

Light dark states: phenomenology and detection

Josef Pradler

ÖAW

AUSTRIAN
ACADEMY OF
SCIENCES



Max-Planck-Institut für Kernphysik

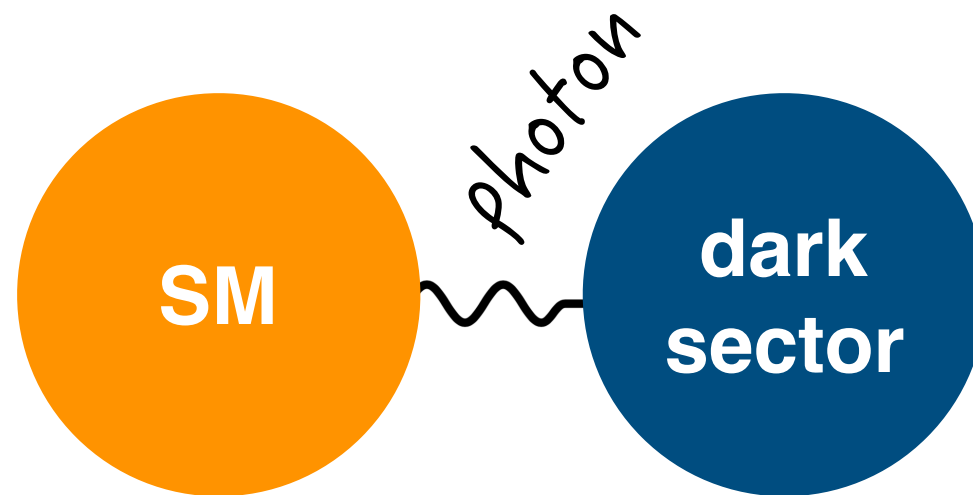
Jan 20 2020

1

Phenomenology

Light dark states through the *photon portal*

Consider a sub-GeV dark sector that talks to SM through direct effective couplings to the photon



Based on

[Chu, JP, Semmelrock, PRD 2019, arXiv:1811.04095](#)

[Chu, Kuo, JP, Semmelrock, PRD 2019, arXiv:1908.00553](#)

[Chu, Kuo, JP, arXiv:2001.06042 \(today\)](#)

The photon as new physics mediator

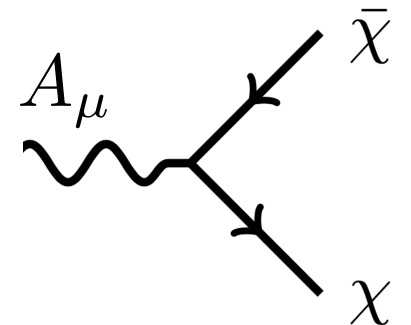
Tinkering with the photon may potentially affect many known phenomena

- change the strength of the EM interaction at various energy scales
- other SM precision observables may be affected, e.g. $g-2$
- new photon-mediated decay channels in flavor physics may open
- cosmological viability of dark states coupled with the photon
- can we make dark matter through the photon coupling?
- astrophysical implications - stellar cooling

Dark States with EM-interactions

Immediate possibility is (milli)charge of dark states

Electromagnetic neutral particles χ can still interact with the photon through higher-dimensional operators



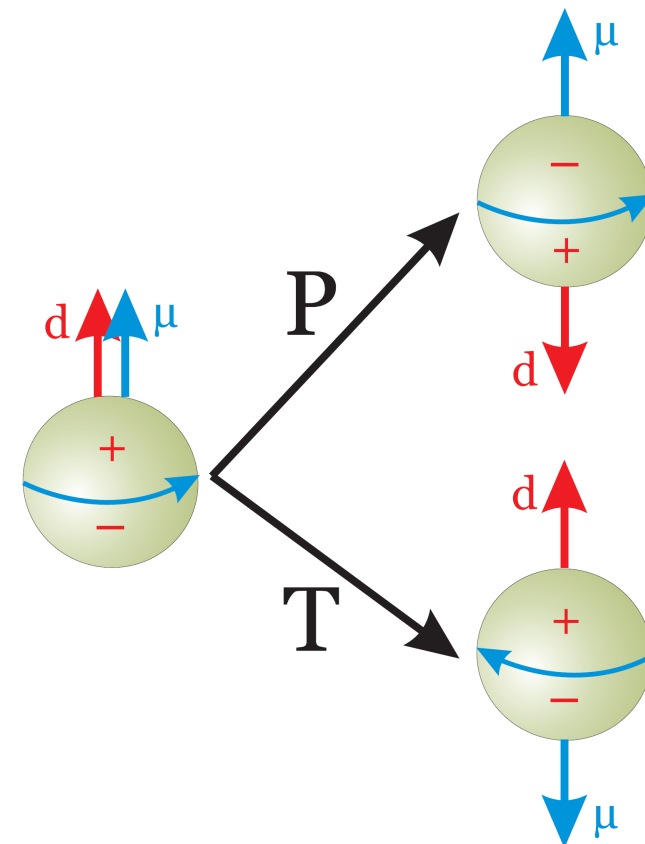
For a Dirac particle, best known are magnetic and electric dipole moments

$$H_{\text{MDM}} = -\mu_\chi (\vec{B} \cdot \vec{\sigma}_\chi)$$

P and T even

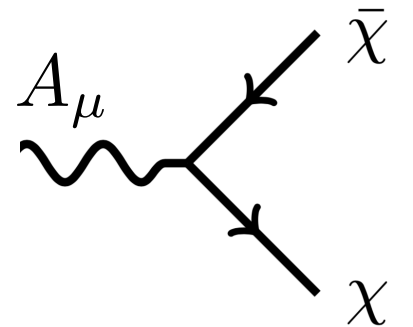
$$H_{\text{EDM}} = -d_\chi (\vec{E} \cdot \vec{\sigma}_\chi)$$

P and T odd $\Rightarrow$ CP violating



Dark States with EM-interactions

Electromagnetic neutral particles χ can interact with the photon through higher-dimensional operators



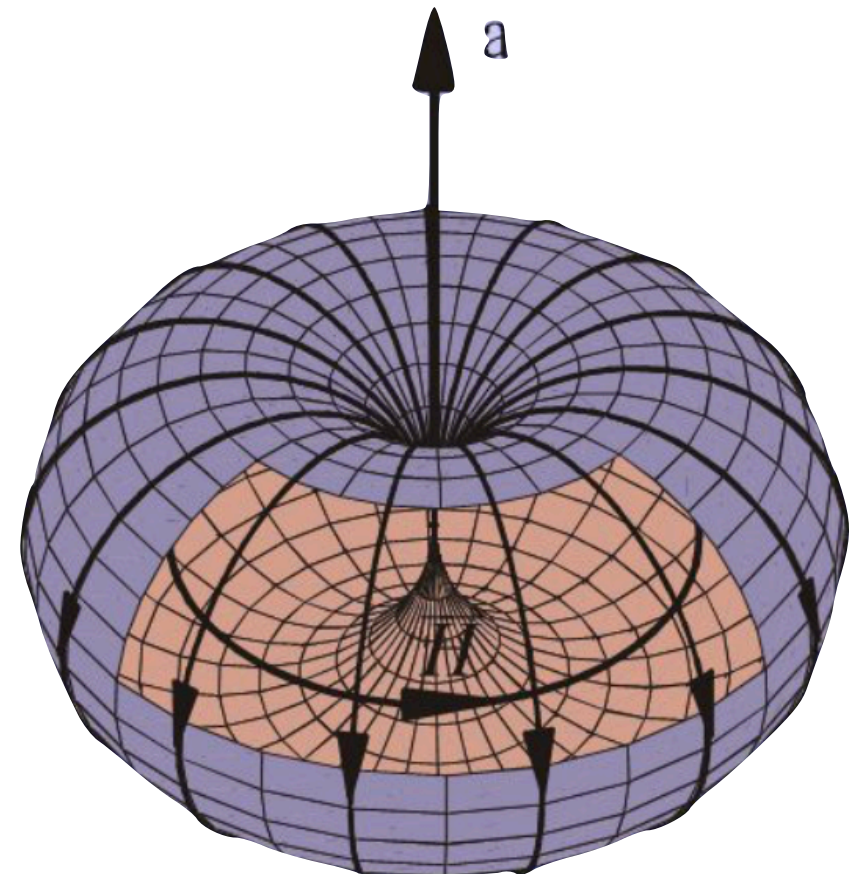
Charge radius interaction and anapole moments

$$H_{\text{AM}} = -a_\chi (\vec{J} \cdot \vec{\sigma}_\chi) \quad \text{Zel'dovich 1958}$$

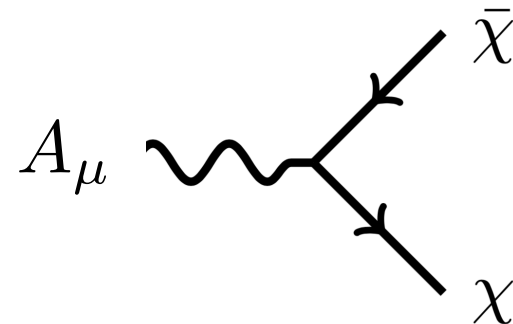
P odd but CP even

$$H_{\text{CR}} = -b_\chi (\vec{\nabla} \cdot \vec{E})$$

P and T even



Dark States with EM-interactions



Effective operators

millicharge (ϵQ):

$$\epsilon e \bar{\chi} \gamma^\mu \chi A_\mu, \quad \text{dim 4}$$

magnetic dipole (MDM):

$$\frac{1}{2} \mu_\chi \bar{\chi} \sigma^{\mu\nu} \chi F_{\mu\nu}, \quad \dots\dots\dots$$

electric dipole (EDM):

$$\frac{i}{2} d_\chi \bar{\chi} \sigma^{\mu\nu} \gamma^5 \chi F_{\mu\nu}, \quad \text{dim5}$$

anapole moment (AM):

$$a_\chi \bar{\chi} \gamma^\mu \gamma^5 \chi \partial^\nu F_{\mu\nu}, \quad \dots\dots\dots$$

charge radius (CR):

$$b_\chi \bar{\chi} \gamma^\mu \chi \partial^\nu F_{\mu\nu}. \quad \text{dim6}$$

NB: Millicharged states have been studied previously

[Prinz et 1998](#); recent refs [Magill et al 2018](#); [Berlin et al 2018](#),

Dark States with EM-interactions

Interactions are assembled into matrix element of the EM current

$$\langle \chi(p_f) | J_\chi^\mu(0) | \chi(p_i) \rangle = \bar{u}(p_f) \Gamma^\mu(q) u(p_i)$$

$$\Gamma^\mu(q) = i\sigma^{\mu\nu} q_\nu [M(q^2) + iD(q^2)\gamma^5] + (q^2\gamma^\mu - q^\mu \not{q}) [V(q^2) - A(q^2)\gamma^5]$$

$\begin{array}{ccccccc} & \uparrow & & \uparrow & & \uparrow & \uparrow \\ & \text{magnetic} & \text{electric} & & \text{charge-radius} & \text{anapole moment} \\ & \text{dipole} & & & & \end{array}$

Assuming that the interactions are generated at a UV scale well above the typical CM energies of the high-intensity beams,

$$\mu_\chi = M(0), \quad d_\chi = D(0), \quad a_\chi = A(0), \quad b_\chi = V(0)$$

Dark States with EM-interactions

Rayleigh/Susceptibility ops

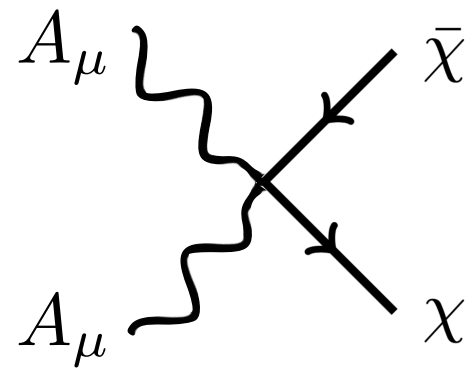
$\bar{\chi}\chi$

$F_{\mu\nu}F^{\mu\nu}$

$\otimes$

$\bar{\chi}\gamma^5\chi$

$F_{\mu\nu}\tilde{F}^{\mu\nu}$



.....

dim 7

.....

=> different (or loop-suppressed) phenomenology

Complex scalars: dim-6 Rayleigh and charge radius interaction

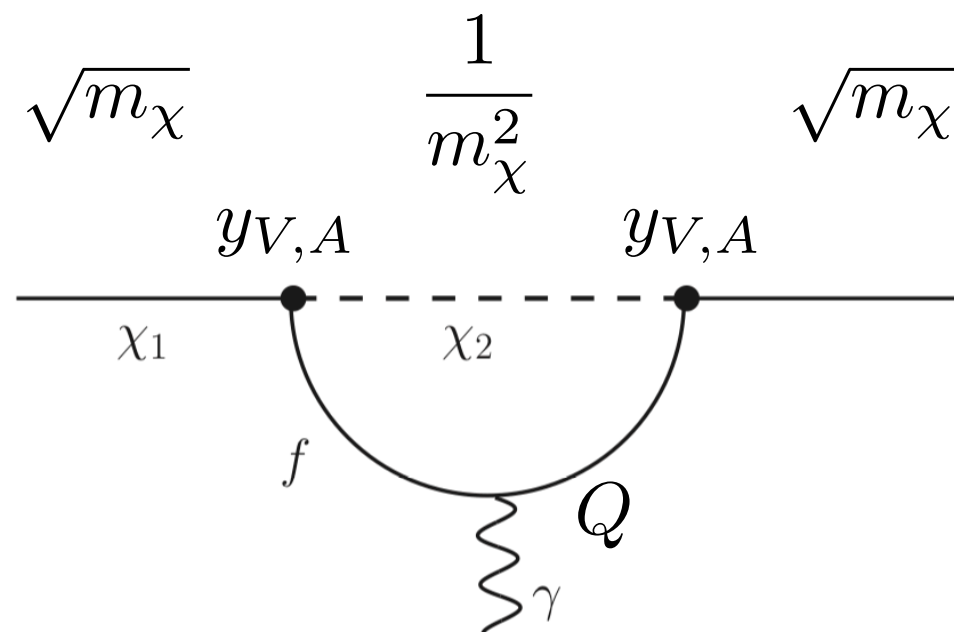
Vectors: also quadrupole moments exist

Origin of form factor interactions

a) compositeness

e.g. Bagnasco, Dine, Thomas 1994; Foadi, Frandsen, Sannino 2009;
Antipin, Redi, Strumia, and Vigiani 2015

b) radiatively (possibly enhanced by mass degeneracies)



$$\mu_\chi \sim \frac{Q|y_{A,V}|^2}{m_\chi} \quad d_\chi \sim \frac{Q \operatorname{Im}[y_V y_A^*]}{m_\chi}$$

$$a_\chi, b_\chi \sim \frac{Q|y_{A,V}|^2}{M^2}$$

or

$$a_\chi, b_\chi \sim \frac{Q|y_{A,V}|^2}{m_\chi} \times \frac{1}{\Delta m}$$

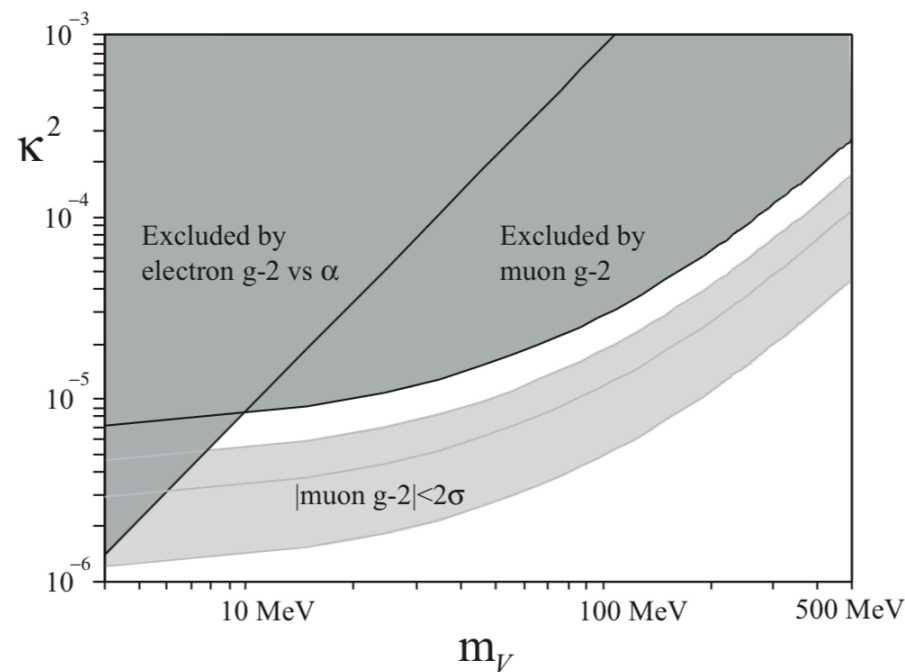
see also Kavanagh, Panci, Ziegler 2018

Muon g-2

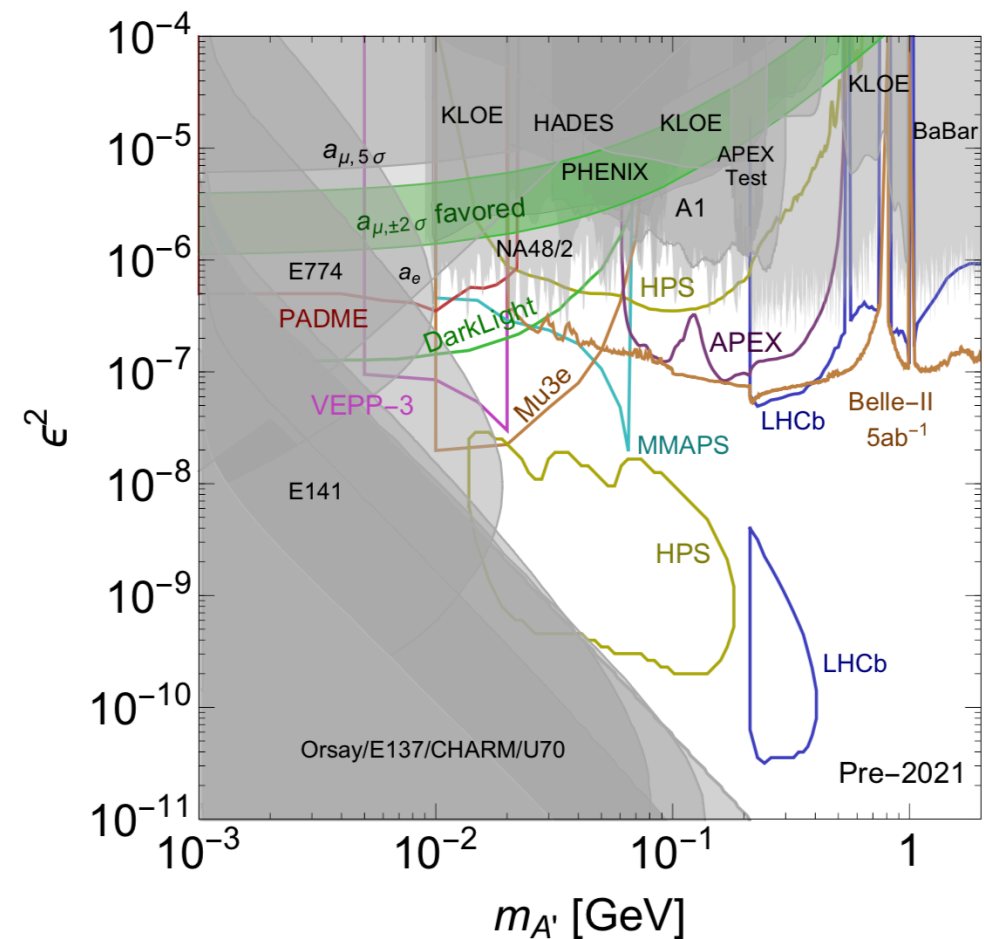
- Muon g-2 puzzle: (3-4) σ tension between SM prediction and measurement

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (290 \pm 90) \times 10^{-11}$$

- Prospective solutions became a driver for intensity frontier efforts, think: dark photon.



$\Rightarrow$



Muon g-2

- Muon g-2 puzzle: (3-4) σ tension between SM prediction and measurement

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (290 \pm 90) \times 10^{-11}$$

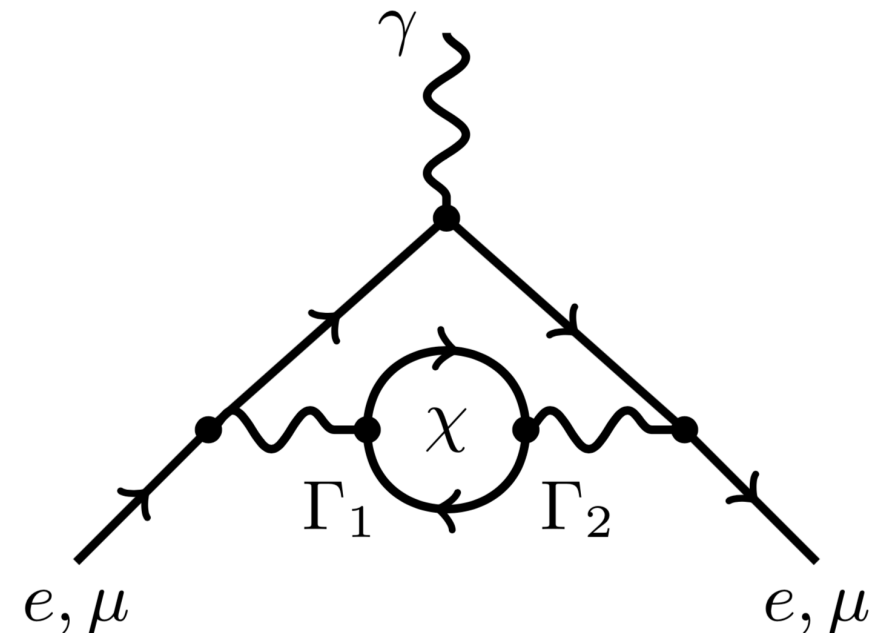
- For form-factor interactions, contributions enter through the vacuum polarization

e.g. use dispersion relation + unitarity

$$\Delta a_\mu = \frac{1}{4\pi^3} \int_{4m_\chi^2} ds \sigma_{e^+e^- \rightarrow \chi\bar{\chi}}(s) K(s)$$

solution to g-2 for

$$|\mu_\chi|, |d_\chi| \sim \text{few} \times 10^{-3} \mu_B$$



Precision tests

- In EW theory, G_F , m_W and m_Z are related and receive calculable quantum corrections, summarized in the Δr parameter

$$\Delta r_{\text{obs}} = 1 - \frac{A_0^2}{M_W^2 s_w^2} = 0.03492 \pm 0.00097$$

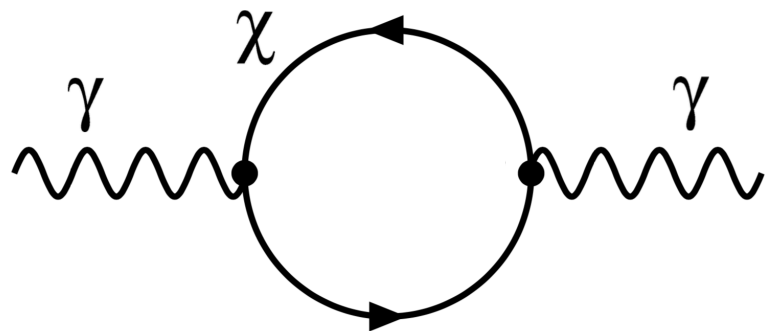
$$A_0 = (\pi\alpha/\sqrt{2}G_F)^{1/2}$$

$$s_w^2 = 1 - M_W^2/M_Z^2$$

$$-0.0038 < \Delta r_{\text{new}} < 0.00018$$

(tighter upper limit from 1.8 tension)

Running of α contributes $\Delta r_{\text{new}} \simeq \Pi(-M_Z^2) - \Pi(0)$



$$|\mu_\chi| \text{ or } |d_\chi| < 3.2 \times 10^{-6} \mu_B$$

(saturating upper limit)

$$|a_\chi| \text{ or } |b_\chi| < 3.2 \times 10^{-5} / \text{GeV}^2$$

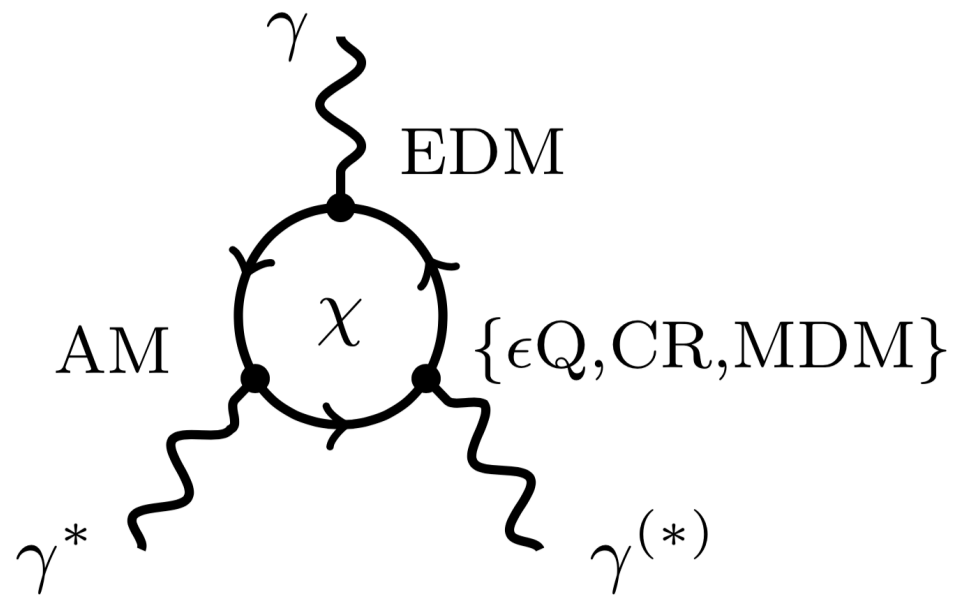
(saturating lower limit)

SM electric dipole moments?

- Recently, ACME collaboration improved bound on electron EDM

$$|d_e| < 1.1 \times 10^{-29} \text{ e cm} = 6 \times 10^{-19} \mu_B$$

- Dark states may induce an EDM operator via insertion of dark d_χ



2 loop?

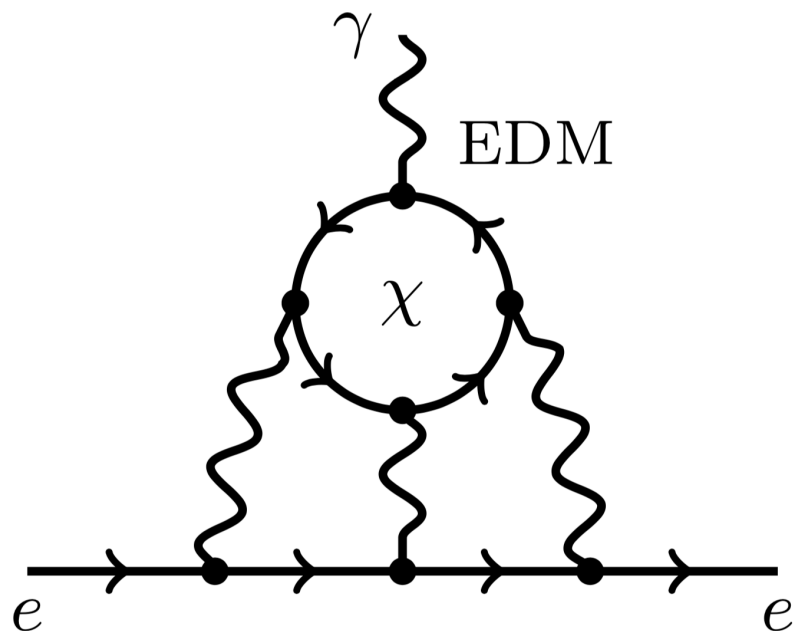
NB: the left loop does not vanish, AM is C-odd operator, so Furry theorem does not hold (in the usual way)

SM electric dipole moments?

- Recently, ACME collaboration improved bound on electron EDM

$$|d_e| < 1.1 \times 10^{-29} \text{ e cm} = 6 \times 10^{-19} \mu_B$$

- Dark states may induce an EDM operator via insertion of dark d_χ



3 loop it is

$$d_e \sim e^3 m_e d_\chi \times (\text{mass})^{-1}$$

$$(\text{mass})^{-1} \sim \epsilon^3 e^3 / m_\chi, \mu_\chi^3 m_\chi^2, \\ d_\chi^2 \mu_\chi m_\chi^2, b_\chi d_\chi^2 m_\chi^3 \dots$$

e.g. dim-5 operators only:

$$(10^{-5} - 10^{-6}) \mu_B \sqrt{\text{GeV} / m_\chi}$$

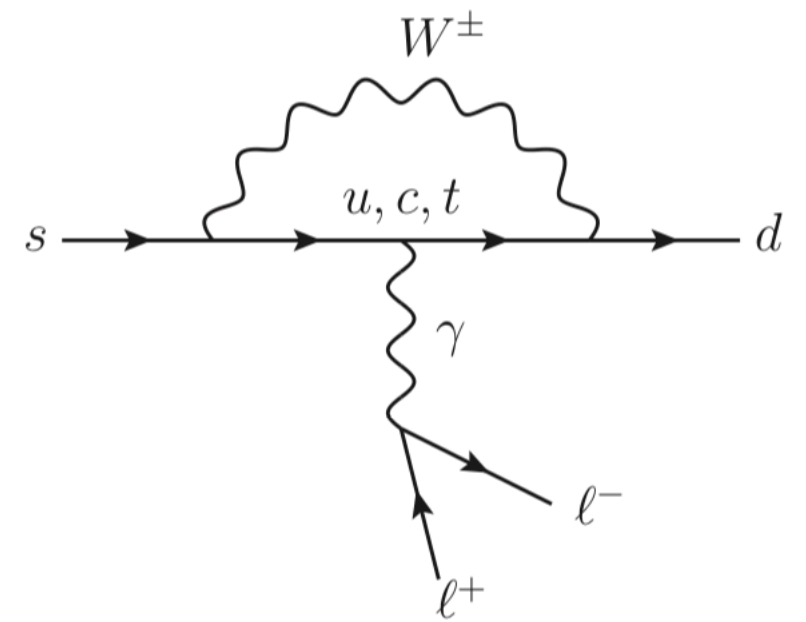
Rare Meson Decays

- χ pair-production through γ^* in flavor changing $s \rightarrow d$ and $b \rightarrow s$ transition closely related to $K^+ \rightarrow \pi^+ l^+ l^-$ and $B^+ \rightarrow K^+ l^+ l^-$

e.g. for Kaons

$$\frac{\Gamma(K^+ \rightarrow \pi^+ \bar{\chi} \chi)}{\Gamma(K \rightarrow \pi e^+ e^-)} \simeq 1.9 \times 10^4 \left(\frac{\mu_\chi \text{ or } d_\chi}{\mu_B} \right)^2$$

$$\frac{\Gamma(K^+ \rightarrow \pi^+ \bar{\chi} \chi)}{\Gamma(K \rightarrow \pi e^+ e^-)} \simeq 2.6 \times 10^4 \left(\frac{a_\chi \text{ or } b_\chi}{\text{TeV}^2} \right)^2$$



constrained from $\text{Br}(K^+ \rightarrow \pi^+ + \text{inv}) \lesssim 4 \times 10^{-10}$ [E949; see also NA62](#)

$$|\mu_\chi| \text{ or } |d_\chi| \lesssim 3 \times 10^{-4} \mu_B$$

$$|a_\chi| \text{ or } |b_\chi| \lesssim 0.2 \text{ GeV}^{-2}$$

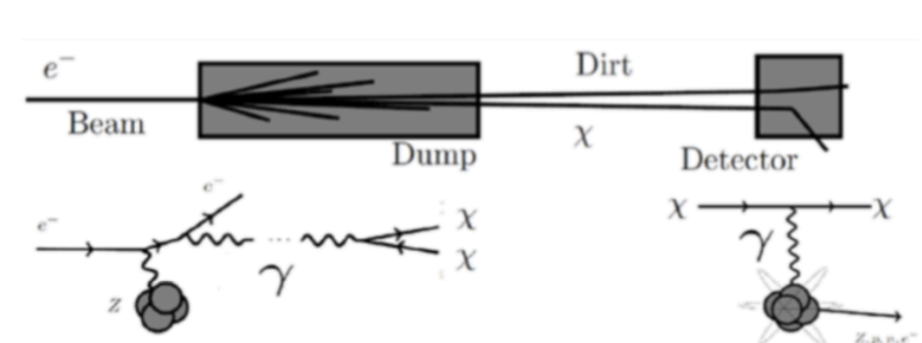
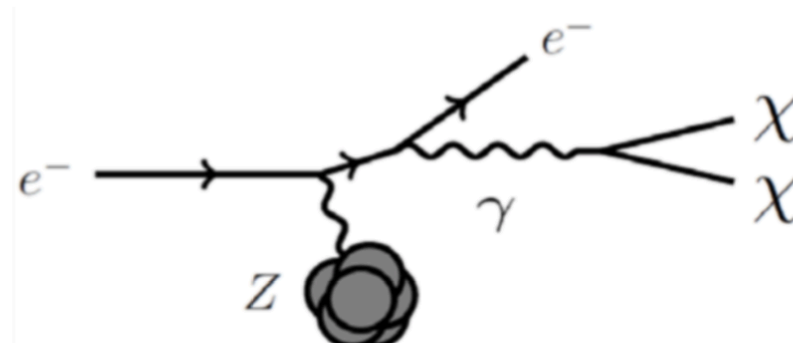
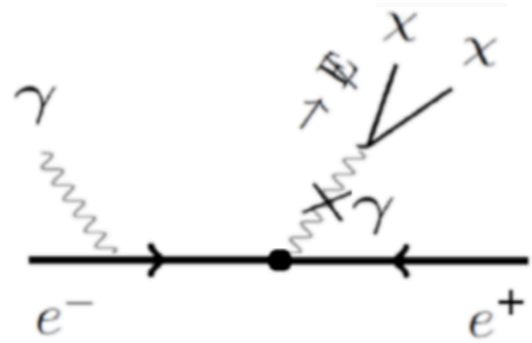
likewise for $\text{Br}(B^+ \rightarrow K^+ + \text{inv}) \lesssim 7 \times 10^{-5}$ [BaBar 2003](#)

A new target for the intensity frontier

missing momentum

missing energy

direct search



BaBar:

- CM energy: 10 GeV
- Luminosity: 28/19 fb⁻¹

Belle II (projected):

- Luminosity: 50 ab⁻¹

Main Backgrounds:

- $e^+e^- \rightarrow \gamma\gamma$
- $e^+e^- \rightarrow \gamma\gamma\gamma$
- $e^+e^- \rightarrow \gamma e^+e^-$

NA64:

- Beam energy: 100 GeV
- Lead Target
- EOT: 10¹⁰

LDMX (projected):

- Beam energy: 4/8 GeV
- Tungsten/Aluminum Target
- EOT: 10¹⁴ / 10¹⁵

Almost no Backgrounds:

- Active veto system
- Cuts on search region

mQ:

- Beam energy: 30 GeV
- Tungsten Target
- EOT: 10¹⁹

BDX (projected):

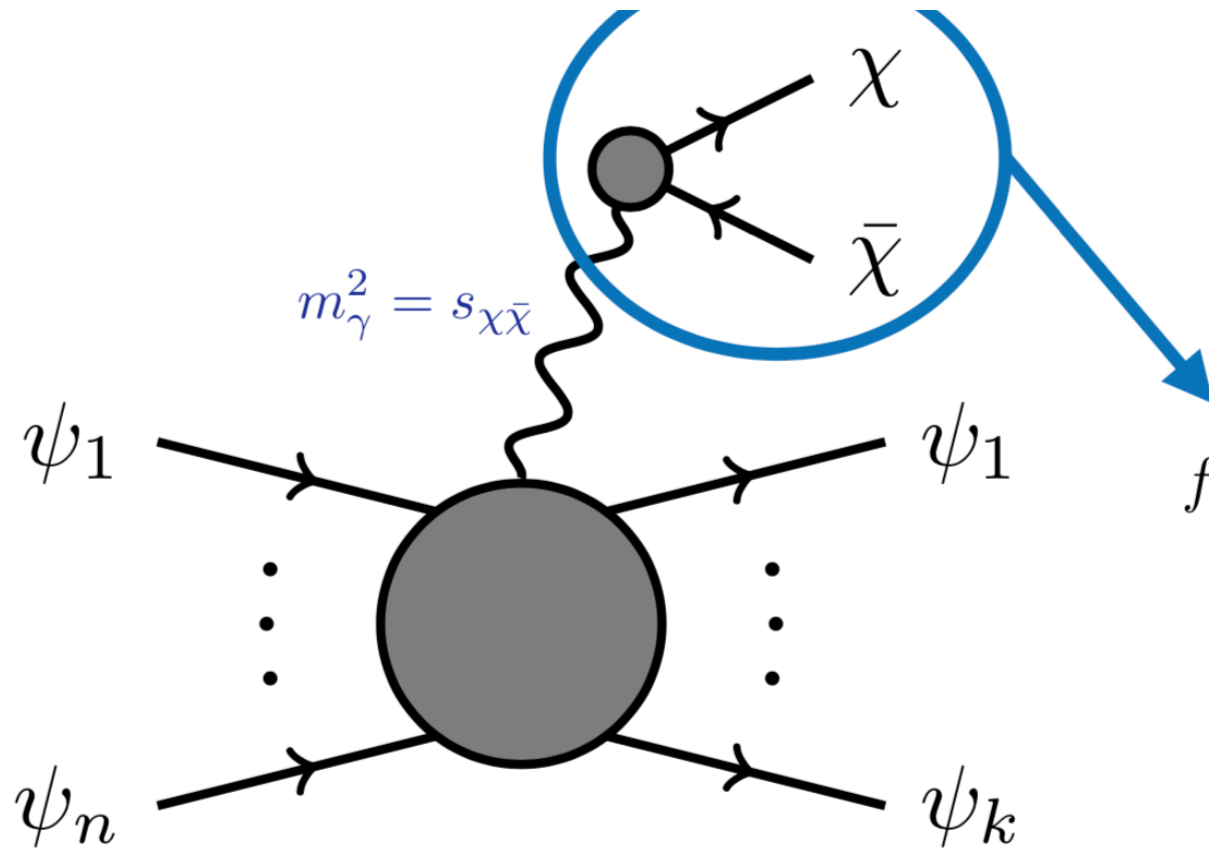
- Beam energy: 11 GeV
- Aluminum Target
- EOT: 10²²

Main Backgrounds:

- High energy neutrinos

Unified description of various interactions

slide credit: Lukas Semmelrock



$$f(s_{\chi\bar{\chi}}) = \begin{cases} \frac{4}{3}\epsilon^2 e^2 s_{\chi\bar{\chi}} \left(1 + \frac{2m_\chi^2}{s_{\chi\bar{\chi}}}\right) \\ \frac{2}{3}\mu_\chi^2 s_{\chi\bar{\chi}}^2 \left(1 + \frac{8m_\chi^2}{s_{\chi\bar{\chi}}}\right) \\ \frac{2}{3}d_\chi^2 s_{\chi\bar{\chi}}^2 \left(1 - \frac{4m_\chi^2}{s_{\chi\bar{\chi}}}\right) \\ \frac{4}{3}a_\chi^2 s_{\chi\bar{\chi}}^3 \left(1 - \frac{4m_\chi^2}{s_{\chi\bar{\chi}}}\right) \\ \frac{4}{3}b_\chi^2 s_{\chi\bar{\chi}}^3 \left(1 + \frac{2m_\chi^2}{s_{\chi\bar{\chi}}}\right) \end{cases}$$

millicharge

magnetic dipole

electric dipole

anapole

charge radius

$$\int \frac{d\Omega_\chi^{R\chi\bar{\chi}}}{4\pi} \text{Tr} \left[(\not{p}_\chi + m_\chi) \Gamma_\mu(q) (\not{p}_{\bar{\chi}} - m_\chi) \bar{\Gamma}_\nu(q) \right] = f(s_{\chi\bar{\chi}}) \left(-g_{\mu\nu} + \frac{q_\mu q_\nu}{s_{\chi\bar{\chi}}} \right)$$

=> for example:

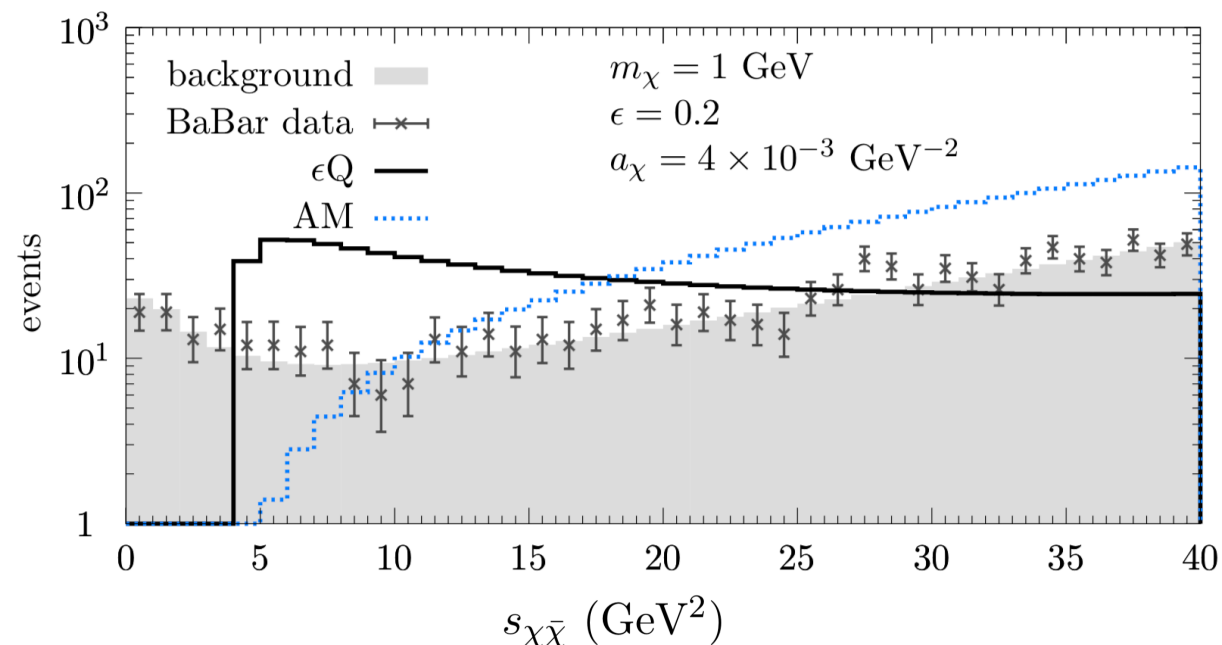
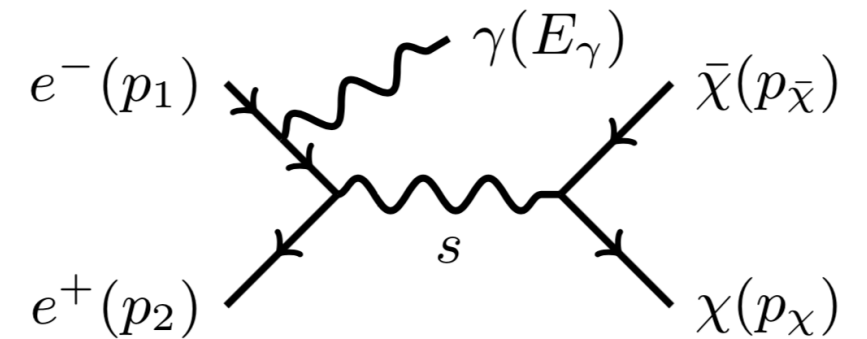
$$\frac{d\sigma_{2\rightarrow 4}}{ds_{\chi\bar{\chi}}} = \sigma_{2\rightarrow 3}(s_{\chi\bar{\chi}}) \frac{f(s_{\chi\bar{\chi}})}{16\pi^2 s_{\chi\bar{\chi}}^2} \sqrt{1 - \frac{4m_\chi^2}{s_{\chi\bar{\chi}}}}$$

Intensity frontier prospects

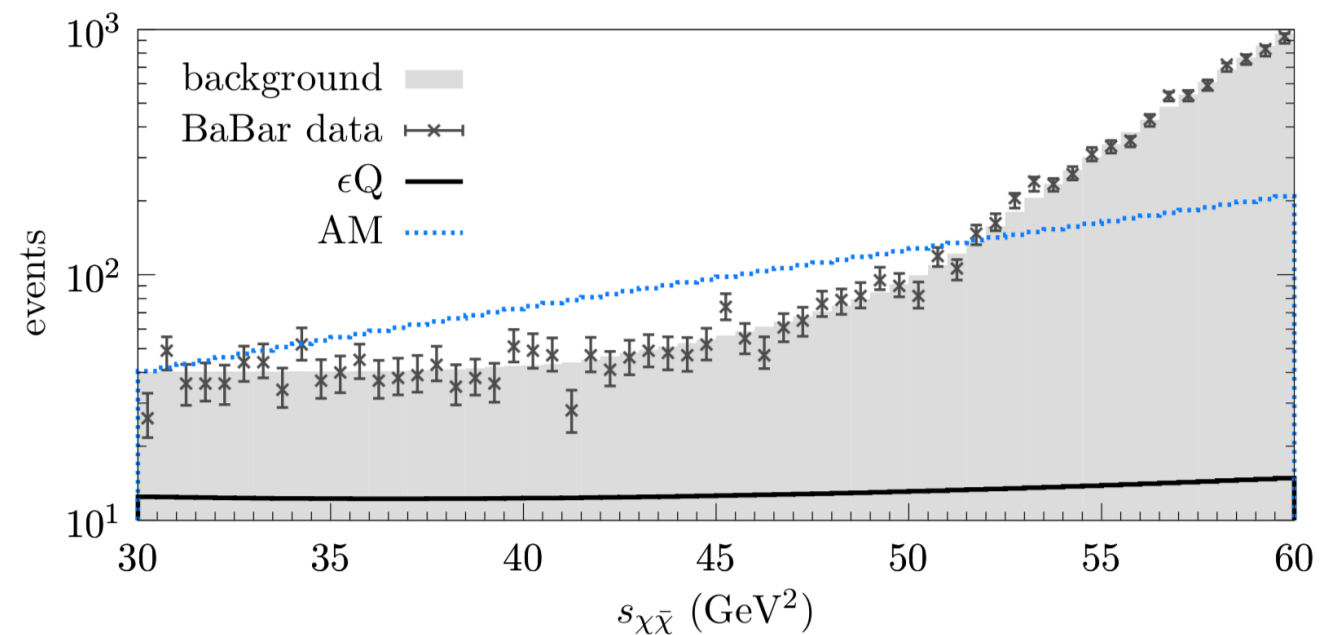
Production in $e^+ e^-$ annihilation, e.g. at BaBar, Belle-II

Mono-photon search $x_\gamma = E_\gamma / \sqrt{s}$

$$\frac{d\sigma_{e^+e^-}}{dx_\gamma d\cos\theta_\gamma} = \sigma_{e^+e^-}(s, s_{\chi\bar{\chi}}) \mathcal{R}^{(\alpha)}(x_\gamma, \theta_\gamma, s)$$



high-energy photon region



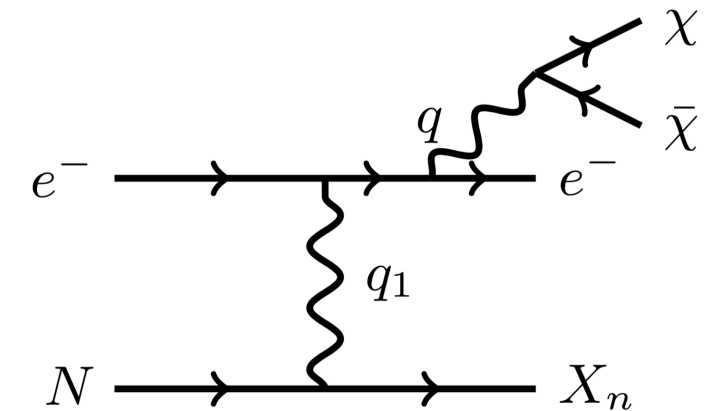
low-energy photon region

Intensity frontier prospects

Production in electron fixed target experiments

- Missing energy (NA64, LDMX)

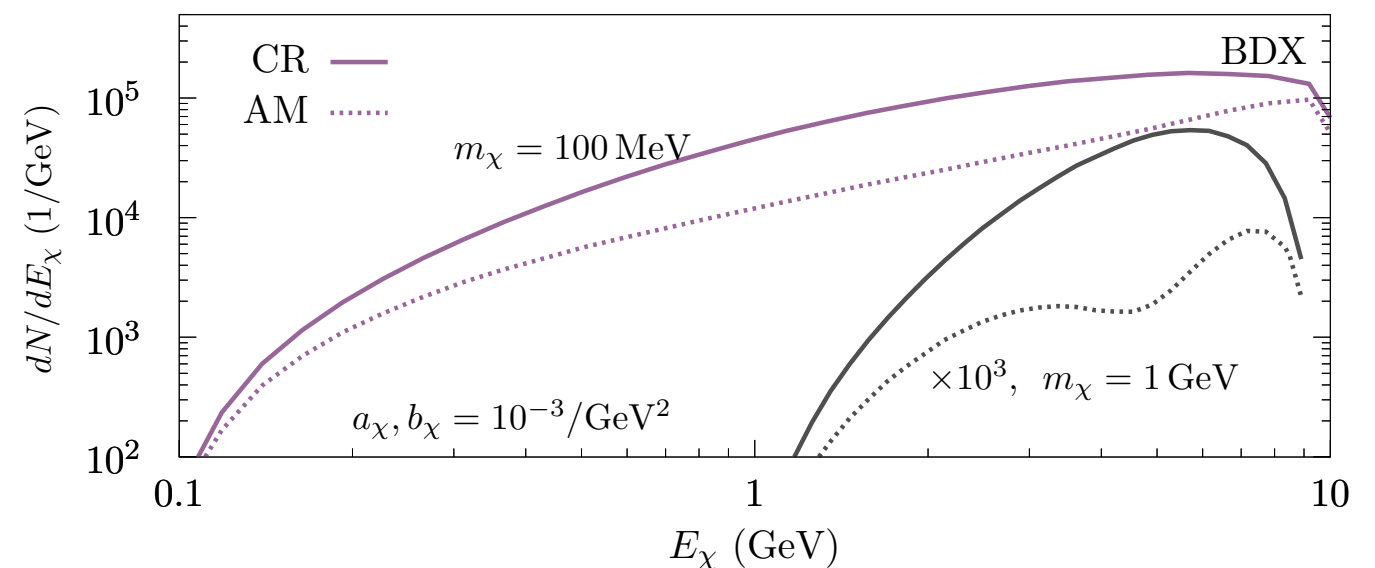
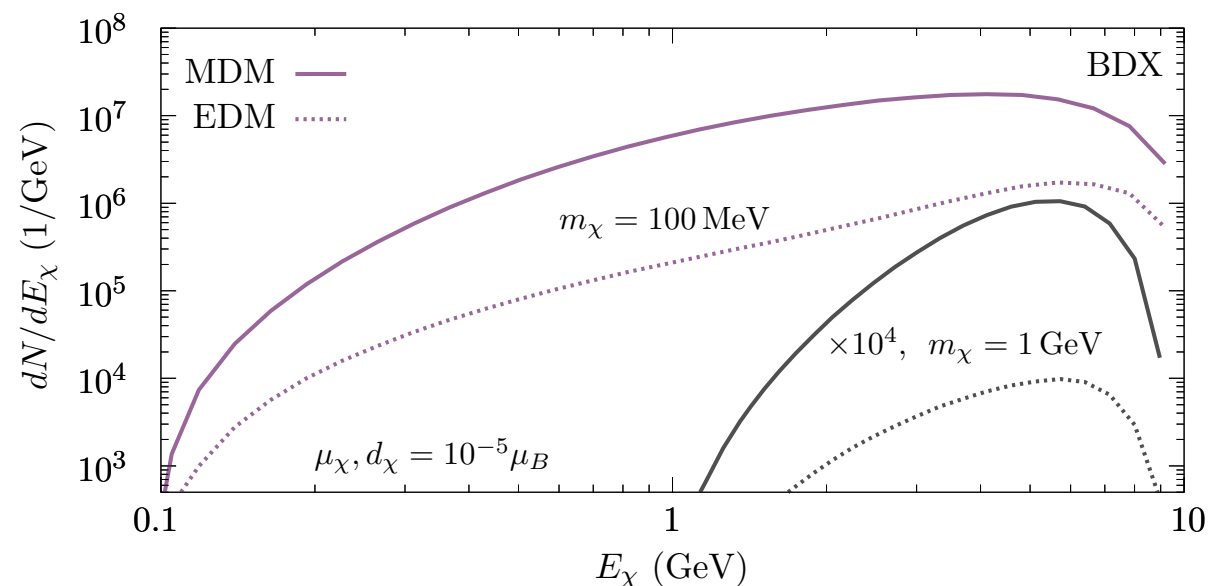
$$\frac{d\sigma_{2\rightarrow 4}}{ds_{\chi\bar{\chi}}} = \sigma_{2\rightarrow 3}(s_{\chi\bar{\chi}}) \frac{f(s_{\chi\bar{\chi}})}{8\pi} \sqrt{1 - \frac{4m_\chi^2}{s_{\chi\bar{\chi}}}}$$



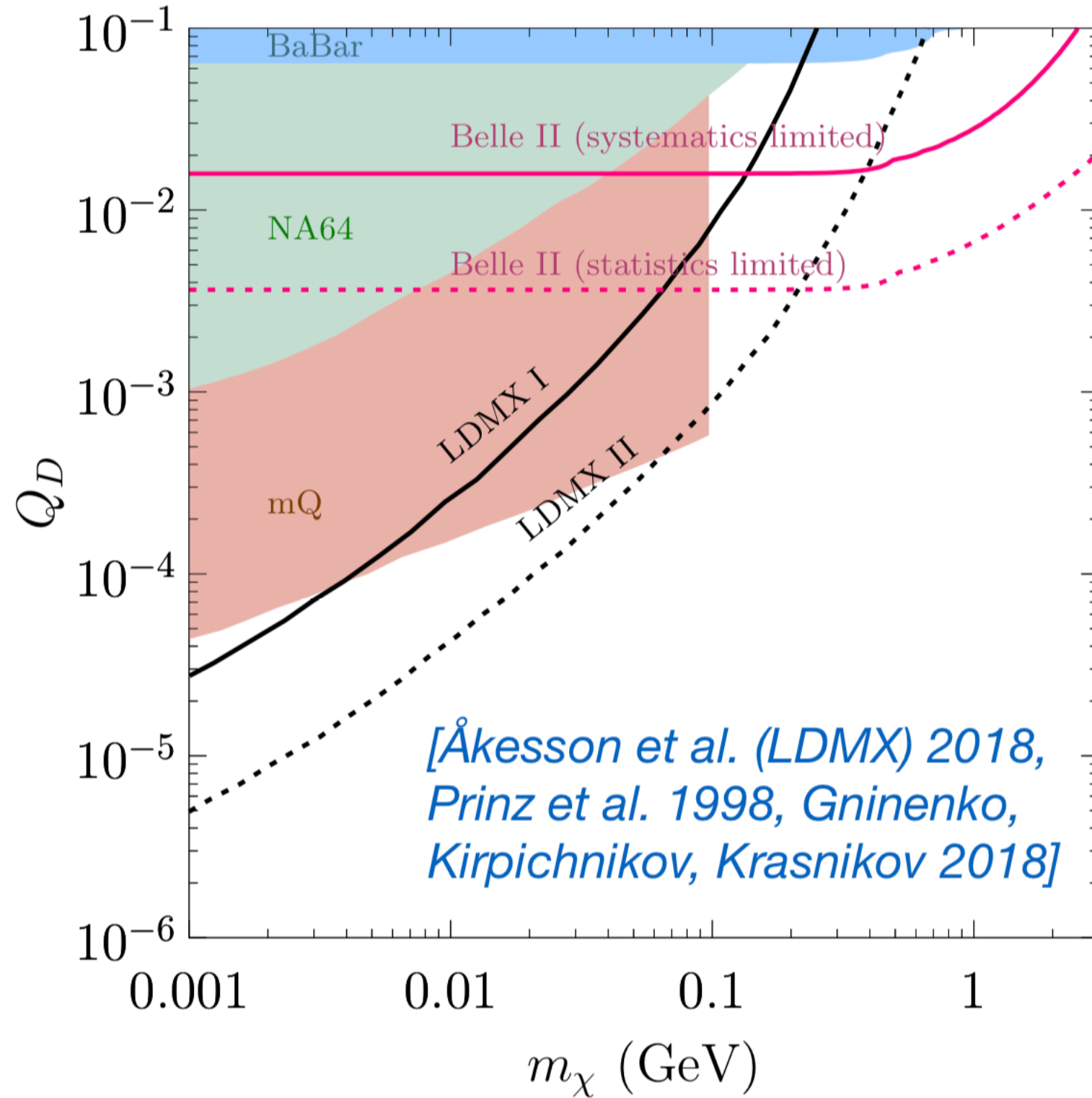
The f's carry the entire information of the new physics vertex

Cuts + veto system make searches largely background free

- Subsequent scattering (mQ, BDX)

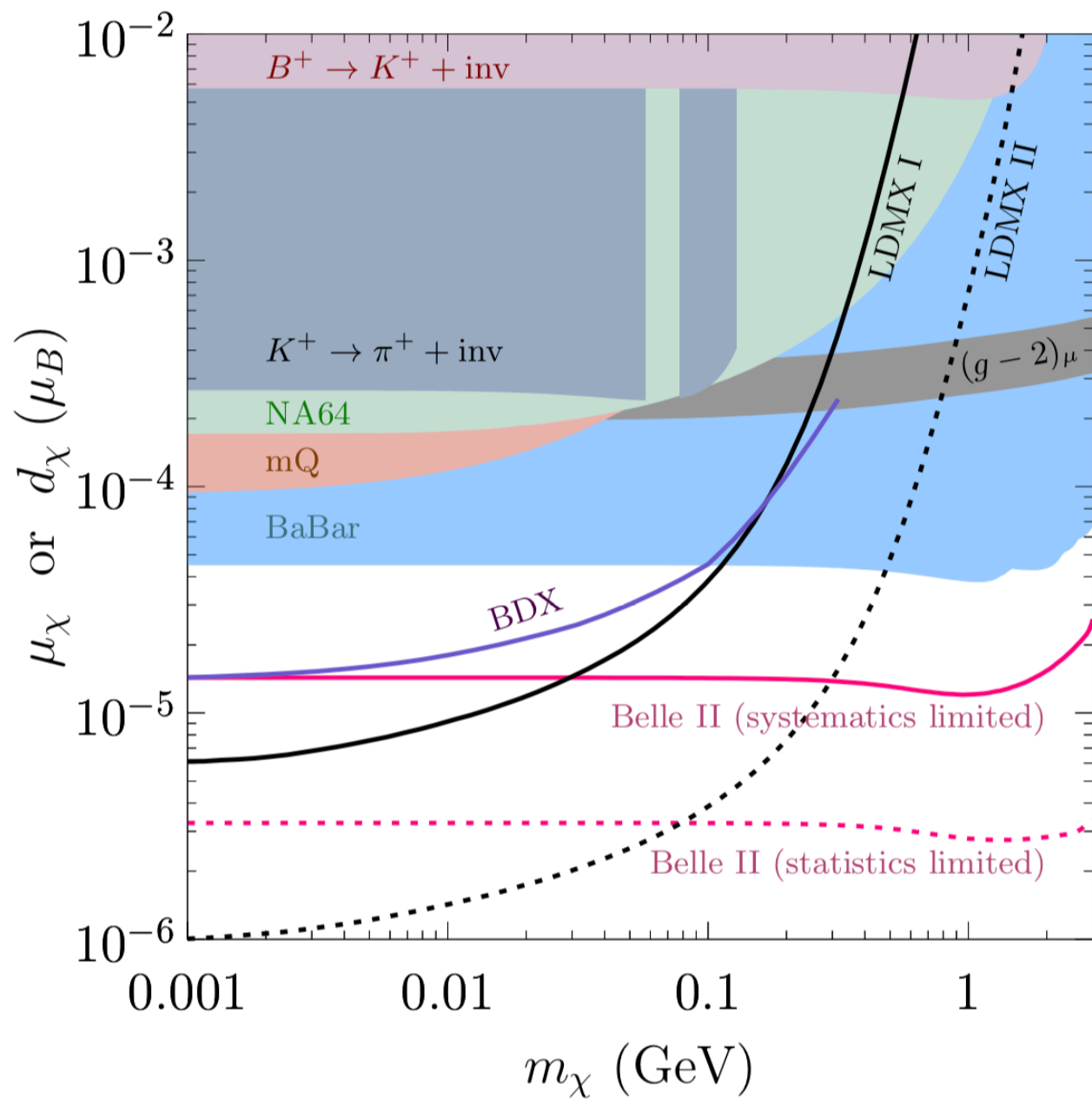


Milli-Charge



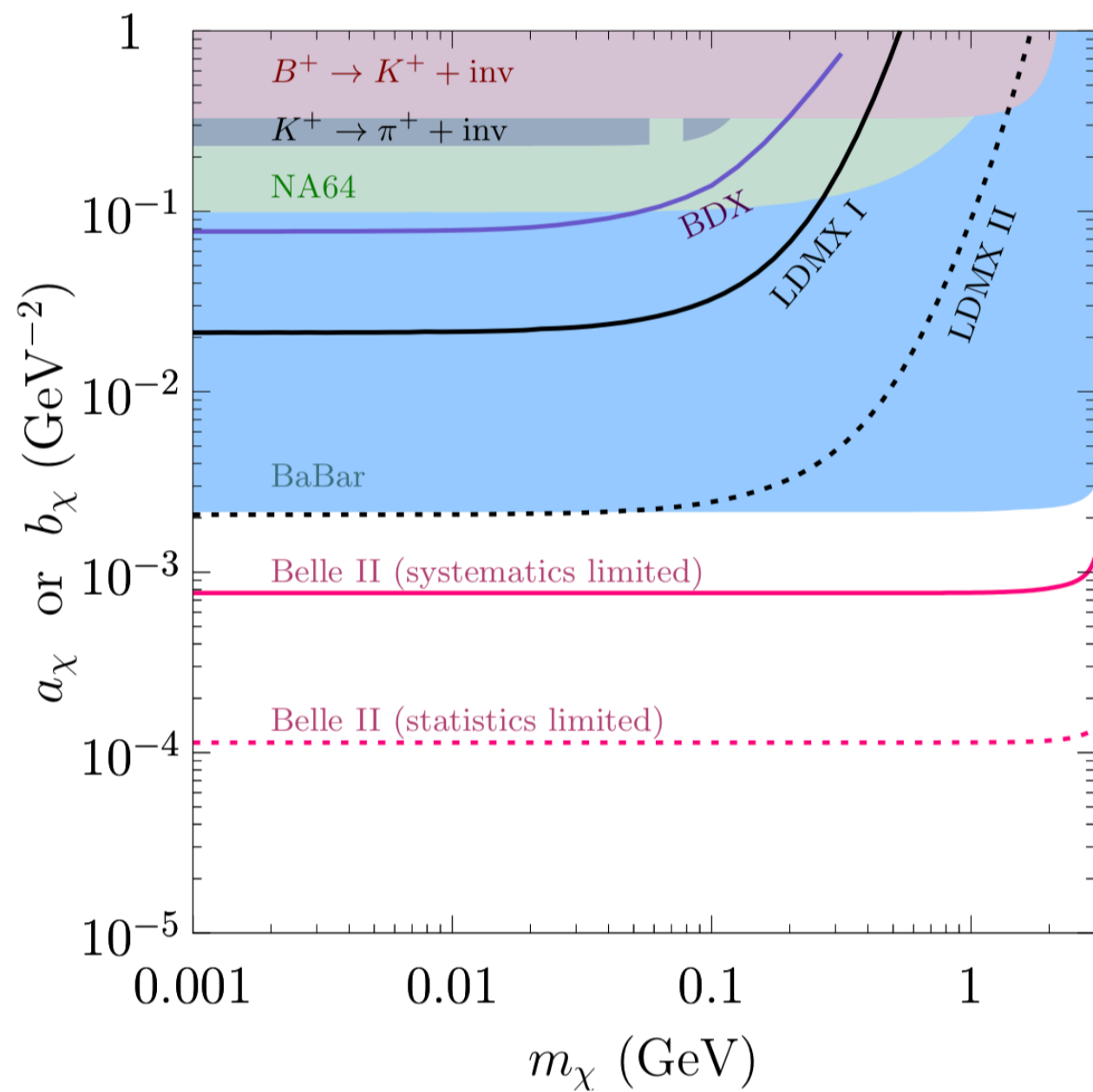
$$f(s_{\chi\bar{\chi}}) \propto s_{\chi\bar{\chi}}$$

Dipole Moment



$$f(s_{\chi\bar{\chi}}) \propto s_{\chi\bar{\chi}}^2$$

Charge Radius



$$f(s_{\chi\bar{\chi}}) \propto s_{\chi\bar{\chi}}^3$$

LEP & LHC

- LEP Mono-photon constraint

$$|\mu_\chi| \text{ or } |d_\chi| < 1.3 \times 10^{-5} \mu_B.$$

Fortin, Tait 2011

Following this analysis, we get

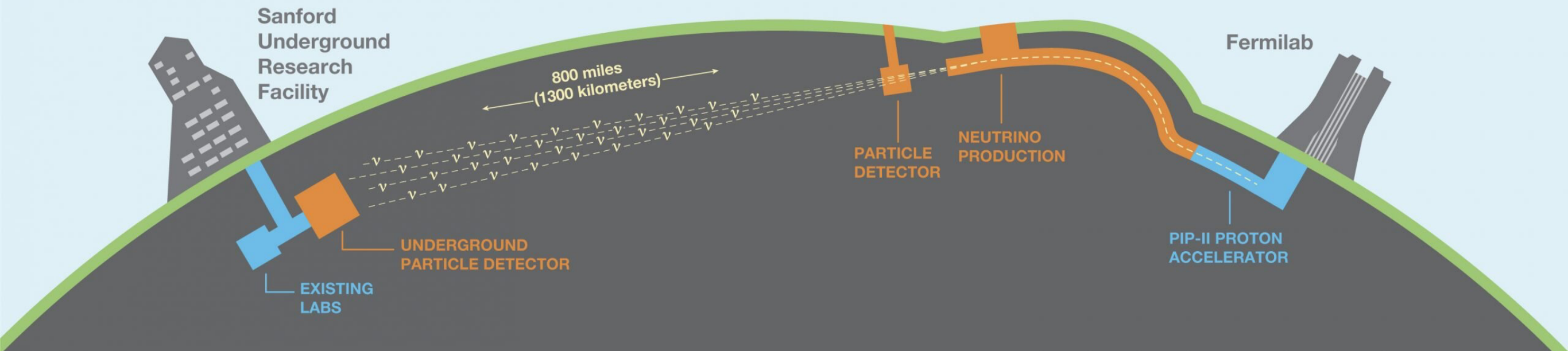
$$|a_\chi| \text{ or } |b_\chi| < 1.5 \times 10^{-5} \text{ GeV}^{-2}$$

- LHC constraints based on mono-photon and monojets comparable

see Barger et al 2012; Gao, Ho, Scherrer 2014

=> Lesson is that high-energy colliders do comparable at dim-5 and are superior for dim-6 operators compared to low-energy, high-intensity e-beams

Proton-beams



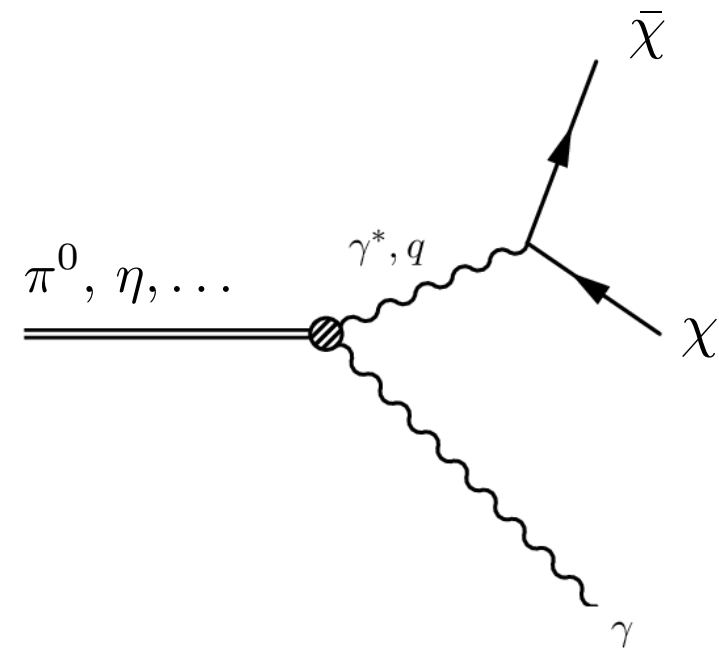
based on X. Chu, J.-L. Kuo, JP (arXiv today)

- proton beams are the workhorses of the short- and long-baseline neutrino program
- new light physics cases explored at near detectors, e.g. at LSND, MiniBooNE, COHERENT, DUNE etc.
- plus dedicated experiments that aim to probe dark sector states such as SHiP

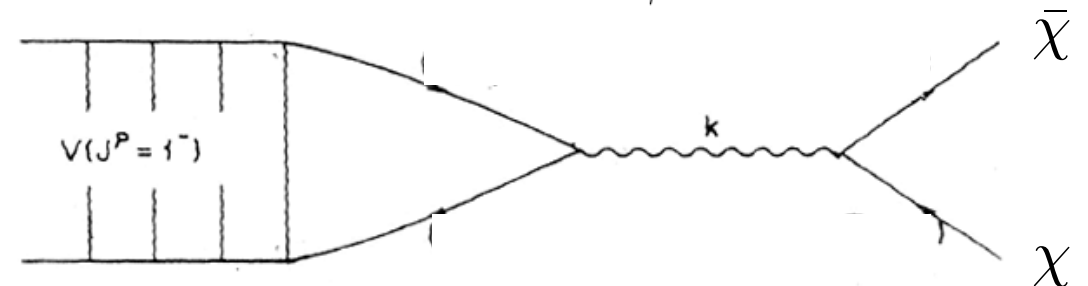
Proton-beams

- primary production channels

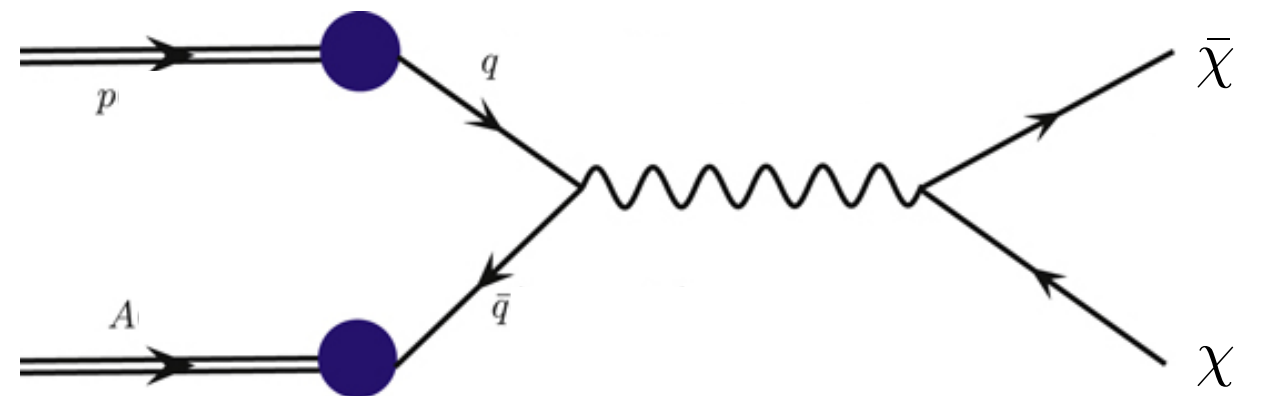
scalar meson Dalitz decay



vector meson 2-body decay



Drell-Yan production



Bremsstrahlung

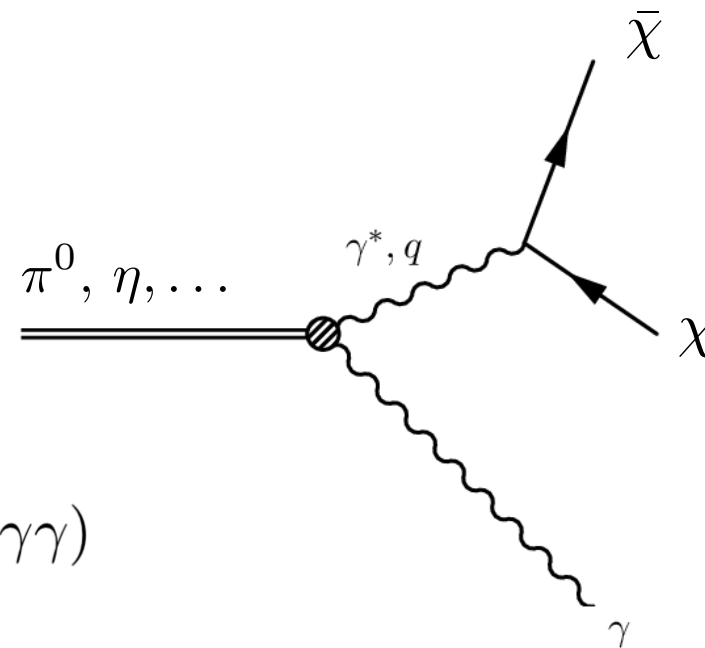
pion capture on nuclei

Proton-beams

- primary production channels

e.g. scalar meson Dalitz decay

$$\text{Br}(\text{sm} \rightarrow \gamma \chi \bar{\chi}) = \frac{\Gamma_{\text{sm} \rightarrow \gamma \chi \bar{\chi}}}{\Gamma_{\text{sm} \rightarrow \gamma \gamma}} \times \text{Br}(\text{sm} \rightarrow \gamma \gamma)$$



observations:

extra energy scale E needed to compensate for the presence of the dimensionful coupling (E for dim-5 and E^2 for dim-6)

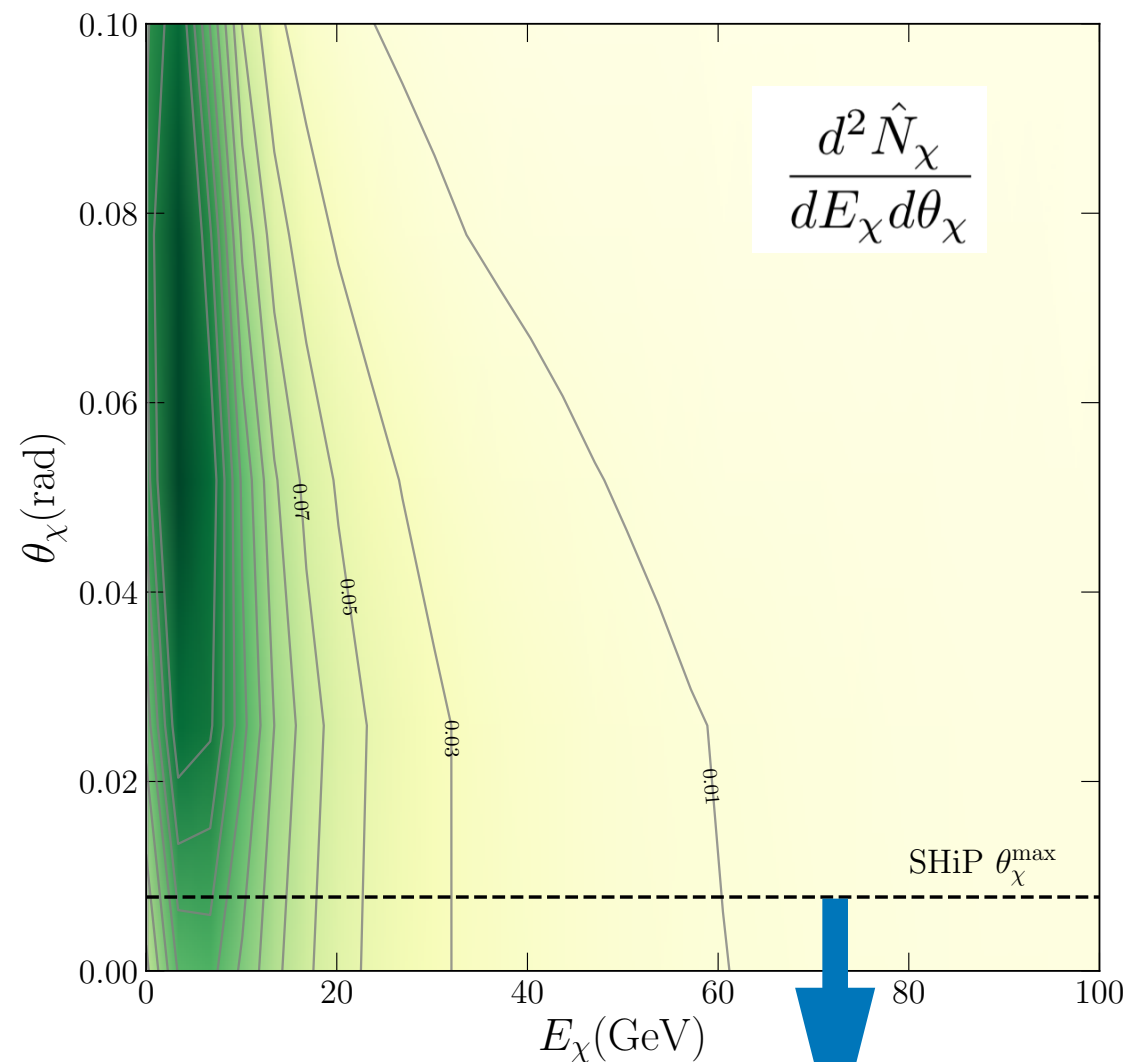
=> Drell-Yan gains importance as $E \sim \sqrt{s}$ compared to $E \sim m_{\text{meson}}$

=> higher mass meson decays become important

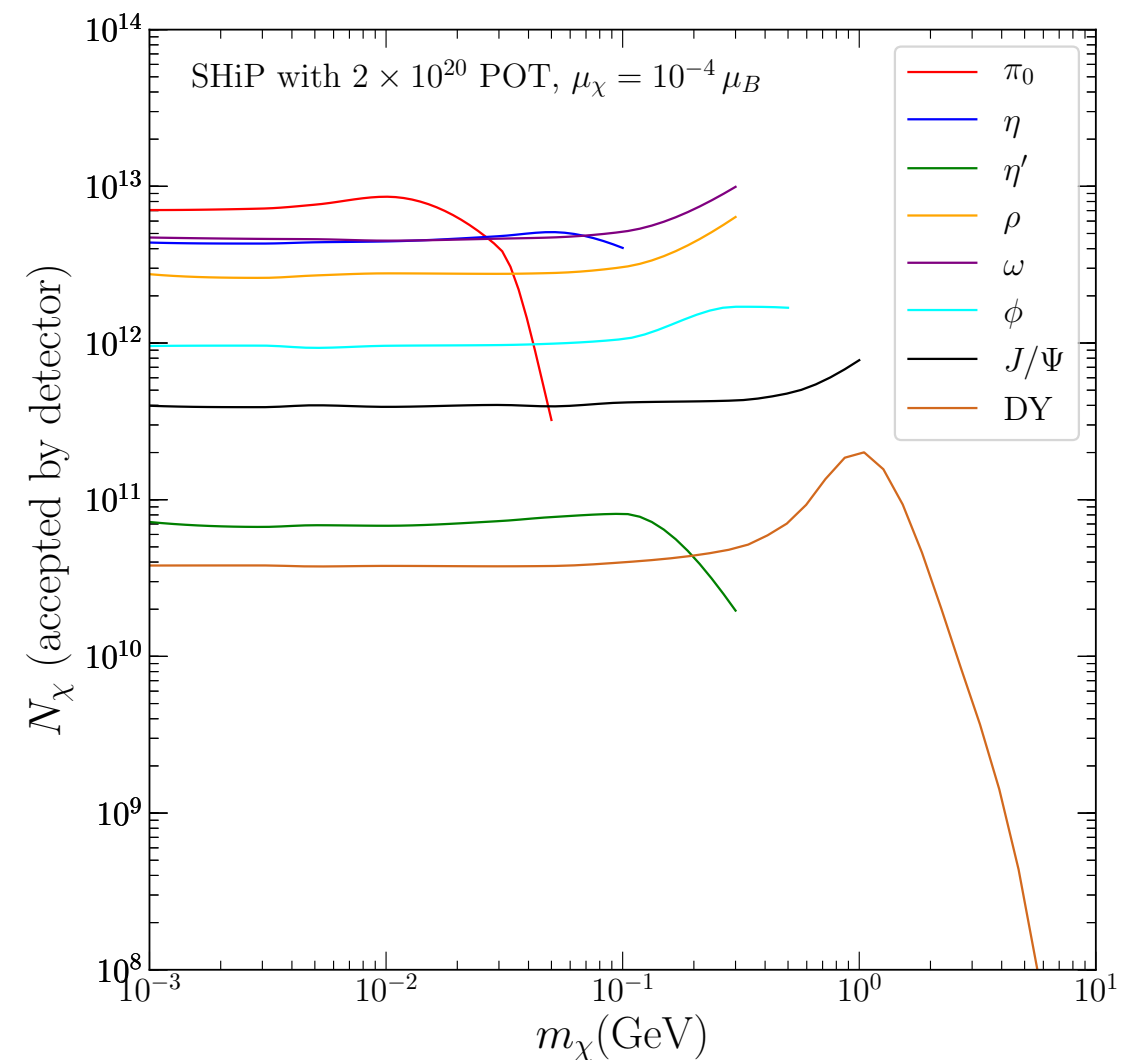
Proton-beams

- primary production channels

e.g. for SHiP

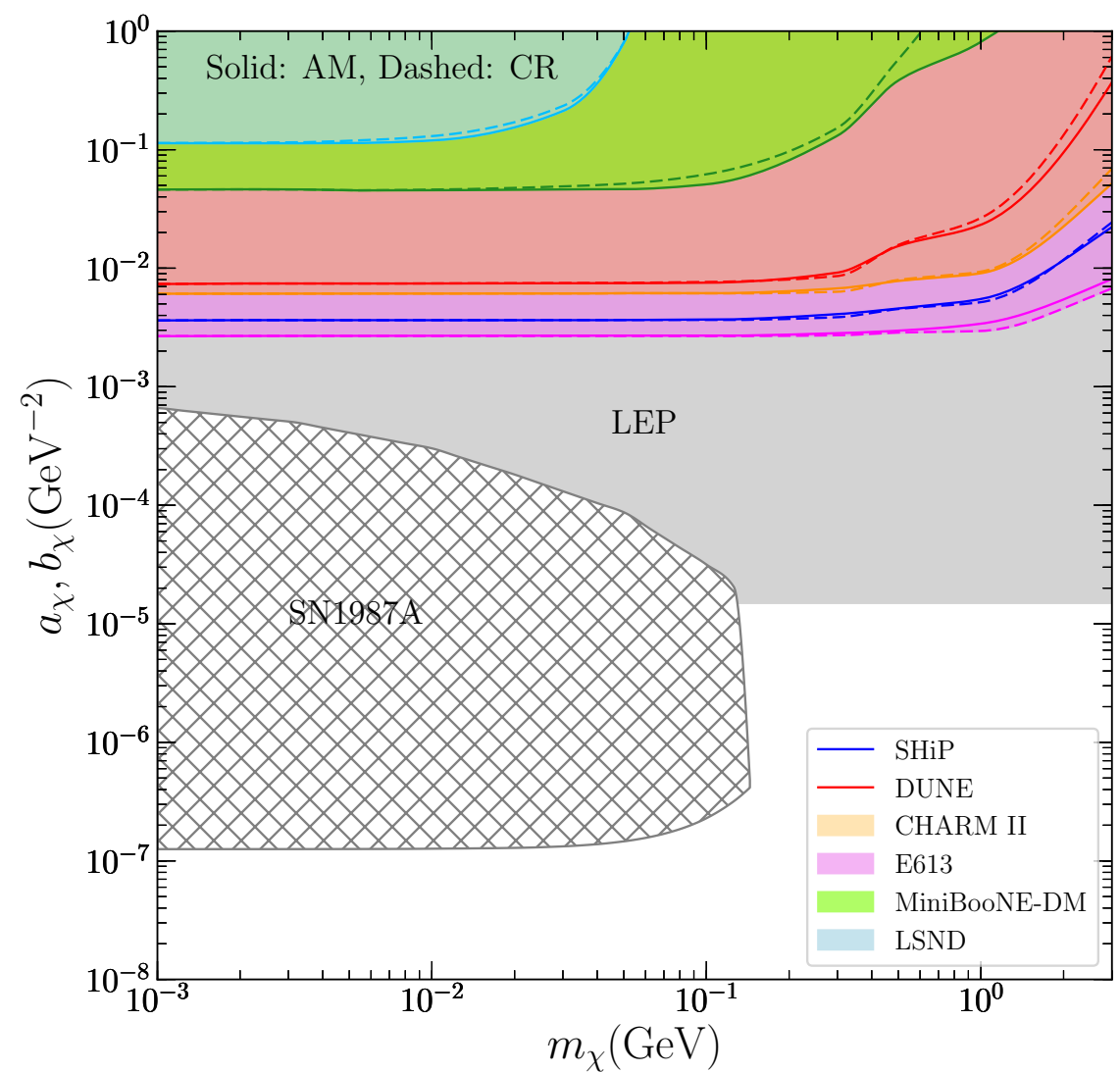
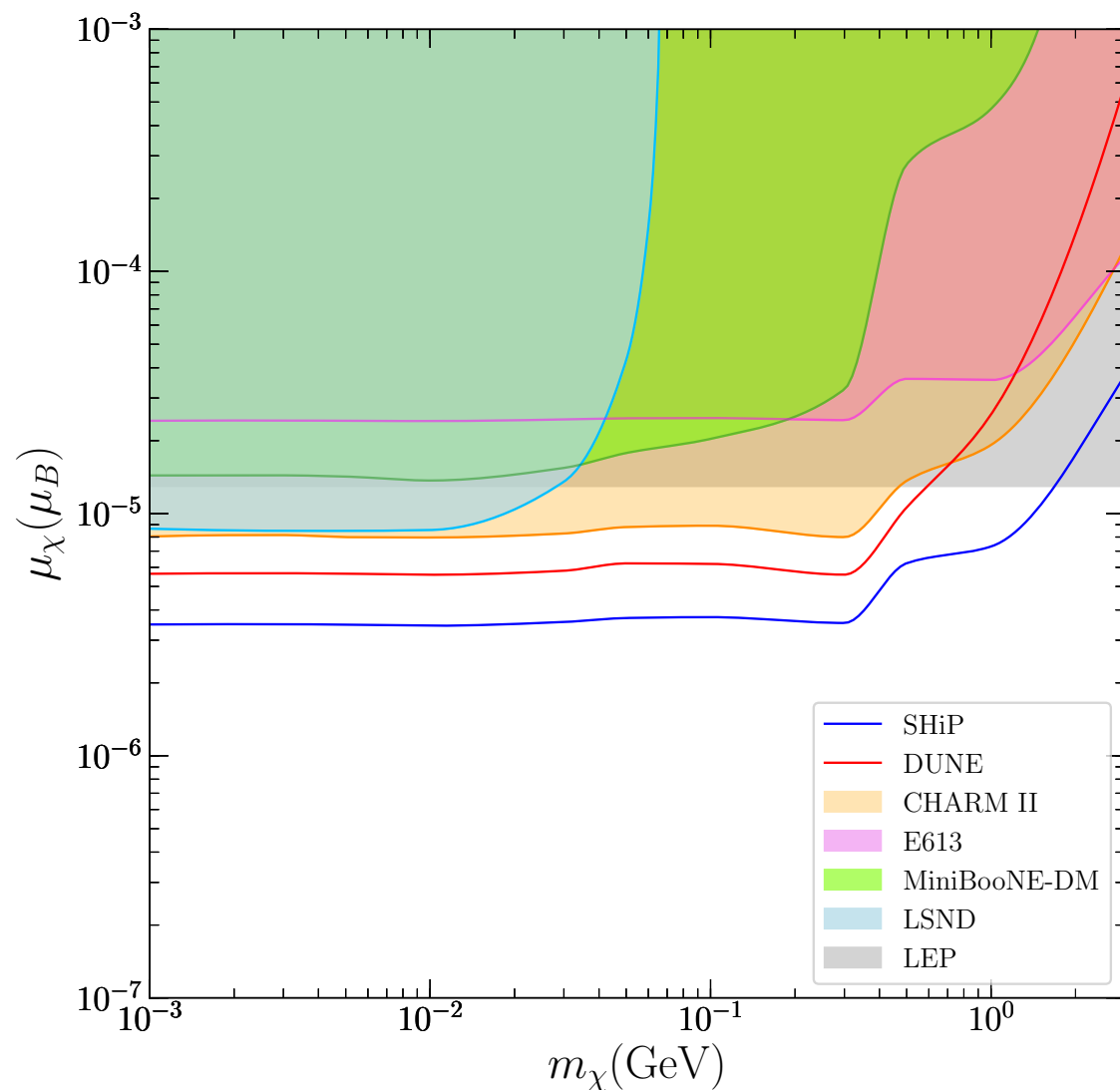


only a small fraction reach the detector



Proton-beams

- detection through electron-recoils and hadronic showers via DIS



=> not much improvement beyond that to be expected at intensity frontier;
 => high(er) energy colliders with efforts to detect milli-charged states beneficial

Can it be dark matter?

- Non-relativistic operators behave very differently, e.g. in annihilation

$\langle \sigma_{\chi\bar{\chi} \rightarrow l+l-\nu} \rangle$ s-wave for ϵQ , MDM, CR; p-wave for EDM, AM

$\langle \sigma_{\chi\bar{\chi} \rightarrow \gamma\gamma\nu} \rangle$ s-wave for ϵQ , MDM, EDM; 0 for AM, CR

=> also govern the indirect CMB and, for p-wave, Voyager limits

- Direct detection: sub-GeV region better probed by DM-electron scattering

MDM: $\overline{|M_{\chi e}(q)|^2} = 16\pi\mu_\chi^2\alpha m_\chi^2,$

EDM: $\overline{|M_{\chi e}(q)|^2} = \frac{64\pi d_\chi^2\alpha m_e^2 m_\chi^2}{q^2},$

AM: $\overline{|M_{\chi e}(q)|^2} = 16\pi a_\chi^2\alpha m_\chi^2 q^2,$

CR: $\overline{|M_{\chi e}(q)|^2} = 64\pi b_\chi^2\alpha m_e^2 m_\chi^2.$

<= various q-dependencies
that are moved into an
atomic form factor

Cosmo- and astro-constraints

- Dark radiation / N_{eff}

(sub-)MeV mass χ particles reach thermal equilibrium for $T > m$ once

$$\begin{array}{llll} \mu_\chi, d_\chi \geq 10^{-9} \mu_B & \text{dim-5} & \Rightarrow & m_\chi \gtrsim 7 - 10 \text{ MeV} \\ a_\chi, b_\chi \geq 5 \times 10^{-5} \text{ GeV}^{-2} & \text{dim-6} & & \end{array}$$

- DM self-interactions

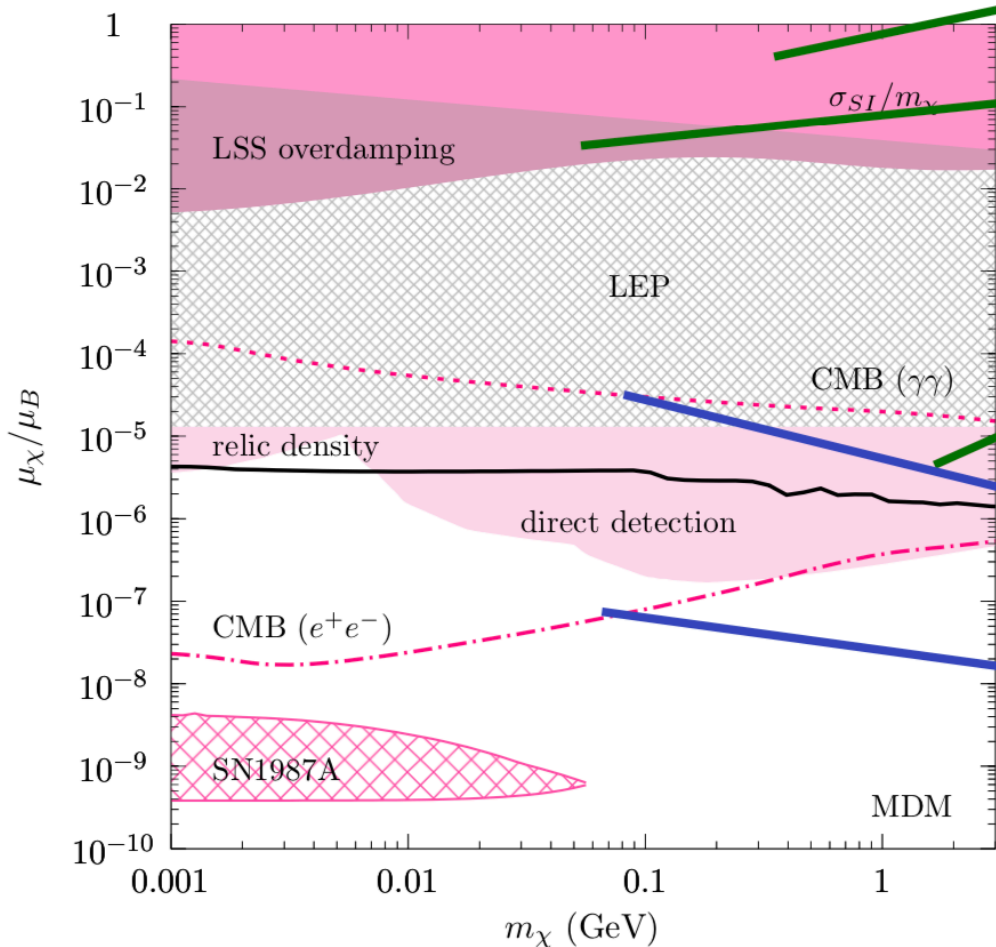
In contrast to Millicharged DM, EM-moments have no enhancement at low relative velocities

$\Rightarrow$ Bullet-cluster limit applies $\sigma_{\text{SI}}/m_\chi \lesssim 1.25 \text{ cm}^2/\text{g}$

Robertson, Massey, Eke 2008

Summary of EMDM Dark Matter constraints

Magnetic Dipole Moment



Dark Matter

Self scattering cross section: $\sigma/m < 1 \text{ cm}^2/\text{g}$

Damping of large scale structures
Kinetic decoupling before $T_\gamma < 0.5 \text{ keV}$

Direct detection: Xenon 10 and Xenon 1T

Symmetric Dark Matter

Annihilation to two photons

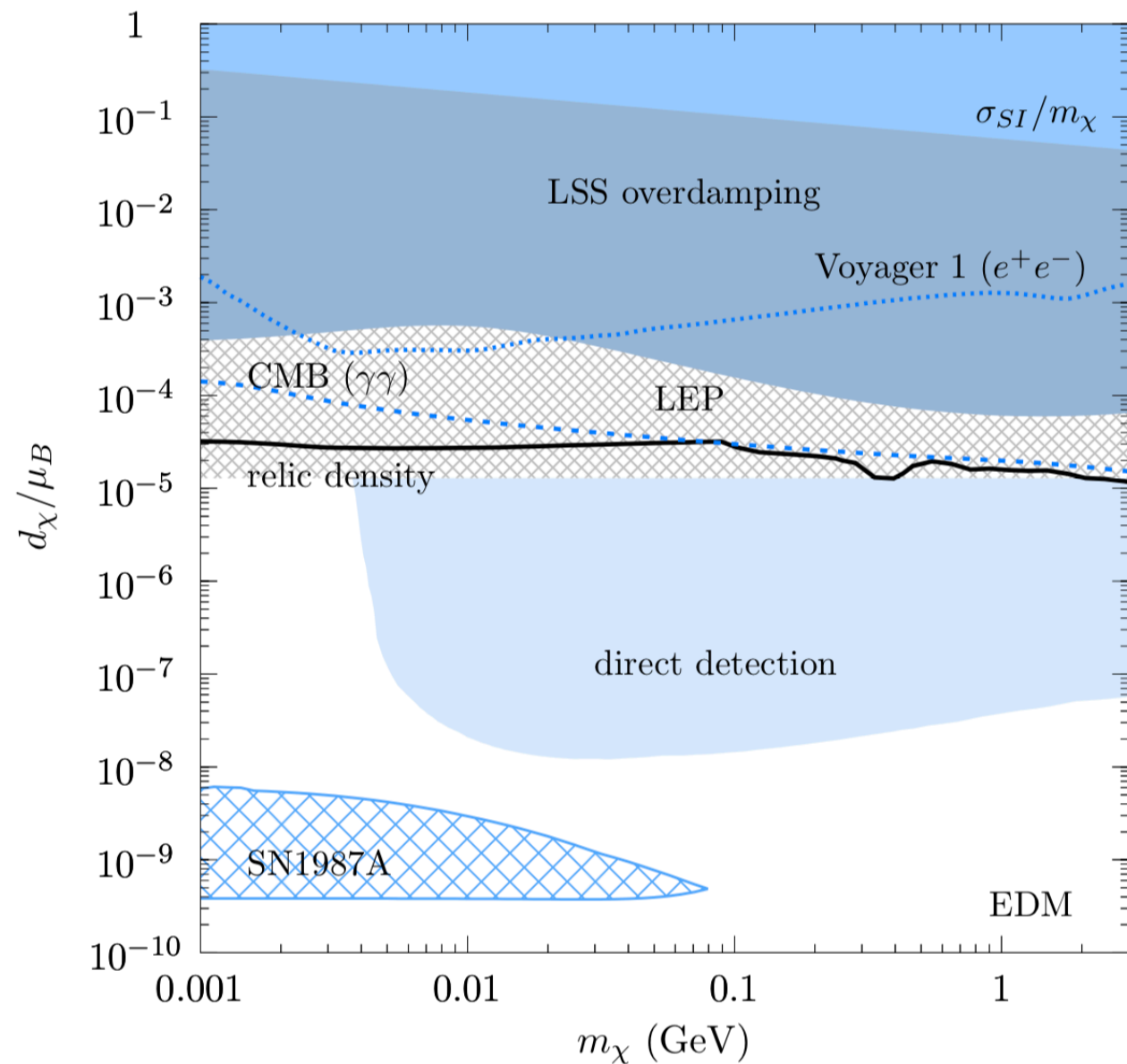
MDM/EDM: s-wave, **AM/CR:** forbidden on tree level

Annihilation to an e^+e^- pair

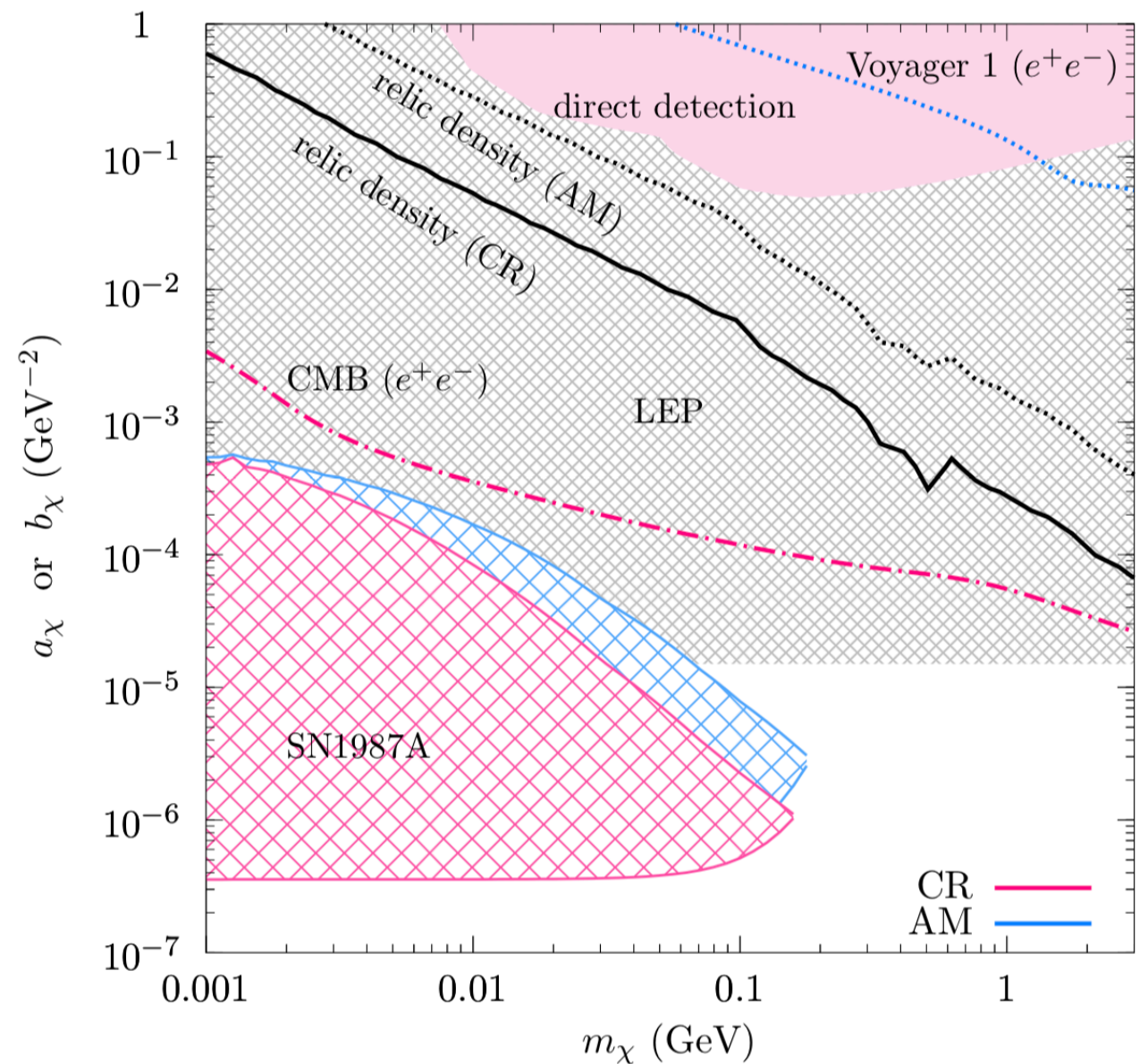
MDM/CR: s-wave (CMB), **EDM/AM:** p-wave (Voyager I)

Summary of EMDM Dark Matter constraints

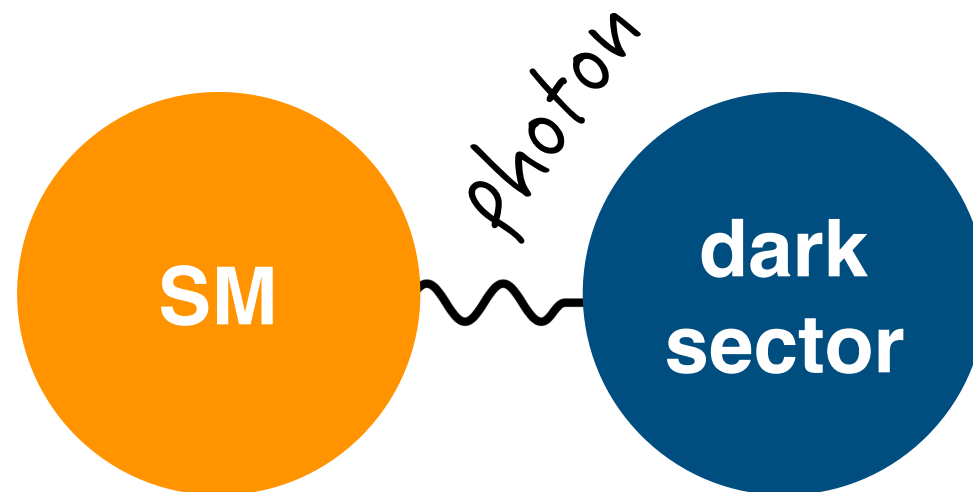
Electric Dipole Moment



Anapole Moment / Charge Radius



Light dark states through the *photon portal*



MeV - GeV mass-bracket:

=> established a complete phenomenological picture

sub-MeV masses:

=> strong astrophysical implications

=> stars as laboratories for dark-sector photon interactions

Stars reacting to energy loss

$$\langle E_{\text{kin}} + E_{\text{grav}} \rangle \searrow$$

1. Stars supported by radiation pressure (active stars):

Virial theorem: $\langle E_{\text{kin}} \rangle = -\frac{1}{2} \langle E_{\text{grav}} \rangle$

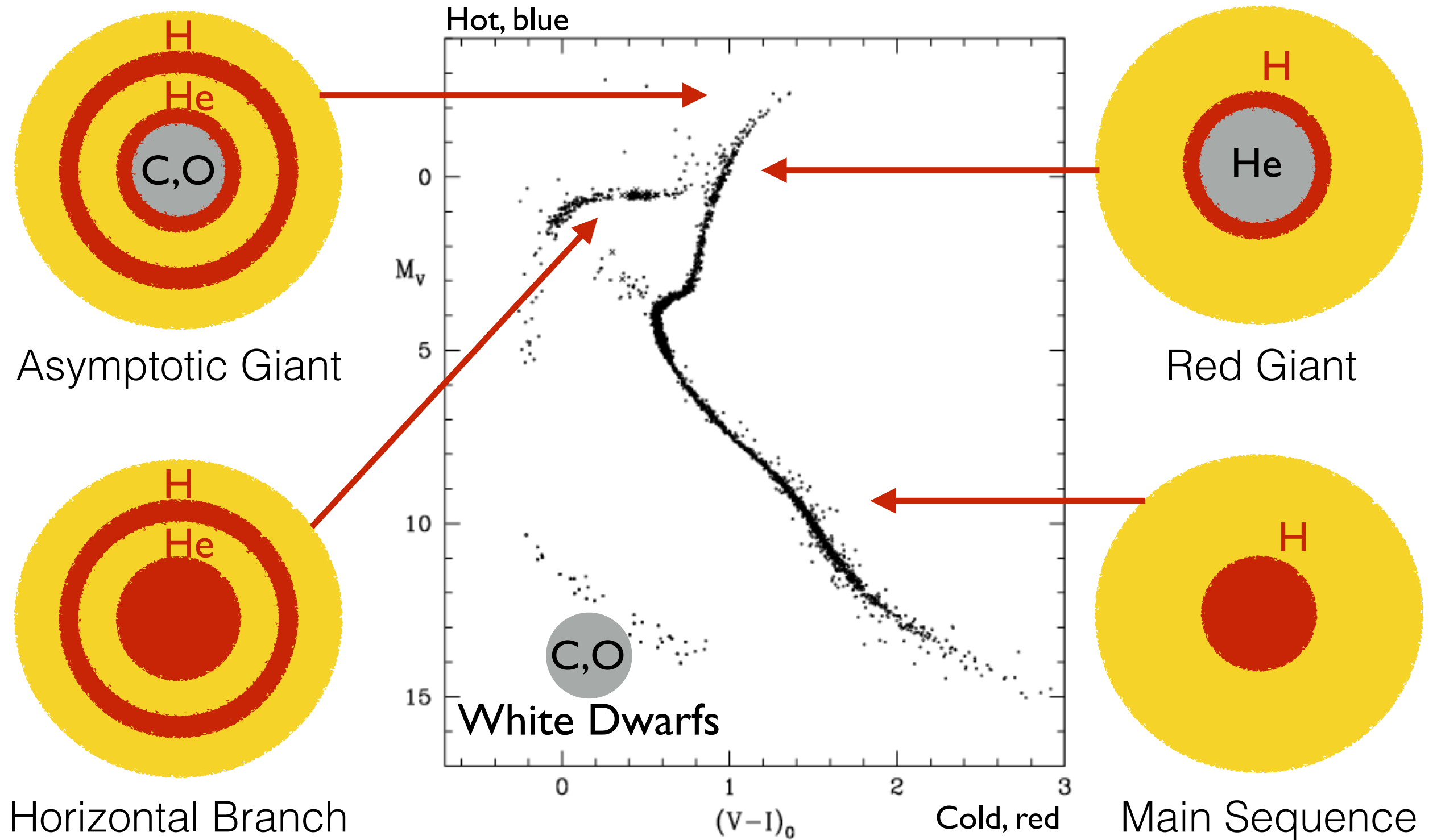
=> Gravitational potential energy becomes more negative (tighter bound)

=> average kinetic energy increases, **star becomes hotter,**
negative heat capacity

2. Stars supported by degeneracy pressure (white dwarfs, neutron stars):

possess positive heat capacity, the star actually cools by the energy loss

Stars as laboratories



Globular Cluster color-magnitude diagram

Inferred limits on anomalous energy loss

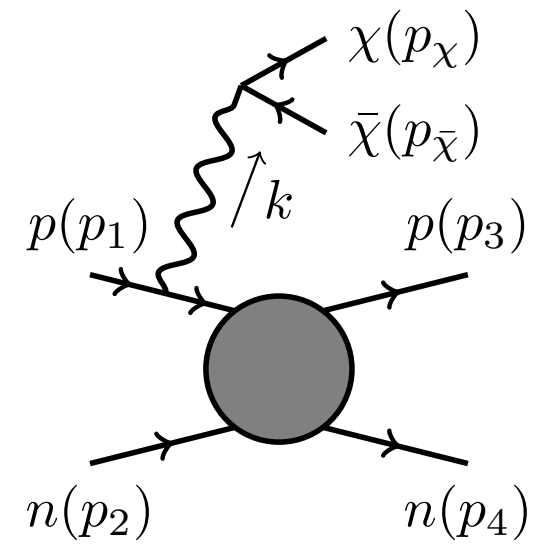
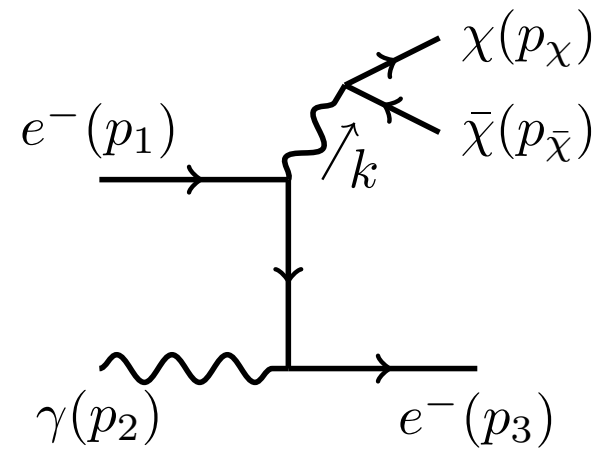
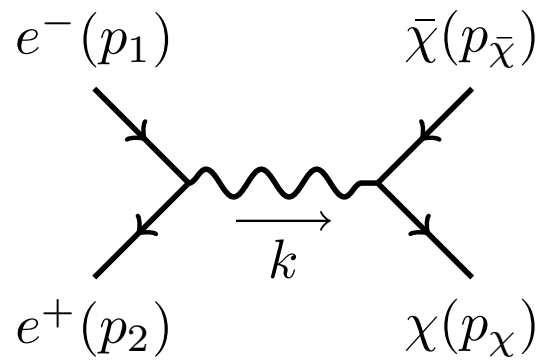
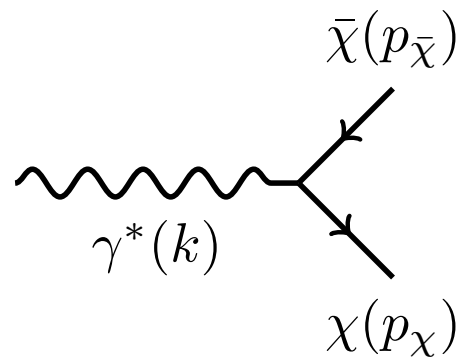
Sun $\int_{\text{sun}} dV \dot{Q} < 10\% \times L_{\odot}$ Inferred from observed boron neutrino flux

HB $\int_{\text{core}} dV \dot{Q} < 10\% \times L_{\text{HB}}$ Inferred from He-burning lifetime

RG $\dot{Q} < 10 \text{ erg/g/s} \times \rho_{\text{RG}}$ Inferred from maximum RG core mass

SN $\int_{\text{core}} dV \dot{Q} < L_{\nu}$ Inferred from cooling curve of SN1987A

Stellar Probes of dark-sector photon interactions

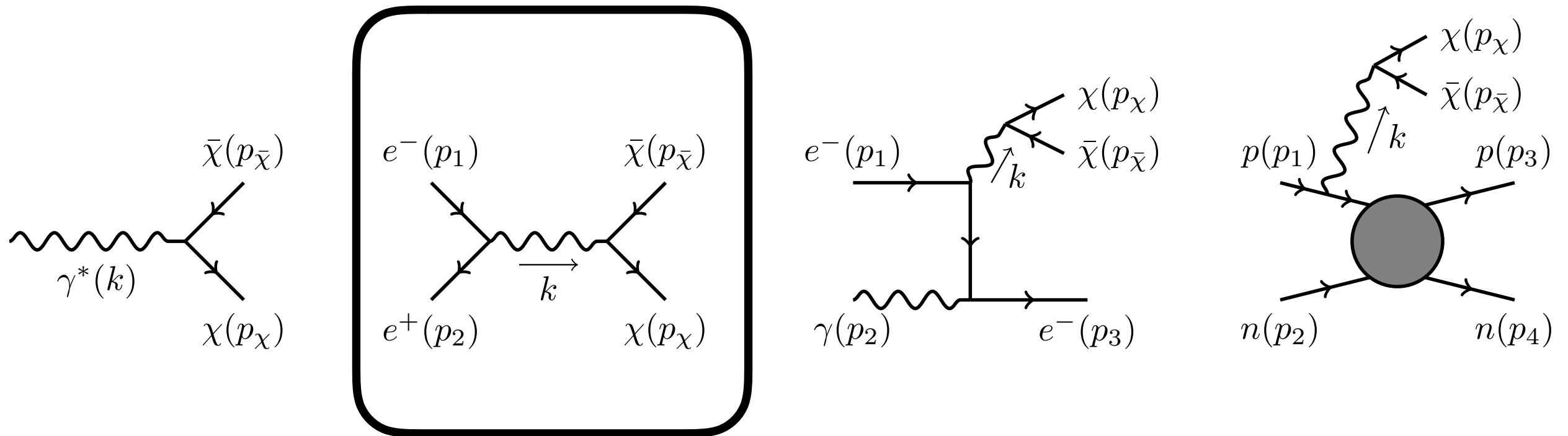


T/L “Plasmon” decay

(all)

$$\omega_p \sim \begin{cases} 0.3 \text{ keV} & \text{Sun's core} \\ 2.6 \text{ keV} & \text{HB's core} \\ 8.6 \text{ keV} & \text{RG's core} \\ 17.6 \text{ MeV} & \text{SN's core} \end{cases}$$

Stellar Probes of dark-sector photon interactions

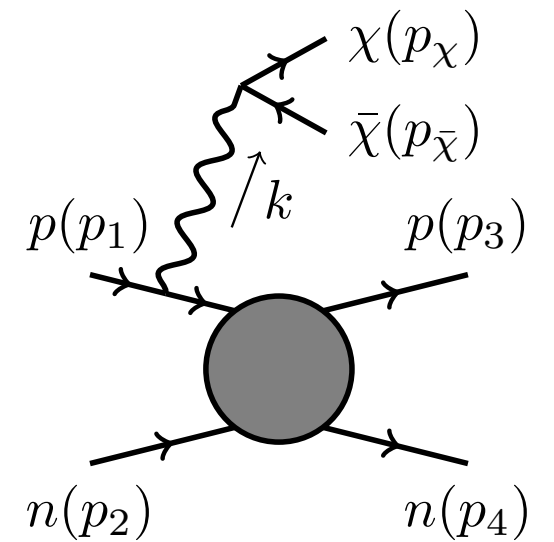
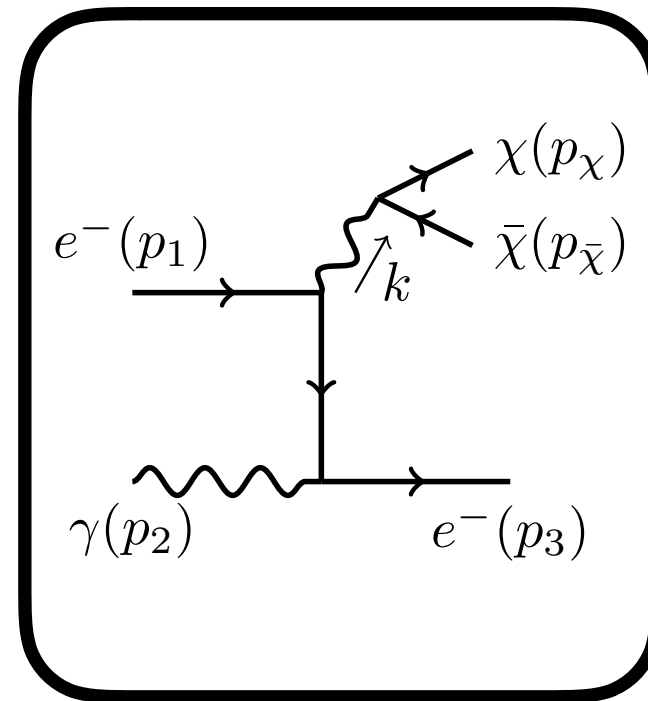
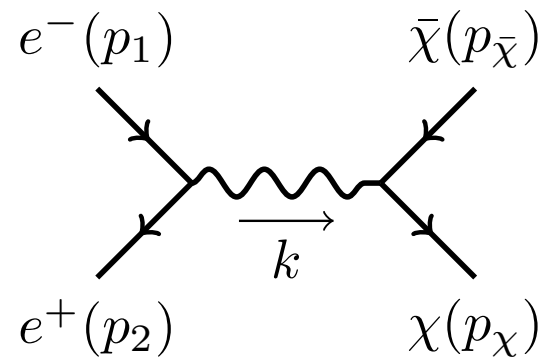
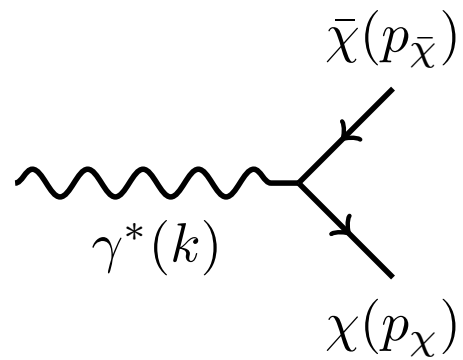


e^+e^- annihilation

(SN)

NB: no overlap with plasmon decay

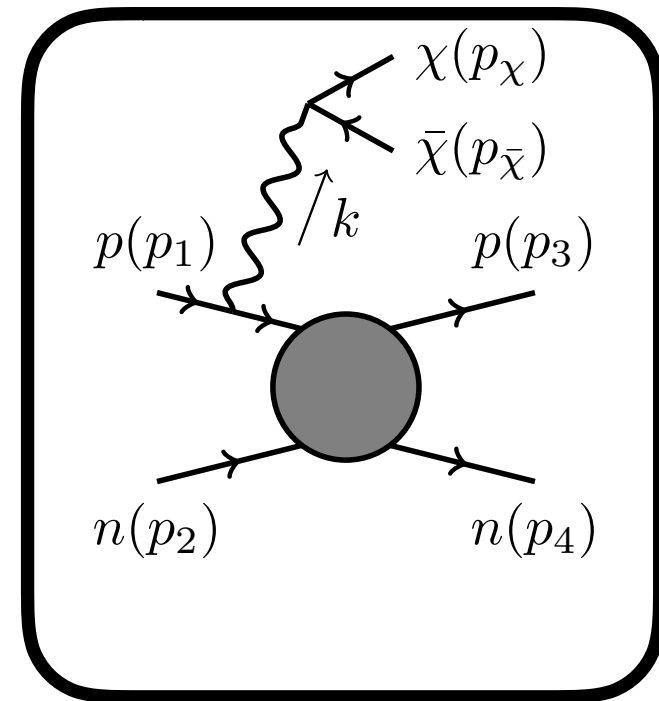
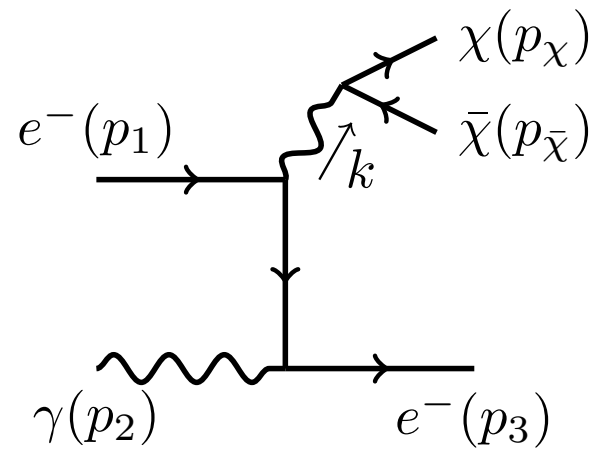
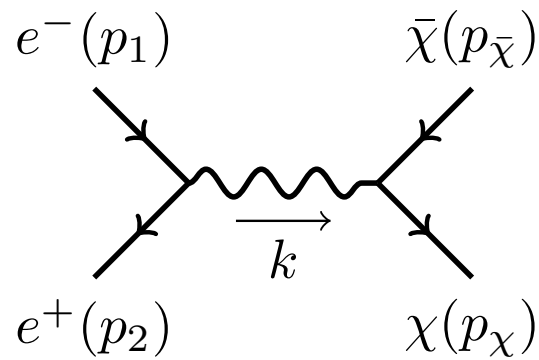
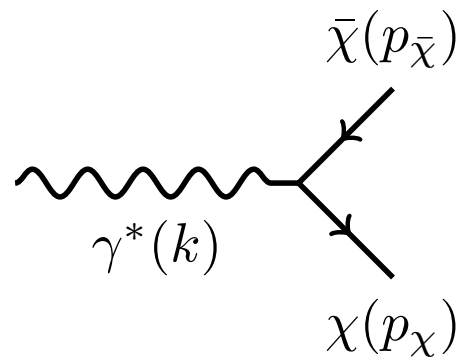
Stellar Probes of dark-sector photon interactions



Compton 2- $\rightarrow$ 3 production

(all)

Stellar Probes of dark-sector photon interactions



Electron-nucleus Bremsstrahlung

(RG, HB, Sun)

NB: soft-photon approximation
not applicable

Neutron-proton Bremsstrahlung

(SN)

NB: we use exp. data for np-brems

Rrapaj, Reddy 2016

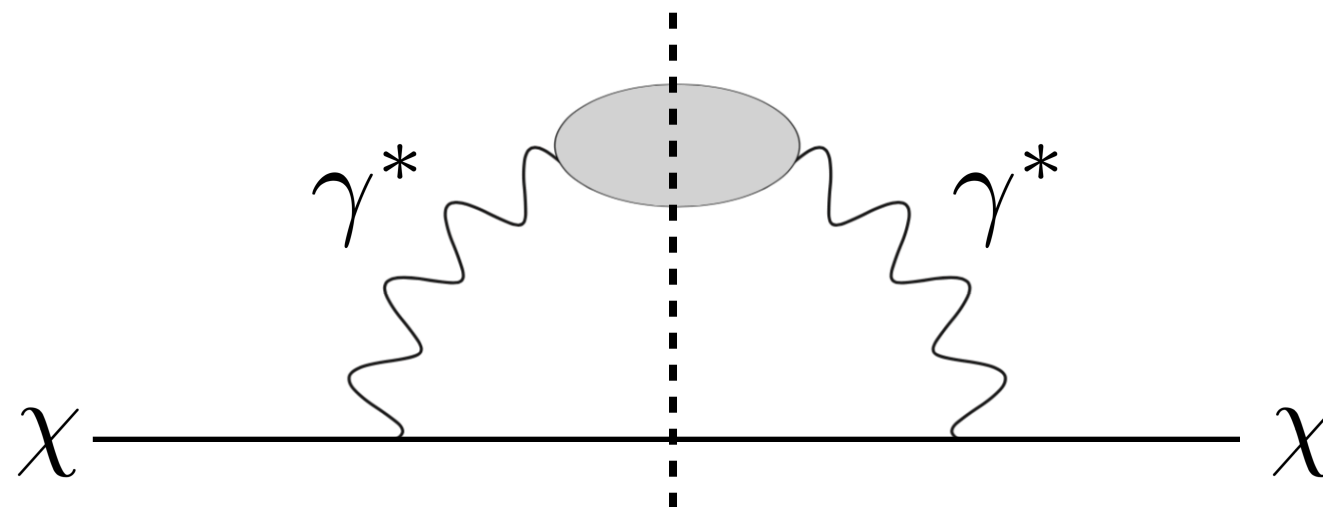
Exact Formula for pair-emission

$$\dot{N}_\chi = - \int \frac{d^3 \vec{p}_\chi}{(2\pi)^3} \frac{1}{(e^{E_\chi/T} + 1)} \frac{\text{Im } \Pi_\chi(E_\chi, \vec{p}_\chi)}{E_\chi}$$

Finite-T optical theorem: rate with which a particle comes into thermal equilibrium is given by the discontinuity of the self energy

$$\text{Im } \Pi_\chi(E_\chi, \vec{p}_\chi) = \bar{u}(p_\chi) \Sigma(E_\chi, \vec{p}_\chi) u(p_\chi)$$

Weldon 1983



Exact Formula for pair-emission

$$\frac{d\dot{N}_\chi}{ds_{\chi\bar{\chi}}} = - \sum_{i=T,L} g_i \int \frac{d^3\vec{k}}{(2\pi)^3} \frac{1}{(e^{\omega/T} - 1)} \frac{\text{Im } \Pi_i(\omega, \vec{k})}{\omega} \times \frac{f(s_{\chi\bar{\chi}})}{16\pi^2 |s_{\chi\bar{\chi}} - \Pi_i|^2} \sqrt{1 - \frac{4m_\chi^2}{s_{\chi\bar{\chi}}}}$$

In this version (derived from works on dilepton-production in hot matter) the imaginary part of the *photon self-energy* enters

$$\Pi^{\mu\rho} = (\epsilon_{T,1}^\mu \epsilon_{T,1}^\rho + \epsilon_{T,2}^\mu \epsilon_{T,2}^\rho) \Pi_T + \epsilon_L^\mu \epsilon_L^\rho \Pi_L$$

=> leading contribution from the pole $s_{\chi\bar{\chi}} = \text{Re } \Pi_{L,T}$
recover plasmon-decay rate

=> further contributions to chi-pair production found from identifying the contributions to the photon self-energy

Breakdown of other processes

$$2 \operatorname{Im} \left[\gamma^* \text{---} \text{SM} \text{---} \gamma^* \right] = 2 \operatorname{Im} \left[\gamma^* \text{---} \text{SM} \text{---} \gamma^* + \gamma^* \text{---} \text{SM} \text{---} \gamma^* + \gamma^* \text{---} \text{SM} \text{---} \gamma^* + \dots \right]$$

One identifies all other important processes:
annihilation, Compton-production, Bremsstrahlung, ...

NB: in the paper we have a careful discussion on potential double-counting between the processes

Breakdown of other processes

$$2 \operatorname{Im} \left[\begin{array}{c} \gamma^* \\ \text{wavy line} \end{array} \bullet \text{SM} \bullet \begin{array}{c} \gamma^* \\ \text{wavy line} \end{array} \right] = \int d\Pi_i \left[\left| \begin{array}{c} \text{SM} \\ \text{SM} \end{array} \right. \begin{array}{c} \text{ } \\ \text{ } \end{array} \begin{array}{c} \text{ } \\ \text{ } \end{array} \bullet \begin{array}{c} \gamma^* \\ \text{wavy line} \end{array} \right|^2 + \left| \begin{array}{c} \text{SM} \\ \gamma \\ \text{SM} \end{array} \right. \begin{array}{c} \text{ } \\ \text{ } \\ \text{ } \end{array} \bullet \begin{array}{c} \gamma^* \\ \text{wavy line} \end{array} \right|^2 + \left| \begin{array}{c} \text{SM} \\ \text{SM} \\ \text{SM} \\ \text{SM} \end{array} \right. \begin{array}{c} \text{ } \\ \text{ } \\ \text{ } \\ \text{ } \end{array} \bullet \begin{array}{c} \gamma^* \\ \text{wavy line} \end{array} \right|^2 + \dots \right]$$

One identifies all other important processes:

annihilation, Compton-production, Bremsstrahlung, ...

NB: in the paper we have a careful discussion on potential double-counting between the processes

Energy loss rates

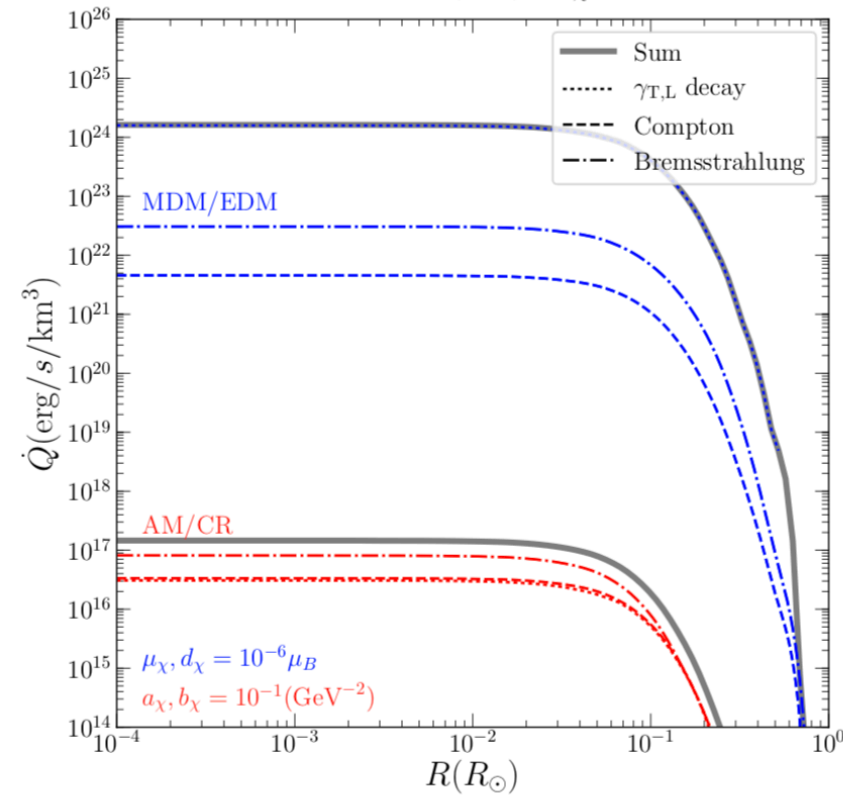
Sun

dominant process:

MDM/EDM: plasmon decay

AM/CR: all

Energy Loss Rate (Sun), $m_\chi = 0.01$ keV



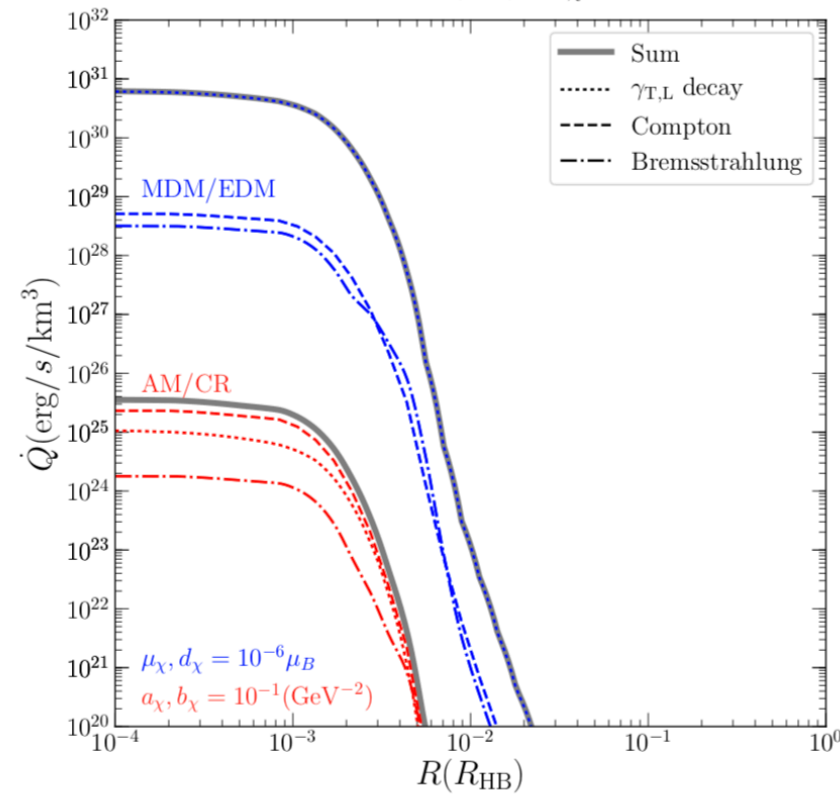
Horizontal Brach Stars

dominant process:

MDM/EDM: plasmon decay

AM/CR: plasmon decay, Compton scattering

Energy Loss Rate (HB), $m_\chi = 0.01$ keV



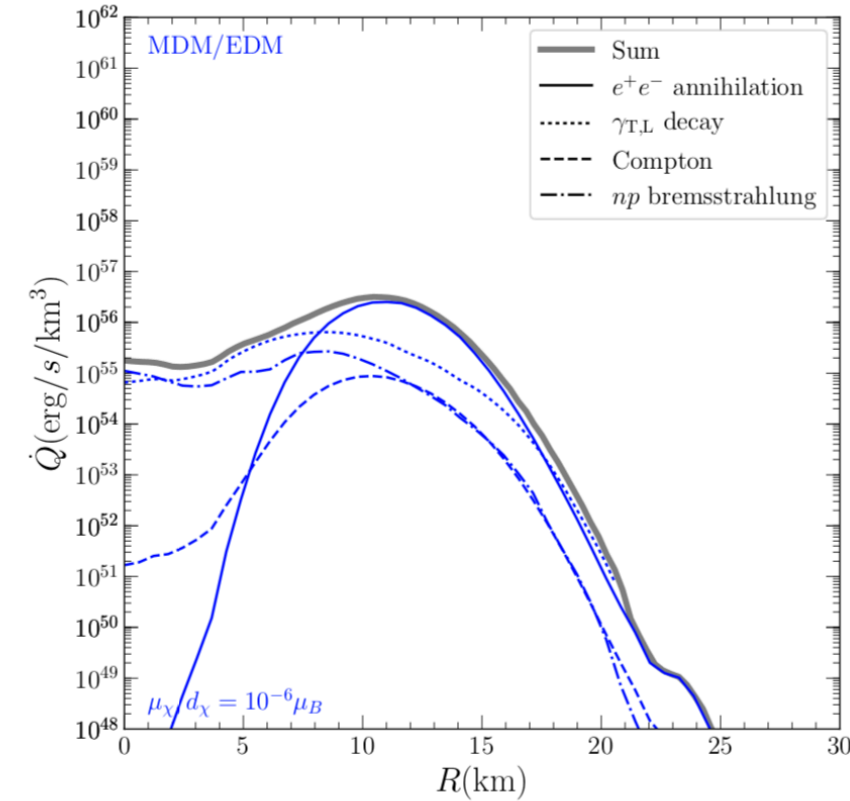
Supernovae

dominant processes:

annihilation, bremsstrahlung,

plasmon decay

Energy Loss Rate (SN), $m_\chi = 1$ MeV





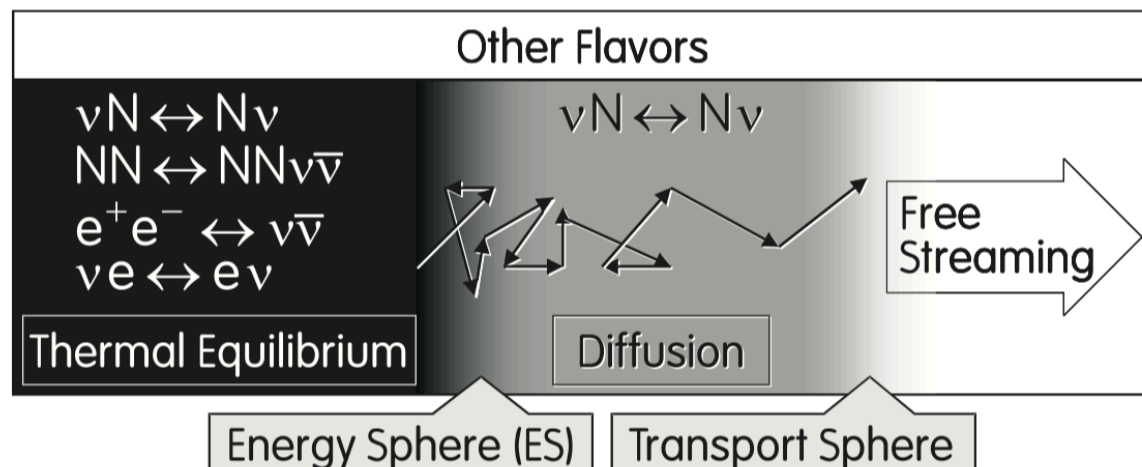
Supernova cooling

- Pair production of χ particles with $m_\chi \lesssim 400 \text{ MeV}$ in SN possible

Lower boundary: use “Raffelt-criterion” $\int_0^{r_{\text{core}}} d^3r \dot{Q} \leq L_\nu$

Upper boundary: energy-loss fails to be efficient because of trapping, rough criterion

=> we do a detailed analysis accounting for diffusion zone

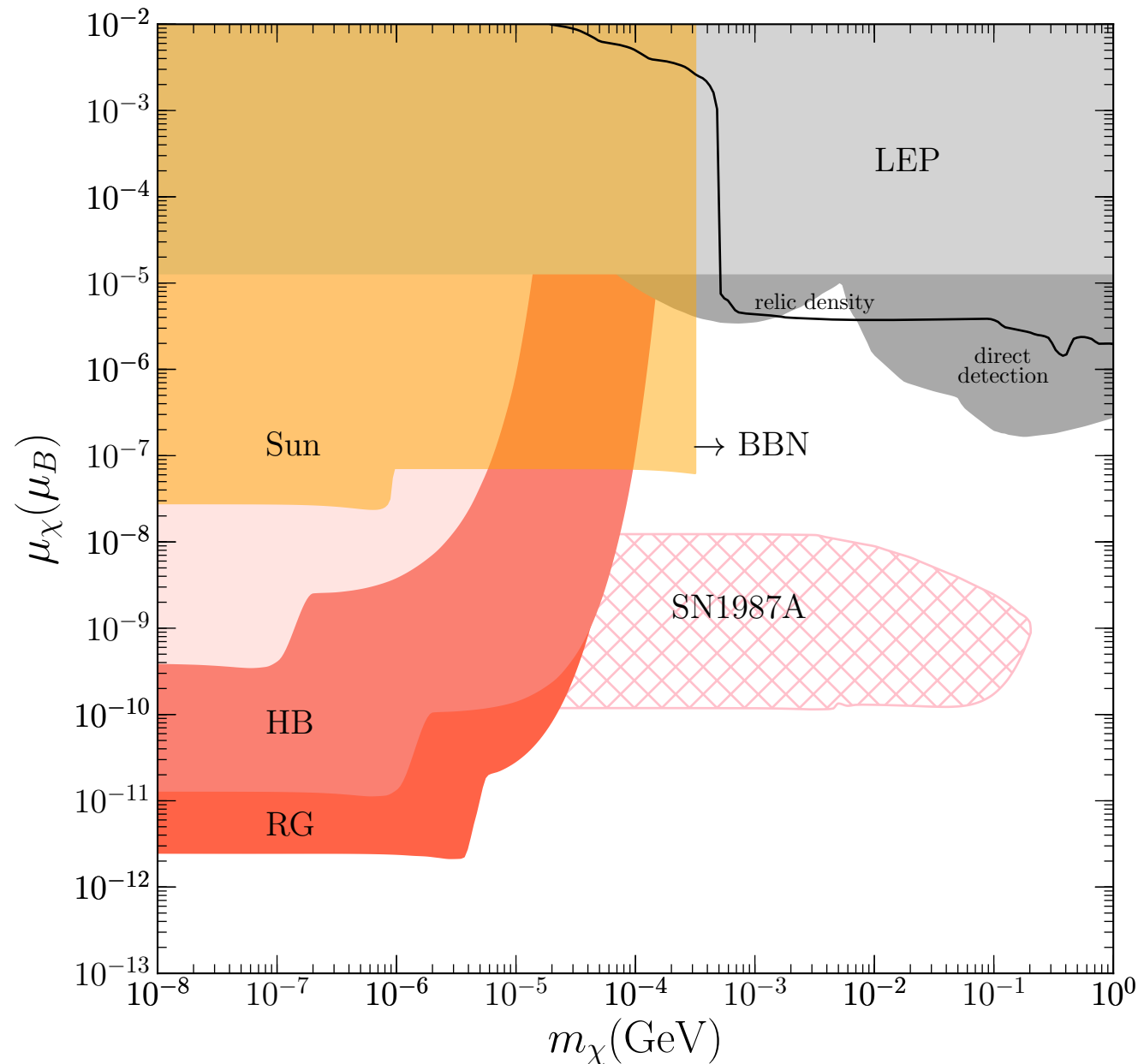


$$L_{\text{inf}} = L_\chi(r_{\text{ES}}) S_{\text{ES}}$$

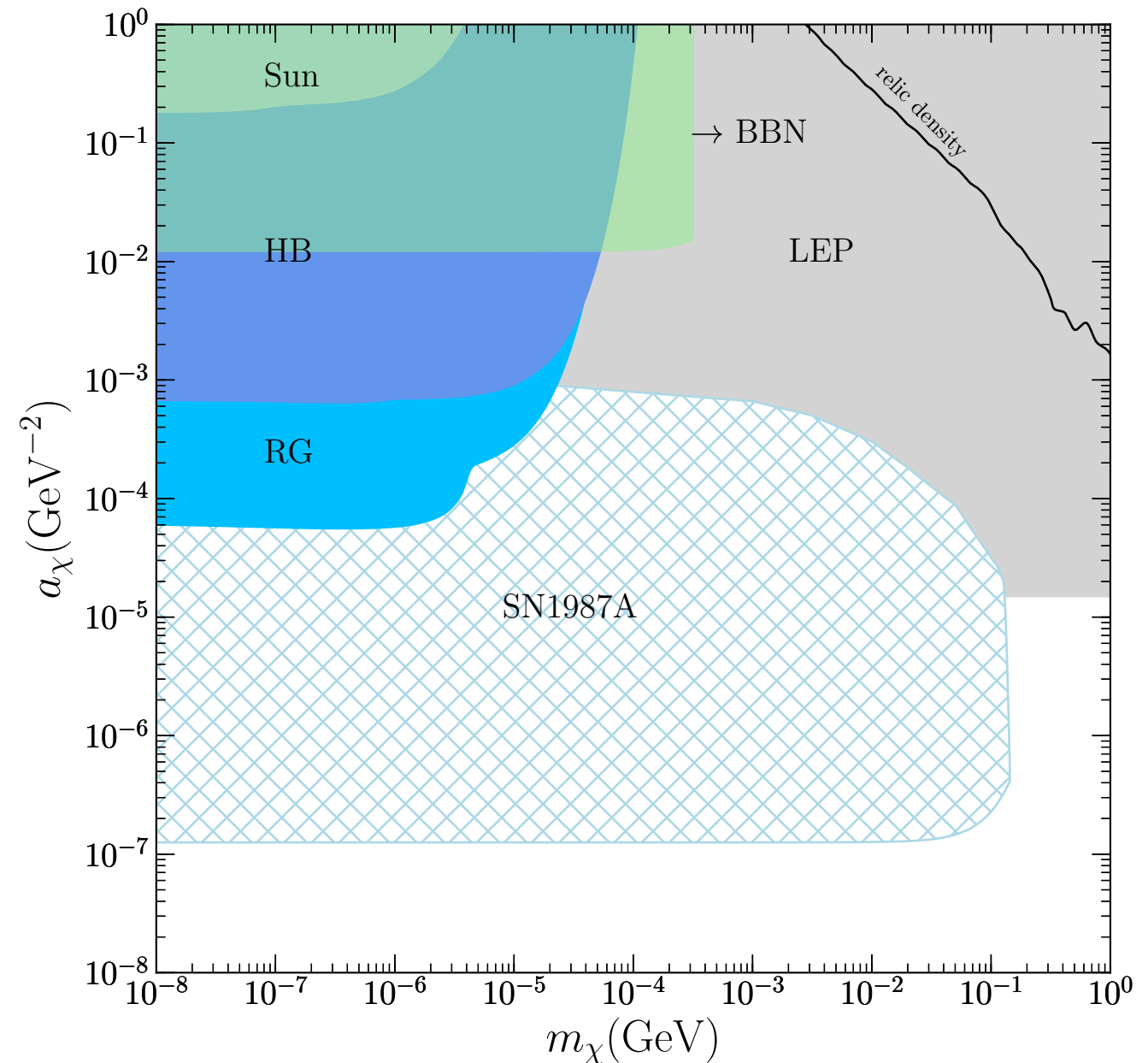
Raffelt 2001

Form-factor “landscape”

dim 5: magnetic dipole



dim 6: Anapole Moment

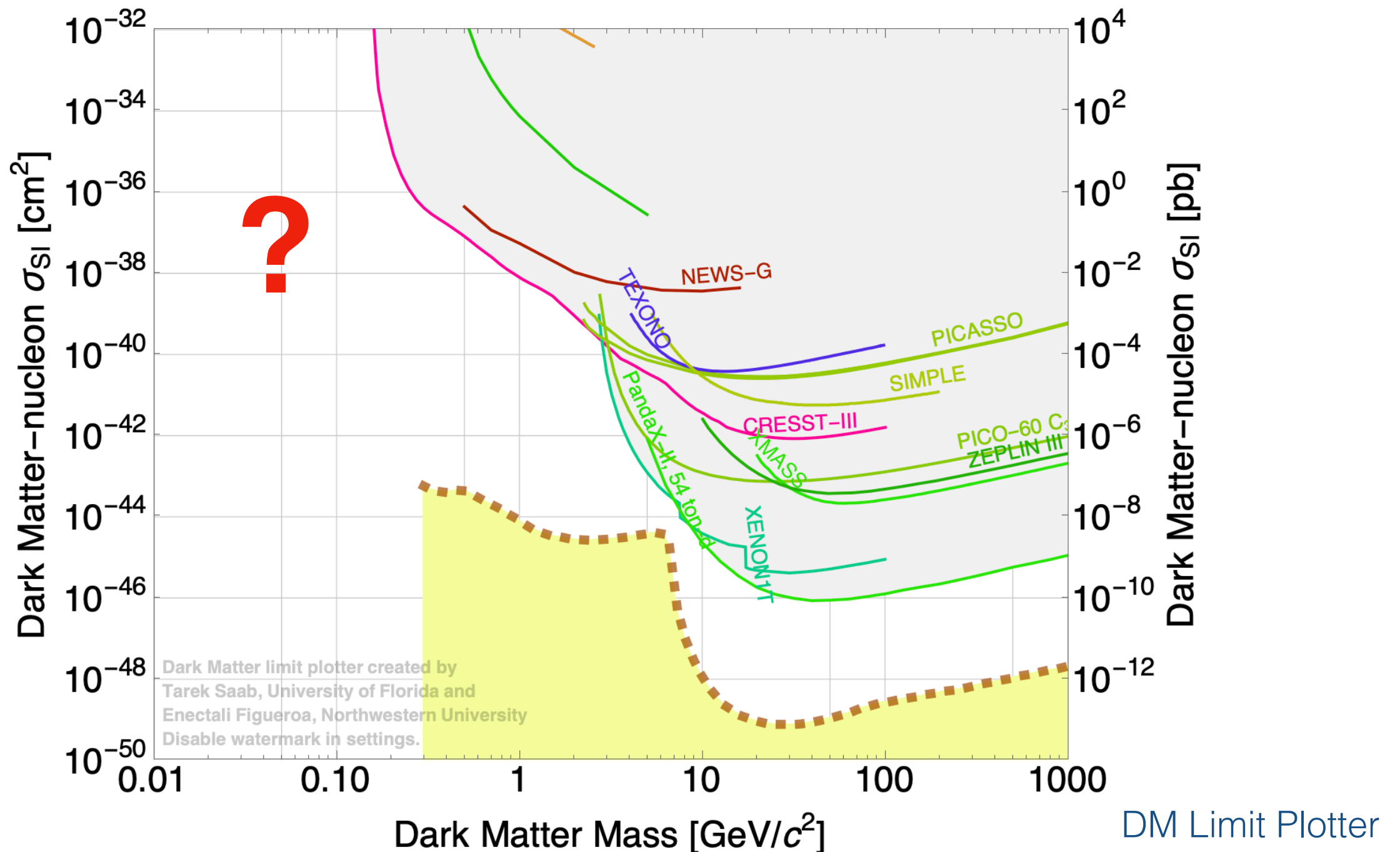


NB: for $m \rightarrow 0$ one recovers previous limits on neutrino MDM interactions [Raffelt 1990++](#)

2

Detection

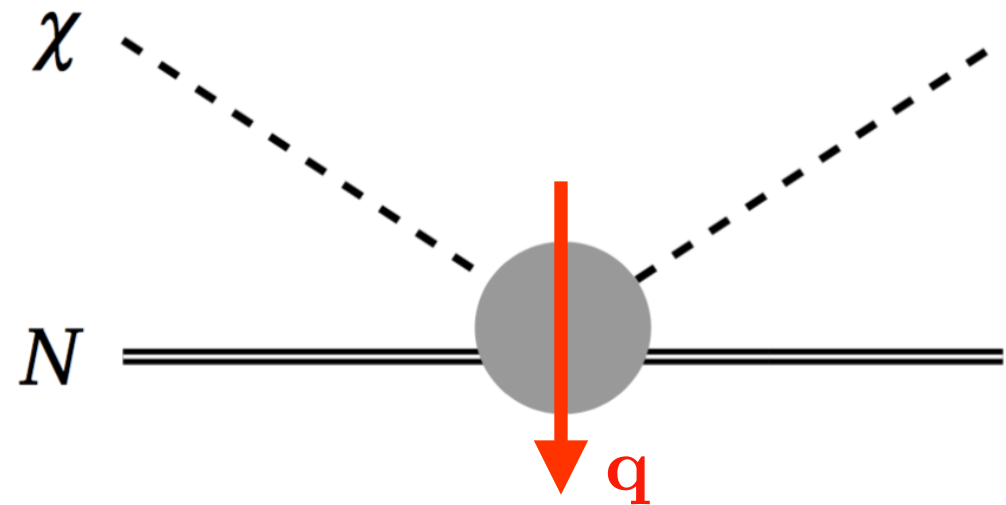
Increasing sensitivity reach of *direct detection*



Direct Detection

Nuclear kinetic recoil energy

$$E_R = \frac{\mathbf{q}^2}{2m_N} = \frac{\mu_N^2 v^2}{m_N} (1 - \cos \theta_*)$$



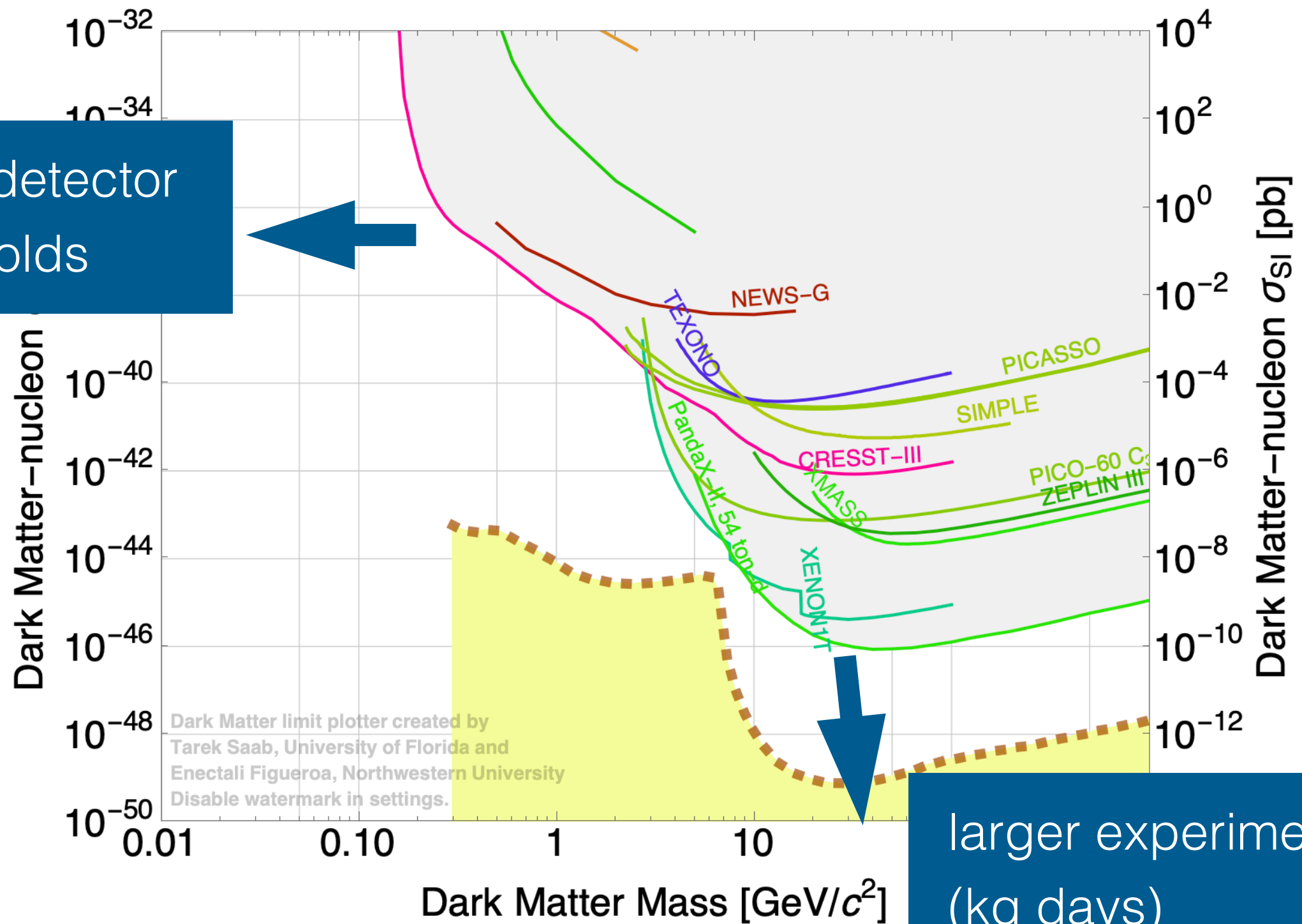
=> A given recoil, demands a *minimum* relative velocity

$$v_{\min} = \sqrt{\frac{m_N E_R}{2\mu_N^2}} \simeq \left(\frac{E_R}{0.5 \text{ keV}} \right)^{1/2} \frac{1 \text{ GeV}}{m_\chi} \times \begin{cases} 1700 \text{ km/s} & \text{Xenon} \\ 600 \text{ km/s} & \text{Oxygen} \end{cases}$$

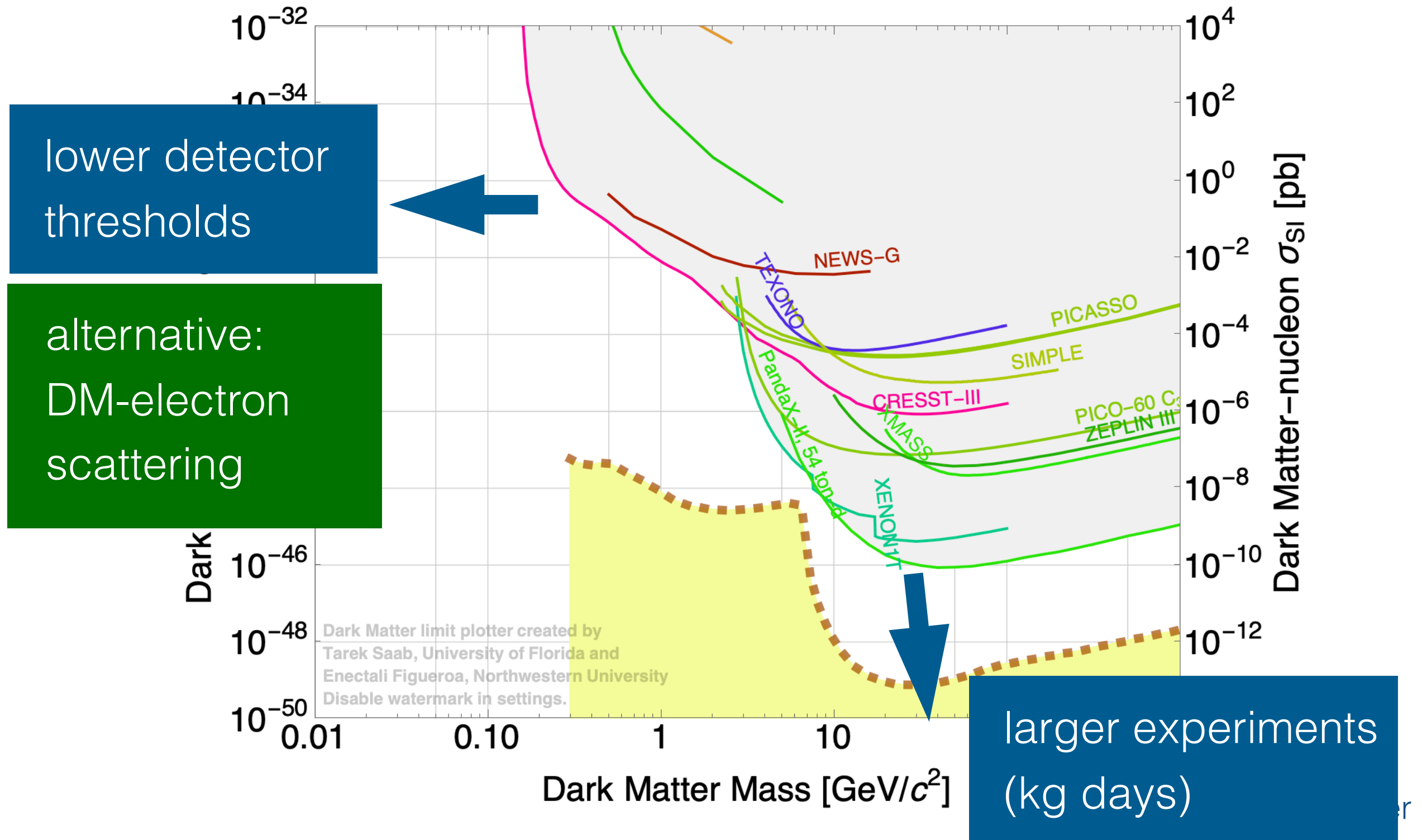
=> if $m < 1 \text{ GeV}$, then there are no particles bound to the Galaxy that could induce a 0.5 keV nuclear recoil on a Xenon atom!

“kinematical no-go theorem”

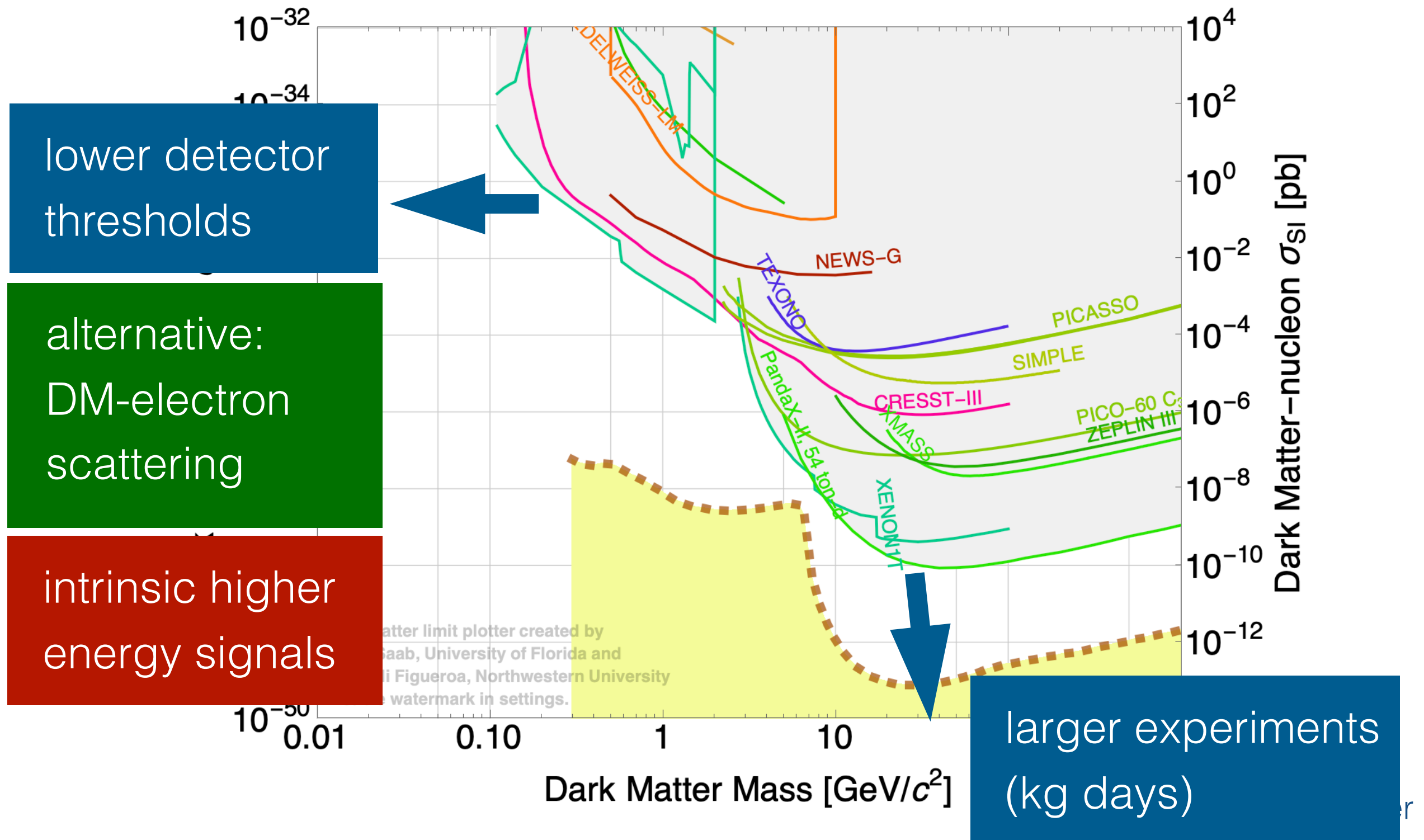
Direct detection low-mass frontier



Direct detection low-mass frontier



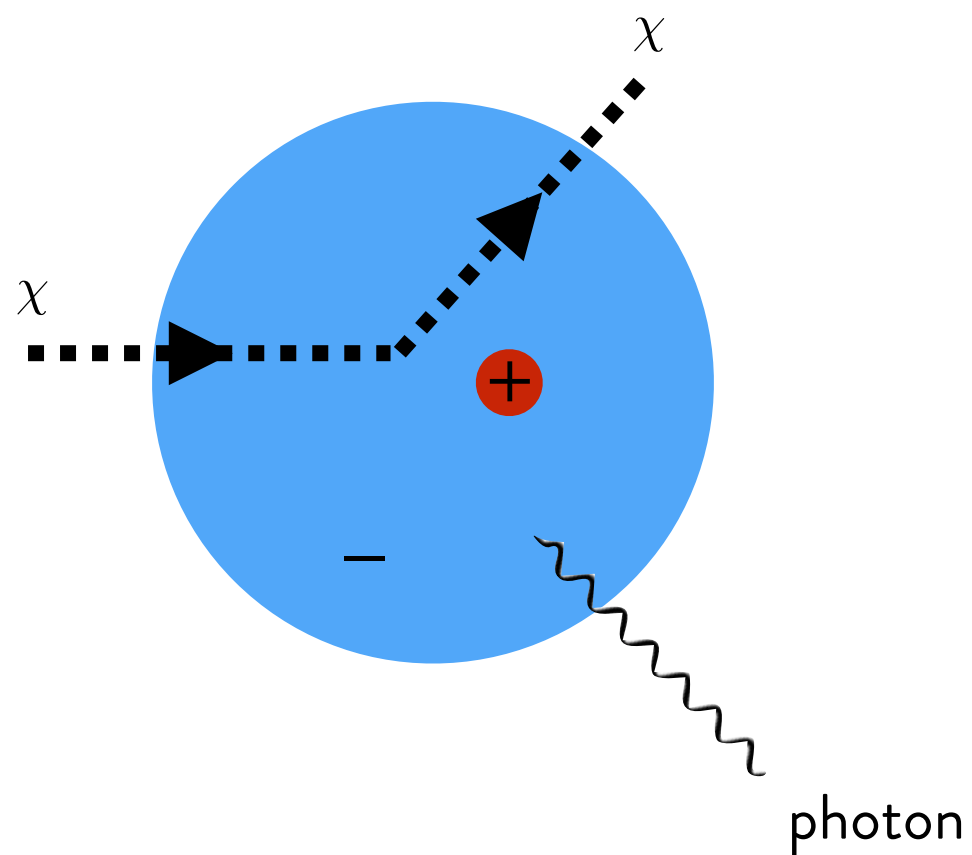
Direct detection low-mass frontier



Irreducible signal components

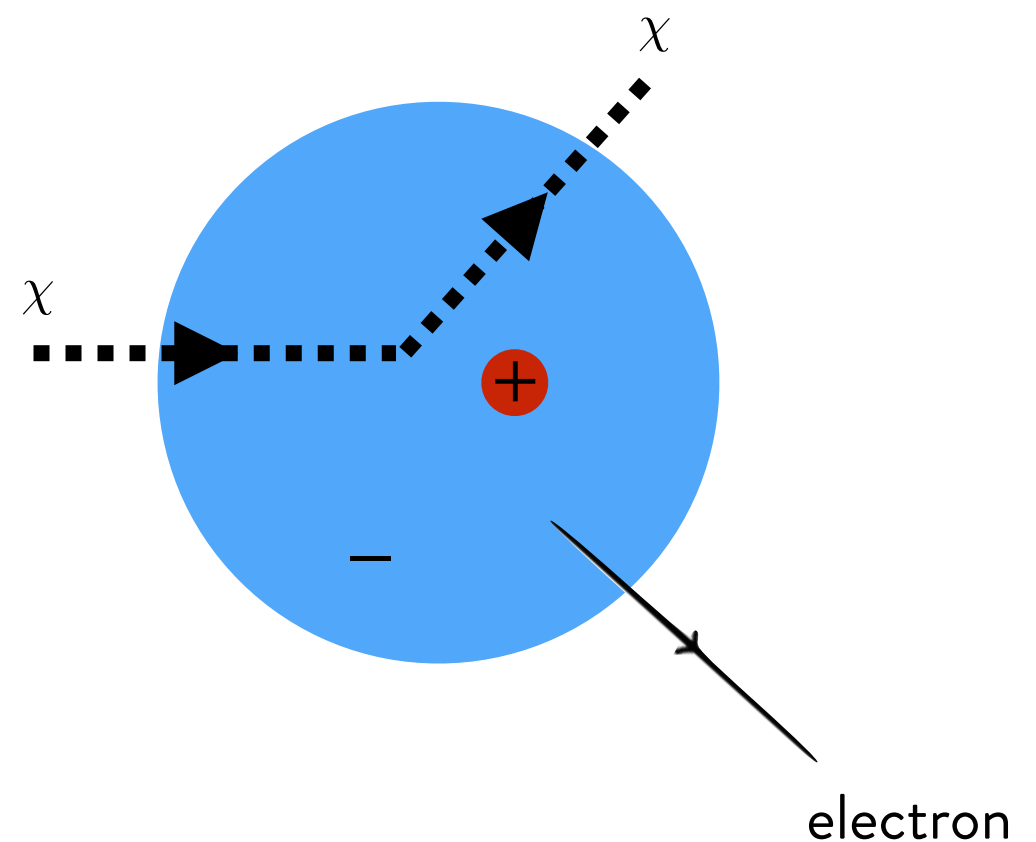
prompt atomic response following nuclear recoil

energetically favoured: entire kinetic energy can be transferred



Bremsstrahlung

Kouvaris, JP PRL 2016



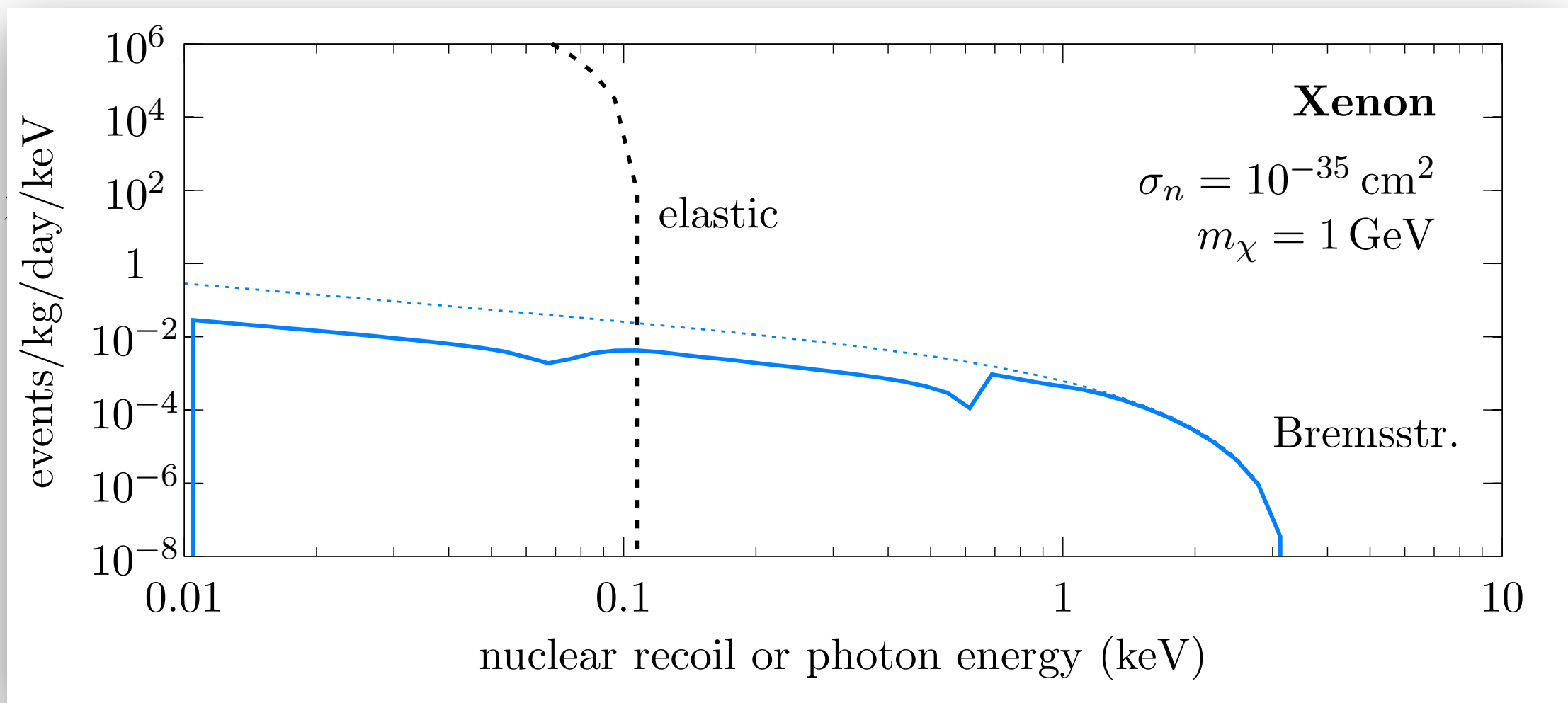
Migdal-effect

Ibe et al JCAP 2017

Irreducible signal components

prompt atomic response following nuclear recoil

energetically favoured: entire kinetic energy can be transferred



Bremsstrahlung

Migdal-effect

Relation between Migdal and DM-e

Essig, JP, Sholapurkar, Yu PRL 2020

1. Migdal effect: boost of electronic cloud relative to nucleus

$$\langle f | e^{i \frac{m_e}{m_N} \mathbf{q} \cdot \sum_{\alpha} \mathbf{x}^{(\alpha)}} | i \rangle \simeq \frac{i}{e} \frac{m_e}{m_N} \mathbf{q} \cdot \mathbf{d}_{fi} \quad (i \neq f) \quad \mathbf{v}'_N = \mathbf{q}/m_N$$

atom dipole transition element $\mathbf{d}_{fi} = \langle f | e \sum_{\alpha} \mathbf{x}^{(\alpha)} | i \rangle$

=> in single electron transitions $\mathbf{d}_{fi} \rightarrow \mathbf{d}_{fi}^{(\beta)} = \langle f | e \mathbf{x}^{(\beta)} | i \rangle$

2. DM-electron scattering

$$\langle f | e^{i \mathbf{q} \cdot \mathbf{x}^{(\beta)}} | i \rangle \simeq \frac{i}{e} \mathbf{q} \cdot \mathbf{d}_{fi}^{(\beta)} \quad (i \neq f)$$

Relation between Migdal and DM-e

Essig, JP, Sholapurkar, Yu PRL 2020

Migdal ionization probability $\left| \langle p_e, l' | e^{i \frac{m_e}{m_N} \mathbf{q} \cdot \sum_{\alpha} \mathbf{x}^{(\alpha)}} | n, l \rangle \right|^2 = \frac{1}{2\pi} \frac{dp_{nl \rightarrow E_e}(q)}{dE_e}$

Related to atomic form factor in DM-electron scattering

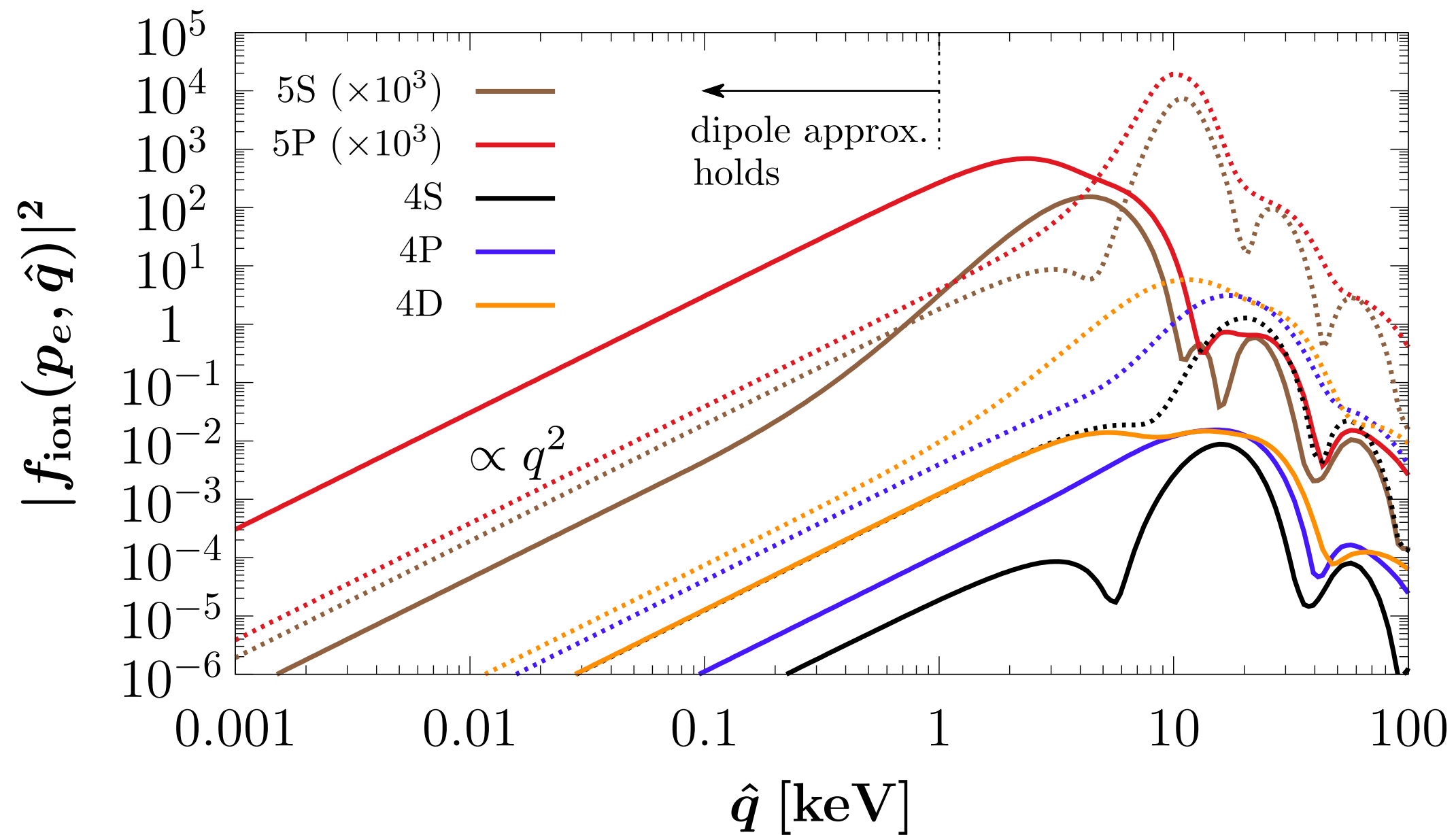
$$\frac{dp_{nl \rightarrow E_e}}{d \ln E_e} = \frac{\pi}{2} |f_{nl}^{\text{ion}}(p_e, q_e)|^2 \quad q_e \simeq \frac{m_e}{m_N} q$$

=> same underlying atomic form factor, evaluated at very different momentum scales

$$|f_{nl}^{\text{ion}}(p_e, q_e)|^2 = (\text{selection rules}) \times (\text{overlap integral})$$

$$|f_{nl}^{\text{ion}}(p_e, q_e)|^2 = \frac{4p_e}{2\pi} \sum_{L=1}^{\infty} \sum_{l'=0}^{\infty} \frac{m_l}{2} (2l' + 1)(2L + 1) \begin{pmatrix} l & l' & L \\ 0 & 0 & 0 \end{pmatrix}^2 \left| \int dr r^2 R_{p_e l'} R_{nl} j_L(q_e r) \right|^2$$

Relation between Migdal and DM-e



Migdal

DM-e

Relation between Migdal and DM-e

comparison of cross sections

Velocity average of ionization cross section

$$\frac{d\langle\sigma_{n,l}v\rangle}{dE_e} = \int_{|\vec{v}| > v_{\min}} d^3\vec{v} g_{\text{det}}(\vec{v}) \frac{d\sigma_{n,l}v}{dE_e}$$

Migdal effect ($F_N = 1$)

$$\frac{d\langle\sigma_{n,l}v\rangle}{d\ln E_e} = A^2 \frac{\bar{\sigma}_n}{8\mu_n^2} \int dq \left\{ q |F_{\text{DM}}(q)|^2 |f_{nl}^{\text{ion}}(p_e, \mathbf{q}_e)|^2 \eta[v_{\min}(q, \Delta E_{n,l})] \right\}$$

$$q_e = \frac{m_e}{m_N} q \sim \frac{10^{-3}}{A} q$$

DM-electron scattering

$$\frac{d\langle\sigma_{n,l}^{\text{DM-e}}v\rangle}{d\ln E_e} = \frac{\bar{\sigma}_e}{8\mu_e^2} \int dq \left\{ q |F_{\text{DM}}(q)|^2 |f_{nl}^{\text{ion}}(p_e, q)|^2 \eta[v_{\min}(q, \Delta E_{n,l})] \right\}$$

Relation between Migdal and DM-e

comparison of event rates

In any concrete model of DM, there is a relation between DM-nuclear and DM-electron scattering

Example: dark photon mediator

$$\bar{\sigma}_e = \frac{16\pi\varepsilon^2\alpha\alpha_D\mu_e^2}{(q_0^2 + m_V^2)^2}, \quad \bar{\sigma}_p = \frac{\mu_p^2}{\mu_e^2}\bar{\sigma}_e$$

=> ratio of differential event rates

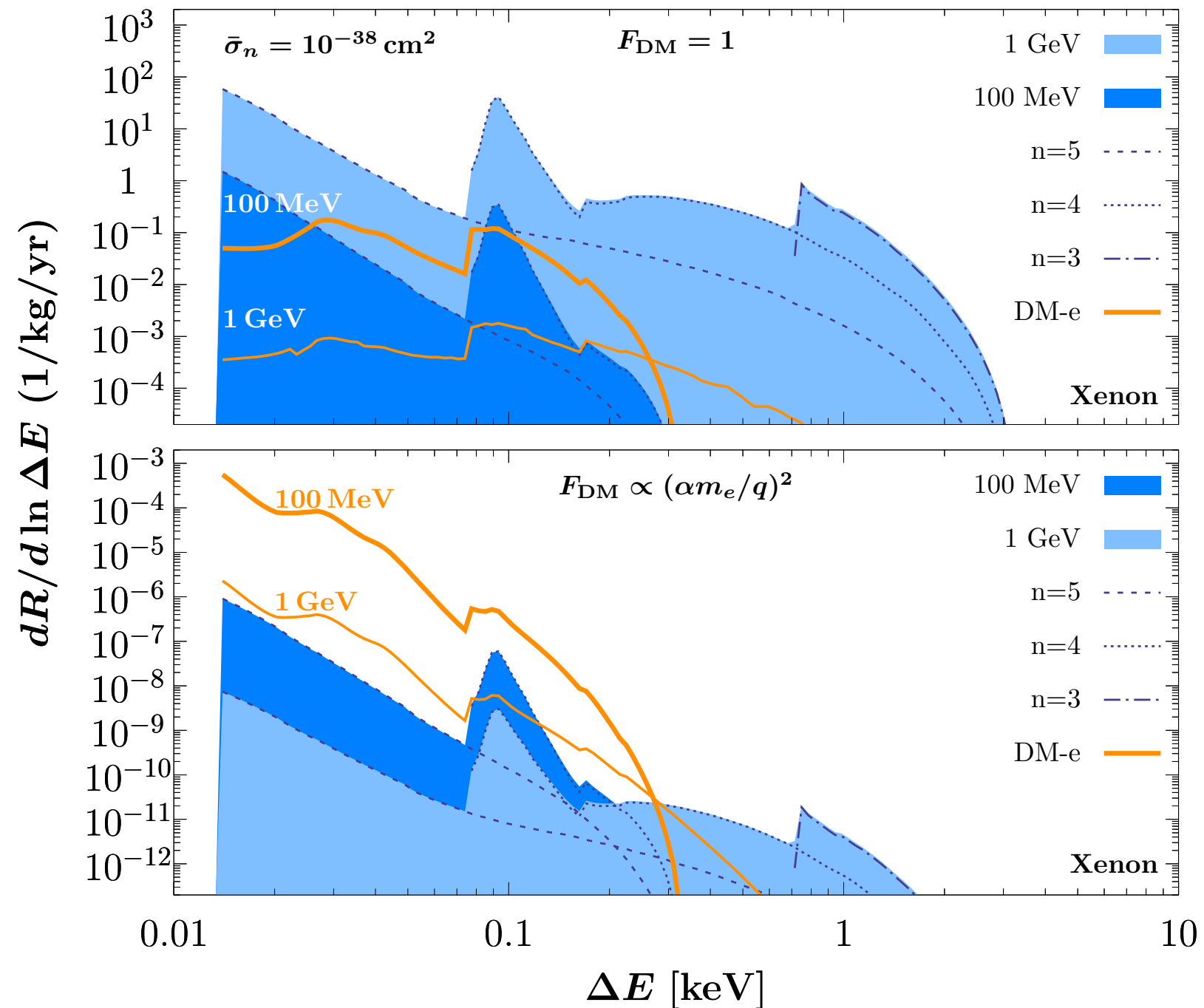
$$\frac{d\langle\sigma_{n,l}^{\text{Migdal}}v\rangle/(d\ln E_e dq)}{d\langle\sigma_{n,l}^{\text{DM-e}}v\rangle/(d\ln E_e dq)} = Z^2 \times \frac{|f_{nl}^{\text{ion}}(p_e, q_e)|^2}{|f_{nl}^{\text{ion}}(p_e, q)|^2}$$

=> naive Dipole scaling of form factors would suggest DM-e always dominant

=> because of form-factor suppression once $q > r_{\text{Electron}}$ Migdal effect dominates over DM- electron scattering for higher (GeV) mass DM

Relation between Migdal and DM-e

comparison of event rates



Migdal in semiconductors

With the relation between Migdal effect and DM-electron scattering, we may latch on to previous calculations of DM-electron scattering in **semiconductors**

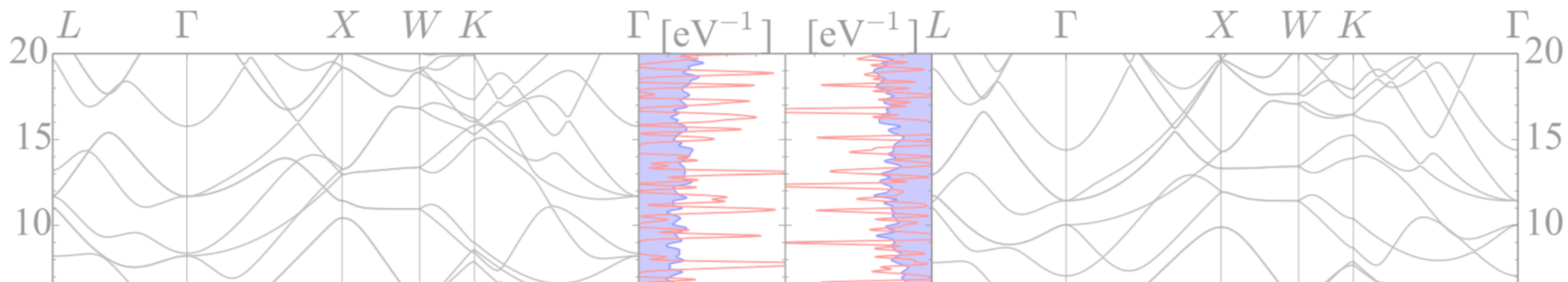
Entirely different electron structure => previous experimental Migdal papers only used inner shell ionization probabilities (e.g. Edelweiss)

$$|f_{n,l}^{\text{ion}}(q_e, E_e)|^2 \rightarrow \frac{8\alpha m_e^2 E_e}{q_e^3} \times |f_{\text{crystal}}(q_e, E_e)|^2$$

“crystal” form factor was computed using solid state tool

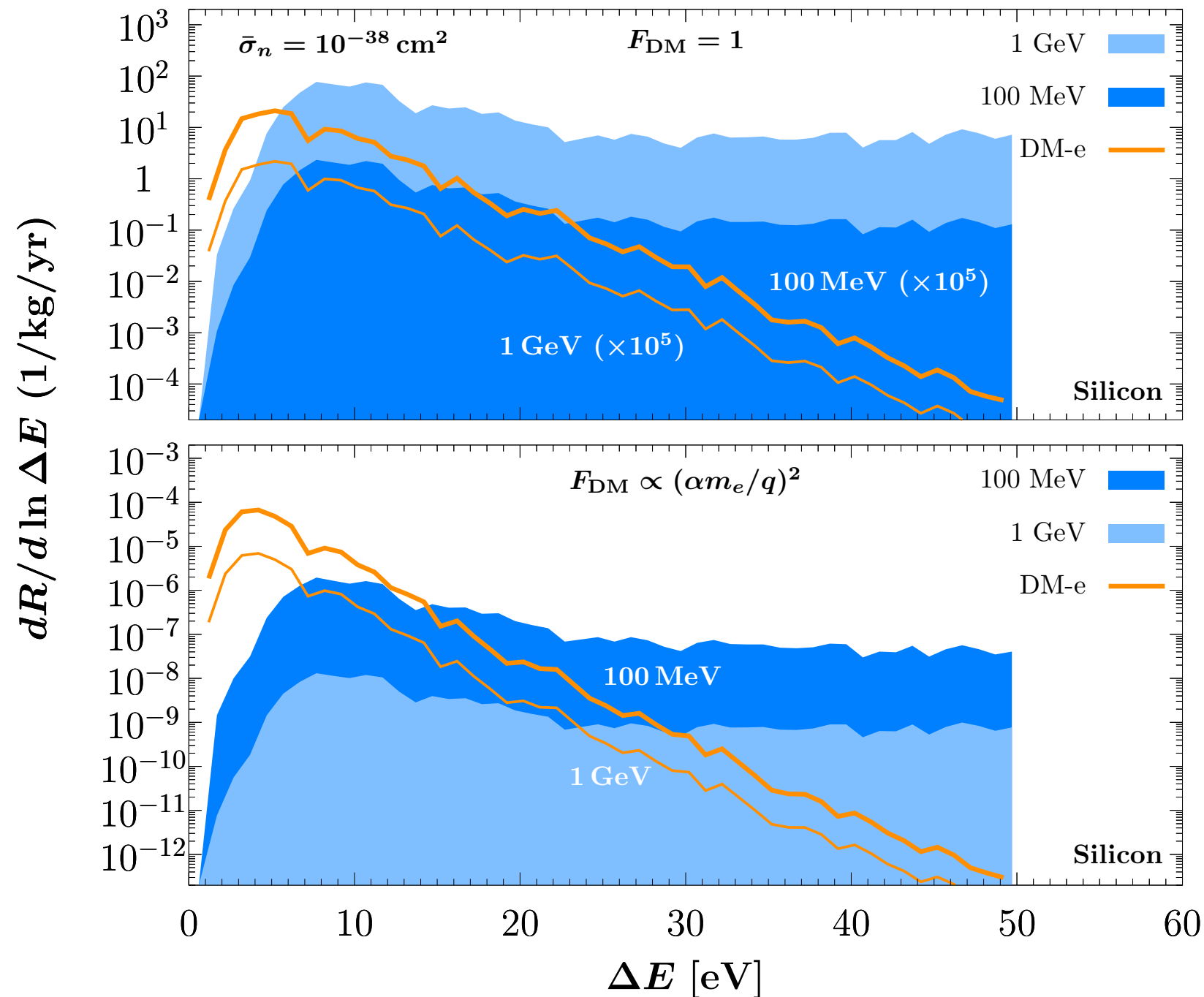
“QuantumESPRESSO” [QEDark]

Essig et al JHEP 2016;

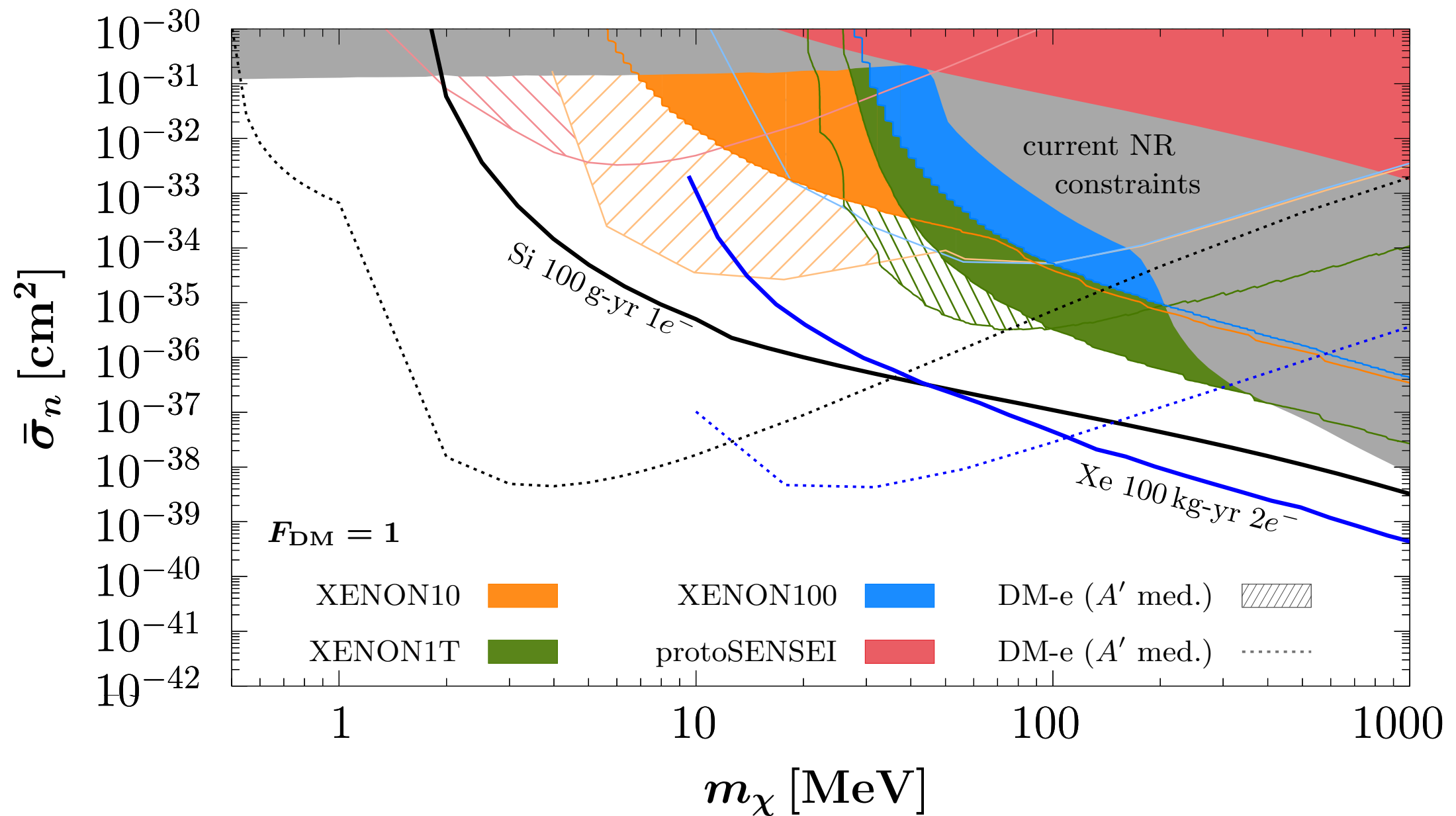


Migdal in semiconductors

=> first proof-of-principle calculation of Migdal scattering in SC



New limits and projections



1

Phenomenology of photon portal

Neutral sub-GeV dark sector particles may directly talk to the photon through electromagnetic interactions, such as magnetic and electric dipole moments, anapole moment or charge radius interactions.

We filled the associated sub-GeV dark sector “landscape”.

New “intensity frontier” science case, although high energy colliders tend to do better for higher-dimensional interactions => additional constraints from UV completion expected.

Thermal DM is excluded. Freeze-in DM is possible (UV-dependence).

Stellar physics is by far the best probe below the MeV (keV) mass scale, pointing to a UV scale of 10^9 GeV (10^7 GeV) for mass-dimension five, and 100 GeV (2.5 TeV) for mass-dimension six operators



On the direct detection of light DM

Prompt electron ionization signal that may accompany DM-nuclear scattering, “Migdal effect”, allows to extend the sensitivity of noble liquid and semiconductor DM detectors into the MeV mass region.

Theoretical description of Migdal effect closely related to DM-electron scattering. Same underlying atomic form factor, but evaluated at very different momentum scale $(m_e/m_N) q \sim 10^{-3} / A$

In a concrete model of DM, direct comparison is possible; for (heavy) dark photon mediator, Migdal dominates for GeV-scale masses and DM-e for MeV-scale masses.

Set the lowest DM-mass constraints on DM-nuclear scattering using XENON10 and XENON100 data.

First step towards a concise formulation of the Migdal effect in semiconductors.