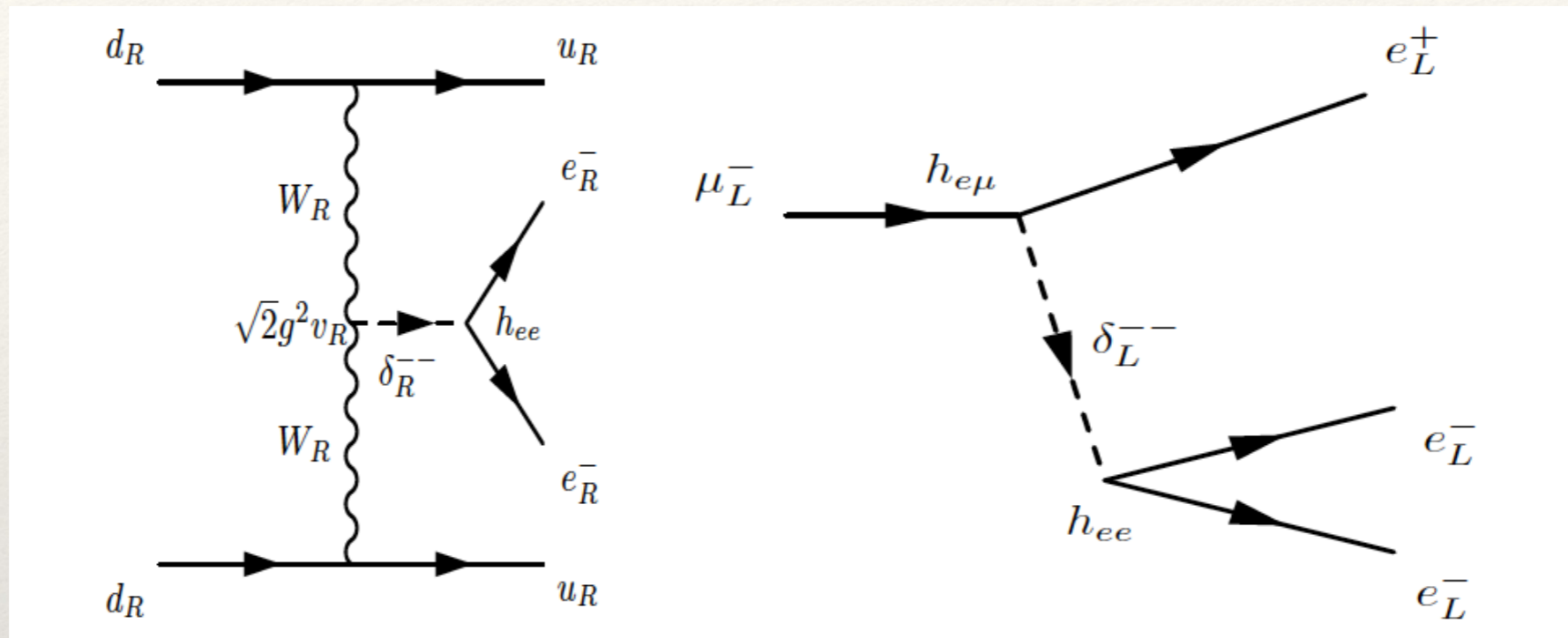
Scales

- ❖ $0\nu\beta\beta$ standard mechanism: $T_{1/2} \propto 1 / (m_\nu^2)$
- ❖ $0\nu\beta\beta$ standard and Weinberg: $T_{1/2} \propto \Lambda^2$
- ❖ $0\nu\beta\beta$ and heavy Physics: $T_{1/2} \propto \Lambda^{10}$
- ❖ cf. to proton decay with $T_{1/2} \propto \Lambda^4$
- ❖ cf. to neutron-antineutron oscillation $P \propto \Lambda^{10}$

Scales

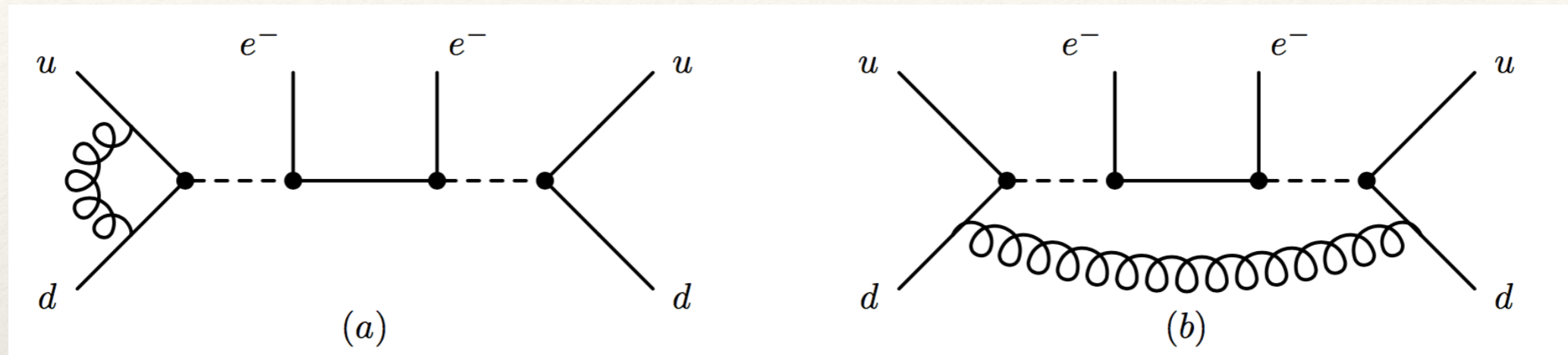
- ❖ $0\nu\beta\beta$ standard mechanism: $T_{1/2} \propto 1 / (m_\nu^2)$
- ❖ $0\nu\beta\beta$ standard and Weinberg: $10^4\text{-}10^{14}$ GeV
- ❖ $0\nu\beta\beta$ and heavy Physics: $T_{1/2} \propto \Lambda^{10}$ 10^3 GeV
- ❖ cf. to proton decay with $T_{1/2} \propto \Lambda^4$ 10^{16} GeV
- ❖ cf. to neutron-antineutron oscillation $P \propto 10^6$ GeV

LFV and Double Beta Decay



Barry, WR, 1303.6324

QCD Corrections

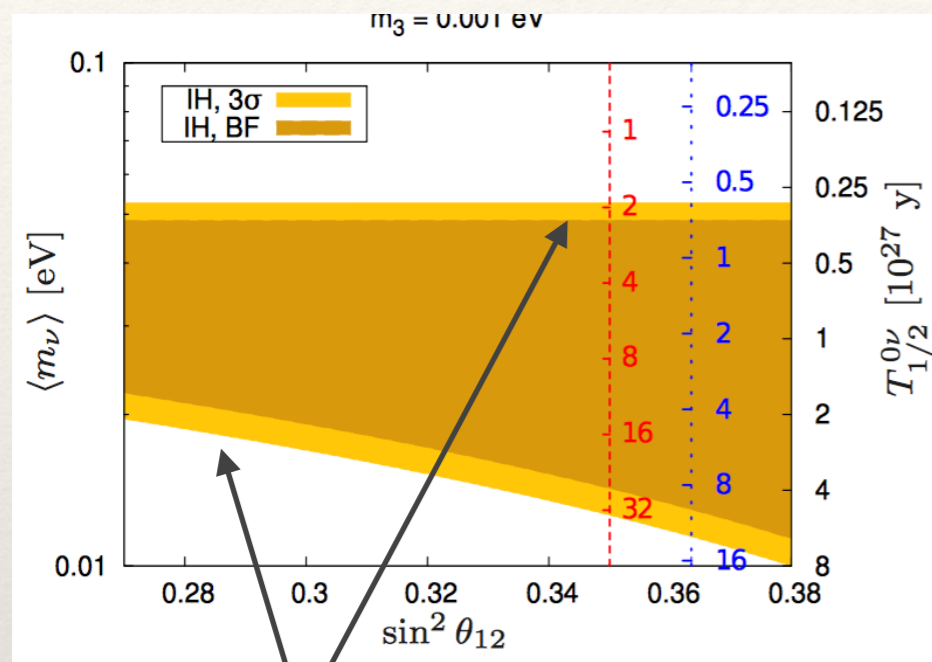


- ❖ naive size $(\alpha_s/4\pi) \ln (M_W/100 \text{ MeV})^2 \simeq 10\%$, true for standard diagram
- ❖ creates in non $(V-A) \otimes (V-A)$ short-range mechanisms color non-singlets, Fierzing to singlets gives different operators with vastly different NMEs
- ❖ \Rightarrow can give effect exceeding NME uncertainty...

Mahajan, PRL 112; Gonzalez, Kovalenko, Hirsch, PRD 93;

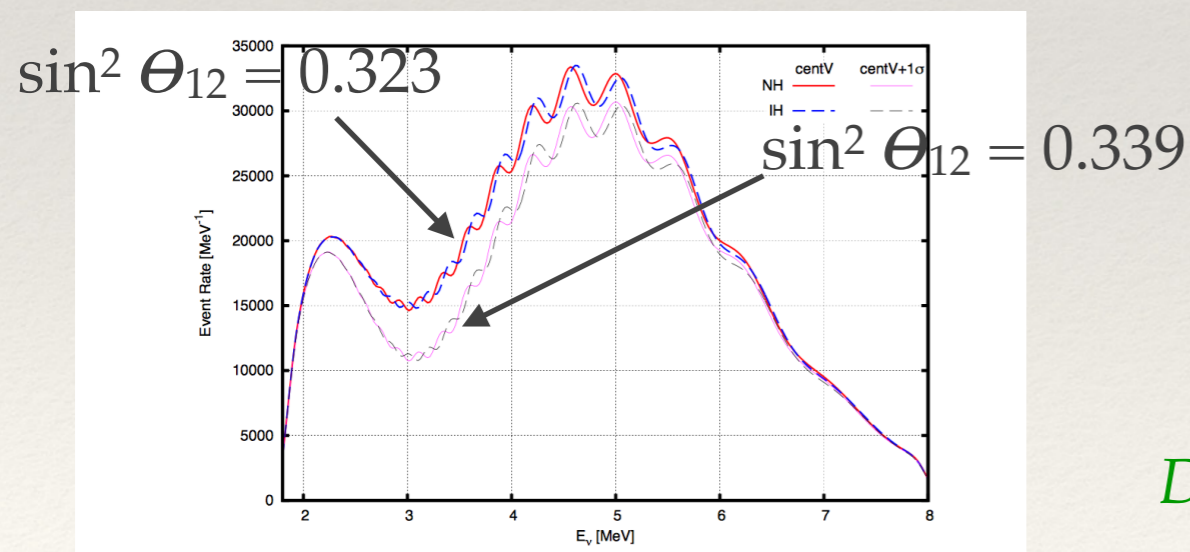
Peng, Ramsey-Musolf, Winslow, PRD 93

Connections to Oscillation Experiments



Nature gives us two scales

Factor 2 uncertainty of minimal m_{ee} in IH, mostly from θ_{12}

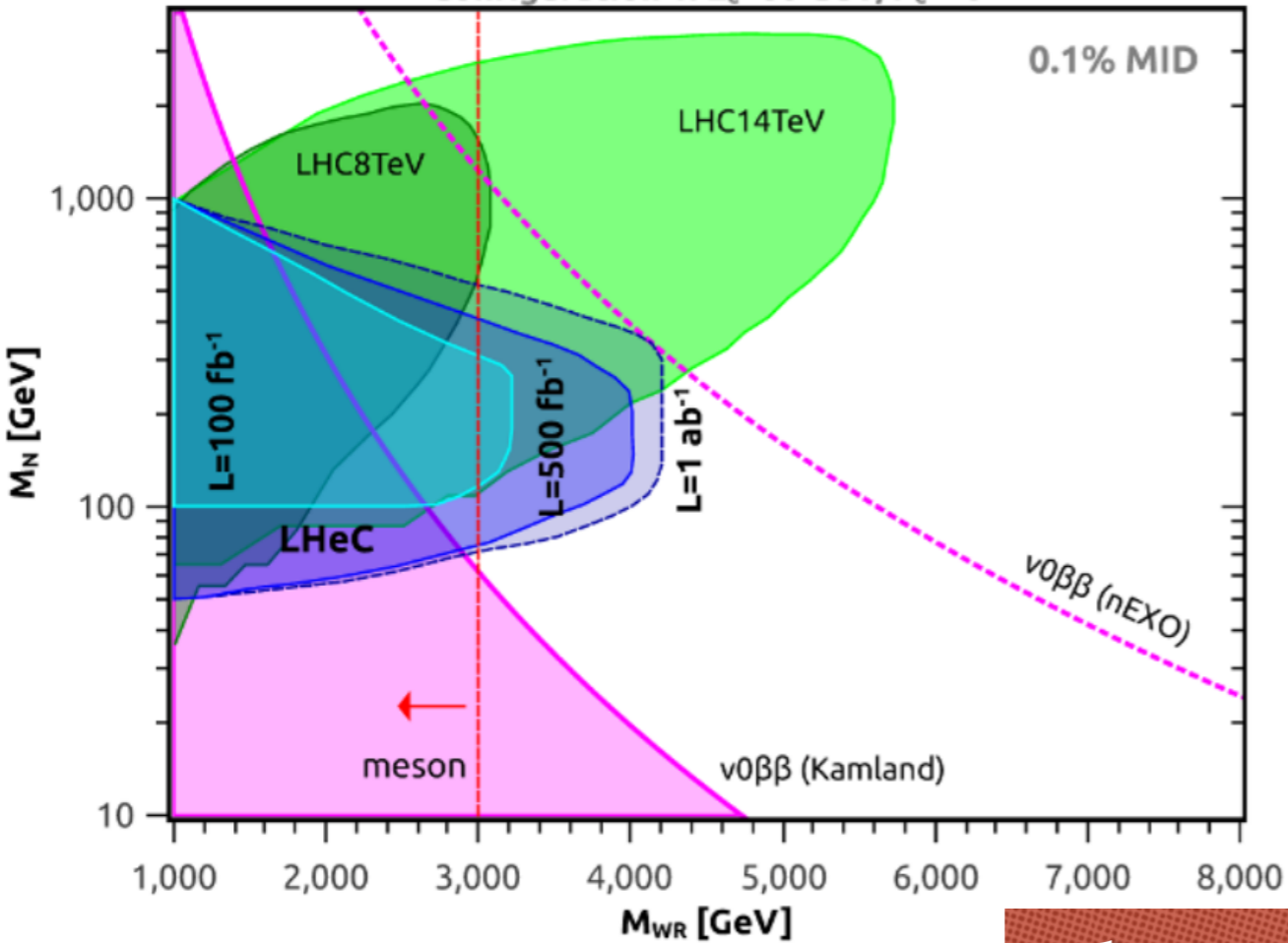


JUNO will fix θ_{12} and remove uncertainty in value of minimal m_{ee} in IH

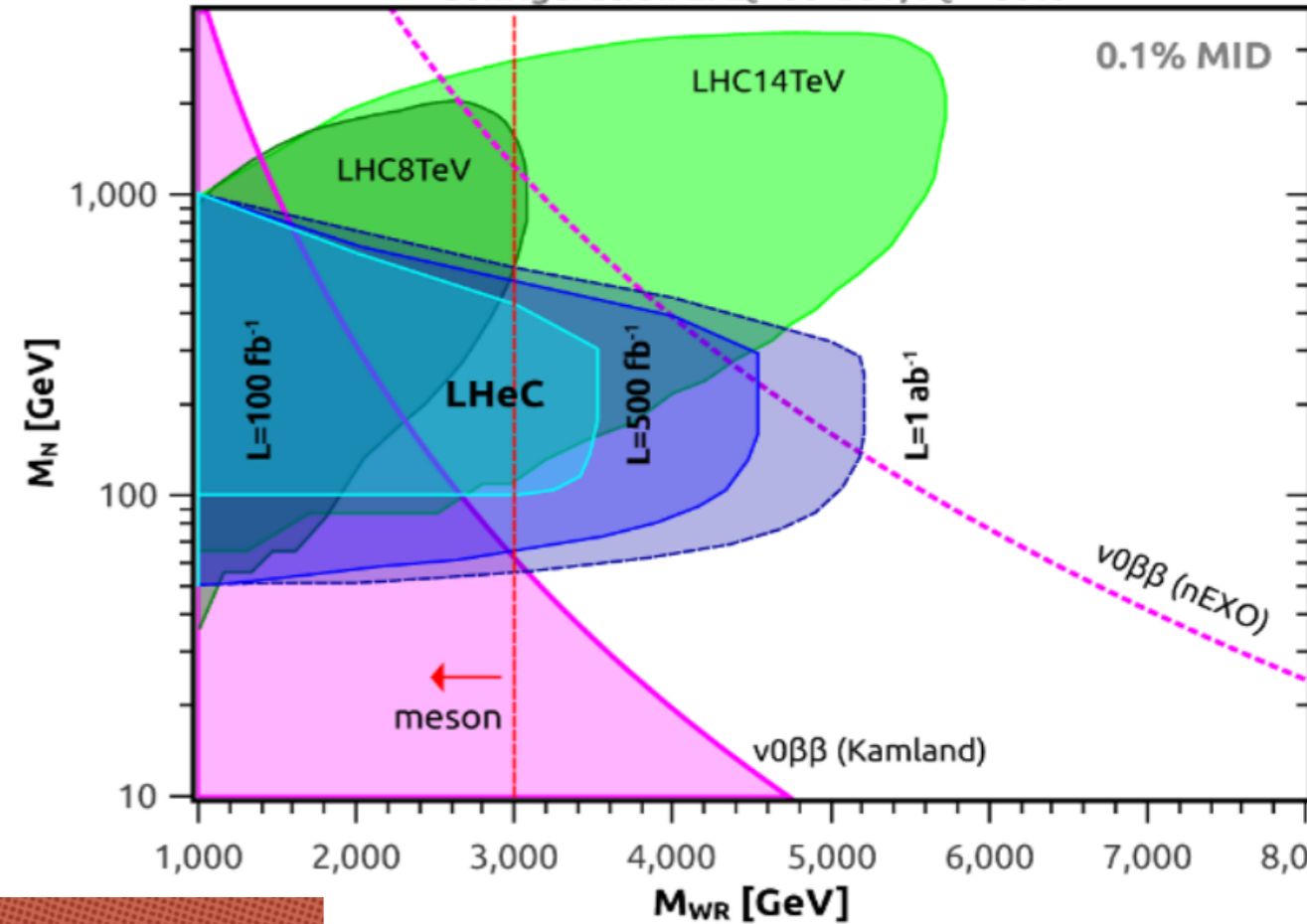
Dueck, WR, Zuber, 1103.4152; Ge, WR, 1507.05514

LHC and Double Beta Decay

Configuration 1: $E_e=60$ GeV, $P_e = 0$



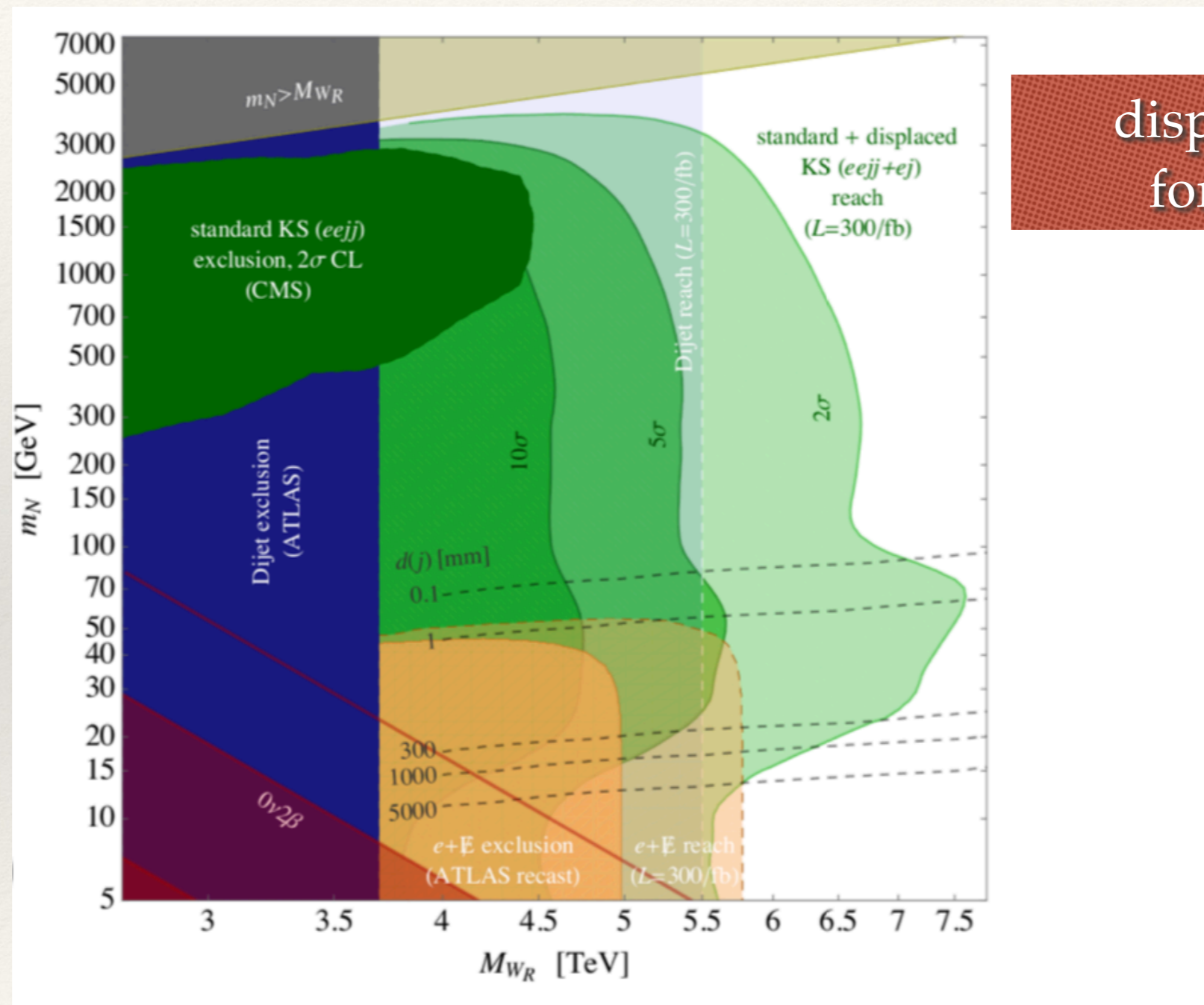
Configuration 2: $E_e=60$ GeV, $P_e = 80\%$



polarization at LHeC

*Lindner, Queiroz,
WR, Yaguna, JHEP1606*

LHC and Double Beta Decay



displaced vertices
for low masses

Nemevsek, Nesti, Popara, 1801.05813

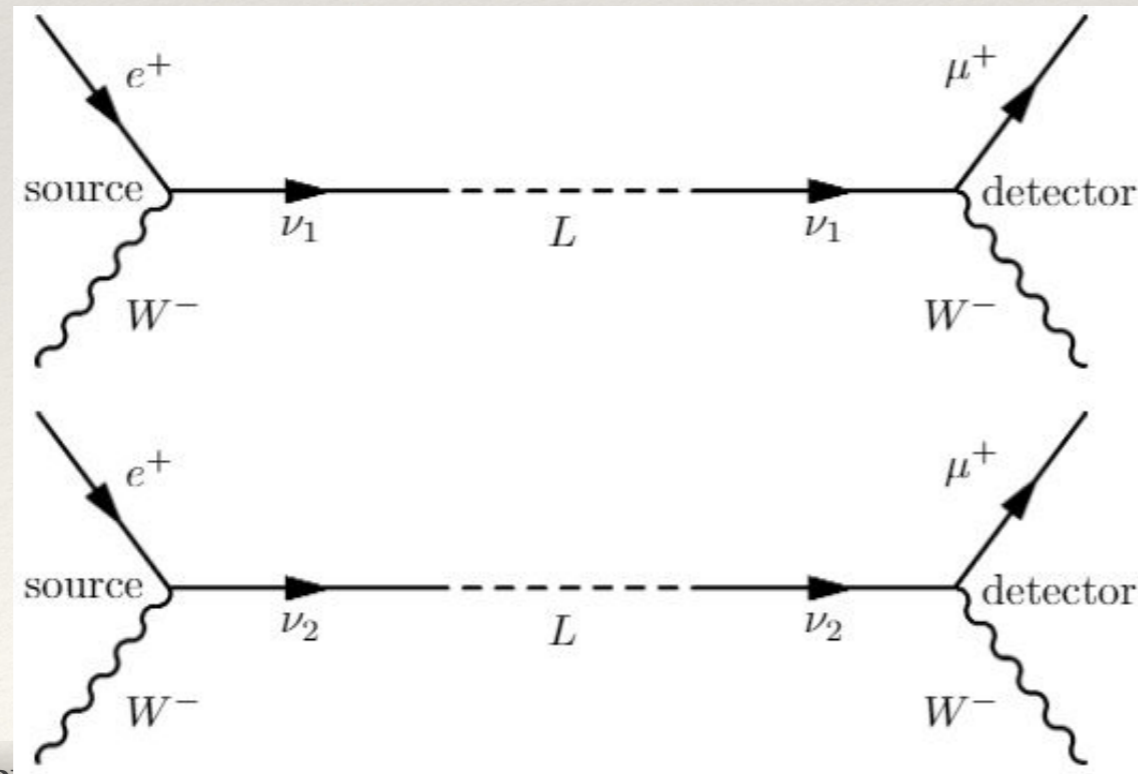
Neutrinos do have mass!

$$\begin{pmatrix} \nu_\alpha \\ \nu_\beta \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

flavor states,
produced in weak
interaction

Mixing matrix
PMNS

mass states,
propagating



A_1

$$A_{\text{tot}} = A_1 + A_2$$

and

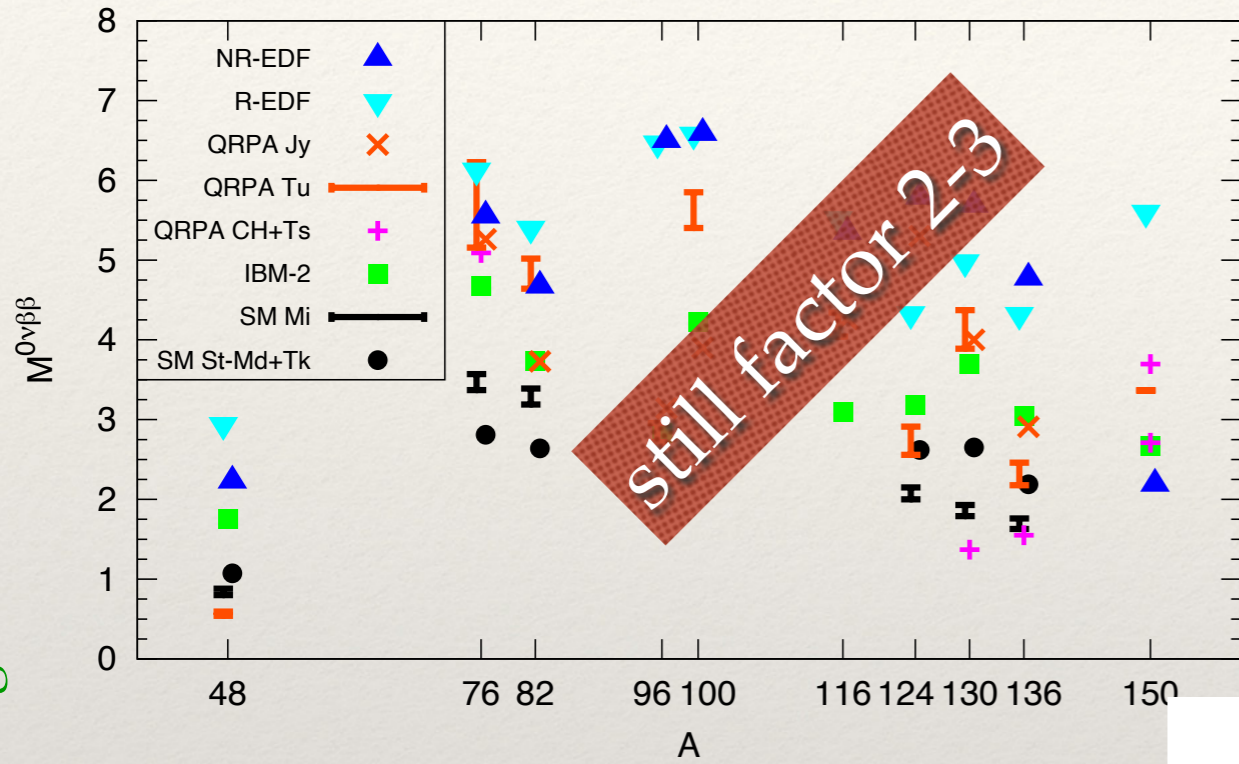
A_2

$$P = |A_1 + A_2|^2$$

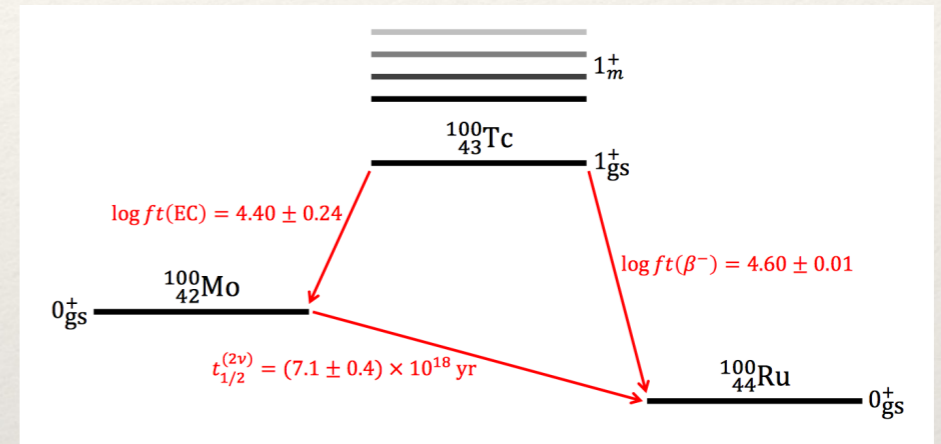
Experiment	Isotope	Technique	Total mass [kg]	Exposure [kg yr]	FWHM @ $Q_{\beta\beta}$ [keV]	Background [counts/keV/kg/yr]	$S^{0\nu}$ (90% c.l.) [10^{25} yr]
<i>Past</i>			<i>Dell’Oro et al., 1601.07512</i>				
Cuoricino, [179]	^{130}Te	bolometers	40.7 (TeO_2)	19.75	5.8 ± 2.1	0.153 ± 0.006	0.24
CUORE-0, [180]	^{130}Te	bolometers	39 (TeO_2)	9.8	5.1 ± 0.3	0.058 ± 0.006	0.29
Heidelberg-Moscow, [181]	^{76}Ge	Ge diodes	11 ($^{\text{enr}}\text{Ge}$)	35.5	4.23 ± 0.14	0.06 ± 0.01	1.9
IGEX, [182, 183]	^{76}Ge	Ge diodes	8.1 ($^{\text{enr}}\text{Ge}$)	8.9	~ 4	$\lesssim 0.06$	1.57
GERDA-I, [167, 184]	^{76}Ge	Ge diodes	17.7 ($^{\text{enr}}\text{Ge}$)	21.64	3.2 ± 0.2	~ 0.01	2.1
NEMO-3, [185]	^{100}Mo	tracker + calorimeter	6.9 (^{100}Mo)	34.7	350	0.013	0.11
<i>Present</i>							
EXO-200, [186]	^{136}Xe	LXe TPC	175 ($^{\text{enr}}\text{Xe}$)	100	89 ± 3	$(1.7 \pm 0.2) \cdot 10^{-3}$	1.1
KamLAND-Zen, [187, 188]	^{136}Xe	loaded liquid scintillator	348 ($^{\text{enr}}\text{Xe}$)	89.5	244 ± 11	~ 0.01	1.9
<i>Future</i>							
CUORE, [189]	^{130}Te	bolometers	741 (TeO_2)	1030	5	0.01	9.5
GERDA-II, [174]	^{76}Ge	Ge diodes	37.8 ($^{\text{enr}}\text{Ge}$)	100	3	0.001	15
LUCIFER, [190]	^{82}Se	bolometers	17 (Zn^{82}Se)	18	10	0.001	1.8
MAJORANA D., [191]	^{76}Ge	Ge diodes	44.8 ($^{\text{enr/nat}}\text{Ge}$)	100 ^a	4	0.003	12
NEXT, [192, 193]	^{136}Xe	Xe TPC	100 ($^{\text{enr}}\text{Xe}$)	300	12.3 – 17.2	$5 \cdot 10^{-4}$	5
AMoRE, [194]	^{100}Mo	bolometers	200 ($\text{Ca}^{\text{enr}}\text{MoO}_4$)	295	9	$1 \cdot 10^{-4}$	5
nEXO, [195]	^{136}Xe	LXe TPC	4780 ($^{\text{enr}}\text{Xe}$)	12150 ^b	58	$1.7 \cdot 10^{-5}$ ^b	66
PandaX-III, [196]	^{136}Xe	Xe TPC	1000 ($^{\text{enr}}\text{Xe}$)	3000 ^c	12 – 76	0.001	11 ^c
SNO+, [197]	^{130}Te	loaded liquid scintillator	2340 ($^{\text{nat}}\text{Te}$)	3980	270	$2 \cdot 10^{-4}$	9
SuperNEMO, [198, 199]	^{82}Se	tracker +	100 (^{82}Se)	500	120	0.01	10

Nuclear Matrix Elements

Engel, Menendez, 1610.06548

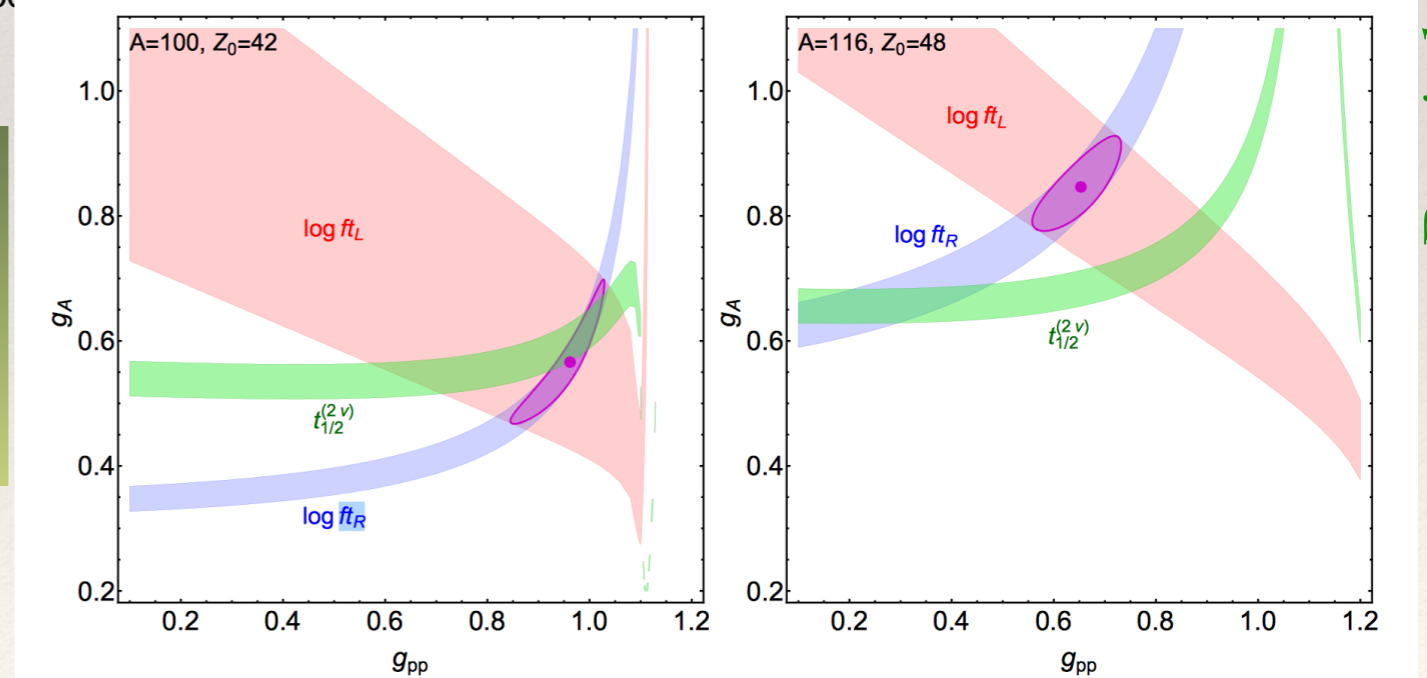


How good are the models?
Example isobaric triplets
within QRPA



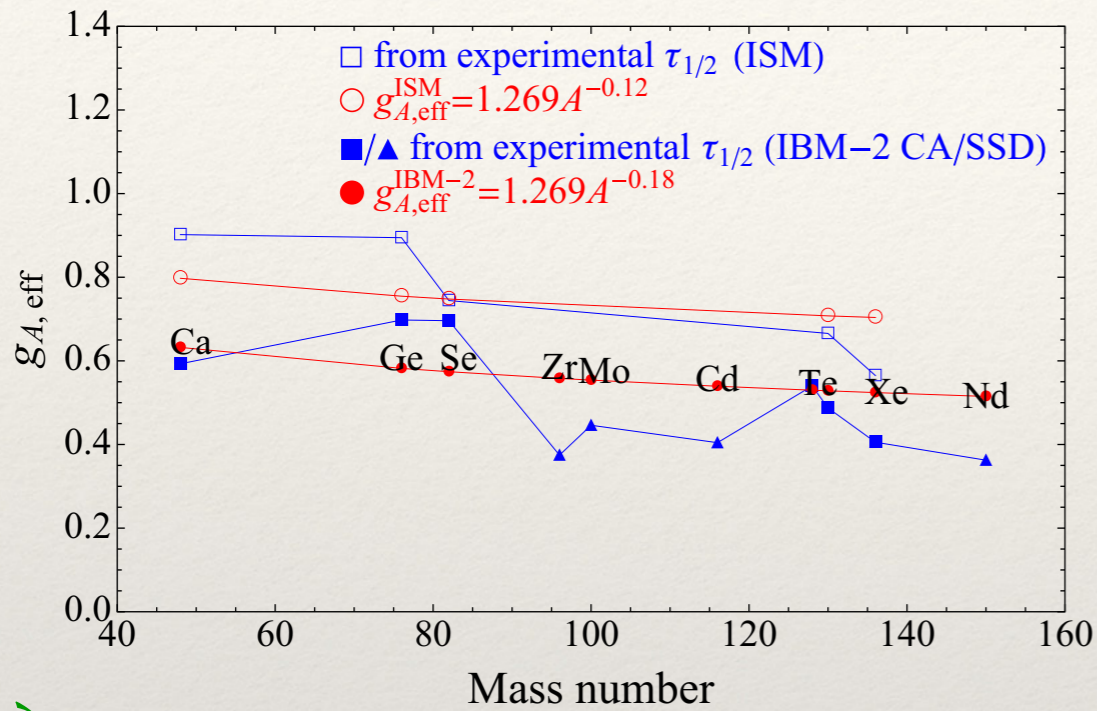
Deppisch, Suhonen, 1606.02908

⇒ Need as much experimental input (e.g. charge exchange) as possible...



Nuclear Matrix Elements

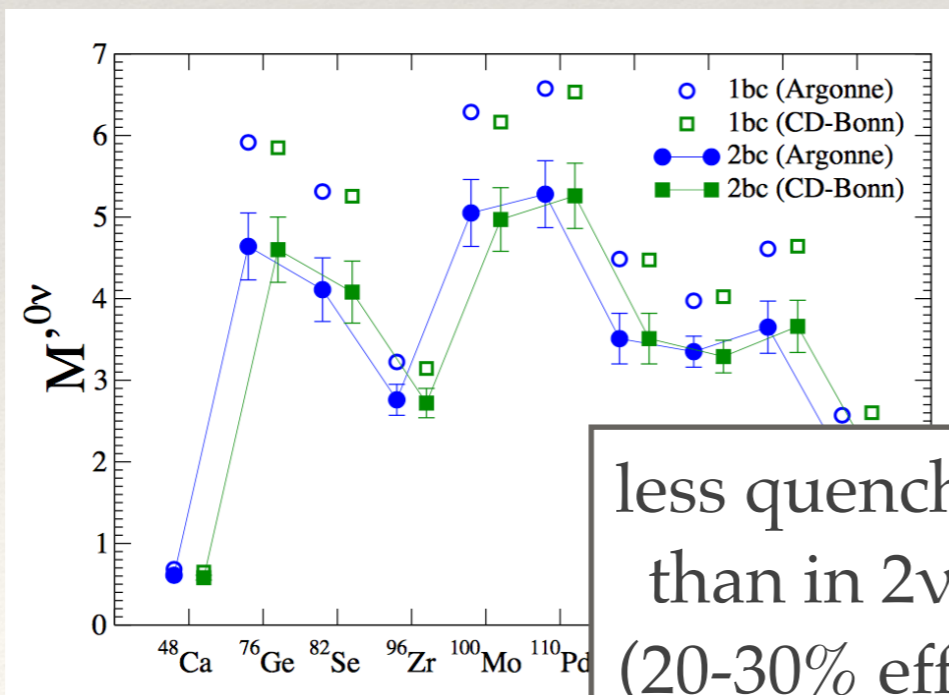
Iachello et al., 1506.08530



QUENCHING??

$$T_{\frac{1}{2}}^{0\nu} \propto g_A^{-4}$$

- ❖ fact in β and $2\nu\beta\beta$
- ❖ truncation of model-space?
- ❖ also in $0\nu\beta\beta$??
 - $q = 10^2$ vs. 10^0 MeV?
 - higher multipolarities?
 - two-body currents?
 - muon capture?
 - SM vs. QRPA

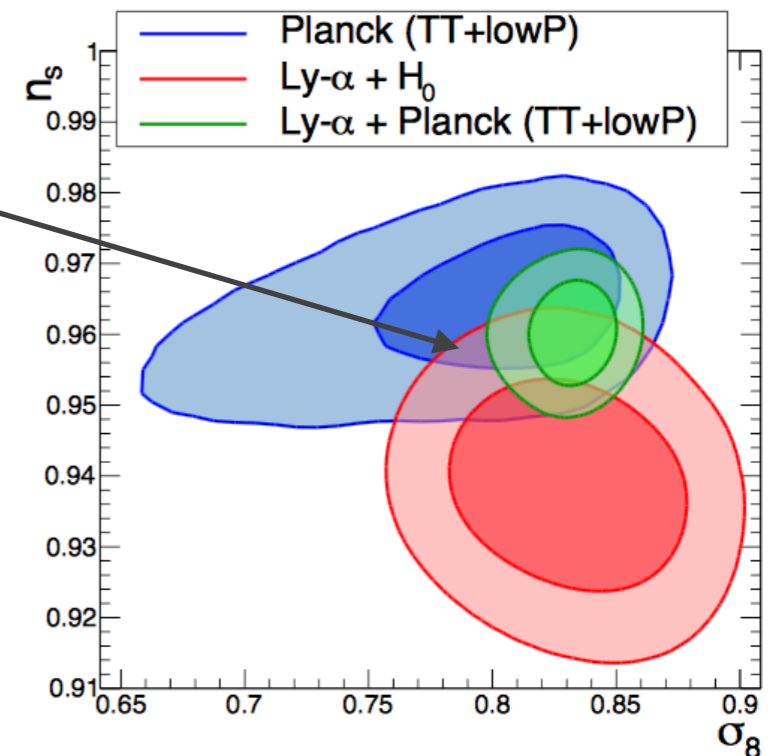
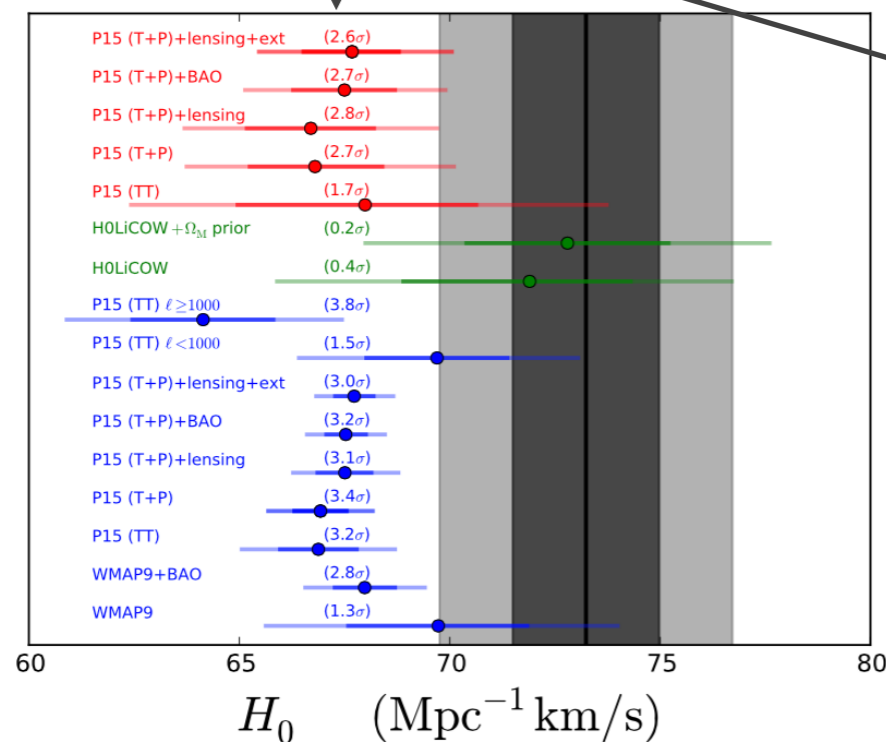
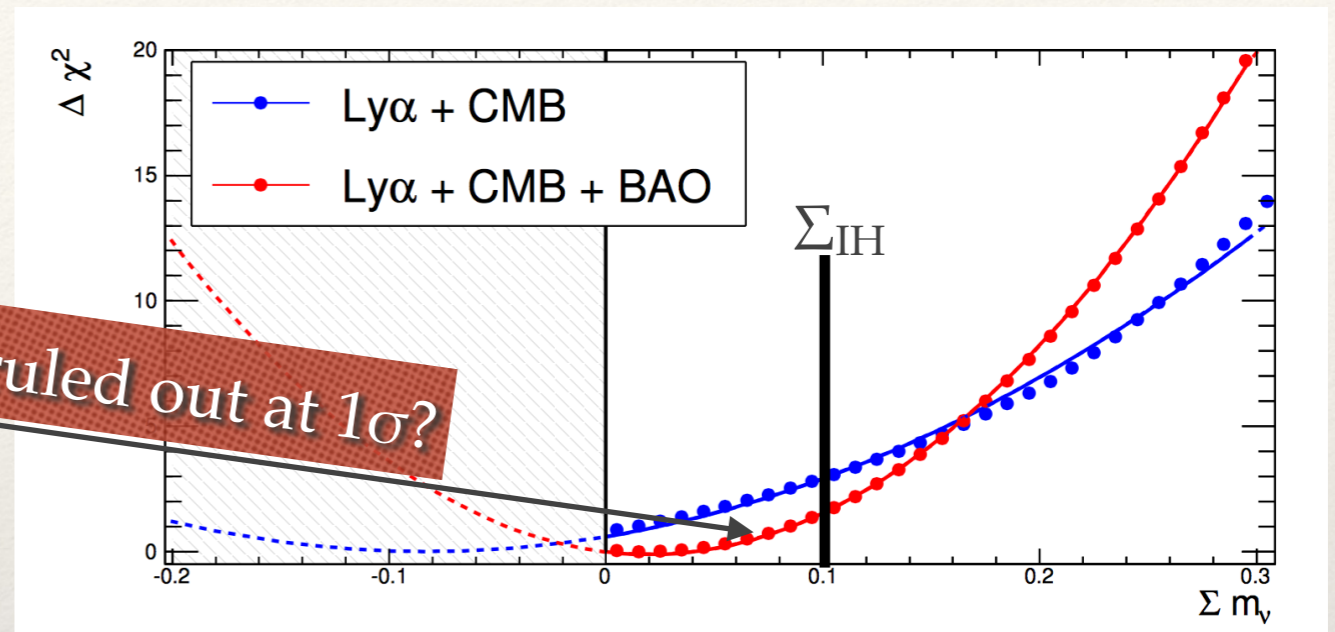


less quenching
than in $2\nu\beta\beta$
(20-30% effect)

*Menendez, Gazit, Schwenk,
1103.3622; Engel, Simkovic,
Vogel, 1403.7860*

Cosmological Mass Limits

- ❖ adding more and more data sets: breaks degeneracies and improves limits
- ❖ BUT: can introduce systematics?



Palanque-Delabrouille et al., 1410.7244 + 1506.05976

Bernal, Verde, Riess, 1607.05617

Neutrinoless Double Beta Decay

$$(T_{1/2}^{0\nu}) \propto \begin{cases} a M \varepsilon t & \text{background free,} \\ a \varepsilon \sqrt{\frac{M t}{B \Delta E}} & \text{with background,} \end{cases}$$

Dolinski, Poon, WR, 1902.04097

