

Lepton (flavour) asymmetries in the early universe



Valerie Domcke CERN

Seminar at *MPIK Heidelberg* 05.02.2024

based on 2208.03237 with K. Kamda, K. Mukaida, K. Schmitz and M. Yamada

baryon asymmetry at BBN (~ 1 MeV) and CMB decoupling (~ eV) : $\frac{n_B}{s} \simeq 8.7 \times 10^{-11}$

In SM, B – L and B + L are conserved below EWPT / sphaleron freeze-out (~ 100 GeV). Above, sphaleron processes drive B + L = 0.

 \rightarrow constrains lepton asymmetry :







Observationally, O(1) lepton flavour asymmetries are not excluded

> Hints from BBN (helium anomaly) and CMB (polarization) for large CP violation

Burns, Tait, Valli 22, Minami, Komatsu 20

Implications for baryogenesis, CP-violating BSM physics, thermal phase transitions,....

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Implications for baryogenesis, CP-violating BSM physics, thermal phase transitions,....

Outline of this talk:

- implications of large spontaneous CP violation in the early universe
- new bounds on lepton flavour asymmetries
- implications for baryogenesis

(1) SM interactions and conserved charges

exactly conserved charges:

$$B/3 - L_{\alpha}, Y$$

(lepton flavour, hypercharge)

• in the early Universe, SM interactions cannot keep up with expansion

 \rightarrow additional approximately conserved charges $q_X = n_X - n_{\bar{X}} = \mu_X T^2/6$:



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 \rightarrow additional approximately conserved charges $q_X = n_X - n_{\bar{X}} = \mu_X T^2/6$:

	$T \; [\text{GeV}]$	$ y_e$	y_{ds}	y_d	y_s	y_{sb}	y_{μ}	y_c	$y_{ au}$	y_b	WS	SS	y_t
(\mathbf{v})	$(10^5, 10^6)$	q_e	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
(iv)	$(10^6, 10^9)$	q_e	$q_{2B_1-B_2-B_3}$	q_{u-d}	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
(iii)	$(10^9, 10^{11-12})$	q_e	$q_{2B_1-B_2-B_3}$	q_{u-d}	q_{d-s}	$q_{B_1-B_2}$	q_{μ}	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
(ii)	$(10^{11-12}, 10^{13})$	q_e	$q_{2B_1-B_2-B_3}$	q_{u-d}	q_{d-s}	$q_{B_1-B_2}$	q_{μ}	q_{u-c}	q_{τ}	q_{d-b}	q_B	\checkmark	\checkmark
(i)	$(10^{13}, 10^{15})$	$ q_e$	$q_{2B_1-B_2-B_3}$	q_{u-d}	q_{d-s}	$q_{B_1-B_2}$	q_{μ}	q_{u-c}	q_{τ}	q_{d-b}	q_B	q_u	\checkmark

conserved charges + # equilibrated interactions = # particle species = 16

asymmetries are redistributed across different species

(2) chiral plasma instability

chiral magnetohydrodynamics (MHD) : hyper gauge fields, plasma w asymmetries

classical Maxwell eqs with
$$J_Y = \sigma_Y (E_Y + v \times B_Y) + \frac{2\alpha_Y}{\pi} \mu_{Y,5} B_Y$$

conductivity

fluid velocity \rightarrow inverse cascade

chiral magnetic effect → chiral plasma instability

 $\mu_{Y,5} = \sum_{i} \varepsilon_{i} g_{i} Y_{i}^{2} \mu_{i}$ chiral chemical potential

(2) chiral plasma instability

chiral magnetohydrodynamics (MHD) : hyper gauge fields, plasma w asymmetries



modes of one helicity with $k < k_{CPI} \equiv \alpha_Y |\mu_{Y,5}| / \pi$ become tachyonically unstable for $|\mu_{Y,5}| \neq 0$

(2) chiral plasma instability

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modes of one helicity with $k < k_{CPI} \equiv \alpha_Y |\mu_{Y,5}| / \pi$ become tachyonically unstable for $|\mu_{Y,5}| \neq 0$

chiral chemical potential converted into helical gauge fields $h = \pi T^2 / \alpha_Y \mu_{Y,5}$ at

$$T_{\rm CPI} \sim 10^5 \text{ GeV} \left(\frac{10^2}{g_*}\right)^{\frac{1}{2}} \left(\frac{\alpha_Y}{0.01}\right)^2 \left(\frac{10^2 T}{\sigma_Y}\right) \left(\frac{\mu_{Y,5}/T}{2 \cdot 10^{-3}}\right)^2 \Big|_{T_{\rm CPI}}$$

$$T_{Y_e} \swarrow$$
Kamada `18
asymmetries in the early universe
5/22
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(3) inverse cascade

Brandenburger et al `17 Schober et al `18

neglecting the fluid velocity, diffusion will erase helical gauge fields on short scales.

fluid velocity introduces non-linear mode coupling, free energy is minimized when helicity stored in long-wave length modes \rightarrow inverse cascade

For sufficiently large helical fields (ie Reynolds number > 1) inverse cascade is triggered and helicity is protected from diffusion

helical gauge fields can survive even after chemical potentials are erased

At EW phase transition, hypermagnetic helicity converted to EM helicity

generation of B+L asymmetry due to ABJ anomaly

Joyce, Shaposhnikov `97

Sphaleron wash-out decouples at EW phase transition

final B+L asymmetry sensitive to detailed time evolution of EW PT

Baryon asymmetry today estimated as:

Kamada, Long `16

$$\frac{n_B^h}{s} = c_B^{\text{dec}} \frac{\alpha_Y}{2\pi} \frac{h}{n_\gamma} \sim 10^{-6} h/T^3 \sim 10^{-4} (\mu_{Y,5}/T)_{T_{\text{CPI}}}$$

for $|\mu| \gtrsim 10^{-6}$ danger of massive overproduction of baryon asymmetry in SM EW PT !

summary and outline

- implications of large spontaneous CP violation in the early universe
 - SM interactions re-shuffle particle asymmetries
 - chiral plasma instability: $\mu \mapsto h$
 - helicity can survive until EW PT and generate (large) baryon asymmetry

- new bounds on lepton flavour asymmetries
- implications for baryogenesis

e.g. at T ~ $10^{5..6}$ GeV

Domcke, Kamada, Mukaida, Schmitz, Yamada `22

$$\frac{\mu_{Y,5}}{T} = \frac{711}{481} \frac{\mu_e}{T} + \frac{5}{13} \frac{\mu_{\Delta_e}}{T} + \frac{4}{37} \frac{\mu_{\Delta_{\mu+\tau}}}{T} \,,$$

 $\Delta_{\alpha} = B/3 - L_{\alpha}$

all SM interactions in equilibrium except electron Yukawa

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consider only B-L conserving lepton flavour asymmetries

 $\mu_e^{
m ini} = 0\,, \quad \sum_lpha \mu_{\Delta_lpha} = 0$

 $\rightarrow \mu_{Y,5} \sim \mu_{\Delta_{\alpha}} \neq 0$

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last SM coupling (electron Yukawa) comes into equilibrium

overproduction of baryon asymmetry if

$$T_{\rm CPI} \gtrsim 10^5 \text{ GeV} \rightarrow \left| \frac{\mu_{\Delta_e}}{T} \right| = \left| \frac{\mu_{\Delta_\mu} + \mu_{\Delta_\tau}}{T} \right| > 0.01$$
 and
 $\frac{n_B}{s} > 10^{-10} \rightarrow |\mu_{\Delta_\alpha}/T| \gtrsim 10^{-5}$

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Domcke, Kamada, Mukaida, Schmitz, Yamada `22



- applies also for B-L = 0 \rightarrow in that case factor 100 stronger than BBN bound
- applies at $T > 10^5$ GeV \longrightarrow constraint on primordial asymmetries
- disfavours leptoflavourgenesis Mukaida, Schmitz, Yamada `21
- if marginally fulfilled, provides a viable (though tuned) baryogenesis mechanism
- sensitive to CPI dynamics, not sensitive to EW PT dynamics
- non-perturbative SU(2) processes (sphalerons) + $\eta_B^{obs} \rightarrow bound on primordial B-L$ non-perturbative U(1) processes (CPI) + $\eta_B^{obs} \rightarrow bound on primordial LFAs$

implications for baryogenesis

models with temporarily large (lepton) asymmetries in the early Universe can lead to large baryon asymmetries

Axiogenesis	[Co, Domcke, Harigaya `22]
Axion inflation	[VD, Kamada, Mukaida, Schmitz, Yamada `22]
wash-in leptogenesis	[VD, Kamada, Mukaida, Schmitz, Yamada `20]

algebraic framework for tracking evolution of chemical potentials

VD, Kamada, Mukaida, Schmitz, Yamada `20,`22

implications for axiogenesis



implications for axiogenesis



implications for axiogensis



 $T > T_S$ inspiral phase

 $T < T_S$ rotation in local minimum of Mexican hat potential

DM production:
$$(T < T_{\rm QCD} < T_S)$$
 $r|\dot{\theta}|^2/s$
 $\Omega_a h^2 = \Omega_{\rm DM} h^2 \times c_\Omega \left(\frac{10^9 \text{ GeV}}{f_a}\right) \left(\frac{Y_{\theta}}{73.3}\right)$

implications for axiogensis



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chiral plasma instability: $(T_{CPI} > T_S)$

$$T_{\rm CPI}^{\rm MD} \simeq 3.0 \ {\rm PeV} \, |c_5|^{4/5} \, c_{\Omega}^{1/5} \left(\frac{10}{c_{\rm CPI}} \frac{50 \, T}{\sigma_Y}\right)^{\frac{2}{5}} \left(\frac{N_{\rm DW} \, m_{\sigma}}{10^5 \ {\rm GeV}}\right)^{\frac{3}{5}} \left(\frac{10^9 \ {\rm GeV}}{f_a}\right)^{\frac{1}{5}} \left(\frac{g_{\rm MSSM}}{g_*(T_{\rm CPI}^{\rm MD})}\right)^{\frac{1}{5}}$$

- CPI is avoided only if $T_{\rm CPI} < T_S$
- If CPI occurs, overproduction of BAU in entire parameter space viable for DM

implications for axiogenesis



Summary

- (spontaneous) CP violation in the early universe can trigger chiral plasma instability, inverse cascade and baryogenesis
- new bound on primordial B-L conserving lepton flavour asymmetries, $|\mu_{\Delta_{\alpha}}|/T < 0.01$
- framework to constrain or predict relic baryon asymmetry for models with large primordial asymmetries

Summary

- (spontaneous) CP violation in the early universe can trigger chiral plasma instability, inverse cascade and baryogenesis
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initial conditions



eg axion inflation $\mu_i/T \sim Q_{Y,i}^2$

axion inflation: additional contribution from decaying helical hypermagnetic fields see VD, von Harling, Morgante, Mukaida `19









'axion' inflation, a minimal setup for SM + inflation:

Domcke, Kamada, Mukaida, Schmitz, Yamada `22

$$\begin{array}{c} \begin{array}{c} \text{axion with} \\ \text{scalar potential} \end{array} & \begin{array}{c} (\text{hyper charge}) \\ \text{U(1) gauge field} \end{array} & \begin{array}{c} \text{massless (SM)} \\ \text{fermions} \end{array} & \begin{array}{c} \text{axion gauge field} \\ \text{coupling} \end{array} \\ \mathcal{L} = \sqrt{-g} \left[\frac{1}{2} \partial^{\mu} \phi \partial_{\mu} \phi - V(\phi) \right] - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \sum_{\alpha} \bar{\psi}_{\alpha} (i\partial \cdot \gamma - gQA \cdot \gamma) \psi_{\alpha} + \frac{\alpha \phi}{4\pi f_{a}} F_{\mu\nu} \tilde{F}^{\mu\nu} \\ \hline (\partial_{\mu} \phi) \bar{\psi} \gamma^{\mu} \gamma^{5} \psi \end{array}$$

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• exponential production of helical gauge fields through tachyonic instability for $\dot{\phi} \neq 0$

chemical potentials for fermions

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chemical potentials for fermions

two contribution to final baryon asymmetry:

$$\eta_B^h \simeq 7.5 \cdot 10^{-3} \left(\frac{c_B^{\text{dec}}}{0.05}\right) \chi$$

from decaying helical hypermagn. gauge fields

$$\eta_B^{\rm N} \simeq 0.01 \left(\frac{c_B^{\rm N}}{0.1}\right) \chi$$

from re-shuffling chemical potentials if right-handed neutrinos included (B-L) = wash-in leptogenesis

asymmetries in the early universe

 $\chi = \frac{q_{CS}}{2T^3} \Big|_{\rm rh}$



- evolution of primordial asymmetries for axion inflation
- analytical expressions for general initial conditions at all temperature ranges given in

Domcke, Kamada, Mukaida, Schmitz, Yamada `22



$$\xi = \frac{\alpha_Y \dot{\phi}}{2H f_a}$$

onset of CPI cancels off helicity and chemical potentials

diffusion erases gauge fields (for conservative estimate of Reynold number)

for RHN mass scale above diffusion temperature, successful wash-in leptogenesis

 $\chi \sim 10^{-8}$ naturally achieved in axion inflation

axion inflation can account for successful baryogenesis



baryogenesis via helicity decay and wash-in leptogenesis

asymmetries in the early universe