



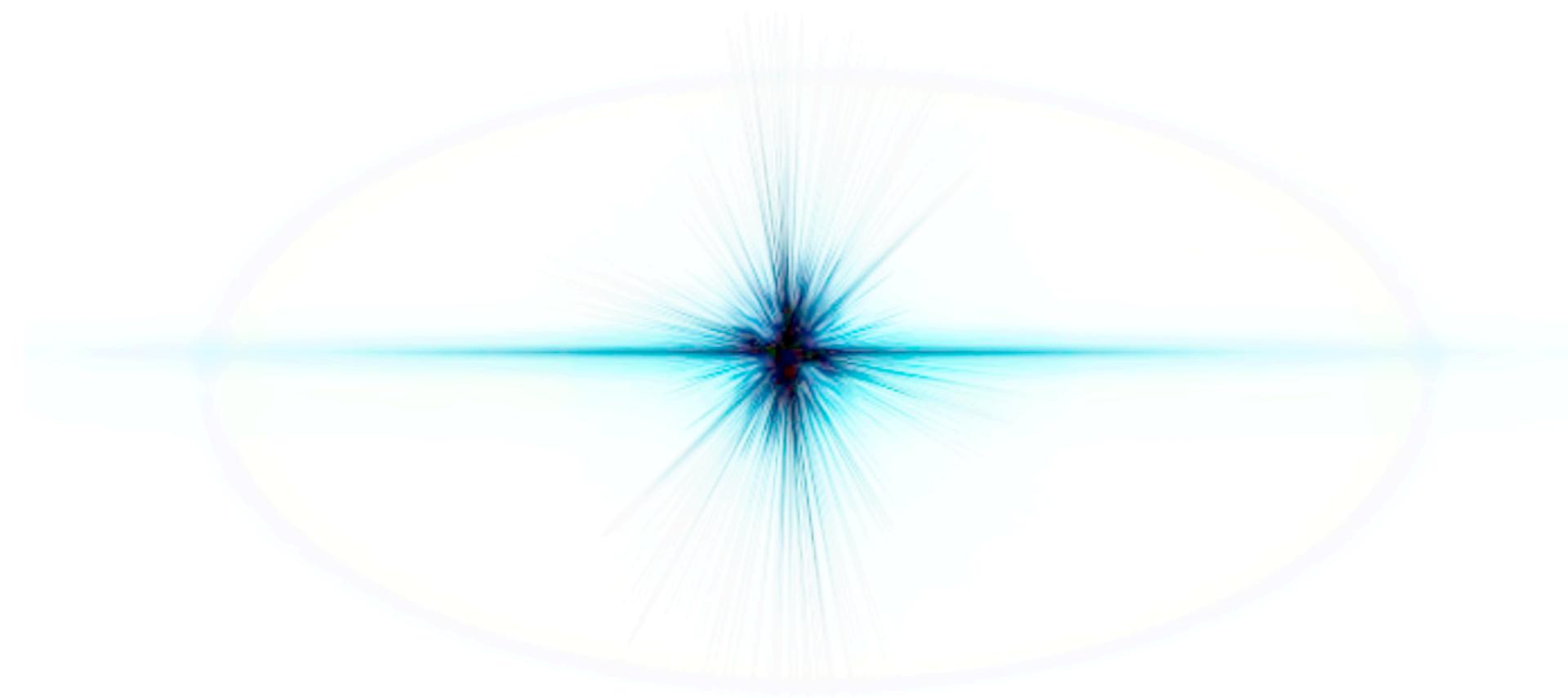
MAX-PLANCK-INSTITUT  
FÜR KERNPHYSIK  
HEIDELBERG

# The electromagnetic properties of a light dark sector

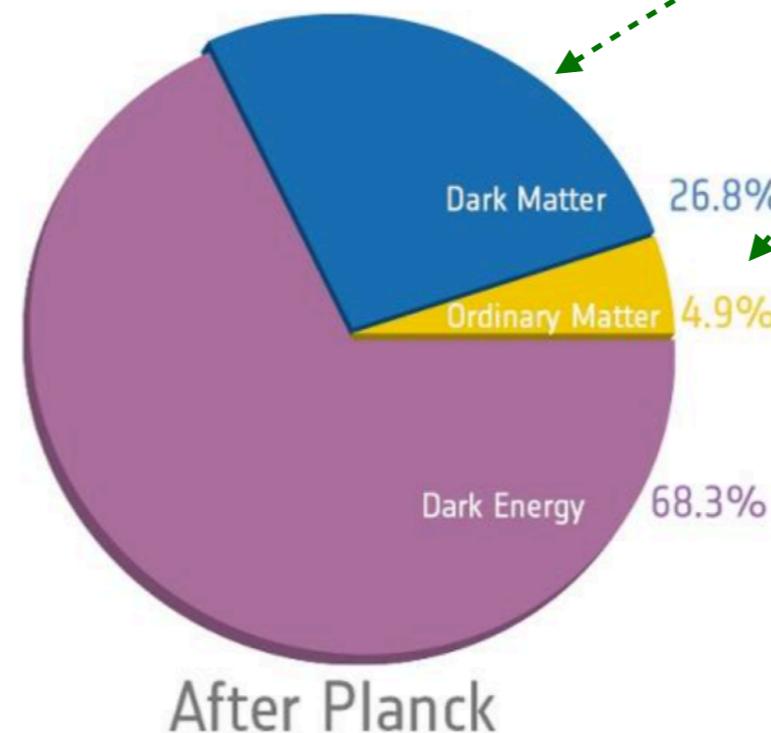
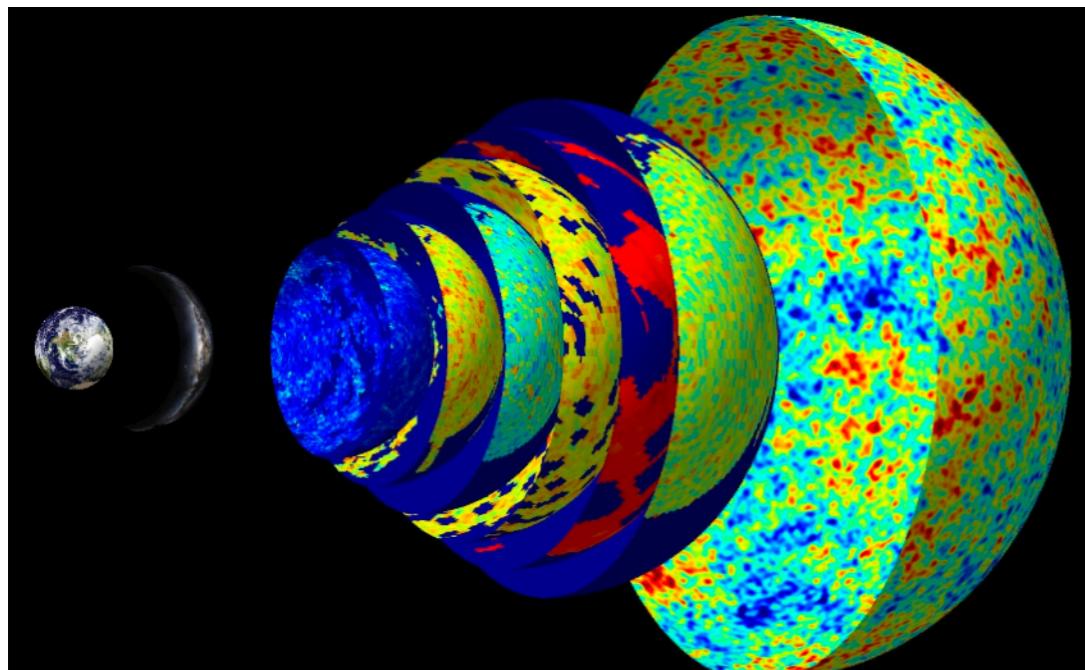
***Xiaoyong Chu*** (HEPHY, Vienna)

In collaboration with Junji Hisano, Alejandro Ibarra,  
Jui-Lin Kuo, Josef Pradler and Lukas Semmelrock

# I. Brief motivations



# Standard cosmology requires a dark sector

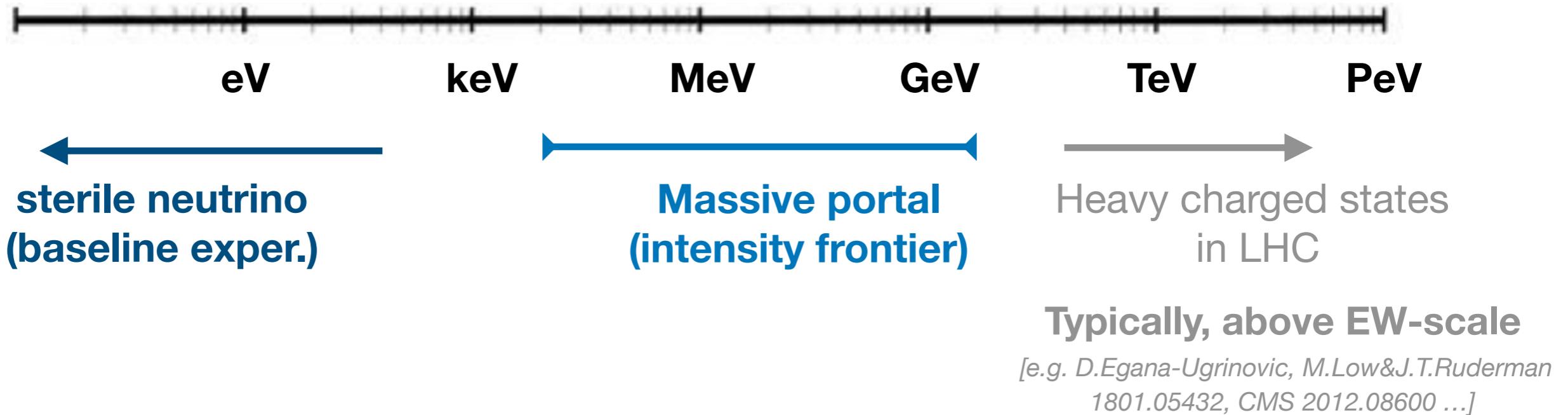


If both sectors are connected via a **portal** that involves **integer-charged particles**:

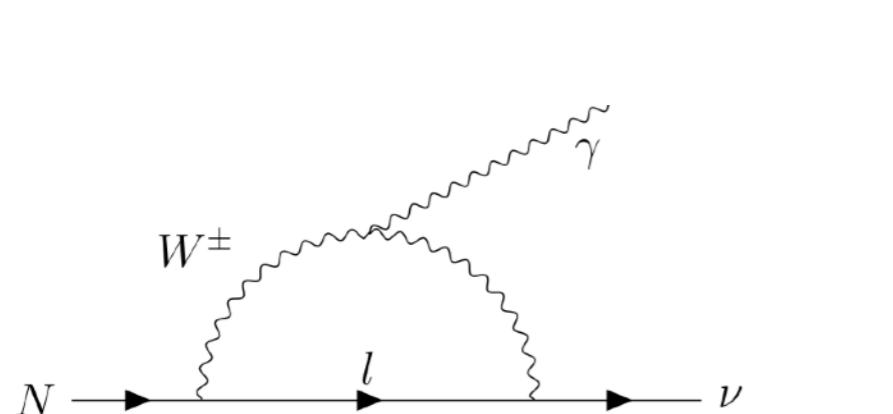


- A new **integer-charged particle** is necessarily heavy;
- But the **dark particle** can be light.

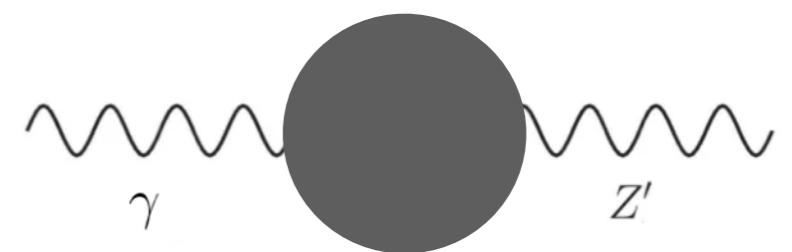
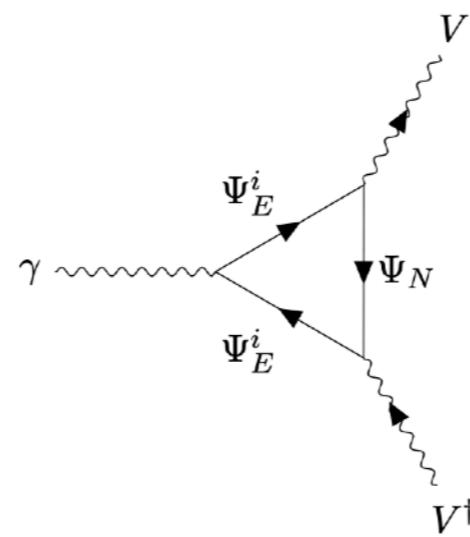
# From the aspect of **particle physics**:



**Light particle can easily couple to a photon:**



SM/BSM charged particles



general kinetic mixing

# Moreover, **no new light d.o.f.** from cosmology yet

**Planck 2018** [1807.06209]

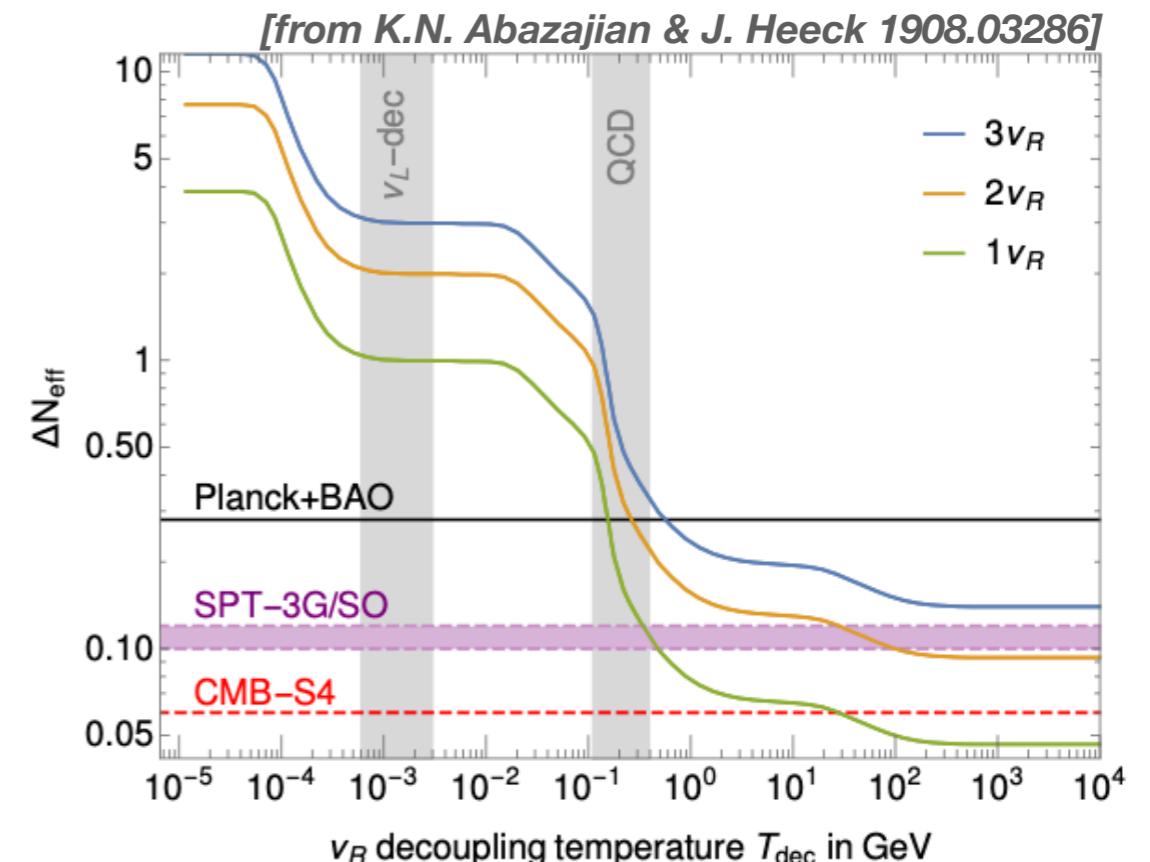
$$N_{\text{eff}} = 2.96^{+0.34}_{-0.33},$$

95 %, *Planck TT,TE,EE+lowE +lensing+BAO.*

$$N_{\text{eff}} = 2.95^{+0.56}_{-0.52}$$

BBN + BAO

**That is, new light mediator can only  
be feeble.**

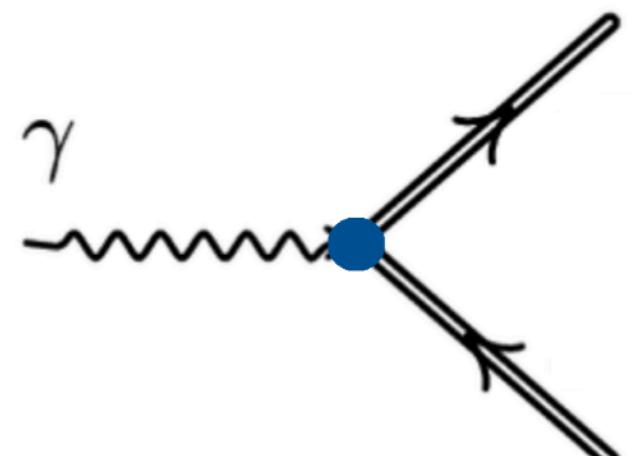


**A simple and rich example of a light mediator:**

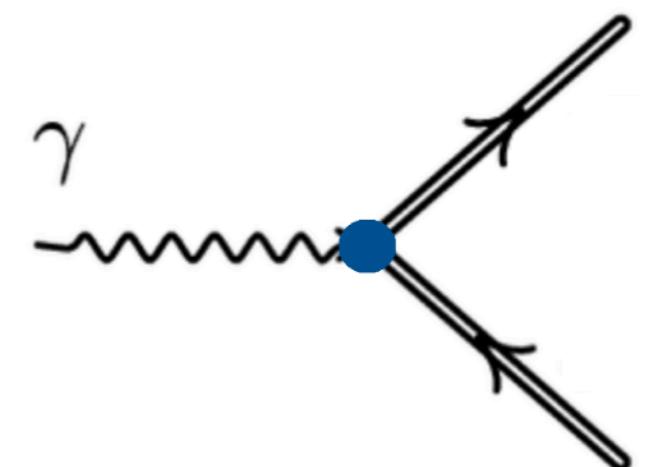
**SM photon portal**

via dark loop/mixing/confinement

[e.g. Holdom 1986, Raby, West 1987,  
Bagnasco, Dine, Thomas 1993, Foadi, Frandsen, Sannino 2008, ...]



## II. Electric-magnetic (EM) form factors, effectively



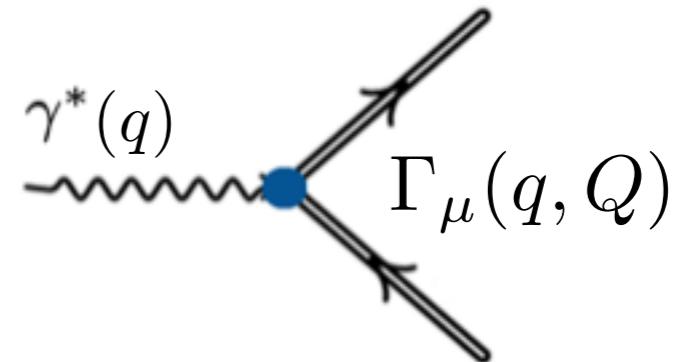
# What can a photon portal be?

Explore the possible **EM form factors** of **light dark particles**:

the most general Lagrangian

$$L_{\text{int}} = -iA^\mu(q)J_\mu(q, Q)$$

↓  
taking non-relativistic limit



**1. milli-charge of a new particle:** electric monopole

Non-rel. definition → momentum-space

$$q = \int d^3x \rho_{\text{EM}}(\vec{x}) \propto J_0(q=0, Q=0)$$

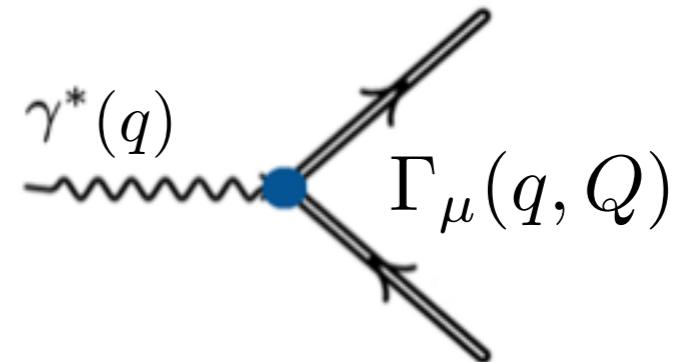
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Non-vanishing terms → the interaction operator

Complex scalar  $\phi^*(\partial_\mu \phi) - (\partial_\mu \phi^*)\phi$

Dirac fermion  $\bar{\psi} \gamma_\mu \psi$

Complex vector  $V_\alpha^+ (\partial_\mu V^\alpha) - (\partial_\mu V_\alpha^+) V^\alpha$  imposing Lorentz gauge

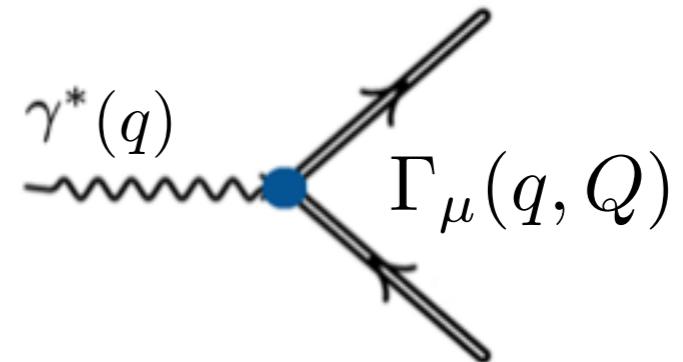
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**2. At higher-order (or a EM-neutral particle):** dipoles, quadrupoles, ...

Non-rel. definition → momentum-space

$$\vec{d}_E = \int d^3x \vec{x} \rho_{\text{EM}}(\vec{x}) \propto \frac{\partial J_0}{\partial \vec{q}}|_{\vec{q}=0}$$

- electric dipole

$$\vec{\mu}_M = \frac{1}{2} \int d^3x \vec{x} \times \vec{J}_{\text{EM}}(\vec{x}) \propto (\nabla_{\vec{q}} \times \vec{J})|_{\vec{q}=0}$$

- magnetic dipole

$$\int d^3x x_i x_j \rho_{\text{EM}}(\vec{x}) \propto \frac{\partial^2 J_0}{\partial q^i \partial q^j}|_{\vec{q}=0}$$

- (trace) charge radius  
- (traceless) electric quadrupole

$$\nabla_{q^i} (\nabla_{\vec{q}} \times \vec{J})_j + (i \leftrightarrow j)|_{\vec{q}=0}$$

- magnetic quadrupole,

$$(\vec{r} \cdot \vec{J}) \vec{r} - 2r^2 \vec{J}$$

- anapole moment, ... ....

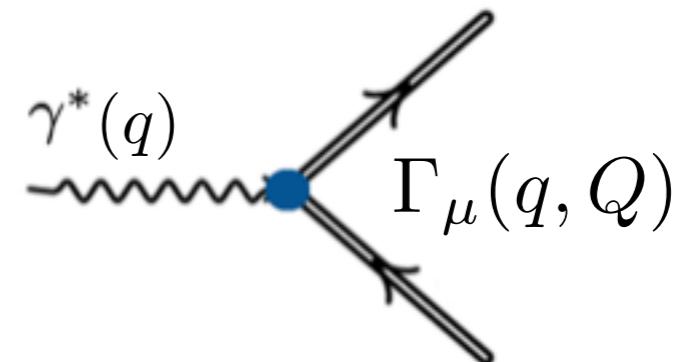
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interaction type	coupling	C	P	CP
magn. dipole	$\mu$	+1	+1	+1
elec. dipole	$d$	+1	-1	-1
elec. quadrupole	$Q$	+1	+1	+1
magn. quadrupole	$\tilde{Q}$	+1	-1	-1
charge radius	$g_1^A/m^2$	+1	+1	+1
toroidal moment	$g_4^A/m^2$	-1	+1	-1
anapole moment	$g_5^A/m^2$	-1	-1	+1

1. **Scalars** have no-spin, thus, at higher-order, only can have  
- (trace) charge radius

$$(\phi^* \overleftrightarrow{\partial}_\mu \phi) \partial_\nu F^{\mu\nu}$$

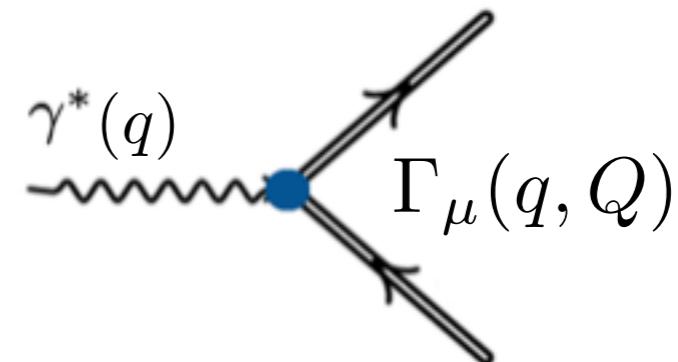
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**2. At higher-order (or a EM-neutral particle):** dipoles, quadrupoles, ...

interaction type	coupling	C	P	CP	2. independent indices for Dirac fermion
magn. dipole	$\mu$	+1	+1	+1	$\bar{\chi}\sigma^{\mu\nu}\chi F_{\mu\nu}$
elec. dipole	$d$	+1	-1	-1	$\bar{\chi}\sigma^{\mu\nu}\gamma^5\chi F_{\mu\nu}$
elec. quadrupole	$Q$	+1	+1	+1	$\bar{\chi}\gamma^\mu\chi\partial^\nu F_{\mu\nu}$
magn. quadrupole	$\tilde{Q}$	+1	-1	-1	$\bar{\chi}\gamma^\mu\gamma^5\chi\partial^\nu F_{\mu\nu}$
charge radius	$g_1^A/m^2$	+1	+1	+1	$[q^2\gamma^\mu - q^\mu q]/[q^2\gamma^\mu - q^\mu q]\gamma^5$
toroidal moment	$g_4^A/m^2$	-1	+1	-1	<small>[e.g. Pospelov, Veldhuis 2000, Sigurdson, Doran, Kurylov, Caldwell, Kamionkowski 2004, M. Nowakowski, E. A. Paschos J. M. Rodriguez 2004, Ho, Scherrer 2012, Kadota, Silk 2014, Mohanty, Rao 2015, ...]</small>
anapole moment	$g_5^A/m^2$	-1	-1	+1	

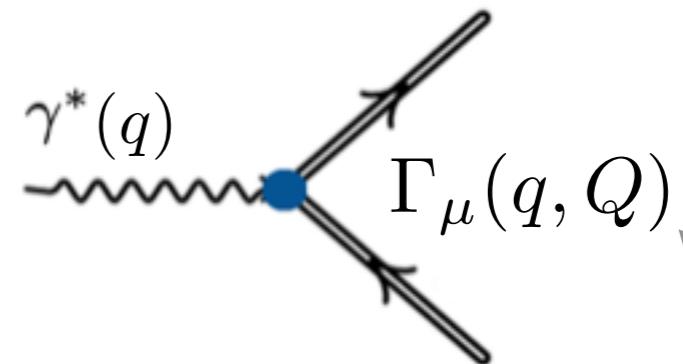
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**3. independent indices for vector boson**

Lorentz gauge

$$\begin{aligned}
 & - 2im_V\mu_V \left[ k^\alpha g^{\mu\beta} - k^\beta g^{\mu\alpha} + \frac{1}{4m_V^2} (k^2 g^{\alpha\beta} p^\mu - 2k^\alpha k^\beta p^\mu) \right] \\
 & - \frac{iQ_V}{4} (k^2 g^{\alpha\beta} p^\mu - 2k^\alpha k^\beta p^\mu) \\
 & - \frac{id_V}{2m_V} p^\mu [kp]^{\alpha\beta} - \frac{i\tilde{Q}_V}{4} (p^\mu [kp]^{\alpha\beta} + 4m_V^2 \epsilon^{\mu\alpha\beta\rho} k_\rho) \\
 & - \frac{ieg_1^A}{2m_V^2} k^2 p^\mu g^{\alpha\beta} - \frac{eg_4^A}{m_V^2} k^2 (k^\alpha g^{\mu\beta} + k^\beta g^{\mu\alpha}) - \frac{eg_5^A}{m_V^2} k^2 \epsilon^{\mu\alpha\beta\rho} p_\rho
 \end{aligned}$$

[e.g. K.Hagiwara, R.Peccei, D.Zeppenfeld&K.Hikasa 1987, J.Nieves & P. B.Pal 1996]

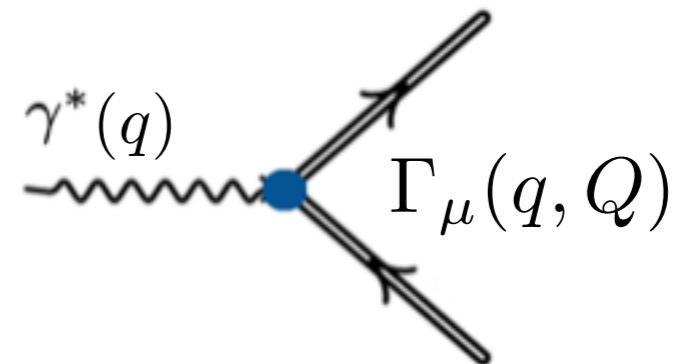
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For Self-Conjugate particles,  
only C-violating factors survive:

$$\text{C} : \Gamma_\mu(q, Q) \rightarrow -\Gamma_\mu(-q, -Q)$$

$$\text{SC} : \Gamma_\mu(q, Q) \rightarrow \Gamma_\mu(-q, -Q)$$

# What can a photon portal be?

Explore the possible **EM form factors** of **light dark particles**:

## 1. milli-charge of a new particle: electric monopole

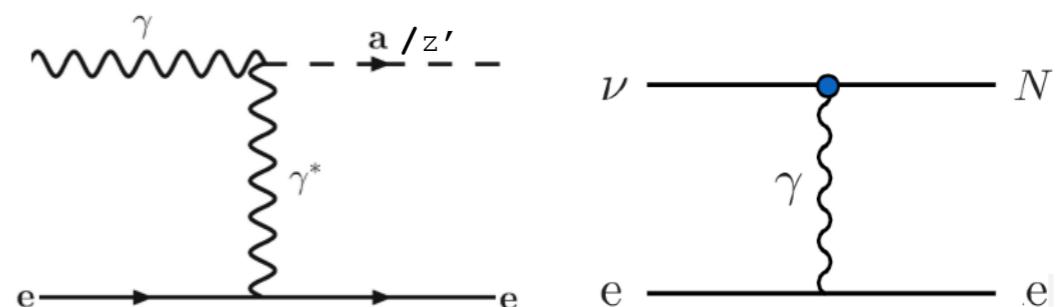
*Relevant for EDGES anomaly, and well constrained recently, see e.g. E. Gabrielli, L. Marzola, M. Raidal & H. Veermäe 1507.00571, A. Berlin, D. Hooper, G. Krnjaic, S. D. McDermott 1803.02804, E. D. Kovetz, V. Poulin, V. Gluscevic, K. K. Boddy, R. Barkana, M. Kamionkowski 1807.11482, T. Emken, R. Essig, C. Kouvaris & M. Sholapurkar, 1905.06348, S. Foroughi-Abari, F. Kling & Y. Tsai 2010.07941, M. A. Buen-Abad, R. Essig, D. McKeen, Y. Zhong 2107.12377, M. Montigny, P. A. Ouimet, J. Pinfold, A. Shaa & M. Staelens 2307.07855, ...*

## 2. At higher-order (or a EM-neutral particle): dipoles, quadrupoles, ...

*For technical details on multipole expansions, see e.g. V. M. Dubovik and A. A. Cheshkov. 1974, K. Gaemers & G. Gounaris, 1979, J. F. Nieves & P. B. Pal 1996, ...*

## 3. Inelastic cases (and two-photon cases):

typically easier to produce and detect;  
but will not discussed.

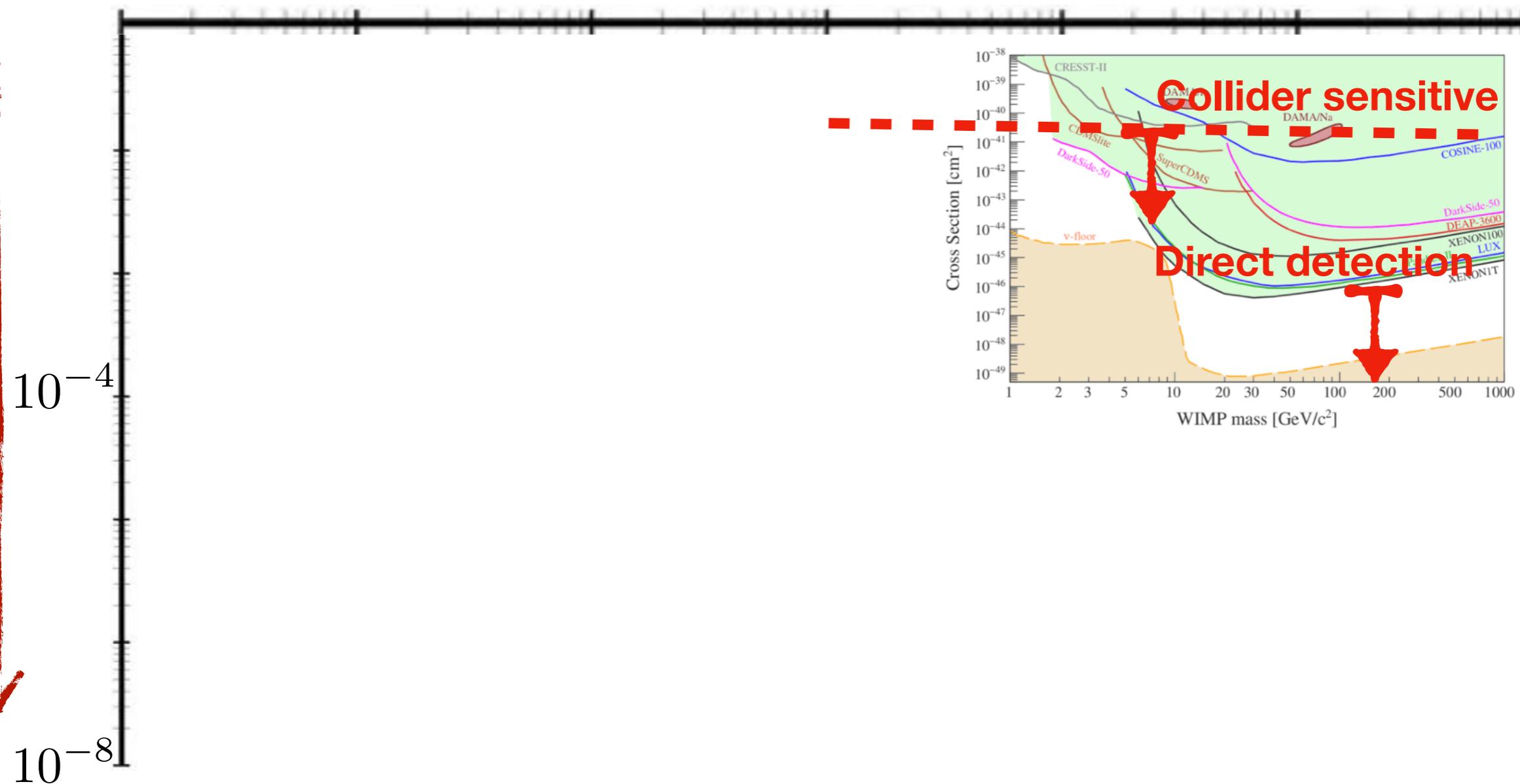


### III. Sketch of constraints

# A typical exclusion plot for a light dark particle

New physics

eV keV MeV GeV TeV Heavier mass



Coupling to SM

# A typical exclusion plot for a light dark particle

New physics

eV

keV

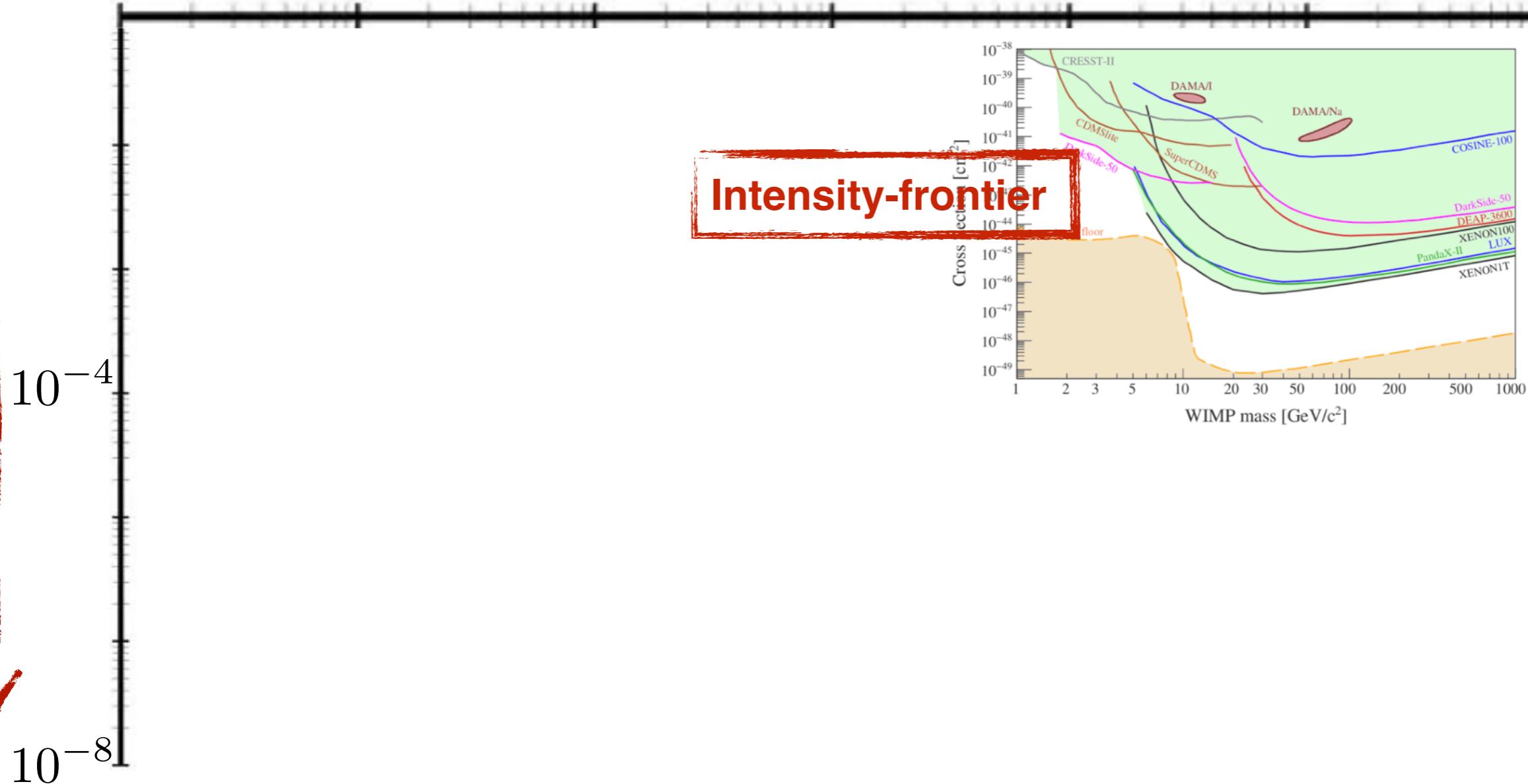
MeV

GeV

TeV

Heavier mass

Intensity-frontier

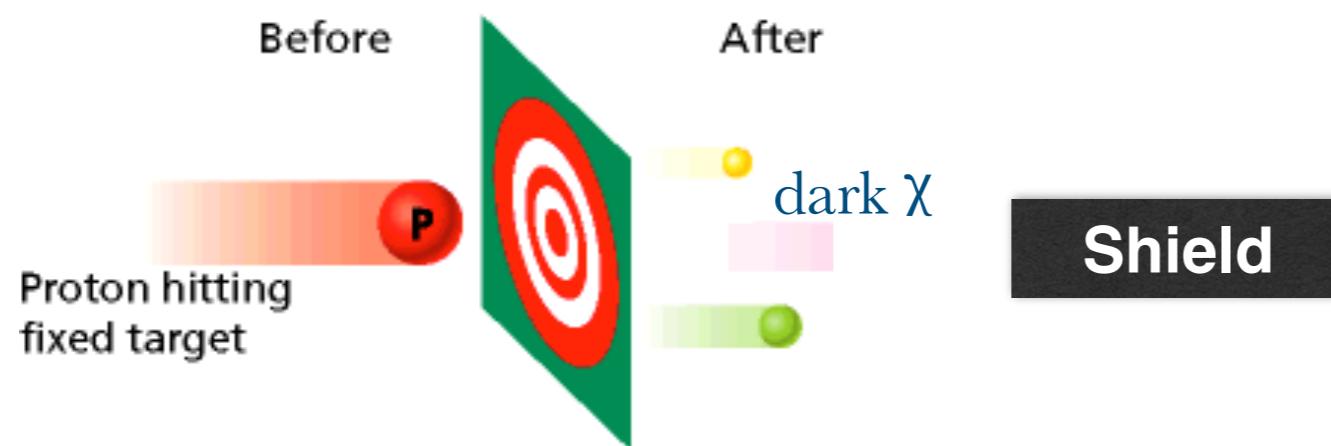


Coupling to SM

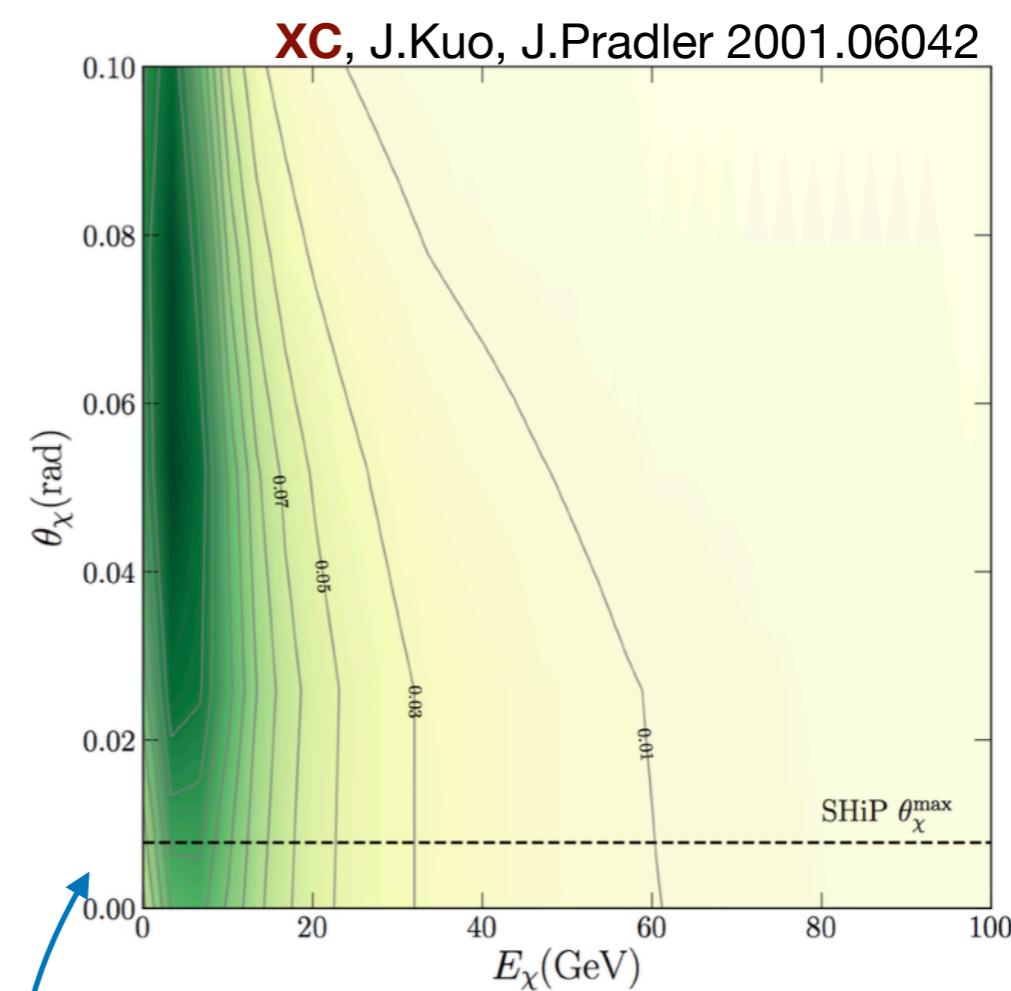
# dark $\chi$ around GeV: intensity-frontier

## Proton-beam experiments:

Proton beam experiments

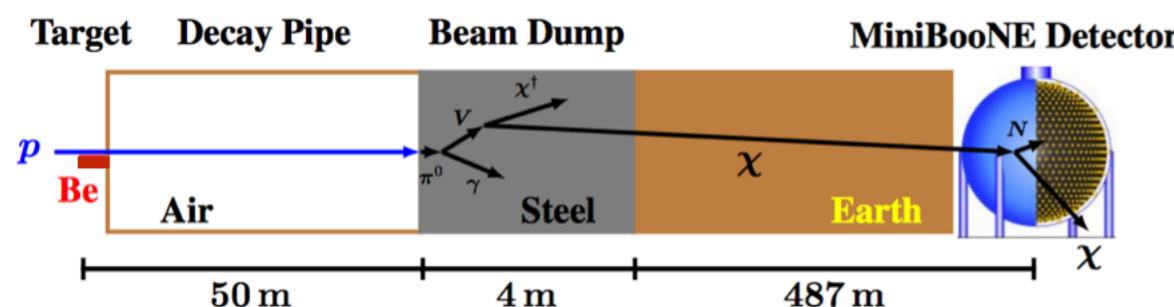


- Parton collisions via **pp $\rightarrow$ DS pair (DY)**;
- Proton Bremsstrahlung via **pp $\rightarrow$ pp'+DS pair**;
- Secondary production via **meson decay** (*potentially double-counting e.g. conversion of vector meson to off-shell photon*);
- Secondary collisions ....

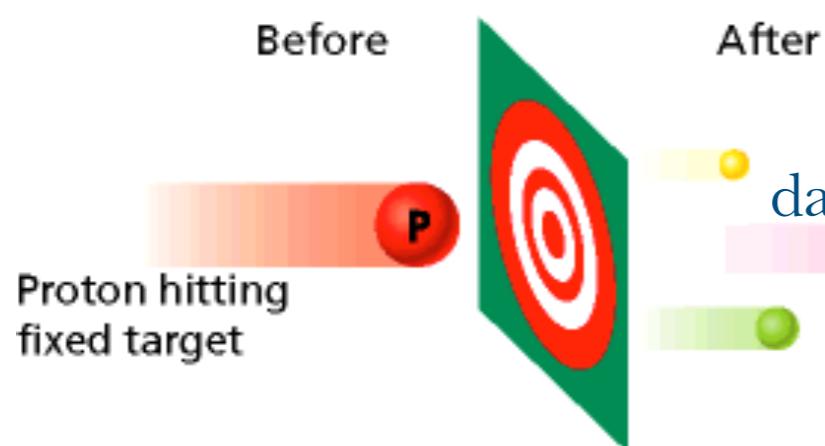


Only a tiny fraction  
of dark particles  
enter the detector

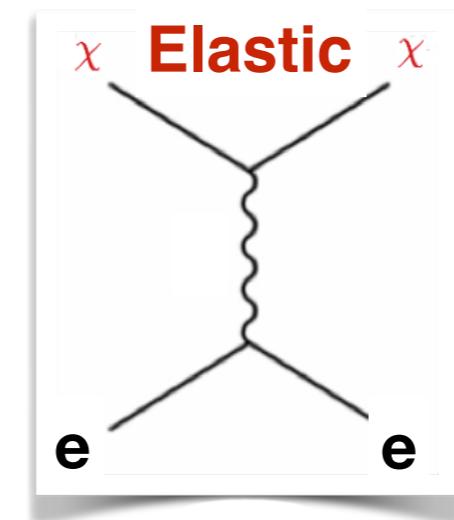
# dark $\chi$ around GeV: intensity-frontier



Proton beam experiments



$E_{\text{beam}} \setminus \text{meson}$
8.9 GeV (MiniBooNE-DM)
120 GeV (DUNE)
400/450 GeV (SHiP, E613/CHARM II)



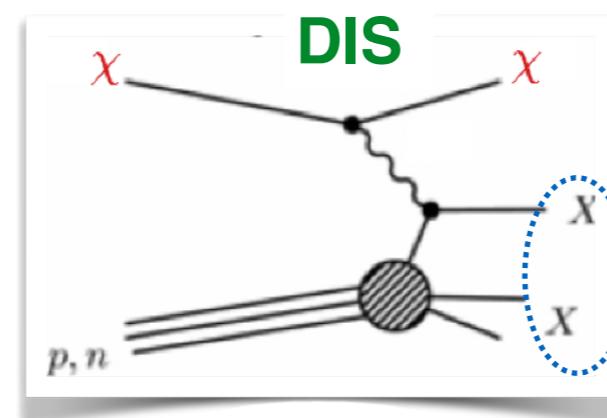
sub-GeV recoil, hard scattering:

e-recoil ( $E_R \in [75, 850]$  MeV,  $\theta_R \leq 140$  mrad)

$10^{20}$  POT produced no single-e events (after cut)!

elastic scattering off electron

deep inelastic scattering



above-GeV hadronic shower:

(take E613 at FermiLab)

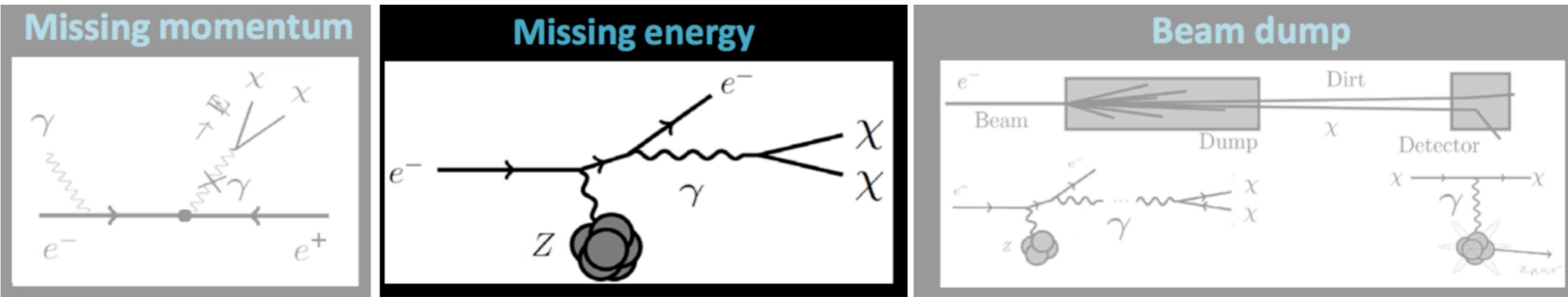
$E_N^{\text{dep}} \geq 20$  GeV per event

bkg N: below 180

# dark $\chi$ around GeV: intensity-frontier

With electron-beam: additional search for missing momentum/energy

credit: B. Eachenard



I) Babar, projected Belle

II) NA64, projected LDMX

III) mQ, projected BDX

**Signature:** mono- $\gamma$  + missing momentum (low-energy colliders).

**Signature:** forwardly-scattered electron, with significant energy loss.

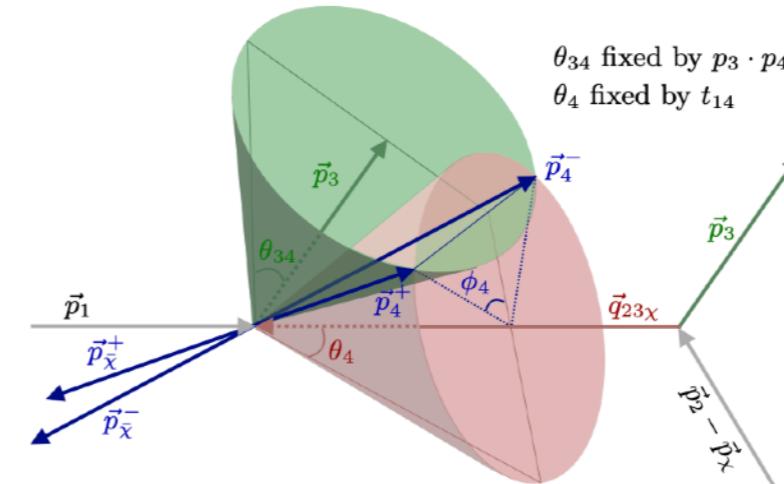
**Signature:** similar to proton-beam above.

Analytically solve

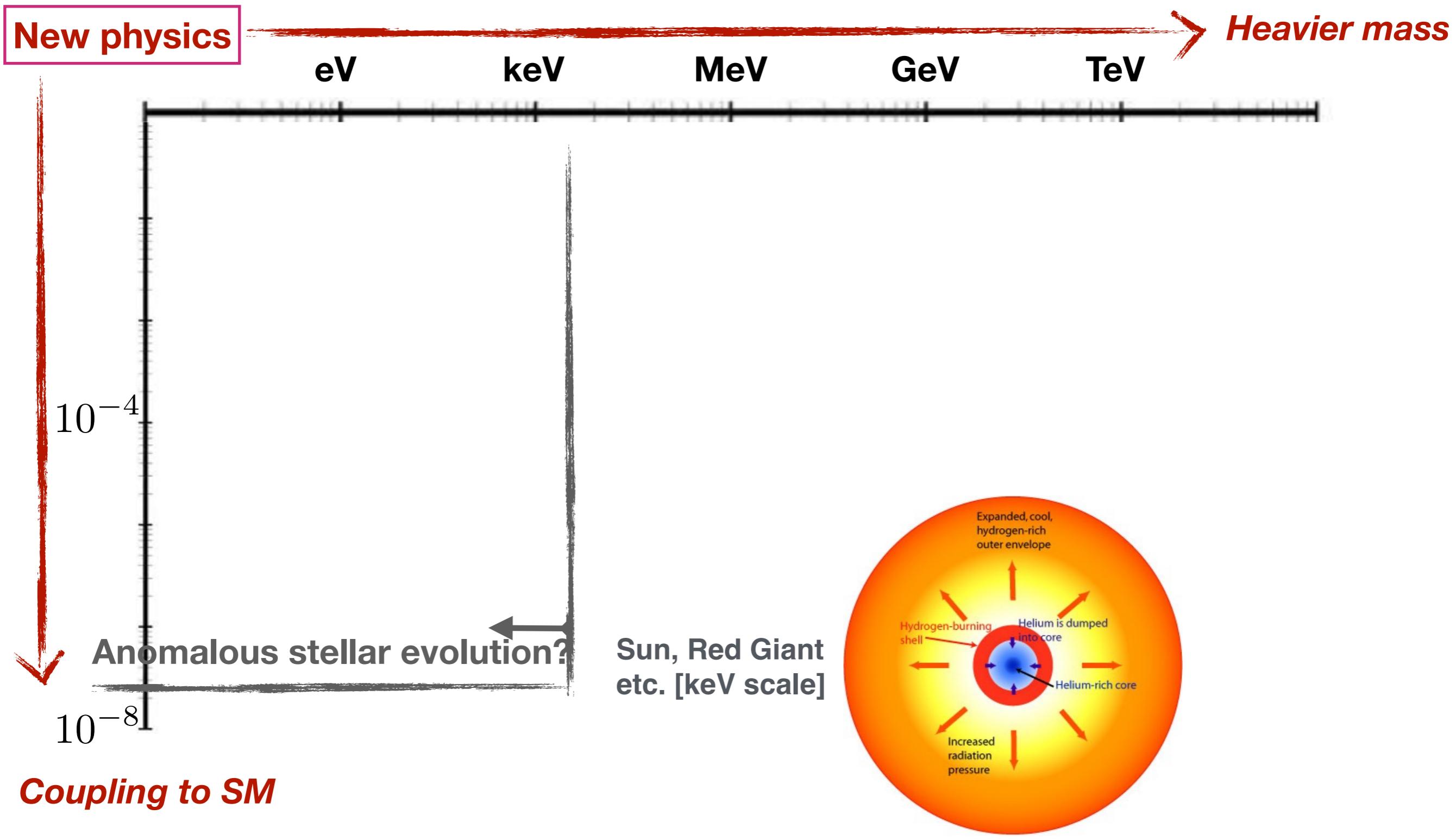
$$\frac{d^2\sigma_{eN \rightarrow eN\chi\chi}}{dE_e d\cos\theta_e}$$

missing energy larger than  $0.5E_0$

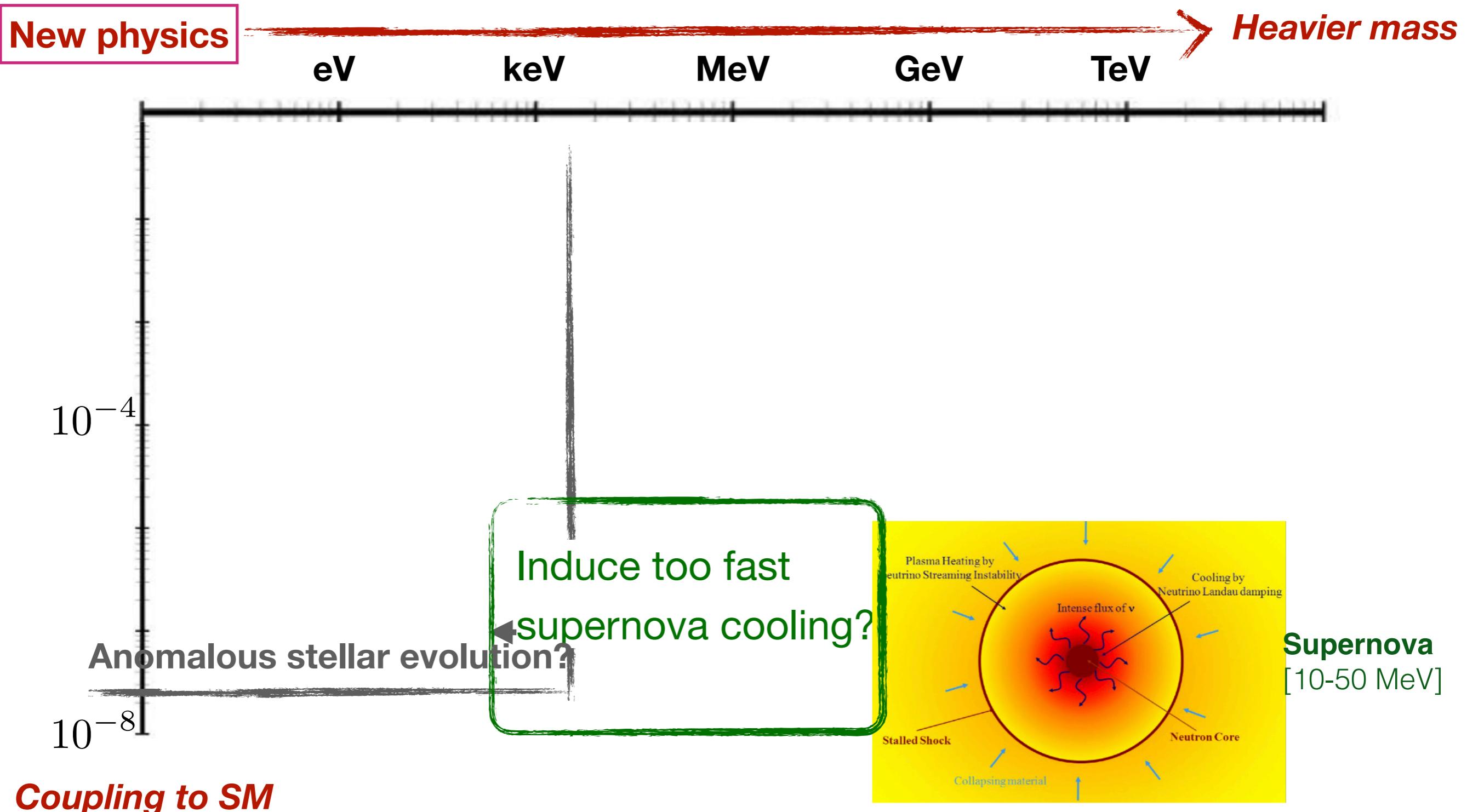
polar angular coverage of  $\theta_4 < 0.23$  rad



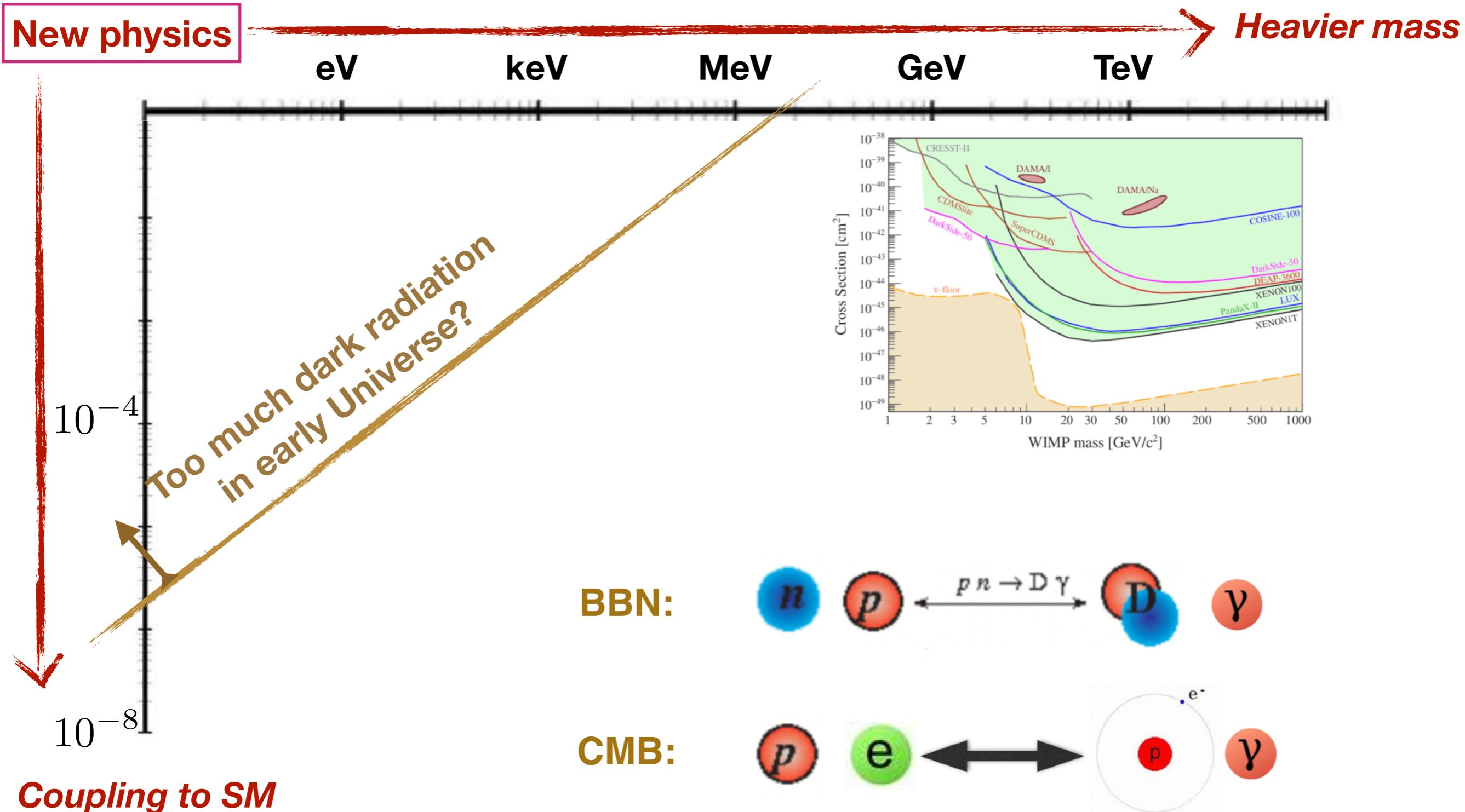
# A typical exclusion plot for a light dark particle



# A typical exclusion plot for a light dark particle



# A typical exclusion plot for a light dark particle



# dark X around keV-MeV: cosmos/stellar

They all are based on the argument that:

**(Meta-)stable dark particle should not be overproduced in dense medium.**

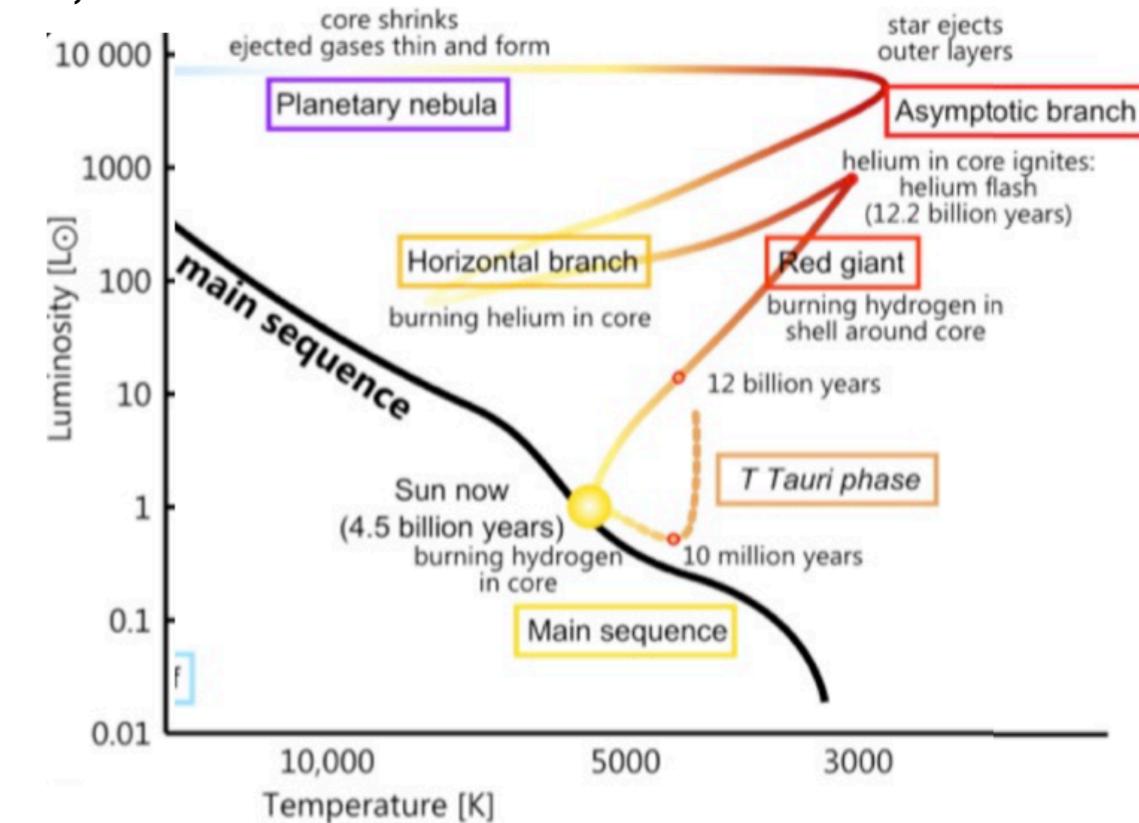
**1. Standard Solar Model** has been quite successful, constraining anomalous energy loss [J. A. Frieman, S.

Dimopoulos & M. S. Turner 1987, G. G. Raffelt and G. D. Starkman 1989]:

$$\int_{\text{Sun}} dV \dot{Q} < 10\% \times L_{\odot} \quad (\text{Sun}).$$

**2. Maximal core mass NOT to ignite Helium burning (red giant)** [G. G. Raffelt 1995]:

$$\dot{Q} < 10 \text{ erg/g/s} \times \rho \quad (\text{RG}).$$



**3. Anomalous cooling speeds up stable Helium burning** in Horizontal branch, reducing its typical ratio in Globular Cluster observations [G. G. Raffelt 1995]:

$$\int_{\text{core}} dV \dot{Q} < 10\% \times L_{\text{HB}} \quad (\text{HB}).$$

# dark X around keV-MeV: cosmos/stellar

They all are based on the argument that:

**(Meta-)stable dark** particle should not be **overproduced** in dense medium.

**4. To have successful neutrino-driven SN explosion:**

$$\int_{\text{core}} dV \dot{Q} < L_\nu = 3 \times 10^{52} \text{ erg/s} \quad (\text{SN}).$$

To make  $\chi$  escape, its **mean-free-path in SN** should be longer than  $\sim 40$  km (or than  $v$ ).

**5. At early Universe (BBN time), medium is at most mild for dark above electron mass, so zero-temperature QFT is adopted here.**

	$\omega_p$	$T$
Sun's core	0.3 keV	1.4 keV
HB's core	2.6 keV	10.6 keV
RG's core	8.6 keV	8.6 keV
SN's core	17.6 MeV	12.1 MeV

**BBN:**  $T \sim \text{MeV}$

# Anomalous cooling relies on its production in medium

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**Caveats do exist in the argument, such as:**

- dark state **trapping** by additional dark states [e.g. Y. Zhang 1404.7172];
- **Production suppression** from large **thermal** mass/small **thermal** coupling of dark states [e.g. W. DeRocco, P. W. Graham, S. Rajendran 2006.15112].
- if **SN1987A** was not neutrino-driven explosion [e.g. N. Bar, K. Blum & Guido D'Amico 1907.05020, and earlier 1601.03422].

# Anomalous cooling relies on its production in medium

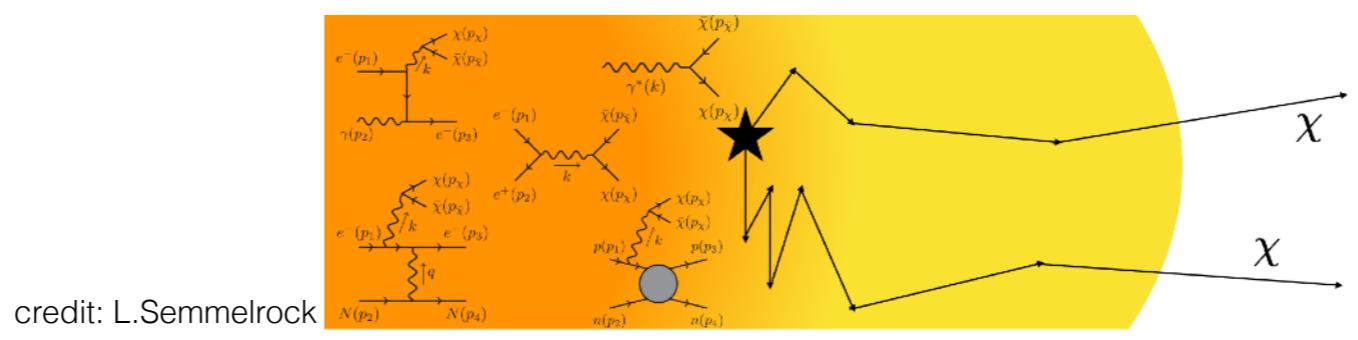
First half: total production rate of (off-shell) photons in medium

$$2 \text{Im} \left[ \gamma^* \text{SM} \gamma^* \right] = 2 \text{Im} \left[ \gamma^* \overset{\text{SM}}{\text{---}} \gamma^* + \gamma^* \overset{\text{SM}}{\text{---}} \gamma^* + \gamma^* \overset{\text{SM}}{\text{---}} \gamma^* + \dots \right]$$
$$= \int d\Pi_i \left[ \left| \overset{\text{SM}}{\text{---}} \gamma^* \right|^2 + \left| \overset{\text{SM}}{\gamma} \gamma^* \right|^2 + \left| \overset{\text{SM}}{\text{---}} \overset{\text{SM}}{\text{---}} \overset{\text{SM}}{\text{---}} \gamma^* \right|^2 + \dots \right]$$

**SM particle pair annihilation**      **Compton scattering**      **SM particle Bremsstrahlung**

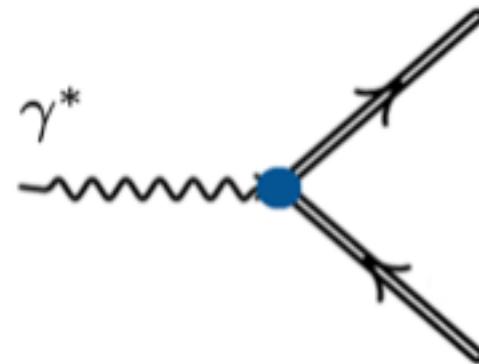
Preciser to separate the **resonant (plasmon)** and **non-resonant** contributions

$$-\frac{\text{Im} \Pi_{L,T}}{\pi |s_{\gamma^*} - \Pi_{L,T}|^2} = \delta(s_{\gamma^*} - \Pi_{L,T}) + \text{non-reson.}$$



# Anomalous cooling relies on its production in medium

Second half: **plasmon/photon decays** into a pair of **dark particles (1,2)** via



$$I_{\text{invis.}}^{\mu\nu} = \int d\Pi_{p_1, p_2} (2\pi)^4 \delta^4(q - p_1 - p_2) M_{\gamma^* \rightarrow 12}^\mu M_{\gamma^* \rightarrow 12}^{\nu*}$$
$$= \frac{1}{8\pi} \sqrt{1 - \frac{4m_{12}^2}{s_{\gamma^*}}} f(s_{\gamma^*}) \left( -g^{\mu\nu} + \frac{q^\mu q^\nu}{s_{\gamma^*}} \right)$$

E.g. plasmon decay

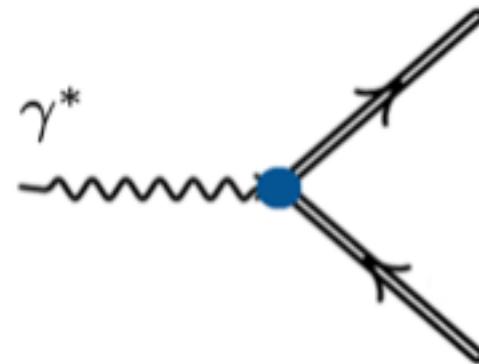
$$\Gamma_{T,L} = \frac{1}{16\pi} Z_{T,L} \sqrt{1 - \frac{4m_\chi^2}{\omega_{T,L}^2 - |\vec{k}|^2}} \frac{f(\omega_{T,L}^2 - |\vec{k}|^2)}{\omega_{T,L}}$$

**Stellar cooling bounds** are thus derived from dark pair production:

- For  $T \gg m$ , **plasmon decay** usually dominates the dark production;
- For  $T \sim m$ , **electron annihilation** (in SN) or **np Bremsstrahlung** (in RG/HB).

# Anomalous cooling relies on its production in medium

Second half: **plasmon/photon decays** into a pair of **dark particles (1,2)** via



$$\begin{aligned} I_{\text{invis.}}^{\mu\nu} &= \int d\Pi_{p_1, p_2} (2\pi)^4 \delta^4(q - p_1 - p_2) M_{\gamma^* \rightarrow 12}^\mu M_{\gamma^* \rightarrow 12}^{\nu*} \\ &= \frac{1}{8\pi} \sqrt{1 - \frac{4m_{12}^2}{s_{\gamma^*}}} f(s_{\gamma^*}) \left( -g^{\mu\nu} + \frac{q^\mu q^\nu}{s_{\gamma^*}} \right) \end{aligned}$$

Need to be aware of: **vector particle is different**

- compare **f(s)** for milli-charged scalar(S) / fermion(F) / vector(V)

$$f_S(s) = \frac{(\epsilon e)^2 s (1 + 4m_\phi^2/s)}{3}$$

similar up to a pre-factor

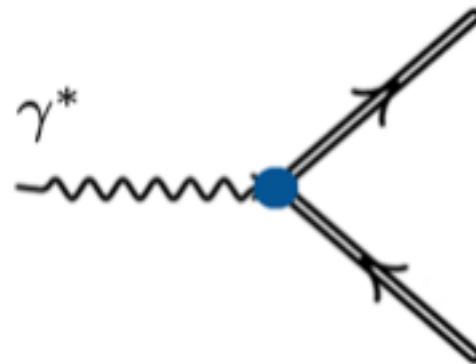
$$f_F(s) = \frac{4(\epsilon e)^2 s (1 + 2m_\chi^2/s)}{3}$$

$$f_V(s) = \frac{(\epsilon e)^2 (s - 4m_V^2)(s^2 - 4m_V^2 s + 12m_V^4)}{12m_V^4}$$

diverge at  $m_V \rightarrow 0$ ?

# Anomalous cooling relies on its production in medium

Second half: **plasmon/photon decays** into a pair of **dark particles (1,2)** via



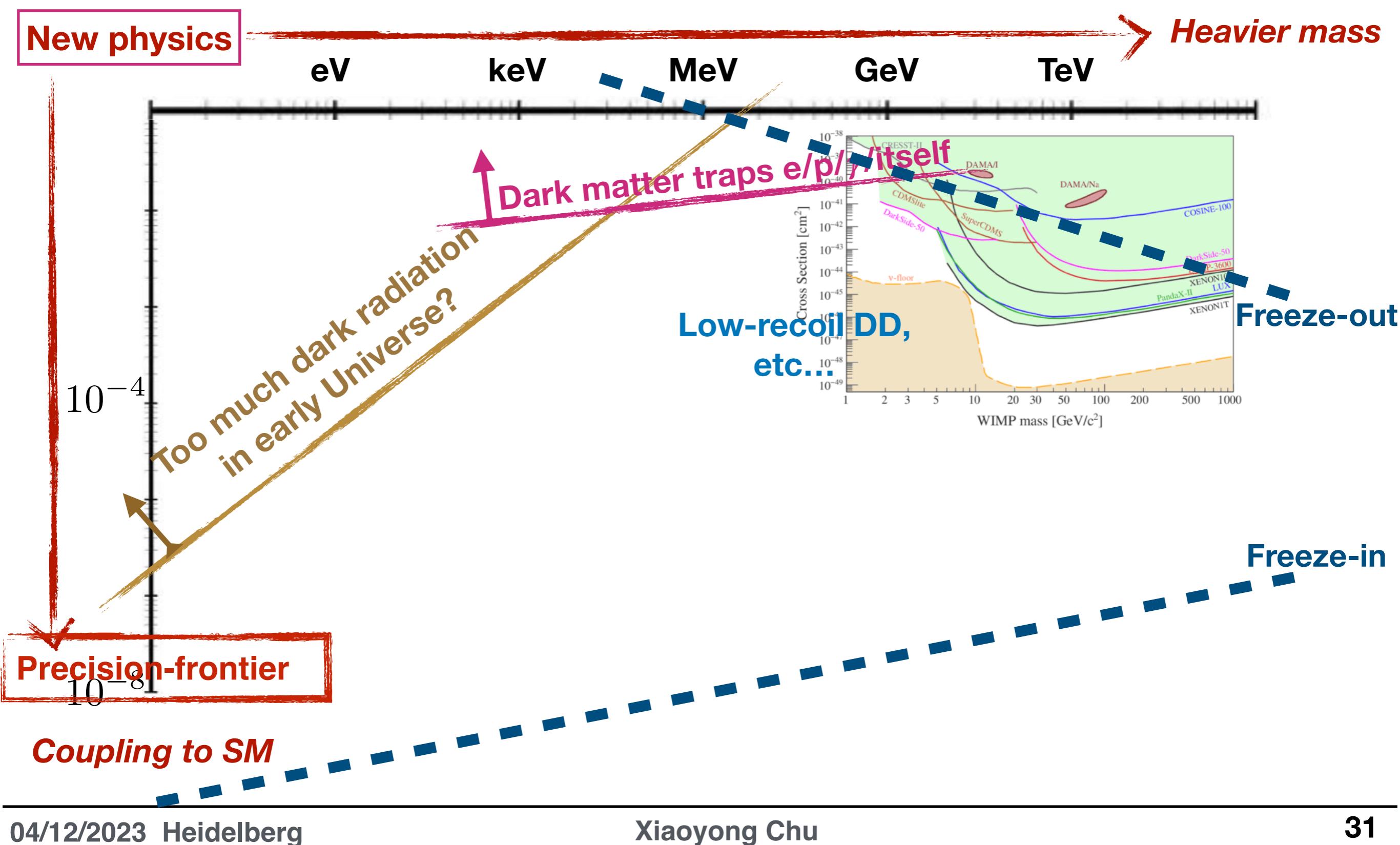
$$I_{\text{invis.}}^{\mu\nu} = \int d\Pi_{p_1, p_2} (2\pi)^4 \delta^4(q - p_1 - p_2) M_{\gamma^* \rightarrow 12}^\mu M_{\gamma^* \rightarrow 12}^{\nu*}$$

$$= \frac{1}{8\pi} \sqrt{1 - \frac{4m_{12}^2}{s_{\gamma^*}}} f(s_{\gamma^*}) \left( -g^{\mu\nu} + \frac{q^\mu q^\nu}{s_{\gamma^*}} \right)$$

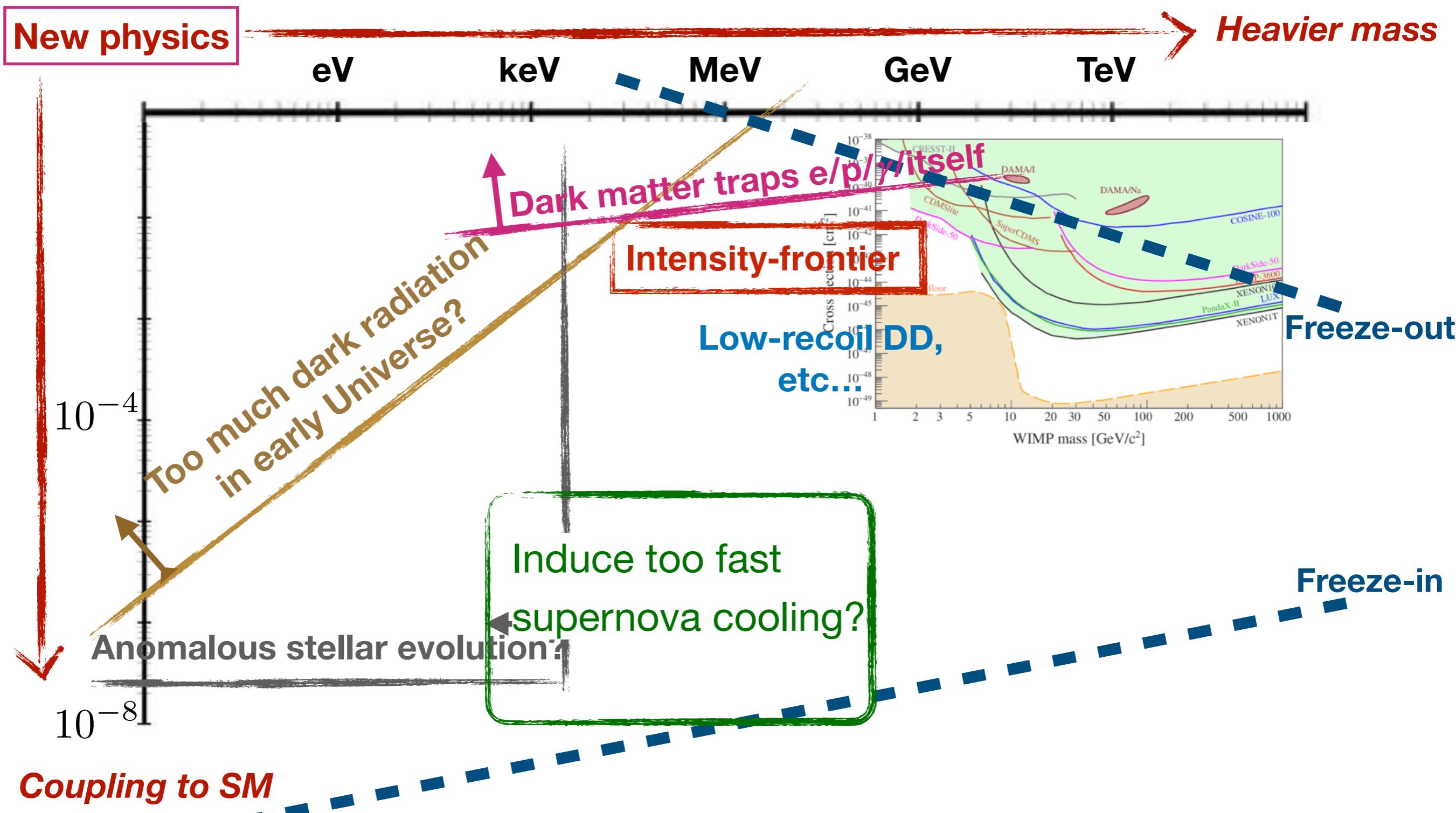
interaction type	fermion $f(s)$	vector $f(s)$
magnetic dipole	$\frac{2}{3}\mu_\chi^2 s^2 \left(1 + \frac{8m_\chi^2}{s}\right)$	$\frac{\mu_V^2 s (s - 4m_V^2)(16m_V^2 + 3s)}{12m_V^2}$
electric dipole	$\frac{2}{3}d_\chi^2 s^2 \left(1 - \frac{4m_\chi^2}{s}\right)$	$\frac{d_V^2 s (s - 4m_V^2)^2}{6m_V^2}$
electric quadrupole		$\frac{Q_V^2 s^2 (s - 4m_V^2)}{16}$
magnetic quadrupole		$\frac{\tilde{Q}_V^2 s^2 (s + 8m_V^2)}{24}$
charge radius	$\frac{4}{3} \frac{e^2 (g_1^\chi)^2 s^3}{m_\chi^4} \left(1 + \frac{2m_\chi^2}{s}\right)$	$\frac{e^2 (g_1^A)^2 s^2 (s - 4m_V^2)(12m_V^4 - 4m_V^2 s + s^2)}{48m_V^8}$
toroidal moment		$\frac{e^2 (g_4^A)^2 s^3 (s - 4m_V^2)}{3m_V^6}$
anapole moment	$\frac{4}{3} \frac{e^2 (g_5^\chi)^2 s^3}{m_\chi^4} \left(1 - \frac{4m_\chi^2}{s}\right)$	$\frac{e^2 (g_5^A)^2 s^2 (s - 4m_V^2)^2}{3m_V^6}$

**More factor**  
 $s/m_V^2$   
**for dark vector.**

# A typical exclusion plot for a light dark particle



# To sum up, also with dark matter production



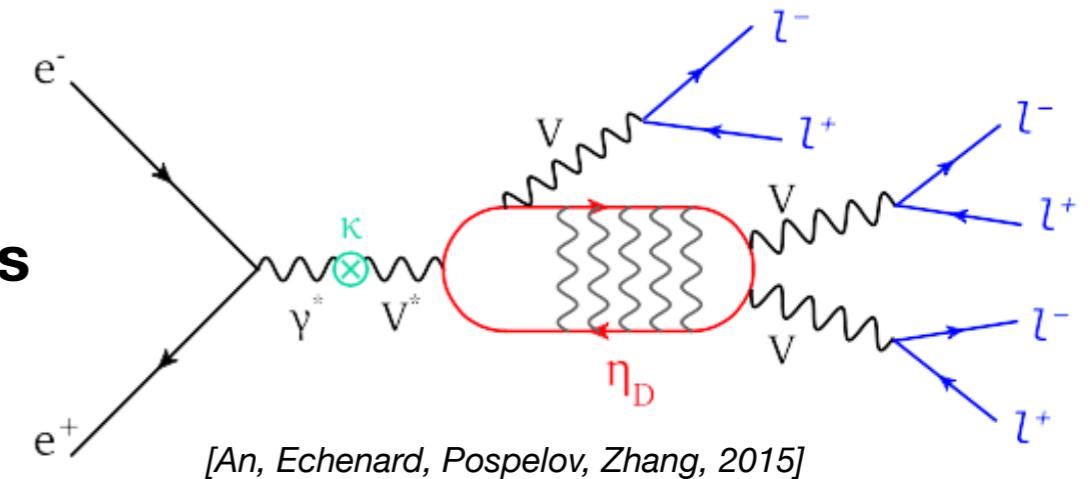
# More dark structure, more signatures:

Higher-derivatives, more photons, non-conserved current, ....

**Displaced vertex in detectors:**

e.g. mixing with long-lived  $A'$ , dark bound states

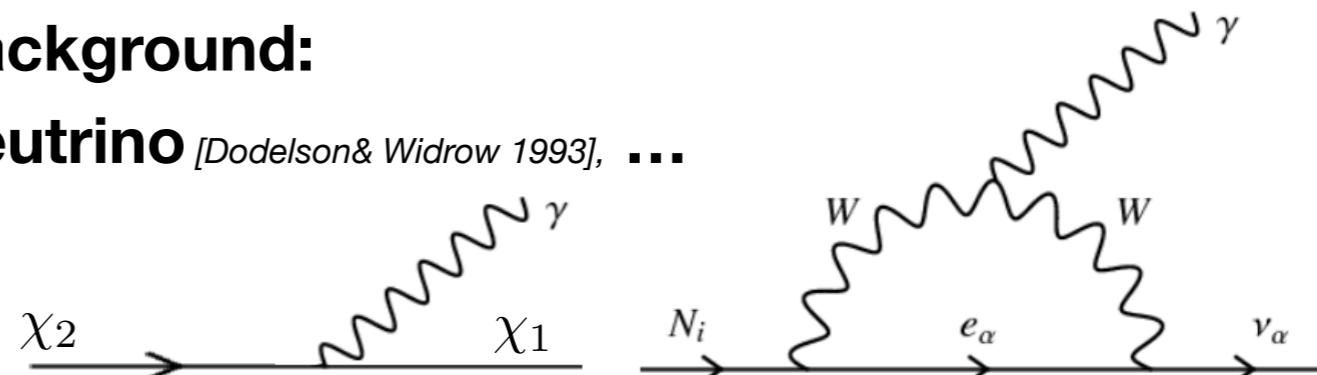
**Displaced vertex**



**Low-energy cosmic photon beyond background:**

**excited state** [Tucker-Smith & Weiner, 2001], **sterile neutrino** [Dodelson & Widrow 1993], ...

**Detailed cosmos/astro.**



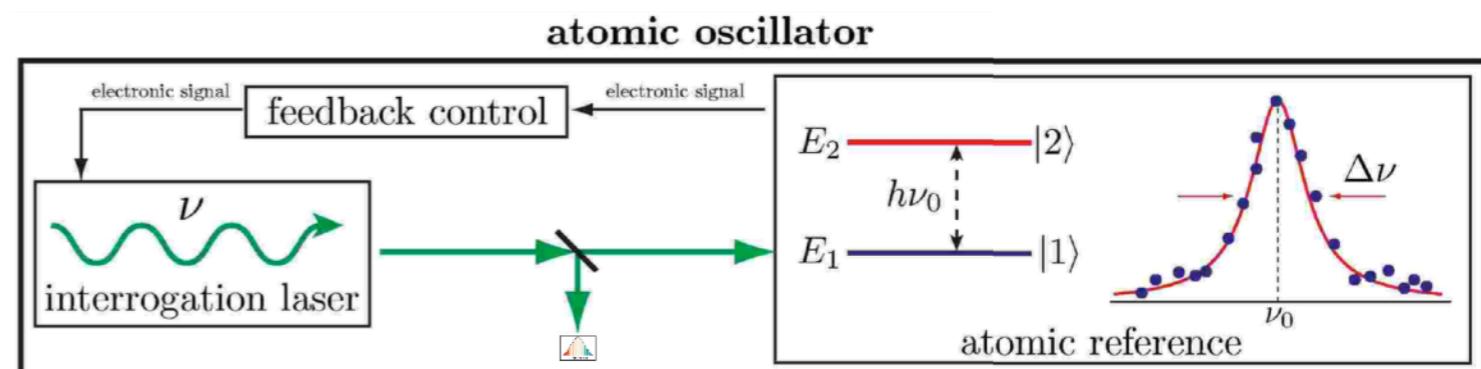
**Oscillating fine-structure constant:**

e.g. a light scalar [Arvanitaki, Huang, Tilburg, 2014, Tilburg, Leefer,

Bougas, Budker, 2015, Stadnik and V. V. Flambaum 2015, ...]

$$s F^{\mu\nu} F_{\mu\nu}$$

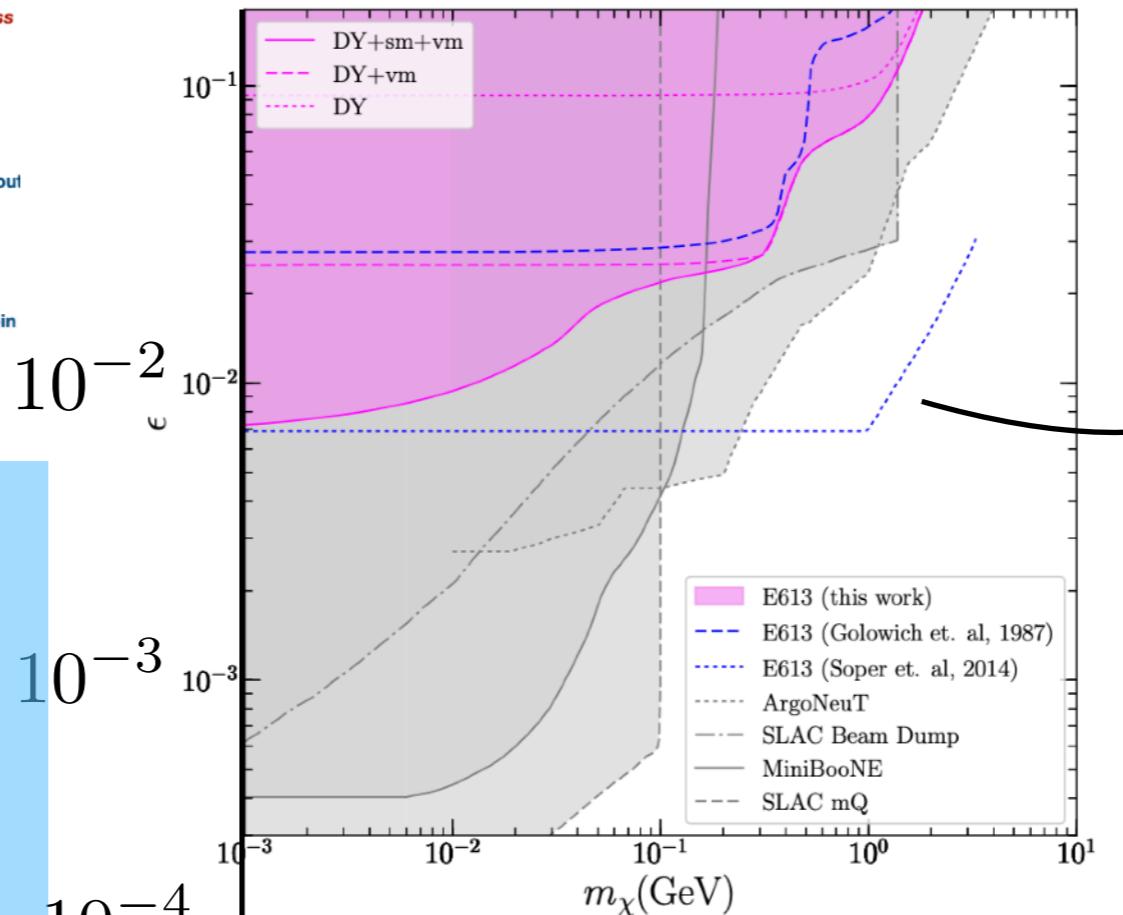
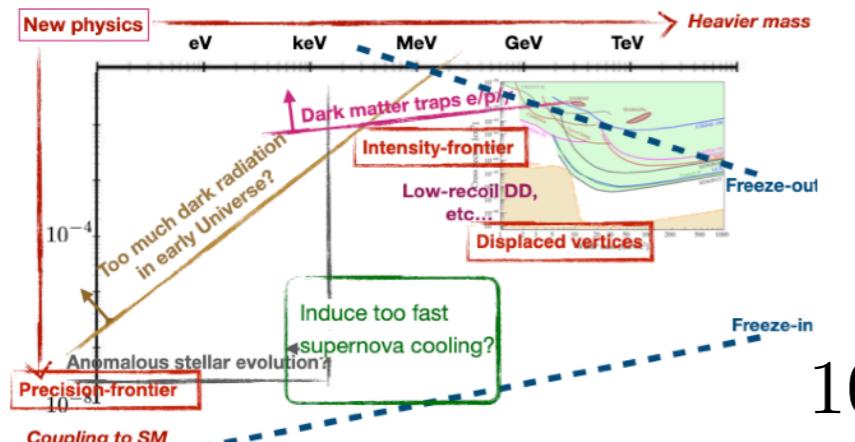
**Precision-frontier**



### III. discuss exclusions

# Summarise dim-4 constraints:

**milli-charged**, well known in the literature

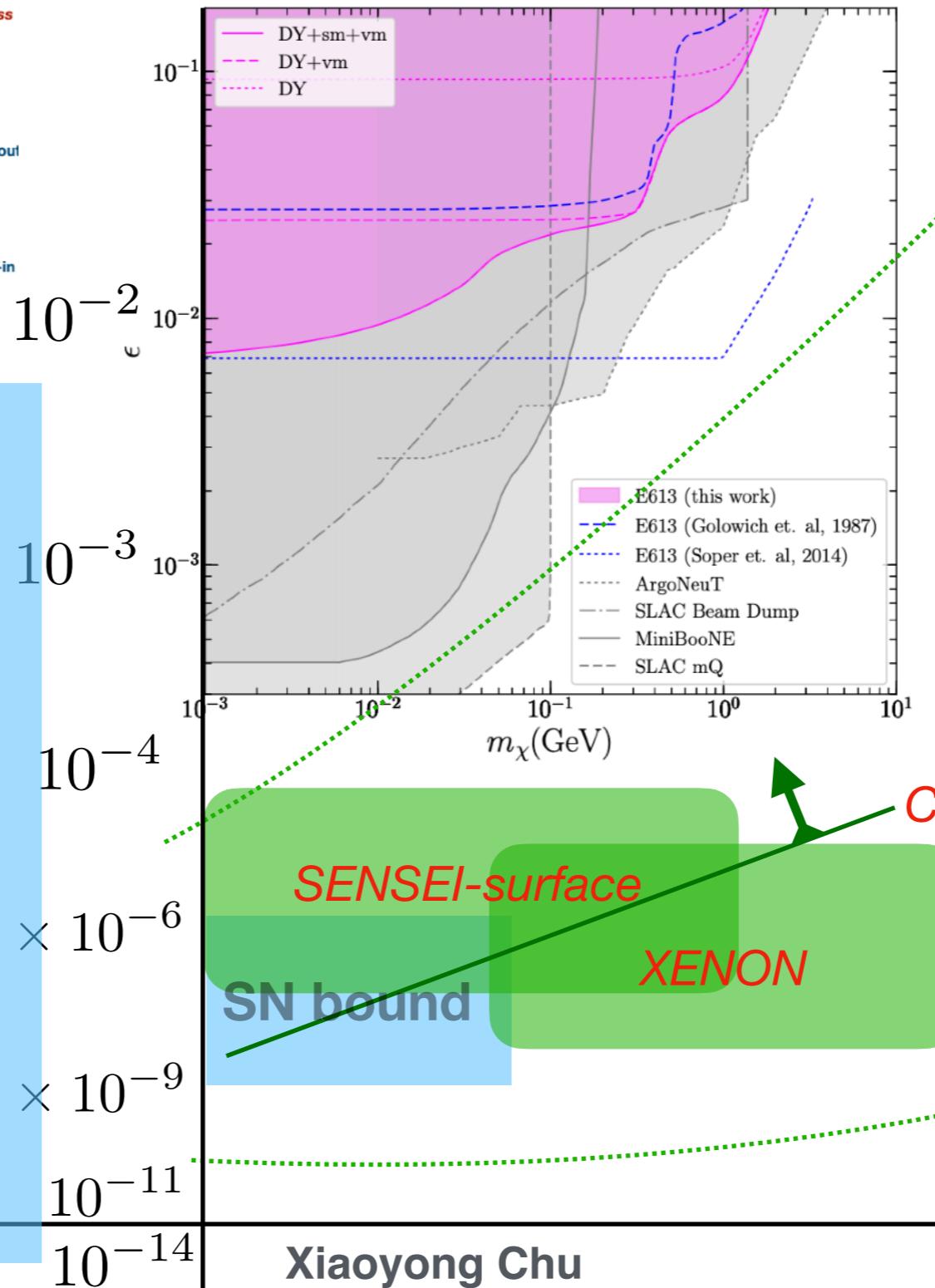
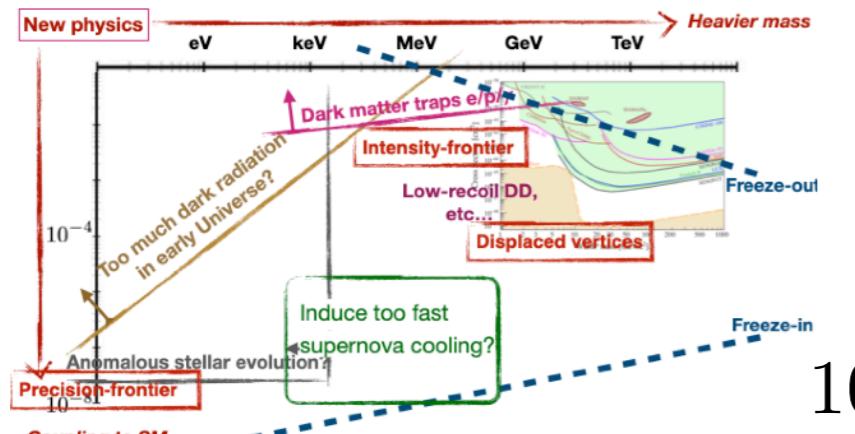


**XC, J.Kuo, J.Pradler  
2001.06042**

We corrected a previous result by including the **attenuation of protons.**

# Summarise dim-4 constraints:

**milli-charged**, well known in the literature



**XC**, J.Kuo, J.Pradler  
2001.06042

**freeze-out [excluded]**

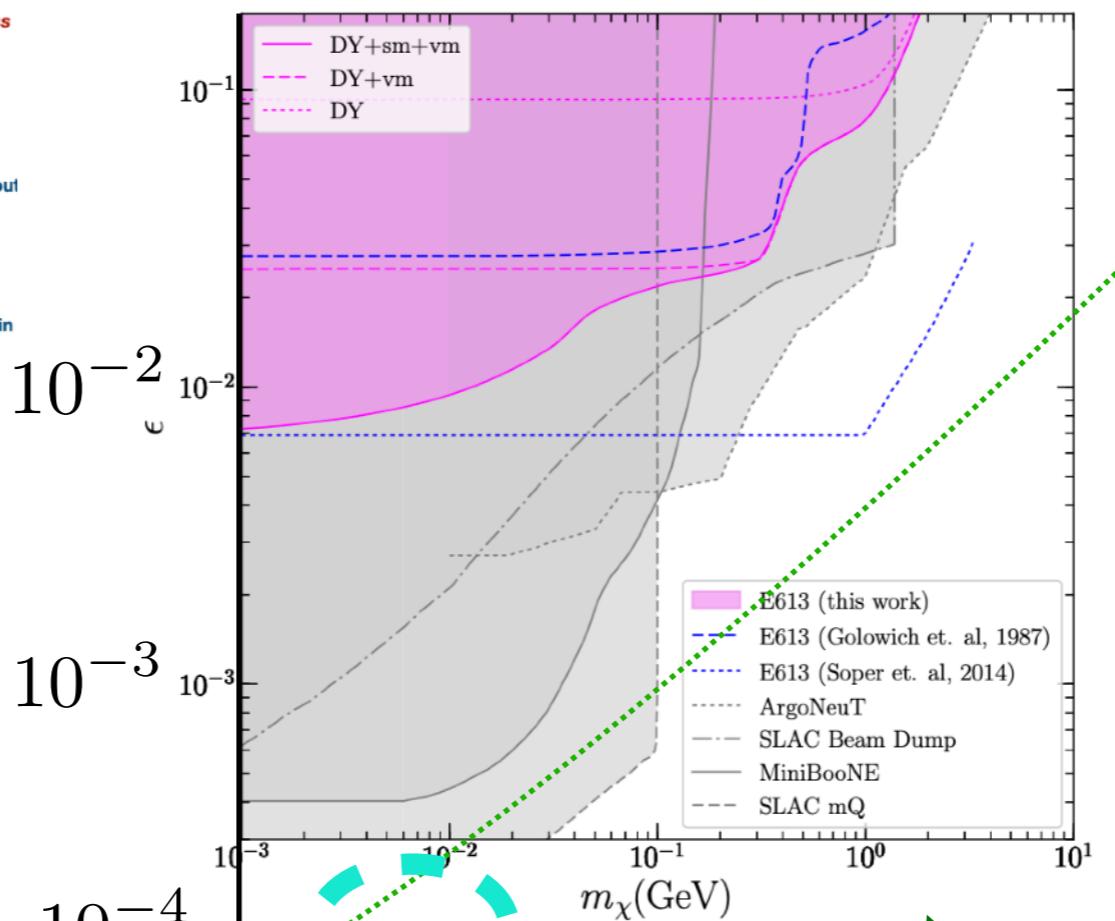
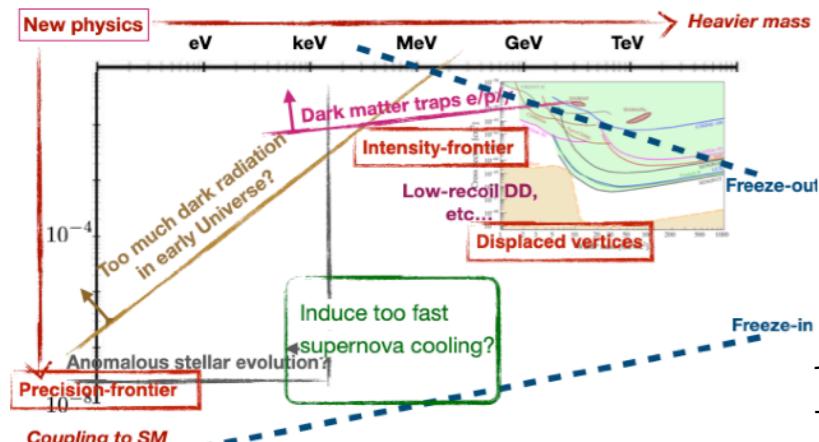
**If full dark matter**

**CMB spectrum**

**freeze-in**

# Summarise dim-4 constraints:

**milli-charged**, well known in the literature

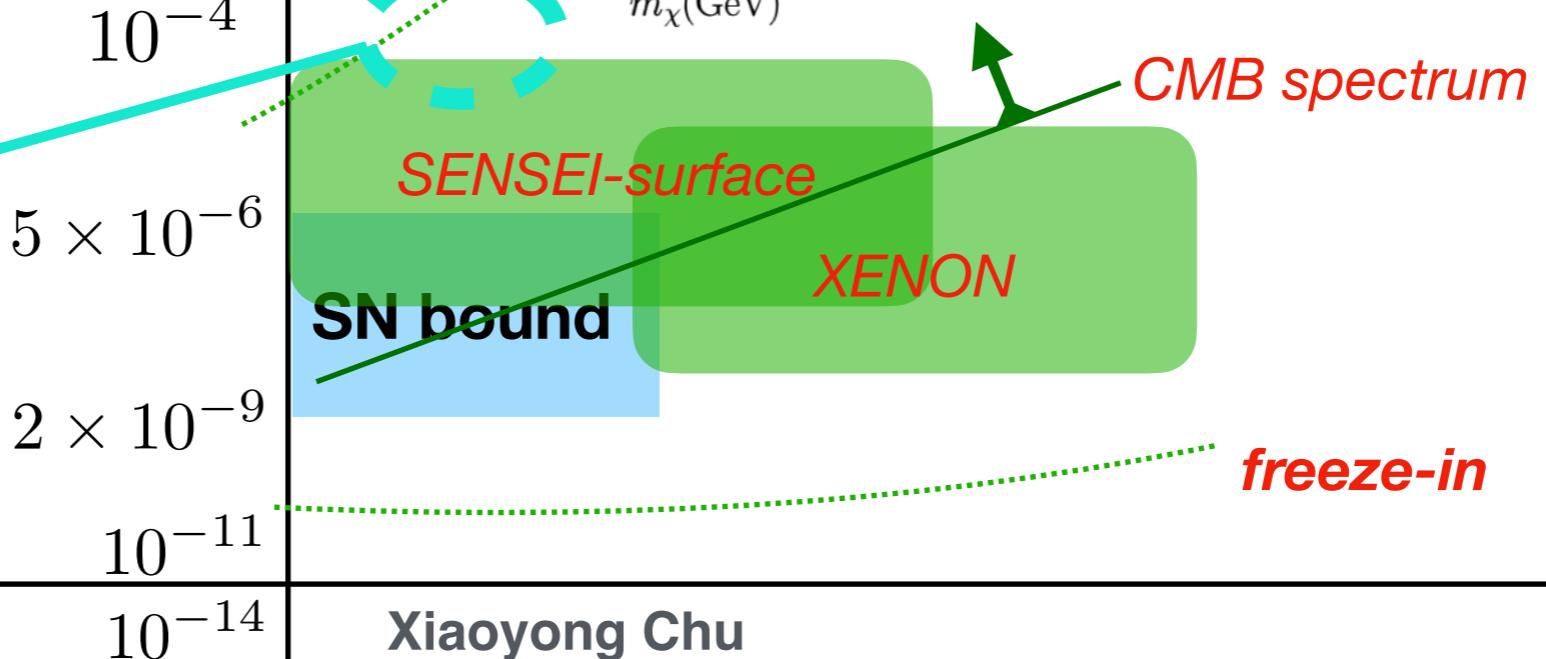


**XC**, J.Kuo, J.Pradler  
2001.06042

**freeze-out [excluded]**

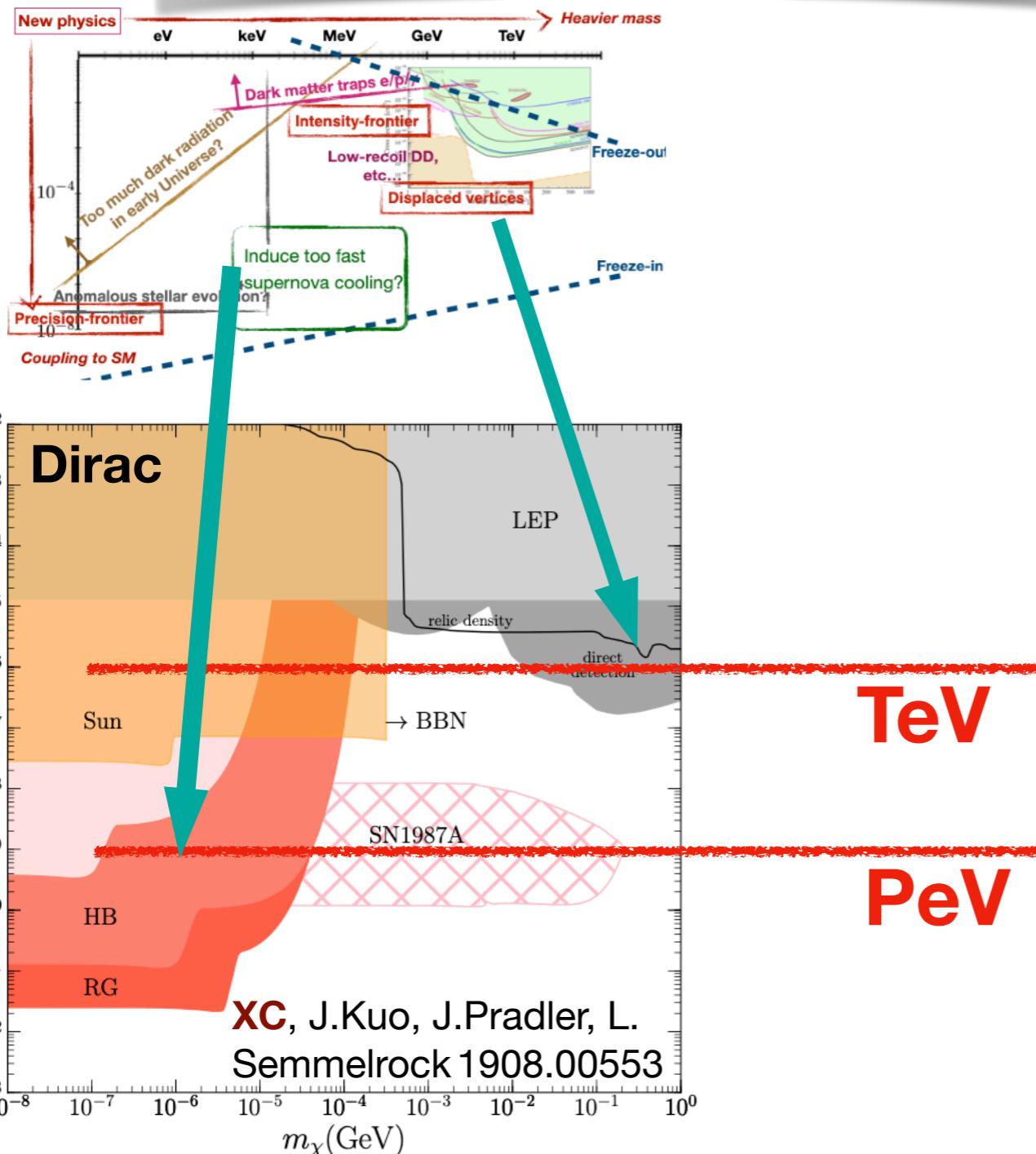
**If full dark matter**

adding neutrino annihilation  
 $\sigma v_\nu \sim 10^2 \sigma v_\gamma$   
 $\rightarrow 0.2\% \text{ DM relic, explaining EDGES}$   
**[XC & J.Pradler 2310.06611]**



# Summarise **dim-5 constraints** on fermions:

interaction type	fermion $f(s)$
magnetic dipole	$\frac{2}{3}\mu_\chi^2 s^2(1 + \frac{8m_\chi^2}{s})$



- **Thermal freeze-out via EM factors** is unlikely, while small regions (**p/d-wave annihilation**) left for detailed investigation.
- **High-order operators** are not enough to **cool down baryons** for 21cm observables (EDGES).

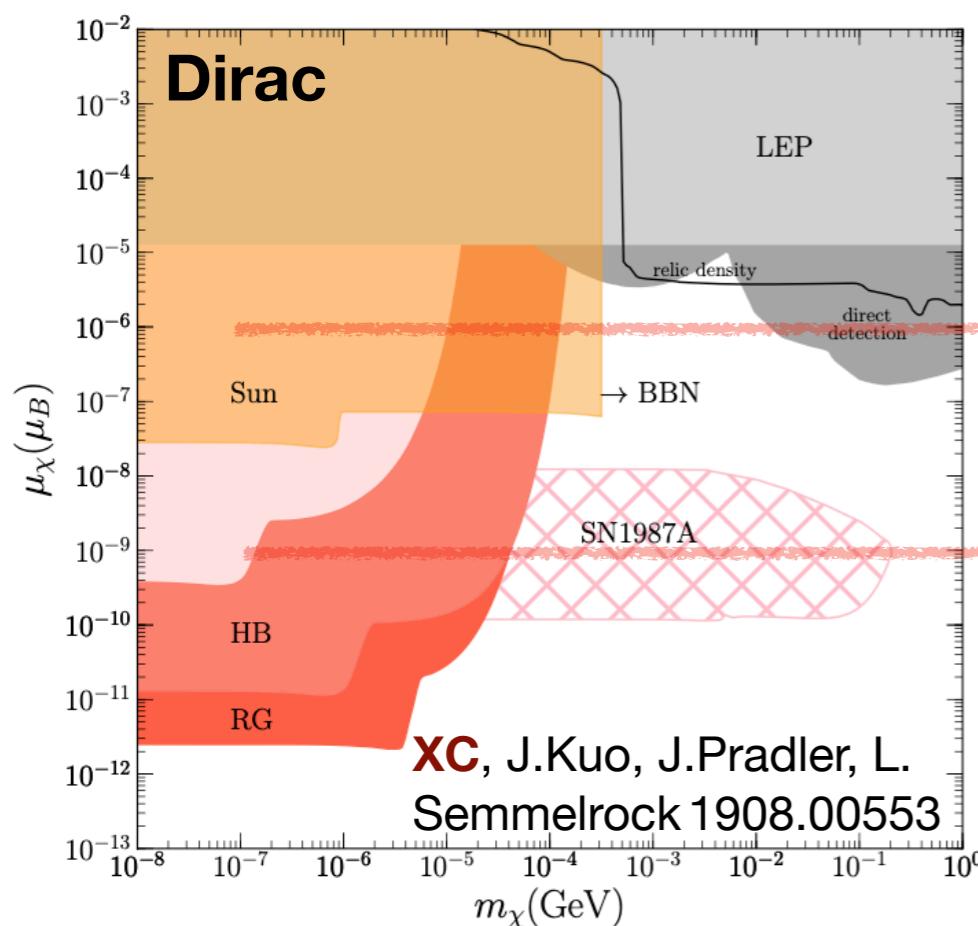
# Summarise **dim-5 constraints** on fermions:

interaction type	coupling	$C$	$P$	$CP$
magn. dipole	$\mu$	+1	+1	+1
elec. dipole	$d$	+1	-1	-1

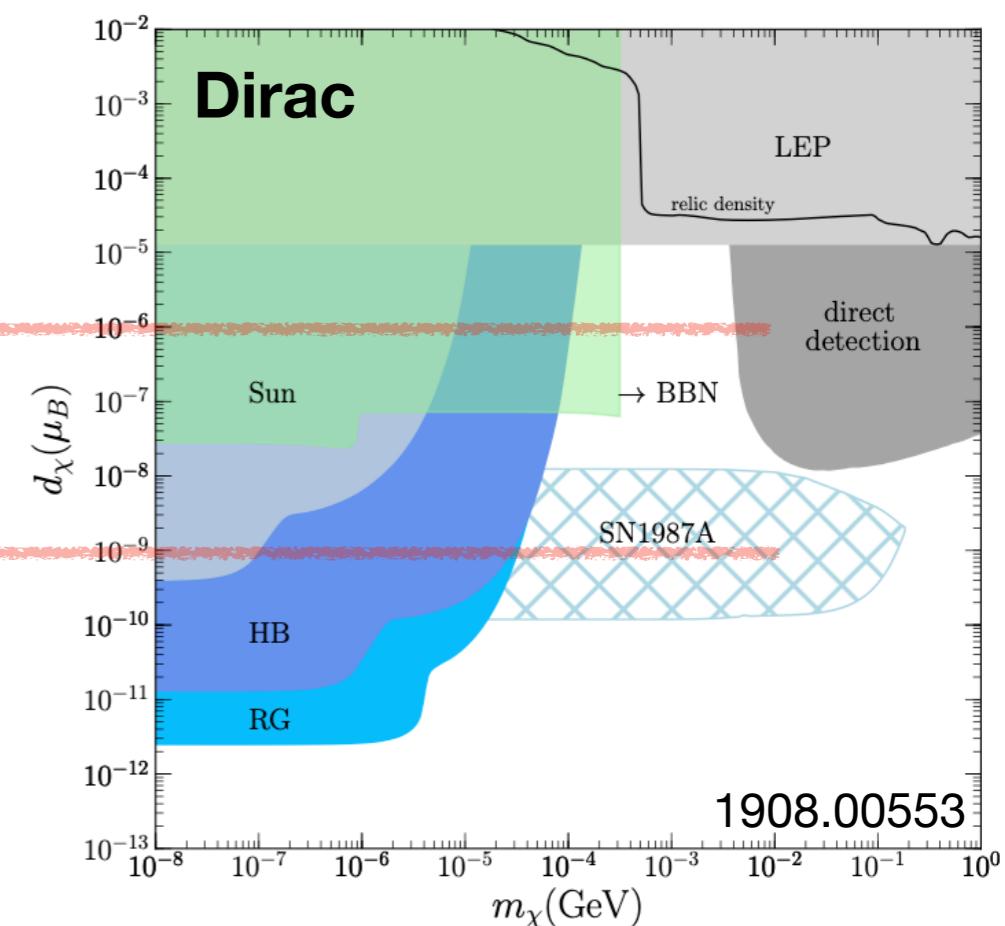
**CP affects mildly**

up to velocity suppressions  
in non-relativistic regime

**MDM**



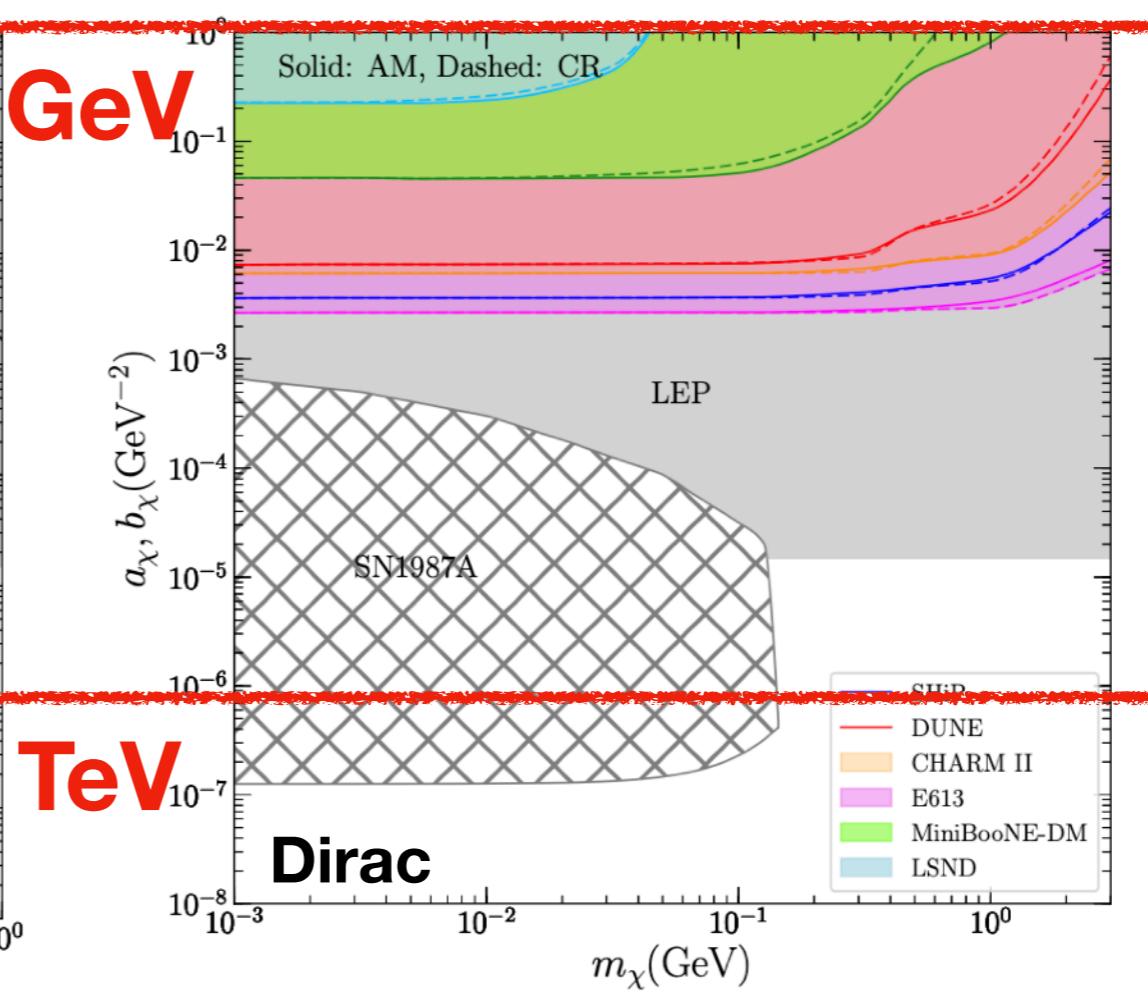
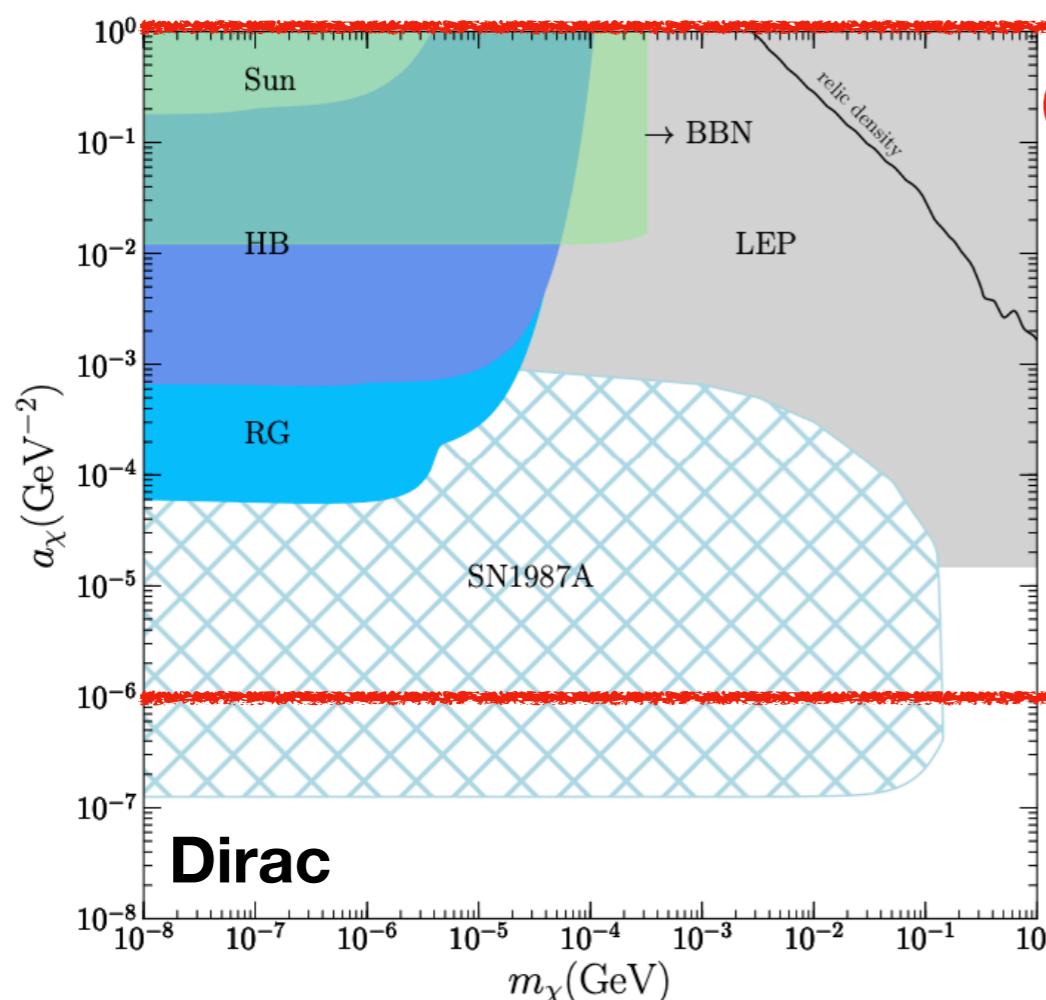
**EDM**



# Summarise **dim-6 constraints** on fermions:

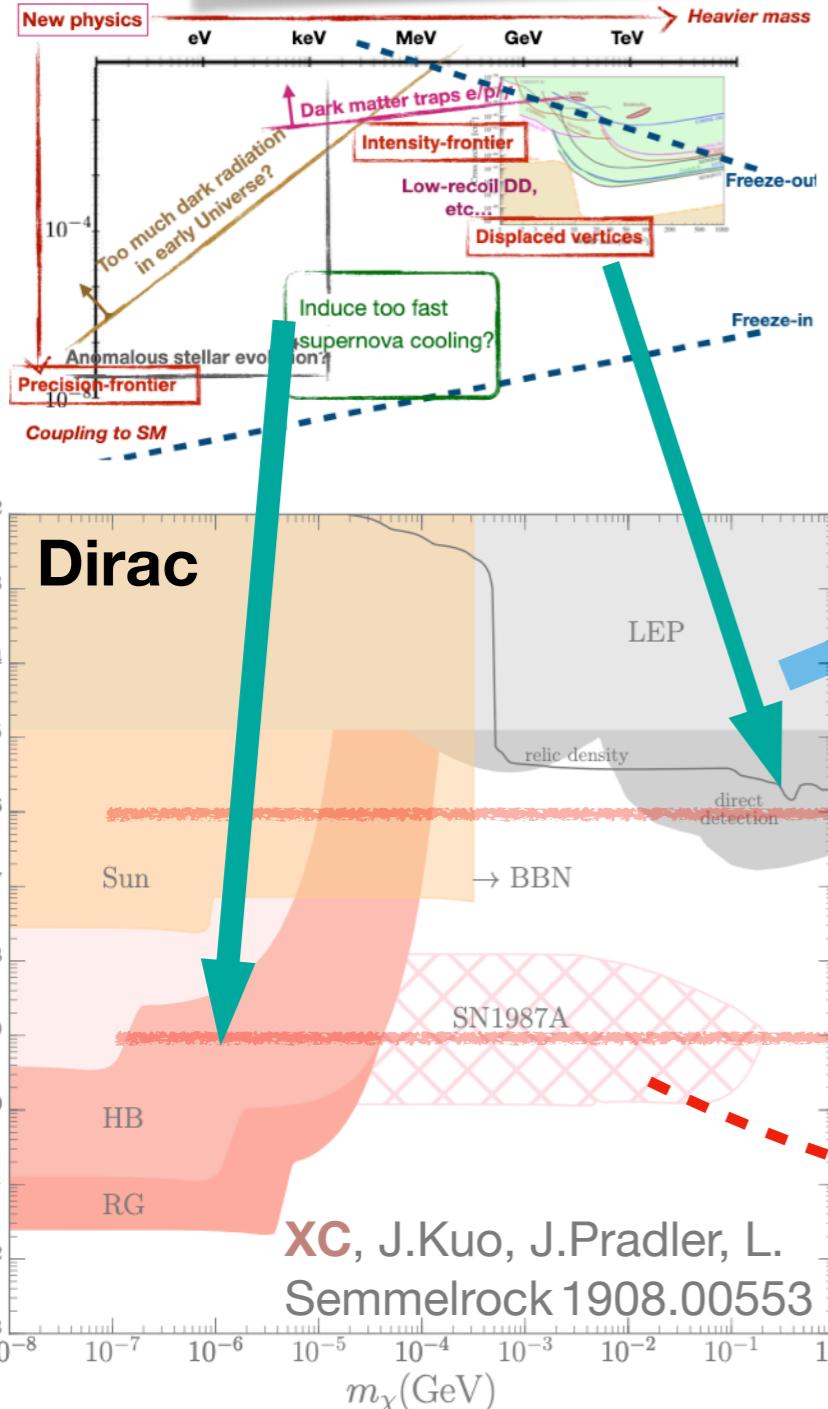
interaction type	fermion $f(s)$
charge radius	$\frac{4}{3} \frac{e^2 (g_1^\chi)^2 s^3}{m_\chi^4} (1 + \frac{2m_\chi^2}{s})$
anapole moment	$\frac{4}{3} \frac{e^2 (g_5^\chi)^2 s^3}{m_\chi^4} (1 - \frac{4m_\chi^2}{s})$

- Thermal **freeze-out fully excluded**.
- **LEP** easily beats **intensity-frontier** for **dim-6 operators**, while both hardly apply to GeV UV-scales.



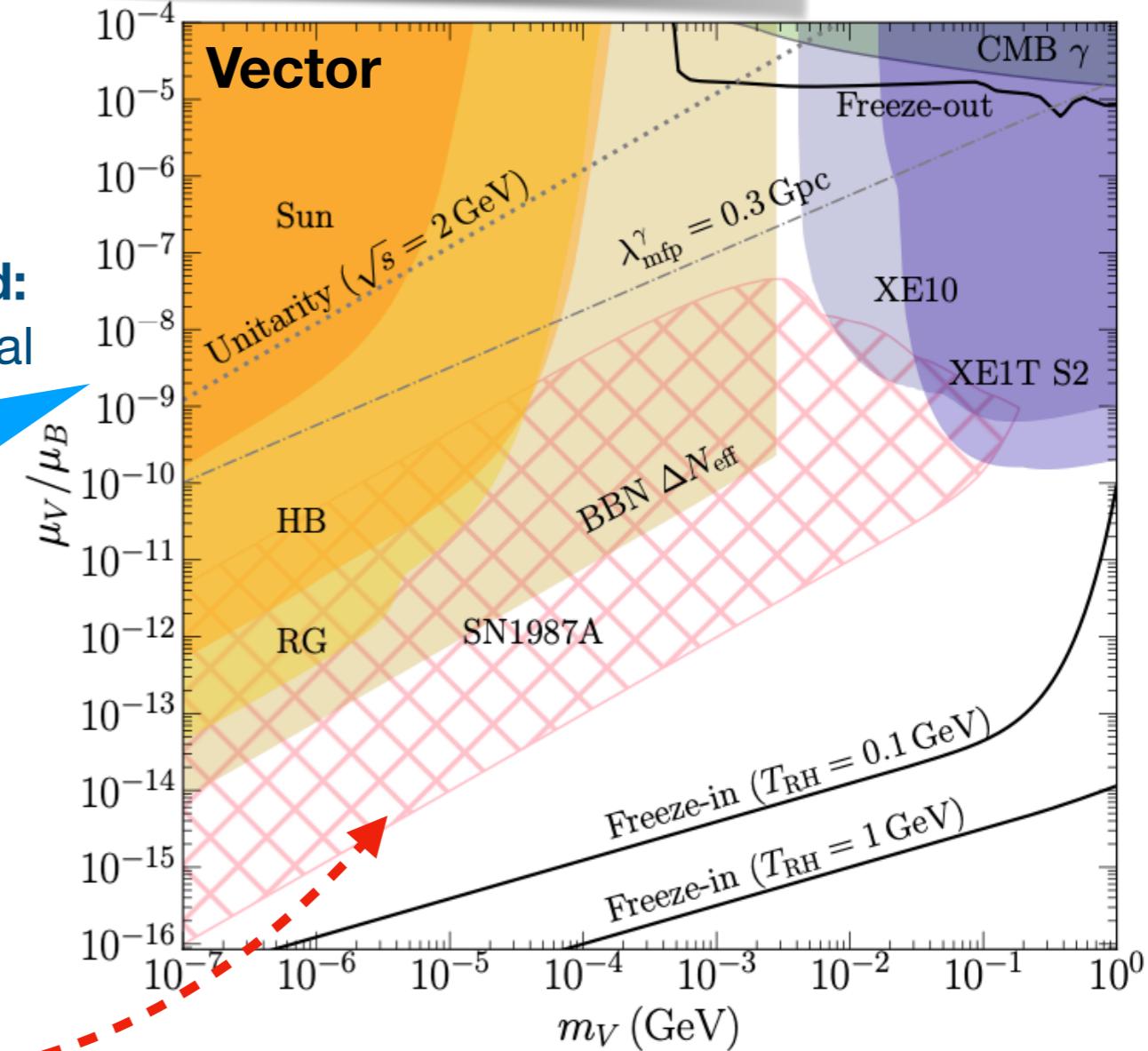
# Turn to spin-1 case: vector is different

interaction type	fermion $f(s)$	vector $f(s)$
magnetic dipole	$\frac{2}{3}\mu_\chi^2 s^2(1 + \frac{8m_\chi^2}{s})$	$\frac{\mu_V^2 s(s - 4m_V^2)(16m_V^2 + 3s)}{12m_V^2}$



1/m-enhanced:  
from longitudinal  
mode

TeV  
PeV



# V. Validity of the constraints

# Theoretical validity

---

**EM form factors are defined at extremely IR-end:**

- *For all spins, the C.o.M energy has to be below UV-theory scale  $\Lambda$ .  
we can not exclude regions where dimensionless coeff.  $\times (\text{C.o.M})^n \geq 1$*
- *Spin-1 case needs to be treated with additional caution:*

we indicate unitarity bound as:  $\sigma_{V+V \rightarrow V+V}(s) \lesssim \frac{4\pi}{s} \sum_l (2l + 1)$

similar to WW-scattering (with a dark higgs mass above the energy-scale).

**This is still not enough**, which can be seen in a **UV-completion**.

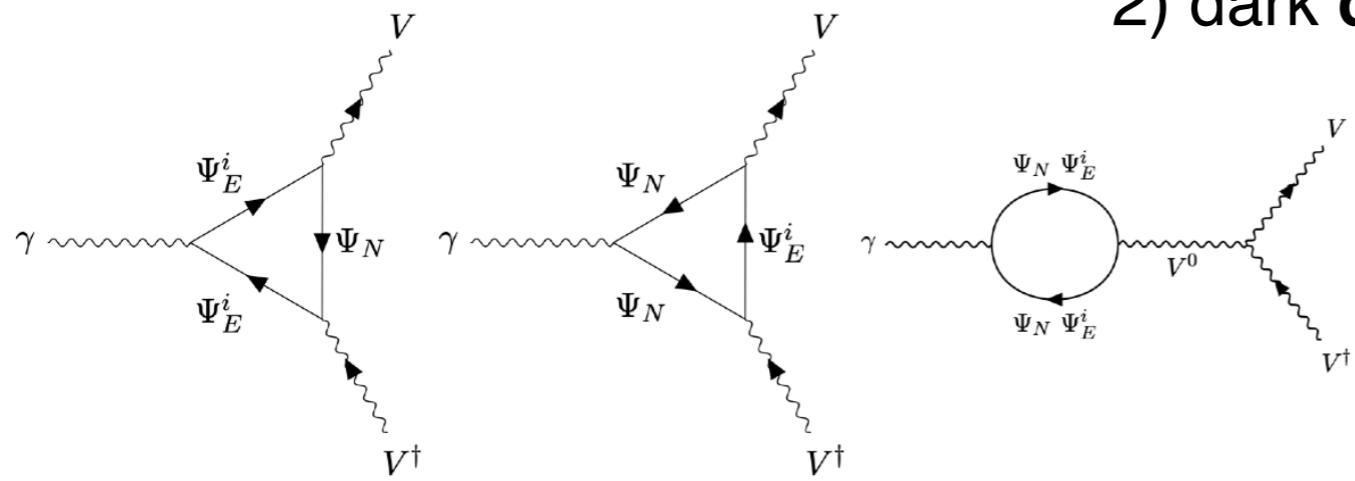
- EM form factors are not necessarily independent.

# Realization of UV-completion

J. Hisano, A.Ibarra, and R. Nagai, 2007.03216

**Dark SU(2) gauge bosons** with: 1) dark doublet leptons that couple to photon;

2) dark doublet Higgs that generates masses.



In the limit of heavy dark fermions/scalars

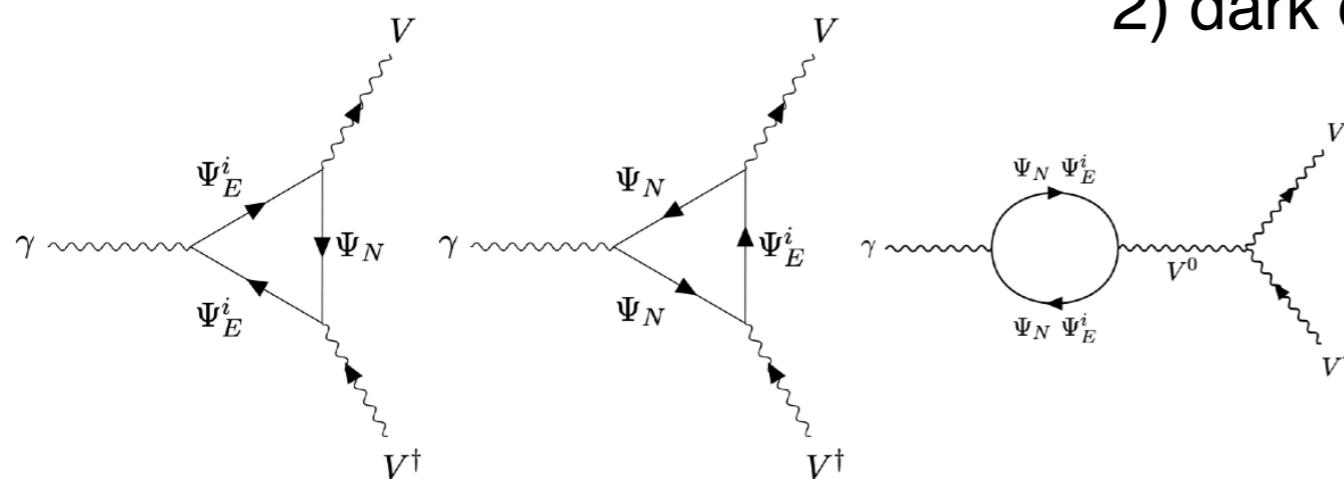
one can write down **all the EM form factors in terms of UV parameters**

# Realization of UV-completion

**xc**, J. Hisano, A.Ibarra, J.Kuo, J.Pradler, 2303.13643

**Dark SU(2) gauge bosons** with: 1) dark **doublet leptons** that couple to photon;

2) dark **doublet Higgs** that generates masses.



A) dim-6 terms:

interaction type	coupling	$C$	$P$	$CP$
charge radius	$g_1^A/m^2$	+1	+1	+1
toroidal moment	$g_4^A/m^2$	-1	+1	-1
anapole moment	$g_5^A/m^2$	-1	-1	+1

This UV model gives at first-order:

$$g_1^A \propto g_5^A \propto m_V^2/m_F^2 \quad \text{and} \quad g_4^A = 0$$

so the full couplings are **independent of  $m_V$** .

For such terms, a UV-completion gives the correct scaling of production rates,

$$\dot{Q}_{\lambda\lambda'} \propto \begin{cases} g_D^4/m_V^4 & \lambda\lambda' = LL, \\ g_D^4/m_V^2 & \lambda\lambda' = LT, \\ g_D^4 & \lambda\lambda' = TT. \end{cases}$$

$$\text{seen from } \epsilon_L = \left( \frac{p}{m_V}, 0, 0, \frac{E}{m_V} \right), \quad \epsilon_T^\pm = \left( 0, \frac{1}{\sqrt{2}}, \pm \frac{i}{\sqrt{2}}, 0 \right)$$

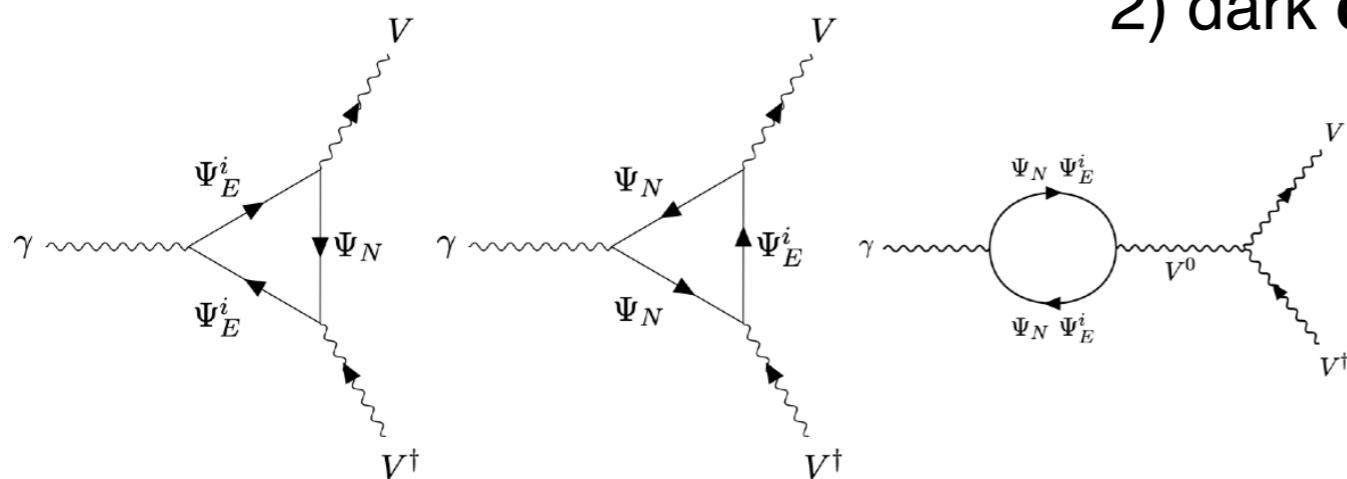
which can stay valid until the SSB scale, which **heavy dark higgs** enters.

# Realization of UV-completion

xc, J. Hisano, A.Ibarra, J.Kuo, J.Pradler, 2303.13643

**Dark SU(2) gauge bosons** with: 1) dark doublet leptons that couple to photon;

2) dark doublet Higgs that generates masses.



B) consider terms with CP (+ -):

interaction type	coupling	$C$	$P$	$CP$
elec. dipole	$d$		+1	-1
magn. quadrupole	$\tilde{Q}$		+1	-1

each amplitude diverges at  $m_V \rightarrow 0$ , even for transverse  $V$ -boson production.

In the UV model, there is, at first-order,

$$d_V = -\tilde{Q}_V m_V / 2$$

the divergences in transverse modes cancel with each other.

- Seems unphysical to **separate the two operators** for vector states *-under investigation*;
- Operators with the same CP can be seen as belonging to the same group.
- Our bounds are mostly sensitive to **the scaling of  $f(s)$** , and thus easy to generalize.

# VI. Conclusions

# Conclusions

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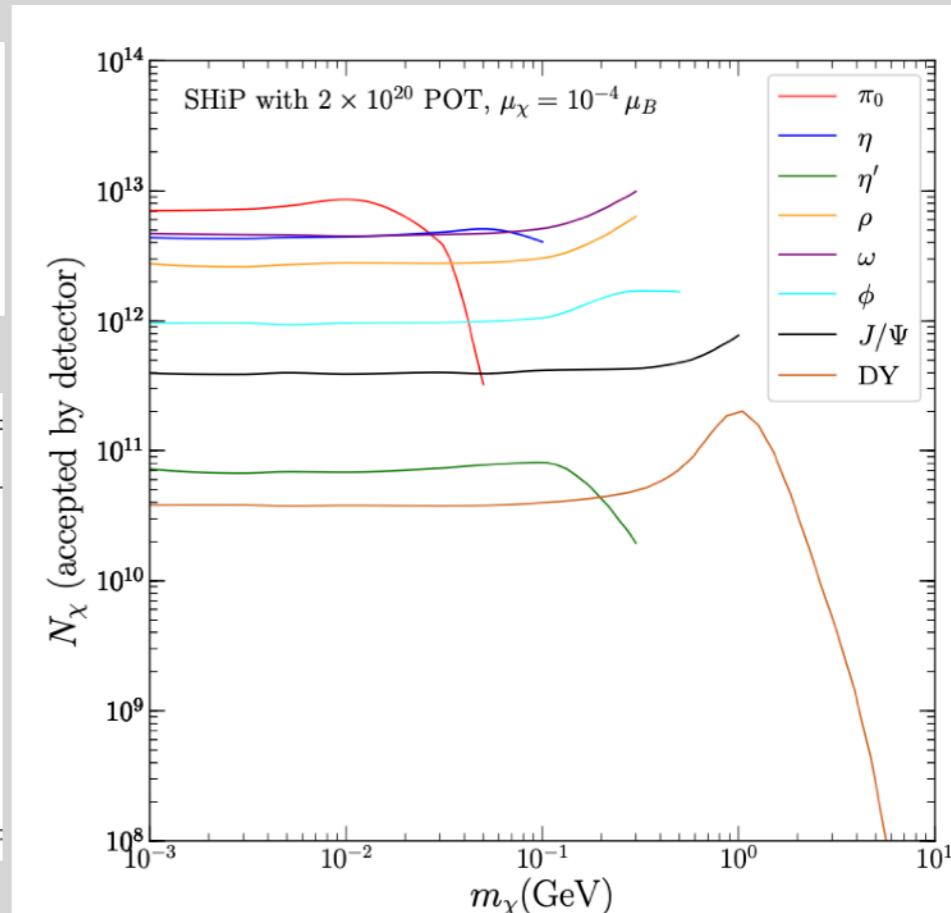
- So far no heavy new particles, try **something (with) light?**
- Most appealing light portal: **multi-messenger** constraints/  
observations will be important to identify dark states;
- **Intensity/neutrino** experiments play an important role.
- **Astrophysics** can be extremely useful in probing feeble dark states.
- **Parameters/values of EM factors** not always justified by UV  
models.

# Backup

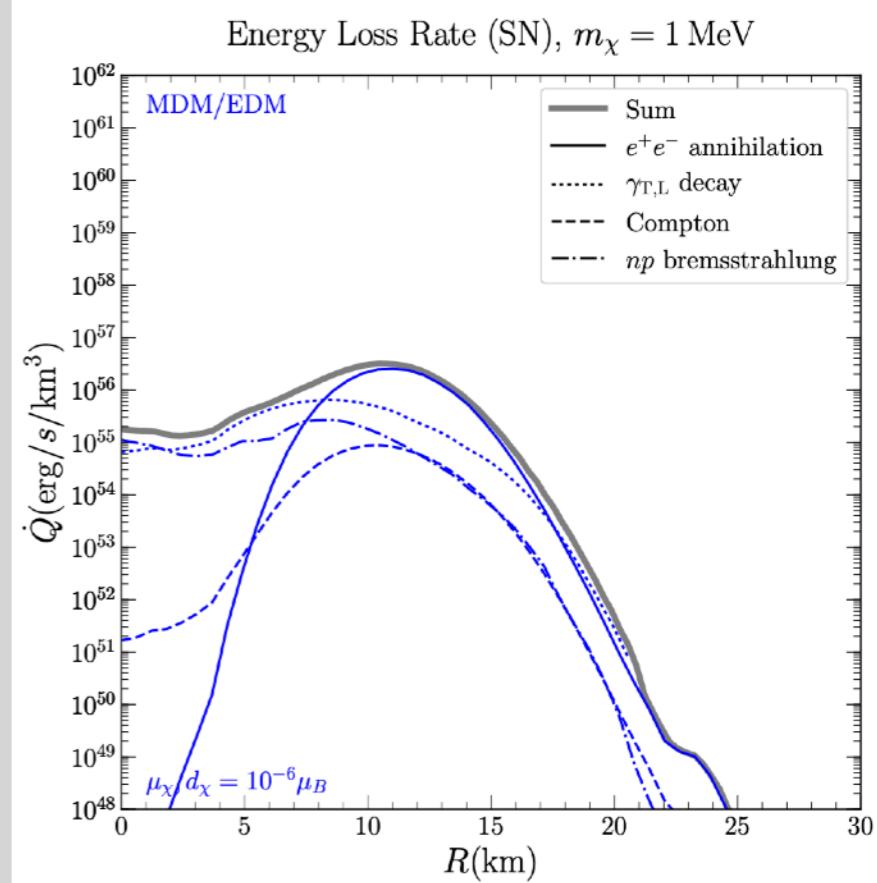
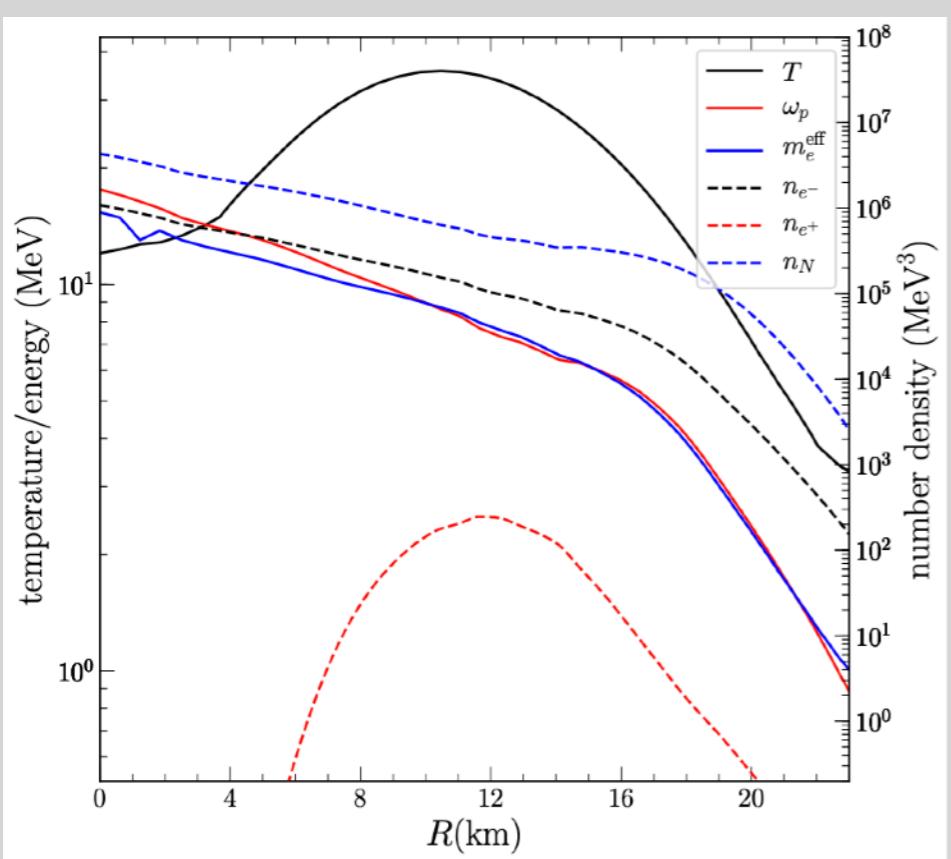
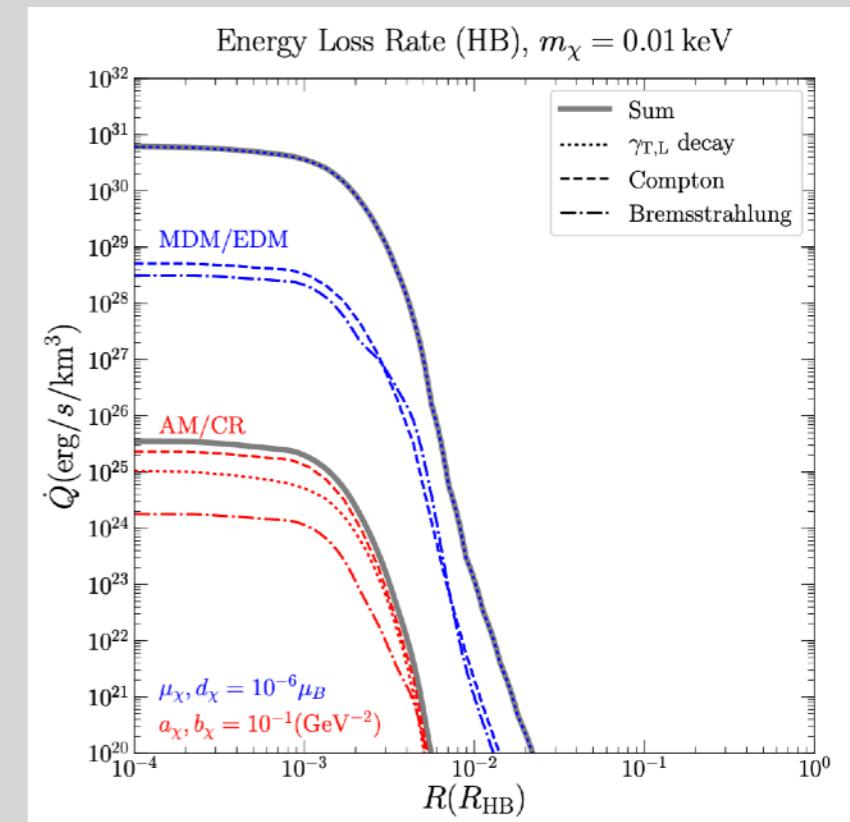
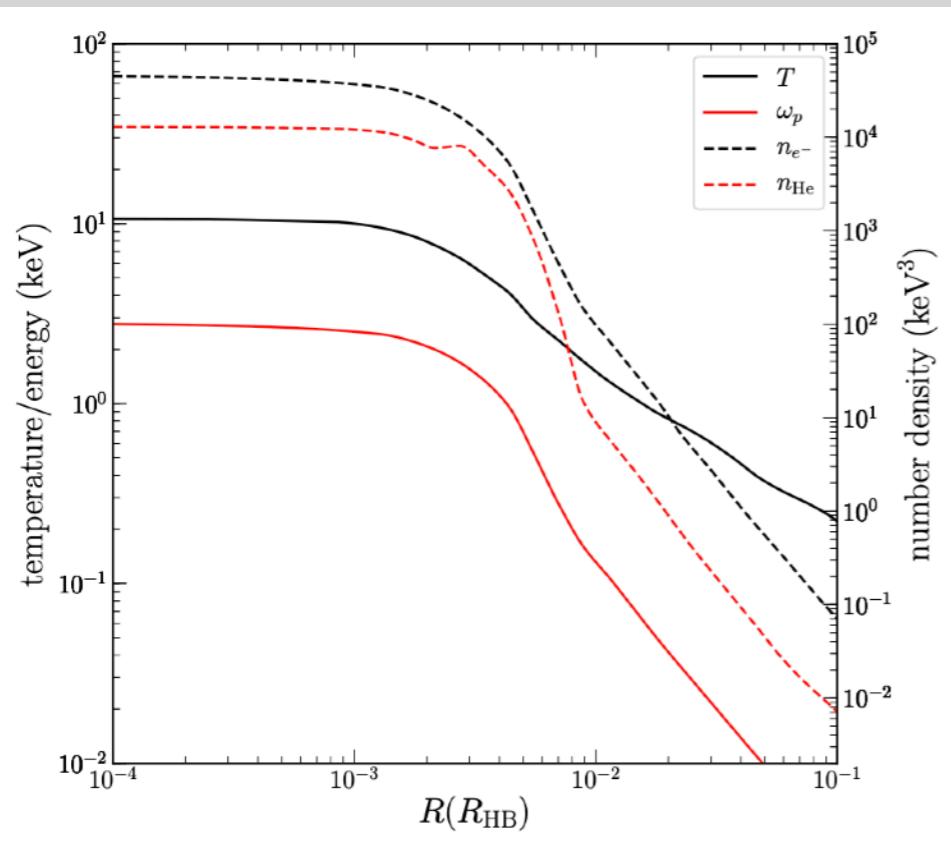
# Experimental parameters

$E_{\text{beam}} \setminus \text{meson}$	$\pi^0$	$\eta$	$\eta'$	$\rho$	$\omega$	$\phi$	$J/\Psi$
8.9 GeV (MiniBooNE-DM)	$8.6 \times 10^{-1}$	$8.2 \times 10^{-2}$	$4.9 \times 10^{-3}$	$6.9 \times 10^{-2}$	$7.4 \times 10^{-2}$	$1.1 \times 10^{-4}$	0
120 GeV (DUNE)	2.9	$3.2 \times 10^{-1}$	$3.4 \times 10^{-2}$	$3.7 \times 10^{-1}$	$3.7 \times 10^{-1}$	$1.1 \times 10^{-2}$	$5.0 \times 10^{-7}$
400/450 GeV (SHiP, E613/CHARM II)	4.1	$4.6 \times 10^{-1}$	$5.1 \times 10^{-2}$	$5.4 \times 10^{-1}$	$5.4 \times 10^{-1}$	$1.9 \times 10^{-2}$	$8.0 \times 10^{-6}$

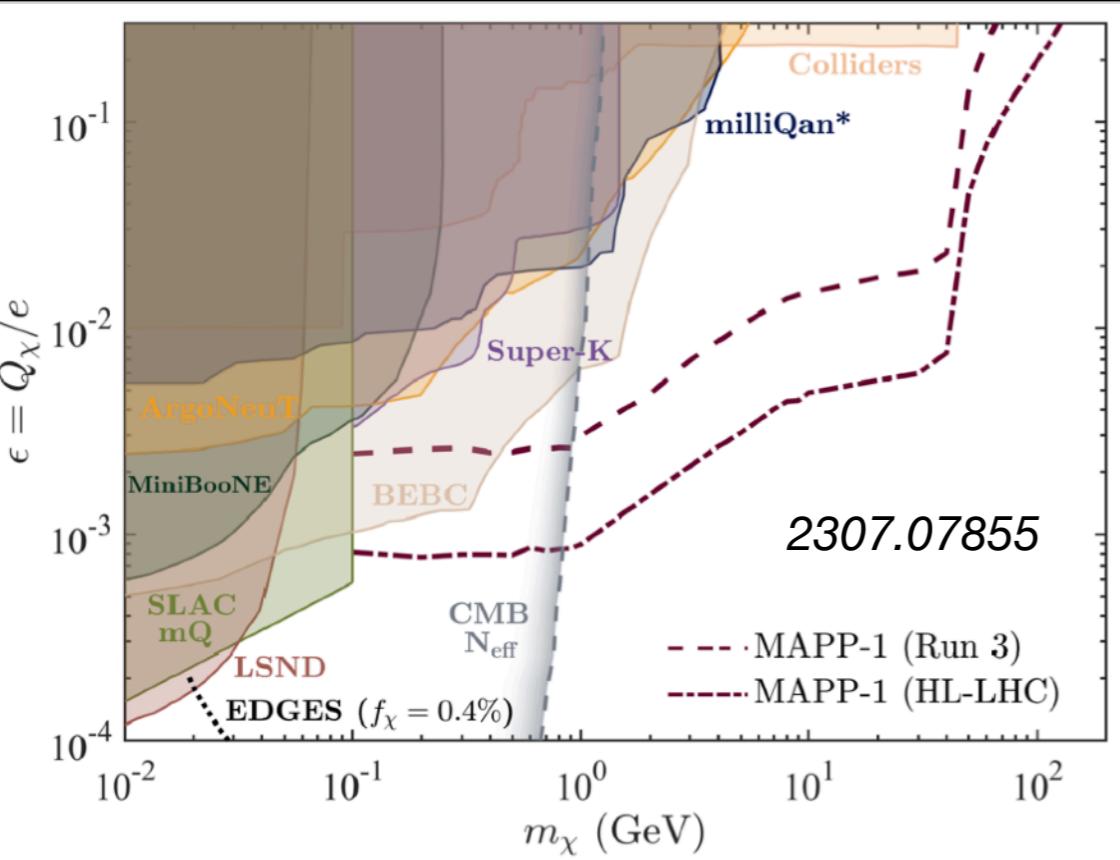
Experiments	POT ( $10^{20}$ )	$ \theta_{\chi}^{\max} $	Signal process and cuts	$N_{\text{bkg}}$	$\epsilon_{\text{eff}}$	on/off axis
LSND	1800	-	e-recoil ( $E_R \in [18, 52] \text{ MeV}, \theta_R \leq \pi/2$ )	$N_{\text{sig}} \leq 110$	0.16	$31^\circ$
MiniBooNE-DM	1.86	12.4 mrad	e-recoil ( $E_R \in [75, 850] \text{ MeV}, \theta_R \leq 140 \text{ mrad}$ )	0	0.2	$0^\circ$
CHARM II	0.25	2.1 mrad	e-recoil ( $E_R \in [3, 24] \text{ GeV}, E_R \theta_R^2 \leq 3 \text{ MeV}$ )	5429	$\sim 1$	$0^\circ$
DUNE (10 yr)	11/yr	3.4 mrad	e-recoil ( $E_R \in [0.6, 15] \text{ GeV}, E_R \theta_R^2 \leq 1 \text{ MeV}$ )	8930/yr	0.5	$0^\circ$
SHiP	2	7.8 mrad	e-recoil ( $E_R \in [1, 20] \text{ GeV}, \theta_R \in [10, 20] \text{ mrad}$ )	846	$\sim 1$	$0^\circ$
E613	0.0018	12.8 mrad	had. shower ( $E_N^{\text{dep}} \geq 20 \text{ GeV per event}$ )	$N_{\text{sig}} \leq 180$	$\sim 1$	$0^\circ$



# Stellar parameters



# Milli-charged fermions, in the literature



$$\begin{aligned}
 & -\mu(\vec{B} \cdot \vec{\sigma}) - d(\vec{E} \cdot \vec{\sigma}) - a(\vec{j} \cdot \vec{\sigma}) \\
 & - b(\nabla \cdot \vec{E}) - Q_{ij, \text{traceless}} \nabla_i \vec{E}_j - \tilde{Q}_{ij} \nabla_i B_j - \dots
 \end{aligned}$$

