

# Beyond the EFT Approach to Dark Matter

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THE UNIVERSITY OF  
MELBOURNE



**CoEPP**  
ARC Centre of Excellence for  
Particle Physics at the Terascale

1311.6169, 1407.4566

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# The Dark Universe

## Ordinary Matter



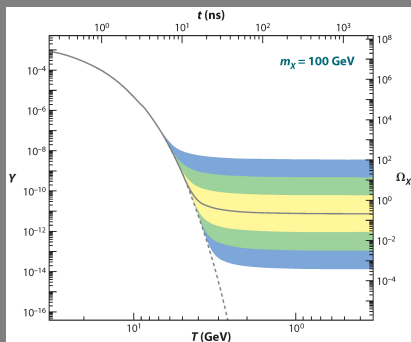
## Dark Matter

- **Existence**  
from rotational curves to CMB, proofs across all cosmological scales ✓
- **Amount**  
roughly a quarter ✓
- **Identity**  
non-baryonic ✓  
species, mass, spin, interaction strength, its own particle ... ?

# DM Candidates

## Weakly Interacting Massive Particle

- mass: weak scale
- interaction: weak scale
- $\Omega h^2 \sim \mathcal{O}(1)$
- many candidates: neutralino ...

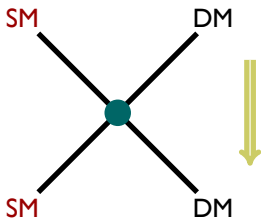


## The Non-WIMP Ones

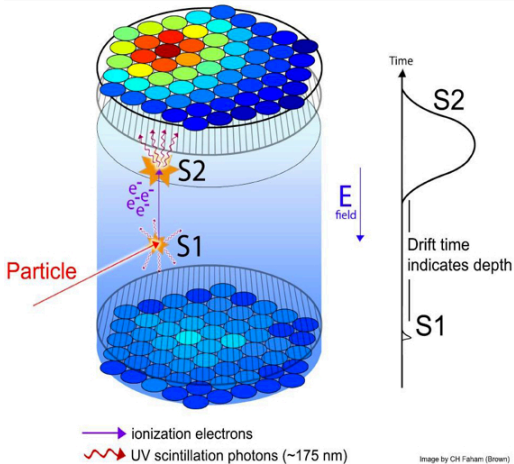
- warm dark matter, axion, asymmetric dark matter...

Let's look at the WIMP ones for now.

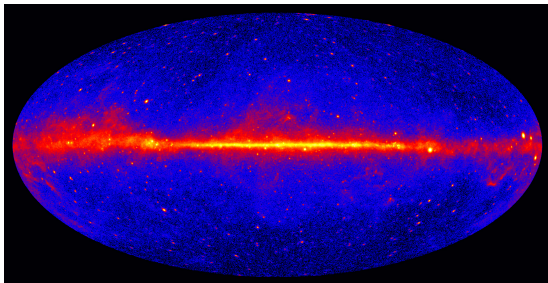
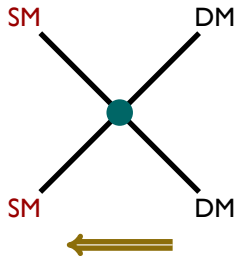
# Our Expedition



- **Direct Detection**  
nuclear recoil

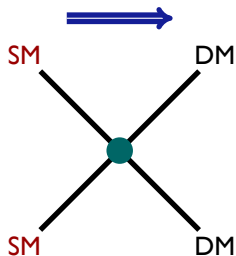


# Our Expedition

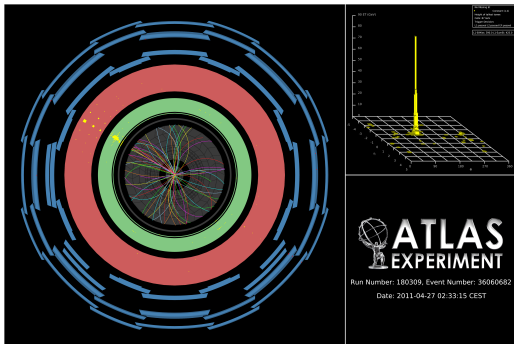


- **Direct Detection**  
nuclear recoil
- **Indirect Detecion**  
 $\gamma, e^{\pm}, \bar{p}, \nu$

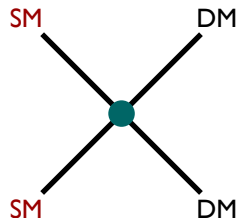
# Our Expedition



- **Direct Detection**  
nuclear recoil
- **Indirect Detecion**  
 $\gamma, e^{\pm}, \bar{p}, \nu$
- **Collider Searches**  
missing ET



# The Theoretical Interpretation



the form of  
interaction here is  
unknown

## UV Complete Theories

MSSM, mSUGRA, UED, Little Higgs...

too many parameters, very much model dependent

↑ **a gap needs to be bridged** ↑

## !(UV Complete) Theories

### **EFT:**

contact int., dipole int.

### **Simplified Models:**

$Z'$ , Higgs portal, dark photon ...



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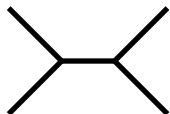
Summary

# The EFT Approach

Fermionic DM

**UV**

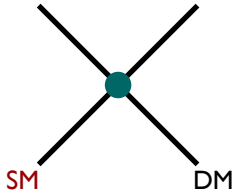
SM DM



SM DM

**EFT**

SM DM



SM DM

$$Q^2 \ll M^2$$

$$\frac{g_\chi g_q}{Q^2 - M^2} \Rightarrow \frac{g_\chi g_q}{M^2} = \frac{1}{\Lambda^2}$$

$$\mathcal{L}_{\text{EFT}} = \frac{1}{\Lambda^2} (\bar{\chi} \Gamma_\chi \chi) (\bar{q} \Gamma_q q)$$
$$\Gamma_i \in \{1, \gamma^5, \gamma^\mu, \gamma^5 \gamma^\mu, \sigma^{\mu\nu}\}$$

parameters:  $\Lambda, m_\chi$

# Variations

$\alpha_s$  shows up as loop factors and  $m_q$  for Yukawa couplings.

operator	coefficient
...	...
$(\bar{\chi}\Gamma_i\chi)(G_{\mu\nu}G^{\mu\nu})$	$\sim \alpha_s/\Lambda^3$
$(\bar{\chi}\Gamma_i\chi)(G_{\mu\nu}\tilde{G}^{\mu\nu})$	$\sim \alpha_s/\Lambda^3$

Table: Dirac fermion

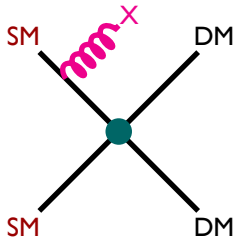
**also a list for Majorana fermions**

operator	coefficient
$(\phi^\dagger\phi)(\bar{q}\gamma^{0,5}q)$	$\sim m_q/\Lambda^2$
$(\phi^\dagger\partial_\mu\phi)(\bar{q}\gamma^\mu\gamma^{0,5}q)$	$1/\Lambda^2$
$(\phi^\dagger\phi)(G_{\mu\nu}G^{\mu\nu})$	$\alpha_s/4\Lambda^2$
$(\phi^\dagger\phi)(G_{\mu\nu}\tilde{G}^{\mu\nu})$	$\alpha_s/4\Lambda^2$

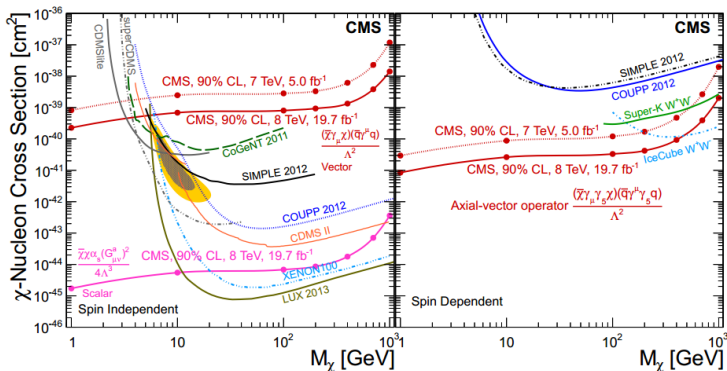
operator	coefficient
$(\phi^2)(\bar{q}\gamma^{0,5}q)$	$\sim m_q/\Lambda^2$
$(\phi^2)(G_{\mu\nu}G^{\mu\nu})$	$\alpha_s/4\Lambda^2$
$(\phi^2)(G_{\mu\nu}\tilde{G}^{\mu\nu})$	$\alpha_s/4\Lambda^2$

Table: Complex and real scalar

# Interplay of EFT among DM Experiments

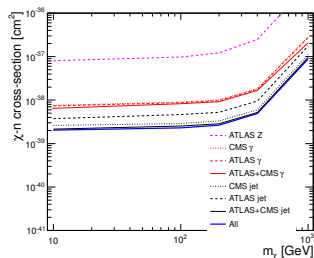
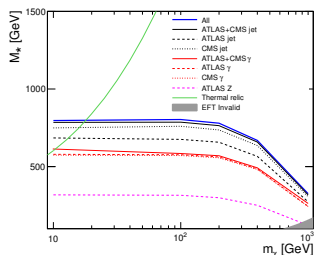


- Collider searches
  - signature: mono- $j$ ,  $\gamma$ ,  $Z$ ,  $W$ ...
  - observation: no excess
  - place limit on  $\Lambda$
- Compare with DD:  $\sigma_{\chi N}$



# On the Validity of EFT

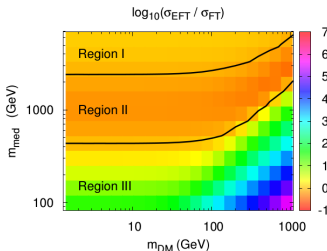
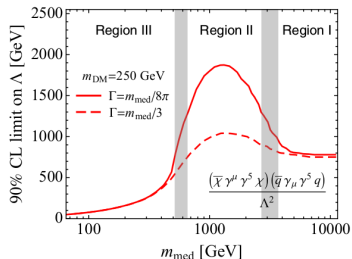
- $\Lambda \sim \text{TeV}$ , mediator can be on-shell



1302.3619

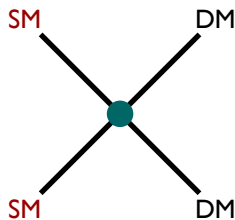
# On the Validity of EFT

- $\Lambda \sim \text{TeV}$ , mediator can be on-shell
- $\sigma_{EFT}/\sigma_{FT}$ 
  - underestimate resonance, new colored particles
  - overestimate light mediator
- Relic abundance?

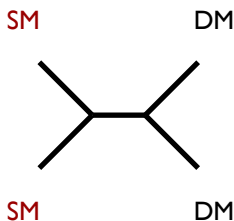


1308.6799

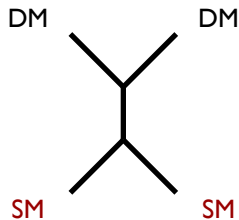
# Upgrade from the EFT: the Simplified Models



**open the operator**



mediator lighter or heavier than  
DM



mediator heavier than DM, carry  
SM quantum number

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# Leptophilic Dark Matter

## Leptophilic

$$(\bar{q}\Gamma_q q) (\bar{\chi}\Gamma_\chi \chi) \Rightarrow (\bar{l}\Gamma_l l) (\bar{\chi}\Gamma_\chi \chi)$$

- 0907.3159, 1406.1269
- Direct detection: no nuclear recoil at leading order
- LHC constraints from mono-X don't apply

## $s$ -channel vector exchange

$$\begin{aligned} \mathcal{L} = & \mathcal{L}_{SM} - \frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu} - \frac{\epsilon}{2} Z'_{\mu\nu} B^{\mu\nu} + i\bar{\chi}\gamma_\mu \partial^\mu \chi \\ & + \bar{\chi}\gamma^\mu (g_\chi^V + g_\chi^A \gamma^5) \chi Z'_\mu + \bar{l}\gamma^\mu (g_\ell^V + g_\ell^A \gamma^5) l Z'_\mu \\ & - m_\chi \bar{\chi}\chi + \frac{1}{2} m_{Z'}^2 Z'_\mu Z'^\mu \end{aligned}$$

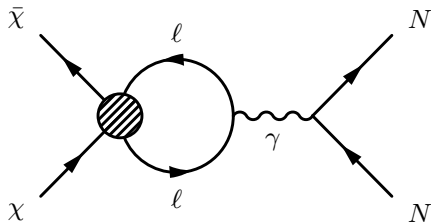
At low energy,  $\Lambda = \frac{m_{Z'}}{\sqrt{g_\chi g_\ell}}$

# Direct Detection

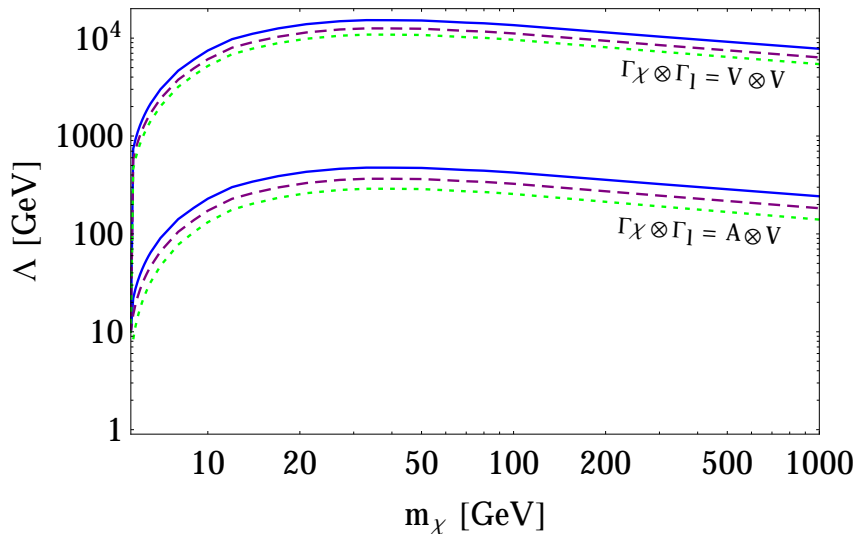
Table: Lorentz structure of the  $Z'$  couplings.

$\Gamma_\chi \otimes \Gamma_\ell$	$\sigma(\chi\chi \rightarrow \bar{\ell}\ell)$	$\sigma(\chi N \rightarrow \chi N)$	Gauge invariant?
$V \otimes V$	<i>s</i> -wave	1 (1-loop)	Yes
$A \otimes V$	<i>p</i> -wave	$v^2$ (1-loop)	Yes
$V \otimes A$	<i>s</i> -wave	-	No
$A \otimes A$	<i>p</i> -wave	-	No

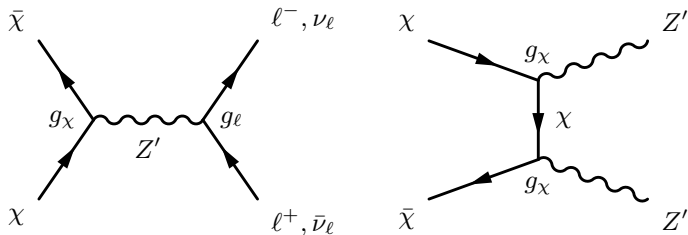
- $\Gamma_l$  **A**: the loop-level  $\sigma = 0$ .
- $\Gamma_l$  **V**: respect  $U(1)_L$ .
- $\Gamma_\chi$  **V**: forbidden for Maj. DM.
- $L_\mu - L_\tau$  considered before.
- Experimentally a natural choice to take each flavor in turn.



# Direct Detection Constraints from LUX



# Relic Density

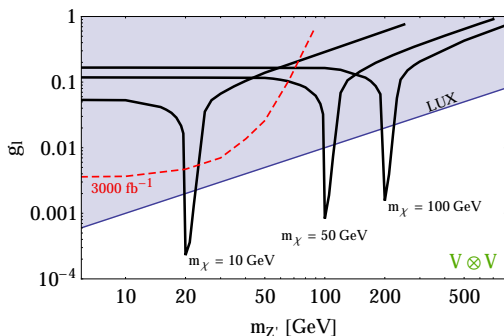


## Parameters

$$m_\chi, m_{Z'}$$
$$g_l, g_\chi = \# g_l, \# = 1, 4, 8$$

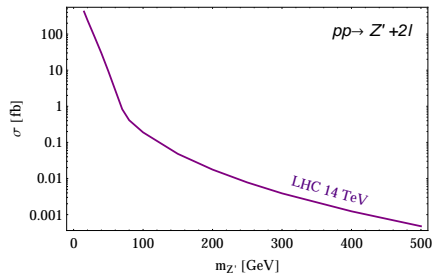
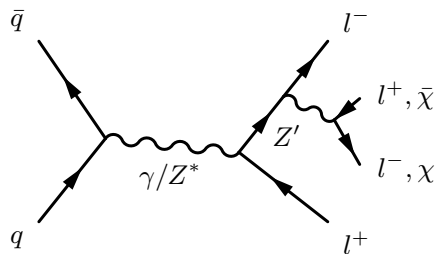
$$\Omega_\chi h^2 = 0.1187$$

# Constraints at a Glance



- $\Delta(g - 2)_l \sim \frac{g_l^2}{6\pi^2} \frac{m_l^2}{m_{Z'}^2} : 4 \times 10^{-10}, 8 \times 10^{-9}, 8 \times 10^{-2}$
- LSND,  $\nu$ - $e$  scattering,  $g_e \lesssim 3 \times 10^{-3} \frac{m_{Z'}}{\text{GeV}}$
- LEP II,  $Z'$ ,  $g_e \lesssim 0.044 \times m_{Z'}/200\text{GeV}$ ,  $m_{Z'} > 200\text{GeV}$
- LEP II, mono-photon

# LHC Search



- production via Drell-Yan
- possible signals
  - 4 leptons
  - 2 lepton + MET
- production cross section for  $g_l = 0.1$
- signal rates depend on the branching ratios

## 4 Leptons at the $Z$ Resonance

- Background:

$$pp \rightarrow Zl^+l^- \rightarrow l^+l^-l^+l^-$$

$$pp \rightarrow ZZ \rightarrow l^+l^-l^+l^-$$

- Follow ATLAS 4  $e$  and 4  $\mu$ , no 4  $\tau$  analysis
- Use  $20.7fb^{-1}$  data from 8 TeV LHC

### 4 $e$

- $p_T > 7$  GeV,  $|\eta| < 2.47$ ,  
 $\Delta R_{ee} > 0.1$
- $M_{e^+,e^-} > 20, 5$  GeV for the leading and next to leading pair
- $p_T > 20, 15, 10$  for the first three  $e$
- $80 \text{ GeV} < M_{4e} < 100 \text{ GeV}$

### 4 $\mu$

- $p_T > 4$  GeV,  $|\eta| < 2.7$ ,  
 $\Delta R_{\mu\mu} > 0.1$
- $M_{\mu^+,\mu^-} > 20, 5$  GeV for the leading and next to leading pair
- $p_T > 20, 15, 8$  for the first three  $\mu$
- $80 \text{ GeV} < M_{4\mu} < 100 \text{ GeV}$

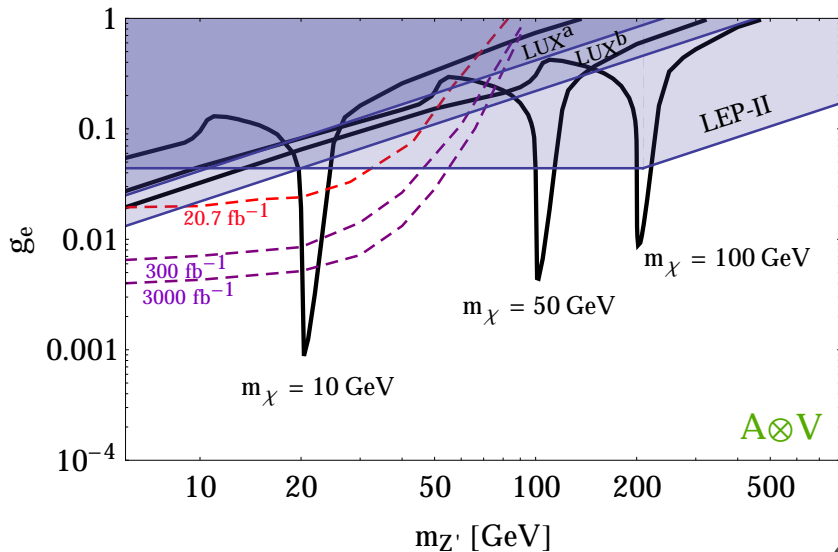
## 4 Lepton with Higher $m_{Z'}$

- **4  $e$**  case not considered since the higher mass region is completely eliminated by the LEP  $Z'$  search
- **4  $\mu$** 
  - $p_T > 4 \text{ GeV}$  ,  $|\eta| < 2.7$ ,  $\Delta R_{\mu\mu} > 0.1$
  - $M_{\mu^+, \mu^-} > 100$  for the leading pairs
  - $p_T > 120, 100, 8$  for leading  $\mu$ s
  - $M_{4\mu}$  not constrained so that we can probe above the  $Z$  mass
  - Detector simulation is not performed since efficiency for  $\mu$  is high



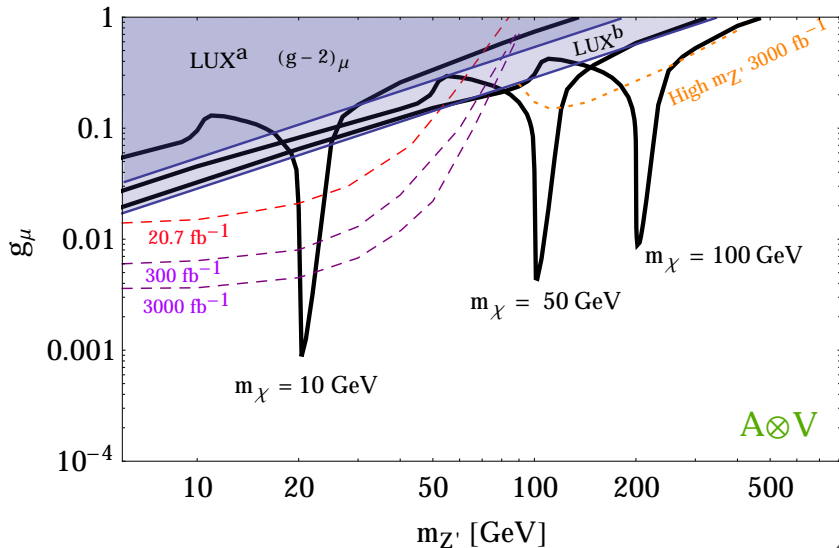
# Results for 4 $e$

$$g_\chi = g_e$$



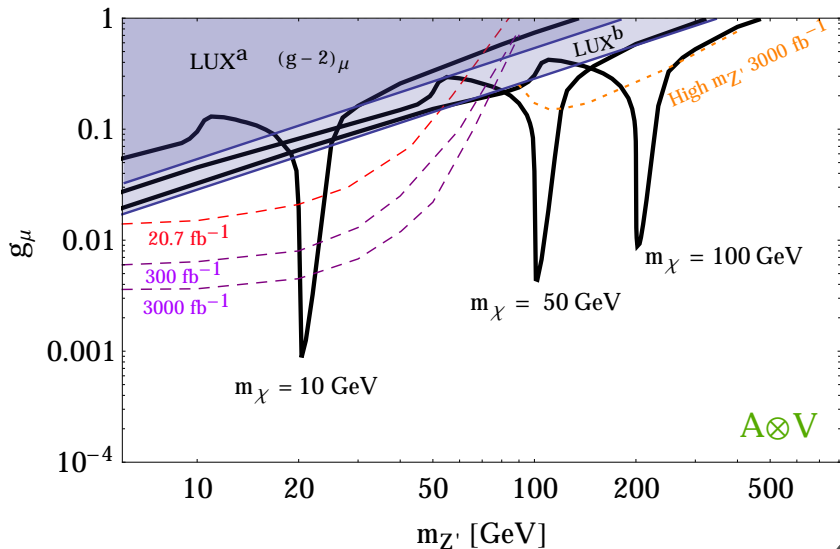
# Results for $4 \mu$

$$g_\chi = g_\mu$$



# Results for $4 \mu$

$$g_\chi = 4g_\mu$$



# Generalize the EFT Description

- Other particles in the dark sector sometimes can not neglected.
- Consider a simple extension with two dark sector particles of similar mass.
  - Relic density controlled by co-annihilation of  $\chi_1$  and  $\chi_2$
  - $\chi_2$  decays to  $\chi_1$  with lifetime  $\ll$  age of universe

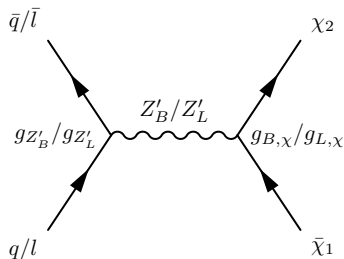
- The description

$$\frac{1}{\Lambda_{11}^2} (\bar{\chi}_1 \Gamma_1 \chi_1) (\bar{f} \Gamma_2 f)$$
$$\frac{1}{\Lambda_{12}^2} (\bar{\chi}_1 \Gamma_1 \chi_2) (\bar{f} \Gamma_2 f) + \text{h.c.}$$
$$\frac{1}{\Lambda_{22}^2} (\bar{\chi}_2 \Gamma_2 \chi_1) (\bar{f} \Gamma_2 f)$$

- Assumptions:  $\Lambda_{11} \gg \Lambda_{12}, \Lambda_{22}$

# UV Completion

- When EFT breaks down, the UV completion is necessary.
- Simple completion with two neutral massive gauge bosons,  $Z'_B$  and  $Z'_L$



- Two effective scales

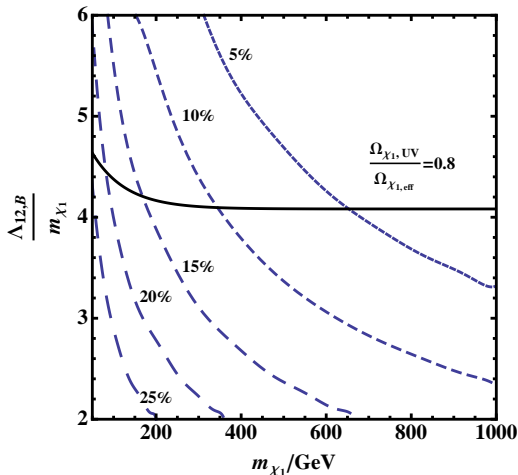
$$\Lambda_{12,B} = \Lambda_{22,B} = \frac{M_{Z'_B}}{\sqrt{g_B^q g_B^X}} \quad \Lambda_{12,L} = \Lambda_{22,L} = \frac{M_{Z'_L}}{\sqrt{g_L^l g_L^X}}$$

- Direct and indirect detection suppressed.

# Relic Density

The effective annihilation cross section:

$$\frac{1}{(g_{eff}/4)^2} \left[ \sigma_{\chi_1 \bar{\chi}_1} + e^{-\Delta x} (1 + \Delta)^{3/2} \sigma_{\chi_1 \bar{\chi}_2} + e^{-2\Delta x} (1 + \Delta)^3 \sigma_{\chi_2 \bar{\chi}_2} \right]$$



$$g_B^q = g_B^\chi = 1$$

$$\Delta = (m_{\chi_2} - m_{\chi_1})/m_{\chi_1}$$

# Constraints on $Z'_L$ and $Z'_B$

$Z'_L$

From di-lepton search at LEP II  $g_L^l \lesssim 0.044 \times (m_{Z'_L}/200\text{GeV})$

$Z'_B$

- Dijet search at hadron colliders
- Limits weakened by decays to dark sector.

$$g_B^q < g_{B,max}^q \frac{1}{\sqrt{Br(Z'_B \rightarrow jj)}}$$

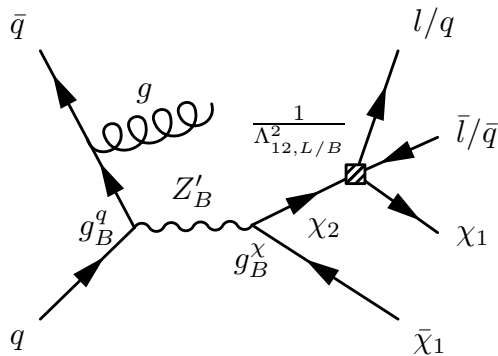
Limits are not saturated in our analysis.

$$g_{L,max}^l - g_L^l = 0.01$$

$$g_{B,max}^q - g_B^q = 0.1$$

# Collider Search

- $\Delta \lesssim 0.3$  leads to soft momenta and small MET.
- Almost back to back  $\chi_1$  pair.
- Irreducible background  $Z + j$ .
- Hard jet from ISR needed to break the back-to-back alignment.





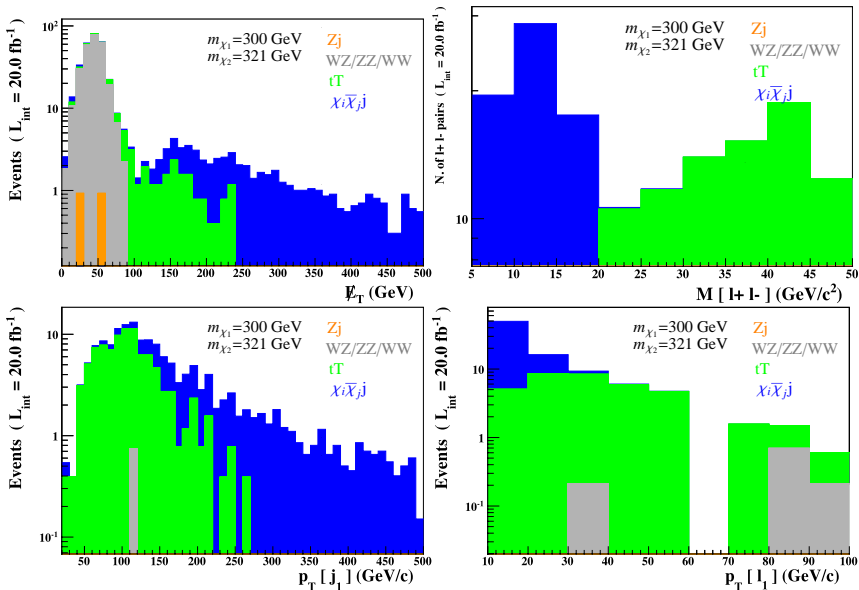
# Dilepton+ $j$ Analysis

- **Trigger:**  $\cancel{E}_T > 120$  GeV
- $p_T(j_1) > 150$  GeV to reduce  $Z + j$  background
- $p_T(l_1) < 30 - 60$  GeV and no  $b$ -jets to reduce  $t\bar{t}$  background

$$m_{\chi_1} = 300 \text{ GeV}, m_{\chi_2} = 321 \text{ GeV}, m_{Z'} = 625 \text{ GeV}$$
$$g_B^q = 0.14, g_B^X = 0.89, g_L^l = 0.045, g_L^X = 0.53$$

Cuts	Signal (S)	Background (B)	Significance ( $S/\sqrt{S + \Delta B}$ )
$p_T(l) > 10$ GeV, $ \eta_{lep}  < 2.5$ , $\Delta R_{l+l^-} > 0.4$ , $\Delta R_{lj} > 0.4$ $M(l+l^-) > 5$ GeV	7520	1062935	0.10
$p_T(j_1) > 150$ GeV	1650	428354	0.04
$\cancel{E}_T > 120$ GeV	1079	22090	0.61
$M(l+l^-) < 20$ GeV	55	85	3.8
$N(b) = 0$	53	38	5.2
$p_T(l_1) < 30$	52	14	6.3

# Histograms



# Other Example Points

example	$m_{\chi_1}$ (GeV)	$m_{\chi_2}$ (GeV)	$m_{Z'_B}$ (GeV)	$g_B^0$	$g_B^\chi$	$m_{Z'_L}$ (GeV)	$g_L^I$	$g_L^\chi$	$\Lambda_I$ (GeV)	$p_T(l_i)$ (GeV)	$M(l^+l^-)$ (GeV)	$\sigma_{pp \rightarrow \bar{\chi}_1 \chi_j}$ 14 TeV (fb)	$\sigma_{pp \rightarrow \bar{\chi}_1 \chi_1 l^+ l^-}$ 14 TeV (fb)
1.	250	270	525	0.15	0.80	250	0.045	0.66	1450	< 30	< 20	6597	552
2.	300	321	625	0.14	0.89	250	0.045	0.53	1620	< 30	< 20	3694	376
3.	400	420	825	0.18	0.68	250	0.045	0.32	2080	< 30	< 20	905	102
4.	600	612	1700	0.23	0.98	250	0.045	0.15	3000	< 20	< 15	442	52
5.	400	432	1375	0.21	2.2	550	0.11	0.8	1840	< 60	< 30	2285	186
6.	500	530	1500	0.18	1.83	550	0.11	0.52	2300	< 60	< 30	1103	104
7.	600	630	1475	0.16	1.61	550	0.11	0.36	2760	< 40	< 30	852	70
8.	700	728	1425	0.12	1.51	550	0.11	0.26	3220	< 30	< 30	193	16

Example #	$\mathcal{L}$ at $s = 14$ TeV	Signal (S)	Background (B)	$S/B$	$S/\sqrt{S + \Delta B}$
1.	$\mathcal{L} = 20 \text{ fb}^{-1}$	67	14	4.8	7.4
2.	$\mathcal{L} = 20 \text{ fb}^{-1}$	52	14	3.7	6.3
3.	$\mathcal{L} = 200 \text{ fb}^{-1}$	106	137	0.77	5.1
4.	$\mathcal{L} = 300 \text{ fb}^{-1}$	23	41	0.56	2.6
5.	$\mathcal{L} = 20 \text{ fb}^{-1}$	159	93	1.7	8.6
6.	$\mathcal{L} = 20 \text{ fb}^{-1}$	81	93	0.87	5.0
7.	$\mathcal{L} = 20 \text{ fb}^{-1}$	51	63	0.80	4.1
8.	$\mathcal{L} = 300 \text{ fb}^{-1}$	114	538	0.21	1.9

# A $Z_3$ Model

- Both fermions and scalars in the dark sector
- Semi-annihilation
- Sommerfeld enhancement
- Non-trivial collider signature: disappearing tracks

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# Summary

- Dark matter exists but its particle nature is behind the veil.
- EFT combines constraints from different experiments easily.
- Its validity is questioned when EFT breaks down or relic density is not populated right.
- Beyond EFT, **simplified models** are able to handle all these problems.