

LOOKING INSIDE THE EARTH WITH NEUTRINOS

Sergio Palomares-Ruiz

IFIC, CSIC-U. Valencia



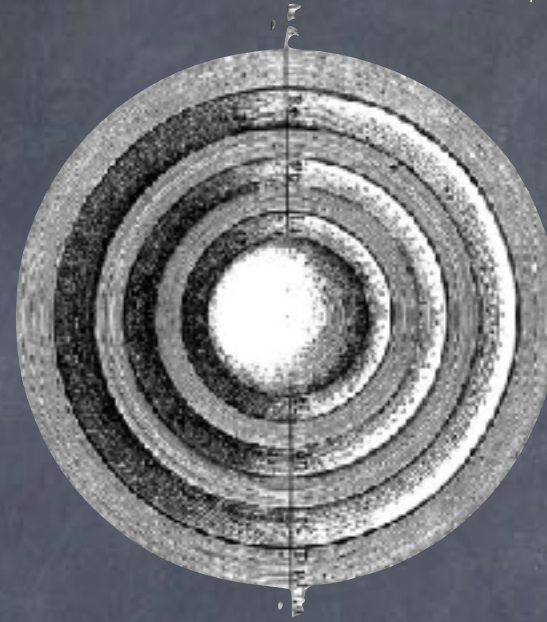
July 3, 2023



THE EARTH'S INTERIOR: EARLY (CRAZY) IDEAS

First hypothesis based on observations: Hollow Earth

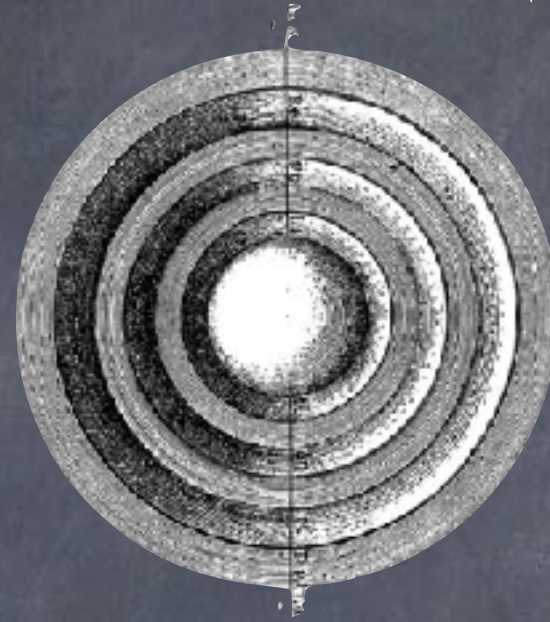
E. Halley, 1692



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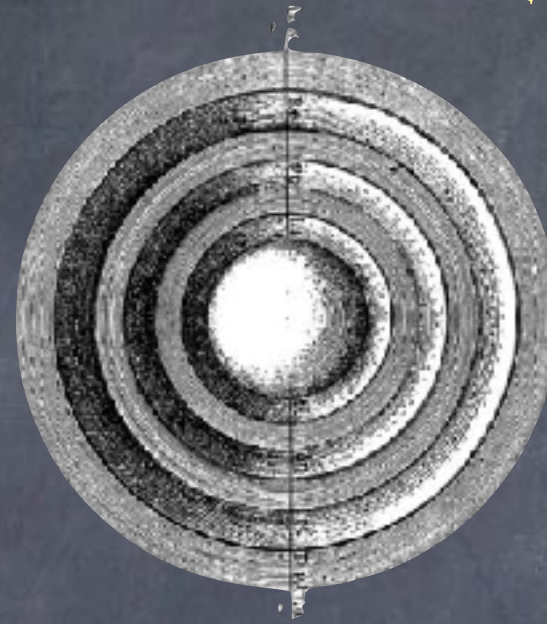


disproven by N. Maskelyne in 1774...

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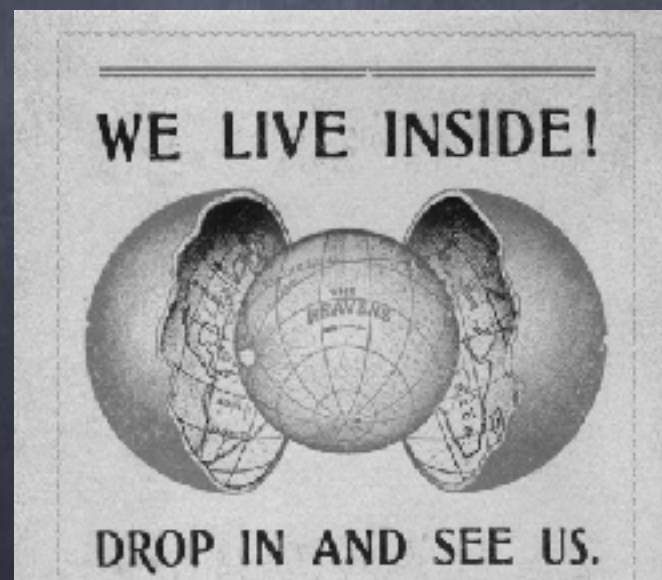


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... but then even crazier ideas...



J. C. Symmes, 1818

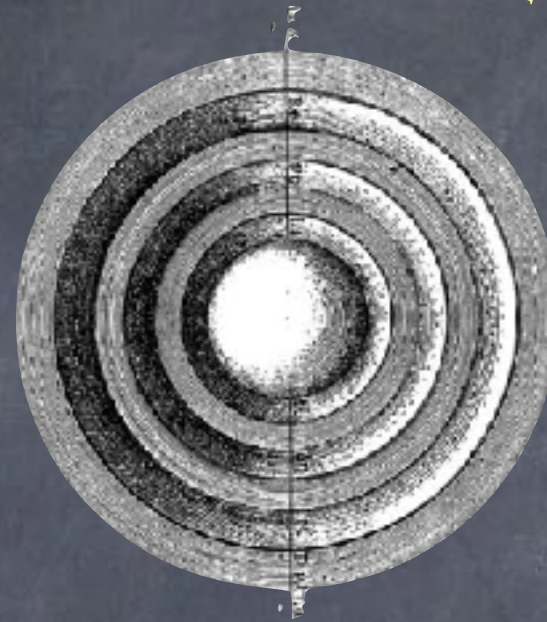


C. R. Teed, 1869

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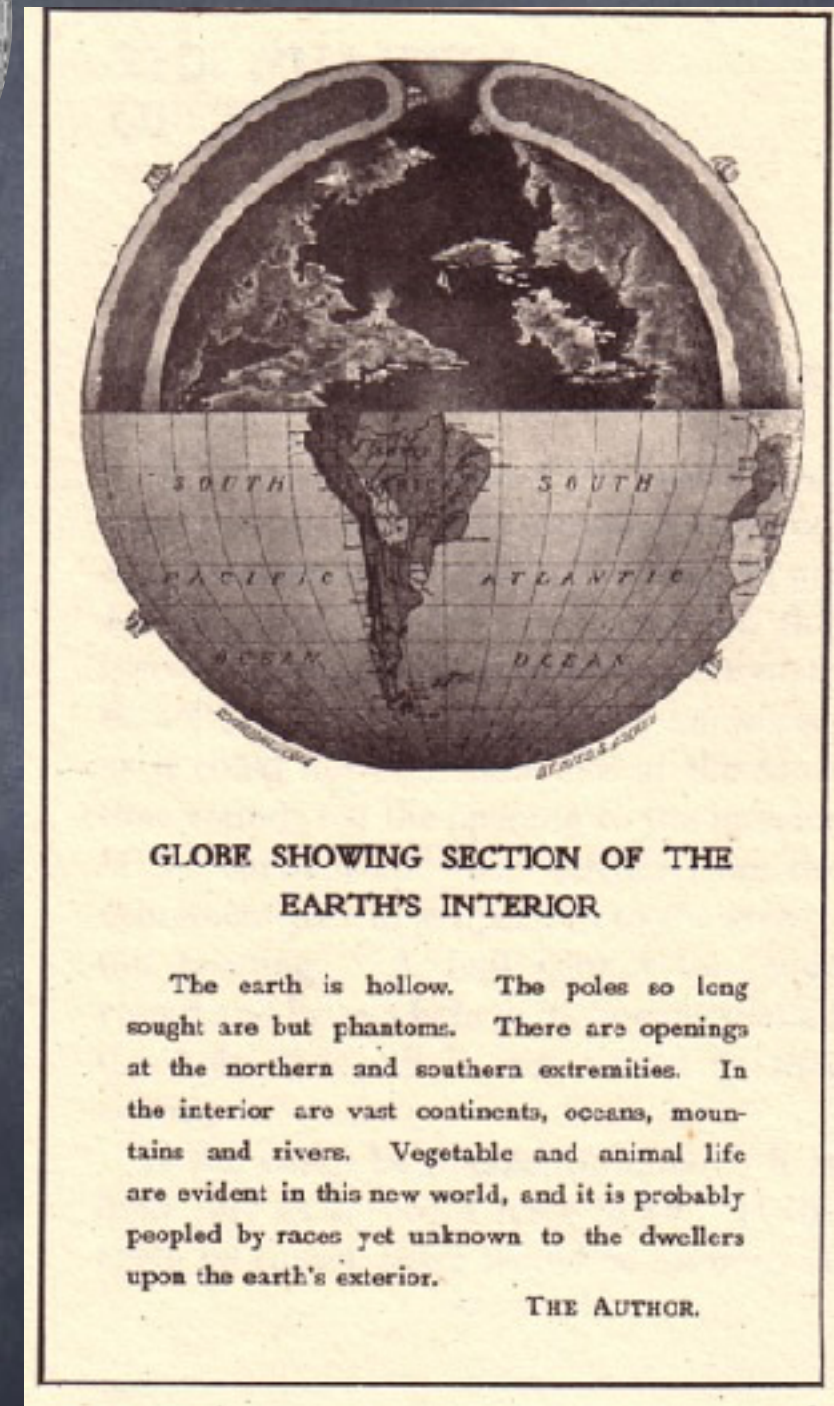
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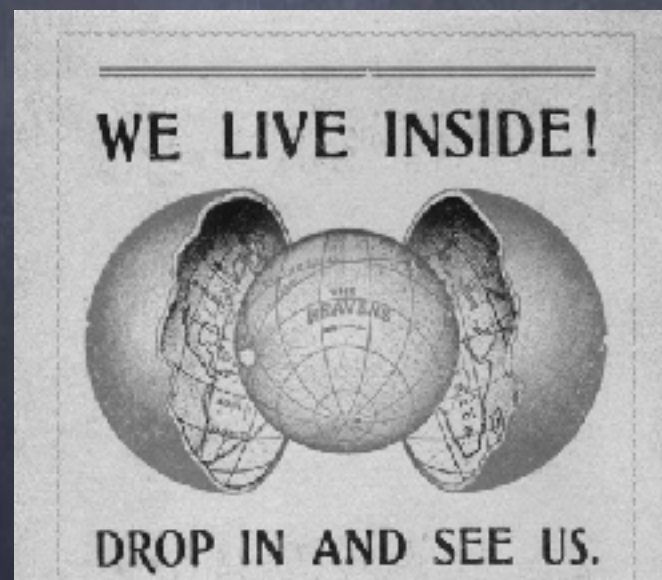


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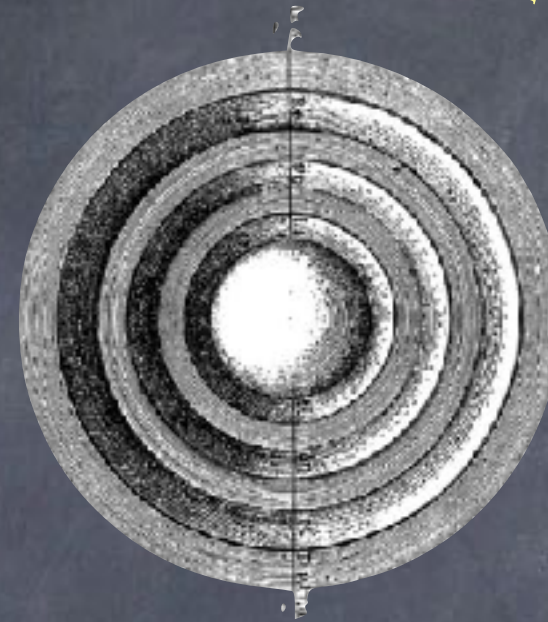
W. Reed, The phantom of the poles, 1906

Looking inside the Earth with neutrinos

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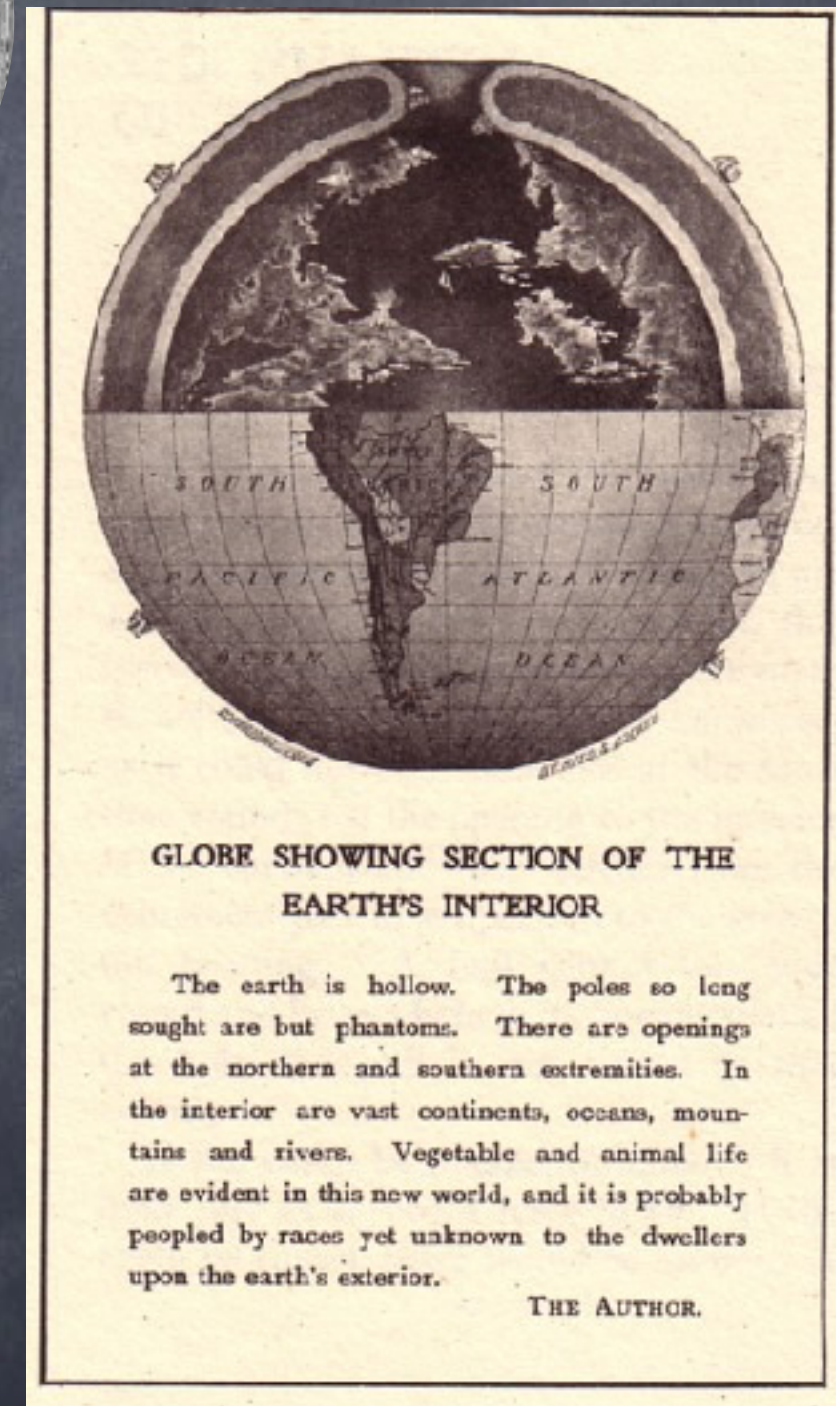
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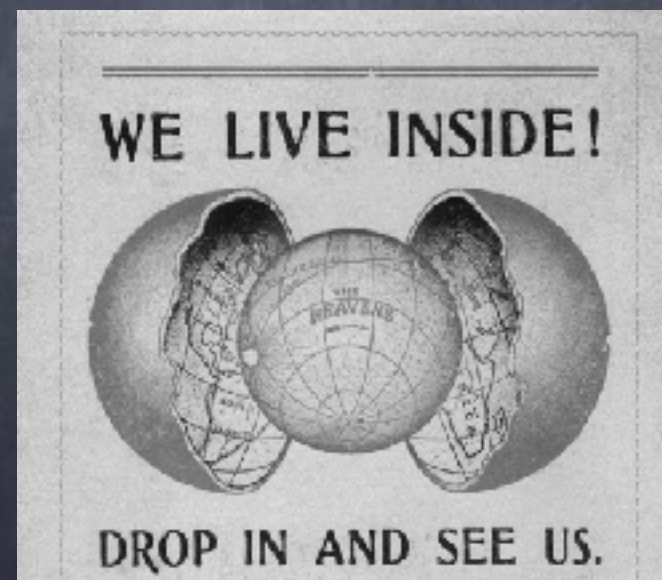


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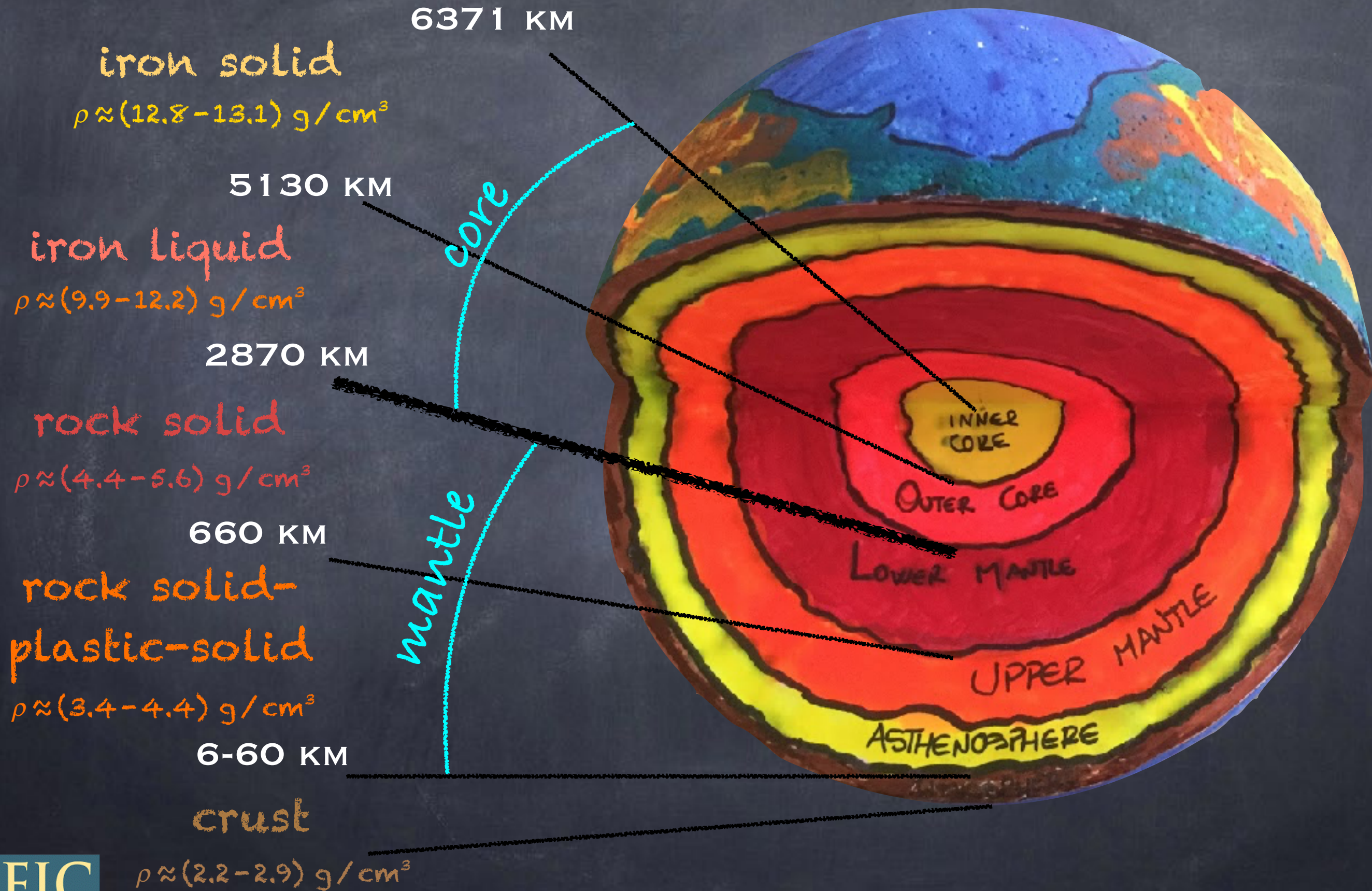


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Looking inside the Earth with neutrinos

THE EARTH'S INTERIOR: THE MODERN VIEW



THE EARTH'S INTERIOR: HOW IS IT INFERRED?

Earthquakes:

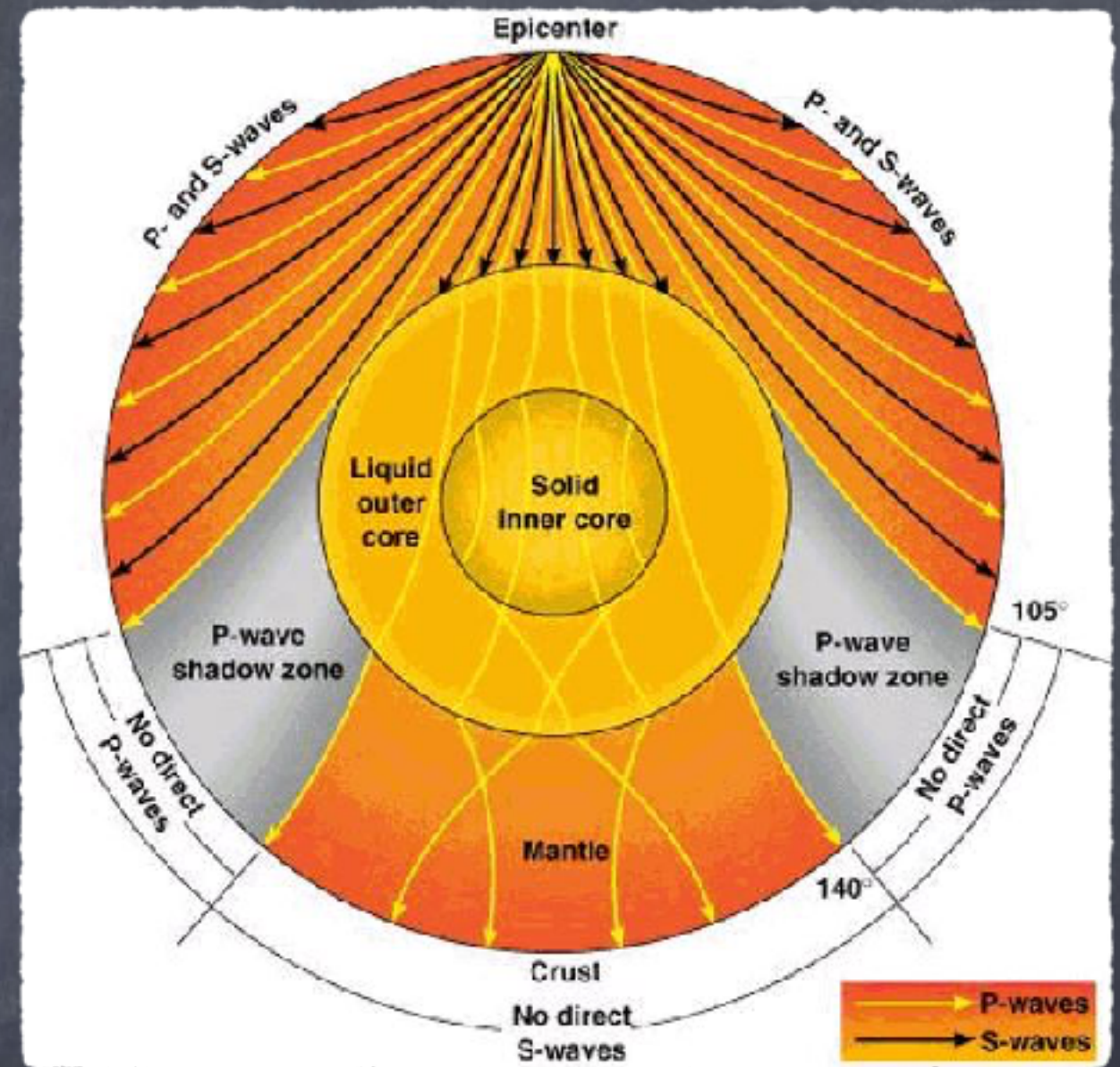
$O(100/\text{yr})$ with magnitude > 6
Shaking and trembling of Earth's surface caused by sudden release of stress within the crust

Seismic waves:

P-waves \rightarrow compressional: travel through liquids and solids

S-waves \rightarrow shear: travel through solids only

propagation depends on composition, temperature and pressure



THE EARTH'S MASS AND MOMENT OF INERTIA: GRAVITATIONAL MEASUREMENTS

GM: satellite laser ranging (SLR)

Measures the gravity field

$$GM = 3.986004418(4) \times 10^{14} \text{ m}^3 \text{ s}^{-2}$$

J. C. Ries, Geophys. Res. Abs. 9:10809, 2007

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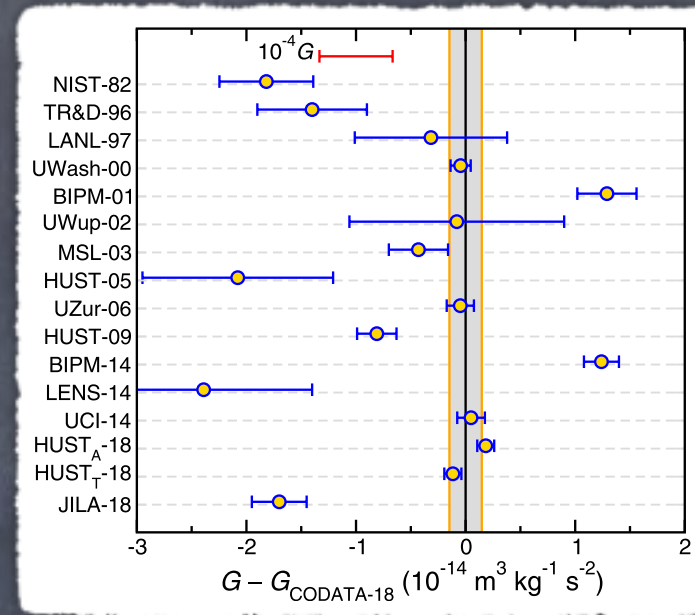
J. C. Ries, Geophys. Res. Abs. 9:10809, 2007

Measures the gravity field

G: variations of the
Cavendish experiment

$$G = 6.67430(15) \times 10^{-11} \text{ kg}^{-1} \text{ m}^3 \text{ s}^{-2}$$

E. Tiesinga, P. J. Mohr, D. B. Newell and B. N. Taylor, CODATA-2018, Rev. Mod. Phys. 93:025010, 2021



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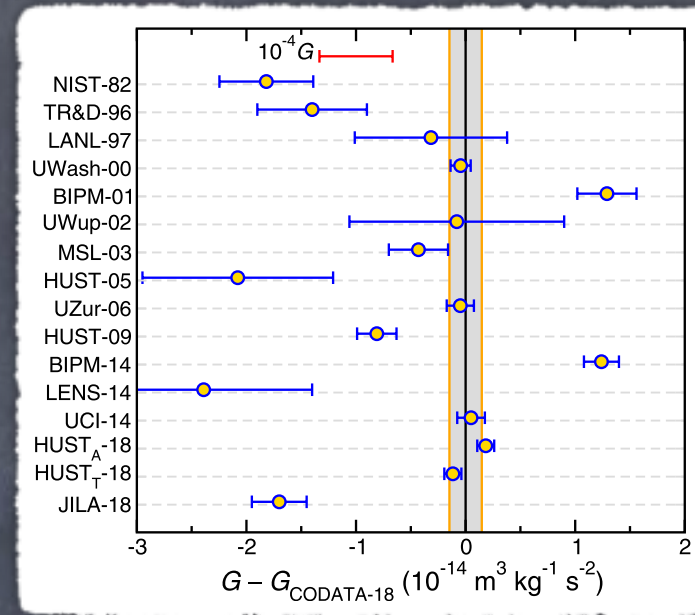
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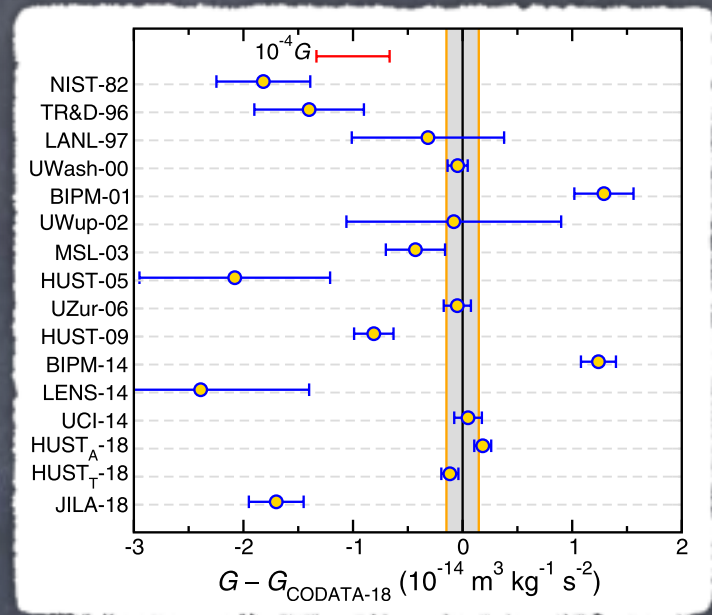
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Earth gravity model:
terrestrial, altimetry-derived
and airborne gravity data

$$I = 8.01736(96) \times 10^{37} \text{ kg m}^2$$

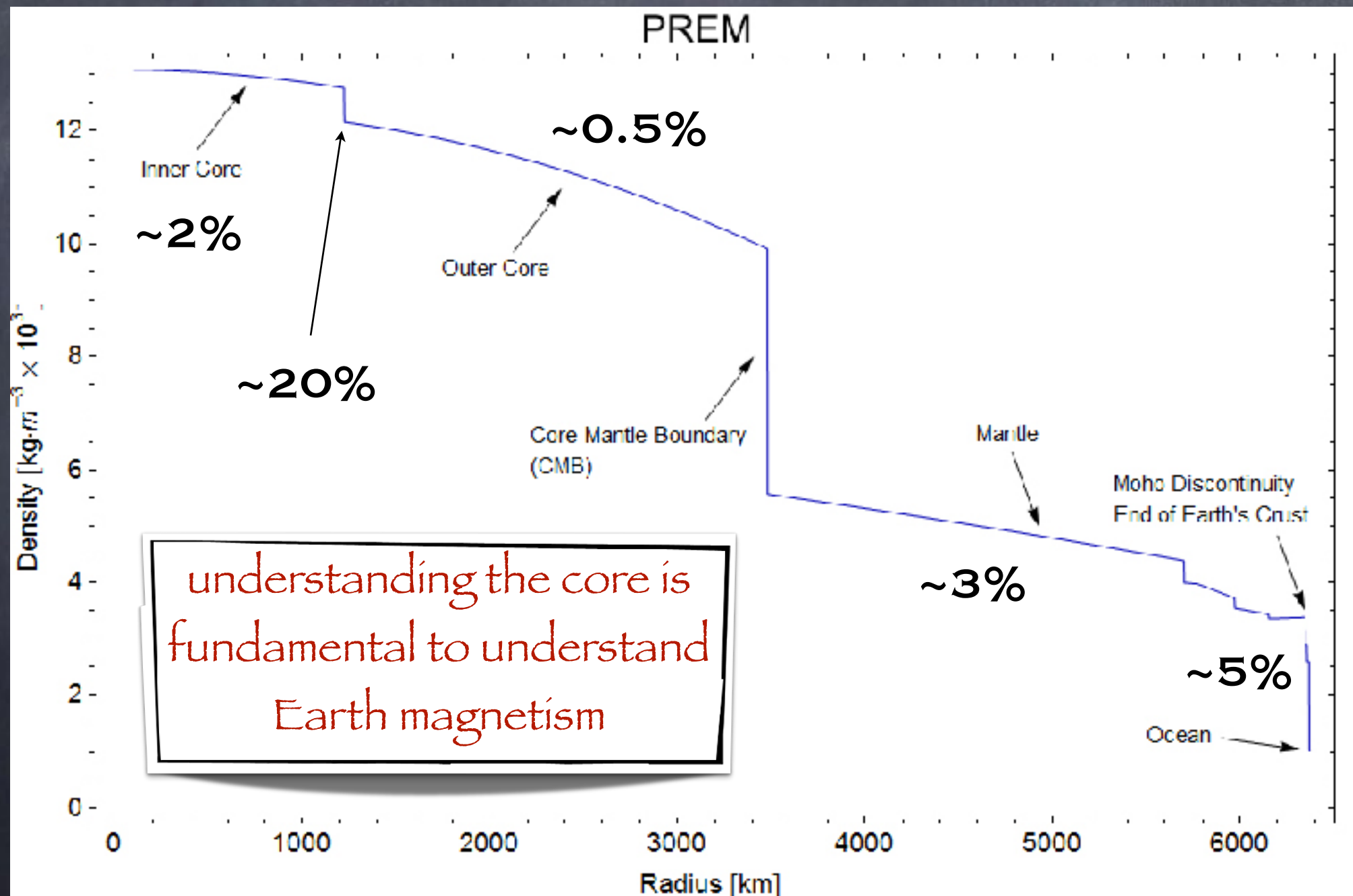
W. Chen et al., J. Geod. 89:179, 2015

PRELIMINARY REFERENCE EARTH MODEL (PREM)

A. M. Dziewonski and D. L. Anderson, Phys, Earth Planet. Inter. 25:297, 1981

1-D density profile

From seismic wave data and imposing the Earth's radius, mass and moment of inertia as additional constraints



Is there any other way to study the Earth's internal structure beyond seismic waves and gravitational measurements?

Is there any other way to study the Earth's internal structure beyond seismic waves and gravitational measurements?

Yes!

Weak interactions: Neutrinos!

DIFFERENT WAYS TO STUDY THE EARTH'S INTERIOR WITH NEUTRINOS

Detecting neutrinos produced inside the Earth

Searching for distortions on the spectra of (external) neutrino fluxes

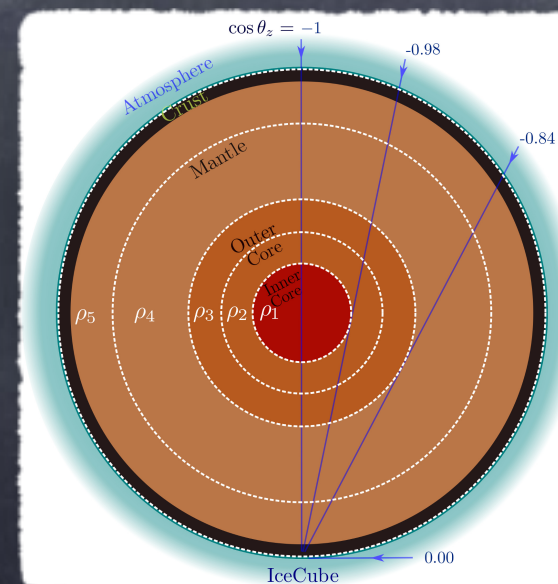
Geoneutrinos: produced by the decay of radioactive isotopes inside the Earth, sensitive to the heat power of the Earth

Neutrino tomography: inelastic scattering (absorption) or elastic forward scattering (refraction), sensitive to the Earth's density profile (and, although technologically unfeasible, neutrino diffraction)



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first proposed by G. Eder in 1965
first detected by KamLAND in 2005

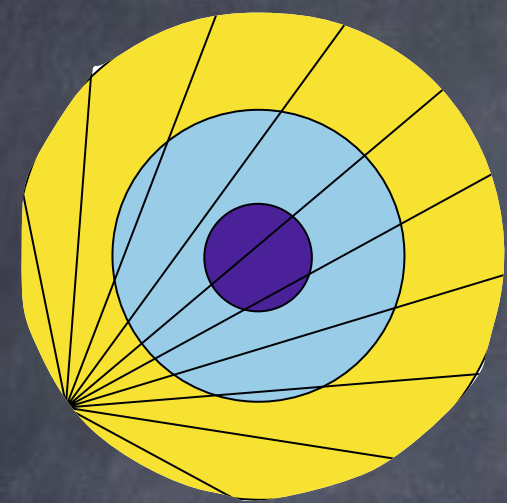


first proposed in a CERN report in October 1973 and also in a talk in 1974

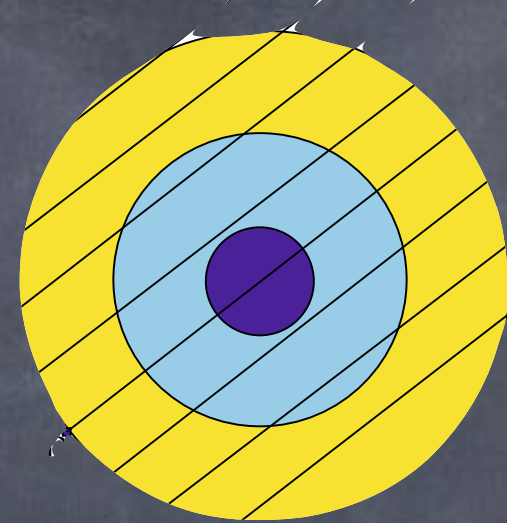
first performed in 2018 (with IceCube data)

NEUTRINO EARTH TOMOGRAPHY: APPROACHES

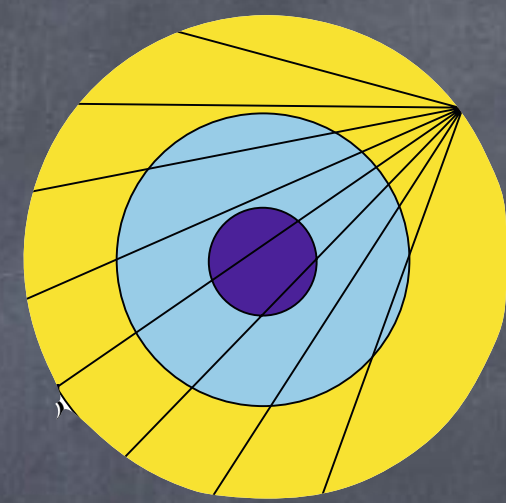
(quasi) isotropic flux



neutrino beam



astrophysical point source



oscillation tomography

absorption tomography

Coherent effect in neutrino propagation

Incoherent effect in neutrino propagation

$$E_\nu < 100 \text{ GeV}$$

$$E_\nu > \text{TeV}$$

sensitive to electron density

sensitive to nucleon density

Neutrino oscillations in matter:
extra effective potential in the hamiltonian

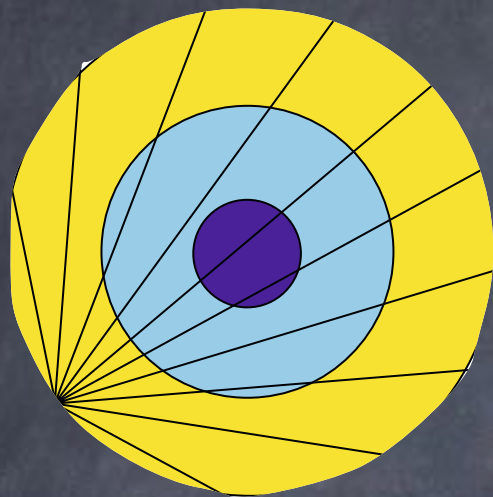
$$\frac{d\phi_\nu(E_\nu, x)}{dx} \approx -n(x) \sigma(E_\nu) \phi_\nu(E_\nu, x)$$

distortion of the energy and angular spectrum per flavor, but the total neutrino flux remains unaffected

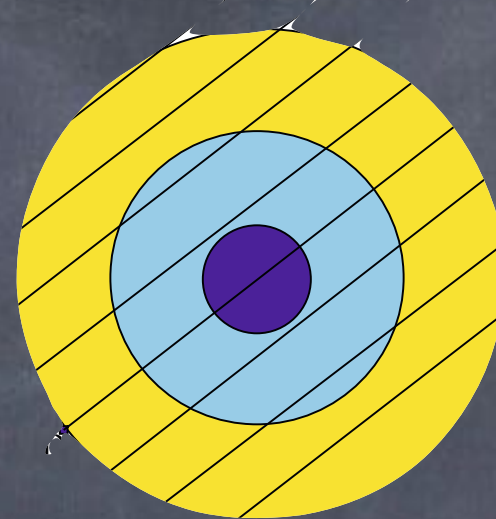
absorption of the flux depending on direction
(traversed column density) and energy

NEUTRINO EARTH TOMOGRAPHY: APPROACHES

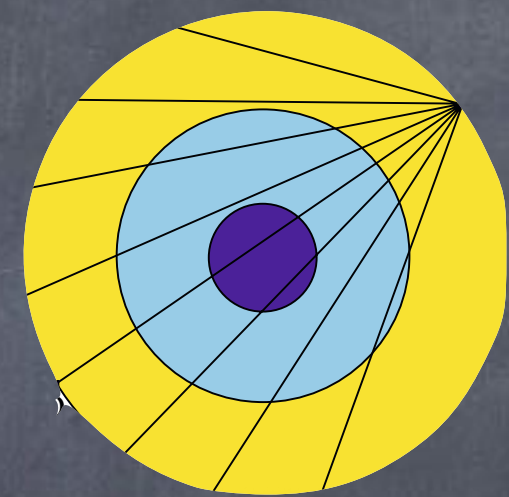
(quasi) isotropic flux



neutrino beam



astrophysical point source



oscillation tomography

absorption tomography

Atmospheric neutrinos

S. K. Agarwalla, T. Lí, O. Mena and SPR, arXiv:1212.2238

Man-made beams

V. K. Ermilova, V. A. Tsarev and V. A. Chechin, JETP Lett. 43:453, 1986

Solar neutrinos

A. N. Ioanissian and A. Smirnov, hep-ph/0201012

Supernova neutrinos

M. Lindner, T. Ohlsson, R. Tomàs and W. Winter, Astropart. Phys. 19:755, 2003

Cosmic neutrinos (diffuse flux)

P. Jaín, J. P. Ralston and G. M. Frichter, Astropart. Phys. 12:193, 1999

Atmospheric neutrinos

M. C. González-García, F. Halzen, M. Maltoni and H. K. M. Tanaka, Phys. Rev. Lett. 100:061802, 2008

Man-made beams

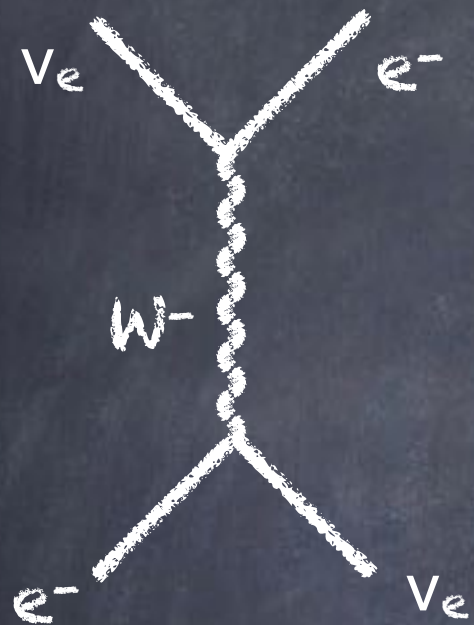
A. Placci and E. Zavattini, CERN report 1973... but never published
L. V. Volkova and G. T. Zatsepin, Izv. Nauk Ser. Fiz. 38N5:1060, 1974

Cosmic neutrinos (point sources)

T. L. Wilson, Nature 309:38, 1984

NEUTRINO EARTH TOMOGRAPHY: MATTER EFFECTS

Propagation through matter induces a phase in the neutrino wave function



index of refraction



$$\text{Amplitude} = e^{iEnL}$$

$$n = 1 + 2\pi N f(0) / E^2 = 1 + V/E$$

coherent forward scattering

incoherent process

$$E \operatorname{Re}(\Delta n) \propto N \operatorname{Re} f(0) / E$$

optical theorem $[4\pi \operatorname{Im} f(0) / E = \sigma]$

Absorption: $E \operatorname{Im}(\Delta n) \propto N \sigma$

$$\operatorname{Re} f(0) \propto G_F$$

$$\sigma \propto G_F^2$$

NEUTRINO MATTER EFFECTS

tiny Δn : a matter of scales

coherent forward scattering

$$\frac{\Delta m_{21}^2}{4\pi E_\nu (100 \text{ MeV})} \sim \frac{\Delta m_{31}^2}{4\pi E_\nu (\text{GeV})} \sim V_\oplus \sim R_\oplus^{-1}$$

absorption

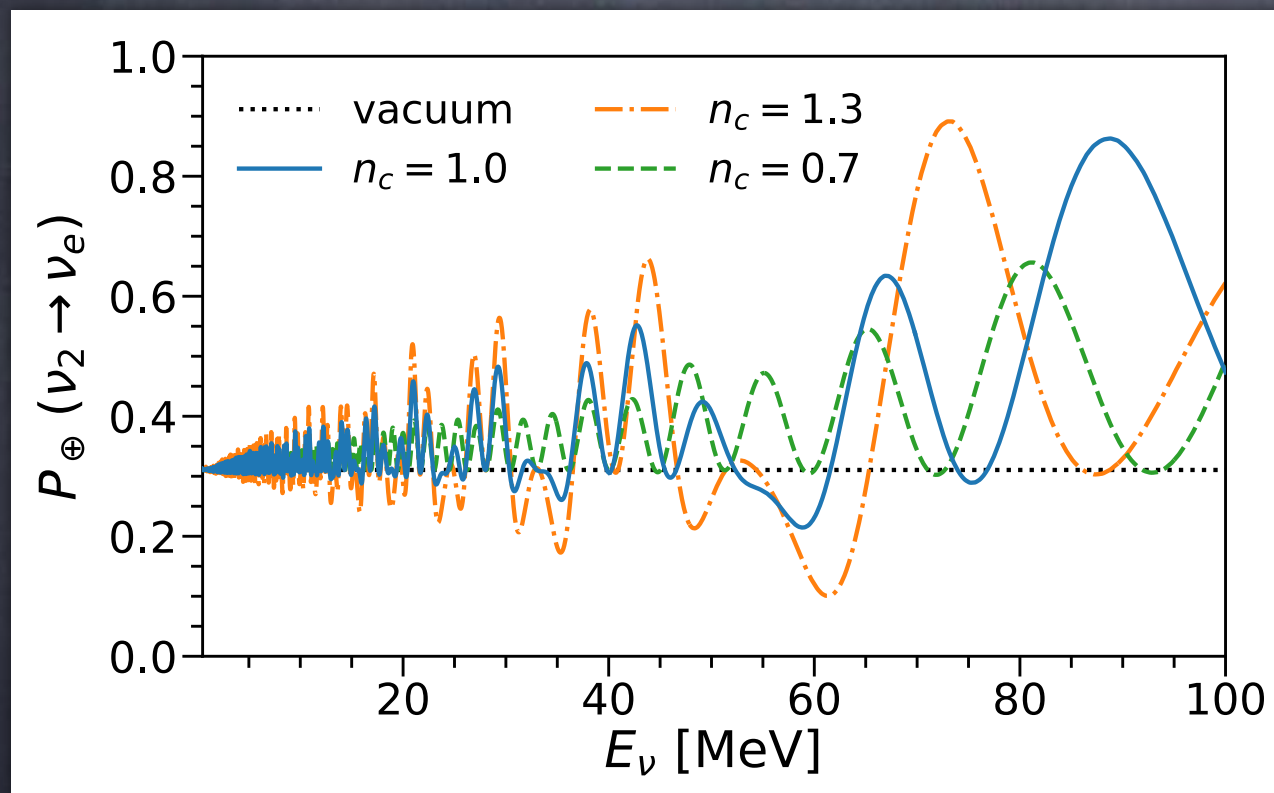
$$\sigma \sim \frac{G_F^2 s}{\pi} \sim 10^{-38} \left(\frac{E_\nu}{\text{GeV}} \right) \text{ cm}^2 \quad n\sigma \sim \left(\frac{E_\nu}{40 \text{ TeV}} \right) R_\oplus^{-1}$$

NEUTRINO OSCILLATION TOMOGRAPHY

3-neutrino problem simplifies to 2-neutrino problem as the two mass-square differences are separated

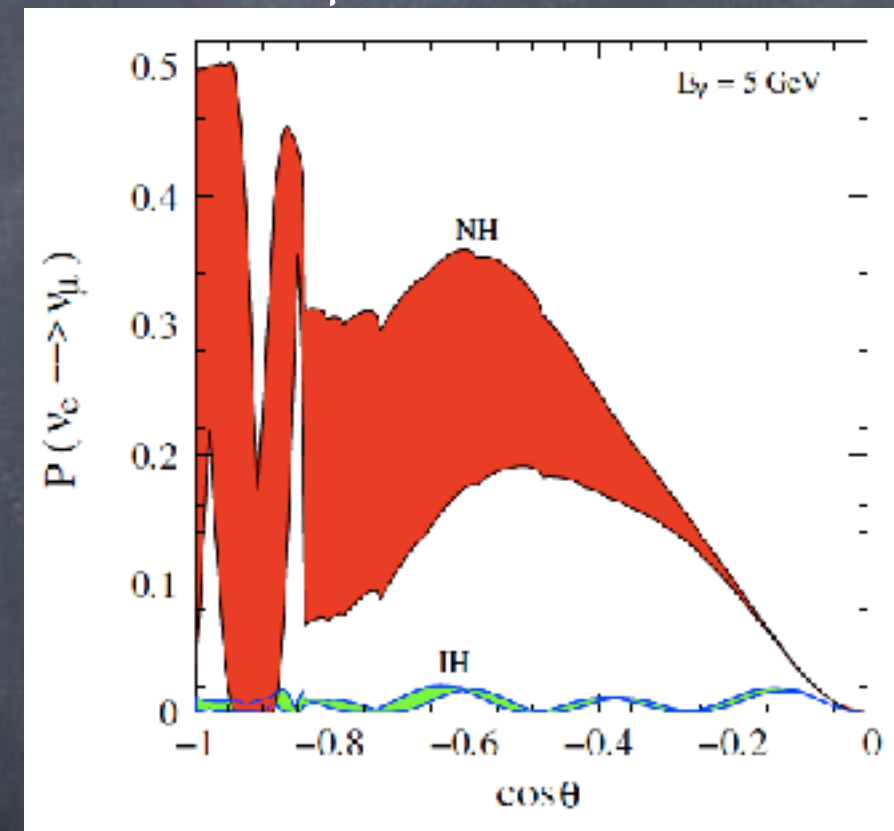
T. K. Kuo and J. Pantaleone, Phys. Rev. Lett. 57:1805, 1986

Δm_{21}^2 – driven matter effect
(solar and supernova neutrinos)



R. Hajjar, O. Mena and SPR, arXiv:2303.09369

Δm_{31}^2 – driven matter effect
(atmospheric neutrinos)

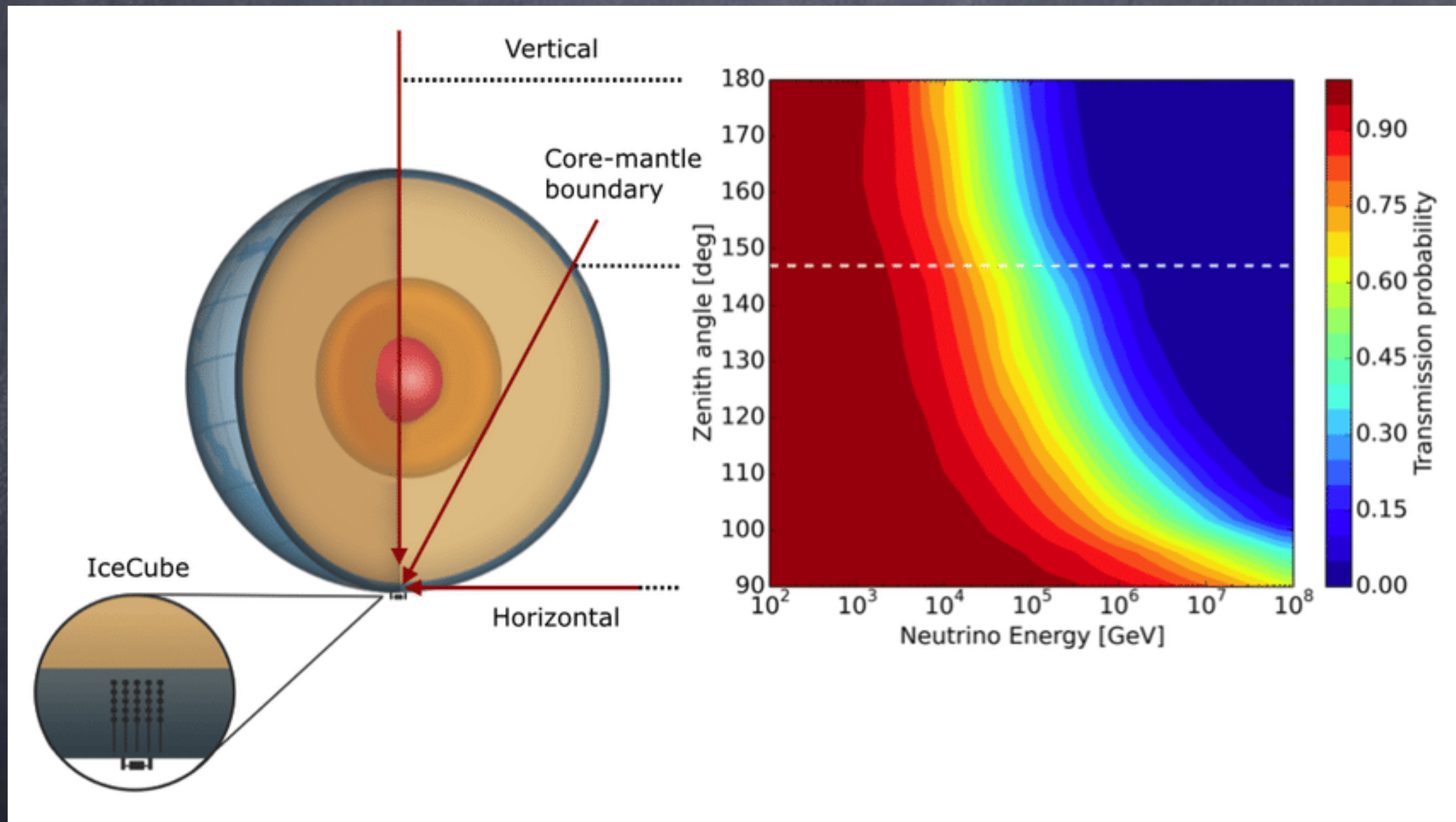


S. K. Agarwalla, T. Li, O. Mena and SPR, arXiv:1212.2238

Matter effect can be resonant for different directions and energies

NEUTRINO ABSORPTION TOMOGRAPHY

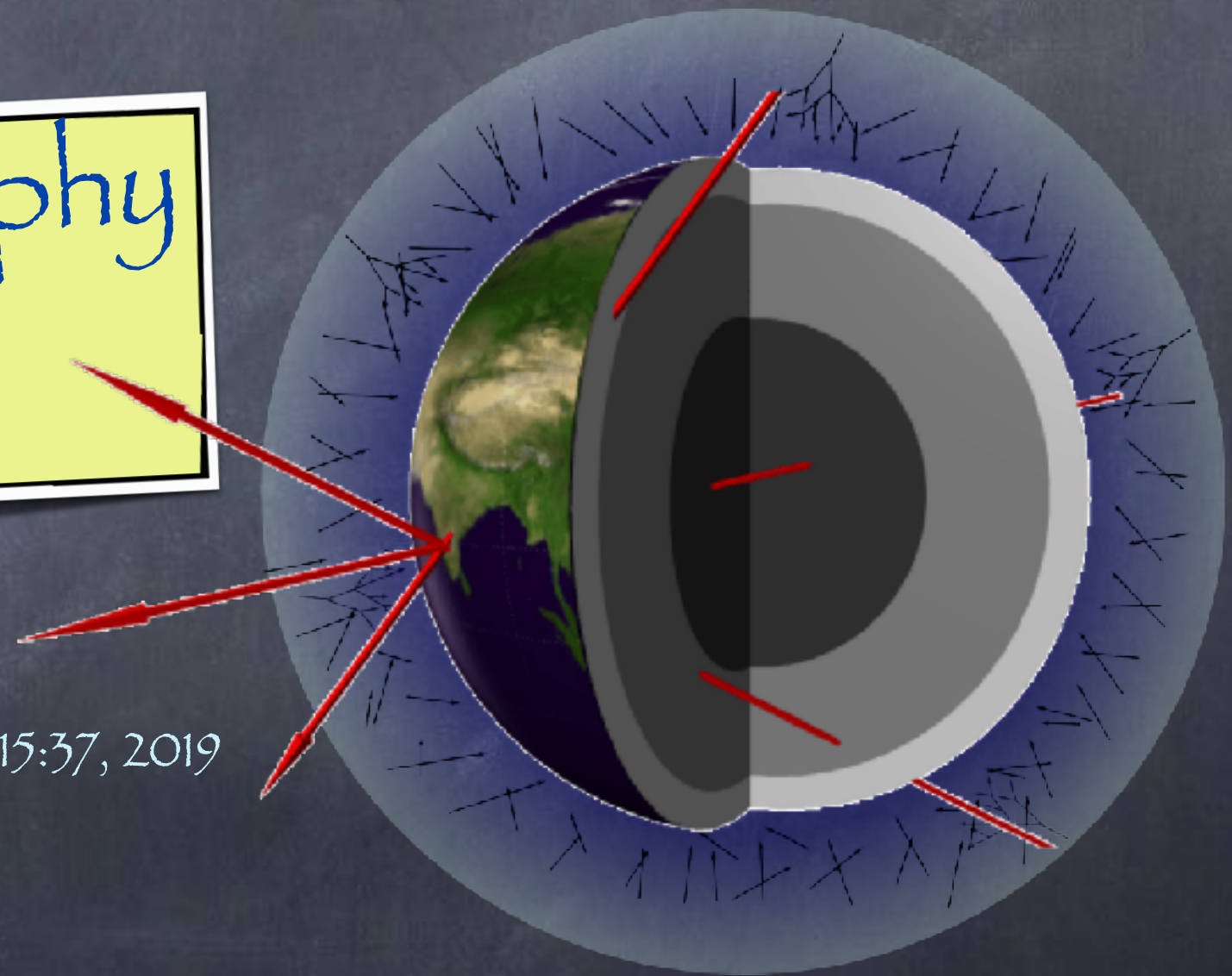
Different flux absorption for different directions and energies
(atmospheric and cosmic neutrinos)



M. G. Aartsen et al. [IceCube Collaboration], Nature 551:596, 2017

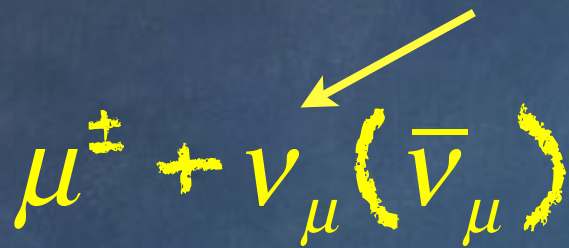
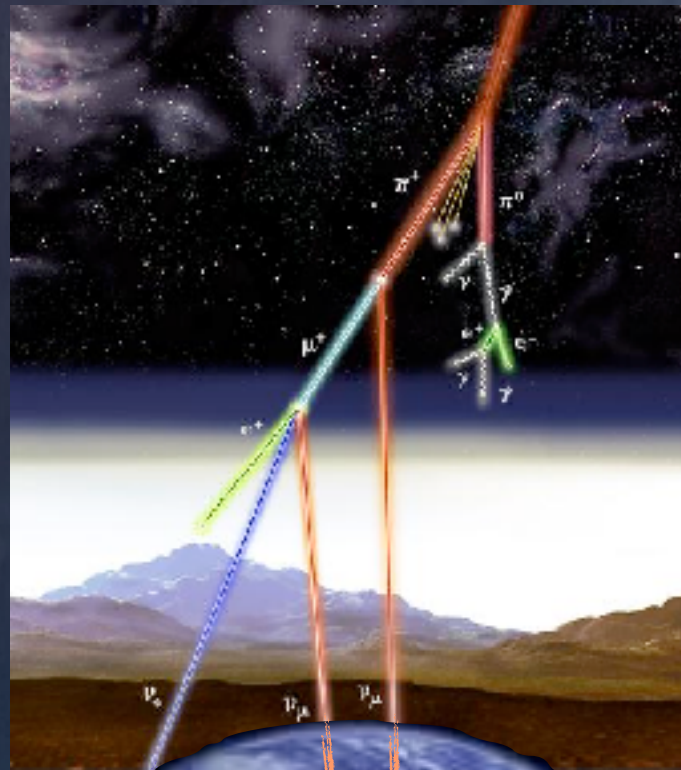
Neutrino absorption tomography

First Earth tomography
with neutrinos!

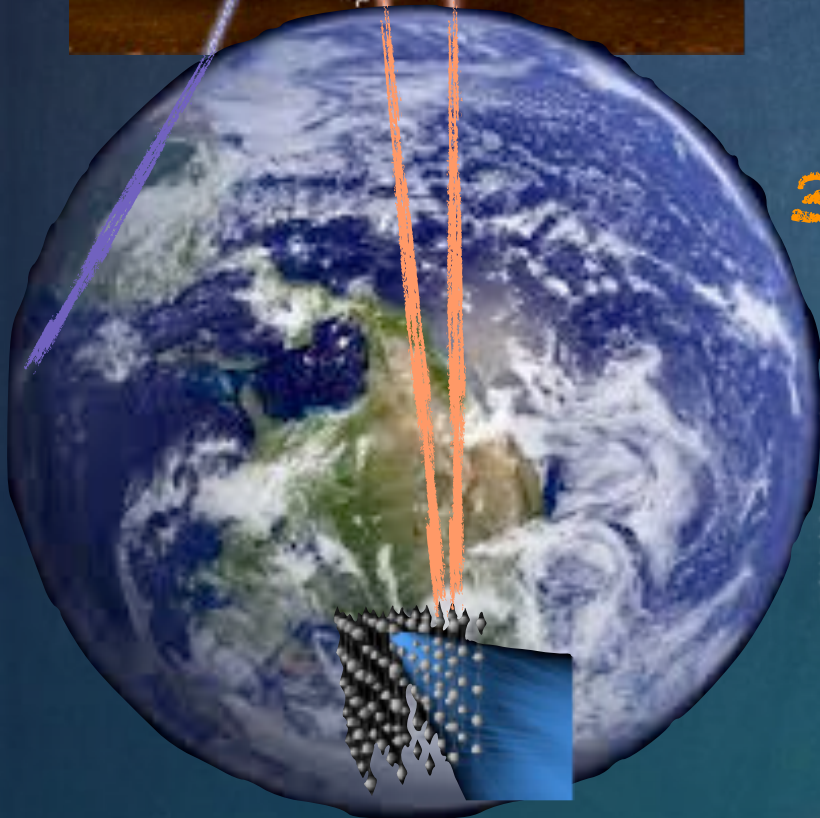


A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

ATMOSPHERIC NEUTRINOS

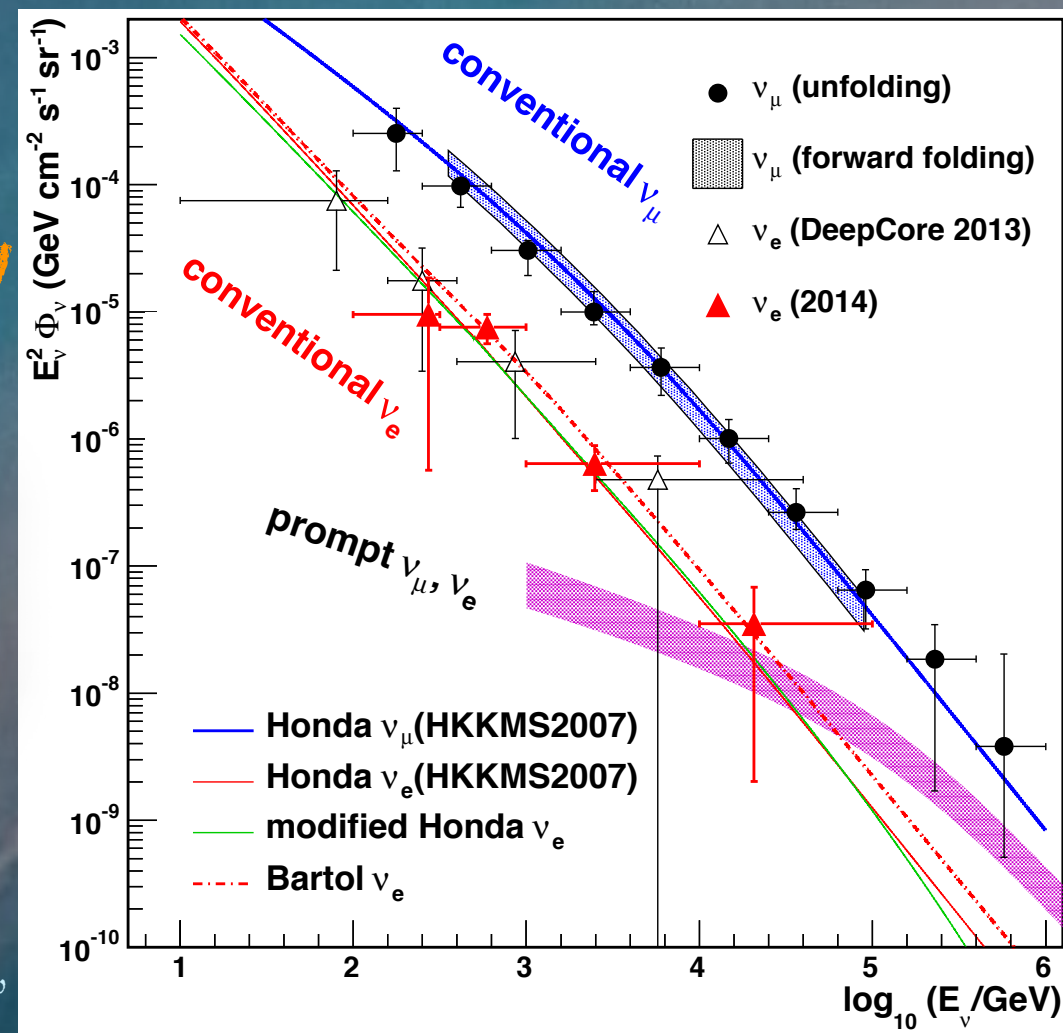


Interactions of cosmic rays in the atmosphere



$30 \text{ MeV} < E < 100 \text{ TeV}$

Huge range of energies and baselines



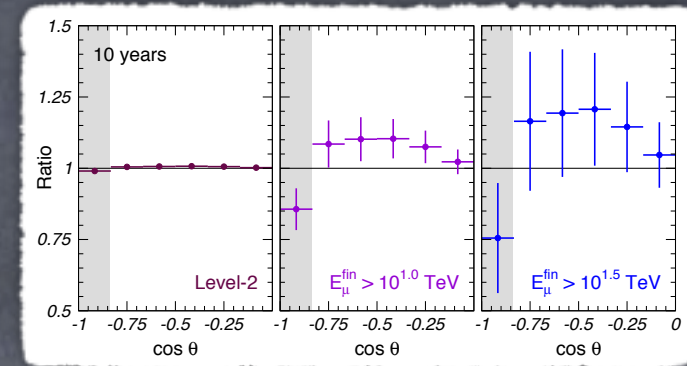
M. G. Aartsen et al. [IceCube Collaboration],
Phys. Rev. D91:122004, 2015

PREVIOUS STUDIES

First forecast of absorption neutrino tomography using atmospheric neutrinos (for IceCube)

M. C. González-García, F. Halzen, M. Maltoni and H. K. M. Tanaka, Phys. Rev. Lett. 100:061802, 2008

Non-homogeneity at $(3.4-4.7)\sigma$ after 10 years

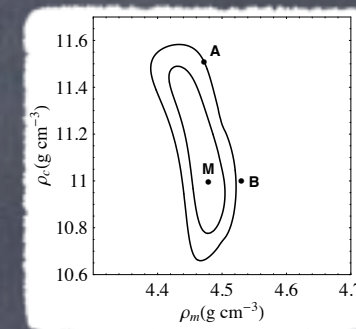


First forecast for KM3NeT

E. Borriello et al., JCAP 0906:030, 2009

E. Borriello et al., Earth Planets Space 62:211, 2010

few percent error after 10 years



Study of lateral heterogeneities (with IceCube)

N. Takeuchi, Earth Planets Space 62:215, 2010

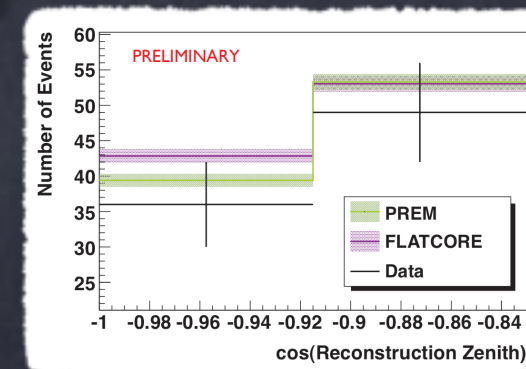
Needs ~300 years

Another study of Earth non-homogeneity (with IceCube)

I. Romero and O. A. Sampayo, Eur. Phys. J. C71:1696, 2011

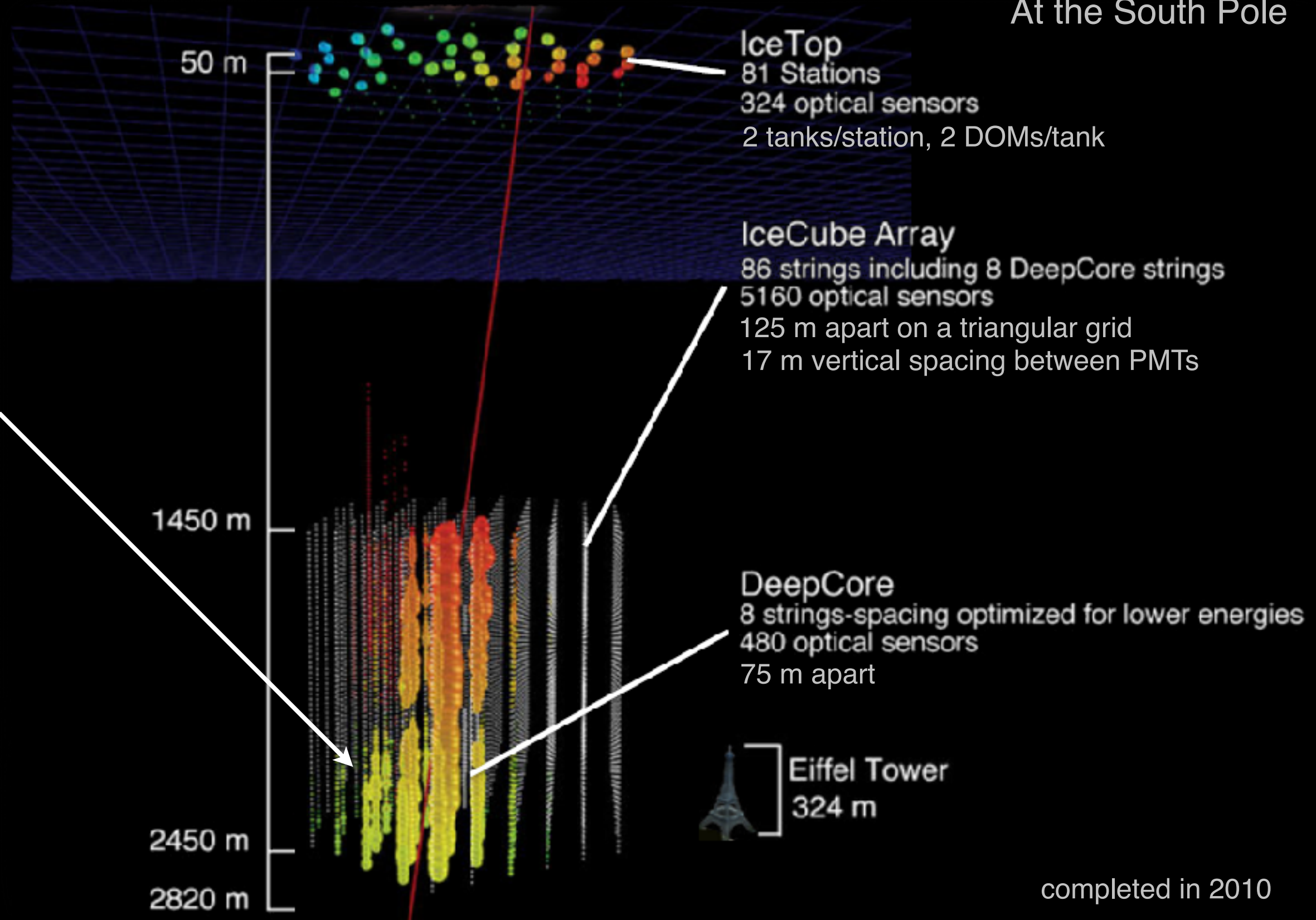
First attempt using 1 year of IC-40 data

K. Hoshina and H. K. M. Tanaka, Poster at Neutrino 2012



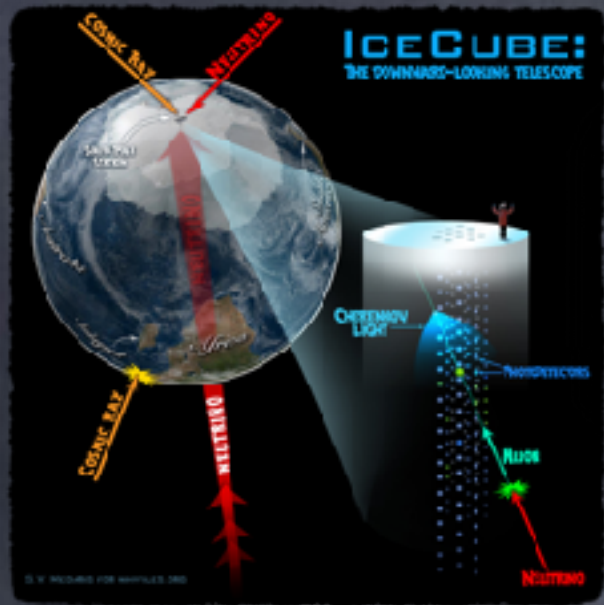
THE ICECUBE NEUTRINO TELESCOPE

At the South Pole



Secondary particles detected via Cherenkov radiation

ICECUBE DATA SET

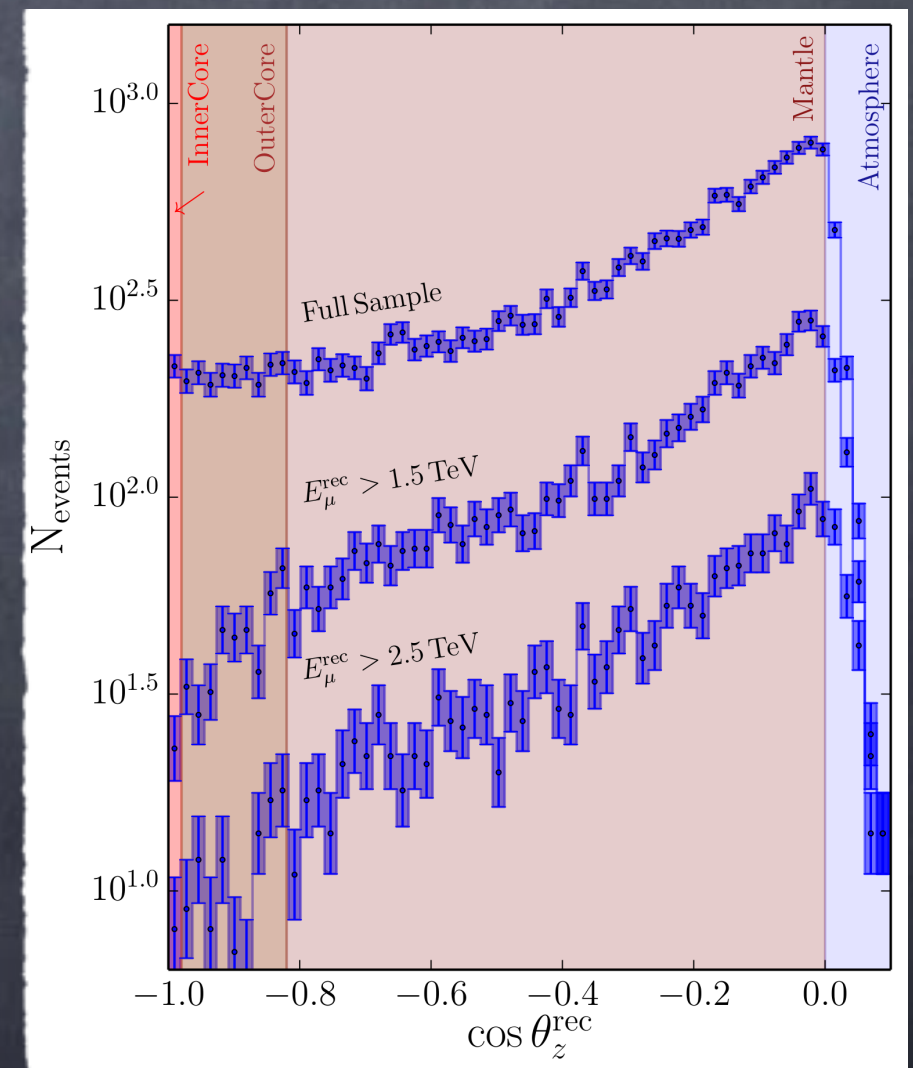


1 year of up-going high-energy muon neutrino events (IC86)
used and prepared for the IC sterile neutrino analysis

M. G. Aartsen et al. [IceCube Collaboration], Phys. Rev. Lett. 117:071801, 2016

Energy range: $\sim 400 \text{ GeV} - 20 \text{ TeV}$
Zenith angle range: $\cos \theta = [-1, 0.2]$
Number of events: 20145 (343.7 days)
>99.9% muon neutrino purity

Publicly available!

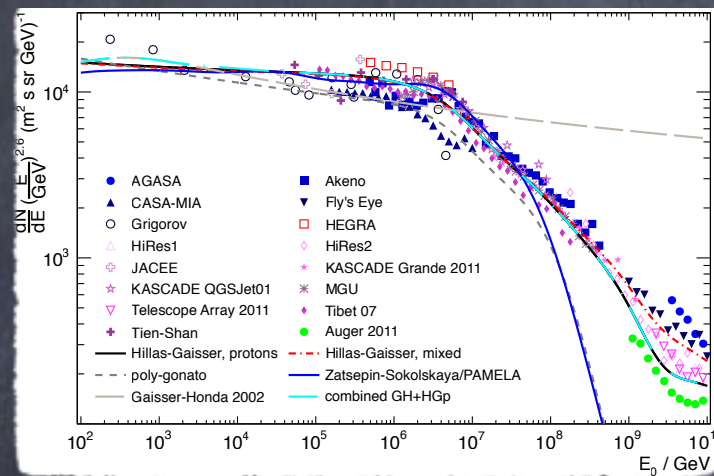


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ANALYSIS INGREDIENTS

Primary cosmic-ray spectrum

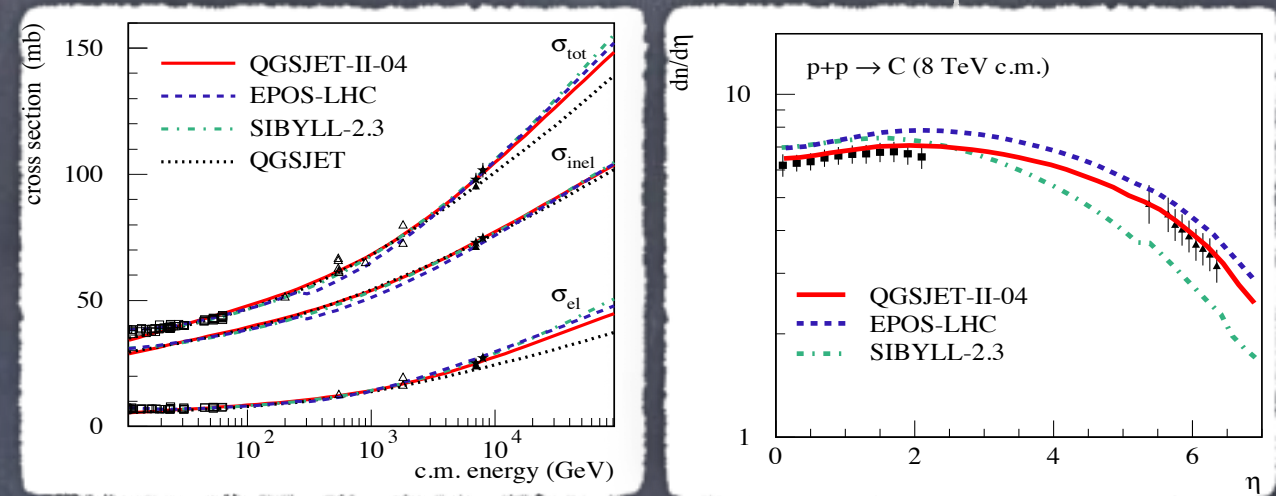
3-population models to fit cosmic-ray data



A. Fedynitch, J. B. Tjus and P. Desiati,
Phys. Rev. D86:114024, 2012

Hadronic-interaction model

Models for cascade development

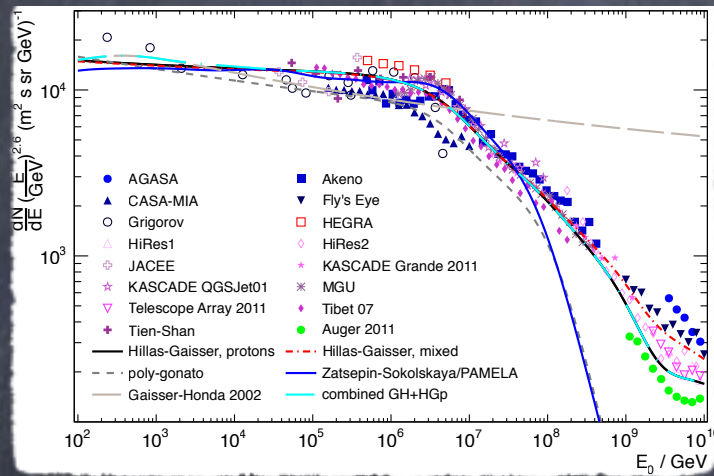


S. Ostapchenko, ECRS 2016, arXiv:1612.09461

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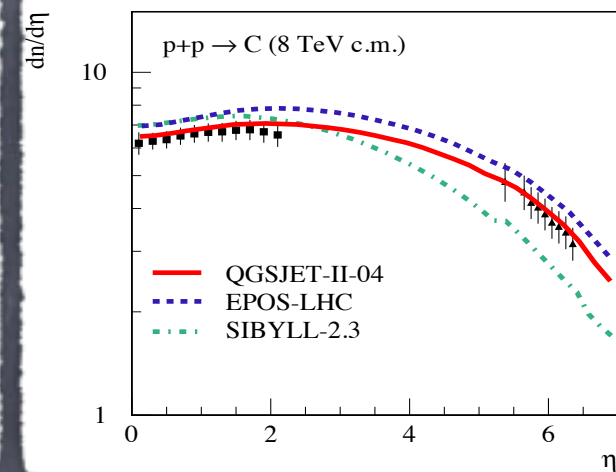
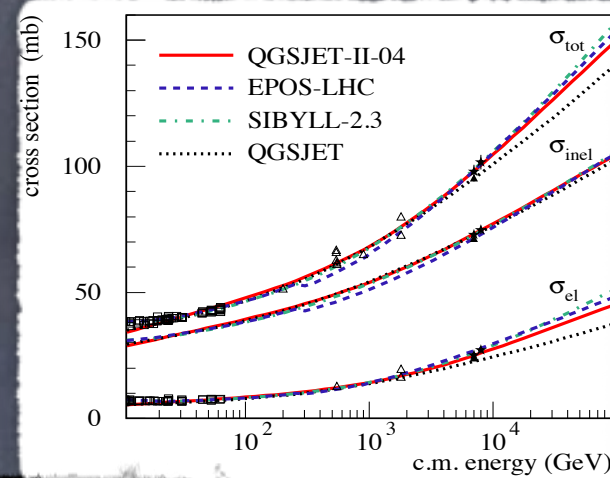
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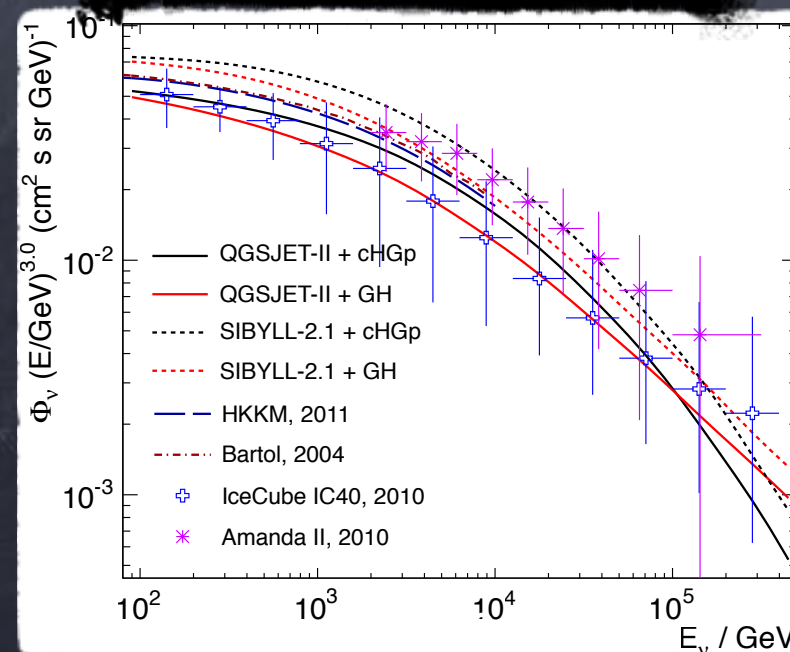
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Models for cascade development



S. Ostapchenko, ECRS 2016, arXiv:1612.09461

Neutrino flux



A. Fedynitch, J. B. Tjus and P. Desiati,
Phys. Rev. D86:114024, 2012

Looking inside the Earth with neutrinos

ANALYSIS INGREDIENTS

Neutrino propagation through the Earth

we propagate neutrinos with ν -SQuIDS

C. Argüelles, J. Salvado and C. Weaver, <https://github.com/arguelles/nuSQuIDS>

In addition to absorption, we also include neutrino oscillations

ANALYSIS INGREDIENTS

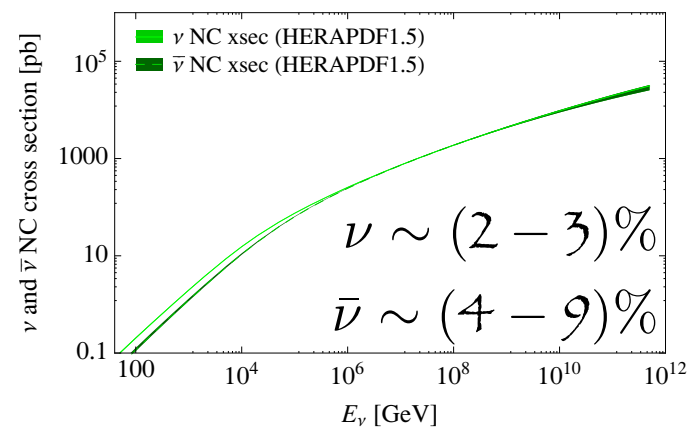
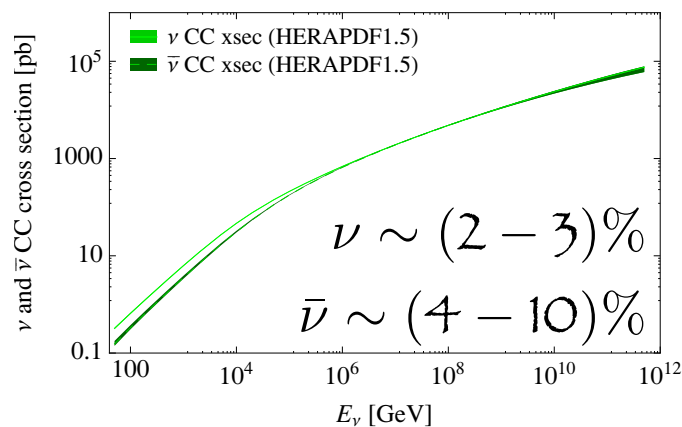
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Neutrino interactions with nucleons



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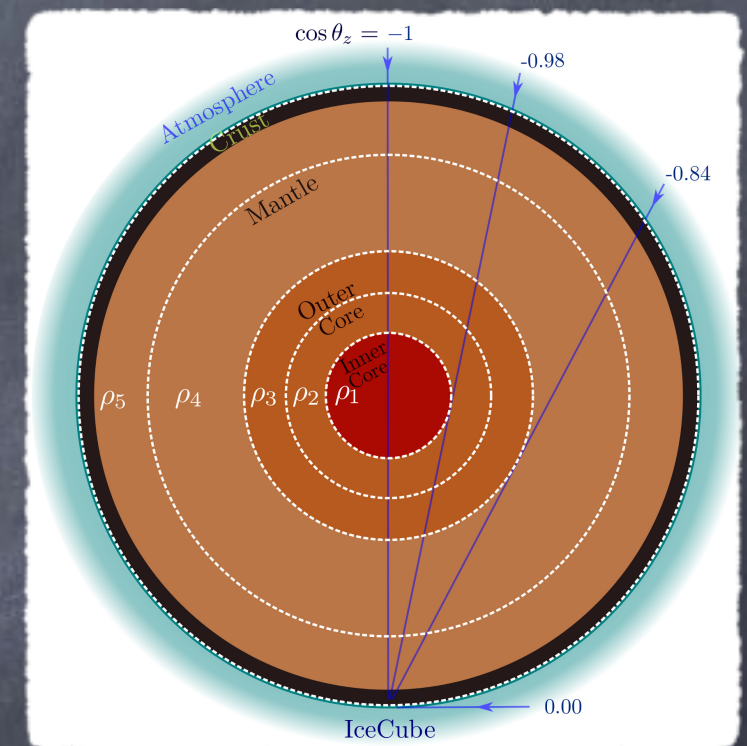
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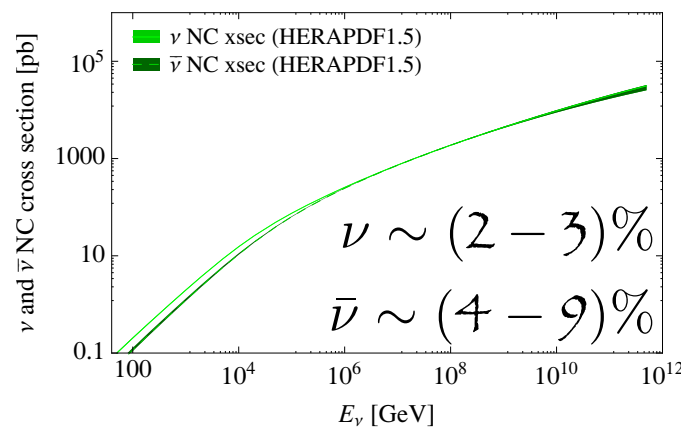
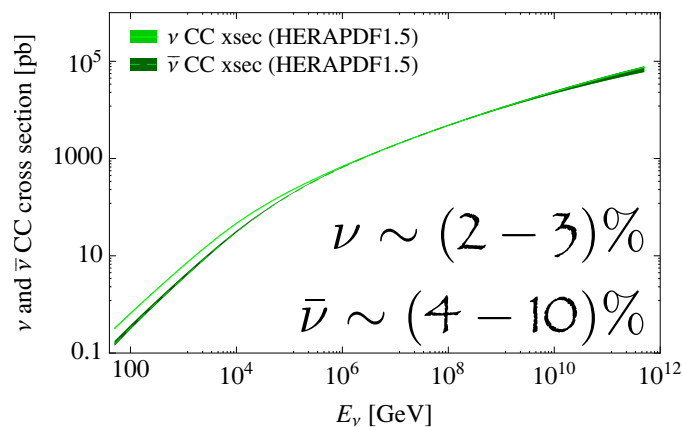
C. Argüelles, J. Salvado and C. Weaver, <https://github.com/arguelles/nuSQUIDS>

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Earth model



Neutrino interactions with nucleons



5 spherical layers:
 1 for the inner core
 2 for the outer core
 2 for the mantle

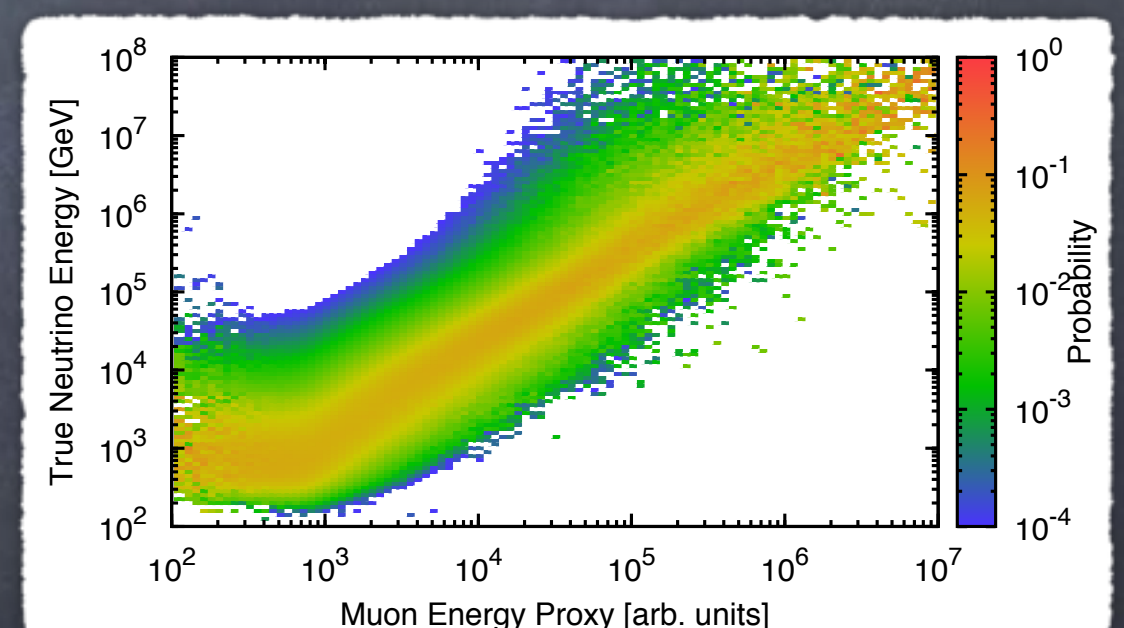
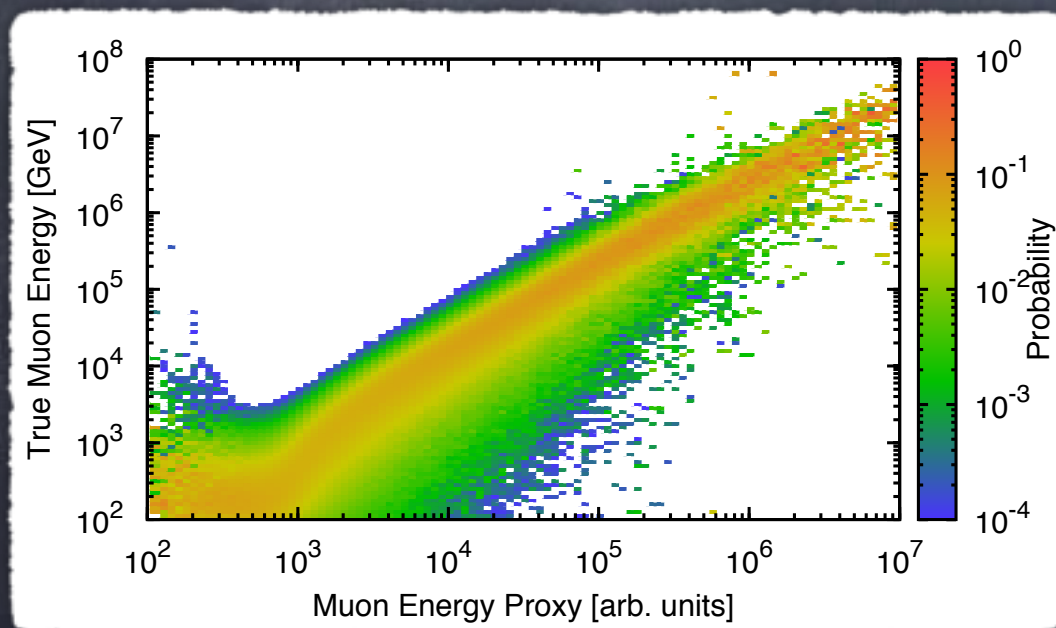
ANALYSIS INGREDIENTS

Detector simulation

Publicly available!

We map E_ν and θ_ν to E_{rec} and θ_{rec} using the official IceCube Monte Carlo

<https://icecube.wisc.edu/science/data/IC86-sterile-neutrino>



M. G. Aartsen et al. [IceCube Collaboration], Phys. Rev. Lett. 115:081102, 2015

$$\sigma_{\log(E_\mu/\text{GeV})} \sim 0.5$$

$$\sigma_{\cos(\theta)} \sim 0.005 - 0.015$$

STATISTICAL ANALYSIS

densities of the
5 Earth layers

Binned maximum likelihood analysis

$$\ln \mathcal{L}(\vec{\rho}; \vec{\eta}) = \sum_{i \in \text{bins}} \left(N_i^{\text{data}} \ln N_i^{\text{th}}(\vec{\rho}; \vec{\eta}) - N_i^{\text{th}}(\vec{\rho}; \vec{\eta}) \right) - \sum_j \frac{(\eta_j - \eta_j^0)^2}{2\sigma_j^2}$$

4 nuisance parameters

other systematics

DOM efficiency

Flux continuous parameters:

- overall normalization
- pion/kaon ratio
- spectral index

Primary CR spectra

Hadronic-interaction models

Neutrino cross sections

We use MultiNest for parameter inference

F. Feroz and M. Robson, <https://github.com/farhanferoz/MultiNest>

STATISTICAL ANALYSIS

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other systematics

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- pion/kaon ratio
- spectral index

Primary CR spectra

Hadronic-interaction models

Neutrino cross sections

Optical properties
of ice not included!

We use MultiNest for parameter inference

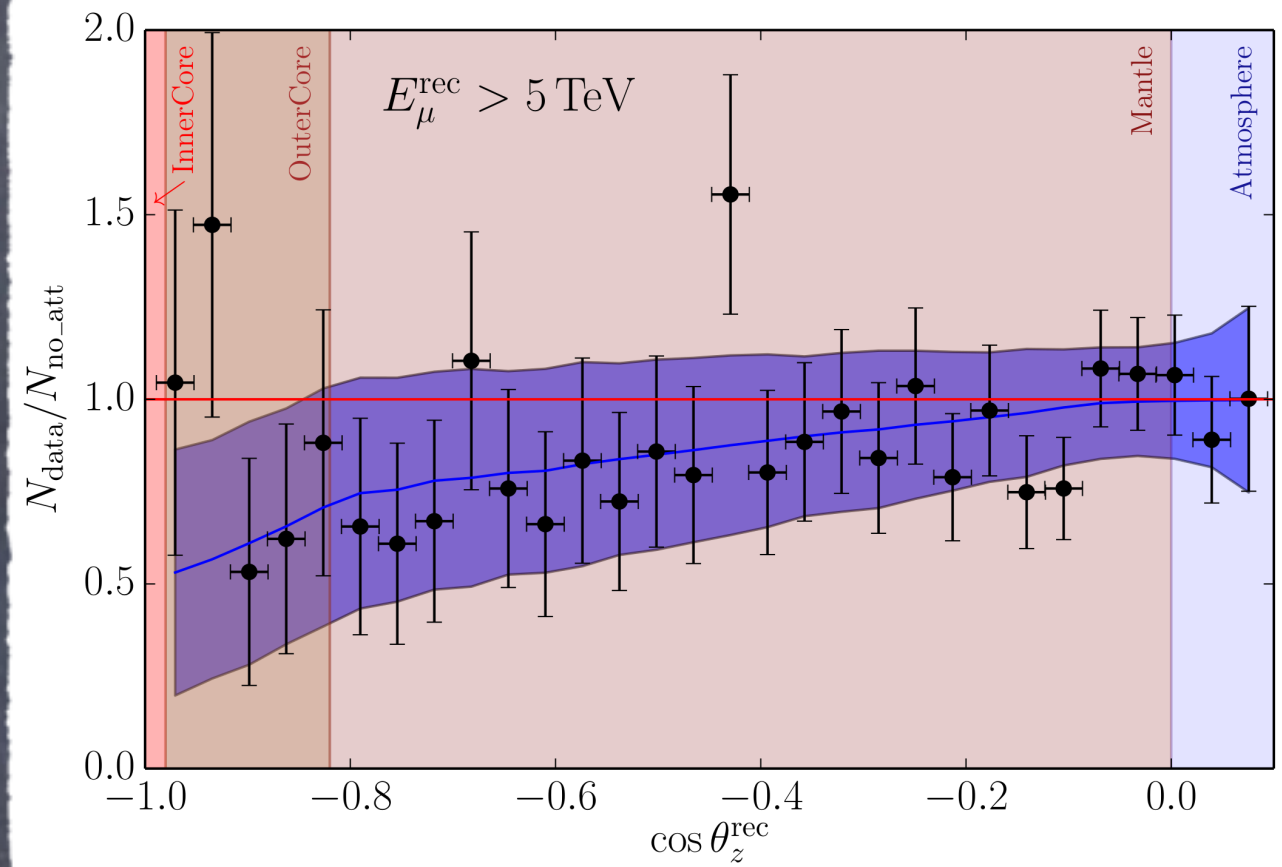
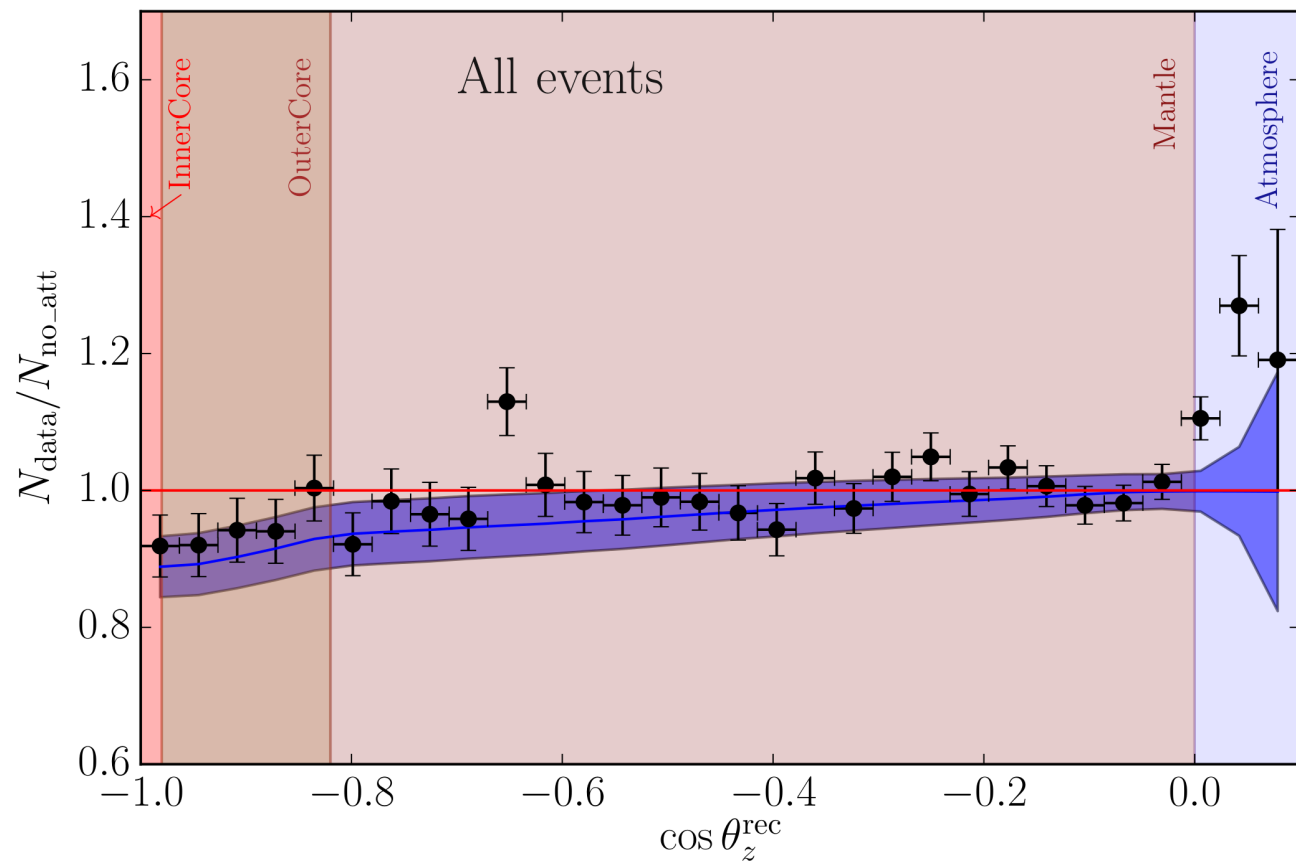
F. Feroz and M. Robson, <https://github.com/farhanferoz/MultiNest>

IS THE EARTH THERE?



All events

$E > 5 \text{ TeV}$



A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

Full sample:
useful to fix normalization

core-crossing neutrinos:
attenuation can be 50% ($>5 \text{ TeV}$)

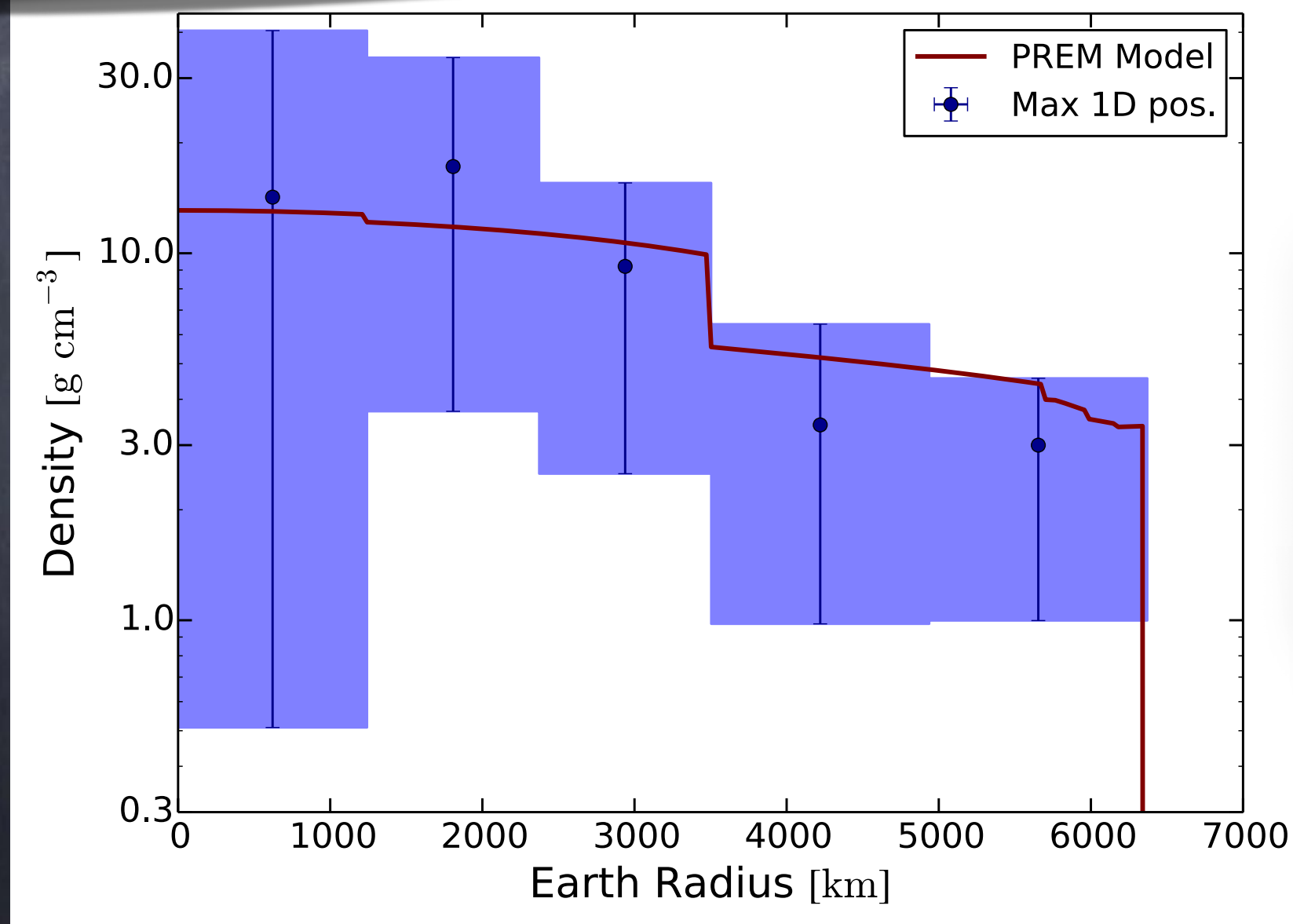
MAIN RESULT: 1-D DENSITY PROFILE

First Earth tomography
with neutrinos!

nature
physics

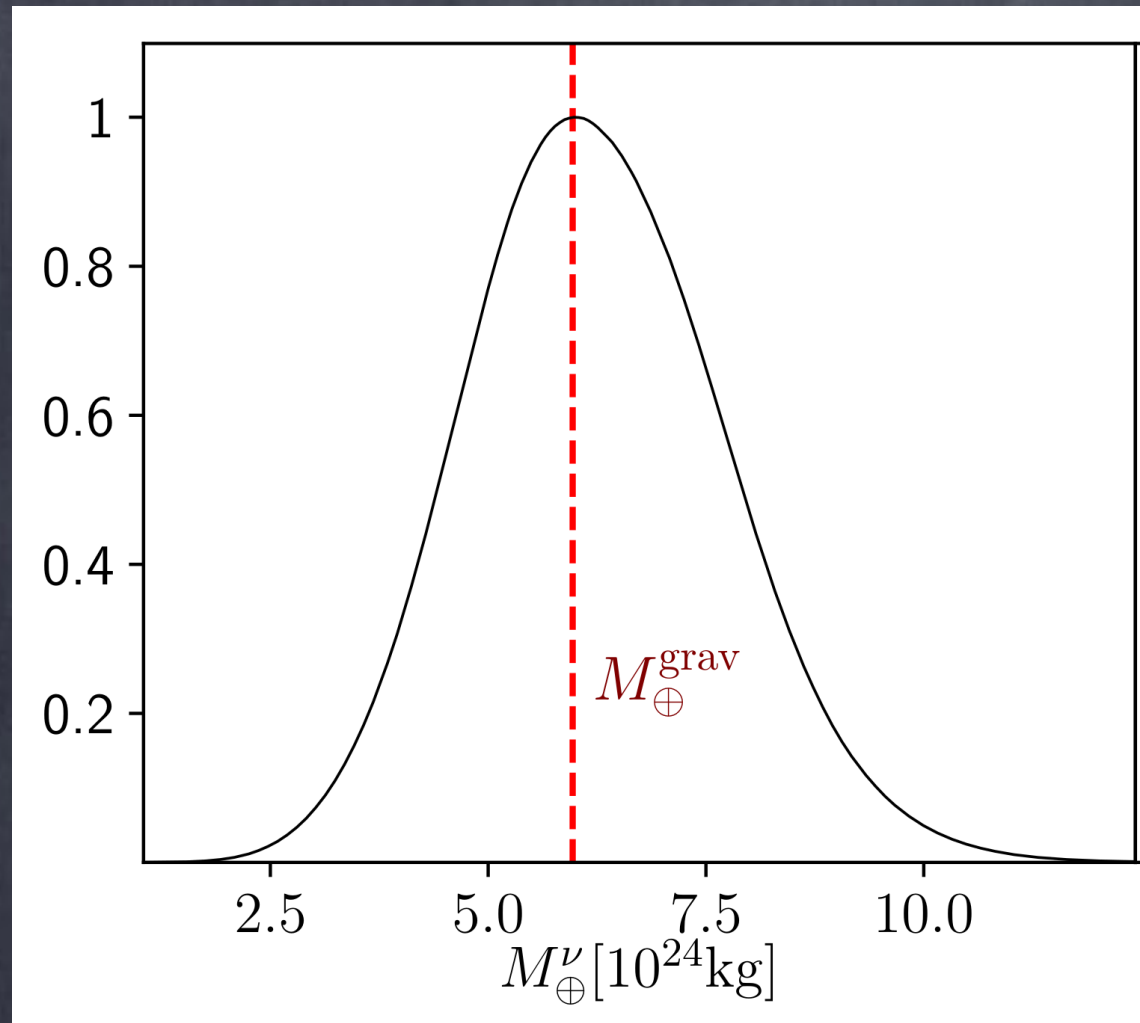
Neutrino tomography of Earth

Andrea Donini¹, Sergio Palomares-Ruiz^{1*} and Jordi Salvado^{1,2}



unlike reconstructions
with seismic data,
NO constraint on the
Earth mass or
moment of inertia

EARTH'S MASS



First measurement of the Earth's mass using the weak force!

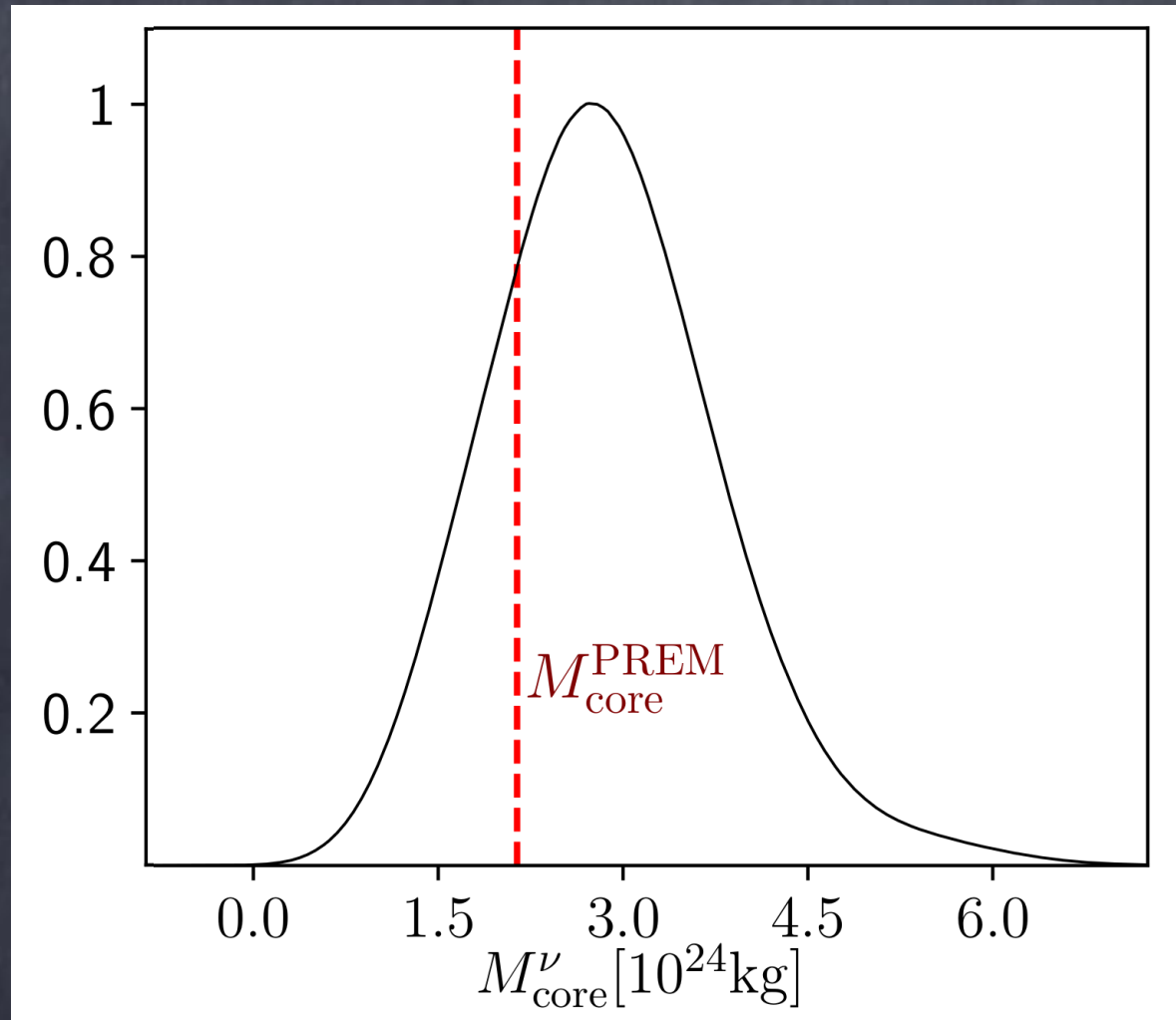
$$M_{\nu} = \left(6.0^{+1.6}_{-1.3} \right) \times 10^{24} \text{ kg}$$

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

Gravitational measurement

$$M_{\text{grav}} = 5.97217(13) \times 10^{24} \text{ kg}$$

EARTH'S CORE MASS



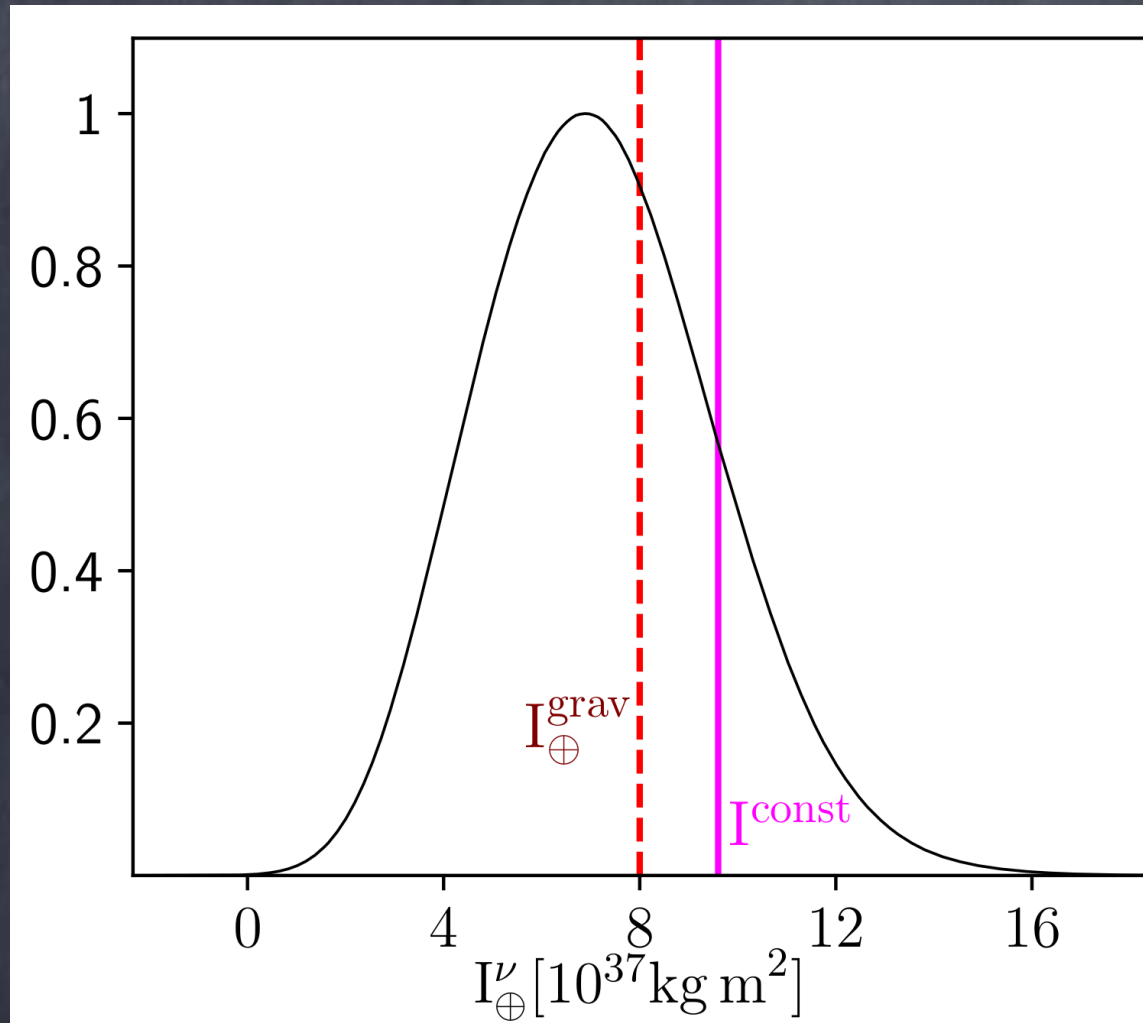
First measurement of the Earth's core mass using the weak force!

$$M_{\text{core-}\nu} = \left(2.7^{+1.0}_{-0.9} \right) \times 10^{24} \text{ kg}$$

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

$$\frac{M_{\text{core-}\nu}}{M_{\nu}} = 0.45^{+0.21}_{-0.18}$$

EARTH'S MOMENT OF INERTIA



First measurement of the Earth's moment of inertia using the weak force!

$$I_\nu = (6.9 \pm 2.4) \times 10^{37} \text{ kg m}^2$$

$$\frac{I_\nu}{I_{\text{sphere-}\nu}} = 0.7 \pm 0.3$$

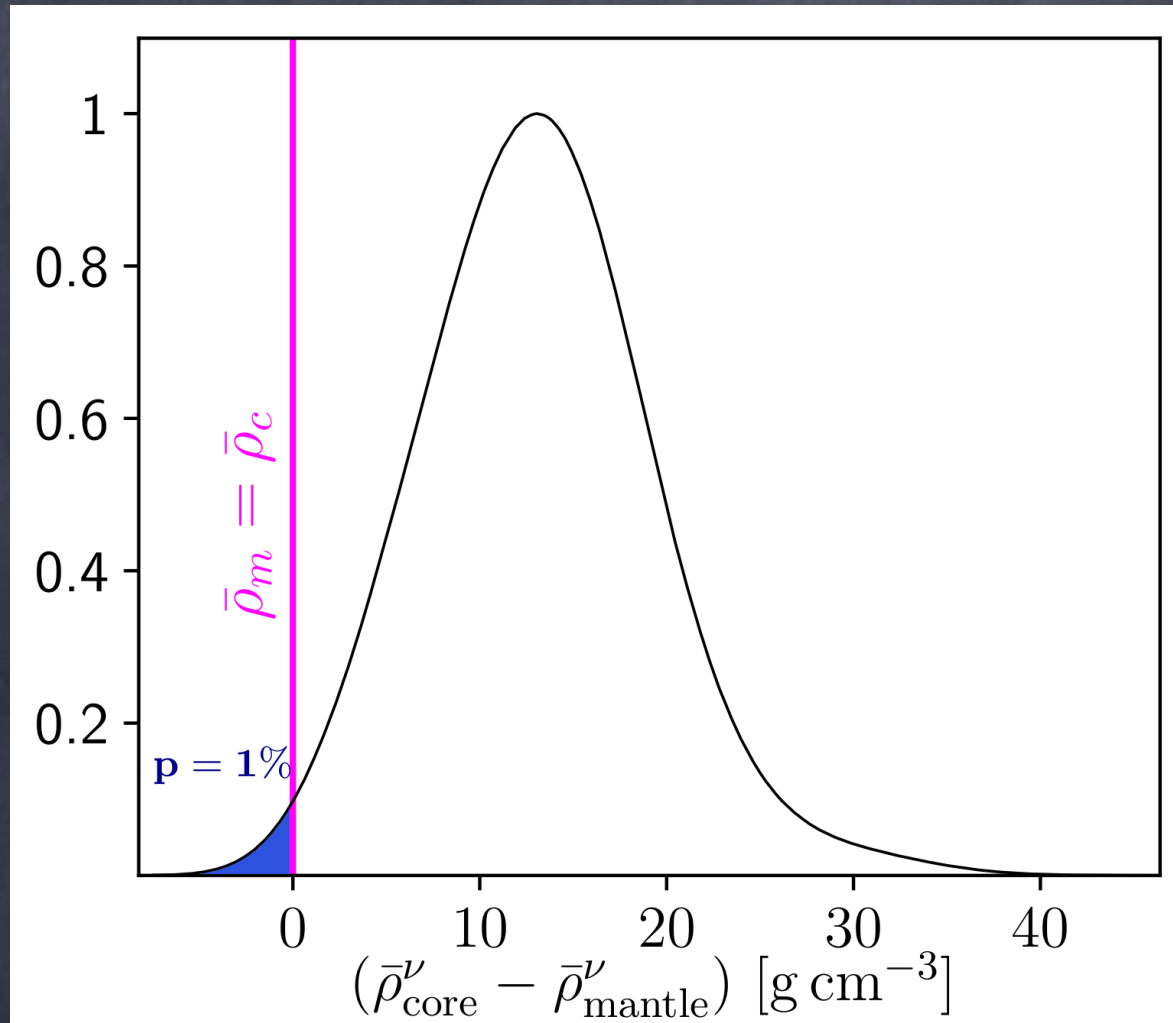
Gravitational measurement

$$\frac{I_{\text{grav}}}{I_{\text{sphere}}} = 0.82681(11)$$

$$I_{\text{grav}} = 8.01736(96) \times 10^{37} \text{ kg m}^2$$

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

MANTLE DENSER THAN CORE



First measurement of the Earth's core-mantle discontinuity using the weak force!

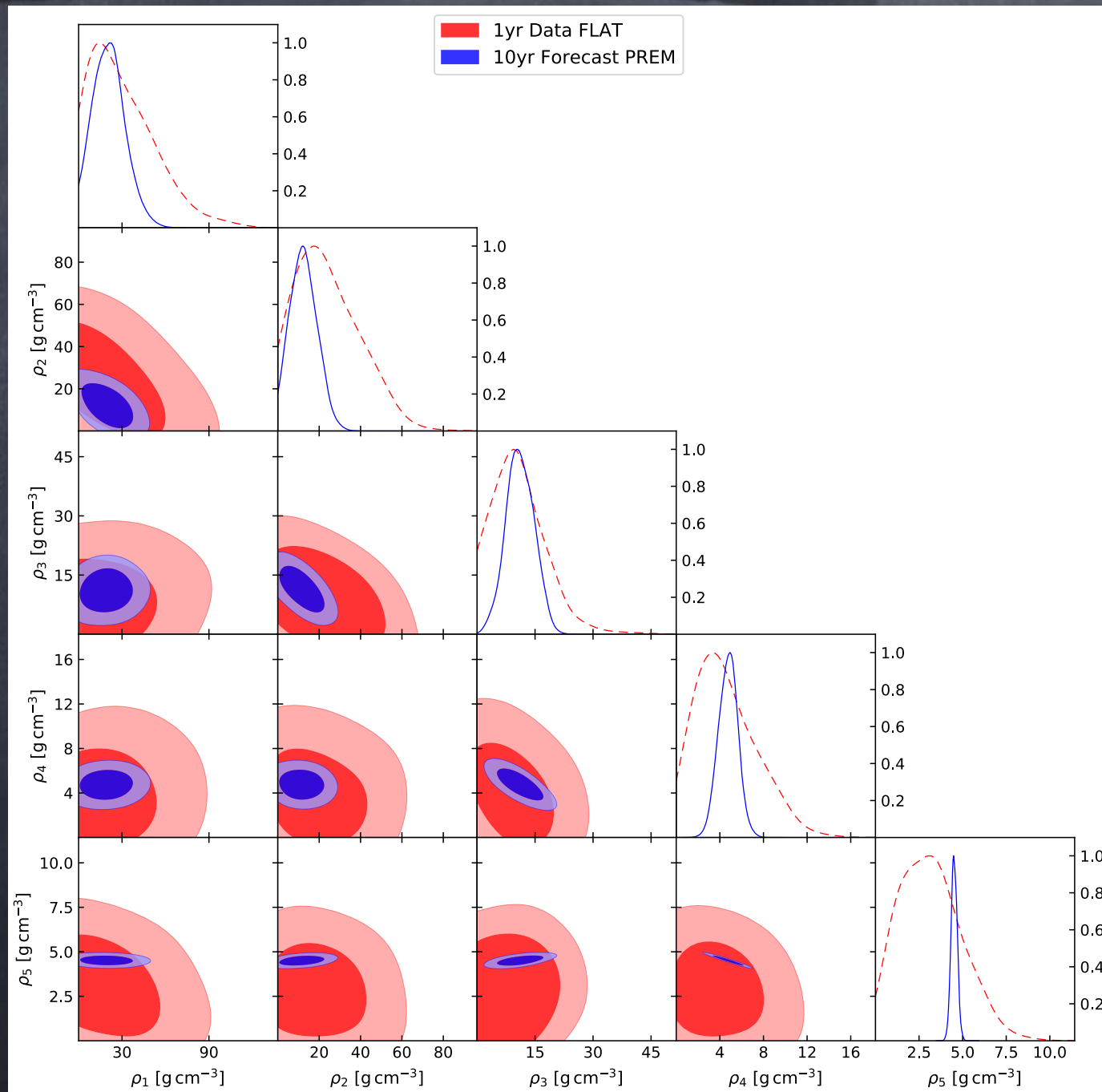
$$\left(\bar{\rho}_{\text{core}}^{\nu} - \bar{\rho}_{\text{mantle}}^{\nu} \right) = \left(13.1^{+5.8}_{-6.3} \right) \text{ g / cm}^3$$

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

A denser mantle has a p-value of $p=0.011$

WHAT ABOUT THE FUTURE? ... ACTUALLY THE PRESENT

Forecast for 10 years of data



Few per cent error in
the mantle

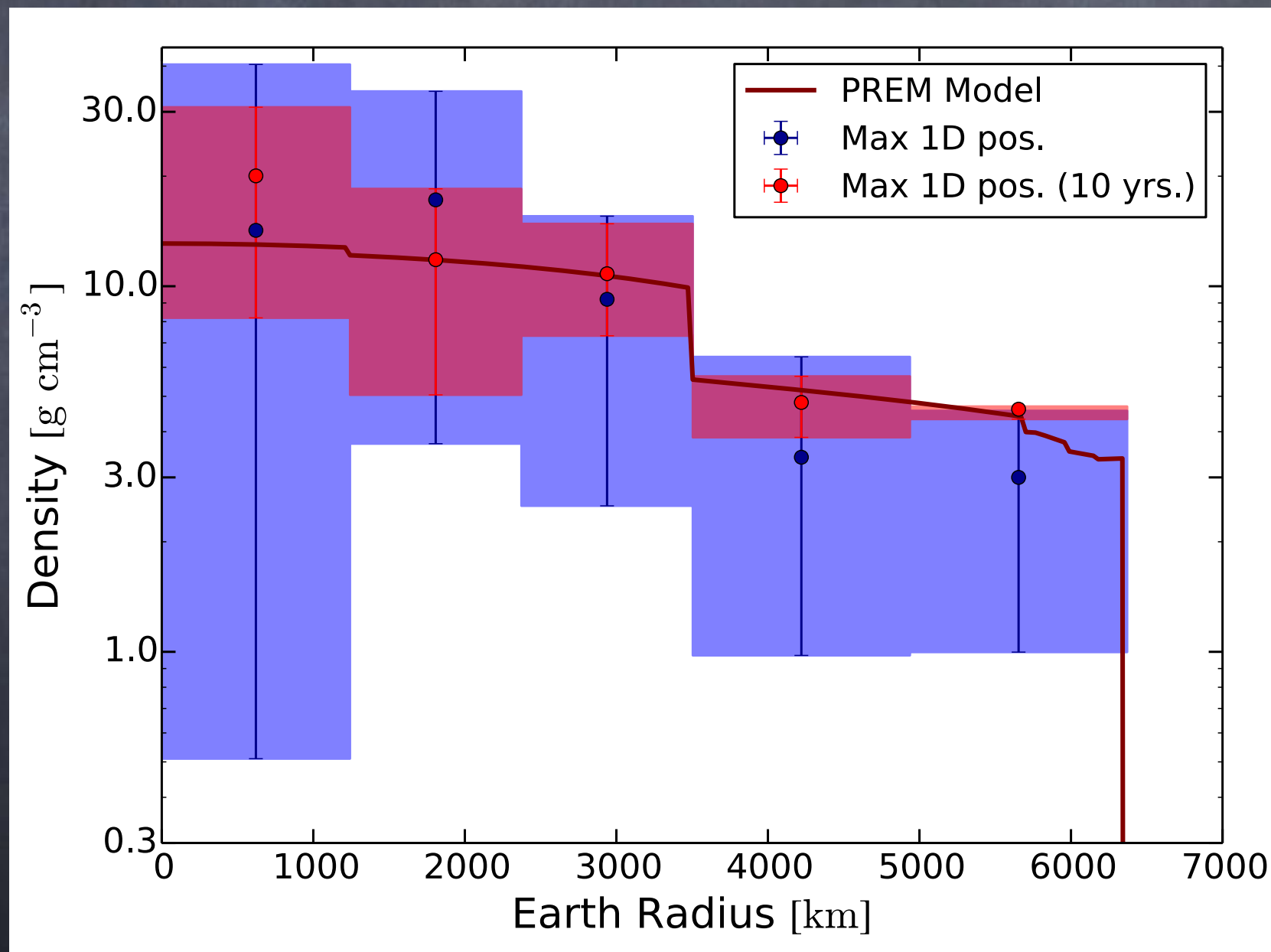
A finer modeling can
be considered

Test of
discontinuities

Knowledge of hadronic-
interaction model
impacts systematics

WHAT ABOUT THE FUTURE? ... ACTUALLY THE PRESENT

Forecast for 10 years of data

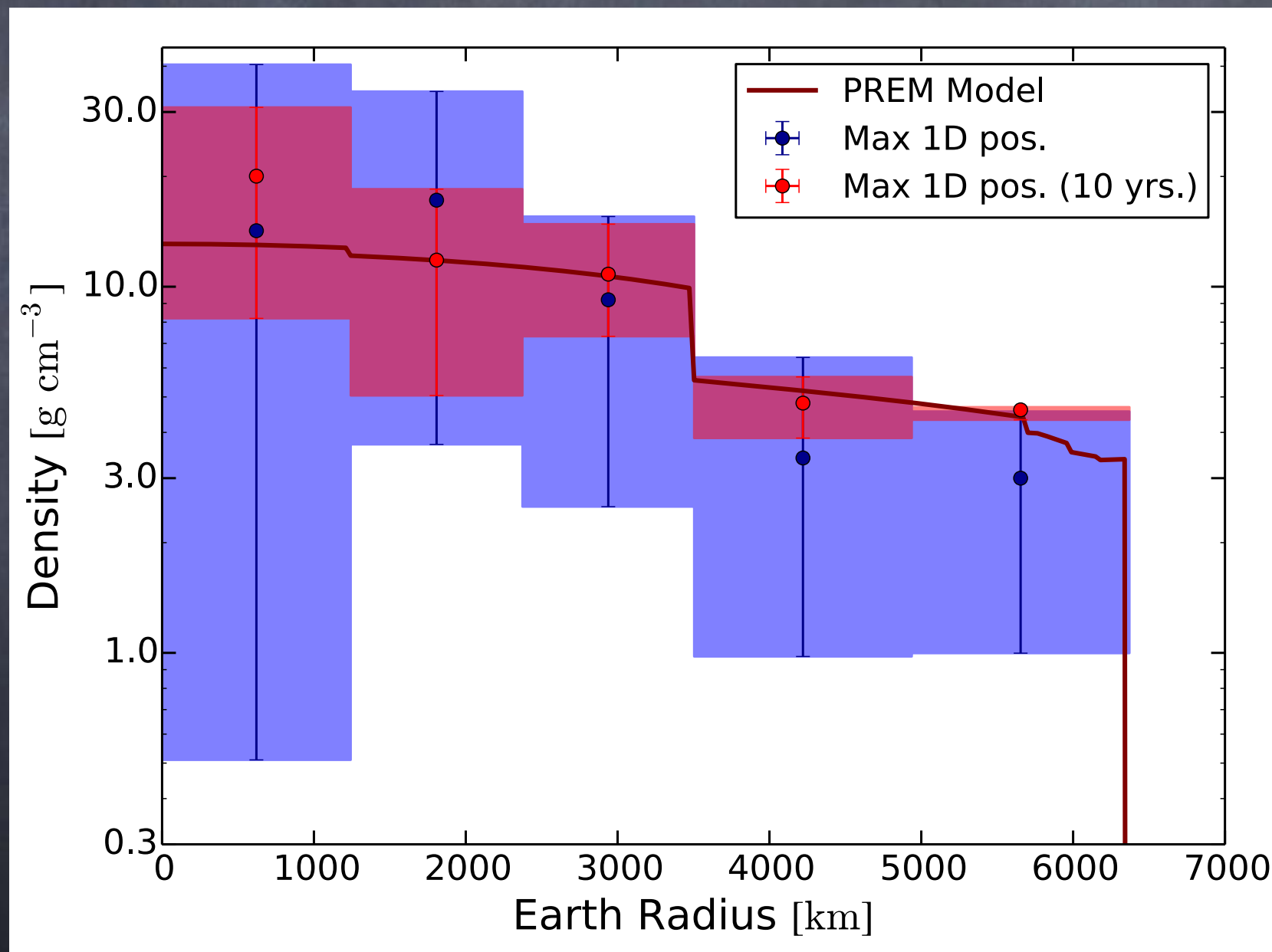


A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

WHAT ABOUT THE FUTURE? ... ACTUALLY THE PRESENT

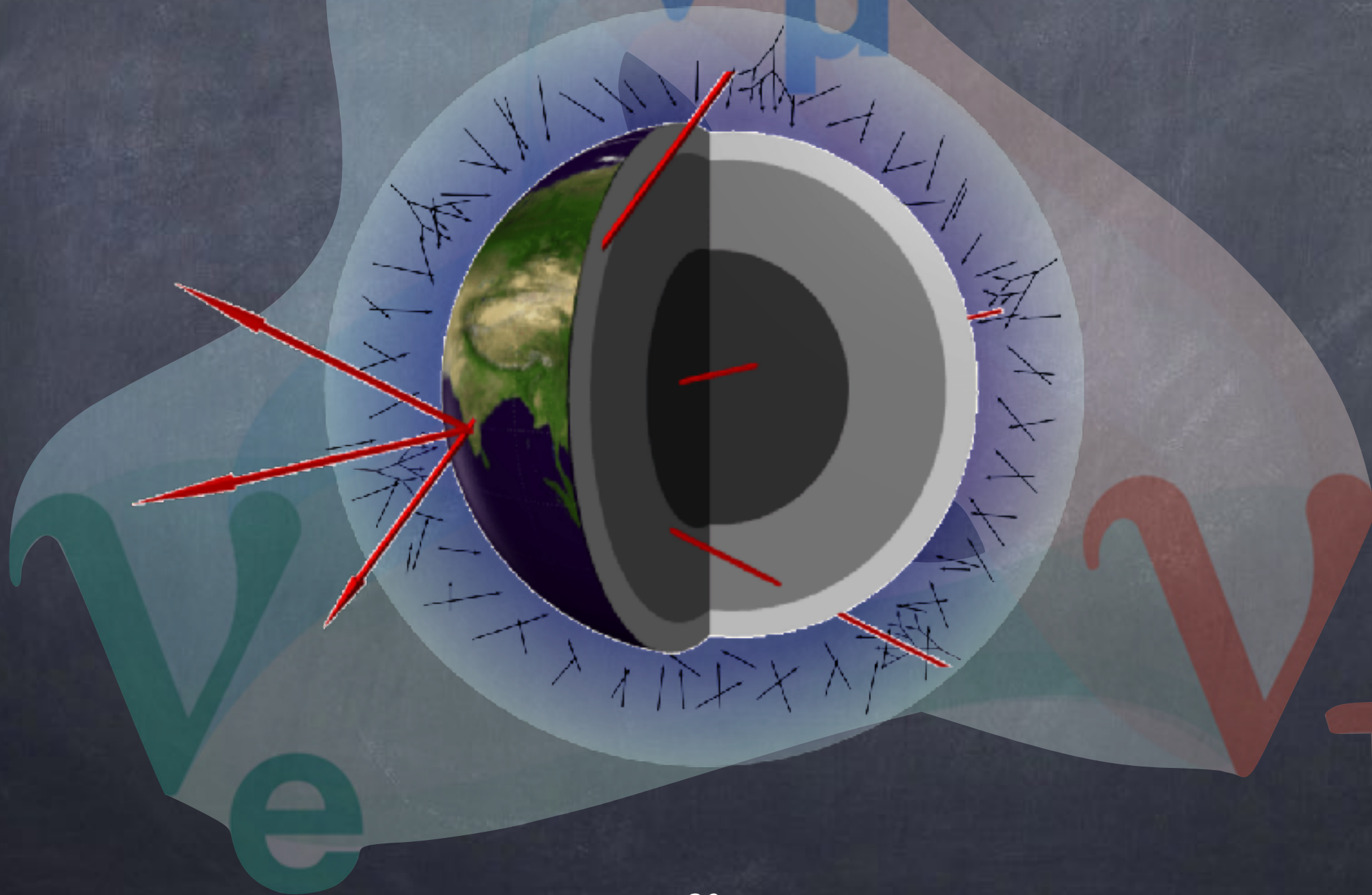
Forecast for 10 years of data

... but already 10 years of actual data!



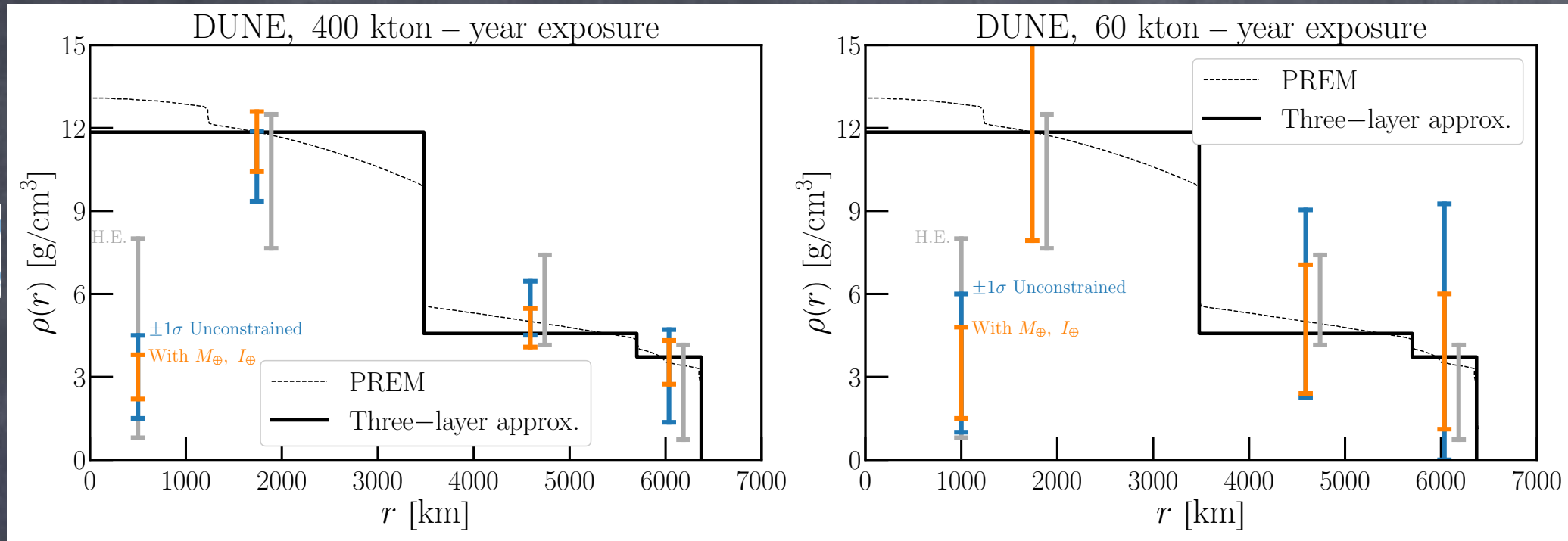
A. Donini, SPR and J. Salvado, *Nature Physics* 15:37, 2019

Neutrino oscillation tomography

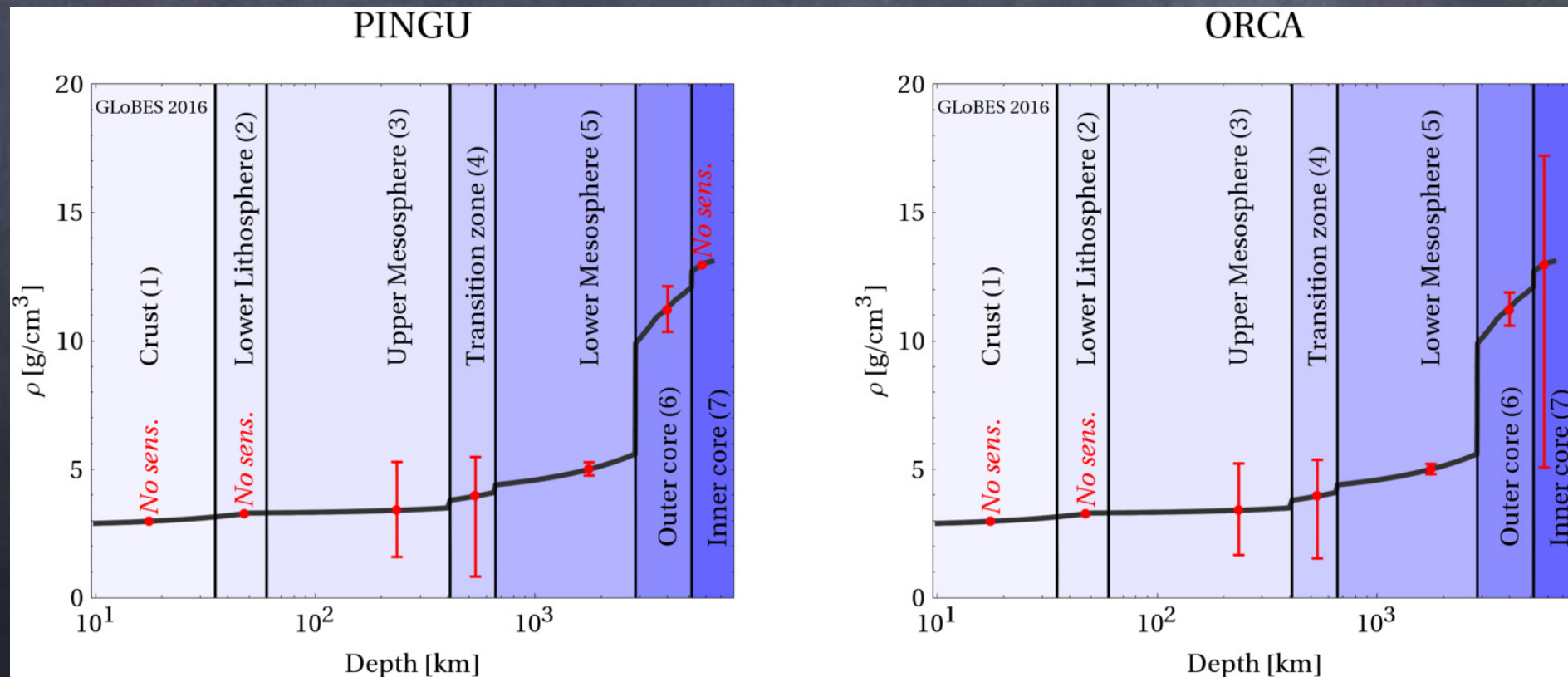


ATMOSPHERIC NEUTRINOS (GEV)

Tomography first considered in S. K. Agarwalla, T. Li, O. Mena and SPR, arXiv:1212.2238



K. J. Kelly, P. A. N. Machado, I. Martínez-Soler and Y. F. Pérez-González, JHEP 05:187, 2022



W. Winter, Nucl. Phys. B908:250, 2016

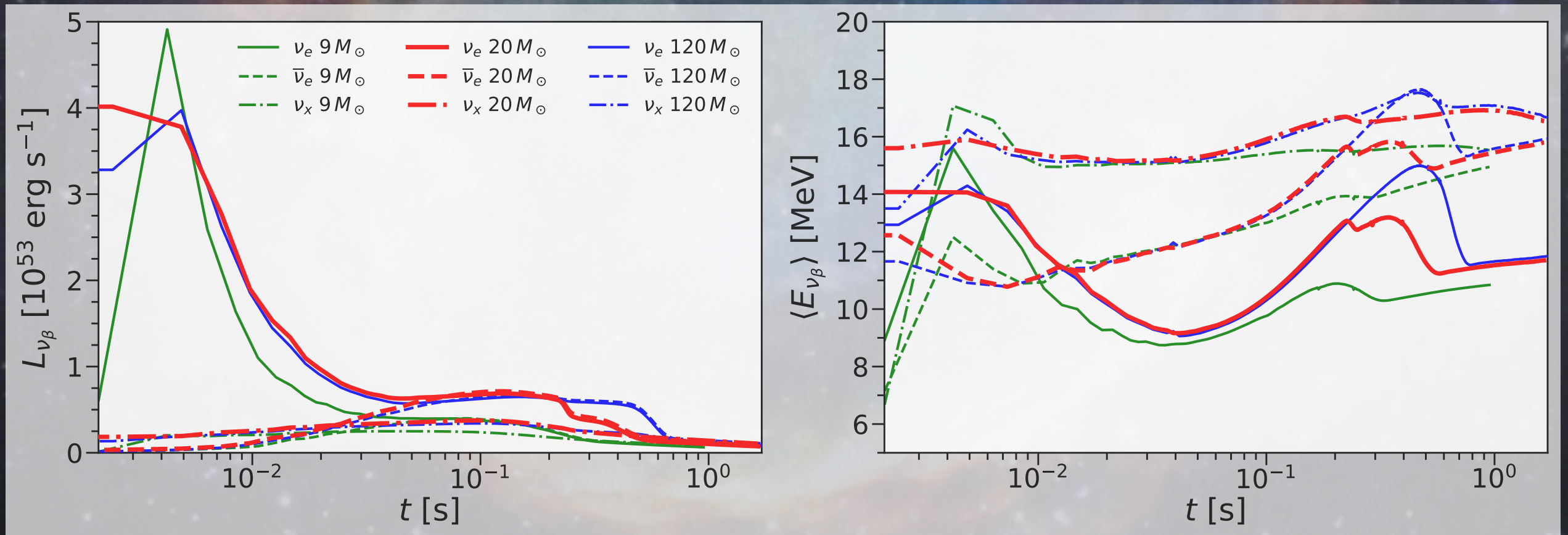


SUPERNOVA NEUTRINOS (MEV)

Tomography first considered in M. Lindner, T. Ohlsson, R. Tomàs and W. Winter, *Astropart. Phys.* 19:755, 2003
 and later also in E. K. Akhmedov, M. A. Tortola and J. W. F. Valle, *JHEP* 06:053, 2005

$$\phi_{\nu\beta}^0(t, E_\nu) = \frac{L_{\nu\beta}(t)}{\langle E_{\nu\beta} \rangle(t)} \frac{(\alpha_{\nu\beta}(t) + 1)^{\alpha_{\nu\beta}(t)+1}}{\langle E_{\nu\beta} \rangle(t) \Gamma(\alpha_{\nu\beta}(t) + 1)} \left(\frac{E_\nu}{\langle E_{\nu\beta} \rangle(t)} \right)^{\alpha_{\nu\beta}(t)} \exp \left(- \frac{(\alpha_{\nu\beta}(t) + 1) E_\nu}{\langle E_{\nu\beta} \rangle(t)} \right)$$

M. T. Keil, G. G. Raffelt and H.-T. Janka, *Astrophys. J.* 590:971, 2003



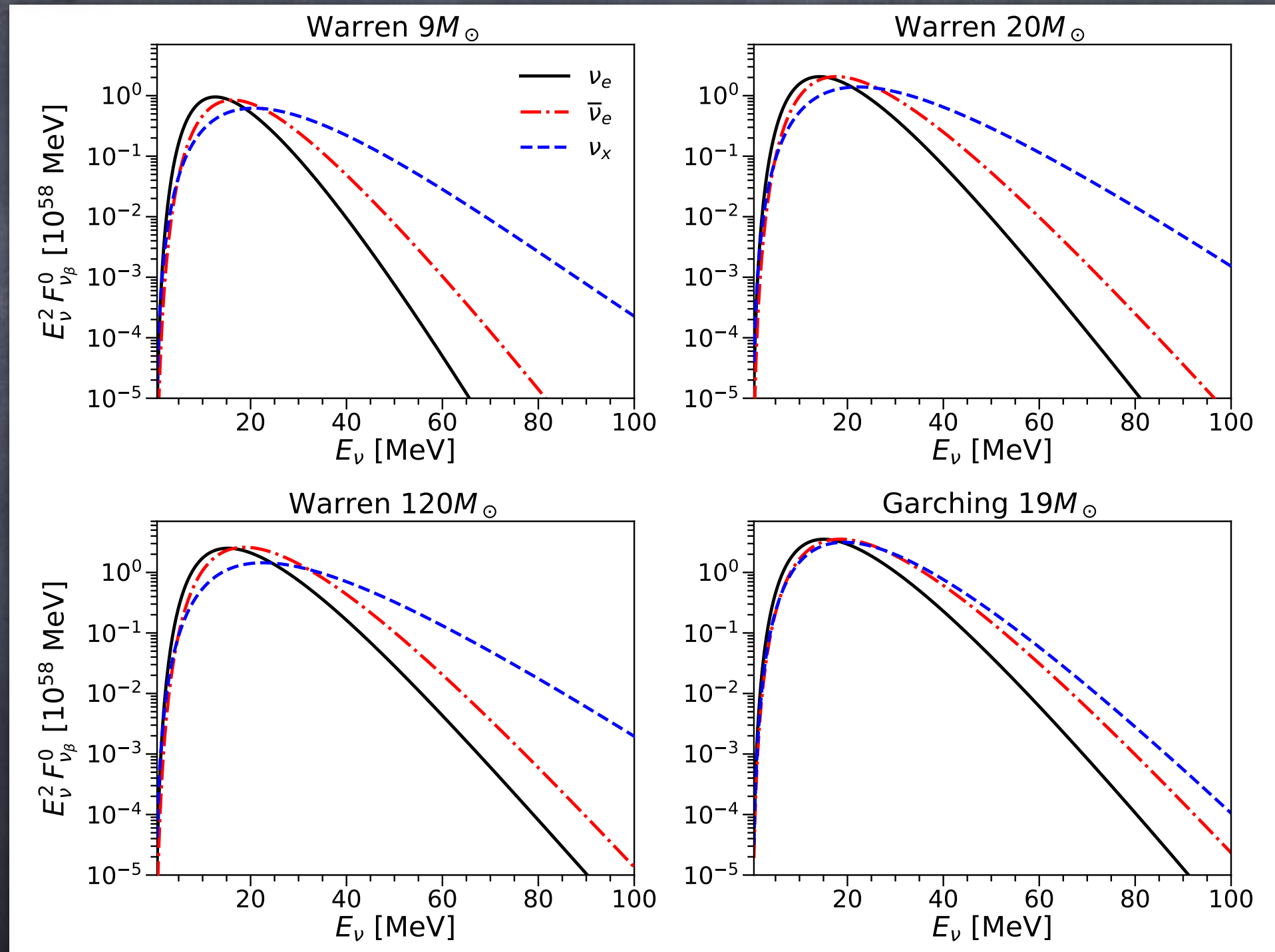
From the simulations of M. L. Warren, S. M. Couch, E. P. O'Connor and V. Morozova, *Astrophys. J.* 898:139, 2020

Supernova neutrino spectra at production

3 progenitor masses
and 2 simulations

M. L. Warren, S. M. Couch, E. P. O'Connor and V. Morozova, *Astrophys. J.* 898:139, 2020
R. Bollig et al., *Astrophys. J.* 915:28, 2021

time-integrated
spectra



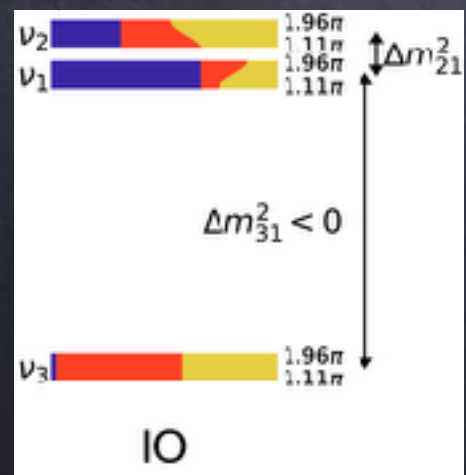
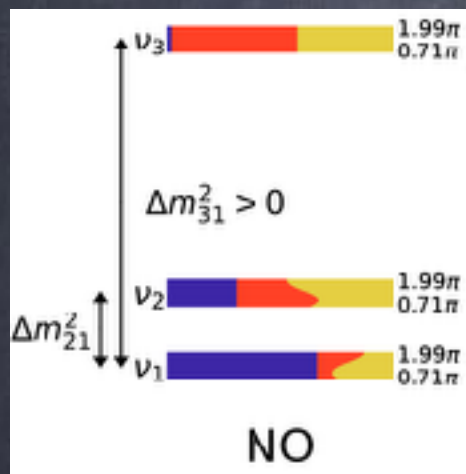
R. Hajjar, O. Mena and SPR, arXiv:2303.09369

Supernova neutrino spectra at Earth

Neutrinos are produced in a high-density medium, so the effective neutrino mixings are strongly suppressed and neutrinos are produced as mass eigenstates

Flavor conversions are fully adiabatic inside the SN,

so mass eigenstates can be identified with flavor spectra at production



$$F_{\nu_3}^O = F_{\nu_e}^O$$

$$F_{\nu_1}^O = F_{\nu_2}^O = F_{\nu_x}^O$$

$$F_{\bar{\nu}_1}^O = F_{\bar{\nu}_e}^O$$

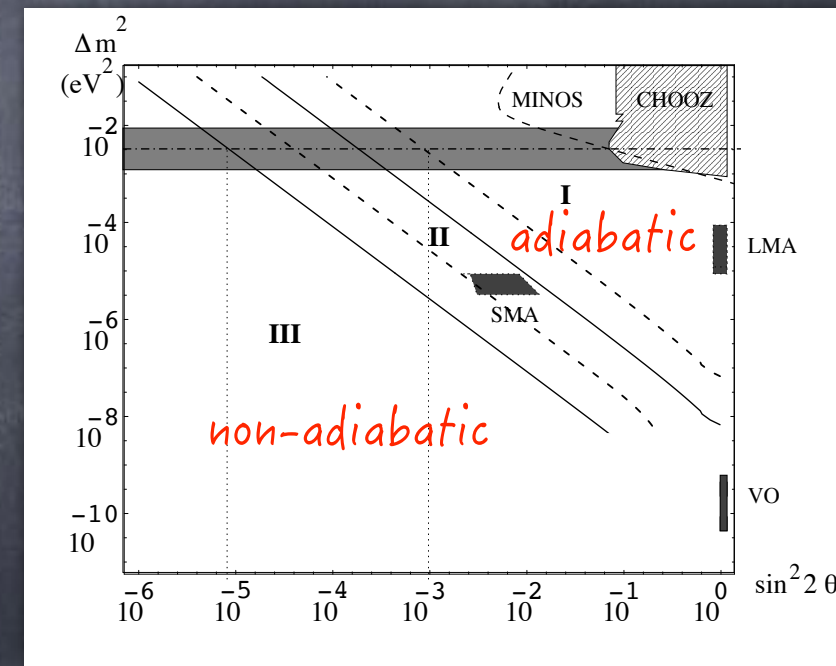
$$F_{\bar{\nu}_2}^O = F_{\bar{\nu}_3}^O = F_{\nu_x}^O$$

$$F_{\nu_2}^O = F_{\nu_e}^O$$

$$F_{\nu_1}^O = F_{\nu_3}^O = F_{\nu_x}^O$$

$$F_{\bar{\nu}_3}^O = F_{\bar{\nu}_e}^O$$

$$F_{\bar{\nu}_1}^O = F_{\bar{\nu}_2}^O = F_{\nu_x}^O$$



A. S. Dighe and A. Yu. Smirnov,
Phys. Rev. D62:033007, 2000

P. F. Salas et al., JHEP 02:071, 2021

Supernova neutrino FLAVOR spectra at Earth

$$F_{\nu_e}^D = p F_{\nu_e}^O + (1 - p) F_{\nu_x}^O$$

$$F_{\bar{\nu}_e}^D = \bar{p} F_{\bar{\nu}_e}^O + (1 - \bar{p}) F_{\nu_x}^O$$

$$p_{\oplus}^{\text{NO}} \equiv P_{\oplus}(\nu_3 \rightarrow \nu_e) \simeq \sin^2 \theta_{13}$$

$$p_{\oplus}^{\text{IO}} \equiv P_{\oplus}(\nu_2 \rightarrow \nu_e) \simeq \cos^2 \theta_{13} P_{\oplus}^{2\nu}$$

$$\bar{p}_{\oplus}^{\text{NO}} \equiv P_{\oplus}(\bar{\nu}_1 \rightarrow \bar{\nu}_e) \simeq \cos^2 \theta_{13} (1 - \bar{P}_{\oplus}^{2\nu})$$

$$\bar{p}_{\oplus}^{\text{IO}} \equiv P_{\oplus}(\bar{\nu}_3 \rightarrow \bar{\nu}_e) \simeq \sin^2 \theta_{13}$$

2-neutrino probability for constant density: $P_{\oplus}^{2\nu} = \sin^2 \theta_{12} + \sin 2\theta_{12}^{\oplus} \sin(2\theta_{12}^{\oplus} - 2\theta_{12}) \sin^2 \left(\pi \frac{L}{l_{\oplus}} \right)$

$$l_{\oplus} = \frac{\frac{4\pi E_{\nu}}{\Delta m_{21}^2}}{\sqrt{(\cos 2\theta_{12} \mp \epsilon \cos^2 \theta_{13})^2 + \sin^2 2\theta_{12}}}$$

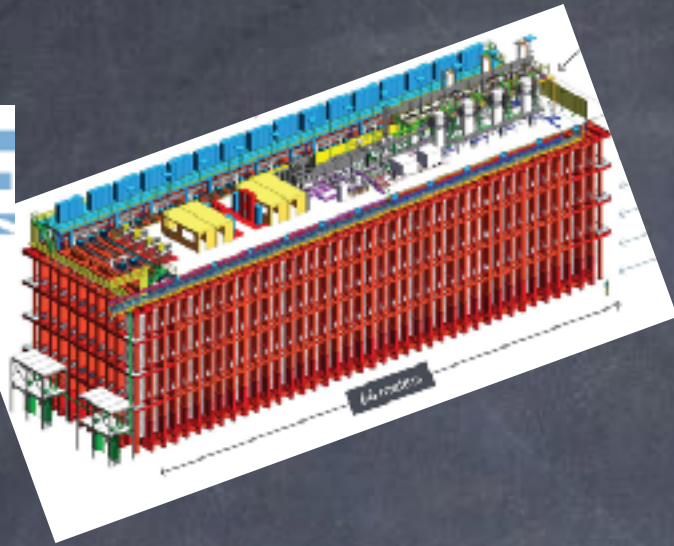
$$\sin 2\theta_{12}^{\oplus} = \frac{\sin 2\theta_{12}}{\sqrt{(\cos 2\theta_{12} \mp \epsilon \cos^2 \theta_{13})^2 + \sin^2 2\theta_{12}}}$$

$$\epsilon \equiv \frac{2E_{\nu}V}{\Delta m_{21}^2} \simeq 0.12 \left(\frac{E_{\nu}}{20 \text{ MeV}} \right) \left(\frac{Y_e \rho}{3 \text{ g/cm}^3} \right) \left(\frac{7.5 \times 10^{-5} \text{ eV}^2}{\Delta m_{21}^2} \right)$$

Regeneration factor: $f_{\text{reg}} \equiv p_{\oplus} - p_{\text{vac}} = \epsilon \cos^4 \theta_{13} \sin^2 2\theta_{12}^{\oplus} \sin^2 \left(\pi \frac{L}{l_{\oplus}} \right)$

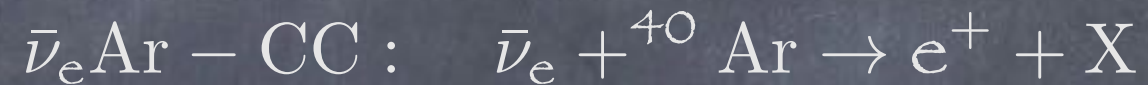
$$F_{\nu_e}^D - F_{\nu_e}^{\text{vac}} = f_{\text{reg}} (F_{\nu_e}^O - F_{\nu_x}^O)$$

Future neutrino detectors



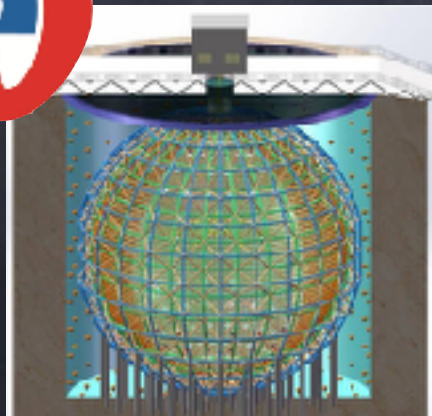
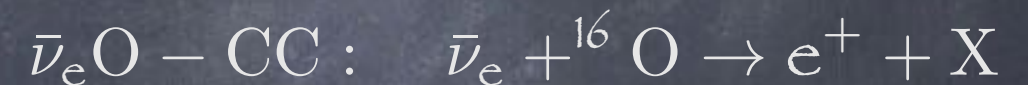
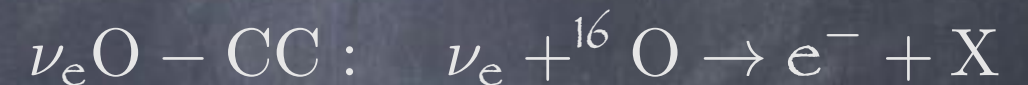
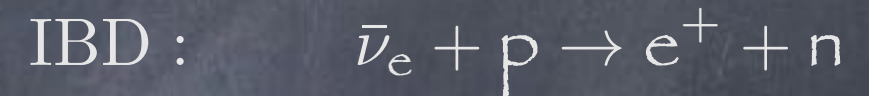
40 kton liquid Argon

$$\sigma_{\text{DUNE-Ar}}/E_\nu = 0.2$$



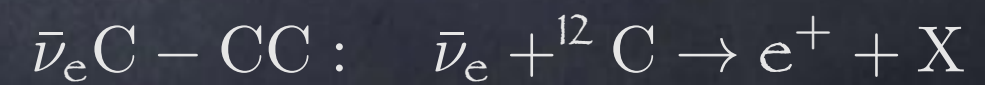
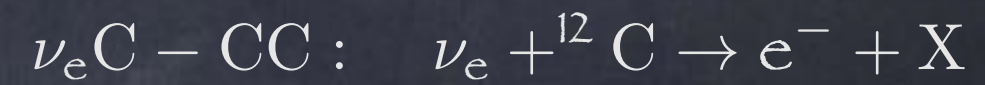
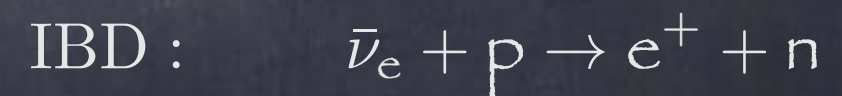
2x187 kton water Cherenkov
with Gadolinium

$$\sigma_{\text{HK}}/E_e \sim 0.08$$



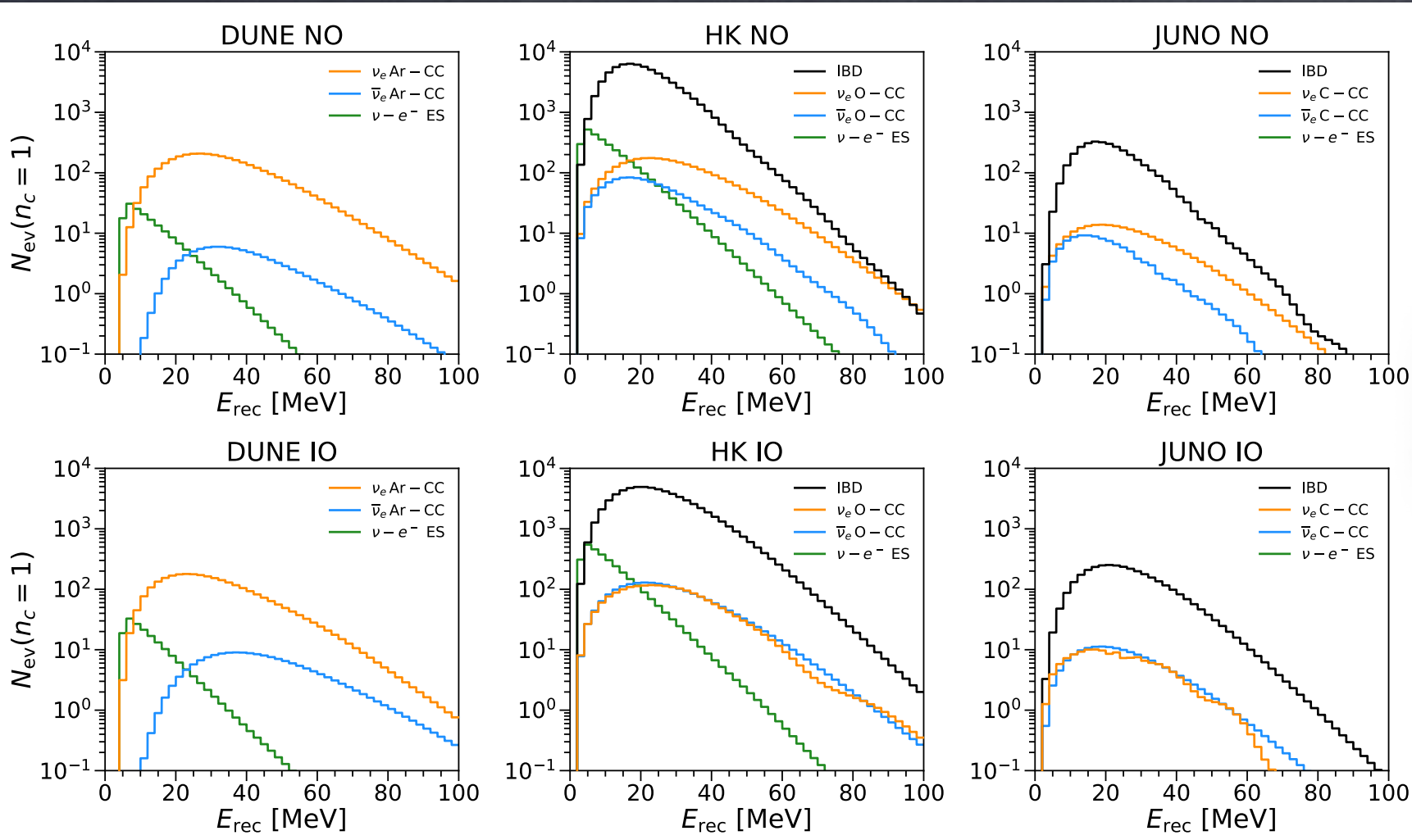
20 kton liquid scintillator

$$\sigma_{\text{JUNO}}/E_e \sim 0.01$$



Event distributions

(for W20 simulation at 10 kpc)



NO: matter effects for antineutrinos

Search for spectral distortions along the tails

IO: matter effects for neutrinos

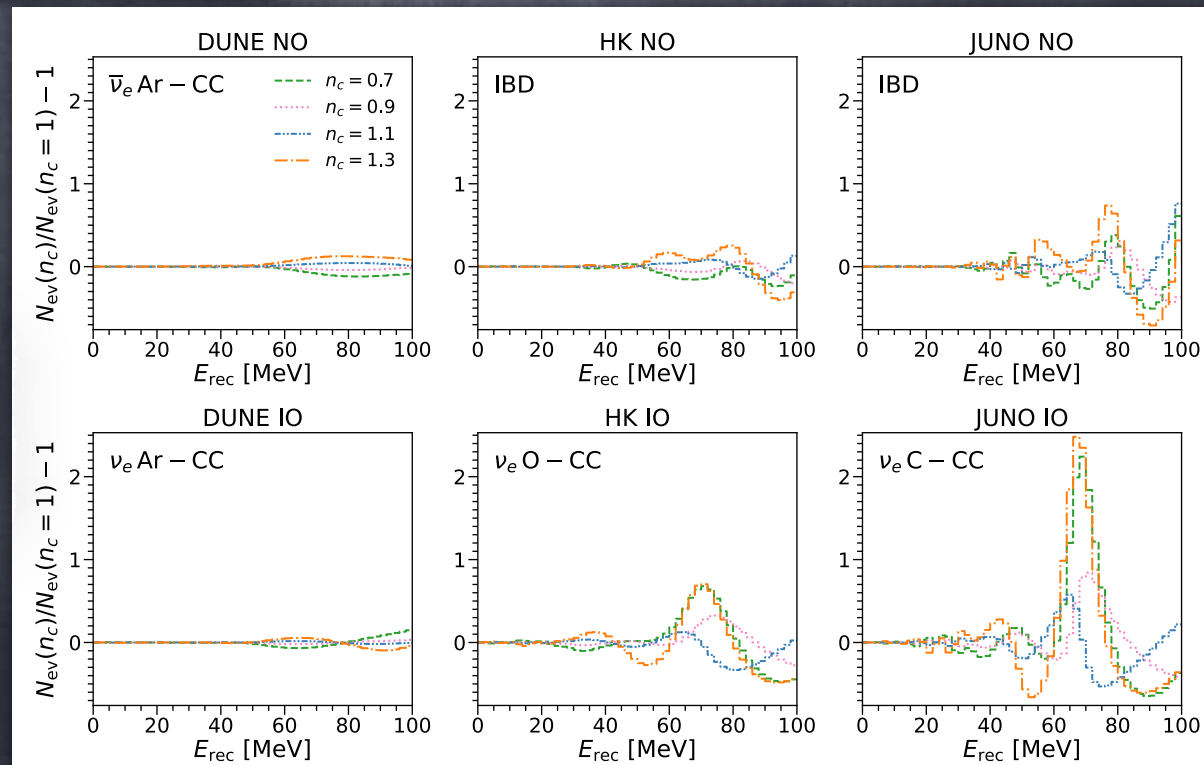
R. Hajjar, O. Mena and SPR, arXiv:2303.09369

Two-layer Earth model
imposing the Earth mass:

n_c = core density
normalization

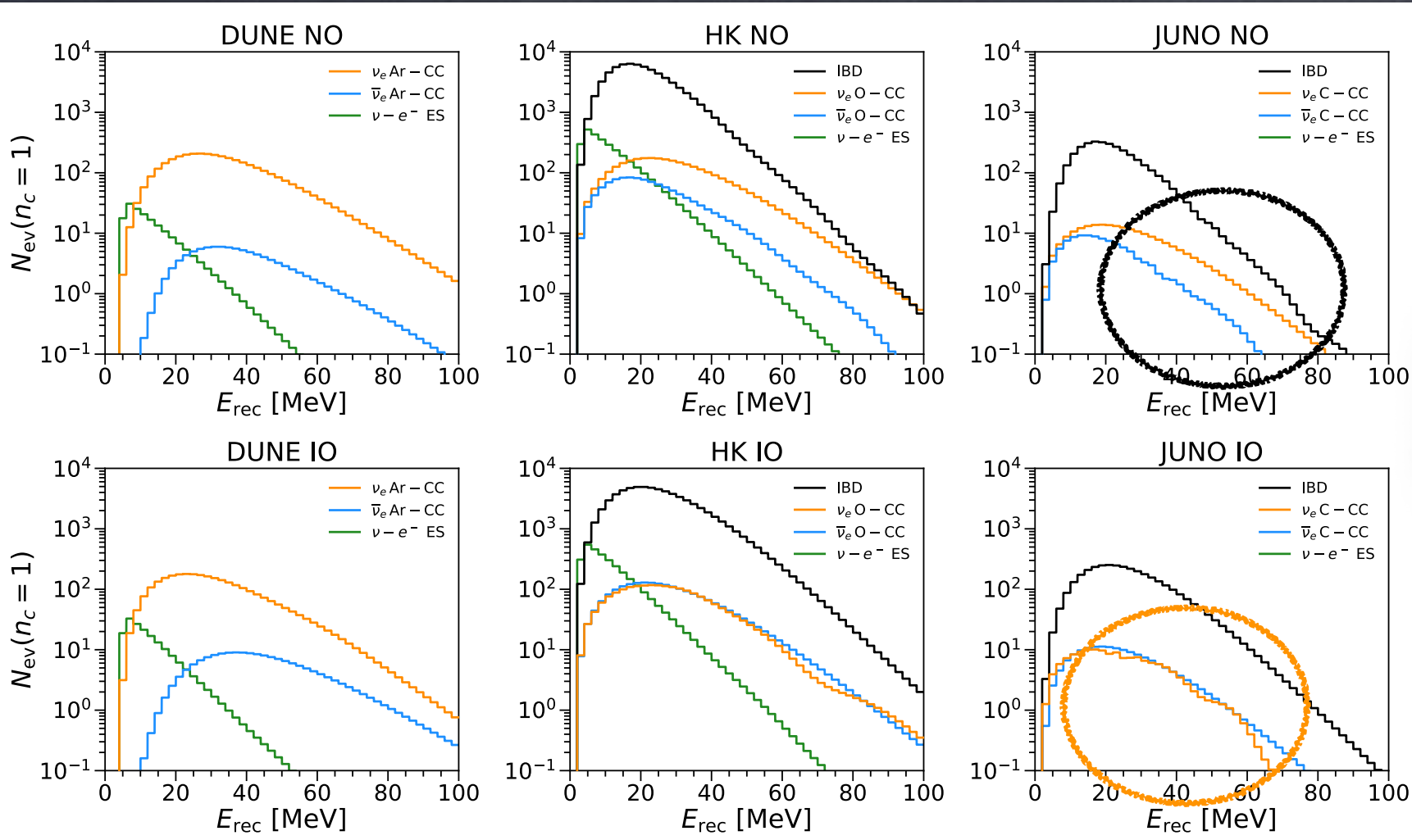
[$n_c = 1$ (PREM)]

energy resolution is critical
for Earth tomography



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(for W20 simulation at 10 kpc)



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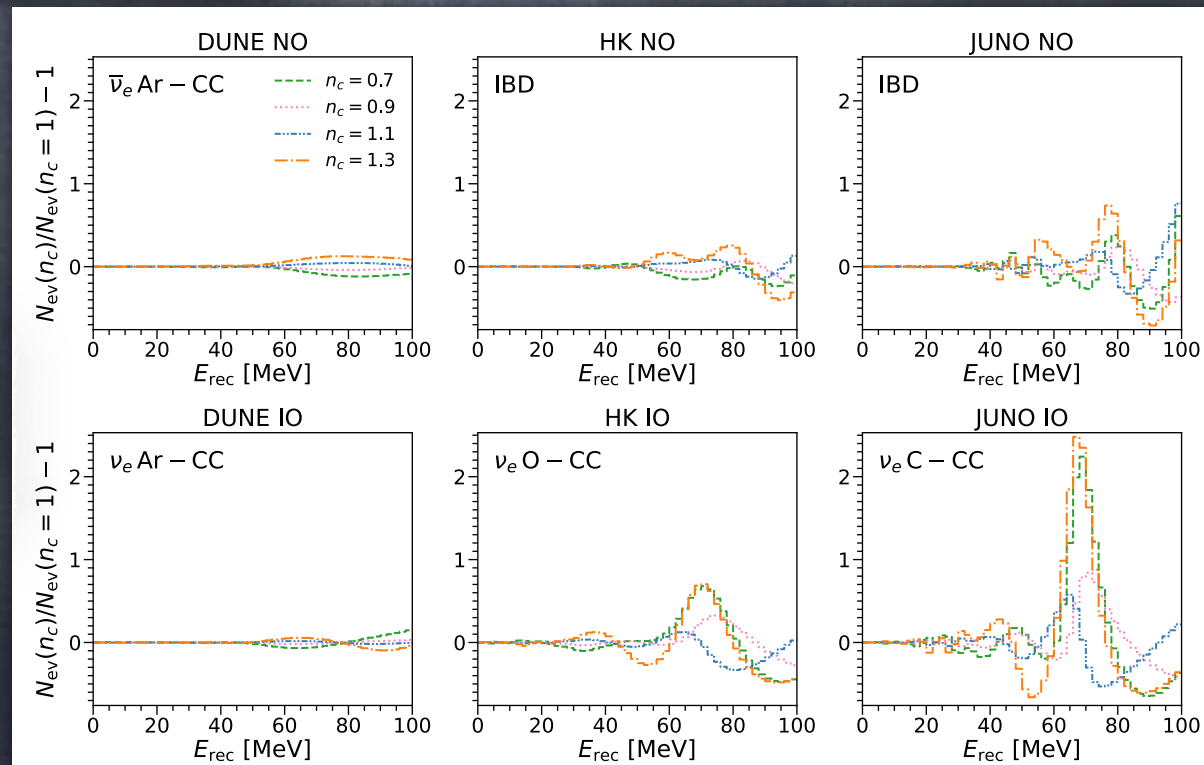
R. Hajjar, O. Mena and SPR, arXiv:2303.09369

Two-layer Earth model
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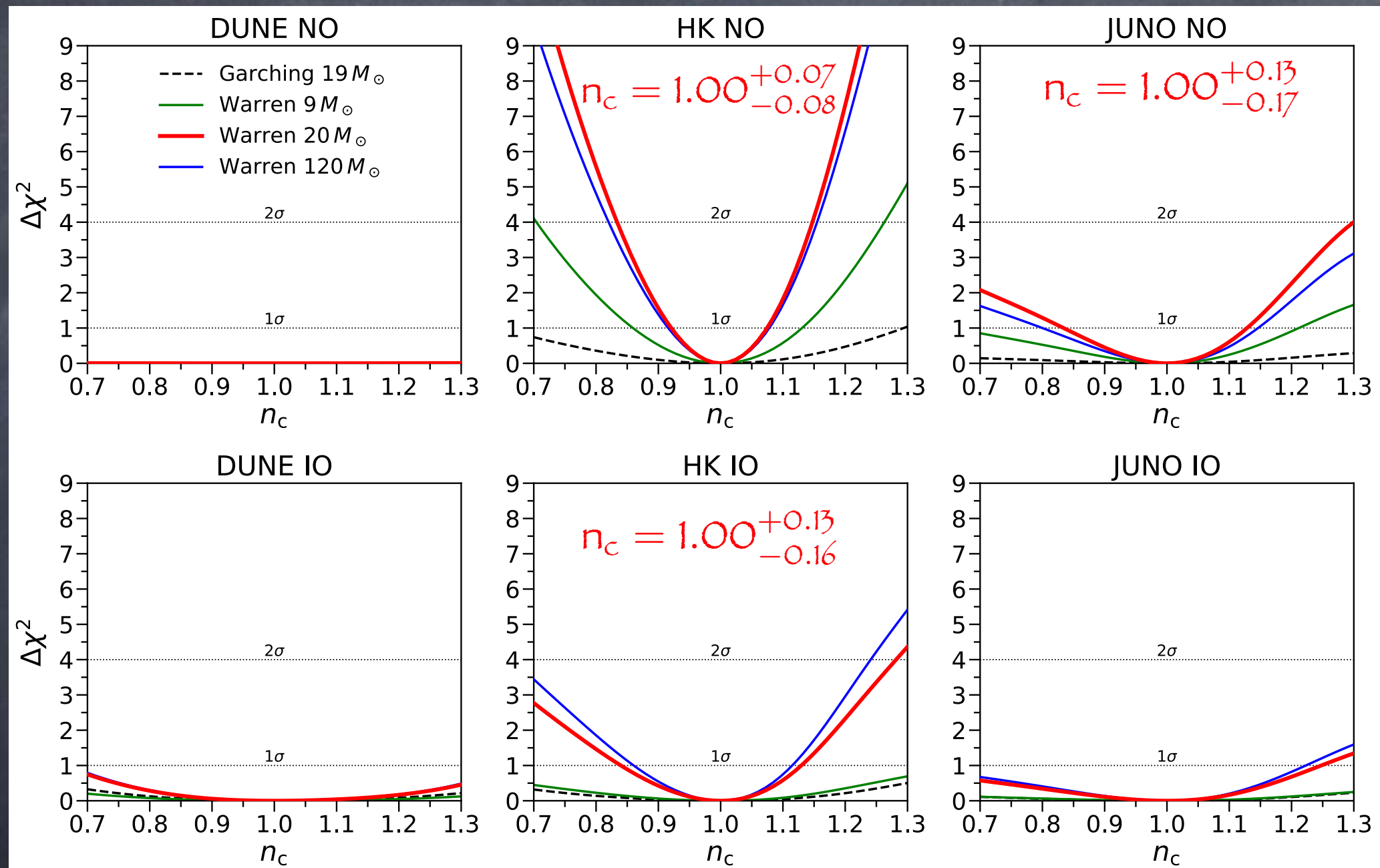
[$n_c = 1$ (PREM)]

energy resolution is critical
for Earth tomography



Dependence on the SN neutrino spectra

(in all analyses we assume a two-layer Earth model and we impose the constraint on the Earth mass)



R. Hajjar, O. Mena and SPR, arXiv:2303.09369

only if initial spectra are sufficiently different, Earth tomography would be possible

Dependence on the energy resolution

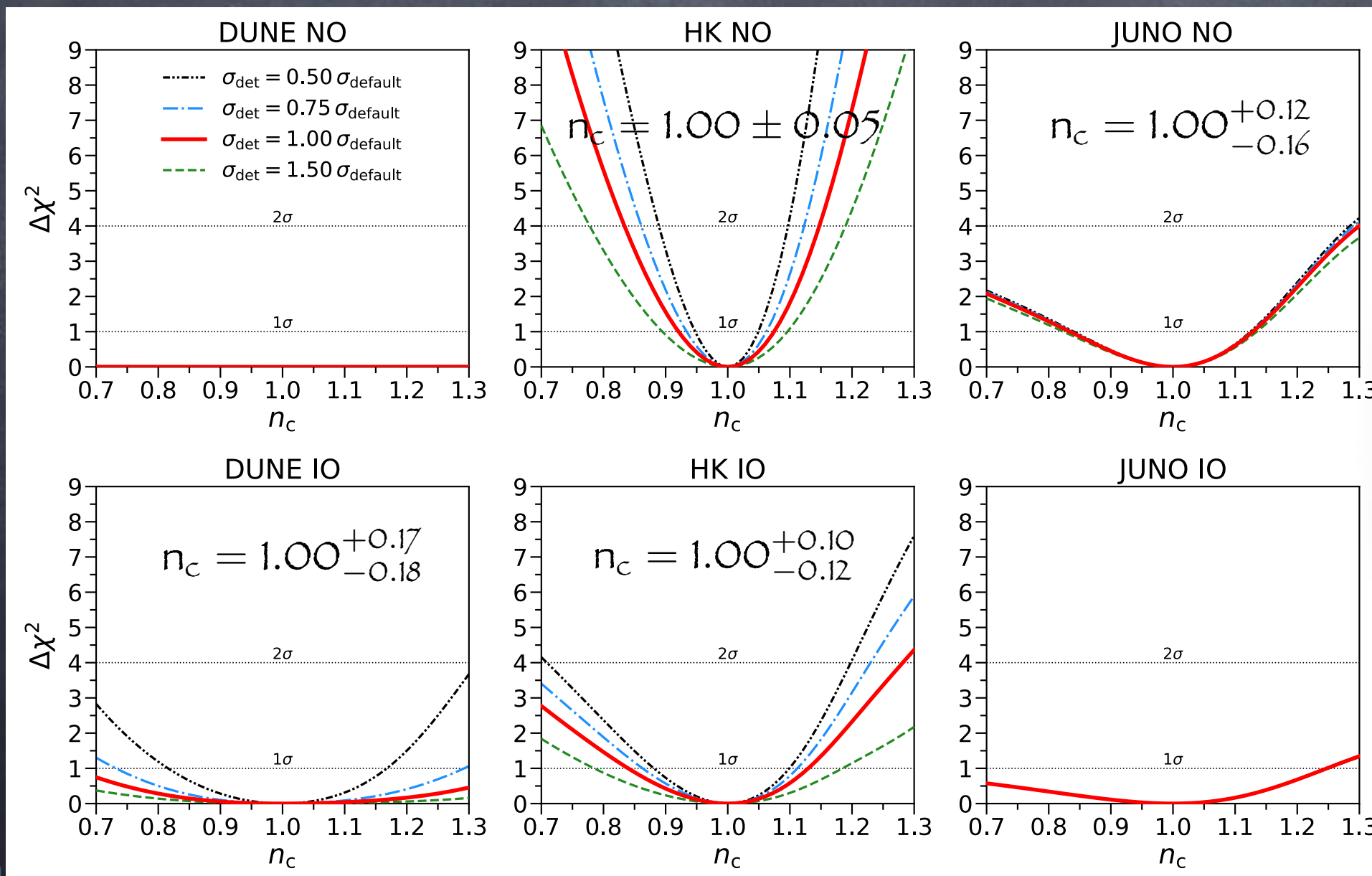
Attenuation (wash out) effect

A. N. Ioannisián and A Yu. Smirnov, Phys. Rev. Lett. 93:241801, 2004

A. N. Ioannisián, N. A. Kazarián, A Yu. Smirnov and D. Wyler, Phys. Rev. D71:033006, 2005

$$\lambda_{\text{att}} \equiv l_0 \left(\frac{E_\nu}{\pi \sigma_E} \right) = 4209 \text{ km} \left(\frac{E_\nu}{40 \text{ MeV}} \right) \left(\frac{7.5 \times 10^{-5} \text{ eV}^2}{\Delta m_{21}^2} \right) \left(\frac{0.1}{\sigma_E/E_\nu} \right)$$

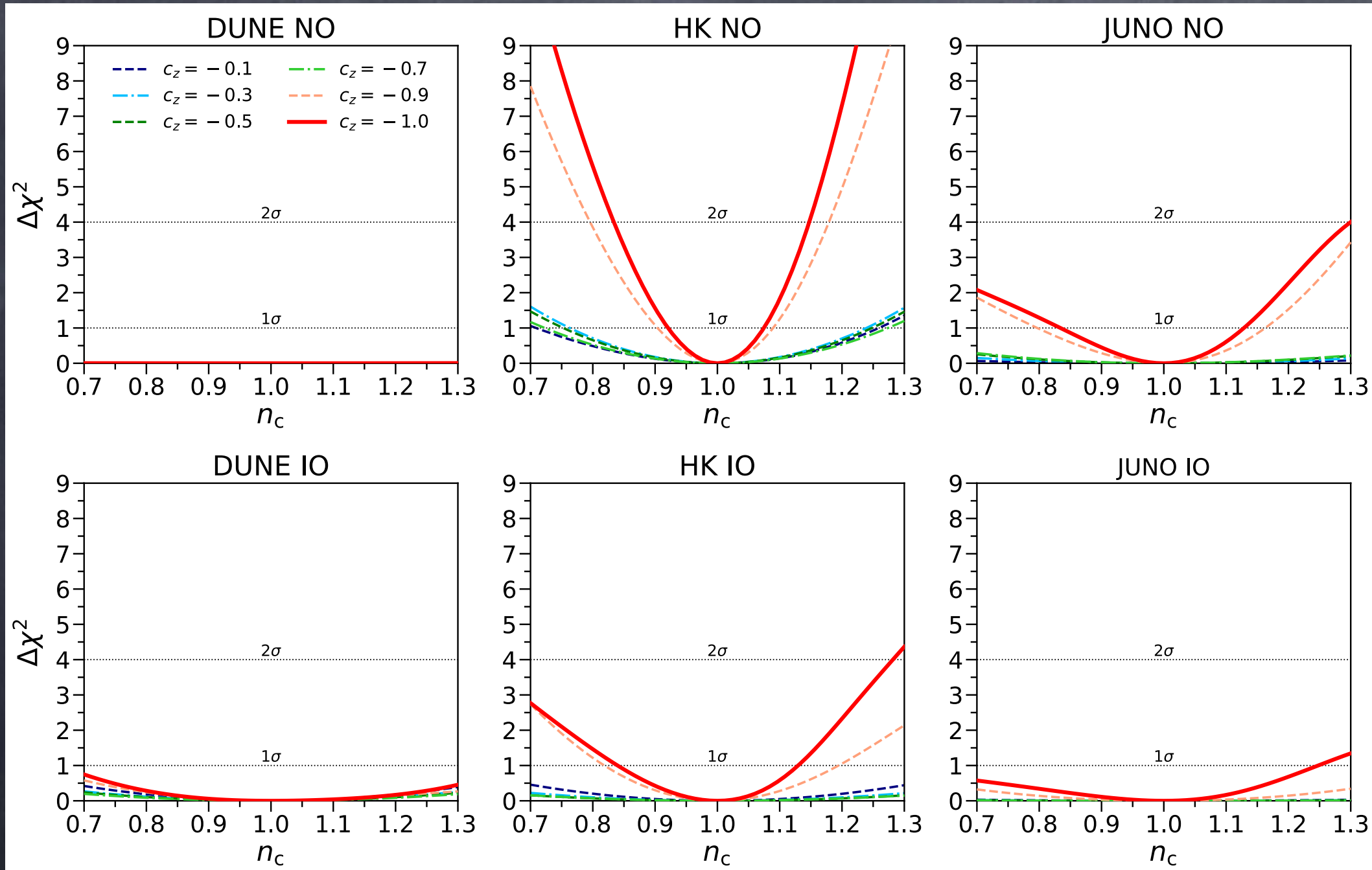
(for W20 simulation at 10 kpc)



Very little impact in JUNO: dominated by the neutrino energy spread in IBD

Dependence on the SN direction

(for W20 simulation at 10 kpc)



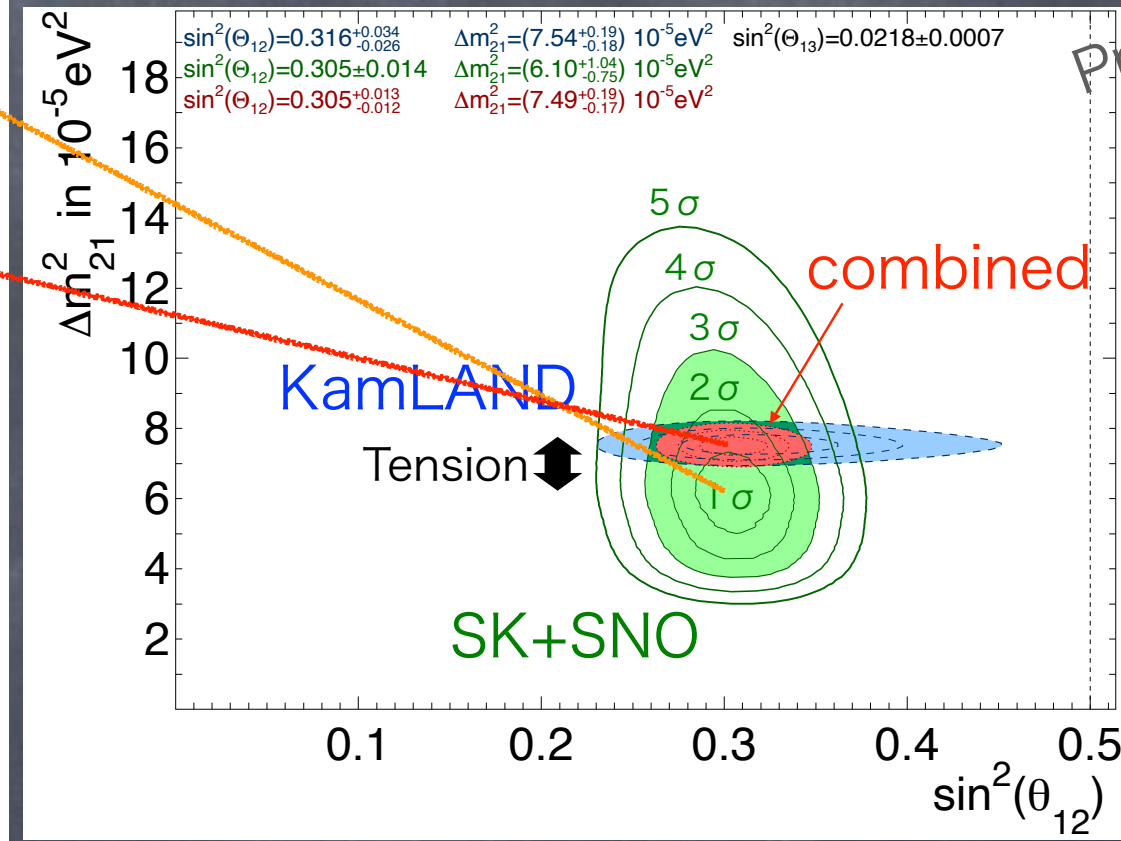
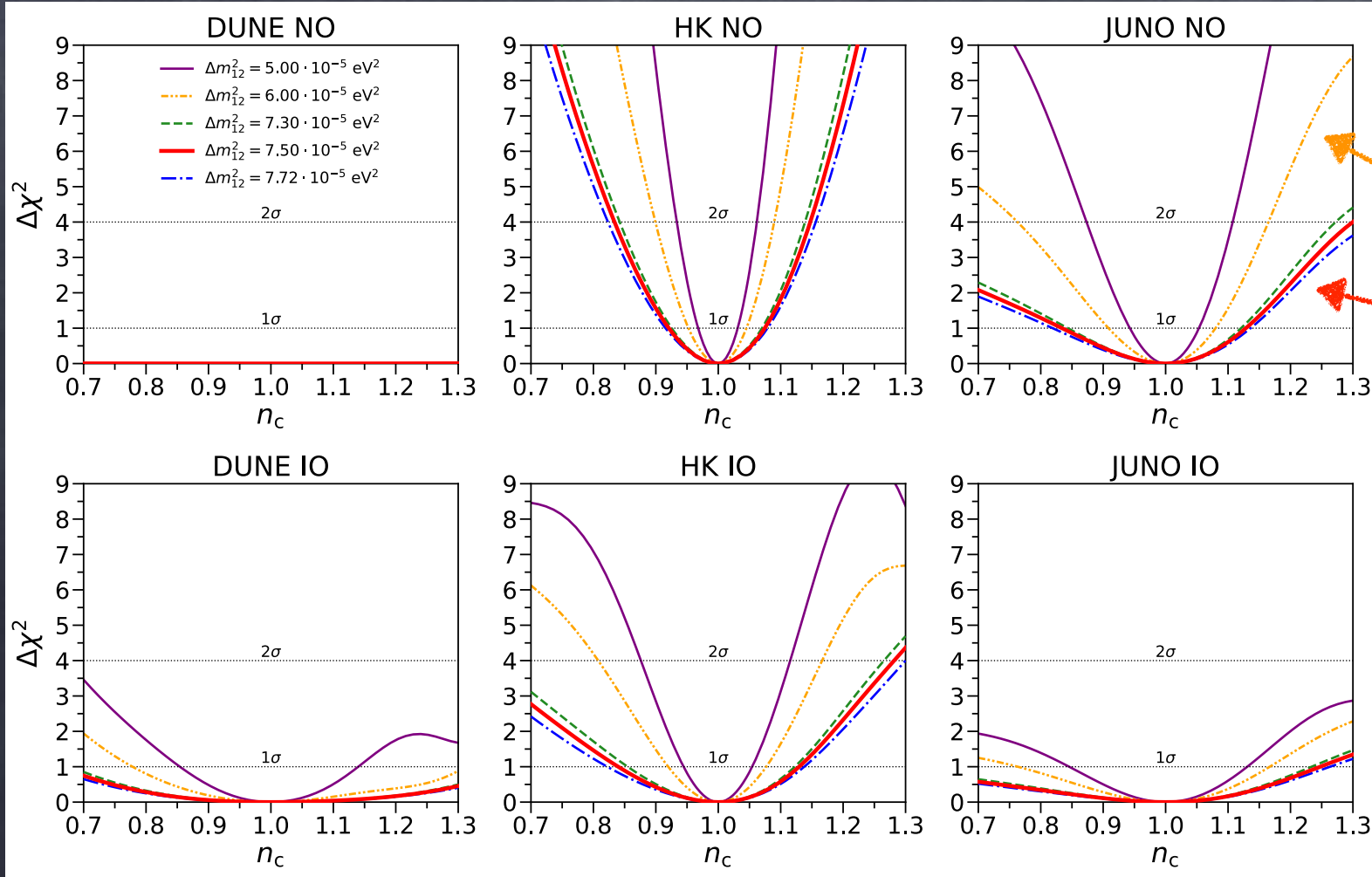
core-crossing
is required

R. Hajjar, O. Mena and SPR, arXiv:2303.09369

Δm_{21}^2

Dependence on neutrino mixing parameters

(for W20 simulation at 10 kpc)

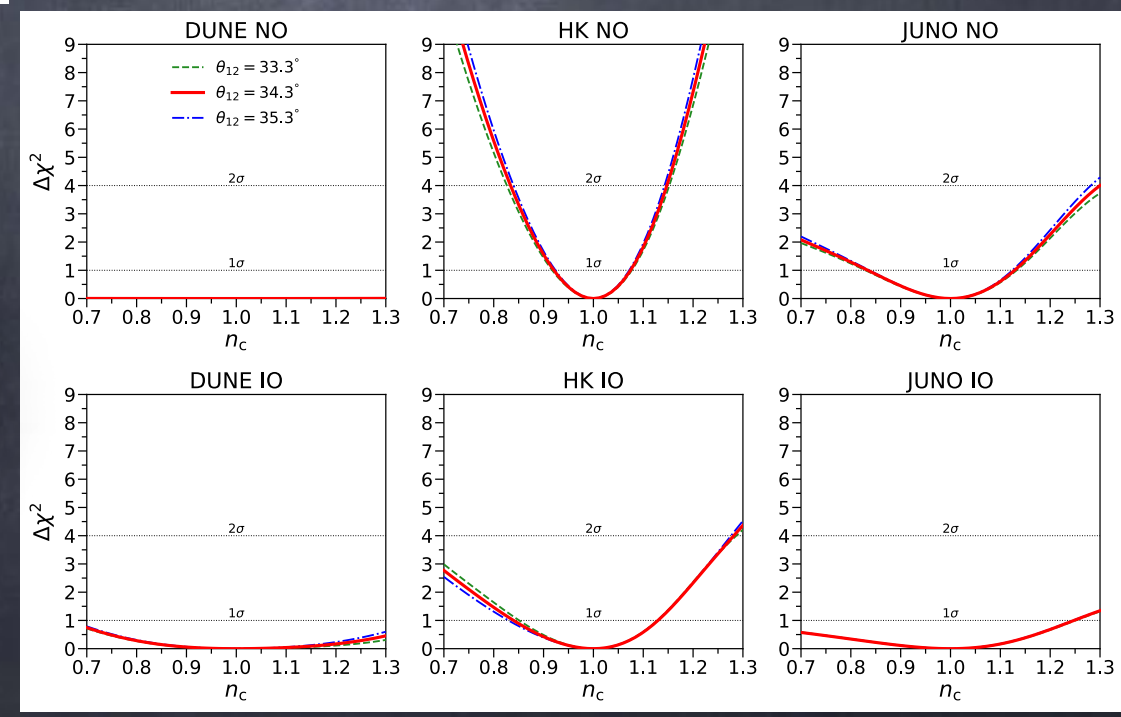


Y. Koshio, Talk at Neutrino 2022

R. Hajjar, O. Mena and SPR, arXiv:2303.09369

 θ_{12}

very mild effect due to uncertainties



CONCLUSIONS

Neutrinos allow us to look inside the Earth in a completely different manner from standard techniques

Main neutrino tomography approaches:
oscillation and absorption tomography

After 45 years of being proposed, we performed the first Earth (absorption) tomography with neutrinos:
first measurement of the Earth's mass using only the weak force!

Analysis with 1 year of data,
but 10 years of data already collected by IceCube
... and other future experiments: KM3NeT, Baikal-GVD

Promising prospects with future detectors for neutrino oscillation tomography using atmospheric and supernova neutrinos

Edmund Halley,

Philosophical Transactions of the Royal Society of London XVII:195, 563 (1692):

“what curiosity in the structure, what accuracy in the mixture and composition of the parts, ought not we to expect in the fabric of this globe”

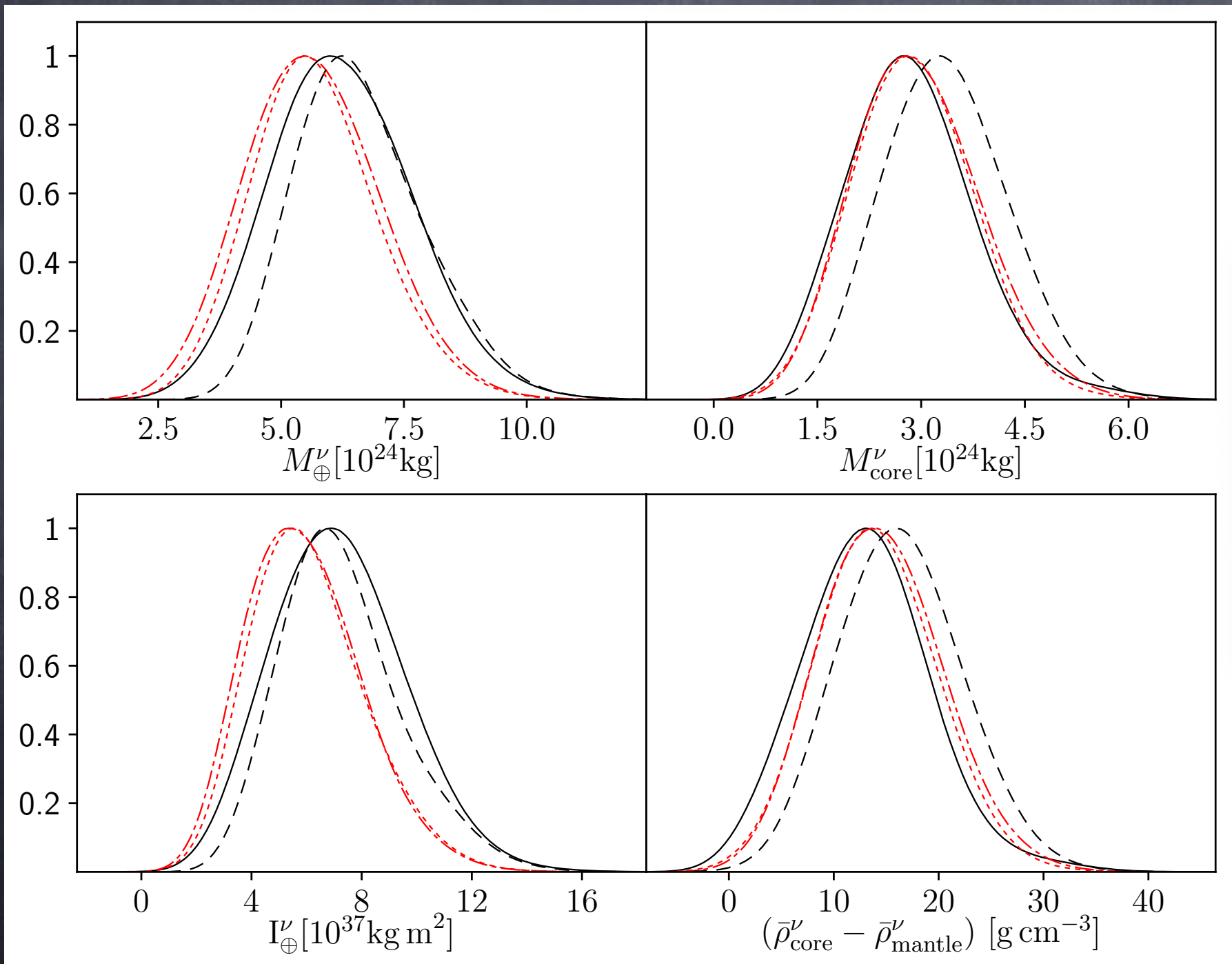
Thanks!

Extras

IMPACT OF DISCRETE SYSTEMATICS

Different atmospheric neutrino fluxes

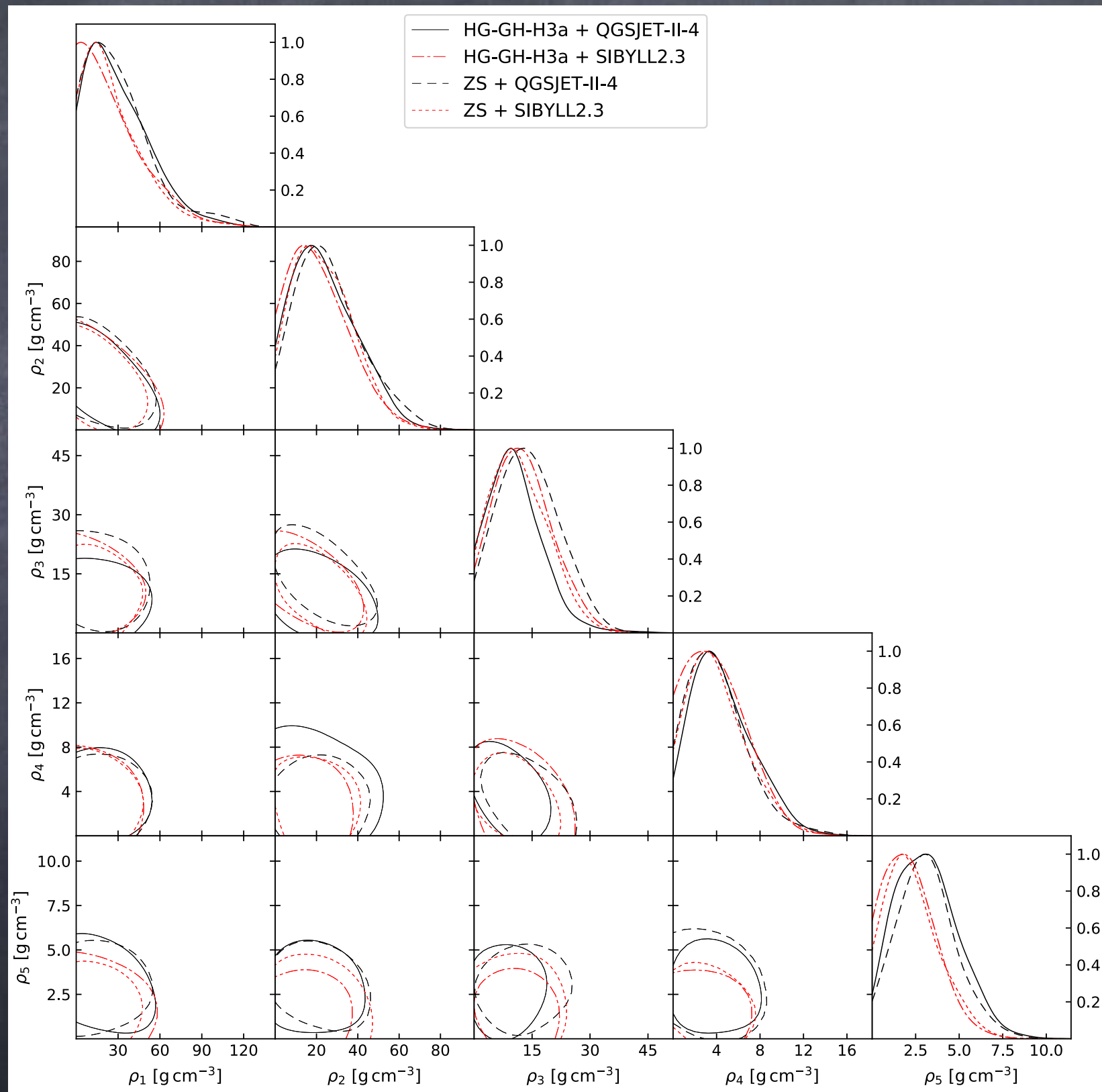
- HG-GH-H3a + QGSJET-II-4
- - - HG-GH-H3a + SIBYLL2.3
- - - ZS + QGSJET-II-4
- - - ZS + SIBYLL2.3



systematics
 (mainly driven by the
 hadronic-interaction
 modeling)
 ~ (20-30) %

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

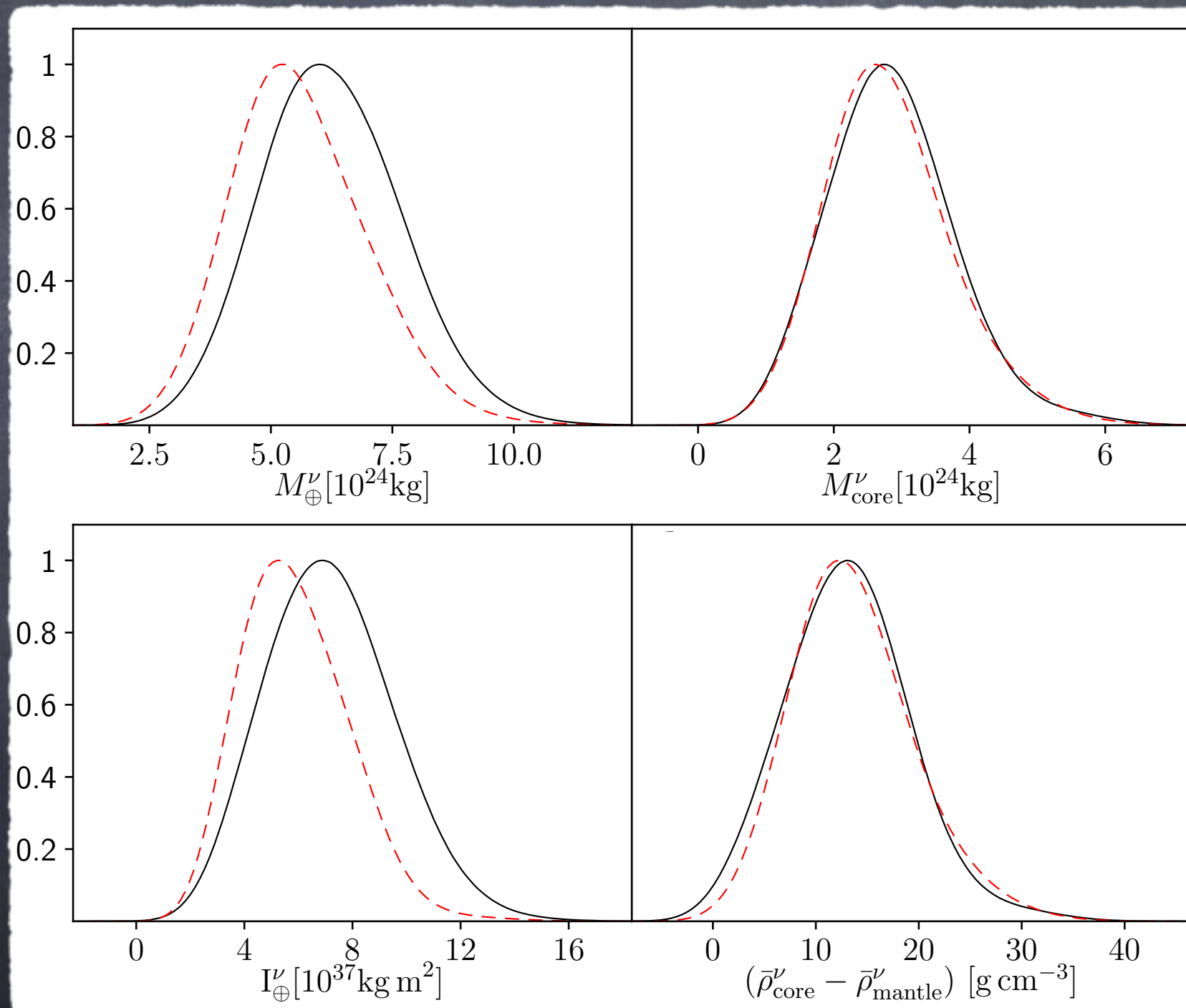
NEUTRINO FLUXES: CORRELATIONS



A. Donini, SPR and J. Salvado, *Nature Physics* 15:37, 2019

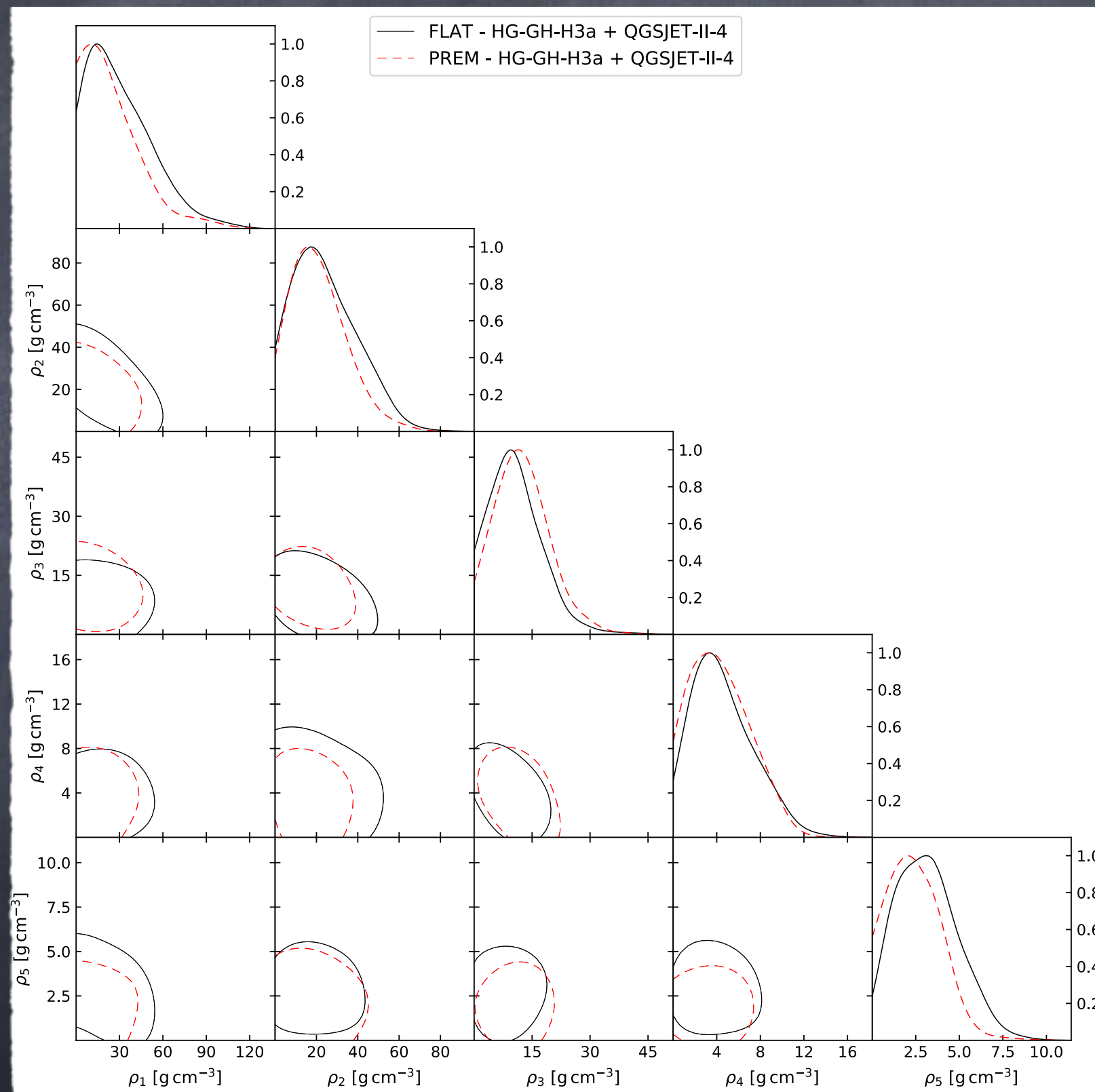
IMPACT OF DENSITY PROFILE

— FLAT - HG-GH-H3a + QGSJET-II-4
- - - PREM - HG-GH-H3a + QGSJET-II-4



A. Donini, SPR and J. Salvado, *Nature Physics* 15:37, 2019

IMPACT OF DENSITY PROFILE: CORRELATIONS



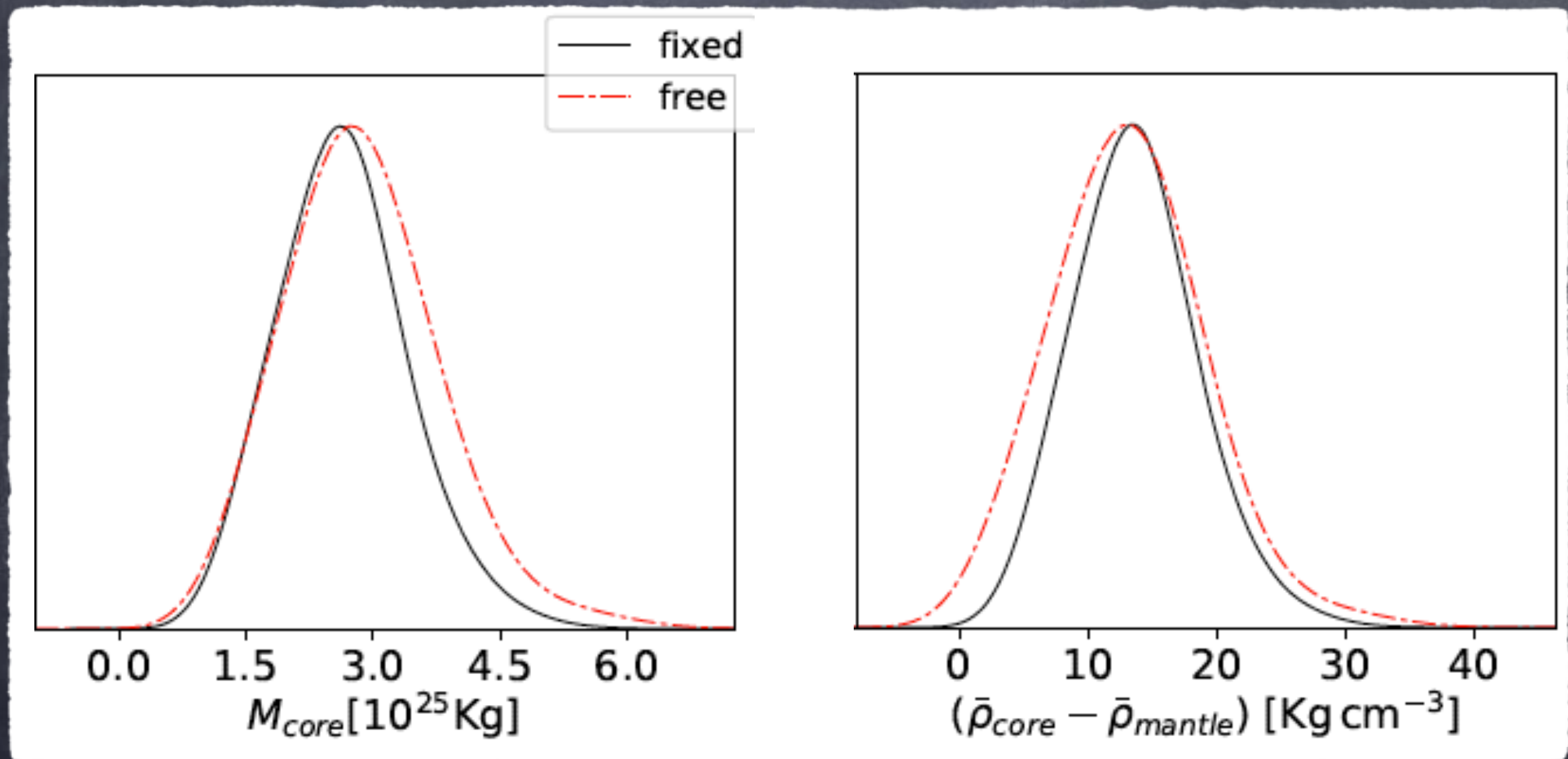
A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

IMPACT OF SYSTEMATICS

	Piecewise flat Earth's profile				PREM Earth's profile
	HG-GH-H3a + QGSJET-II-04	HG-GH-H3a + SIBYLL2.3	ZS + QGSJET-II-04	ZS + SIBYLL2.3	HG-GH-H3a + QGSJET-II-04
M_{\oplus}^{ν} [10^{24} kg]	$6.0^{+1.6}_{-1.3}$	$5.5^{+1.5}_{-1.3}$	$6.2^{+1.4}_{-1.2}$	$5.5^{+1.3}_{-1.2}$	$5.3^{+1.5}_{-1.3}$
M_{core}^{ν} [10^{24} kg]	$2.72^{+0.97}_{-0.89}$	$2.79^{+0.98}_{-0.85}$	$3.27^{+0.92}_{-0.89}$	$2.84^{+0.89}_{-0.88}$	$2.62^{+0.97}_{-0.84}$
I_{\oplus}^{ν} [10^{37} kg cm ²]	6.9 ± 2.4	$5.4^{+2.3}_{-1.9}$	$6.7^{+2.3}_{-2.0}$	$5.5^{+2.2}_{-1.9}$	$5.3^{+2.3}_{-1.7}$
$\bar{\rho}_{\text{core}}^{\nu} - \bar{\rho}_{\text{mantle}}^{\nu}$ [g/cm ³]	$13.1^{+5.8}_{-6.3}$	$14.0^{+6.0}_{-5.9}$	$15.9^{+6.0}_{-5.9}$	$13.5^{+6.1}_{-5.5}$	$12.3^{+6.3}_{-5.4}$
p – value mantle denser than core	1.1×10^{-2}	2.4×10^{-3}	9.4×10^{-4}	4.6×10^{-3}	3.8×10^{-3}

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

ADDING GRAVITY CONSTRAINTS



Density of the mantle determined at $\sim 4\%$