



What is spacetime? and how does it come about? the quest for quantum gravity

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Quantum Gravity: the problem

gravitational physics well described by General Relativity

- basis for our description of astrophysics and cosmology
- predicts amazing new phenomena (deflection of light, gravitational distortion of space and time measurements, gravitational waves, black holes, expansion of universe,)

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R = \frac{8\pi G}{c^4}T_{\mu\nu} - \Lambda g_{\mu\nu}$$



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what do we learn from GR?

- gravitational interaction described (macroscopically) by geometry of spacetime
 - continuum, local picture of spacetime adequate
- dynamics and (local) interaction with matter described by Einstein's equations: "matter tells spacetime how to curve, spacetime tells matter how to move"
- spacetime itself is physical system
- there is no fixed background over which things happen, if not as approximation
 - deeper understanding of gravity is deeper understanding of space and time

Space and Time in General Relativity



GR key ingredients: only dynamical fields + diffeomorphism invariance

- no preferred time/space direction infinity of equally valid local notions of time/space
- only dynamical and diffeo-invariant quantities are physical (correspond to predictions of theory)
- manifold points, paths on manifolds, values of fields at points or regions, are -not- physical per se
- they have to be made physical (given some operational meaning) by defining them via dynamical fields

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two incompatible conceptual (and mathematical) frameworks for space, time, geometry and matter

GR

spacetime (geometry) is a dynamical entity itself

there are no preferred temporal (or spatial) directions

physical systems are local and locally interacting

everything (incl. spacetime) evolves deterministically

all dynamical fields are continuous entities

every property of physical systems (incl. spacetime) and of their interactions can be precisely determined, in principle

QFT

spacetime is fixed background for fields' dynamics

evolution is unitary (conserved probabilities) with respect to a given (preferred) temporal direction

nothing can be perfectly localised

everything evolves probabilistically

interaction and matter fields are made of "quanta"

every property of physical systems and their interactions is intrinsically uncertain, in general

so, what are, really, space, time, geometry, and matter?

several open physical issues, at limits of GR and QFT or at interface (where both are expected to be relevant)

• breakdown of GR for strong gravitational fields/large energy densities

spacetime singularities - black holes, big bang - quantum effects expected to be important





- divergences in QFT what happens at high energies? how does spacetime react to such high energies?
- what happens to quantum fields close to big bang? what generates cosmological fluctuations, and how?

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- divergences in QFT what happens at high energies? how does spacetime react to such high energies?
- what happens to quantum fields close to big bang? what generates cosmological fluctuations, and how?
- no proper understanding of interaction of geometry with quantum matter, if gravity is not quantized

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R + \Lambda g_{\mu\nu} = \frac{8\pi G}{c^4} \langle \Psi | \hat{T}_{\mu\nu} | \Psi \rangle$$
 not a consistent theory



hints of disappearance of spacetime itself, more radical departure from GR and QFT

• challenges to "localization" in semi-classical GR

minimal length scenarios

- spacetime singularities in GR
- black hole thermodynamics

black holes satisfy thermodynamic relations

breakdown of continuum itself?

if spacetime itself has (Boltzmann) entropy, it has microstructure if entropy is finite, this implies discreteness

• Einstein's equations as equation of state (Jacobson et al)

GR dynamics is effective equation of state for any microscopic dofs collectively described by a spacetime, a metric and some matter fields

fundamental discreteness of spacetime? is spacetime itself "emergent" from non-spatiotemporal, non-geometric, quantum building blocks ("atoms of space")?



if spacetime (with its continuum structures, metric, matter fields, topology) is emergent,

even large scale features of gravitational dynamics can (and maybe should) have their origin in more fundamental ("atomic") theory

cannot trust most notions on which effective quantum field theory is based (locality, separation of scales, etc)

e.g. : dark matter (galactic dynamics), dark energy (accelerated cosmological expansion) - either 95% of the universe is not known, or we do not understand gravity at large scales





e.g. cosmological constant as possible large scale manifestation of microscopic (quantum gravity) physics

What has to change (in going from GR to QG)

- quantum fluctuations (superpositions) of spacetime structures
 - geometry (areas, distances, volumes, curvature, etc)
 - causality (causal relations)
 - topology?
 - dimensionality?
- breakdown of continuum description of spacetime?
 - fundamental discreteness? of space only? of time as well?
 - entirely new degrees of freedom "atoms of space"? which ones?
 - but then, how does usual spacetime "emerge"?
- new QG scale: Planck scale



What could be the relevant scale for QG effects?

based on current theories, i.e. GR and QFT: Planck scale

 \sim where both GR and QFT are relevant

$$l = \sqrt{\frac{Gh}{c^3}} = 3.99 \times 10^{-33} \ cm = 3.99 \times 10^{-35} \ m,$$

$$m = \sqrt{\frac{Ch}{G}} = 5.37 \times 10^{-5} \ g = 5.37 \times 10^{-8} \ kg,$$

$$t = \sqrt{\frac{Gh}{c^5}} = 1.33 \times 10^{-43} \ \text{sec},$$

$$T = \frac{1}{k} \sqrt{\frac{c^5h}{G}} = 3.60 \times 10^{32} \ \text{deg K}.$$

in principle, Quantum Gravity from cosmological scales to Planck scale



cautionary remark: this is on the basis of current physics, tested only up to very different scales (compared to Planck scale) and based on concepts that may not be valid beyond such scales

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no spacetime or geometry?

how can we even talk of "scales"? total failure of effective field theory intuition?



Quantum Gravity and the nature of spacetime

Quantum Gravity is not about "quantizing GR", but about understanding the "microstructure of spacetime"

quantum gravity = microscopic theory of pre-geometric quantum degrees of freedom ("quantum (field) theory of atoms of space")

the goals are:

- identify the fundamental (quantum) degrees of freedom of spacetime
 the "atoms of space (or spacetime)" and their quantum dynamics
- show that an approximately continuum, classical spacetime emerges
- show that GR is good effective description of emergent spacetime dynamics



gravitational field result of collective dynamics



spacetime and geometry are emergent entities, obtained after coarse graining of fundamental, non-spatiotemporal dofs

candidate "atoms of quantum space" --- how to recover continuum spacetime (and GR)?

Quantum Gravity: variety of approaches

Quantum Gravity: contemporary approaches



String theory (and related)

(....., a lot of people,)

starting idea: quantum theory of strings, interacting and propagating on given spacetime background

string excitations: particles of any spin/mass; incl. graviton = quantum of gravitational field

consistent (around flat space) and finite perturbation theory in 10d

background spacetime satisfies GR equations



many different (consistent) versions (different matter content, different symmetries) - all require supersymmetry and spacetime dimension > 4

central result: spacetime as seen by strings, as opposed to point particles/fields, has very different topology and geometry; e.g. distances smaller than minimal string length cannot be probed

many non-perturbative aspects; extended (d>1) configurations (branes) as fundamental as strings, and interacting with them (Polchinski,, 1994 -)

String theory (and related)

dualities between various string theories and supergravity: different aspects of same underlying fundamental theory (M-theory)?

dualities show that spacetime topology and dimension are themselves dynamical

AdS/CFT correspondence: a (gauge) QFT with conformal invariance on 4d flat space could fully encode the physics of a gravitational theory in 5d (with AdS boundary); viceversa, semiclassical GR (with extra conditions) could describe the physics of a peculiar many-body quantum system in different dimension

is the world holographic? are gravity and gauge theories equivalent? many results and new directions

large number of mathematical results and radical generalisation of quantum field theory





QG as (Effective) QFT - Asymptotic Safety Scenario

Quantum gravity is perturbatively non-renormalizable, as a QFT for the metric field (e.g. around Minkowski space)

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$$

can still be used as effective field theory (incorporating quantum (loop) corrections) with fixed cutoff

$$S_{grav} = \int d^4x \sqrt{g} \left[\Lambda + \frac{2}{\kappa^2} R + c_1 R^2 + c_2 R_{\mu\nu} R^{\mu\nu} + \dots + \mathscr{L}_{matter} \right]$$

J. Donoghue, C. Burgess,

and it is predictive (eg graviton scattering and corrections to Newtonian potential)

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Can it make sense non-perturbatively? Asym

Asymptotic safety scenario

S. Weinberg, M. Reuter, C. Wetterich, R. Percacci, D. Benedetti, A. Eichhorn,

Effective action (~ covariant path integral) $\Gamma_k(g_{\mu\nu}; g_i^{(n)}) = \sum_{n=0}^{\infty} \sum_i g_i^{(n)}(k) \mathcal{O}_i^{(n)}(g_{\mu\nu})$

(a)
$$\partial_t \Gamma_k = \frac{1}{2} \operatorname{STr} \left(\frac{\delta^2 \Gamma_k}{\delta \phi_A \delta \phi_B} + R_k^{AB} \right)^{-1} \partial_t R_k^{BA}$$

as solution to non-perturbative RG equations (e.g. Wetterich eqn)

look for non-Gaussian UV fixed points \tilde{G}

necessarily studied in various truncations (+ matter fields etc)

eg Einstein-Hilbert truncation

$$\Gamma_k^{(n \le 2)} = \int d^d x \sqrt{g} \left[2Z_g \Lambda - Z_g R + \frac{1}{2\lambda} C^2 + \frac{1}{\xi} R^2 \right]$$



QG as canonical and/or covariant quantization of GR

Canonical quantization of GR:

3+1 splitting of manifold and fields; canonical phase space of 3-metric and extrinsic curvature

$$[\hat{h}_{ab}(x), \hat{p}^{cd}(y)] = i\hbar \delta^c_{(a} \delta^d_{b)} \delta(x, y)$$
 wavefunctions depend in 3-metric or extrinsic curvature

symmetries and dynamics fully encoded in diffeomorphism and Hamiltonian constraints

$$\hat{\mathcal{H}}_{\perp}\Psi := \left(-16\pi G\hbar^2 G_{abcd}\frac{\delta^2}{\delta h_{ab}\delta h_{cd}} - \frac{\sqrt{h}}{16\pi G}({}^{(3)}R - 2\Lambda)\right)\Psi = 0,$$
$$\hat{\mathcal{H}}_a\Psi := -2D_bh_{ac}\frac{\hbar}{i}\frac{\delta\Psi}{\delta h_{bc}} = 0.$$
no time/space dependence

Covariant (path integral) quantization of GR:

$$Z[g] = \int \mathcal{D}g_{\mu\nu}(x) \, \mathrm{e}^{\mathrm{i}S[g_{\mu\nu}(x)]}$$

formidable mathematical (and conceptual) difficulties

functional aspects diffeomorphism symmetry

and transition amplitudes



Lattice Quantum Gravity

Basic idea: covariant quantisation of gravity as sum over "discrete geometries"

Continuum spacetime manifold replaced by simplicial lattice; metric data encoded in edge lengths

Gravitational action is discretised version of Einstein-Hilbert action (Regge action)

Quantum Regge calculus

Path integral of discrete geometries: fixed simplicial lattice, sum over edge length variables continuum limit via lattice refinement

(Causal) Dynamical Triangulations

Path integral of discrete geometries: sum over all possible (causal) simplicial lattices (fixed topology), fixed edge lengths continuum limit via sum over finer and finer lattices

n

$$S_R = \frac{1}{8\pi} \sum_t A_t \varepsilon_t$$

T. Regge, R. Williams, H. Hamber, B. Dittrich, B. Bahr,

$$Z = \lim_{\Delta \to \infty} \int d\mu(\{L_e\}) e^{-S_R^{\Delta}(\{L_e\})}$$

J. Ambjorn, J. Jurkiewicz, R. Loll, D. Benedetti, A. Goerlich, T. Budd, ...

$$Z = \lim_{a \to 0} \sum_{\Delta} \mu(a, \Delta) e^{-S_R^{\Delta}(\{L_e = a\})}$$

spin foam models)

nnection variables):

molin, T. Thiemann, J. Lewandowski, J. Pullin, H. Sahlmann, B. Dittrich, $(A_a^i, E_i^b = \frac{1}{\gamma}\sqrt{e}e_i^b)$

Canonical quantization of GR as gauge theory

quantum states of "space" are graphs labeled by algebraic (group-theoretic) data: spin networks

spin networks can be understood as (generalised) piecewise-flat discrete geometries

underlying graphs are dual to (simplicial lattices)

e at vGeometric observables correspond to operators; some of them have discrete spectrum: discretization of quantum geometry! (Rovelli, Smolin, Ashtekar, Lewandowski, 1995-1997)

$$\widehat{A}_{\prod_{j}} | \underset{j}{\bigcirc} = 8\pi\beta l_{p}^{2} \sqrt{j(j+1)} | \underset{j}{\bigcirc} \rangle$$

$$j_{22}$$
 j_{20} j_{18} j_{17} j_{16} j_{16} j_{16} j_{16} j_{17} j_{16} j_{16} j_{17} j_{10} j

$$= \lim_{\gamma} \frac{\bigcup_{\gamma} \mathcal{H}_{\gamma}}{\approx} = L^2 \left(\bar{\mathcal{A}}\right)$$
$$\mathcal{H}_{\gamma} = L^2 \left(\frac{G^2}{G^2}, a\mu = \prod_{e=1}^{E} a\mu_e^{Haar} \right) \qquad \text{G=SU(2)}$$

Loop Quantum Gravity (and spin foam models)

M. Reisenberger, C. Rovelli, J. Baez, J. Barrett, L. Crane, A. Perez, E. Livine, DO, S. Speziale,

evolution of spin networks involves changes in combinatorial structure and in algebraic labels "histories" (dynamical interaction processes) are also purely algebraic and combinatorial: spin foams



spin networks/spin foams can be understood as (generalised) piecewise-flat discrete geometries

the underlying graphs and 2-complexes are dual to (simplicial) lattices

Lots of results on quantum geometry and mathematics of quantum gravitational field; inspiring models of quantum black holes and quantum cosmology

• failures of GR and QFT at high energies/small distances

breakdown of continuum spacetime itself?

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• black hole thermodynamics

J. Bekenstein, S. Hawking,

$$S = \frac{1}{4} \frac{c^3}{\hbar G} A$$
$$T = \frac{\hbar c^3}{8\pi k G M}$$

solution of information loss paradox require non-locality?

if spacetime itself has entropy, it has microstructure if entropy is finite, this implies discreteness



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$$T_{dS} \stackrel{hc}{=} \pi_{k} (I \stackrel{(I)}{=} \Lambda \quad dS) \quad dE \quad \text{if spacetime itself has entropy, it has microstructure} \\ \delta Q = T dS \quad p = T (\partial S / \partial V) \\$$

$$\delta S = \alpha \, \delta A = 0 \qquad \theta_p = 0$$

• failures of GR and QFT at high energies/small distances

breakdown of continuum spacetime itself?

 insights from analog gravity models in condensed matter physics
 C. Barcelo, S. Liberati, M. Visser, '05 effective curved metric and matter fields from non-geometric atomic theory

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> Is gravity an emergent phenomenon? Are spacetime and fields just collective emergent entities? suggested also by modern QG approaches - new non-spatiotemporal dofs

Quantum Gravity: (possible) phenomenology
QG phenomenology

- minimal length
- deformed uncertainty relations

$$[X,P] = i\hbar \left(1 + \tau P^2\right)$$

 violation/deformation of spacetime symmetries (e.g. Lorentz symmetry)



G. Amelino-Camelia, '08S. Hossenfelder, '12T. Jacobson, S. Liberati, D. Mattingly, '07

QG modification of effective field theory

modified dispersion relations

$$m^2 \approx E^2 - \vec{p}^2 + \alpha \left(\frac{E}{m_{\rm p}}\right) E^2$$

- modified scattering thresholds
- non-local terms (violation of locality)

many (simplified) scenarios are already testable



QG effects in black hole physics

- Hawking radiation and BH evaporation
 - reviation from thermal radiation?
 - end result: compact remnant? nothing?
 - black hole information paradox (is unitarity violated? renounce locality?)
 - BH formation, horizon and singularity

•

- regular black hole-like objects in QG (with "horizon", but no singularity)
 - inner quantum region A. Ashtekar, M. Bojowald,
 - black hole -> white hole transition (radio bursts) H. Haggard, C. Rovelli, F. Vidotto, ...
- exotic compact objects
 - horizonless imperfect absorption (modified GW signal) V. Cardoso, P. Pani
 - outer "membrane" GW echo J. Abedi, H. Dykaar, N. Afshordi, '16







QG in cosmological scenarios for the early universe

why a close to homogeneous and isotropic universe? why an approximately scale invariant power spectrum?

R. Brandenberger, '10, '11, '14





Bouncing

cosmology

Inflation

Emergent universe

QG in Cosmological scenarios for the early universe

why a close to homogeneous and isotropic universe? why an approximately scale invariant power spectrum?

R. Brandenberger, '10, '11, '14



Inflation

 classical contracting phase "before" the big bang, bouncing to current expanding phase

Bouncing cosmology.

- various realizations (e.g. LQC)
- can produce scale invariant spectrum
- trans-Planckian modes not needed

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Emergent universe

new physics needed to describe/justify cosmological bounce

Bouncing cosmology needs Quantum Gravity

QG in cosmological scenarios for the early universe

why a close to homogeneous and isotropic universe? why an approximately scale invariant power spectrum?

R. Brandenberger, '10, '11, '14



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Inflation

Bouncing cosmology

Emergent

universe

- phase transition between static and expanding universe
- various realizations (e.g. string gas cosmology)
- density perturbations as thermal fluctuations
- · can give scale invariant power spectrum
- trans-Planckian modes not needed
- static phase and phase transition require new physics



 $\mathbf{p} = \mathbf{0}$

Emergent universe needs Quantum Gravity

p = rho / 3

 $\sim t^{1/2}$

QG effects in emergent gravity scenarios

Verlinde's emergent gravity

gravity as eqn of state

+

modified entropy formula (new volumedependent term, akin to dark energy)

E. Verlinde, '16, S. Hossenfelder, '17



modified gravity to explain dark matter (new acceleration scale ~ MOND)

proposals for cosmological constant/dark energy

non-local gravity (continuum only approximate; also from other perspectives)	C. Wetterich, '97;; M. Maggiore, '17
suggestions from analogue gravity models (e.g. cosmological constant from depletion factor if spacetime is Bose condensate)	S. Finazzi, S. Liberati, L. Sindoni, '12
vanishing vacuum energy from global equilibrium of spacetime fluid	G. Volovik, '01, '05, '11

new dissipative effects in dispersion relations S. Liberati, L. Maccione, '13

if spacetime is like fluid or superfluid medium, should expect dissipation

manifest in dispersion relations
$$\omega^2 \simeq c^2 k^2 \left[1 - i \frac{4}{3} \frac{\nu k}{c} - \frac{8}{9} \left(\frac{\nu k}{c} \right)^2 + i \frac{8}{27} \left(\frac{\nu k}{c} \right)^3 \right]$$

QG effects (potentially) testable

despite suppression by Planck scale

Main theoretical problem:

most testable effects obtained within simplified models and phenomenological frameworks

very weak link with fundamental theory

no real control over approximations and assumptions

pressing issue: connect simplified models with fundamental formalisms

Group field theory: an example of fundamental quantum gravity formalism



















DO, '13

Many-body Hilbert space for "quantum space": Fock space

$$\mathcal{F}(\mathcal{H}_v) = \bigoplus_{V=0}^{\infty} sym\left\{ \left(\mathcal{H}_v^{(1)} \otimes \mathcal{H}_v^{(2)} \otimes \cdots \otimes \mathcal{H}_v^{(V)} \right) \right\}$$

Fock vacuum: "no-space" state | 0 >

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Fock vacuum: "no-space" state | 0 >

Second-quantised representation: ladder and geometric operators

$$\begin{bmatrix} \hat{\varphi}(\vec{g}), \, \hat{\varphi}^{\dagger}(\vec{g}') \end{bmatrix} = \mathbb{I}_{G}(\vec{g}, \vec{g}') \qquad \begin{bmatrix} \hat{\varphi}(\vec{g}), \, \hat{\varphi}(\vec{g}') \end{bmatrix} = \begin{bmatrix} \hat{\varphi}^{\dagger}(\vec{g}), \, \hat{\varphi}^{\dagger}(\vec{g}') \end{bmatrix} = 0$$

$$\rightarrow \quad \widehat{\mathcal{O}_{n,m}} \left(\hat{\varphi}, \hat{\varphi}^{\dagger} \right) = \int [d\vec{g}_{i}] [d\vec{g}_{j}'] \, \widehat{\varphi}^{\dagger}(\vec{g}_{1}) ... \widehat{\varphi}^{\dagger}(\vec{g}_{m}) \mathcal{O}_{n,m} \left(\vec{g}_{1}, ..., \vec{g}_{m}, \vec{g}_{1}', ..., \vec{g}_{n}' \right) \widehat{\varphi}(\vec{g}_{1}') ... \widehat{\varphi}(\vec{g}_{n}') \mathcal{O}_{n,m} \left(\vec{g}_{1}, ..., \vec{g}_{m}, \vec{g}_{1}', ..., \vec{g}_{n}' \right) \widehat{\varphi}(\vec{g}_{1}') ... \widehat{\varphi}(\vec{g}_{n}') \mathcal{O}_{n,m} \left(\vec{g}_{1}, ..., \vec{g}_{m}, \vec{g}_{1}', ..., \vec{g}_{n}' \right) \widehat{\varphi}(\vec{g}_{1}') ... \widehat{\varphi}(\vec{g}_{n}') \mathcal{O}_{n,m} \left(\vec{g}_{1}, ..., \vec{g}_{m}, \vec{g}_{1}', ..., \vec{g}_{n}' \right) \widehat{\varphi}(\vec{g}_{1}') ... \widehat{\varphi}(\vec{g}_{n}') \mathcal{O}_{n,m} \left(\vec{g}_{1}, ..., \vec{g}_{m}, \vec{g}_{1}', ..., \vec{g}_{n}' \right) \widehat{\varphi}(\vec{g}_{1}') ... \widehat{\varphi}(\vec{g}_{n}') \mathcal{O}_{n,m} \left(\vec{g}_{1}, ..., \vec{g}_{n}, \vec{g}_{1}', ..., \vec{g}_{n}' \right) \widehat{\varphi}(\vec{g}_{1}') ... \widehat{\varphi}(\vec{g}_{n}') \mathcal{O}_{n,m} \left(\vec{g}_{1}, ..., \vec{g}_{n}' \right) \widehat{\varphi}(\vec{g}_{1}') ... \widehat{\varphi}(\vec{g}_{n}') \mathcal{O}_{n,m} \left(\vec{g}_{1}, ..., \vec{g}_{n}' \right) \widehat{\varphi}(\vec{g}_{1}') ... \widehat{\varphi}(\vec{g}_{n}') \mathcal{O}_{n,m} \left(\vec{g}_{1}, ..., \vec{g}_{n}' \right) \widehat{\varphi}(\vec{g}_{1}') ... \widehat{\varphi}(\vec{g}_{n}') \mathcal{O}_{n,m} \left(\vec{g}_{n}' \right) \widehat{\varphi}(\vec{g}_{n}') \widehat{\varphi}(\vec{g}_{n}') \mathcal{O}_{n,m} \left(\vec{g}_{n}' \right) \widehat{\varphi}(\vec{g}_{n}') \widehat{\varphi$$

DO, '13

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e.g. total space volume (extensive quantity):

$$\hat{V}_{tot} = \int [dg_i] [dg'_j] \hat{\varphi}^{\dagger}(g_i) V(g_i, g'_j) \hat{\varphi}(g'_j) = \sum_{J_i} \hat{\varphi}^{\dagger}(J_i) V(J_i) \hat{\varphi}(J_j)$$

DO, '13

Many-body Hilbert space for "quantum space": Fock space

$$\mathcal{F}(\mathcal{H}_v) = \bigoplus_{V=0}^{\infty} sym\left\{ \left(\mathcal{H}_v^{(1)} \otimes \mathcal{H}_v^{(2)} \otimes \cdots \otimes \mathcal{H}_v^{(V)} \right) \right\}$$
 Fock vacuum: "no-space" state | 0 >

Second-quantised representation: ladder and geometric operators

$$\begin{bmatrix} \hat{\varphi}(\vec{g}), \, \hat{\varphi}^{\dagger}(\vec{g}') \end{bmatrix} = \mathbb{I}_{G}(\vec{g}, \vec{g}') \qquad \begin{bmatrix} \hat{\varphi}(\vec{g}), \, \hat{\varphi}(\vec{g}') \end{bmatrix} = \begin{bmatrix} \hat{\varphi}^{\dagger}(\vec{g}), \, \hat{\varphi}^{\dagger}(\vec{g}') \end{bmatrix} = 0$$

$$\rightarrow \quad \widehat{\mathcal{O}_{n,m}}\left(\hat{\varphi}, \hat{\varphi}^{\dagger}\right) = \int [d\vec{g}_{i}][d\vec{g}_{j}'] \, \widehat{\varphi}^{\dagger}(\vec{g}_{1})...\widehat{\varphi}^{\dagger}(\vec{g}_{m})\mathcal{O}_{n,m}\left(\vec{g}_{1}, ..., \vec{g}_{m}, \vec{g}_{1}', ..., \vec{g}_{n}'\right) \widehat{\varphi}(\vec{g}_{1}')..\widehat{\varphi}(\vec{g}_{n}')$$

e.g. total space volume (extensive quantity):

$$\hat{V}_{tot} = \int [dg_i] [dg'_j] \hat{\varphi}^{\dagger}(g_i) V(g_i, g'_j) \hat{\varphi}(g'_j) = \sum_{J_i} \hat{\varphi}^{\dagger}(J_i) V(J_i) \hat{\varphi}(J_j)$$

Quantum space as an system of many quantum polyhedra/spin network vertices generic states not very "spacey" at all - "connected" many-body states a little more "spacey"



DO, '13

graphs/simplicial complex

Forming extended structures: gluing building blocks -

$$\mathcal{H}_{\gamma} \subset \mathcal{H}_{V} \qquad \Psi_{\gamma}(G_{ij}^{ab}) = \prod_{[(ia),(jb)]} \int_{G} d\alpha_{ij}^{ab} \phi_{V}(\dots, g_{ia} \alpha_{ij}^{ab}, \dots, g_{jb} \alpha_{ij}^{ab}, \dots) = \Psi_{\gamma}(g_{ia}(g_{jb})^{-1})$$



Forming extended structures: gluing building blocks — — graphs/simplicial complex $\mathcal{H}_{\gamma} \subset \mathcal{H}_{V} \qquad \underbrace{\Psi_{\gamma}(G_{ij}^{ab})}_{g_{2}} = \prod_{[(ia),(jb)]} \int_{G} d\alpha_{ij}^{ab} \phi_{V}(\dots, g_{ia} \alpha_{ij}^{ab}, \dots, g_{jb} \alpha_{ij}^{ab}, \dots) = \Psi_{\gamma}(g_{ia}^{ab}, \dots, g_{ib}^{ab}, \dots)$ $\phi(q_i) = \phi(q_i\beta)$ Gluing = connectivity = entanglement between "aton" $=\frac{1}{\sqrt{2j+1}}\sum_{a=1}^{2j+1}\langle U|\gamma_1, j, a, c\rangle \langle U|\gamma_2, j, c, b\rangle$ amaximally mixed state $|\mathcal{I}\rangle = \sum_{\{a,b,c\}}^{i_{\gamma}} j_{i}a, b\rangle = \frac{1}{\sqrt{2j+1}} \sum_{p=1}^{2j+1} |e_{p}\rangle\langle e_{p}|$ Donnelly, '12; Livine, Terno, '08; Chirco, Mele, DO, Vitale, '17 j_{15} $\{|\gamma, j, a, c\rangle\}, \{|\gamma, j, c, b\rangle\}$ j_{18} $\mathcal{H}_{\gamma_1},\,\mathcal{H}_{\gamma_2}$ j_{16} j_{21} j_{13} $\rho_1 = \mathrm{Tr}_2[|\gamma, j, a, b\rangle \langle \gamma, j, a, b|]$ j_2 j_3 j_1

DO, '13

DO, '09; DO, '14

Dynamics governs gluing processes and formation of extended discrete structures

Interactions processes correspond to (simplicial) complexes in one dimension higher

DO, '09; DO, '14

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Interactions processes correspond to (simplicial) complexes in one dimension higher

details depend on (class of) models

$$S(\varphi,\overline{\varphi}) = \frac{1}{2} \int [dg_i] \overline{\varphi(g_i)} \mathcal{K}(g_i) \varphi(g_i) + \frac{\lambda}{D!} \int [dg_{ia}] \varphi(g_{i1}) \dots \varphi(\overline{g}_{iD}) \mathcal{V}(g_{ia},\overline{g}_{iD}) + c.c.$$

"combinatorial non-locality"
in pairing of field arguments

DO, '09; DO, '14

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Example: simplicial interactions





DO, '09; DO, '14

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"combinatorial non-locality"
in pairing of field arguments

$$\mathcal{Z} = \int \mathcal{D}\varphi \mathcal{D}\overline{\varphi} \ e^{i S_\lambda(\varphi,\overline{\varphi})} = \sum_{\Gamma} \frac{\lambda^{N_{\Gamma}}}{sym(\Gamma)} \mathcal{A}_{\Gamma}$$

Feynman diagrams = stranded diagrams dual to cellular complexes of arbitrary topology

sum over triangulations/complexes

amplitude for each triangulation/complex

Multiple relations with other QG formalisms



GFT and Loop Quantum Gravity

Quantum dofs are same as in LQG (spin networks), organised in different (but similar) Hilbert space

DO, '13; DO, '14

2nd quantized reformulation of states and dynamics

$$\mathcal{H}_{\gamma} \subset \mathcal{H}_{V} \qquad \Psi \gamma(G_{ij}^{ab}) = \prod_{[(ia),(jb)]} \int_{G} d\alpha_{ij}^{ab} \phi_{V}(\dots, g_{ia} \, \alpha_{ij}^{ab}, \dots, g_{jb} \alpha_{ij}^{ab}, \dots) = \Psi \gamma(g_{ia}(g_{jb})^{-1})$$

$$\widehat{\mathcal{O}_{n,m}} \rightarrow \langle \vec{\chi}_{1}, \dots, \vec{\chi}_{m} | \widehat{\mathcal{O}_{n,m}} | \vec{\chi}_{1}', \dots, \vec{\chi}_{n}' \rangle = \mathcal{O}_{n,m} \left(\vec{\chi}_{1}, \dots, \vec{\chi}_{m}, \vec{\chi}_{1}', \dots, \vec{\chi}_{n}' \right) \rightarrow$$

$$\rightarrow \widehat{\mathcal{O}_{n,m}} \left(\hat{\varphi}, \hat{\varphi}^{\dagger} \right) = \int [d\vec{g}_{i}] [d\vec{g}_{j}'] \, \widehat{\varphi}^{\dagger}(\vec{g}_{1}) \dots \widehat{\varphi}^{\dagger}(\vec{g}_{m}) \mathcal{O}_{n,m} \left(\vec{g}_{1}, \dots, \vec{g}_{m}, \vec{g}_{1}', \dots, \vec{g}_{n}' \right) \, \widehat{\varphi}(\vec{g}_{1}') \dots \widehat{\varphi}(\vec{g}_{n}')$$

Multiple relations with other QG formalisms



GFT and spin foam models

Spin foam model = quantum amplitude for spin network evolution $Z(\Gamma) = \sum_{\{J\},\{I\}|j,j',i,i'} \prod_{f} A_{f}(J,I) \prod_{e} A_{e}(J,I) \prod_{v} A_{v}(J,I)$

Any spin foam amplitude is the Feynman amplitude of a GFT model

Reisenberger, Rovelli, '00

 $Z(\Gamma) \leftrightarrow \begin{cases} A_f(J) \\ A_e(J,I) \\ A_v(J,I) \end{cases}$

$$\begin{cases} \mathcal{K}(J,I) \sim \mathcal{K}(g) \\ \mathcal{V}(J,I) \sim \mathcal{V}(g) \end{cases} \leftrightarrow S(\varphi,\bar{\varphi}) \\ \mathcal{Z} = \int \mathcal{D}\varphi \mathcal{D}\overline{\varphi} \ e^{i S_{\lambda}(\varphi,\overline{\varphi})} = \sum_{\Gamma} \frac{\lambda^{N_{\Gamma}}}{sym(\Gamma)} \mathcal{A}_{\Gamma} \qquad Z(\Gamma) \equiv \mathcal{A}_{\Gamma} \end{cases}$$



 $= \sum_{\Gamma} \frac{\lambda^{\mu}}{sym(\Gamma)} \mathcal{A}_{\Gamma}$

Application of QFT tools to QG problems: GFT renormalization

$$\mathcal{Z} = \int \mathcal{D}\varphi \mathcal{D}\overline{\varphi} \ e^{i S_{\lambda}(\varphi,\overline{\varphi})}$$

Ben Geloun, Benedetti, Bonzom, Carrozza, Dittrich, DO, Einchhorn, Gurau, Koslowski, Krajewski, Lahoche, Ousmane Samary, Riello, Rivasseau, Tanasa, Toriumi, Vitale, ...

Issue 1:

construction and quantisation ambiguities in definition of GFT models

Issue 2:

continuum limit: controlling quantum dynamics of many interacting QG dofs

- GFT perturbative renormalization
- --> renormalizability of GFT model
- GFT non-perturbative renormalization
- --> RG flow ~ full GFT partition function & continuum phases

general strategy:

treat GFTs as ordinary QFTs defined on Lie group manifold

- · Divergences in simplicial models
- Renormalizability of TGFT models (d>2, non-abelian, w gauge invariance,)
- Generic asymptotic freedom/safety, hints of condensed phase, WF fixed point



Building up continuum space and geometry

Goal: extract continuum geometric (gravitational) physics (dynamics) from QG (GFT) models





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This means:

- control QG states encoding large numbers of microscopic QG dofs
- identify those with (approximate) continuum geometric interpretation
- characterise their (geometric) properties in terms of observables
- extract their effective dynamics and recast it in GR+QFT form





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This requires:

- controlling large graphs/complexes superpositions
- coarse graining of description
- approximations of both states, observables and dynamics

Here: take advantage of QFTformalism/methods (universe as a quantum many-body system cosmology as QG hydrodynamics)

so depends on the gauge invariance (1), we require that the state is invariant under right multiplication of all group elements,
alling that the anti-fields, the fetter of the state only depends on gauge invariance under (8) so that
fields, the fetter of the state only depends on gauge invariant data.
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 $\hat{\sigma} := \int d^4g \sigma(g_I) \hat{\varphi}^{\dagger}(g_I)$ for all
out loss of generality $\sigma(k'g_I) = \sigma(g_I)$ for all
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(15) A second possibility is to use a two-particle
which automatically has the required gauge invariance:

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N. (16)

data and does on apart from tion of spatial Thursday, March 7, 2013

spatial homopatial isotropy δ_{ij} for some a.

$$\hat{\xi} := \frac{1}{2} \int d^4g \ d^4h \ \xi(g_I h_I^{-1}) \hat{\varphi}^{\dagger}(g_I) \hat{\varphi}^{\dagger}(h_I), \qquad (18)$$

where due to (1) and $[\hat{\varphi}^{\dagger}(g_I), \hat{\varphi}^{\dagger}(h_I)] = 0$ the function ξ can be taken to satisfy $\xi(g_I) = \xi(kg_Ik')$ for all k, k' in SU(2) and $\xi(g_I) = \xi(g_I^{-1})$. ξ is a function on the gaugeinvariant configuration space of a single tetrahedron.

We then consider two types of candidate states for macroscopic, homogeneous configurations of tetrahedra: (\hat{a}) to be the tetrahedra in the tetrahedra is the tetrahedra in the tetrahedra is the tetrahedra in the tetrahedra is the tetrahedra i

$$|\sigma\rangle := \exp(\hat{\sigma})|0\rangle, \quad |\xi\rangle := \exp(\hat{\xi})|0\rangle.$$
 (19)

 $|\sigma\rangle$ corresponds to the simplest case of single-particle condensation with gauge invariance imposed by hand: $|\xi\rangle$

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lso depends on the gauge invariance (1), we require that the state is invariant under right multiplication of all group elements, alling the the $q_I \mapsto q_I \oplus q_I$ corresponding to invariance under (8) so that fields, the left antiperstate only depends on gauge-invariant data. int inner prod-que up to the plemented by (6), φ is a field on SU(2) and we require on Ewing, ... embedded tetrathis additional symmetry under the action of SU(2). It ector makes, GFT condensates as homogeneous continuum geometries (not encoding any topological information) $|\sigma \rangle \stackrel{14}{\longrightarrow} \exp(\hat{\sigma}) |0\rangle \qquad \qquad \hat{\sigma} := \int d^4g \,\sigma(g_I) \hat{\varphi}^{\dagger}(g_I) / \hat{\varphi}^{\xi$ 17 ained by $\underline{push}_{\sigma} d^4g \, q_{f}g_{W} \hat{\varphi}^{\dagger} equire \, \sigma(g_I k) \equiv \sigma(g_I)$ for all fields on \overline{G} . J out loss of generality $\sigma(k'g_I) = \sigma(g_I)$ ric now reads because of (1). A second possibility is to use a two-particle)),(15)which automatically has the required gauge invariance: s in the frame {geometries of tetrahedron} \simeq $\sigma(\mathcal{D})$ \simeq icdesquiped by single collective wave function {continuum spatial geometries at a point} \simeq say depending on homogeneous agis or robic begins trid data $g_I h_I^{-1})\hat{\varphi}^{\dagger}(g_I)\hat{\varphi}^{\dagger}(h_{\underline{L}}),$ namisuperspace of homogeneous geometries d by the data Gielen, '14 eity if where due to (1) and $[\hat{\varphi}^{\dagger}(g_I), \hat{\varphi}^{\dagger}(h_I)] = 0$ the function ξ Corresponding effective tolynamics: $aGFSTyeg(s_I) = motion (ibg_I k')$ for all k, k' in N. SU(2) and $\xi(g_I) = \xi(\tilde{\psi}_I^{-1})$. ξ is a function on the gaugedata and does $(g_i)_{i \to 0}$ $(g_i)_{i \to 0}$ We then consider two types of candidate states for on apart from macroscopic, homogeneous configurations of tetrahedra: tion of spatial Thursday, March 7, 2013 $|\sigma\rangle := \exp(\hat{\sigma}) |0\rangle, \quad |\xi\rangle := \exp(\hat{\xi}) |0\rangle.$ (19)spatial homopatial isotropy $|\sigma\rangle$ corresponds to the simplest case of single-particle con- δ_{ii} for some a.

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DO, Sindoni, Wilson-Ewing, '16

• (generalised) EPRL model for 4d Lorentzian QG with SU(2) data, coupled to (discretised) (pre-)scalar field

DO, Sindoni, Wilson-Ewing, '16

• (generalised) EPRL model for 4d Lorentzian QG with SU(2) data, coupled to (discretised) (pre-)scalar field

• coupling of free massless scalar field $\hat{\varphi}(g_{\nu}) \rightarrow \hat{\varphi}(g_{\nu}, \phi) \qquad \qquad |\sigma\rangle \sim \exp\left(\int \mathrm{d}g_{\nu} \mathrm{d}\phi \,\sigma(g_{\nu}, \phi)\hat{\varphi}^{\dagger}(g_{\nu}, \phi)\right) |\mathbf{0}\rangle$

DO, Sindoni, Wilson-Ewing, '16

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• reduction to isotropic condensate configurations (depending on single variable j): $\sigma(g_v, \phi) \rightarrow \sigma_j(\phi)$

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• effective condensate hydrodynamics (non-linear quantum cosmology):

 $A_j \partial_{\phi}^2 \sigma_j(\phi) - B_j \sigma_j(\phi) + w_j \sigma_j(\phi)^4 = 0$

functions A, B, w define the details of the EPRL model

GFT interaction terms sub-dominant

DO, Sindoni, Wilson-Ewing, '16

(generalised) EPRL model for 4d Lorentzian QG with SU(2) data, coupled to (discretised) (pre-)scalar field •

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key relational observables (expectation values in condensate state) with scalar field as clock:

universe volume (at fixed "time")

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$$V(\phi) = \sum_{j} V_{j} \bar{\sigma}_{j}(\phi) \sigma_{j}(\phi) = \sum_{j} V_{j} \rho_{j}(\phi)^{2}$$
momentum of scalar field (at fixed "time")

$$\pi_{\phi} = \langle \sigma | \hat{\pi}_{\phi}(\phi) | \sigma \rangle = \hbar \sum_{j} Q_{j}$$

$$\pi^{2} = \hbar^{2} (\sum_{j} Q_{j})^{2}$$

 $\rho = \frac{\pi \phi}{2V^2} = \frac{\pi (\sum_j \alpha)}{2(\sum_i V_j)}$

$$V_j \sim j^{3/2} \ell_{\rm Pl}^3$$

$$\sigma_j(\phi) = \rho_j(\phi) e^{i\sigma_j(\phi)}$$

Q = constant of motion

energy density of scalar field (at fixed "time")

Emergent bouncing cosmology from full QG

DO, Sindoni, Wilson-Ewing, '16

effective dynamics for volume - generalised Friedmann equations: (GFT interaction terms sub-dominant)

$$\left(\frac{V'}{3V}\right)^2 = \left(\frac{2\sum_j V_j \rho_j \sqrt{E_j - \frac{Q_j^2}{\rho_j^2} + m_j^2 \rho_j^2}}{3\sum_j V_j \rho_j^2}\right)^2$$

$$\frac{V''}{V} = \frac{2\sum_{j} V_j \left[E_j + 2m_j^2 \rho_j^2\right]}{\sum_j V_j \rho_j^2}$$

E = constant of motion

Emergent bouncing cosmology from full QG

DO, Sindoni, Wilson-Ewing, '16

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E = constant of motion

classical approx.
$$\rho_j^2 \gg |E_j|/m_j^2$$
 and $\rho_j^4 \gg Q_j^2/m_j^2$

$$\left(\left(\frac{V'}{3V}\right)^2 = \left(\frac{2\sum_j V_j m_j \rho_j^2}{3\sum_j V_j \rho_j^2}\right)^2\right) \left(\frac{V''}{V} = \frac{4\sum_j V_j m_j^2 \rho_j^2}{\sum_j V_j \rho_j^2}\right)$$
approx. classical Friedmann eqns if $m_j^2 \approx 3G_N$

Emergent bouncing cosmology from full QG

DO, Sindoni, Wilson-Ewing, '16

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E = constant of motion

classical approx.
$$\rho_j^2 \gg |E_j|/m_j^2$$
 and $\rho_j^4 \gg Q_j^2/m_j^2$

$$\left(\frac{V'}{3V}\right)^2 = \left(\frac{2\sum_j V_j m_j \rho_j^2}{3\sum_j V_j \rho_j^2}\right)^2 \qquad \underbrace{V''}_V = \frac{4\sum_j V_j m_j^2 \rho_j^2}{\sum_j V_j \rho_j^2} \quad \text{approx. classical Friedmann eqns if } m_j^2 \approx 3G_N$$

$$\exists j / \rho_j(\phi) \neq 0 \ \forall \phi \qquad \bigvee \qquad \bigvee = \sum_j V_j \rho_j^2$$
remains positive at all times (with single turning point)

generic quantum bounce (solving classical singularity)!

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Accelerated phase after bounce: QG inflation?

 $\frac{\ddot{a}}{a} = \frac{1}{3} \left(\frac{\pi_{\phi}}{V}\right)^2 \left[\frac{\partial_{\phi}^2 V}{V} - \frac{5}{3} \left(\frac{\partial_{\phi} V}{V}\right)^2\right]$

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$$\frac{V^{\prime\prime}}{V} > \frac{5}{3} \left(\frac{V^{\prime}}{V}\right)^2$$

detailed study of behaviour of solutions after bounce confirm a distinct accelerated phase

issue is: number of e-folds

for: $V=a^3$ we have:

$$N = \frac{2}{3} \log \left(\frac{\rho_{\text{end}}}{\rho_{\text{bounce}}} \right)$$

can we get at least N \sim 60?

does the acceleration last long enough (to solve cosmological problems)?



Accelerated phase after bounce: QG inflation?

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 in effective cosmological dynamics neglecting GFT interactions:

 $0.119 \lesssim N \lesssim 0.186$

acceleration is too short-lived to be physically useful

including effects of GFT interactions (in phenomenological way):

$$S = \int \mathrm{d}\phi \, \left(A \, |\partial_{\phi}\sigma|^2 + \mathcal{V}(\sigma) \right)$$
$$\sigma = \sigma \, o^{i\theta}$$

$$\begin{aligned} \mathcal{V}(\sigma) &= B |\sigma(\phi)|^2 + \frac{2}{n} w |\sigma|^n + \frac{2}{n'} w' |\sigma|^{n'} \\ \partial_{\phi}^2 \rho - m^2 \rho - \frac{Q^2}{\rho^3} + \lambda \rho^{n-1} + \mu \rho^{n'-1} = 0 \end{aligned}$$

one finds:

- bounce
- accelerated expansion following bounce
- decelerated phase and recollapse

moreover:

- N at least ~ 60
- no intermediate deceleration between beginning and end of accelerated phase

QG-inflation from GFT condensates



Big Bounce?

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(as in LQC, but from the full QG theory!)

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.... provided the GFT hydrodynamics approximation (and other assumptions) does not break down in that regime

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novelty: it can be done!

exactly as one would do in a BEC....

Cosmological perturbations from full QG

S. Gielen, DO, '17

 $\frac{\Delta V(\phi_0, k_i; \Phi_0, K_i)}{\langle \hat{V}(\phi_0) \rangle^2}$

GFT for 4d gravity coupled to 4 free massless scalar fields used as clock and rods
isotropic reduction of geometric sector
$$\sigma(g_I, \phi^J) = \sum_{j=0}^{\infty} \sigma_j(\phi^J) \mathbf{D}^j(g_I)$$
GFT hydrodynamics equation for
isotropic condensates (weak coupling)
$$\left(-B_j + A_j \partial_{\phi^0}^2 + C_j \Delta_{\phi^i}\right) \sigma_j(\phi^J) = 0$$
small perturbations around homogeneous condensate universes
$$\sigma_j(\phi^J) = \sigma_j^0(\phi^0)(1 + \epsilon \psi_j(\phi^J))$$

volume fluctuations and cosmological power spectrum

$$\Delta V(\phi_0, k_i; \Phi_0, K_i) \equiv \langle \hat{\tilde{V}}(\phi^0, k_i) \hat{\tilde{V}}(\Phi^0, K_i) \rangle - \langle \hat{\tilde{V}}(\phi^0, k_i) \rangle \langle \hat{\tilde{V}}(\Phi^0, K_i) \rangle$$

= $\delta(\phi^0 - \Phi^0) \sum_j V_j^2 |\sigma_j^0(\phi^0)|^2 [(2\pi)^3 \delta^3(k_i + K_i) + \epsilon (\tilde{\psi}_j(\phi^0, k_i + K_i) + \overline{\tilde{\psi}_j}(\phi^0, -k_i - K_i))]$

naturally approximate scale invariance

- dominant part (computed on exactly homogeneous condensate) exactly scale invariant
- scale invariance tied to translation invariance of condensate
- deviations suppressed as universe expands and when inhomogeneities are negligible

small relative amplitude

- dominant term ~ $1/N \sim 1/V$
- perturbations further suppressed as universe expands
- if accelerated phase, further suppression of deviations from scale invariance
- QG inflation without inflation

Thank you for your attention!