

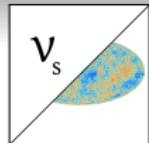
# eV-Scale Sterile Neutrinos and Cosmology - Compatible or Not?

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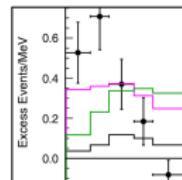
Rasmus Sloth Hansen  
Department of Physics and Astronomy,

Aarhus University

January 30, 2015

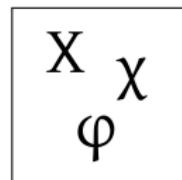
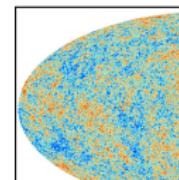


# Outline

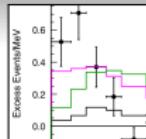


Anomalies

Cosmology



Model Extensions

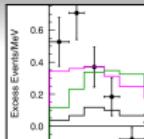


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## Neutrino Anomalies

Three different types of experiments can be explained using an eV sterile neutrino:

- Accelerator experiments observe  $\nu_e$  in a  $\nu_\mu$ -beam incompatible with other  $\nu$ -oscillations. (LSND and MiniBooNE)
- Calibration of gallium solar neutrino detectors give a small but significant deficit. (GALLEX and SAGE)
- The  $\bar{\nu}_e$  flux measured from nuclear reactors is a few percent smaller than expected.



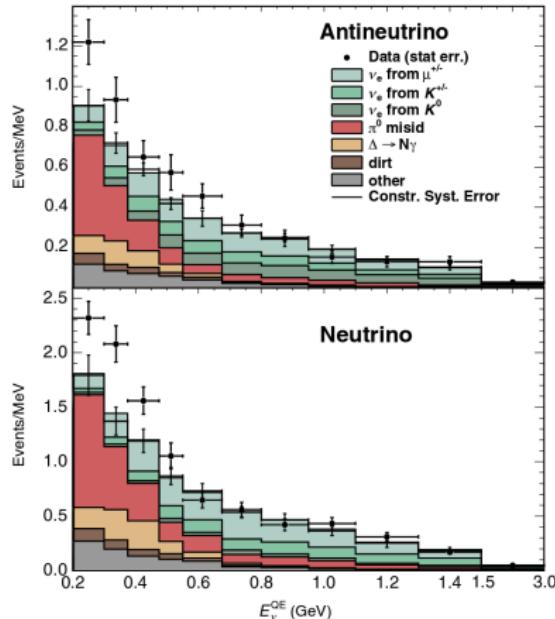
## Neutrino anomalies

# Accelerator Experiments

- LSND observed an excess of  $\nu_e$  in a  $\nu_\mu$ -beam.

LSND Collaboration, 2001  
 (arxiv:hep-ex/0104049)

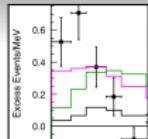
- MiniBooNE was supposed to test the excess, and found similar results.
- Combined with KARMEN and ICARUS, only  $\delta m^2 \sim 0.5\text{eV}^2$  is allowed.



MiniBooNE Collaboration, 2013

(arxiv:1303.2588)

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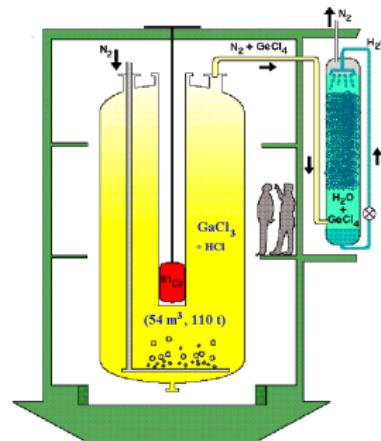


## Neutrino anomalies

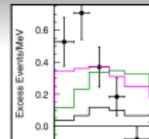
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# Gallium Detectors

- Goal: measure neutrinos from the Sun.
- Calibrated using strong radioactive sources.
- Deficit in measured neutrinos:  
 $R_{\text{measured}}/R_{\text{expected}} = 0.86 \pm 0.05$ .



GALLEX experiment (SAGE  
similar)

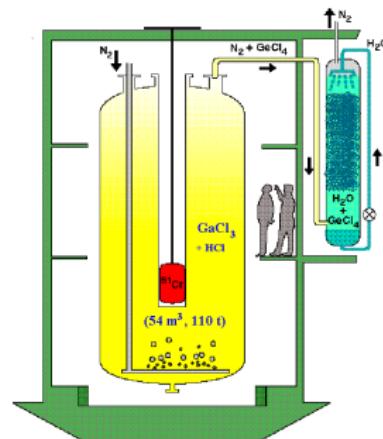


## Neutrino anomalies

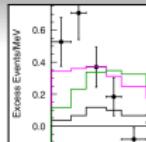
# Gallium Detectors

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- Calibrated using strong radioactive sources.
- Deficit in measured neutrinos:  
 $R_{\text{measured}}/R_{\text{expected}} = 0.86 \pm 0.05$ .
- Corresponds to  $\delta m^2_{\text{new}} \gtrsim 0.35 \text{ eV}^2$ .

(Giunti and Laveder, 2011,  
arxiv:1006.3244)

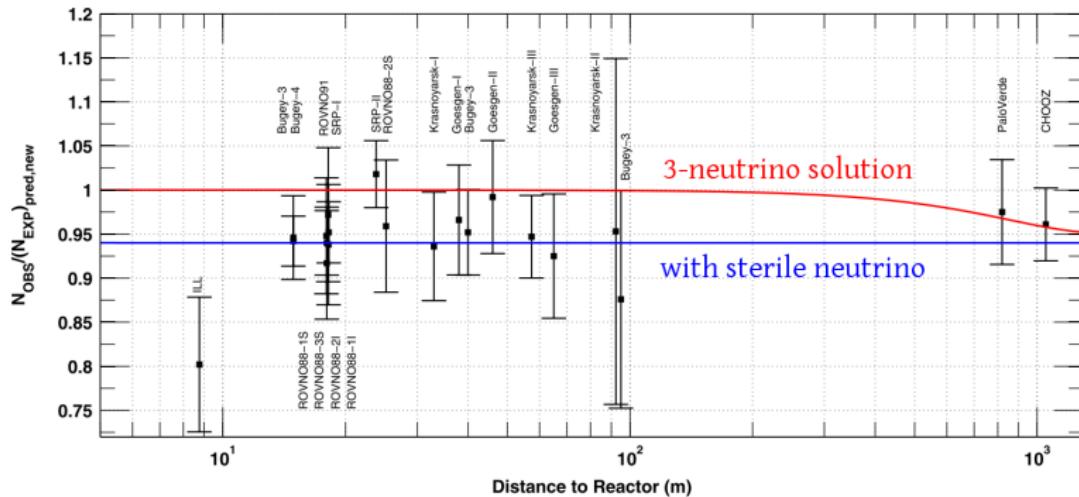


GALLEX experiment (SAGE  
similar)



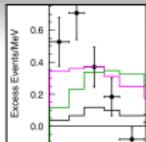
## Neutrino anomalies

# Reactor Anti-neutrinos



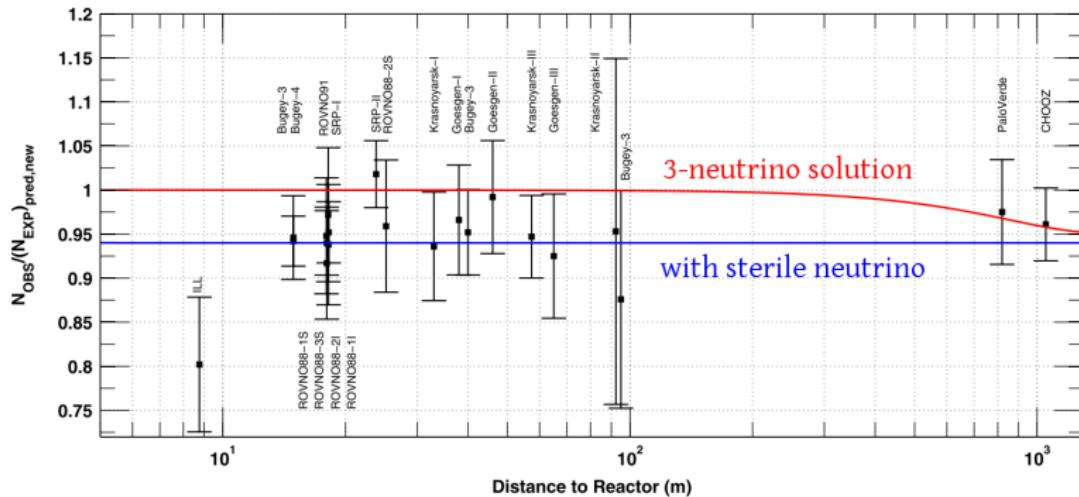
Anomaly points to  $\delta m_{\text{new}}^2 > 1.5 \text{ eV}^2$ .

Mention et al. 2011 (arXiv:1101.2755)



## Neutrino anomalies

# Reactor Anti-neutrinos

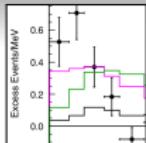


Anomaly points to  $\delta m_{\text{new}}^2 > 1.5 \text{ eV}^2$ .

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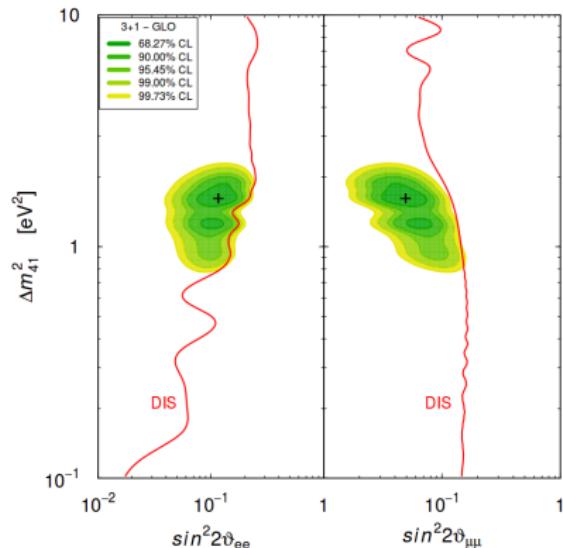
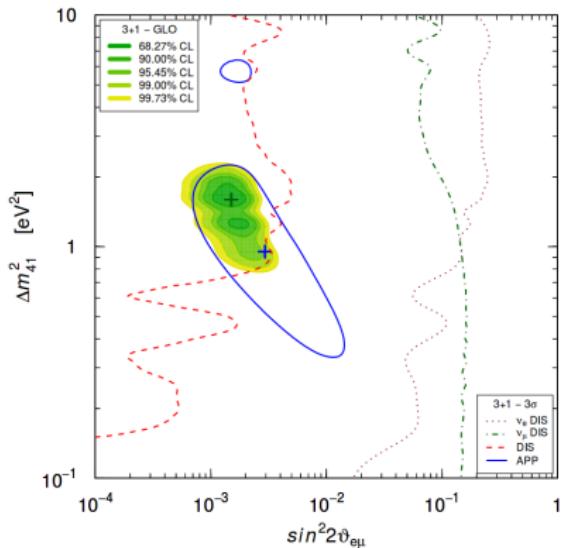
Larger uncertainty claimed by another group.

(Hayes et al. 2013 arXiv:1309.4146)

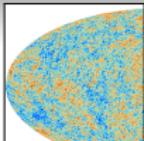


Neutrino anomalies

# Neutrino Anomalies - Global Fit



C. Giunti, M. Laveder, Y.F. Li and H.W. Long, 2013 (arxiv:1308.5288)

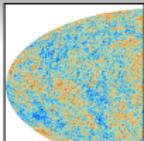


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## Cosmological Probes

Modifying neutrino physics can affect several aspects of cosmology:

- Big bang nucleosynthesis (BBN) via a changed expansion rate and modified nuclear reactions.
- The cosmological microwave background radiation (CMB) via a changed expansion rate and anisotropic stress.
- Large scale structures (LSS) via small scale damping.



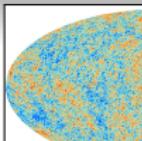
## Describing Neutrinos

The number of neutrinos is

$$N_{\text{eff}} \equiv \frac{\rho_{\nu, \text{rel}}}{\rho_{\nu 0}}, \quad \rho_{\nu 0} \equiv \frac{7}{8} \left( \frac{T_\nu}{T_\gamma} \right)^4 \rho_\gamma.$$

$N_{\text{eff}} = 3$  in the Standard Model, but other relativistic degrees of freedom will also enter.

$N_{\text{eff}} > 3$  effects the expansion of the Universe.

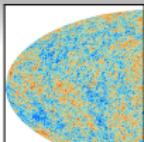


# Big Bang Nucleosynthesis

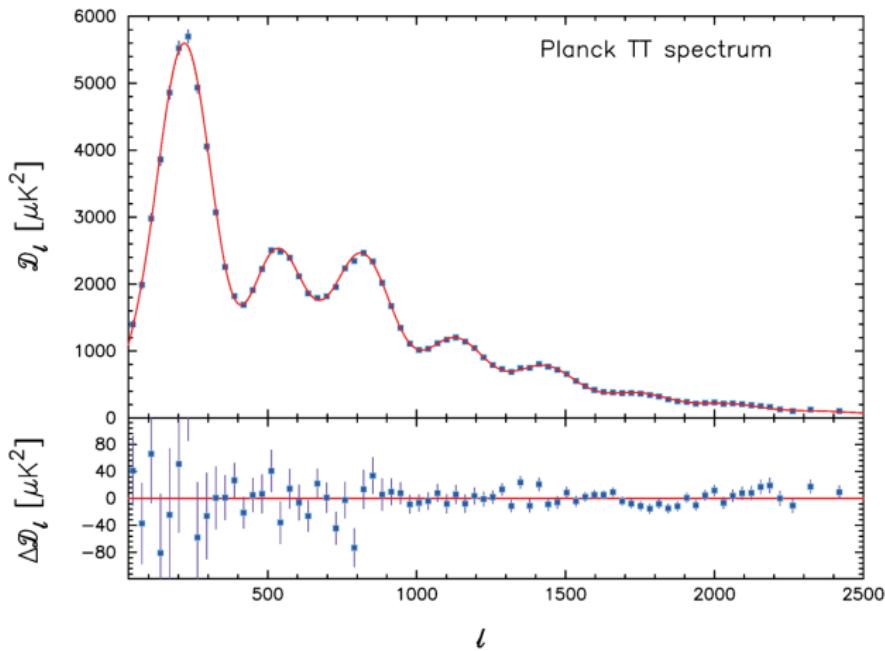
- ${}^4\text{He}$  content is controlled by  $n_n/n_p$ .
- $N_{\text{eff}}$  effects  $H$ , and thereby the energy at which  $p + e^- \leftrightarrow n + \nu_e$  freezes out.
- There are also smaller effects on the abundance of other elements.

Some of the latest limits:

- ${}^2\text{D}$ :  $N_{\text{eff}} = 3.0 \pm 0.5(1\sigma)$ . Pettini and Cooke, 2012 (arxiv:1205.3785)
- ${}^4\text{He}, {}^2\text{D}$ :  $N_{\text{eff}} < 4.0$  at 95% confidence. Mangano and Serpico, 2011 (arxiv:1103.1261)
- ${}^4\text{He}$ :  $N_{\text{eff}} = 3.68^{+0.80}_{-0.70}(2\sigma)$ . Izotov and Thuan, 2010 (arxiv:1001.4440)

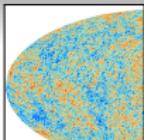


# Cosmological Microwave Background

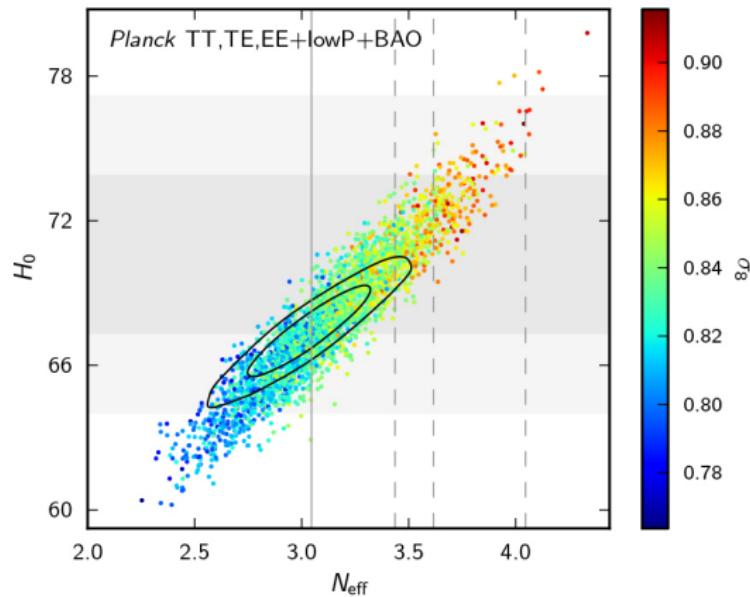


Ade et al., 2013 (arxiv:1303.5076)

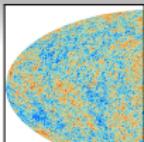
eV-Scale Sterile Neutrinos and Cosmology - Compatible or Not?



# Cosmological Microwave Background



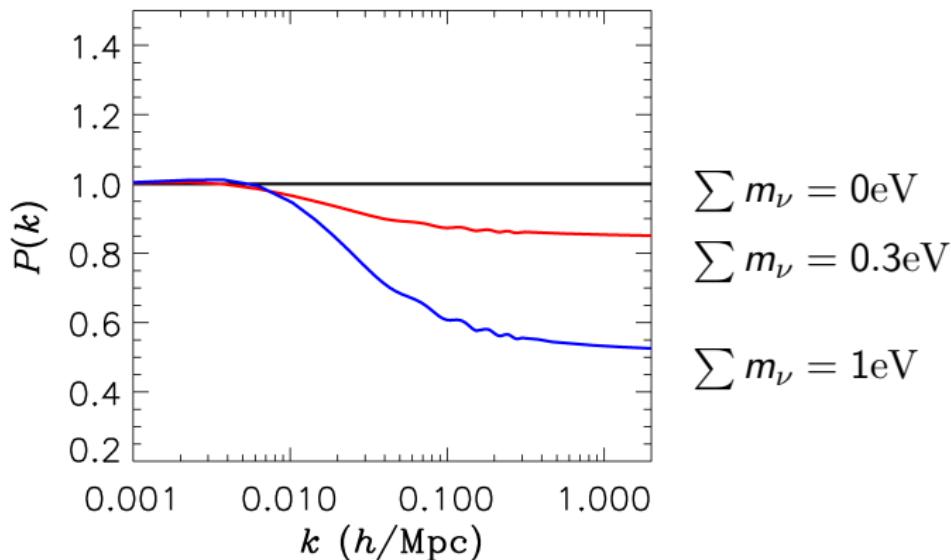
<http://public.planck.fr/resultats>

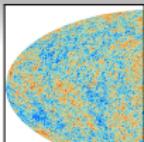


## Large Scale Structure

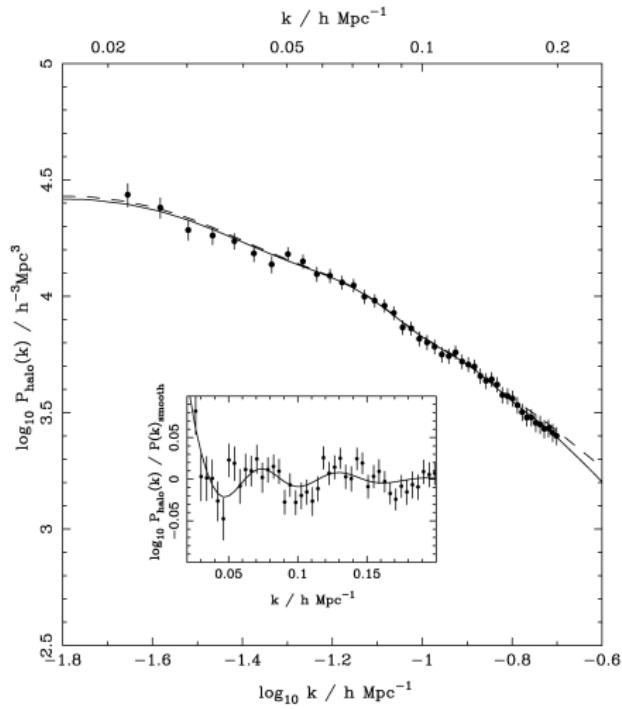
Neutrino mass damps formation of structures below the free streaming length.

Matter power spectrum:





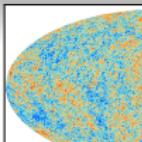
# Large Scale Structure



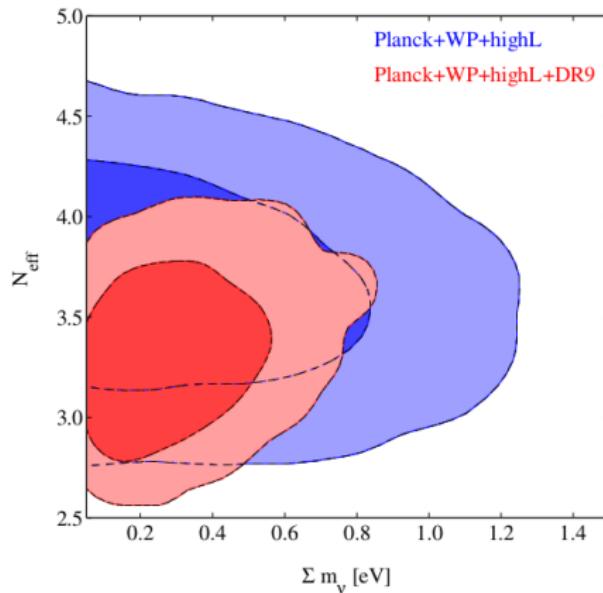
Luminous Red Galaxies  
spectrum, SDSS DR-7

Reid et al., 2009

(arXiv:0907.1659)



# Large Scale Structure

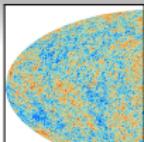


Archidiacono et al., 2013

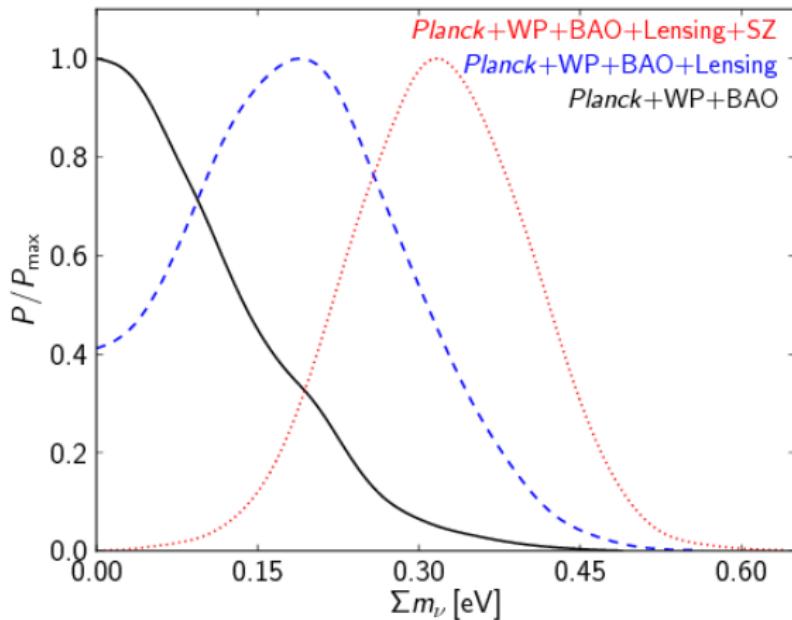
(arXiv:1307.0637)

Marginalized constraints:

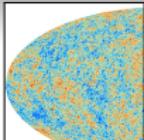
- Planck + WP:  
 $N_{\text{eff}} = 3.65 \pm 0.38$ ,  
 $\sum m_\nu < 1.03 \text{ eV}$ .
- Planck + WP +  
highL + DR9:  
 $N_{\text{eff}} = 3.33 \pm 0.31$ ,  
 $\sum m_\nu < 0.66 \text{ eV}$ .



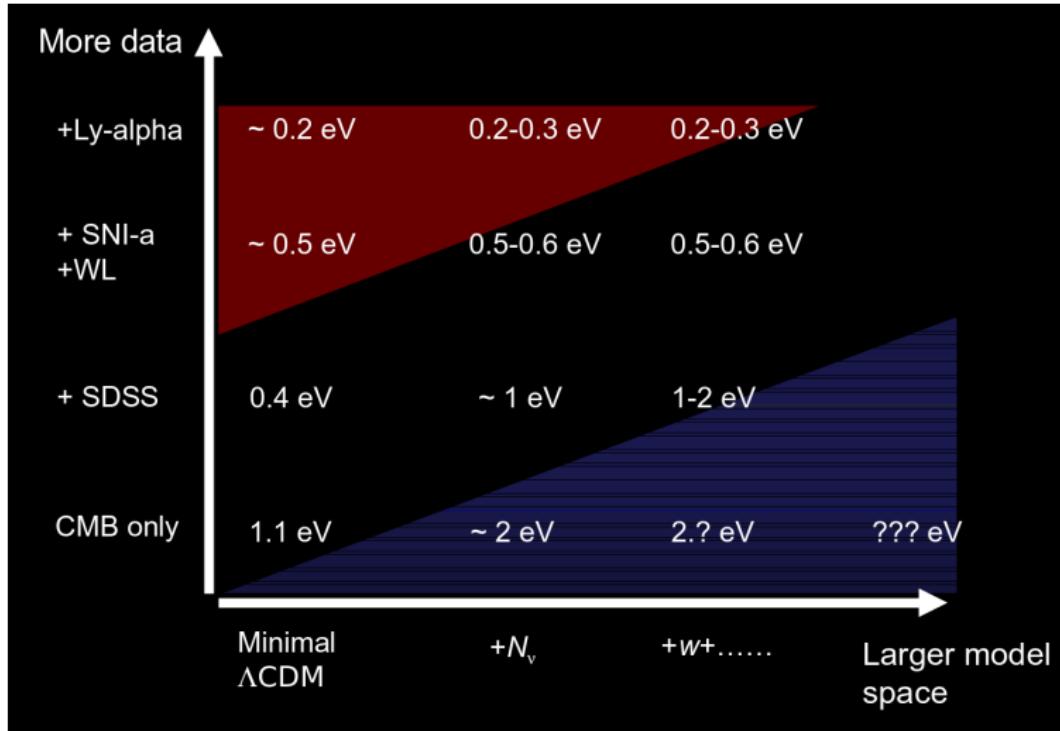
# Large Scale Structure

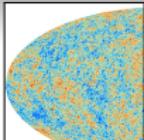


Battye and Moss (arXiv:1308.5870)

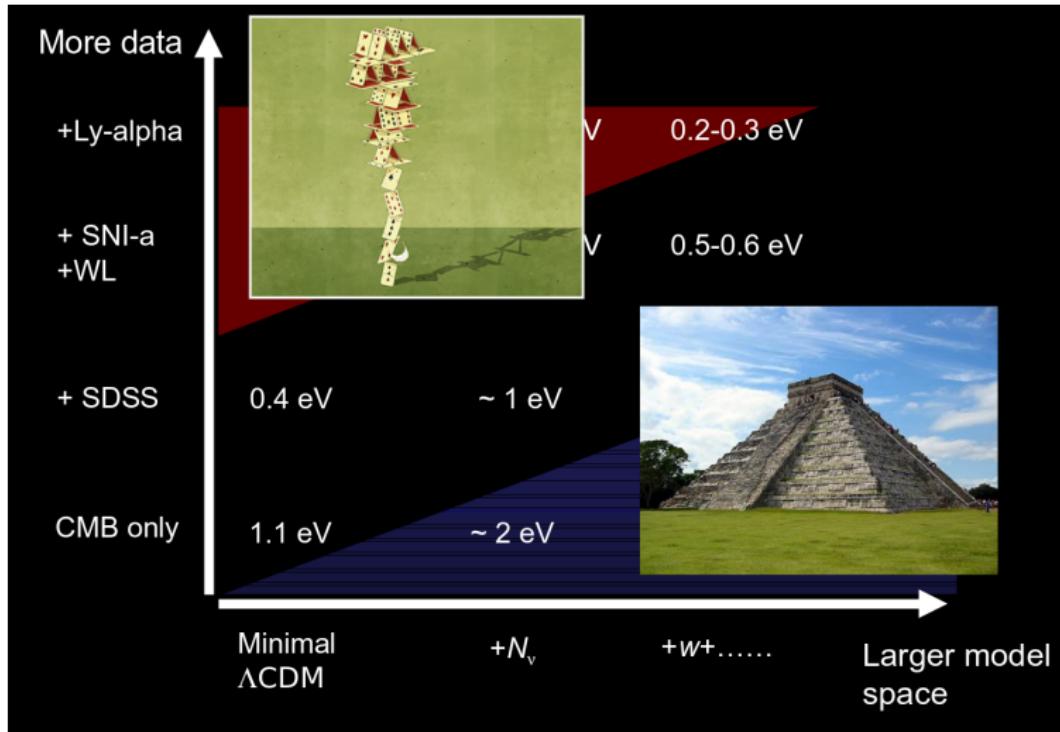


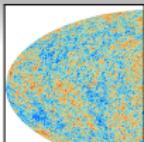
# Model Dependence, $\sum m_\nu$





# Model Dependence, $\sum m_\nu$

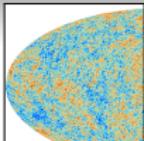




## Summary

$$\Delta N_{\text{eff}} \lesssim 1, \sum_i m_{\nu_i} < 1\text{eV}.$$

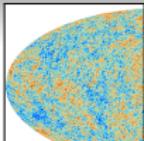
No room for a thermal, 1eV  
sterile neutrino.



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## eV-scale Sterile Neutrinos in Cosmology

- Sterile  $\sim$  no electro-weak or strong coupling.
- Mixed with active neutrinos.
- Non-resonant production if heavier than active neutrinos.
- Resonant production if lighter than active neutrinos, or non-standard matter potentials are present.
- Contributes to  $\Delta N_{\text{eff}}$  and  $\sum_i m_{\nu_i}$ .



## Quantum Kinetic Equations

Describe  $\nu_a$ ,  $\nu_s$ - oscillations using a density matrix:

$$\rho = \begin{pmatrix} \rho_{aa} & \rho_{as} \\ \rho_{sa} & \rho_{ss} \end{pmatrix}$$

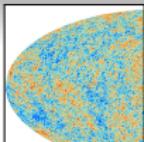
Which evolved according to the quantum kinetic equations:

$$i \frac{d\rho}{dt} = [H(\rho), \rho] + C(\rho)$$

$$H(\rho) = \begin{pmatrix} -\frac{\delta m^2}{2p} \cos 2\theta + V_{\text{matter}} & \frac{\delta m^2}{2p} \sin 2\theta \\ \frac{\delta m^2}{2p} \sin 2\theta & \frac{\delta m^2}{2p} \cos 2\theta - V_{\text{matter}} \end{pmatrix}$$

$C(\rho)$  is the higher order collision term treating non-forward scattering.

$V_{\text{matter}}$  is the potential induced by forward scattering with the background.



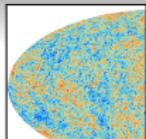
# Thermalisation

- Resonant conversion:
  - Diagonal term in  $H$  is 0.
  - MSW-like oscillations.

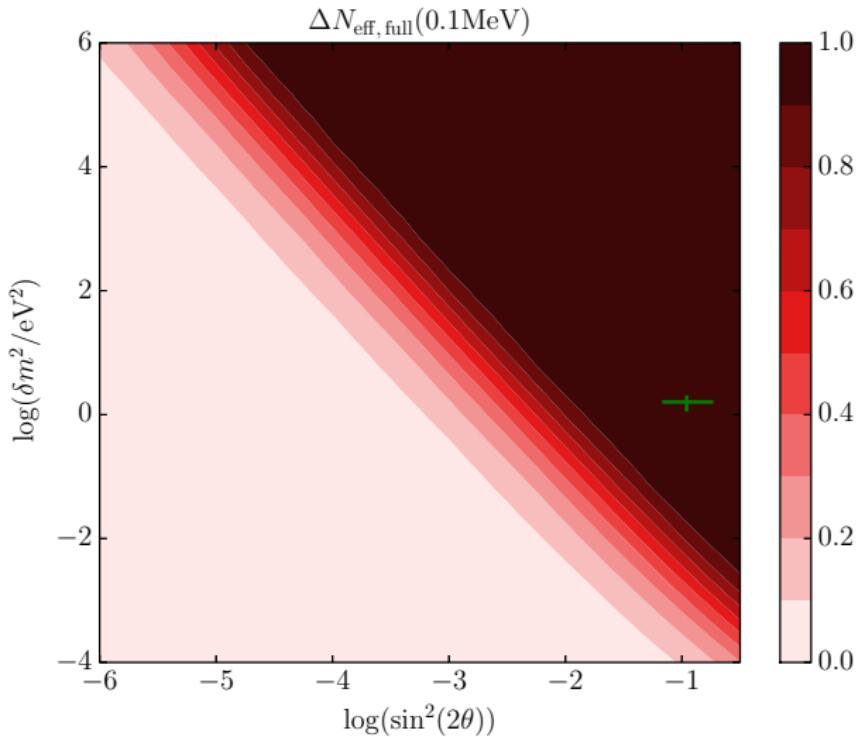
- Small angle oscillations:

$$\Gamma_{\text{thermalise}} = \frac{1}{2} \sin^2(2\theta_m) \Gamma_\nu$$

- $\Gamma_\nu \approx \langle \sigma v \rangle n_e$ .
- $\sin^2(2\theta_m)$  also depends on background.
- Compare  $\Gamma_{\text{thermalise}}$  to Hubble expansion rate.



# Thermalisation - Full Collision Term



X  
 $\chi$   
 $\varphi$

---

## Modifications to Cosmology

- Modified primordial power spectrum. Gariazzo, Giunti and Laveder, 2014 (arXiv:1412.7405)
- Low reheating temperature. Rehagen and Gelmini, 2014, (arXiv:1402.0607)
- Dilution by decay of heavy particles. Fuller, Kishimoto and Kusenko, 2011, (arXiv:1110.6479)
- Large lepton asymmetry. Foot and Volkas, 1995, Hannestad et al. 2012 (arxiv:1204.5861), Saviano et al. 2014 (arxiv:1302.1200)

X  
χ  
φ

## Large Lepton Asymmetry

Cosmology allows for a large lepton asymmetry  
(Remember that the baryon asymmetry  $\sim 10^{-10}$ )

$$L = \sum_f \frac{n_f - n_{\bar{f}}}{n_f} \sim 10^{-1}.$$

This gives rise to a modified matter potential

$$V_L = \frac{2\sqrt{2}\zeta(3)}{\pi^2} G_F T^3 L^{(a)}$$

X  
χ  
φ

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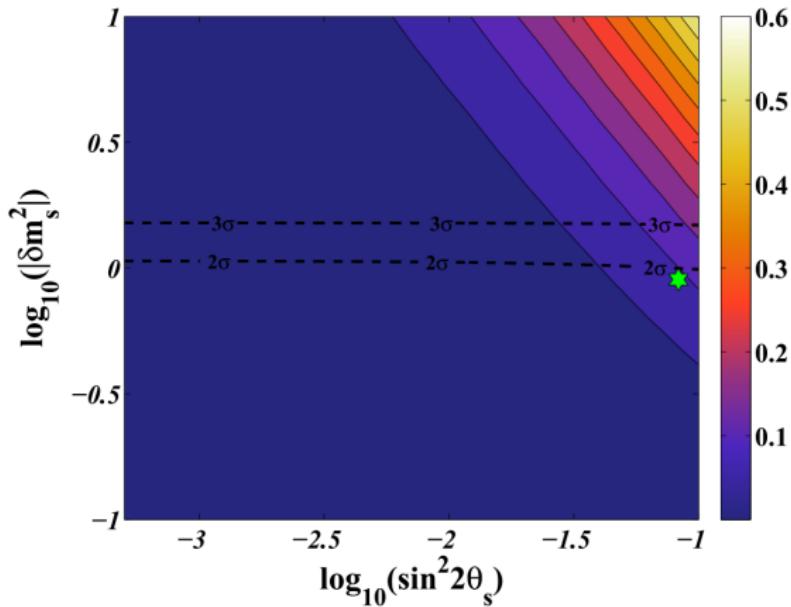
$$V_L = \frac{2\sqrt{2}\zeta(3)}{\pi^2} G_F T^3 L^{(a)}$$

$$L^{(e)} = \left( \frac{1}{2} + 2 \sin^2 \theta_W \right) L_e + \left( \frac{1}{2} - 2 \sin^2 \theta_W \right) L_p - \frac{1}{2} L_n + 2 L_{\nu_e} + L_{\nu_\mu} + L_{\nu_\tau}$$

$L \sim 10^{-2} \Rightarrow$  Suppress both small angle oscillations and resonant production until after  $\nu$  decoupling.

$X$   
 $\chi$   
 $\varphi$ 

# Large Lepton Asymmetry - Thermalisation

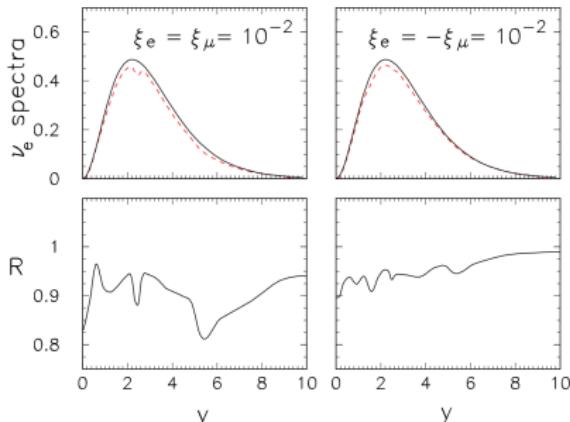


S. Hannestad, I. Tamborra, and T. Tram 2012 (arxiv:1204.5861)

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# Large Lepton Asymmetry

- There is some tension with BBN due to the spectral distortions.
- A mechanism to produce the large lepton asymmetry is missing.
- Possible problems with  $\sum_i m_{\nu_i}$  due to partly thermalised  $\nu_s$  after  $\nu$  decoupling.



Saviano et al., 2013 (arxiv:1302.1200)

X  
χ  
 $\varphi$

---

## Modifications to Particle Physics

Sterile - sterile interactions:

Vector couplings. Hannestad, RSH and Tram 2013 (arXiv:1310.5926), Dasgupta and Kopp, 2013 (arXiv:0805.3300), Saviano et al. 2014 (arXiv:1409.1680)

- Similar to known weak physics.
- Typical boson masses: MeV - GeV.
- Interaction strength decreases with temperature as usual for weak interactions.

X  
χ  
φ

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- Typical boson masses: MeV - GeV.
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Pseudoscalar couplings. Babu and Rothstein, 1992, Bento and Berezhiani 2001 (arxiv:hep-ph/0108064), Archidiacono et al. 2014 (arXiv:1404.5915)

- Well motivated by extended neutrino models, e.g. majorons.
- Typical boson masses:  $\lesssim$  meV.
- Interaction grows as temperature decreases giving rise to some counter-intuitive phenomena.

X  
χ  
φ

## Vector Models

Hannestad, RSH, Tram, 2013 (arXiv:1310.5926)

Fermi-like interaction:

$$G_X = \frac{g_X^2}{M_X^2} \gg G_F$$

$$V_s = \frac{16 G_X}{3\sqrt{2} M_X^2} p u_{\nu_s}$$

$$\Gamma_s = G_X^2 p T_{\nu_s}^4 n_{\nu_s}$$

X  
χ  
φ

## Vector Models

Hannestad, RSH, Tram, 2013 (arXiv:1310.5926)

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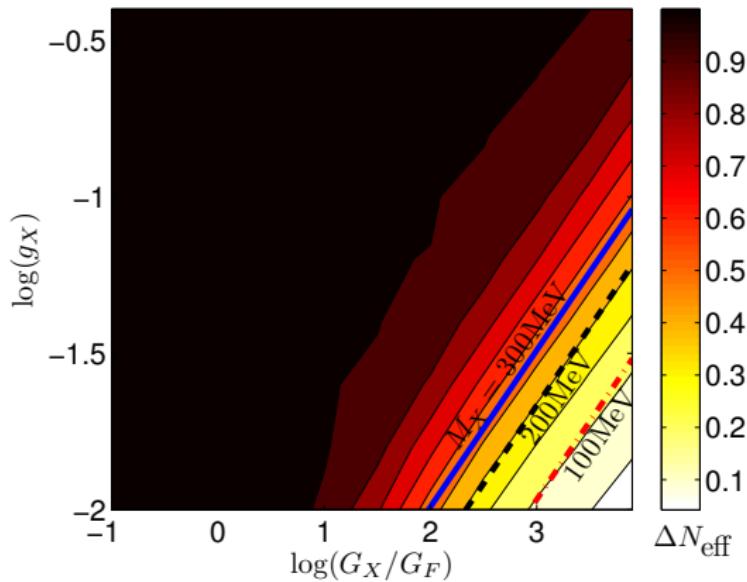
$$\Gamma_s = G_X^2 p T_{\nu_s}^4 n_{\nu_s}$$

$$\Gamma_{\text{thermalise}} \propto \sin^2(2\theta_m) \Gamma_\nu \propto \frac{M_X^4}{G_X^2} G_X^2 \propto M_X^4$$

⇒ Light mediator suppresses thermalisation.

X  
 $\chi$   
 $\varphi$

## Vector Models

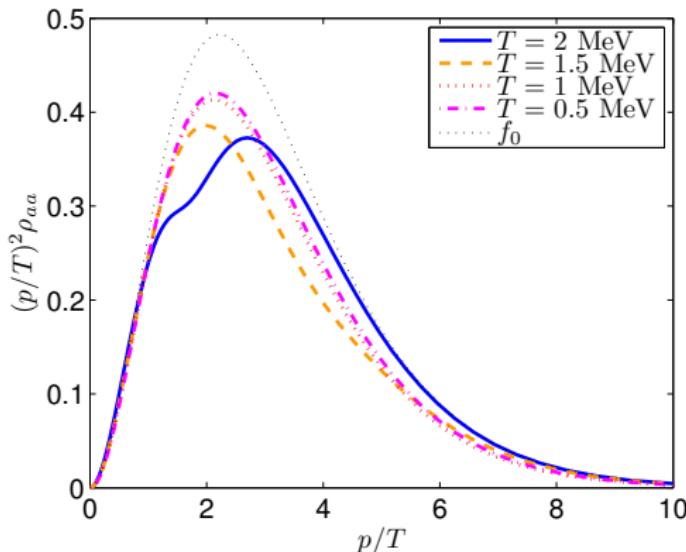


Hannestad, RSH, and Tram 2013 (arXiv:1310.5926)

## Vector Models - BBN

Non-thermal neutrino spectra might change BBN significantly.

$$G_X = 300 G_F, g_x = 0.025 \Rightarrow M_x = 424 \text{ MeV}$$

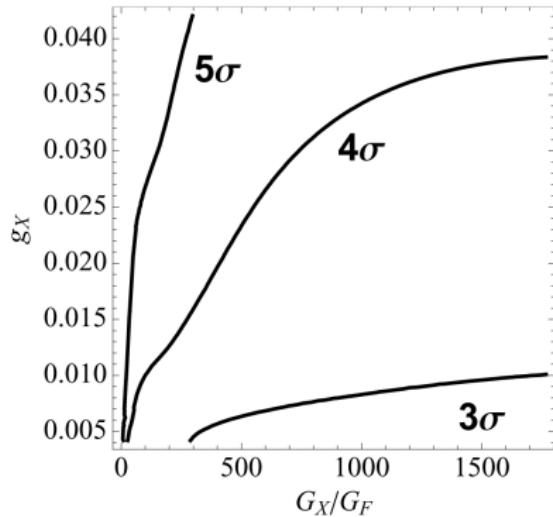


Hannestad, RSH, and Tram 2013 (arXiv:1310.5926)

X  
 $\chi$   
 $\varphi$

## Vector Models - BBN

Exclusion plot using  $^2\text{H}$ -data.



- Bounds can be weakened by raising the baryon density.
- A small  $m_X \lesssim 1\text{MeV}$  will delay the thermalisation until  $T \lesssim 0.1\text{MeV}$  and avoid BBN bounds.

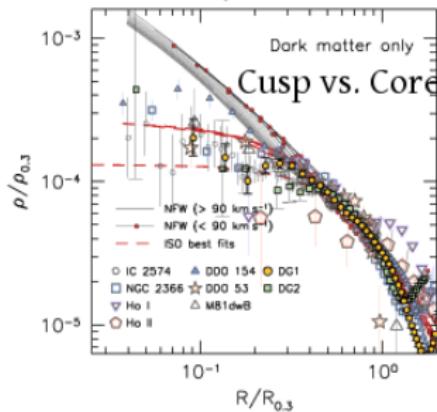
Saviano et al., 2014 (arXiv:1409.1680)

$X$     $\chi$   
 $\varphi$

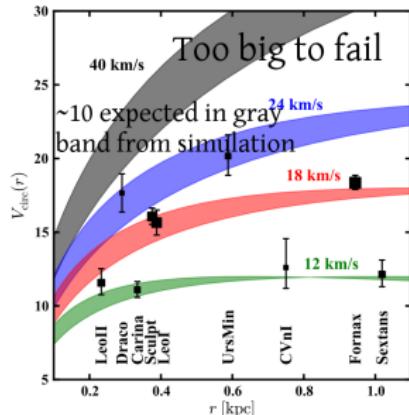
## Modifications to Particle Physics

# Vector Models - DM

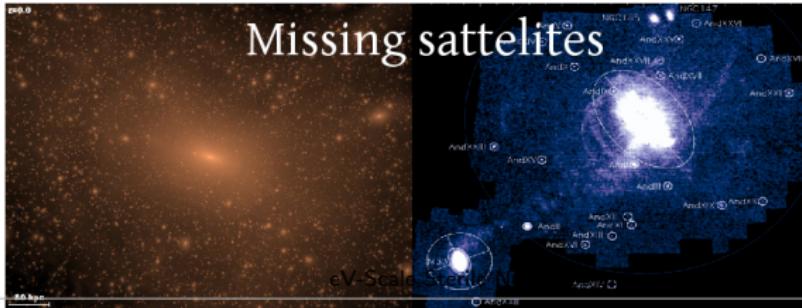
Oh et al., 2010 (arXiv:1011.2777)



Boylan-Kolchin et al., 2010 (arXiv:1111.2048)

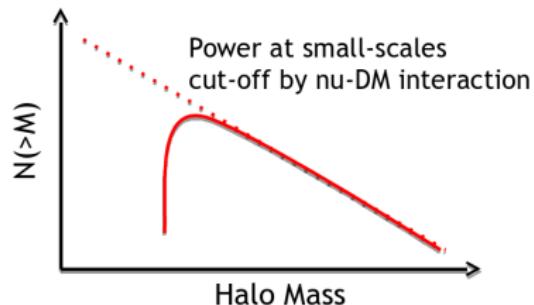
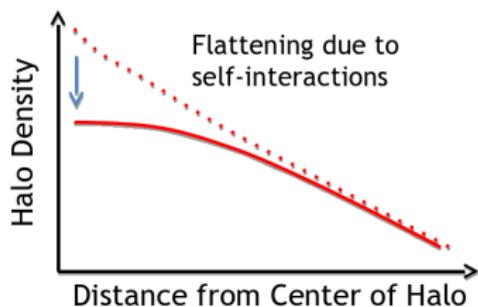


Via Lactea simulation and PAndAS Survey



$X$     $\chi$   
 $\varphi$

## Vector Models - DM



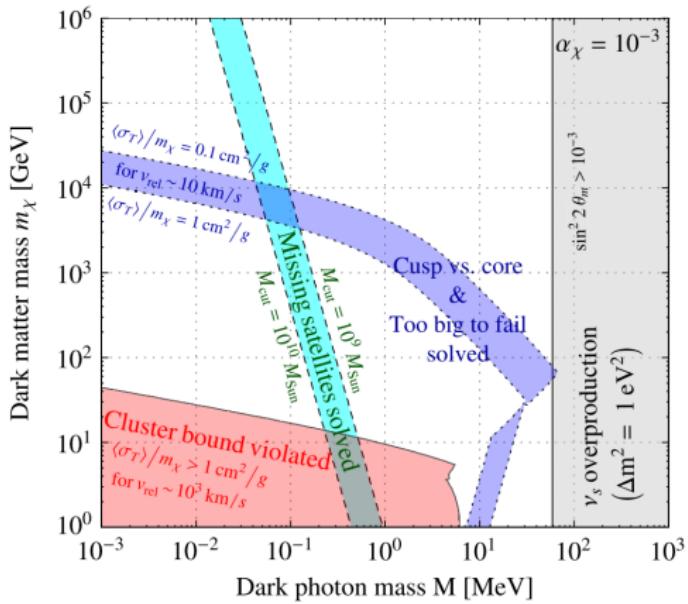
Core-Cusp problem solved using self-interactions.  
TBTF is also solved.

Missing Satellites solved using DM interactions with neutrinos, that leads to late kinetic decoupling

Basudep Dasgupta

X  
χ  
φ

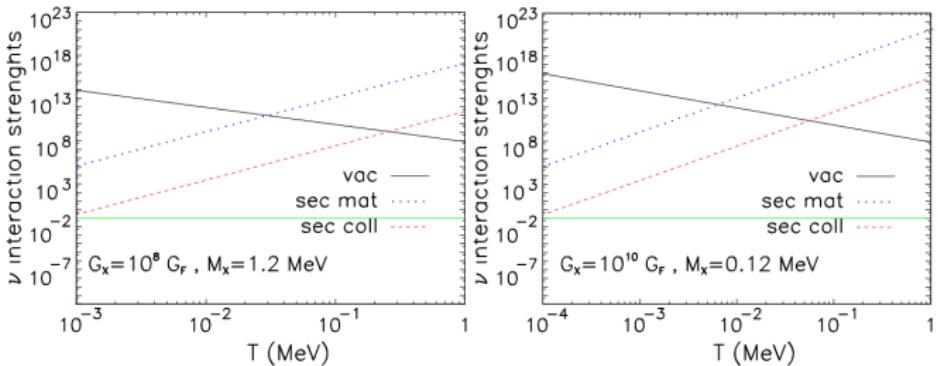
## Vector Models - DM



Dasgupta and Kopp, 2013 (arXiv:0805.3300)

see also Bringmann, Hasenkamp and Kersten, 2013 (arXiv:1312.4947)

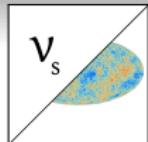
# Vector Models - low $T$ production of $\nu_s$



Mirizzi et  
al., 2014  
(arXiv:1410.1385)

1

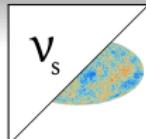
- After no matter suppression, thermalisation via collisions is possible.
- Might conflict with bounds on  $\sum_i m_{\nu_i}$ .
- Not for all parameters. (Disregarding resonant conversion)
- Can dilute with more  $\nu_s$ . Tang, 2014 (arXiv:1501.00059)



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## Summary

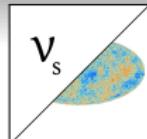
- eV-scale sterile neutrinos are incompatible with standard cosmology and particle physics.
- Different mechanisms can alleviate the tension, but some of them are constrained by other observables. I have reviewed three models today:
  - A large lepton asymmetry is pressed by constraints from BBN.
  - A sterile vector boson interaction gives problems with the neutrino mass bound.
  - A sterile pseudoscalar interaction seems promising, but has not been thoroughly examined yet.



# Sterile neutrino constraints

Dataset	$\Omega_m$	$\sigma_8$	$m_s^{\text{eff}} [\text{eV}]$		$\Delta N_{\text{eff}}$	
			68%CL	95%CL	68%CL	95%CL
Planck	$0.322^{+0.025}_{-0.030}$	$0.800^{+0.052}_{-0.031}$	$< 0.34$	$< 0.86$	$0.49^{+0.18}_{-0.42}$	$< 1.07$
Planck+Cluster	$0.304^{+0.026}_{-0.027}$	$0.745^{+0.023}_{-0.037}$	$0.54^{+0.26}_{-0.26}$	$< 0.98$	$0.84^{+0.32}_{-0.32}$	$0.84^{+0.63}_{-0.60}$
Planck+Cluster( $B_M$ )	$0.295^{+0.019}_{-0.028}$	$0.794^{+0.040}_{-0.032}$	$< 0.38$	$< 0.69$	$0.85^{+0.28}_{-0.30}$	$0.85^{+0.56}_{-0.57}$
Planck+Cluster(BC)	$0.296^{+0.023}_{-0.028}$	$0.770^{+0.031}_{-0.036}$	$0.40^{+0.31}_{-0.19}$	$< 0.81$	$0.88^{+0.30}_{-0.29}$	$0.88^{+0.61}_{-0.60}$
Planck+BAO	$0.306^{+0.009}_{-0.009}$	$0.818^{+0.033}_{-0.026}$	$< 0.19$	$< 0.43$	$0.50^{+0.22}_{-0.39}$	$< 1.04$
Planck+Shear	$0.309^{+0.028}_{-0.028}$	$0.752^{+0.037}_{-0.043}$	$0.48^{+0.22}_{-0.38}$	$< 0.99$	$0.53^{+0.22}_{-0.37}$	$< 1.30$
Planck+Ly- $\alpha$	$0.309^{+0.023}_{-0.024}$	$0.843^{+0.021}_{-0.021}$	$< 0.11$	$< 0.27$	$0.65^{+0.30}_{-0.38}$	$< 1.49$
Planck+BAO+Cluster	$0.303^{+0.009}_{-0.009}$	$0.744^{+0.013}_{-0.014}$	$0.53^{+0.12}_{-0.13}$	$0.53^{+0.26}_{-0.24}$	$0.81^{+0.31}_{-0.32}$	$0.81^{+0.60}_{-0.63}$
Planck+BAO+Cluster( $B_M$ )	$0.303^{+0.007}_{-0.009}$	$0.782^{+0.020}_{-0.018}$	$0.35^{+0.13}_{-0.15}$	$0.35^{+0.27}_{-0.27}$	$0.81^{+0.29}_{-0.30}$	$0.81^{+0.60}_{-0.58}$
Planck+BAO+Shear	$0.305^{+0.09}_{-0.010}$	$0.753^{+0.023}_{-0.022}$	$0.44^{+0.16}_{-0.19}$	$0.44^{+0.34}_{-0.35}$	$0.45^{+0.14}_{-0.40}$	$< 0.99$
Planck+BAO+Ly- $\alpha$	$0.305^{+0.09}_{-0.010}$	$0.844^{+0.020}_{-0.019}$	$< 0.10$	$< 0.22$	$0.61^{+0.28}_{-0.32}$	$< 1.11$
Planck+BAO+Shear+Cluster( $B_M$ )	$0.303^{+0.009}_{-0.009}$	$0.759^{+0.017}_{-0.020}$	$0.44^{+0.14}_{-0.14}$	$0.44^{+0.28}_{-0.26}$	$0.78^{+0.31}_{-0.30}$	$0.78^{+0.60}_{-0.59}$
Planck+BAO+Ly- $\alpha$ +Shear+Cluster( $B_M$ )	$0.293^{+0.009}_{-0.008}$	$0.794^{+0.016}_{-0.016}$	$0.26^{+0.11}_{-0.13}$	$0.26^{+0.22}_{-0.24}$	$0.82^{+0.27}_{-0.31}$	$0.82^{+0.55}_{-0.55}$

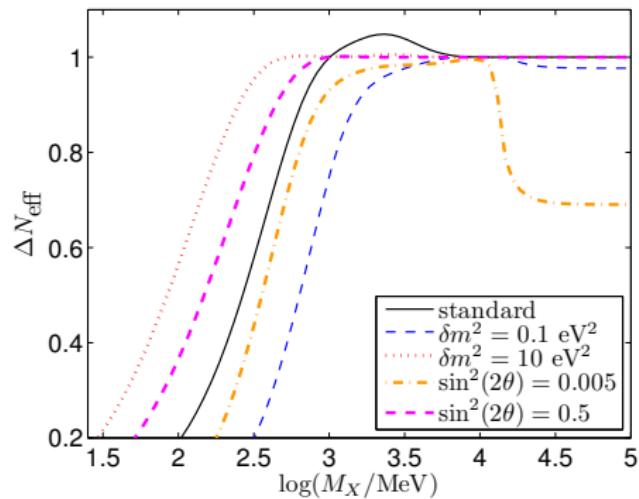
Costanzi et al. 2014 (arXiv:1407.8338)



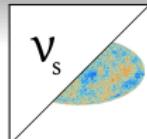
# Sterile Interactions

The mechanism is not very sensitive to the exact values of  $\delta m^2$  and  $\sin^2 2\theta$ .

$$\delta m^2 = 1 \text{ eV}^2, \sin^2(2\theta) = 0.05$$

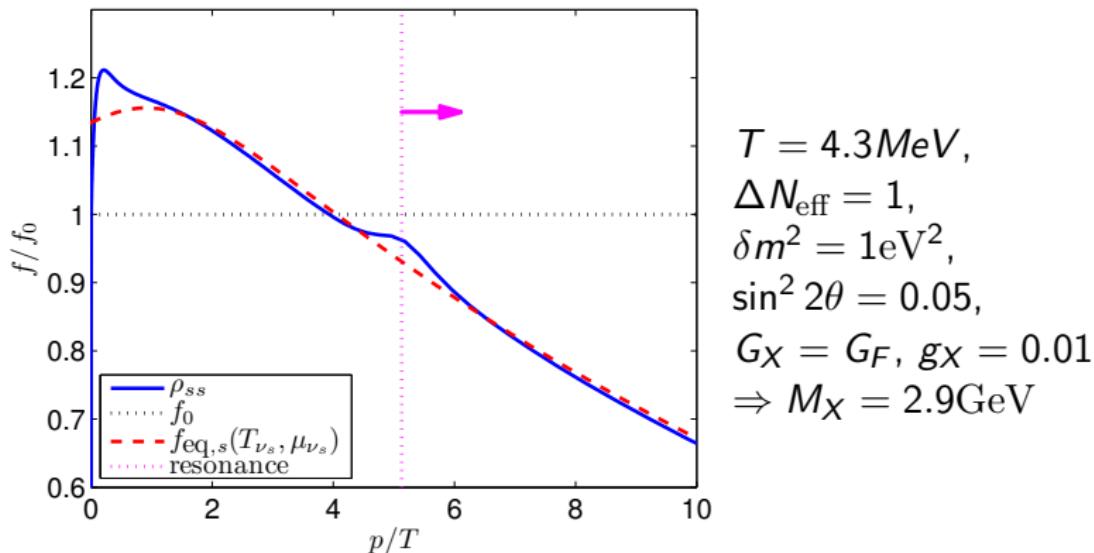


Hannestad, RSH, and Tram 2013 (arXiv:1310.5926)

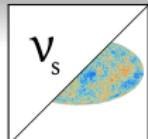


## How Can $\Delta N_{\text{eff}} > 1$ ?

The conversion is efficient at the resonance, where  $\rho_{ss} < \rho_{aa} \sim f_0$ , but not below the resonance where  $\rho_{ss} > \rho_{aa}$ .



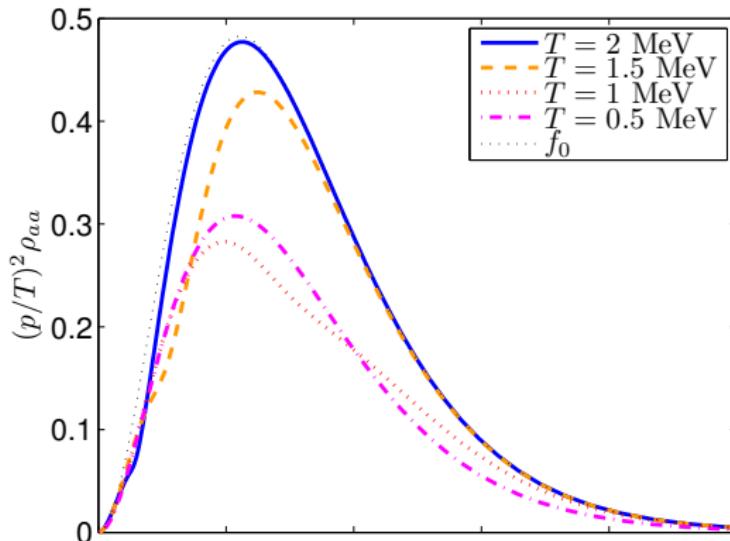
Hannestad, RSH, and Tram 2013 (arXiv:1310.5926)



## Effects on BBN - Open Questions

Non-thermal neutrino spectra might change BBN significantly.

$$G_X = 3000 G_F, g_x = 0.025 \Rightarrow M_x = 134 \text{ MeV}$$



Hannestad, RSH, and Tram 2013 (arXiv:1310.5926)