

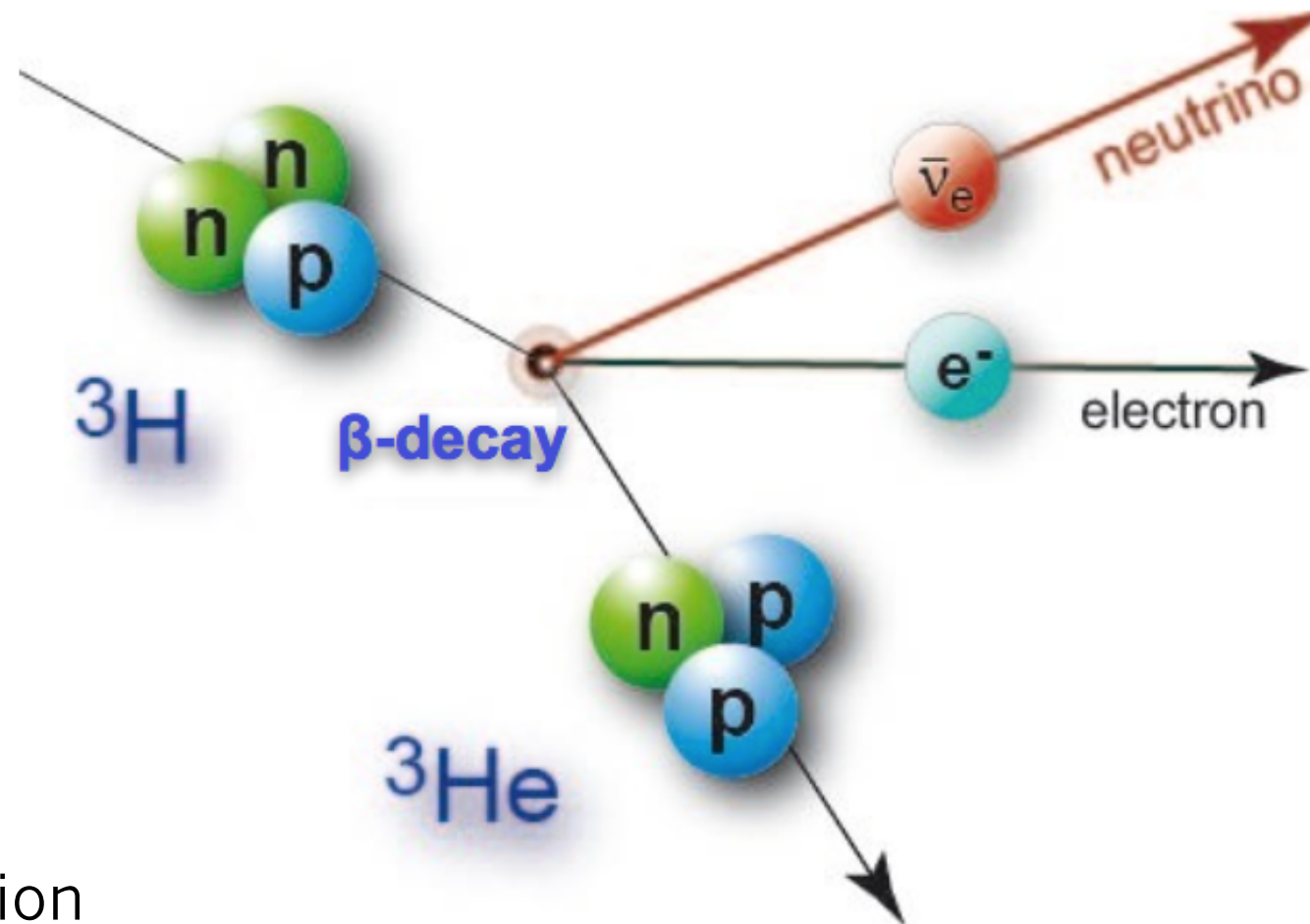
Project 8

Towards a radio-frequency measurement of the neutrino mass

Sebastian Böser

Gentner Kolloquium | MPIK Heidelberg | January 31st 2024

β -decay of tritium



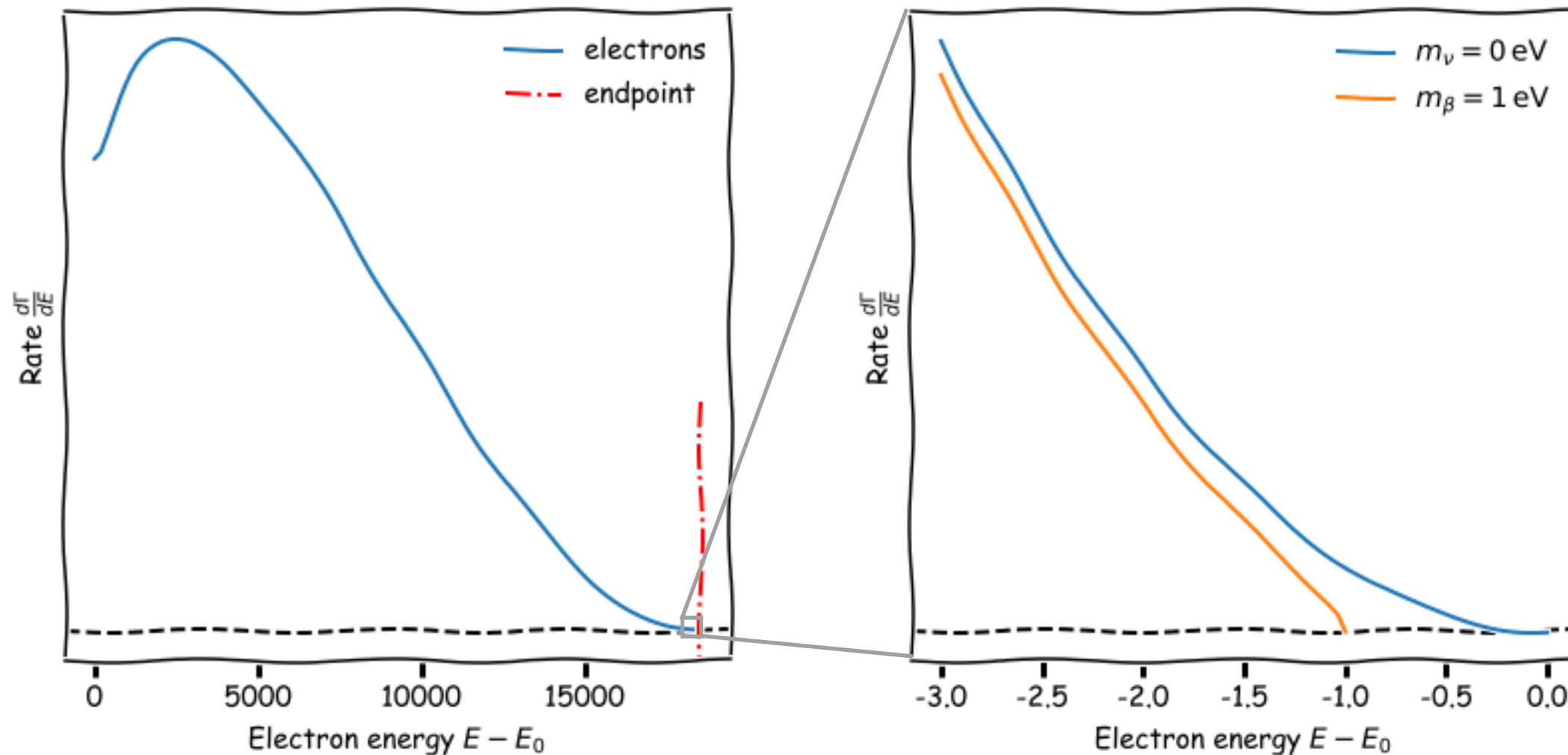
Energy conservation

- sum of rest masses and kinetic energy
 - initial mass of ${}^3\text{H}$ nucleus

Momentum conservation

- electron energy maximal when neutrino at rest
 - $p_\nu = 0 \rightarrow$ solve for m_ν

Tritium β -spectrum

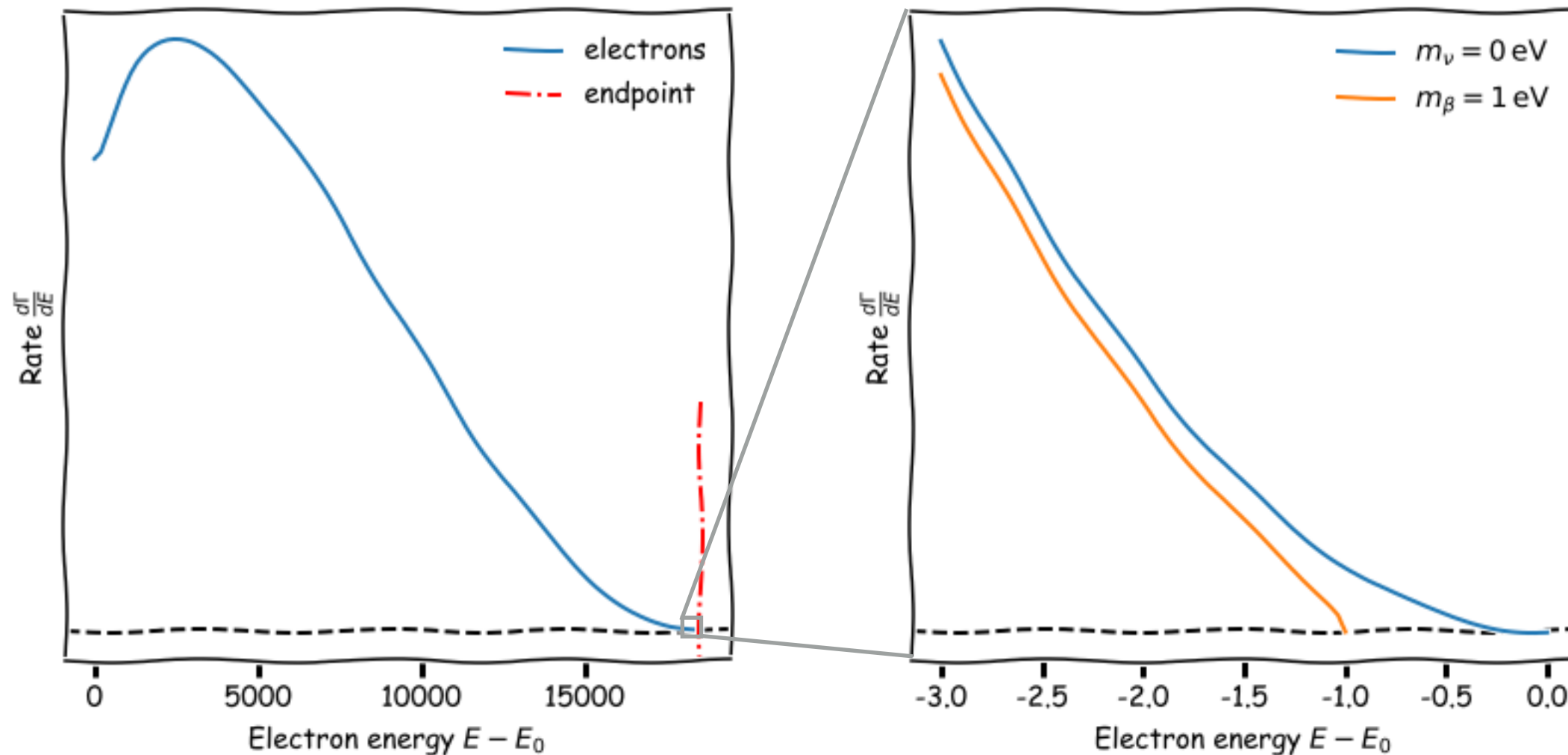


End-point of spectrum depends on neutrino mass

$$\frac{dN}{dE} \sim F(Z, E) p_e(E + m_e) \sqrt{(E - E_0)^2 - m_\beta^2}$$

- direct measurement of *electron* neutrino mass m_β

Tritium β -spectrum



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► direct measurement of electron neutrino mass m_β ???

Mass of the electron neutrino ?!?

Electron neutrino

- super-position of mass eigenstates

$$|\nu_e\rangle = \sum_i^{n_\nu} U_{ei} |\nu_i\rangle$$

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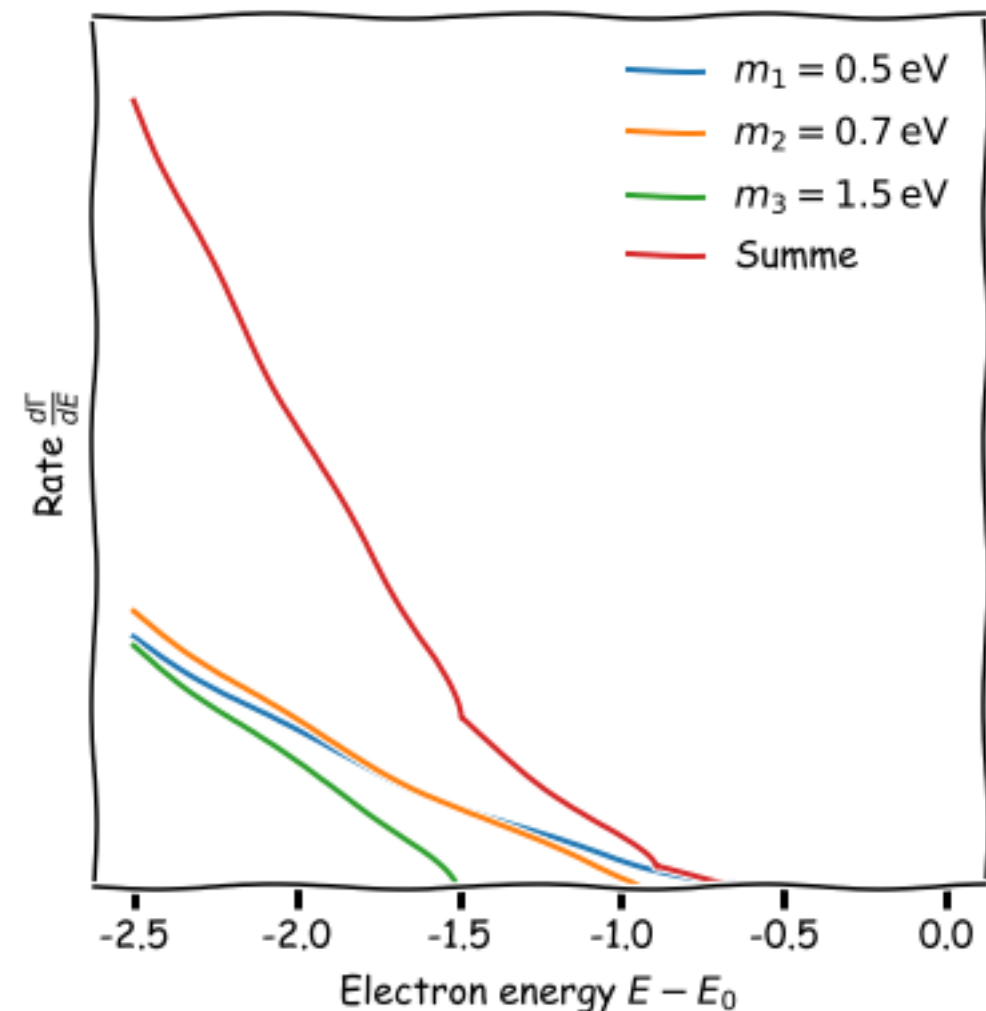
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Kinematik of β -decay

- energy- & momentum conservation
 - ▶ only apply to mass eigenstates
- kinks in the spectrum



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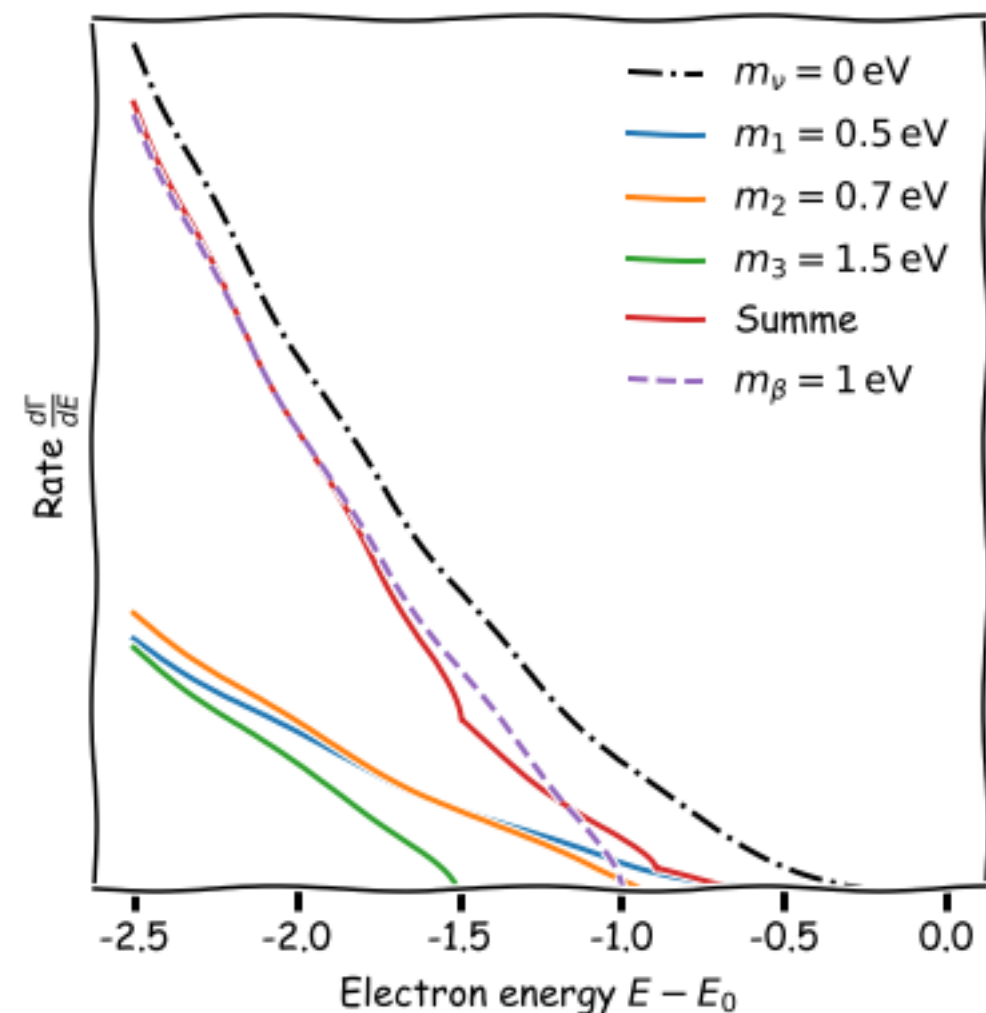
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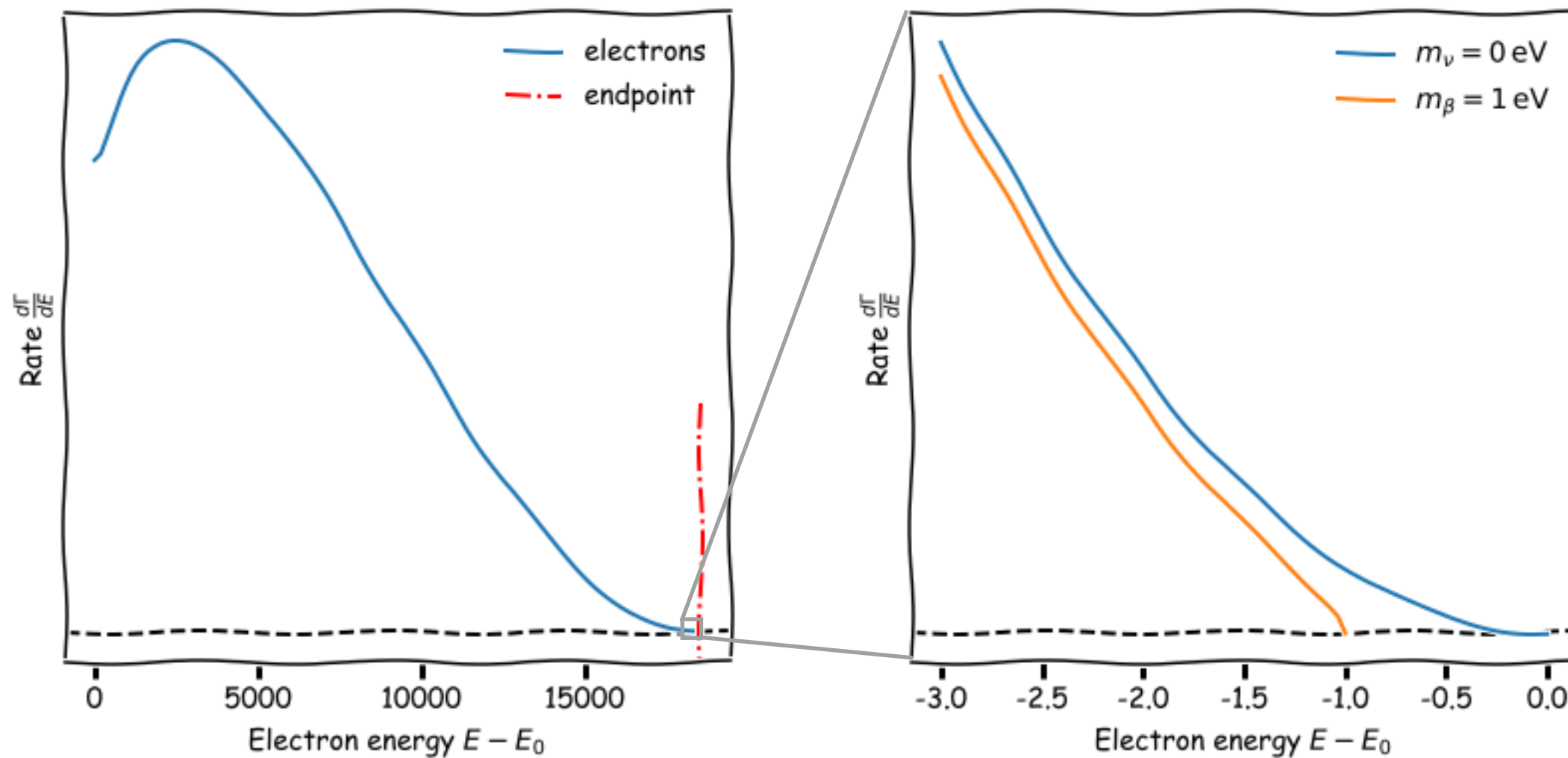
Experimental resolution

- not sufficient
 - ▶ define effective neutrino mass

$$m_\beta^2 = \sum_i^{n_\nu} |U_{ei}|^2 m_i^2$$



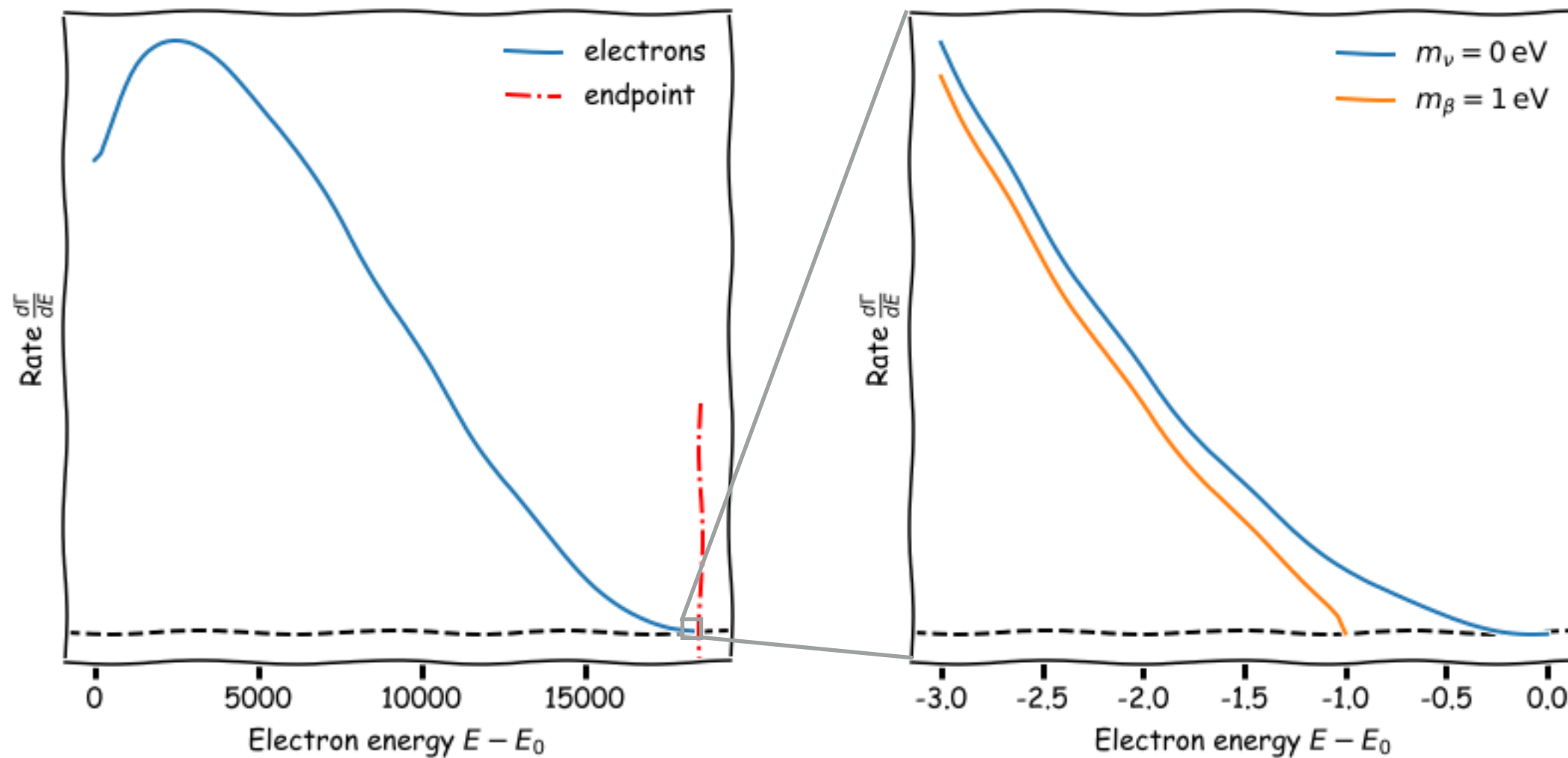
β -decay experiment



Fraction of electrons
in range of interest

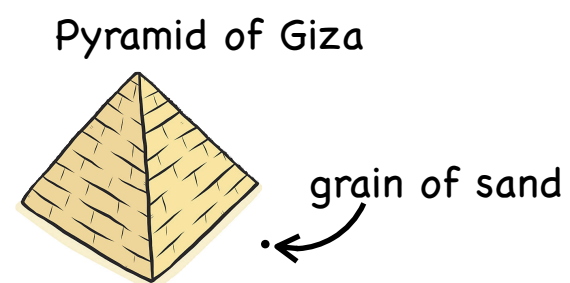
- last 10eV: $2 \cdot 10^{-10}$
- last 1eV: $2 \cdot 10^{-13}$

β -decay experiment

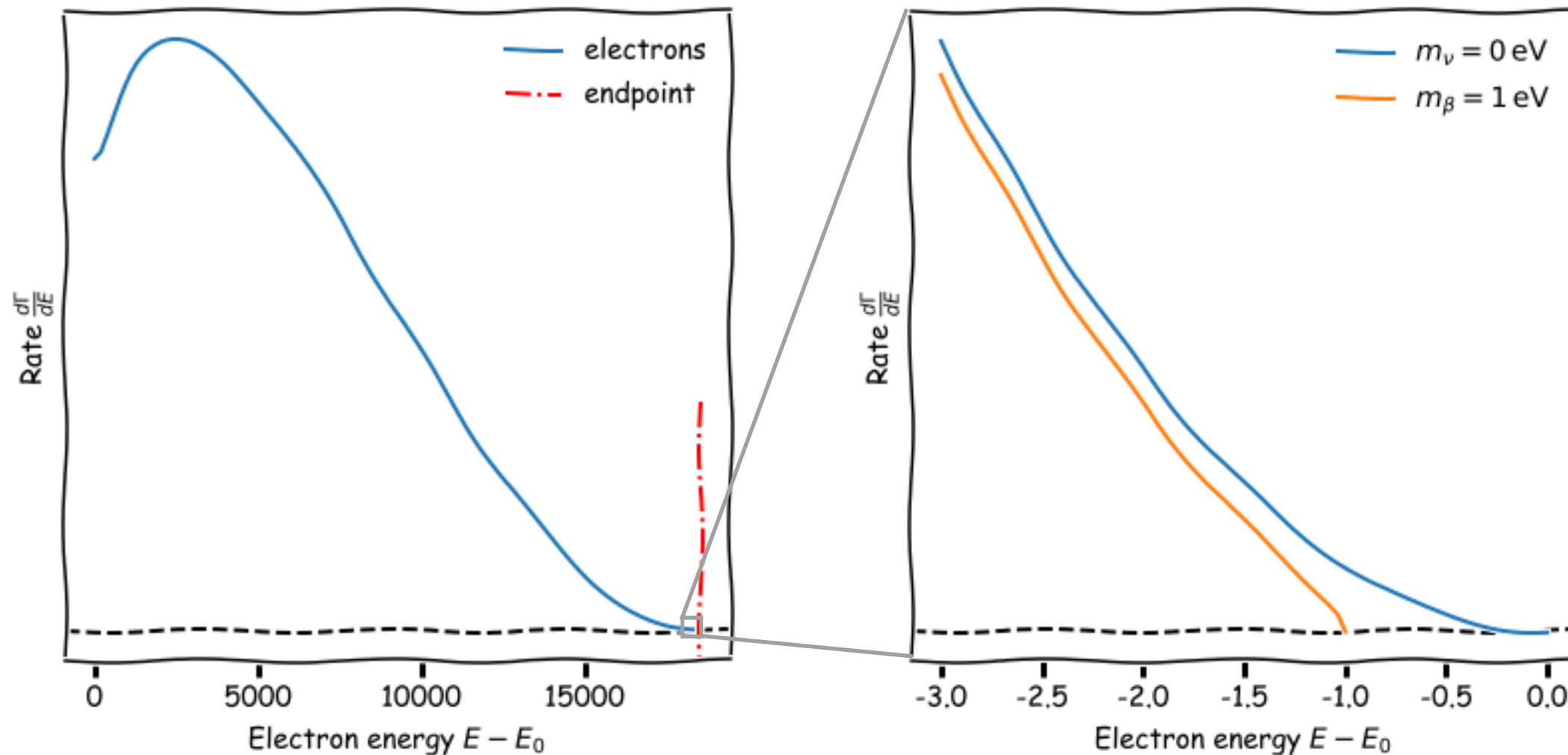


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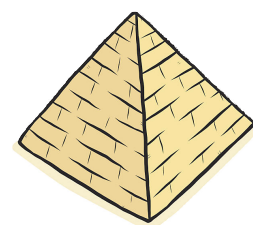
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Pyramid of Giza

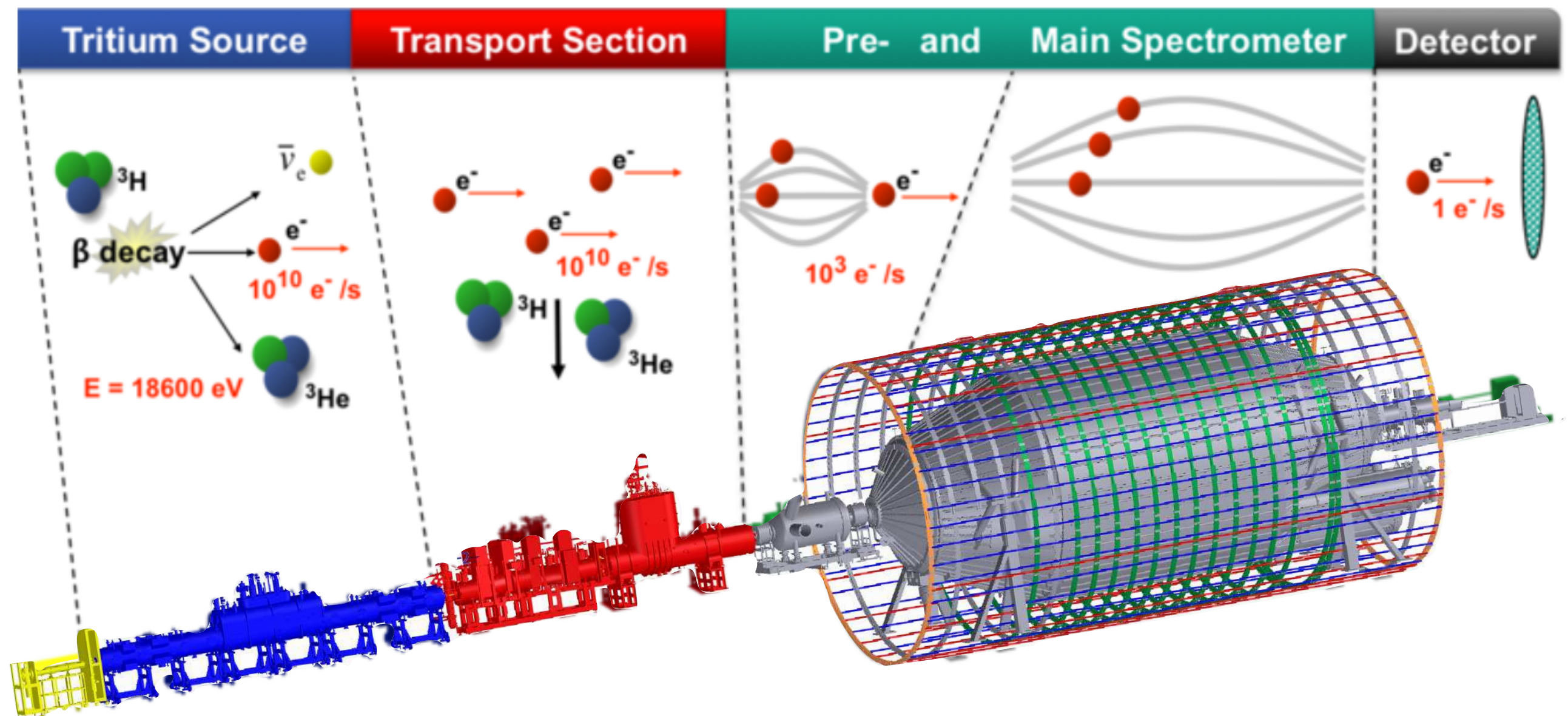


grain of sand

Experimental requirements

- extremely high **statistics**
- very good energy **resolution**

State of the art — KATRIN



Key components

- windowless gaseous tritium source (T_2) → statistic
- MAC-E spectrometer (10m diameter!) → resolution

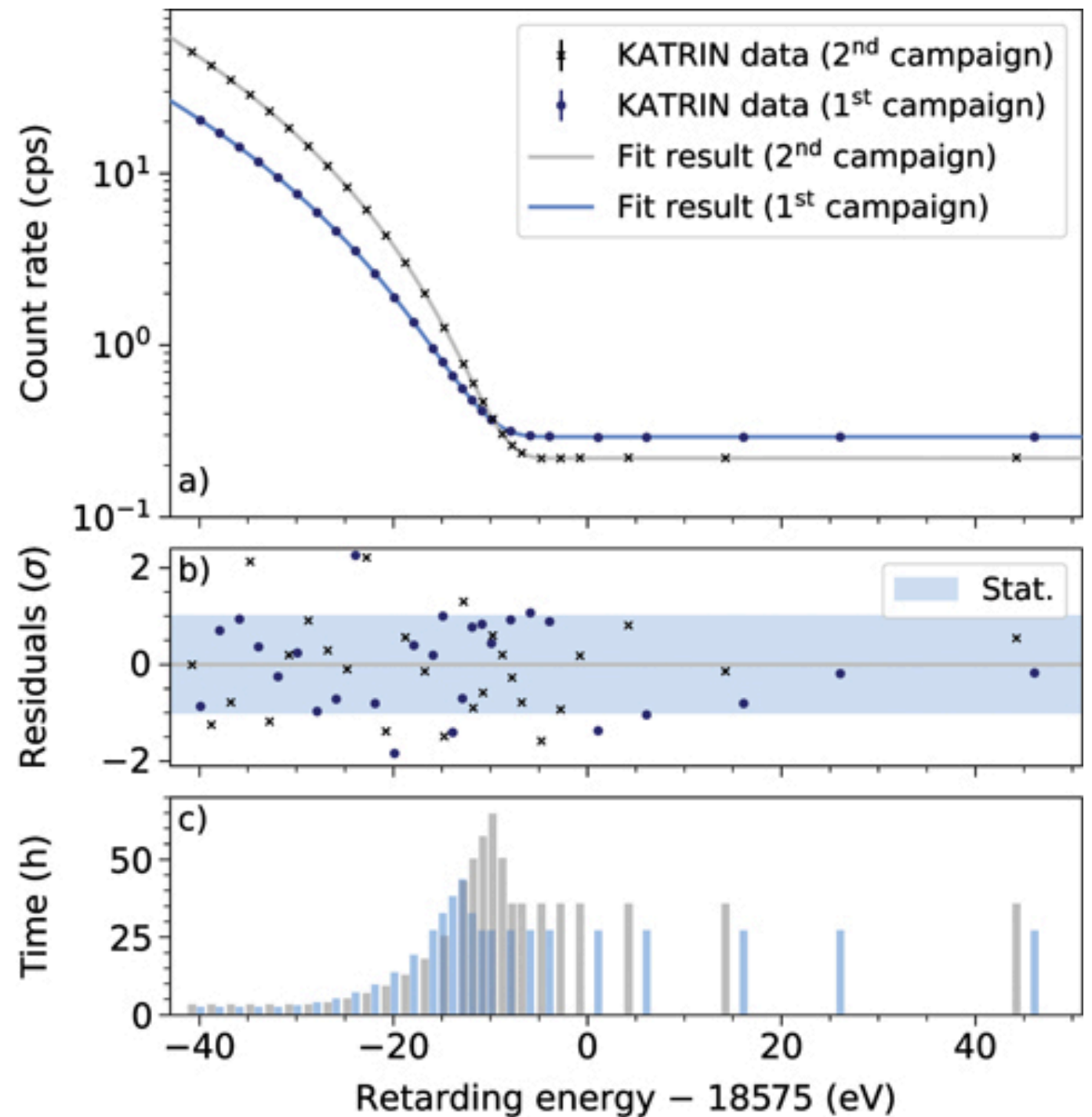
Status — KATRIN limit

Current world-best limit

- Combination of 1st & 2nd campaign results
 - ▶ $m_\beta < 0.8 \text{ eV (90\% CL)}$
- Results from 1st-5th campaign
 - ▶ expected soon
 - ▶ sensitivity to $m_\beta \approx 0.5 \text{ eV (90\% CL)}$

Future

- Expected sensitivity
 - ▶ $m_\beta \approx 0.3 \text{ eV (90\% CL)}$
- Limited by
 - ▶ statistics $\sim$ scales with $N^{-\frac{1}{4}}$
 - ▶ **systematics**
 - ▶ **backgrounds**

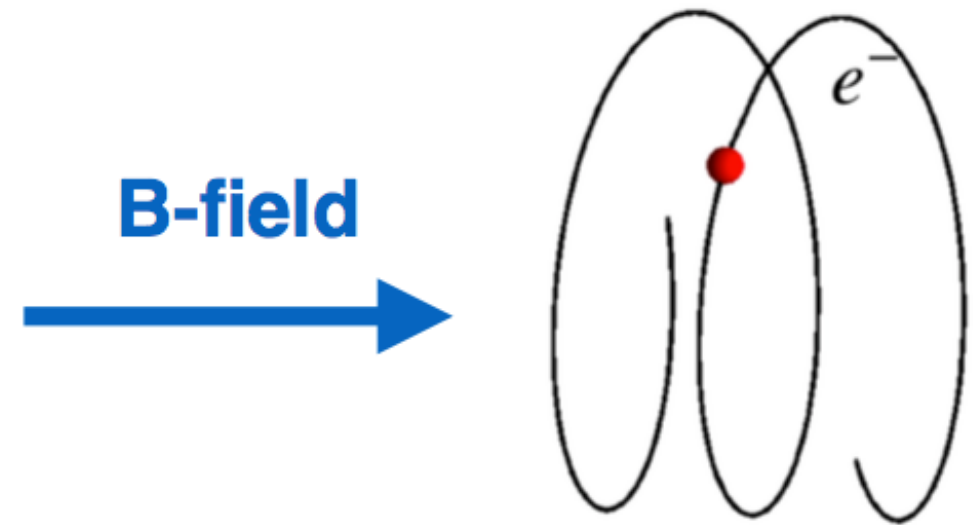


Alternative approach

Electron in B-field

- cyclotron radiation

$$f_c = \frac{1}{2\pi} \frac{eB}{m_e}$$



Alternative approach

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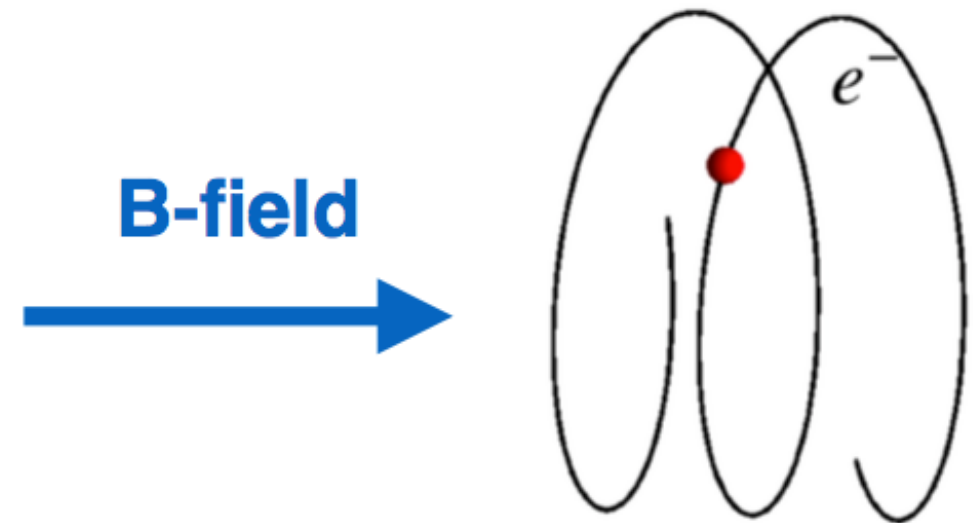
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First-order relativistic correction

$$f_\gamma = \frac{f_c}{\gamma} = \frac{1}{2\pi} \frac{eB}{m_e + E_{\text{kin}}}$$

- energy measurement!



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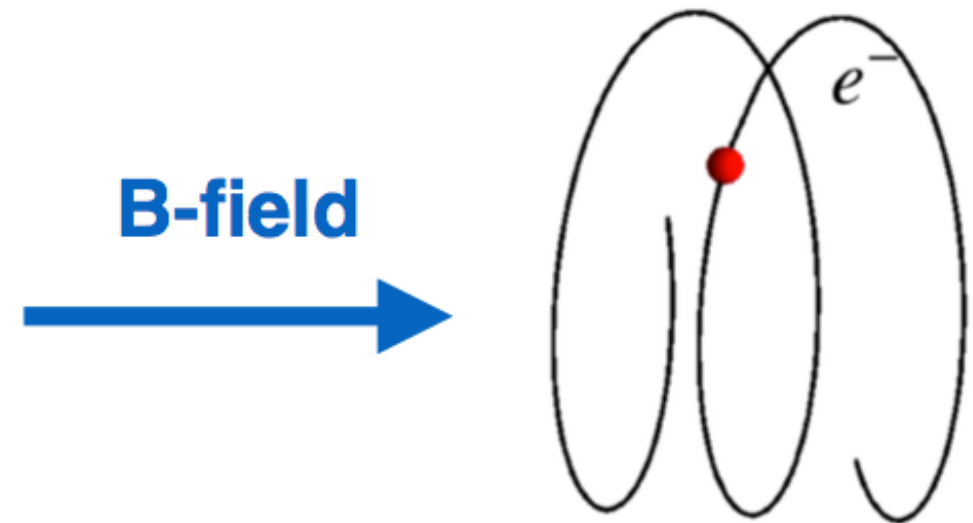
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Energy resolution $\Delta E/E \sim \Delta f/f$

- $\Delta E/E \sim 0.1\text{eV} / 18.6\text{ keV} = 5\text{ppm} \rightarrow \text{easy!}$



"Never measure anything but frequency" — A. L. Schawlow

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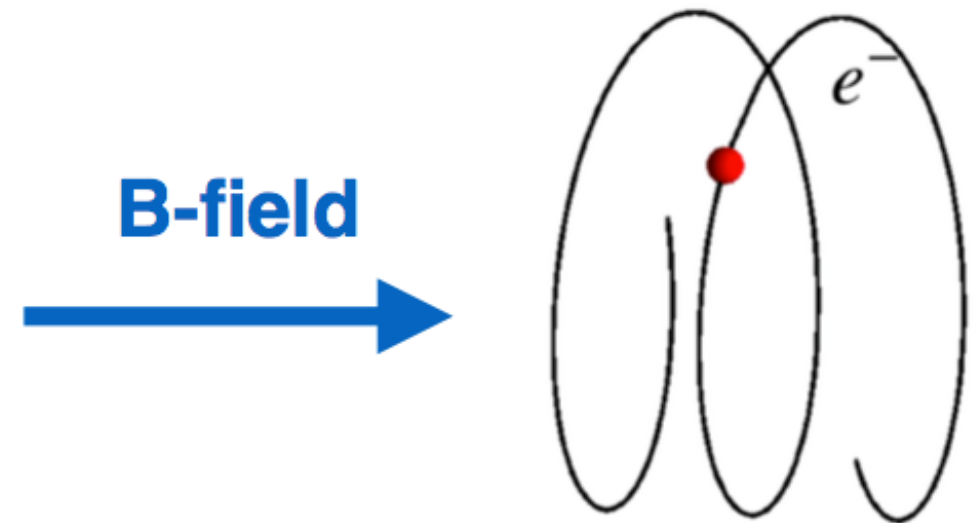
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Frequency resolution $\Delta f \sim 1/\Delta t$

- $\Delta t = 20\mu\text{s} \rightarrow 1400\text{m} @ 18\text{keV} \rightarrow \text{hard!}$

- ▶ store in magnetic trap



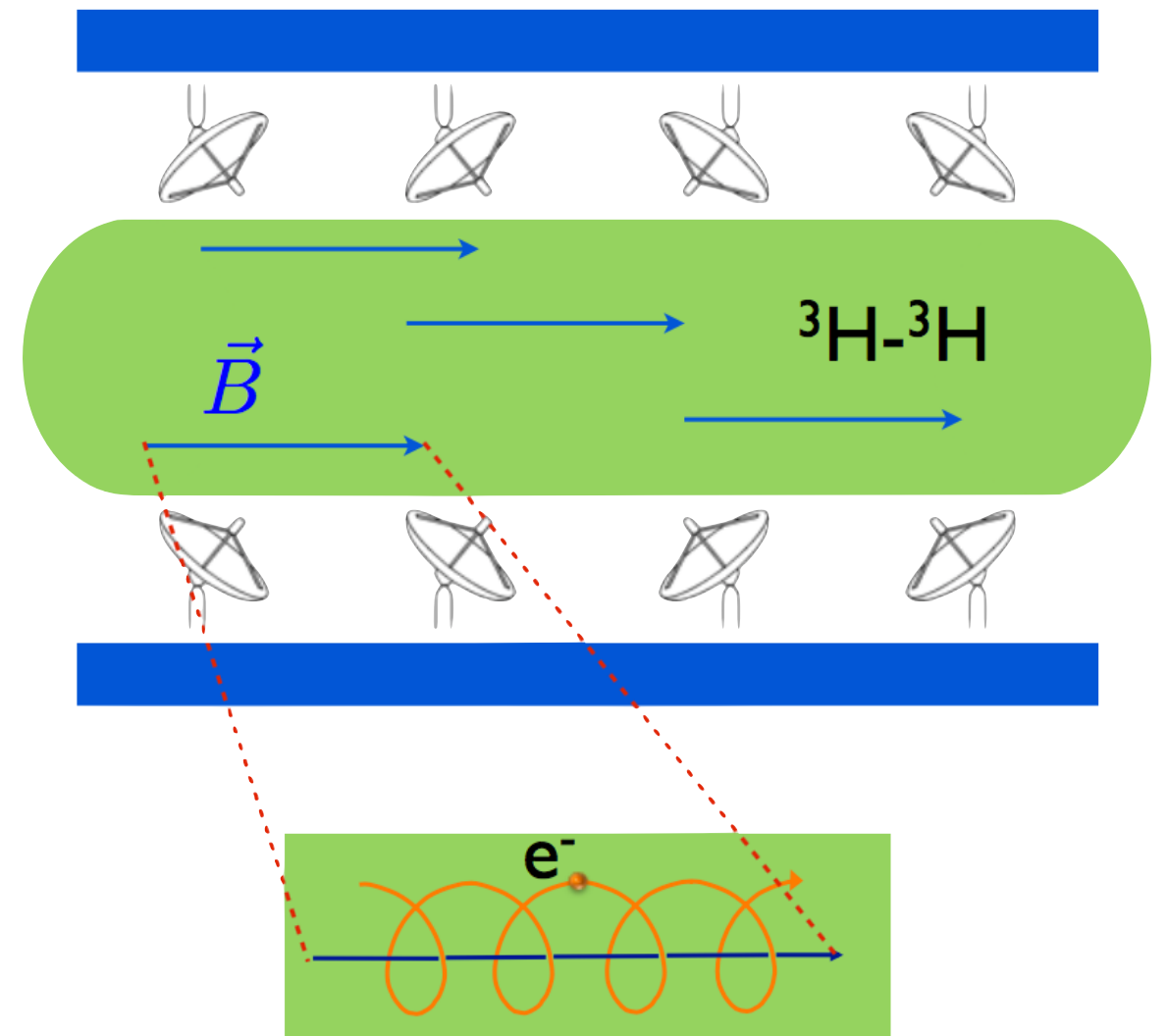
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Experiment

PROJECT 8

Idea

- fill volume with tritium atom gas
- add magnetic field
 - ▶ decay electrons orbit around field lines
- measure cyclotron radiation
 - ▶ electron spectrum

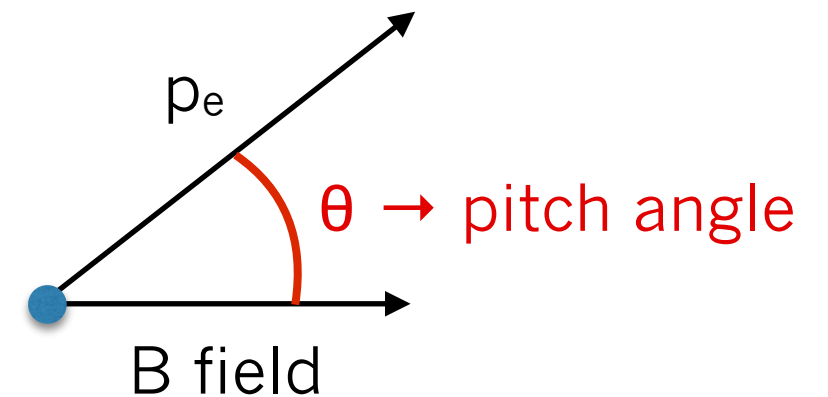


B. Monreal and J. Formaggio, Phys. Rev D80:051301

Radiated power

Larmor formula

$$P(\gamma, \theta) = \frac{1}{4\pi\epsilon_0} \frac{2}{3} \frac{q^4 B^2}{m_e^2} (\gamma^2 - 1) \sin^2 \theta$$



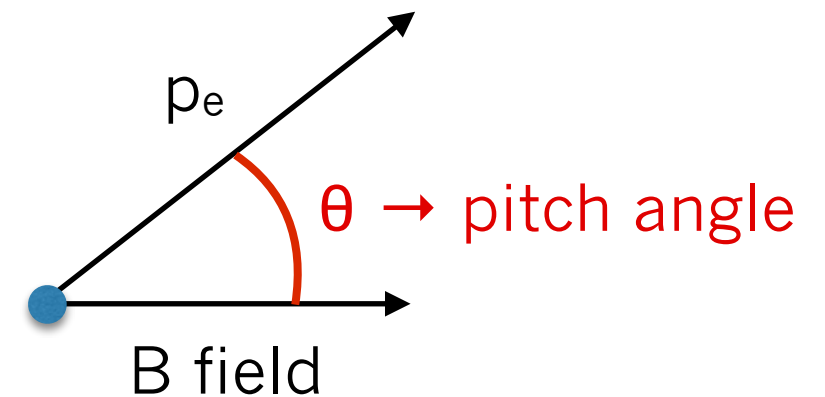
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Radiated power

- 1.1 fW for 18 keV electrons at 90°
- 1.7 fW for 30.4 keV electron at 90°



Radiated power

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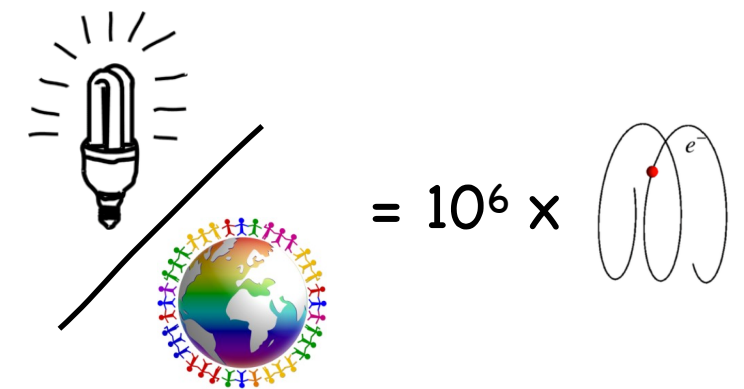
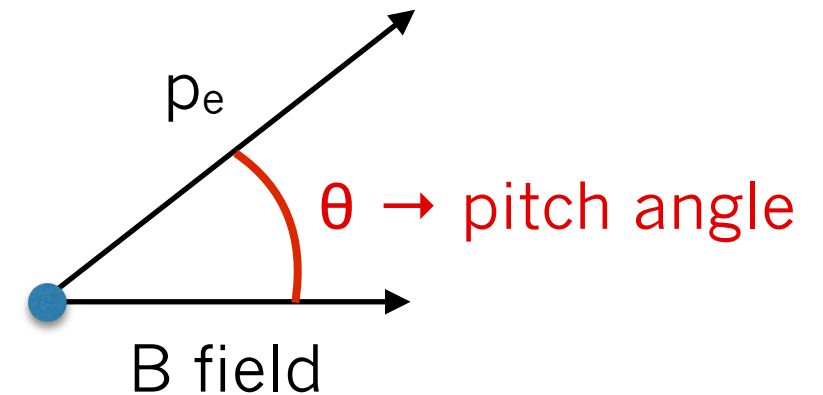
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Comparison

- 10W energy saving light bulb by world population
 - ▶ 10⁶ larger power per person



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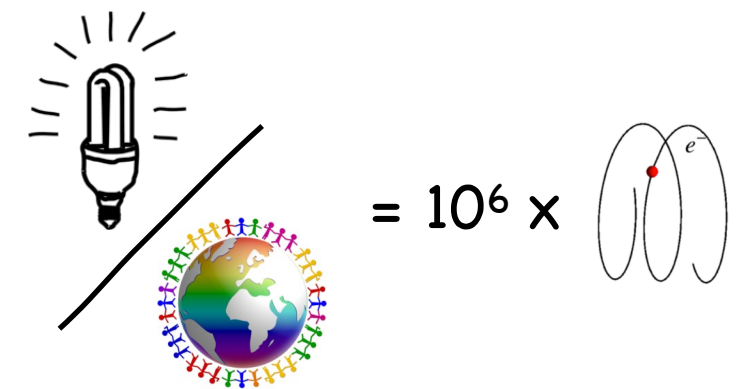
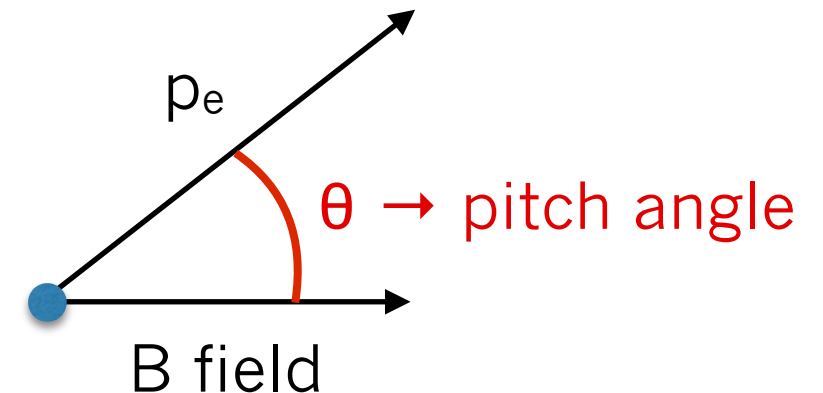
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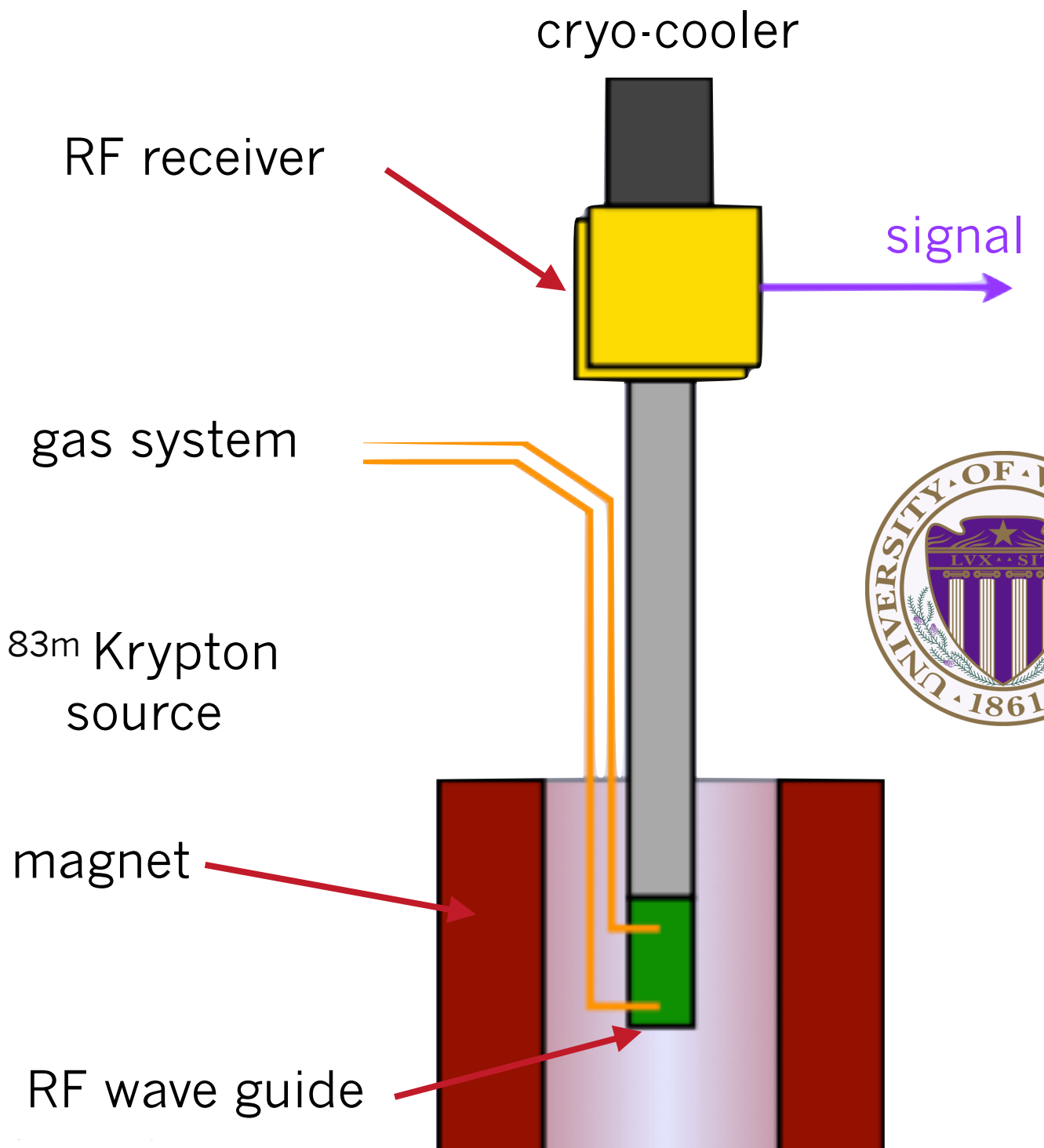
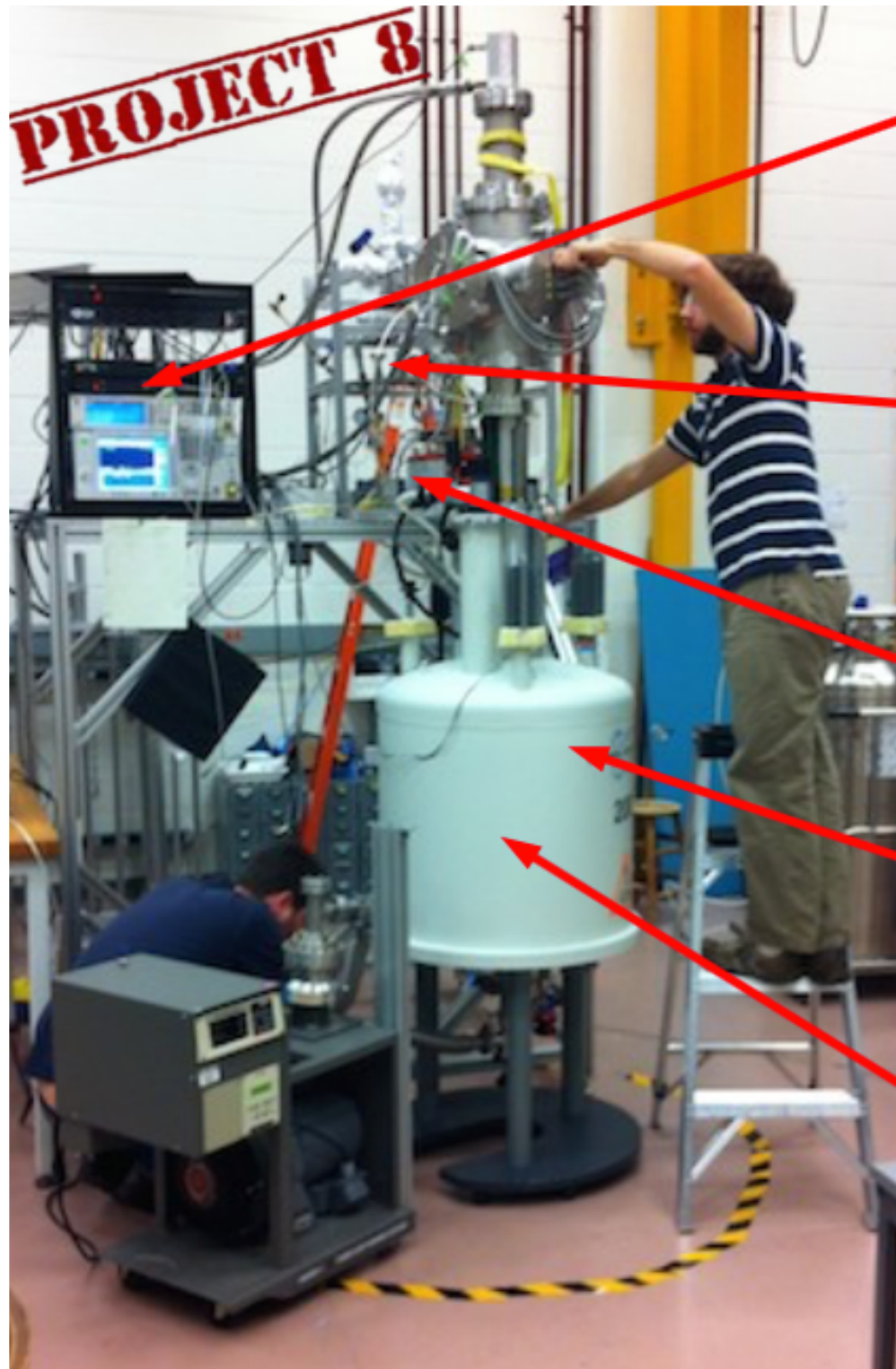
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Consequences

- need very **low-noise** detection system
- see mostly electrons at **very large pitch angle θ**



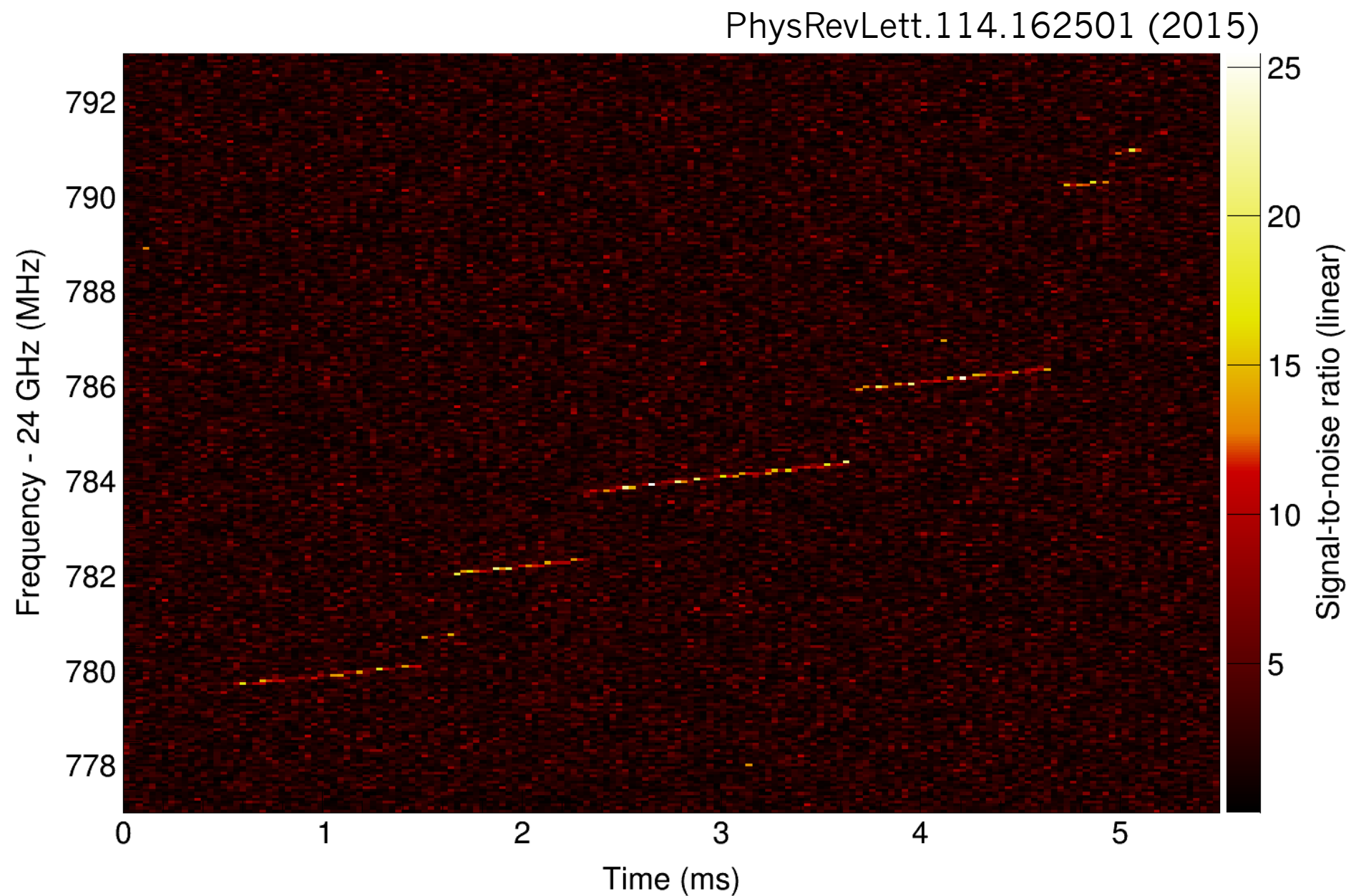
Phase I: apparatus



Measured signal

Begin of data-taking on 06.06.2014

- first signal → captured electron



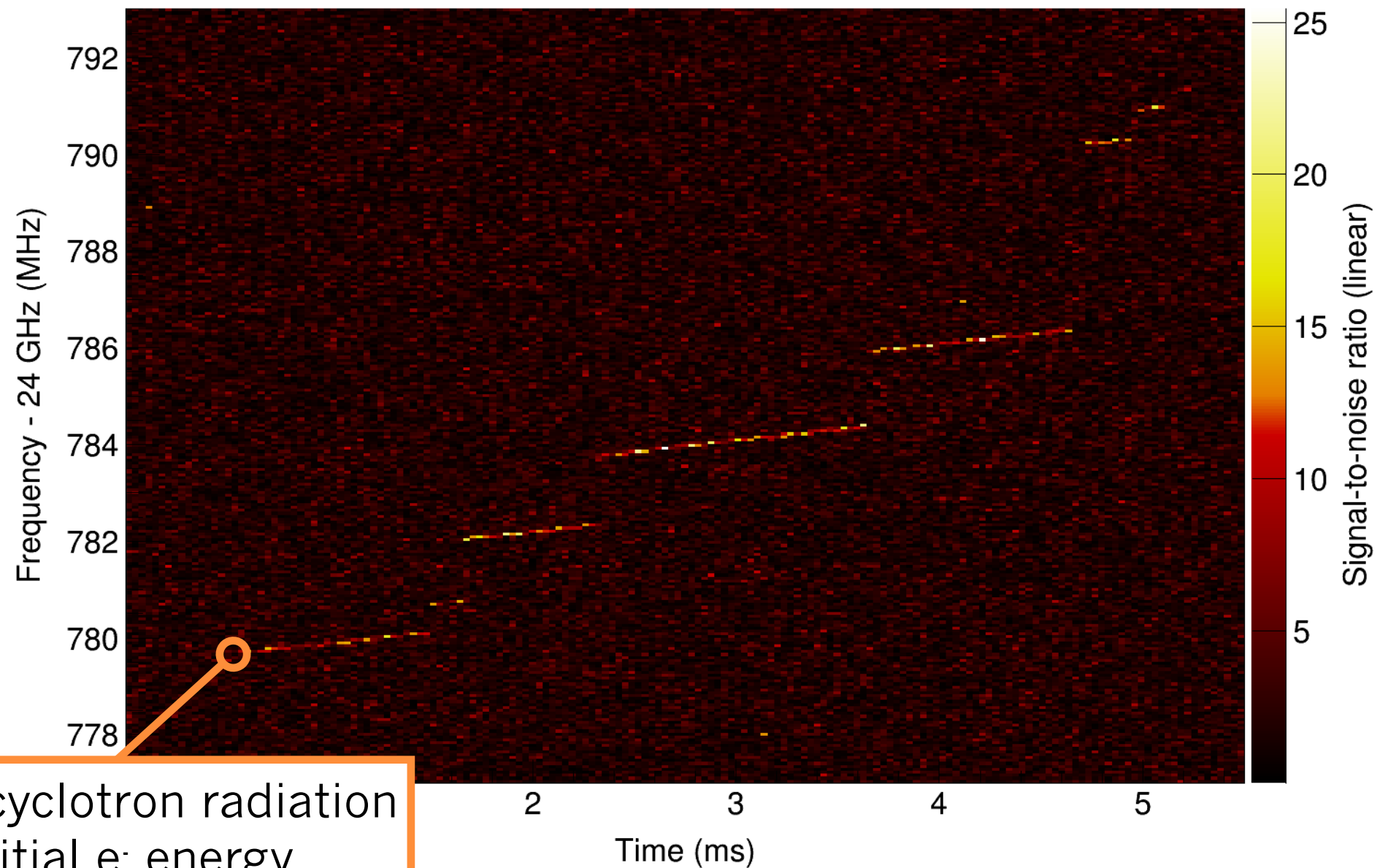
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$$f_{\gamma} = \frac{1}{2\pi} \frac{eB}{m_e + E_{\text{kin}}}$$

PhysRevLett.114.162501 (2015)



Onset of cyclotron radiation
→ initial e⁻ energy

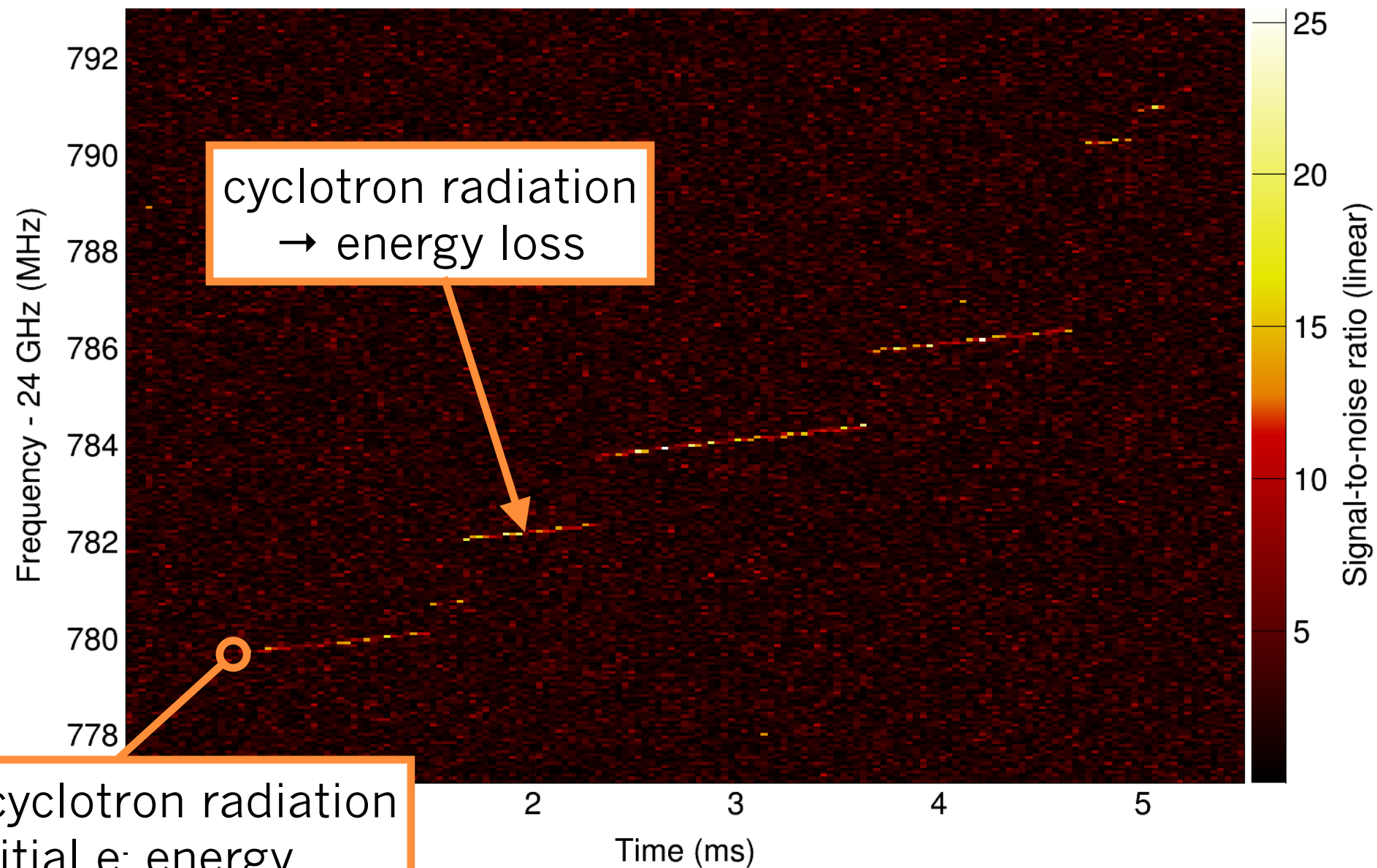
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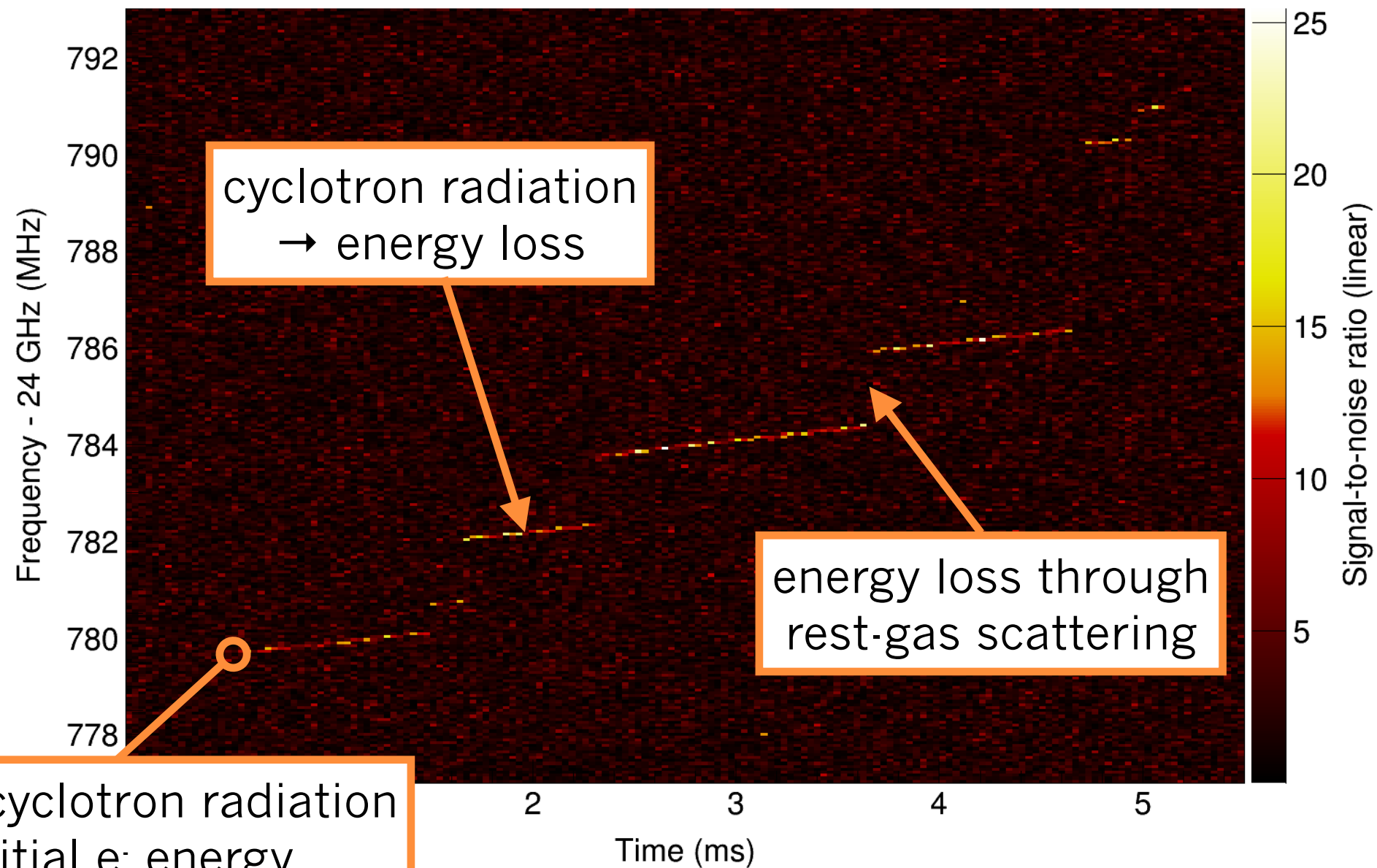
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Phase I: results

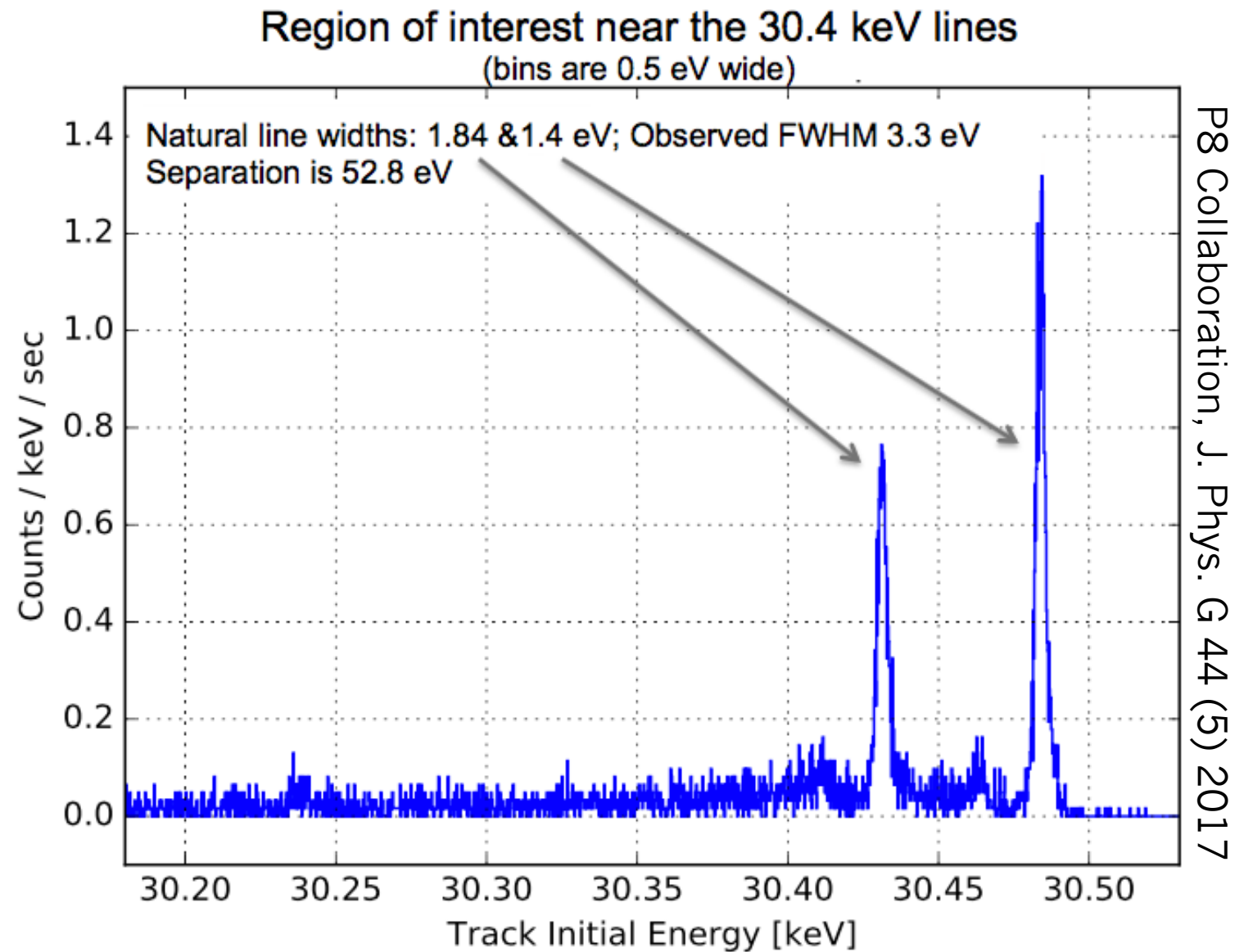
Improved Phase I setup

- more homogeneous B-field
- reduced sensor noise
- improved temperature stability

Achieved resolutions

- $\sigma(E) = 3.3\text{eV}$ @ 30.4keV
- $\sigma(E) = 5.1\text{eV}$ @ 17.8keV

- ▶ new measurement method established



Phase I: results

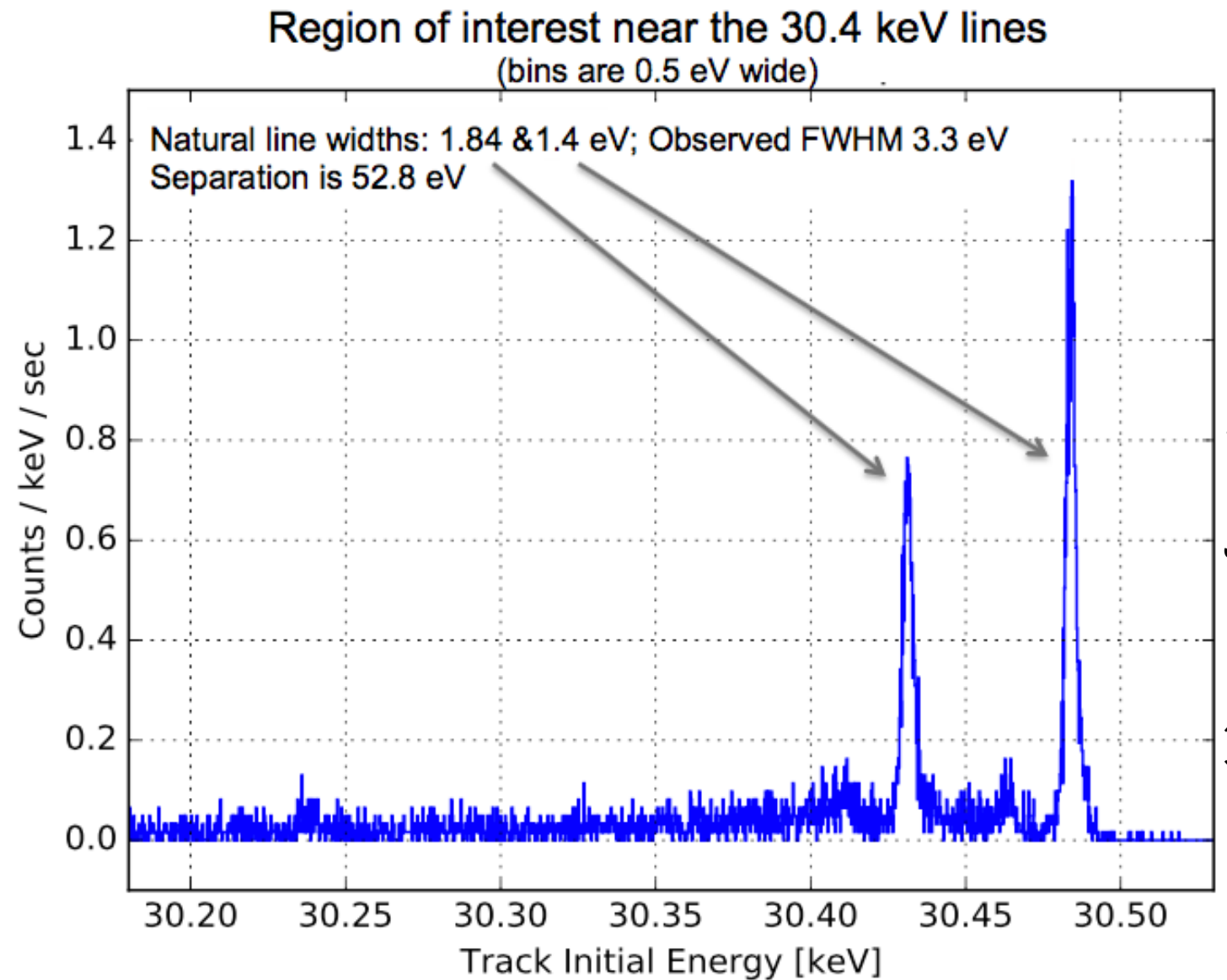
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P8 Collaboration, J. Phys. G 44 (5) 2017

CRES — *Cyclotron Radiation Emission Spectroscopy*

Project Plan (and talk outline)

■ Phase I

- ▶ demonstrate CRES technique ✓

■ Phase II

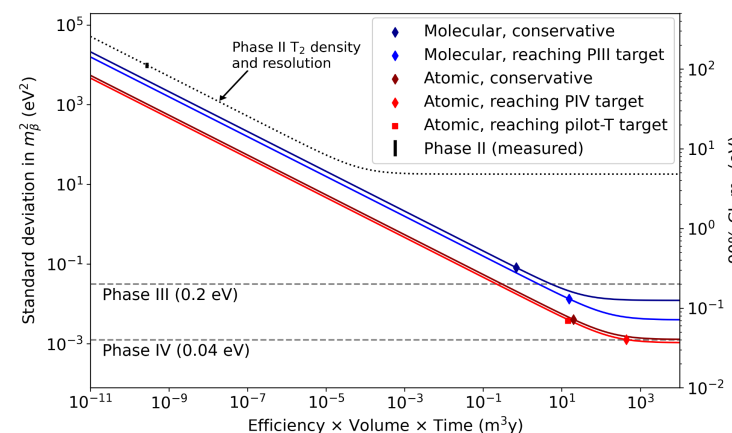
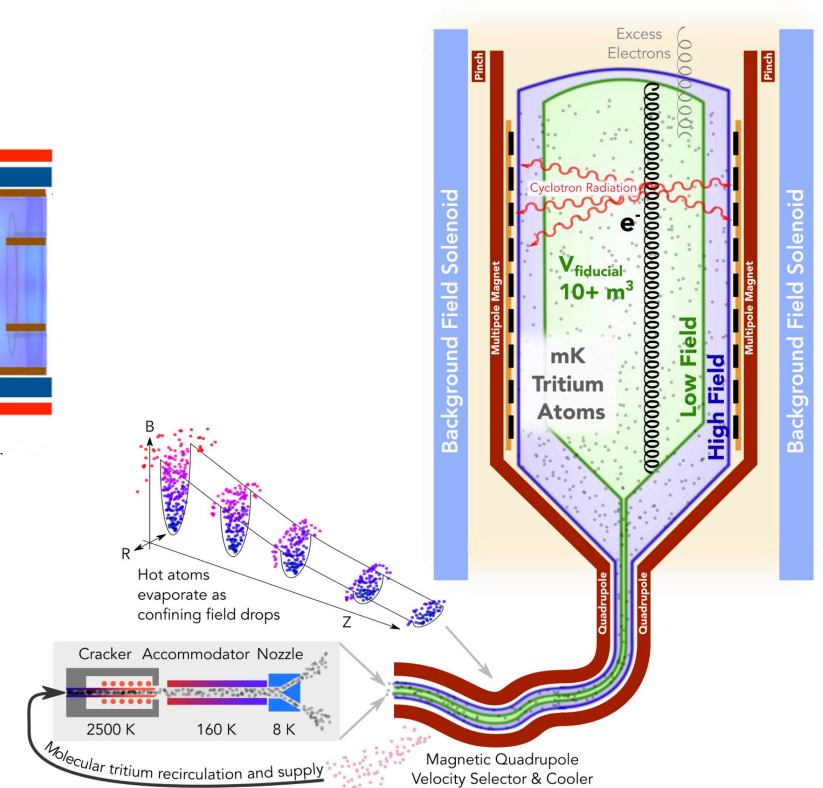
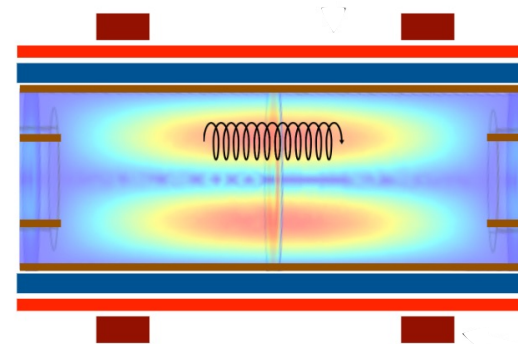
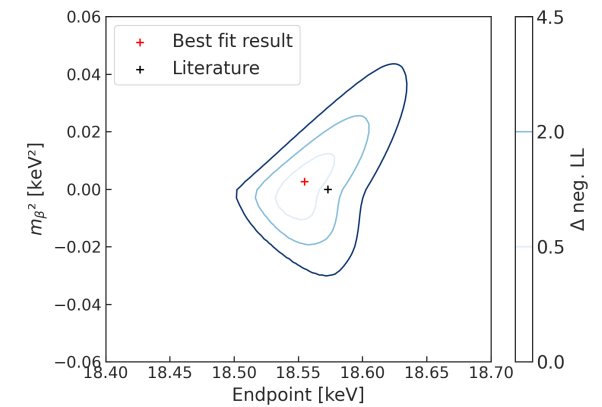
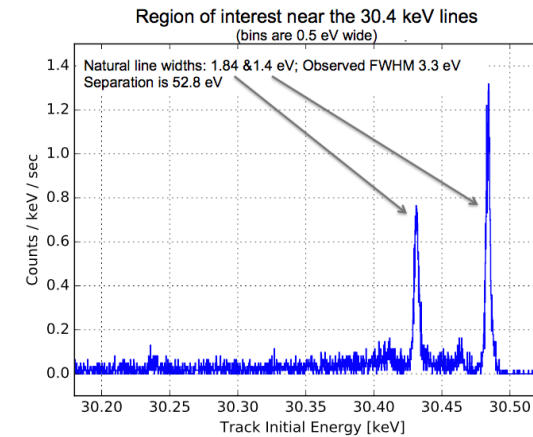
- ▶ first Tritium spectrum with CRES

■ Phase III

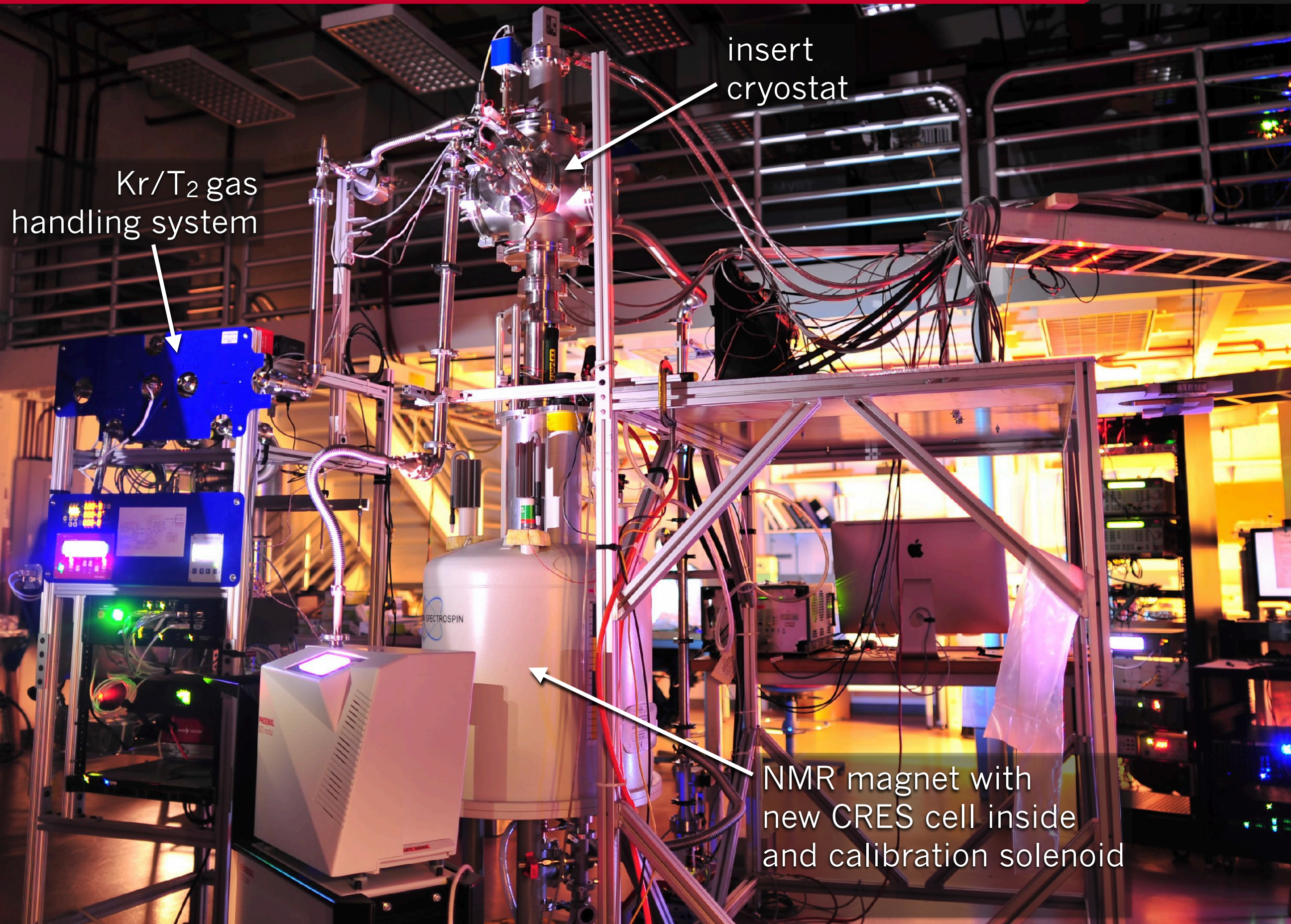
- ▶ Go bigger!
demonstrate large cavity
- ▶ Go atomic!
demonstrate atomic tritium trapping

■ Phase IV

- ▶ full apparatus, reaching $m_\beta < 0.04$ eV sensitivity



Phase II setup



insert
cryostat

Kr/T₂ gas
handling system

NMR magnet with
new CRES cell inside
and calibration solenoid

Phase II: $^{83\text{m}}\text{Kr}$ data

Krypton data taking

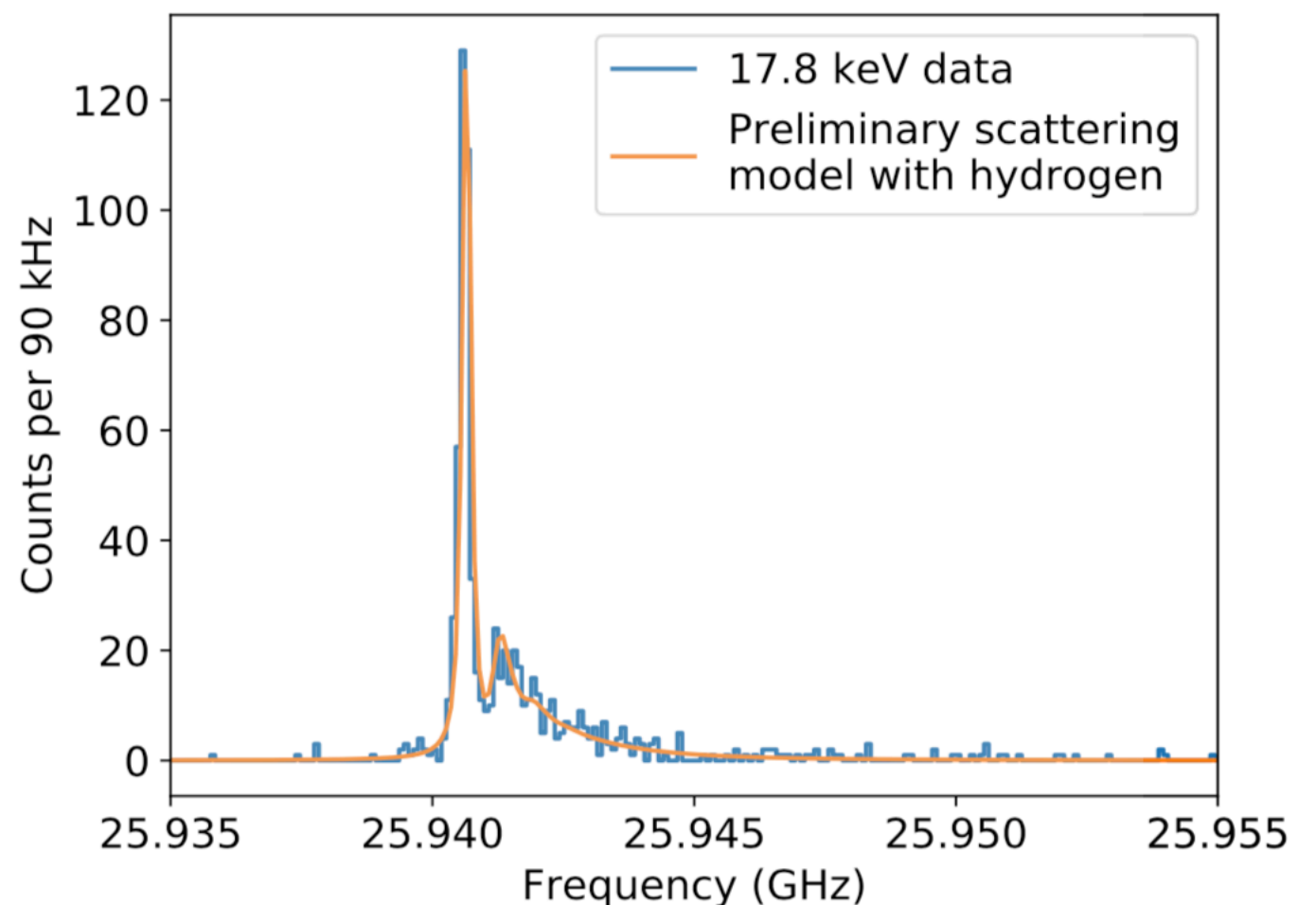
- shallow traps
 - ▶ only retain large pitch angles → low rate
 - ▶ little variation in B field within trap → good energy resolution

Electron scattering

- before detection
 - ▶ low-energy (high-frequency) tail in spectrum

Hydrogen scattering model

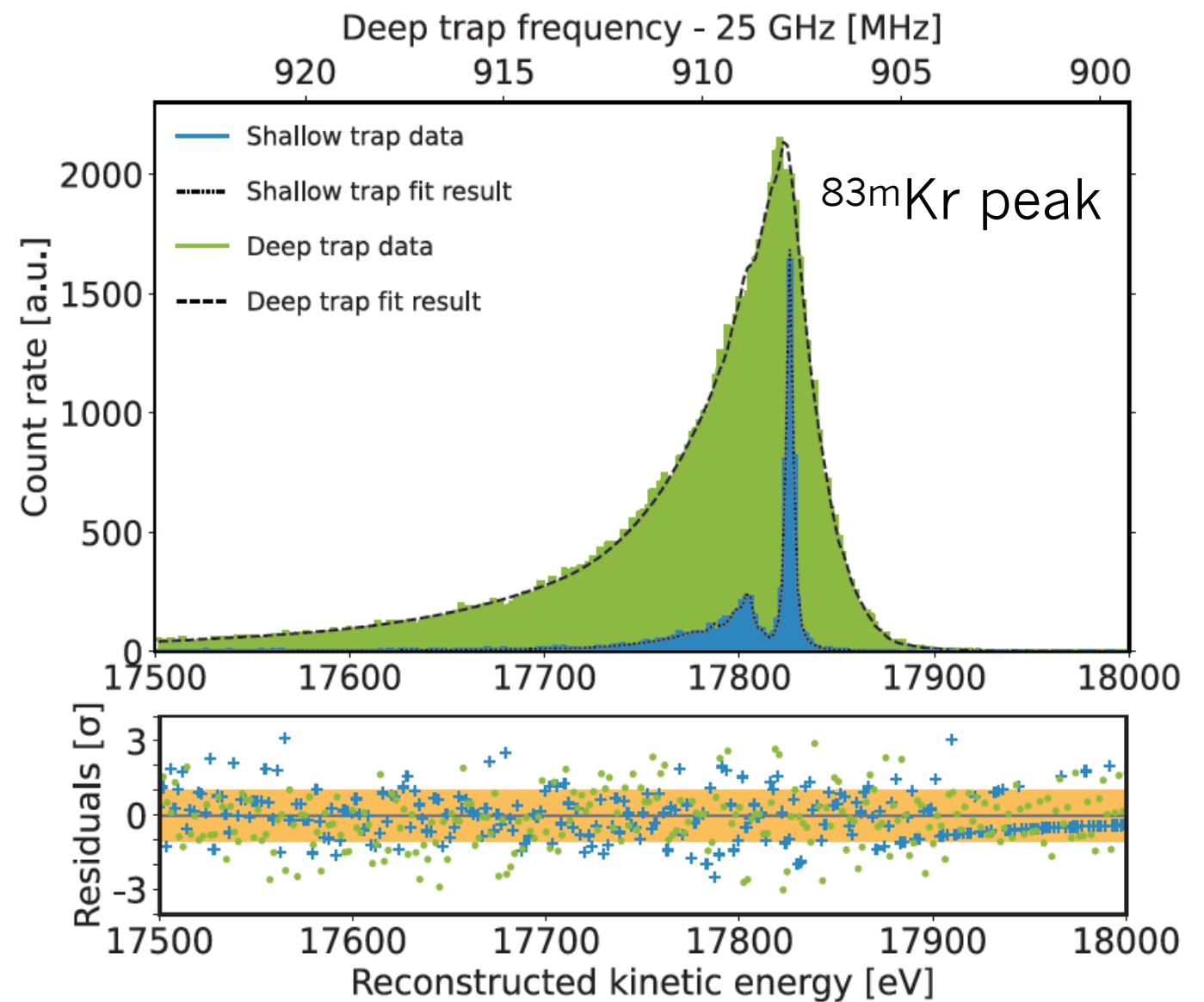
- 4eV FWHM Voigt profile
- 2.84eV line width in $^{83\text{m}}\text{Kr}$
 - ▶ detector resolution surpasses intrinsic line width



Phase II: T₂ data

Tritium data taking

- $6 \cdot 10^4$ longer half-life → dramatically decreased rate
 - ▶ increasing pressure



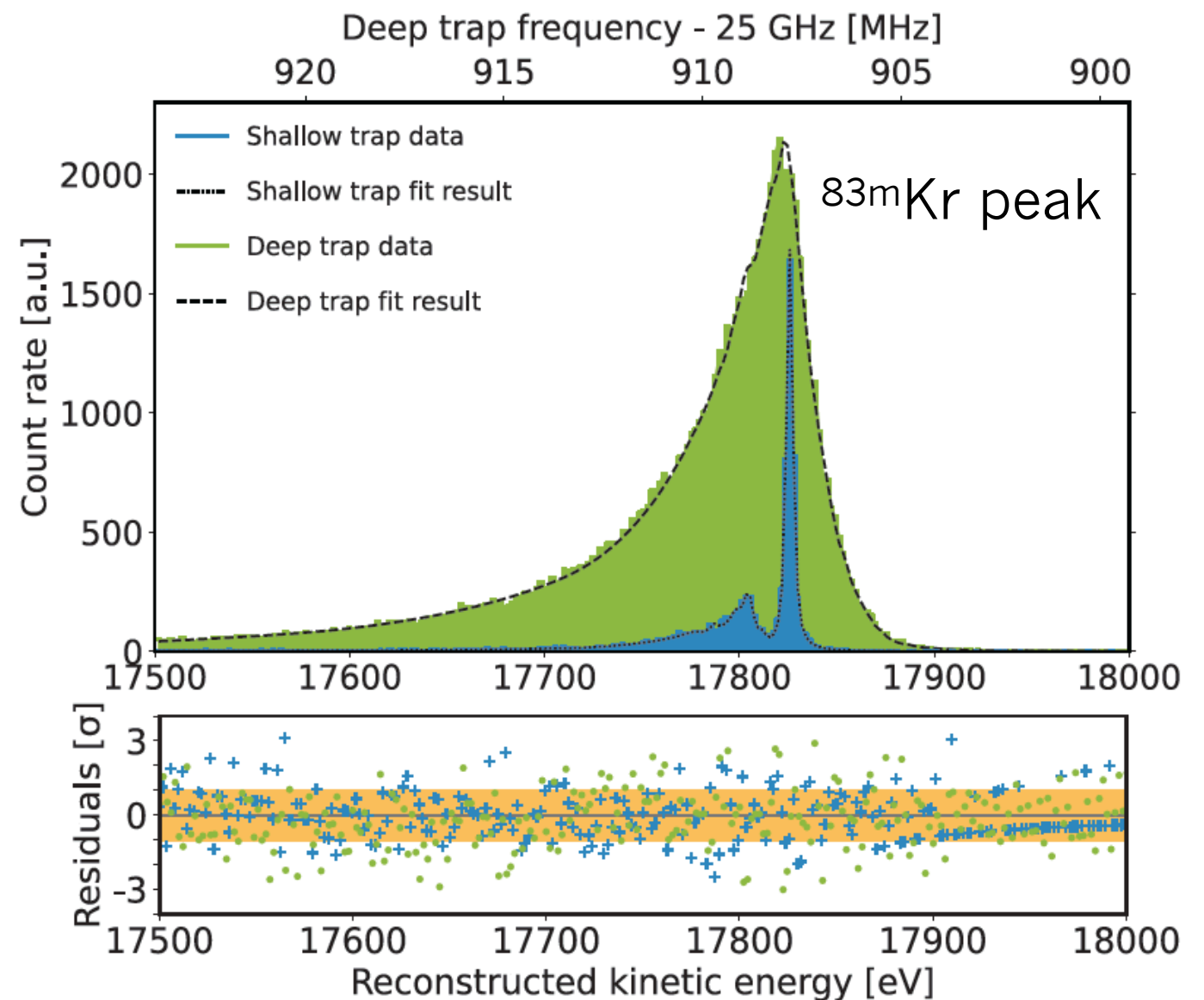
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Tritium configuration

- optimized configuration for best endpoint sensitivity with ~100 days of data
- use deeper trap
 - ▶ better statistics
 - ▶ worse energy resolution
- lineshape still well described by model (gas composition!)



Detection efficiency

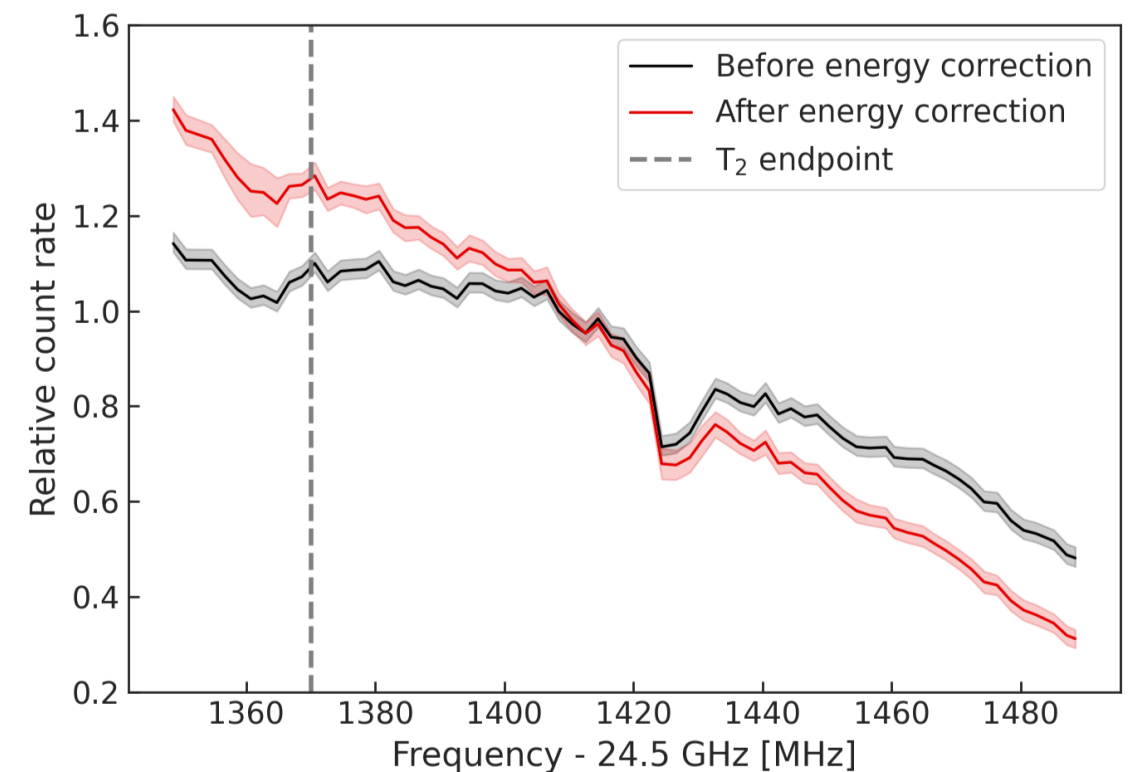
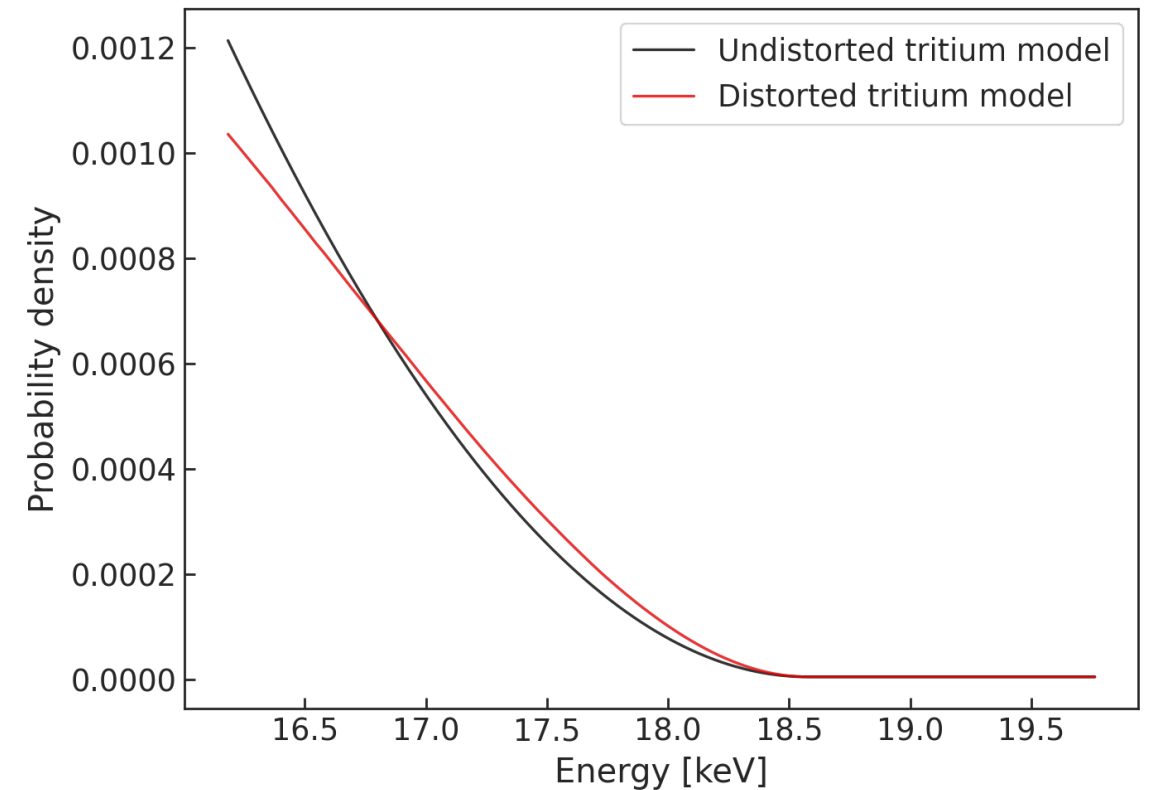
Emitted cyclotron power

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- detection probability is energy ($\rightarrow$ frequency) dependent!
- distorted spectrum
 - impacts neutrino mass analysis

Additional effects

- frequency ($\rightarrow$ energy) dependent effects of waveguide
- frequency ($\rightarrow$ energy) dependent receiver and amplification chain
 - **need calibration over ROI!**



Phase II: Solenoid calibration

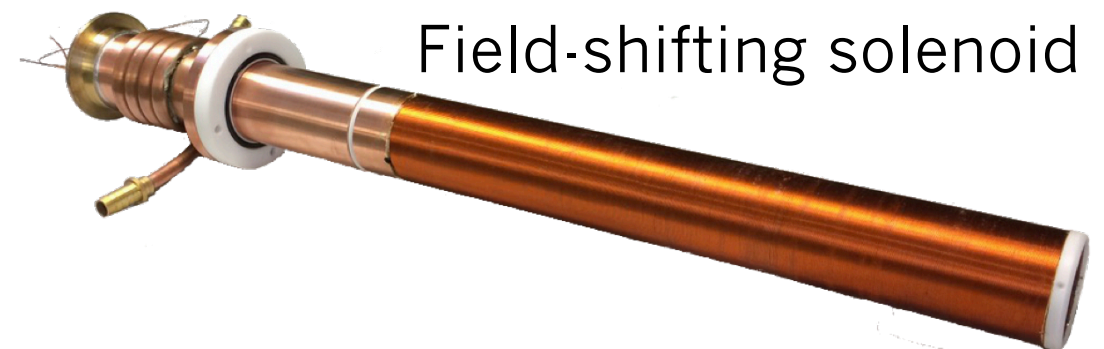
Cyclotron frequency

$$f_c = \frac{1}{2\pi} \frac{eB}{m_e}$$

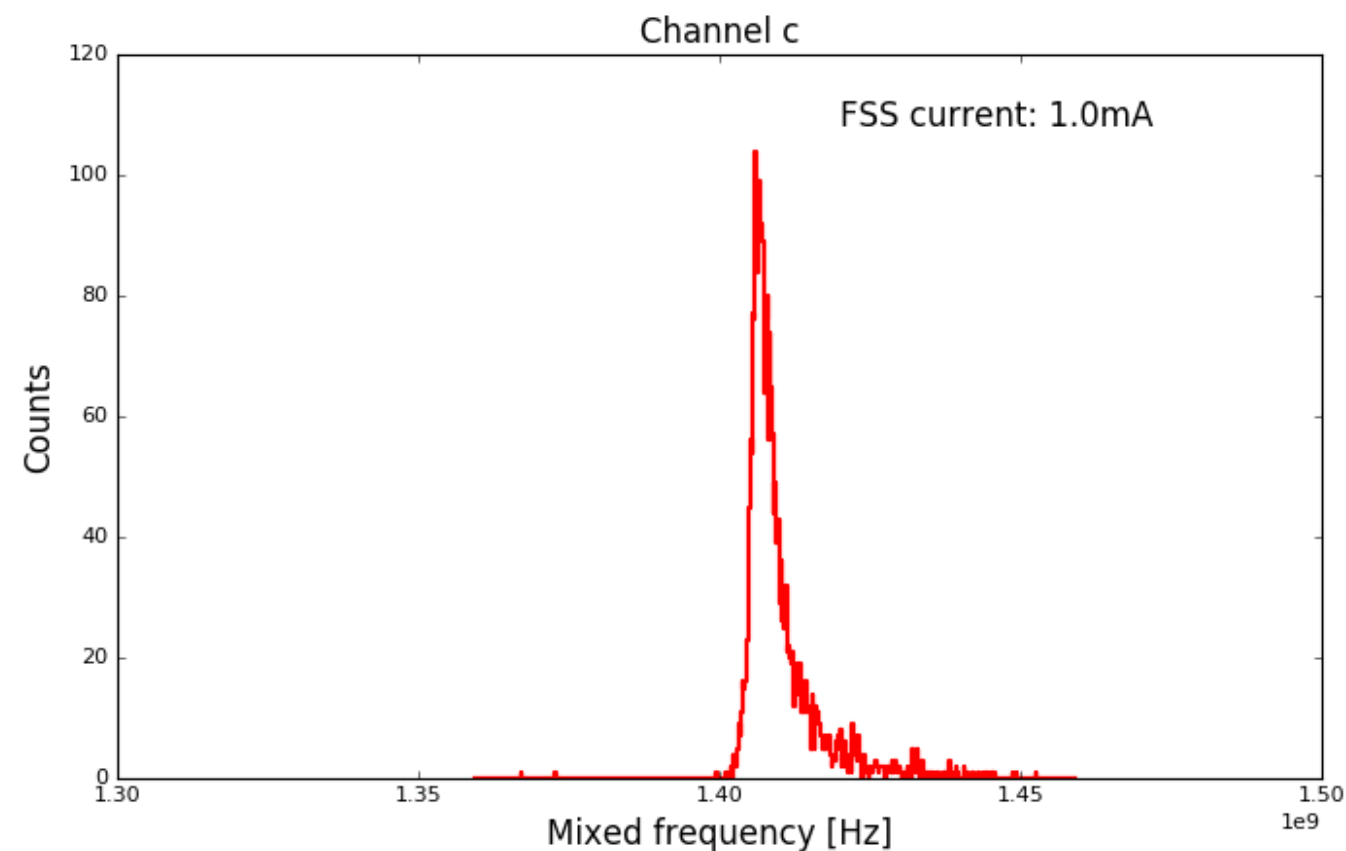
- linear dependence on absolute B-field

Calibration

- cannot easily ramp NMR magnet
 - ▶ installed **field-shifting solenoid** inside NMR bore
 - ▶ shift background field and thus cyclotron frequency
- shifted 17.8 keV line of ^{83}mKr
 - ▶ range of 70MHz (~ 1.5 keV)
 - ▶ **linearity demonstrated** within $\sim 0.010\text{MHz}$ ($\sim 0.0002\text{eV}$)



Field-shifting solenoid



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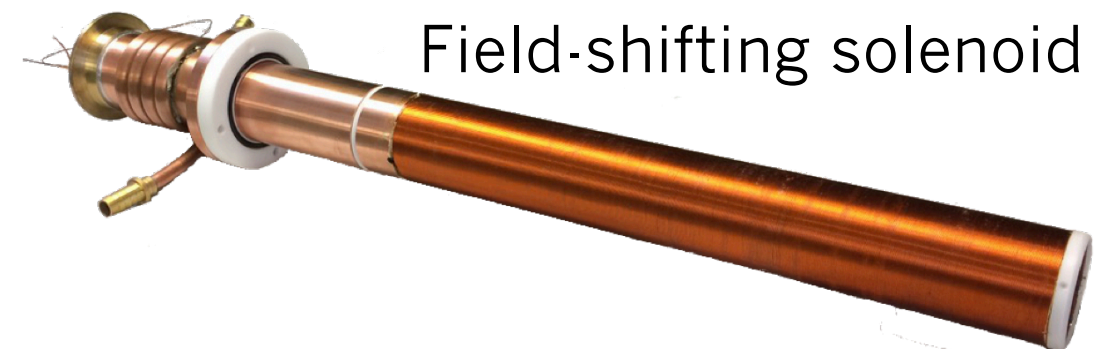
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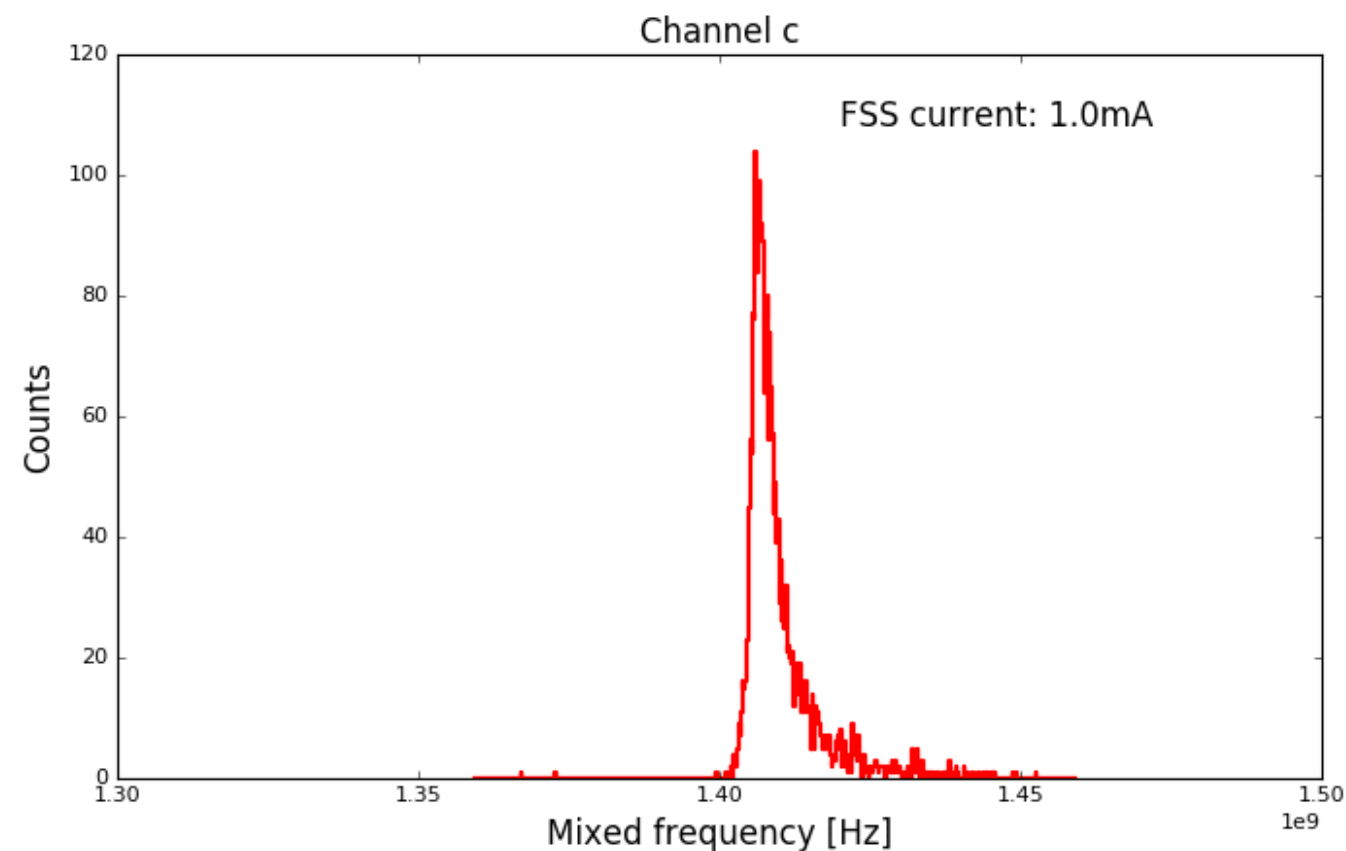
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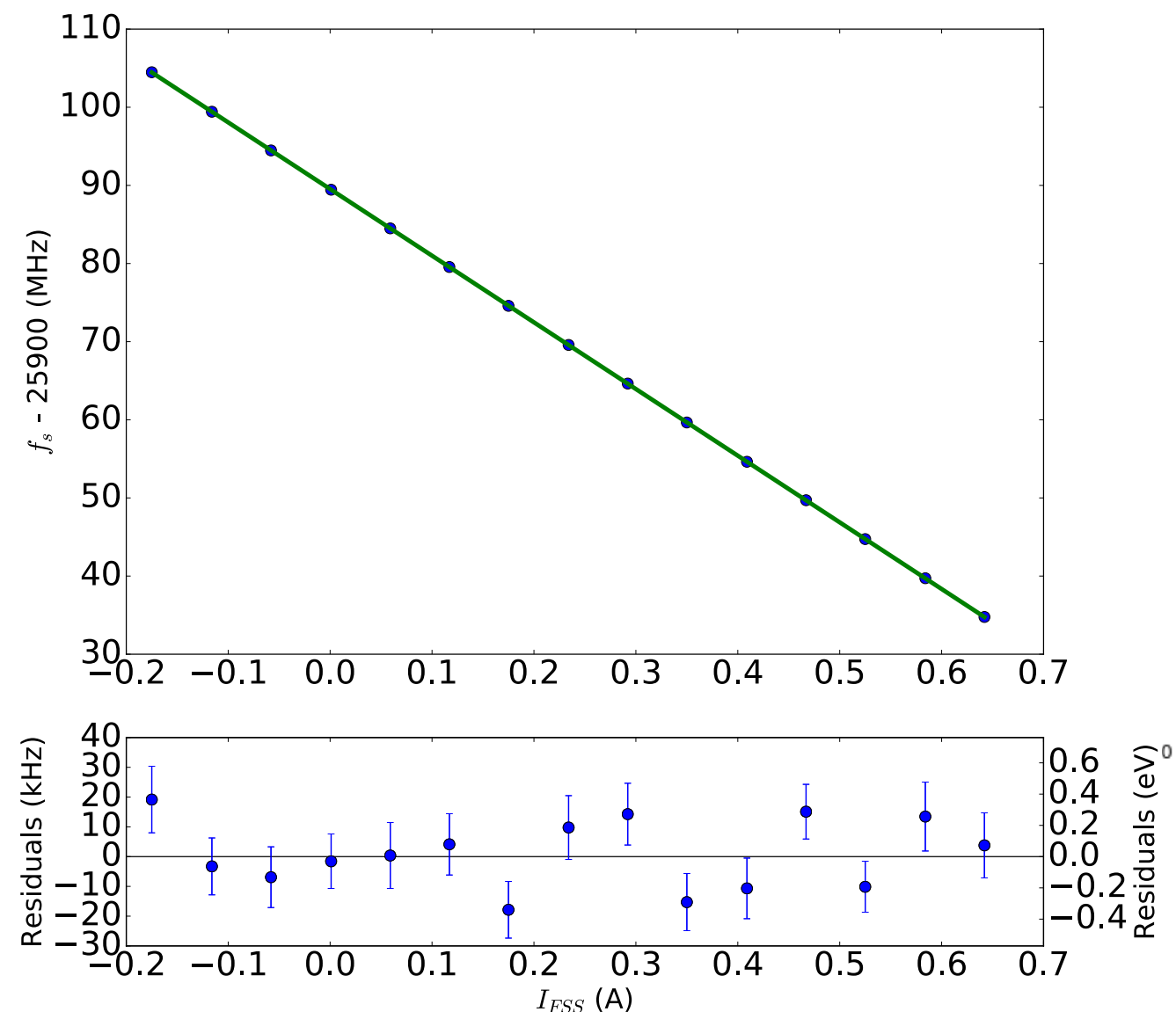
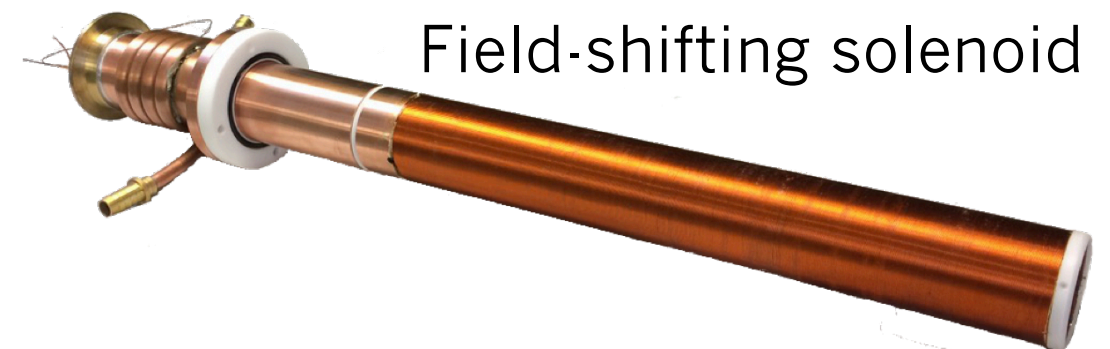
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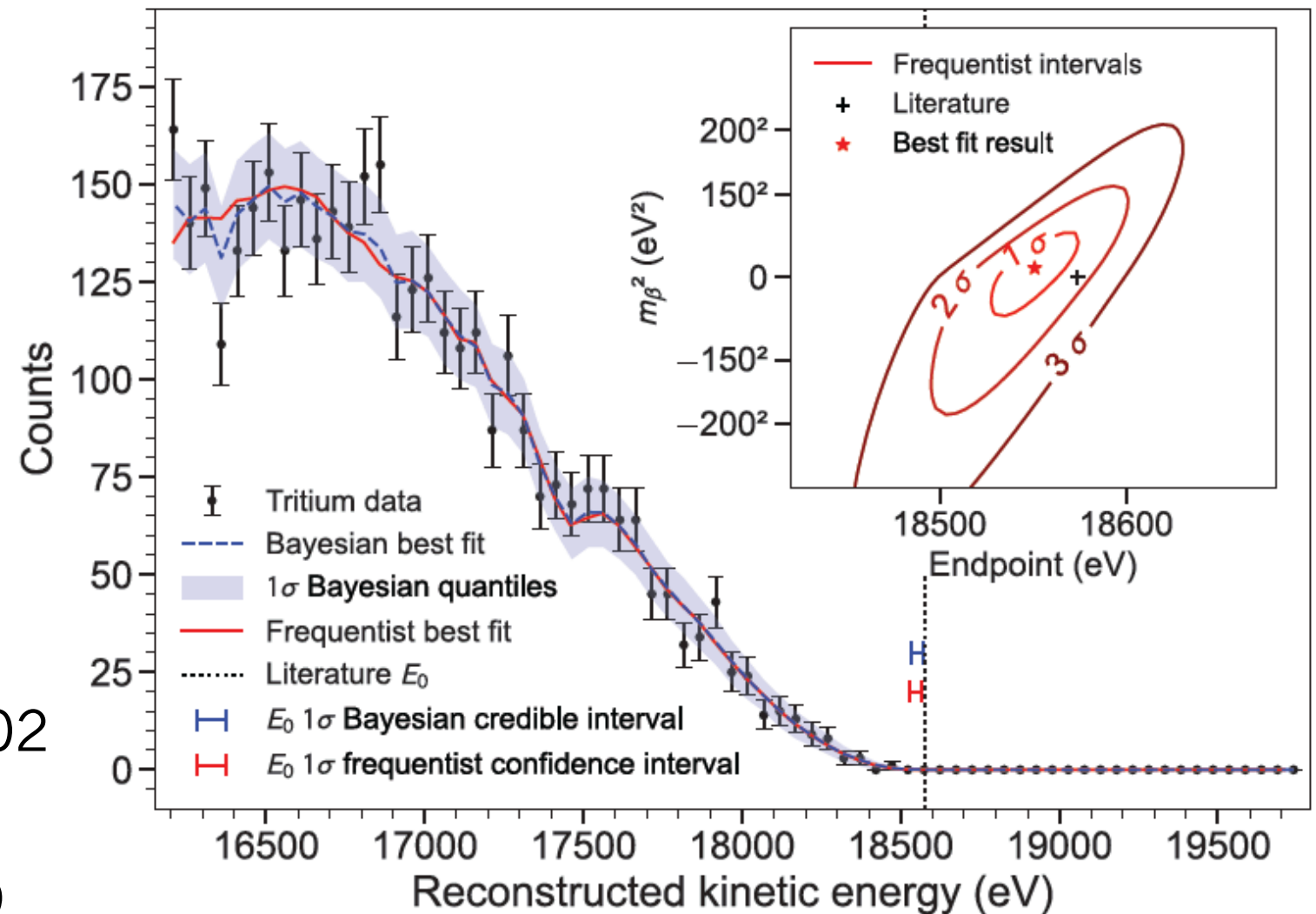
T2 analysis results

Analysis methods

- Frequentist analysis
- Bayesian analysis
 - ▶ good agreement!

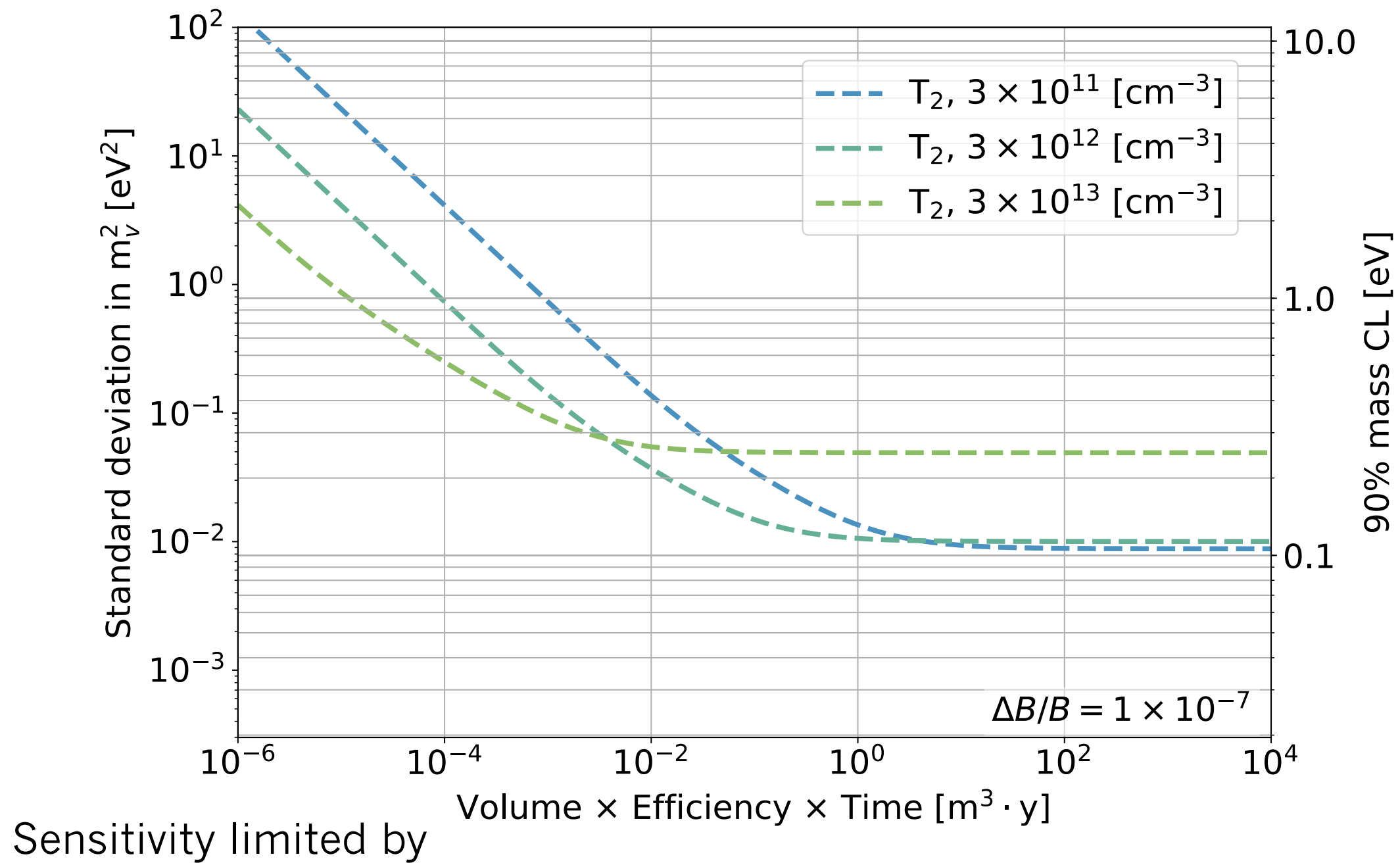
Analysis results

- main result
 - ▶ Phys. Rev. Lett. 131, 102502
- detailed discussion
 - ▶ arXiv:2302.12055 (→ PRC)

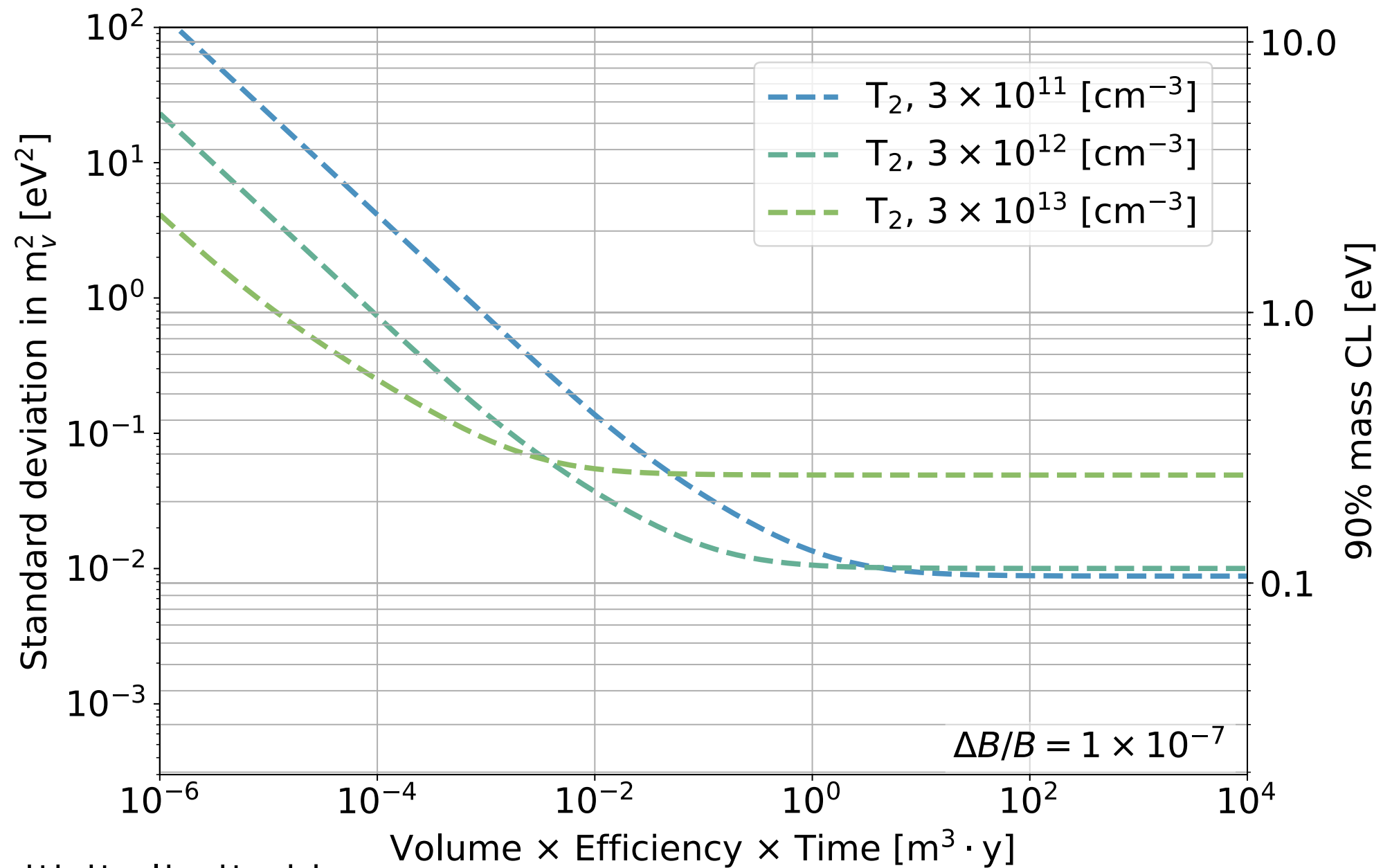


90% CL	T2 endpoint	Neutrino mass	Background rate
frequentist	$E_0 = 18548^{+19}_{-19}$ eV	$m_\beta \leq 152$ eV/c ²	$R \leq 3 \cdot 10^{-10}$ eV ⁻¹ s ⁻¹
bayesian	$E_0 = 18553^{+18}_{-19}$ eV	$m_\beta \leq 155$ eV/c ²	

Potential for neutrino mass?



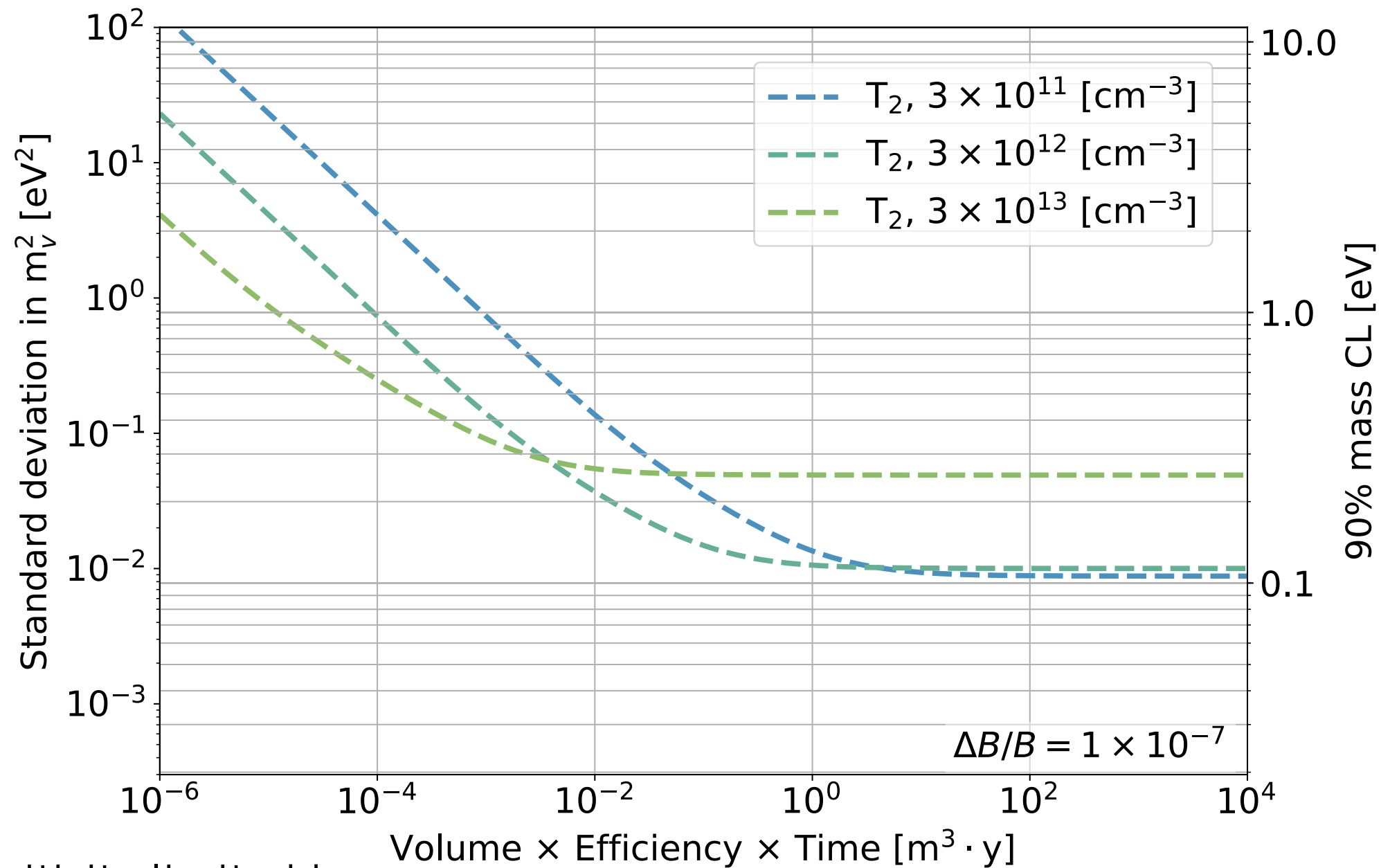
Potential for neutrino mass?



Sensitivity limited by

- density of tritium gas → rest gas interactions

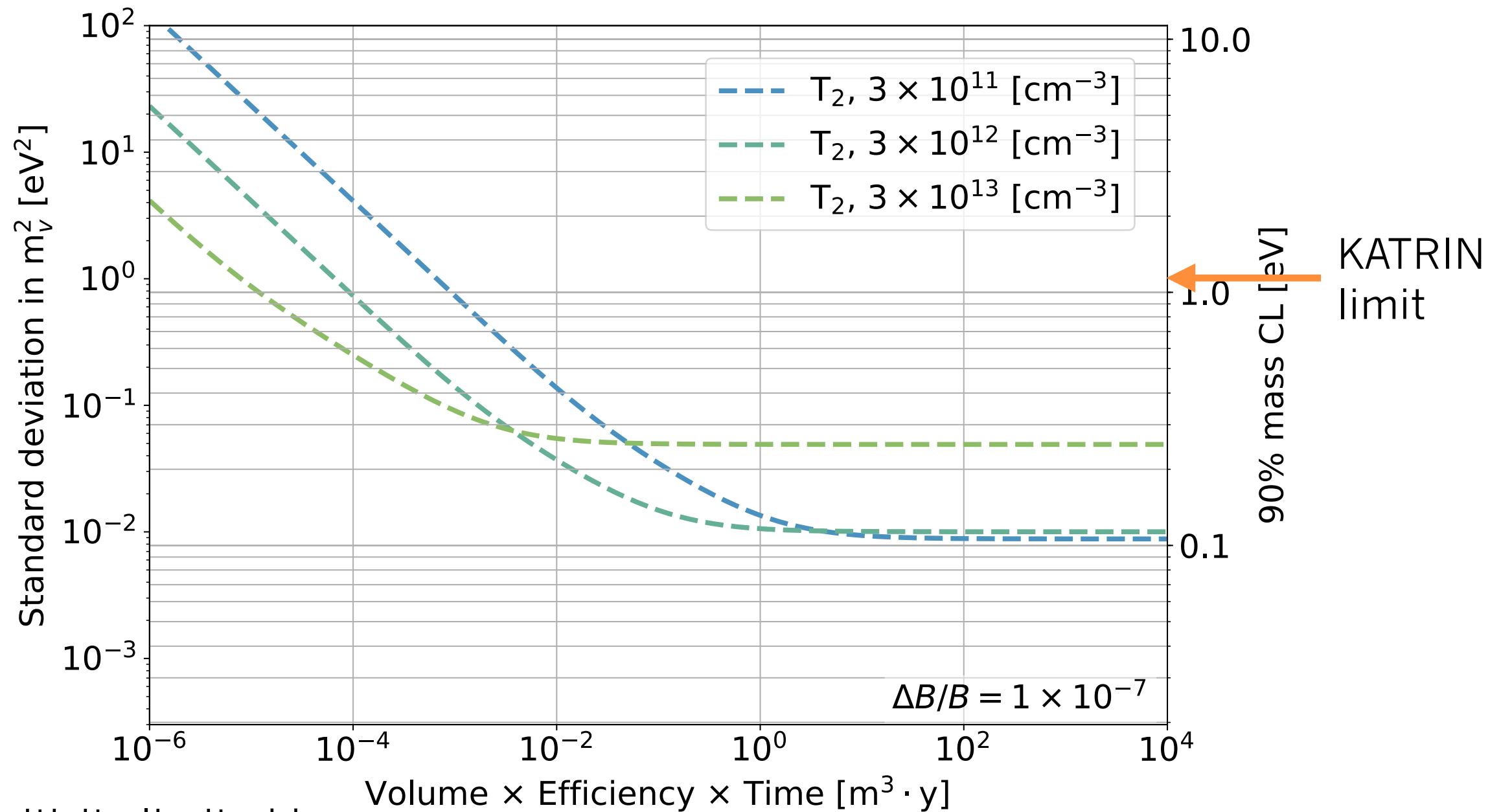
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Sensitivity limited by

- density of tritium gas → rest gas interactions
- molecular excitations in T_2

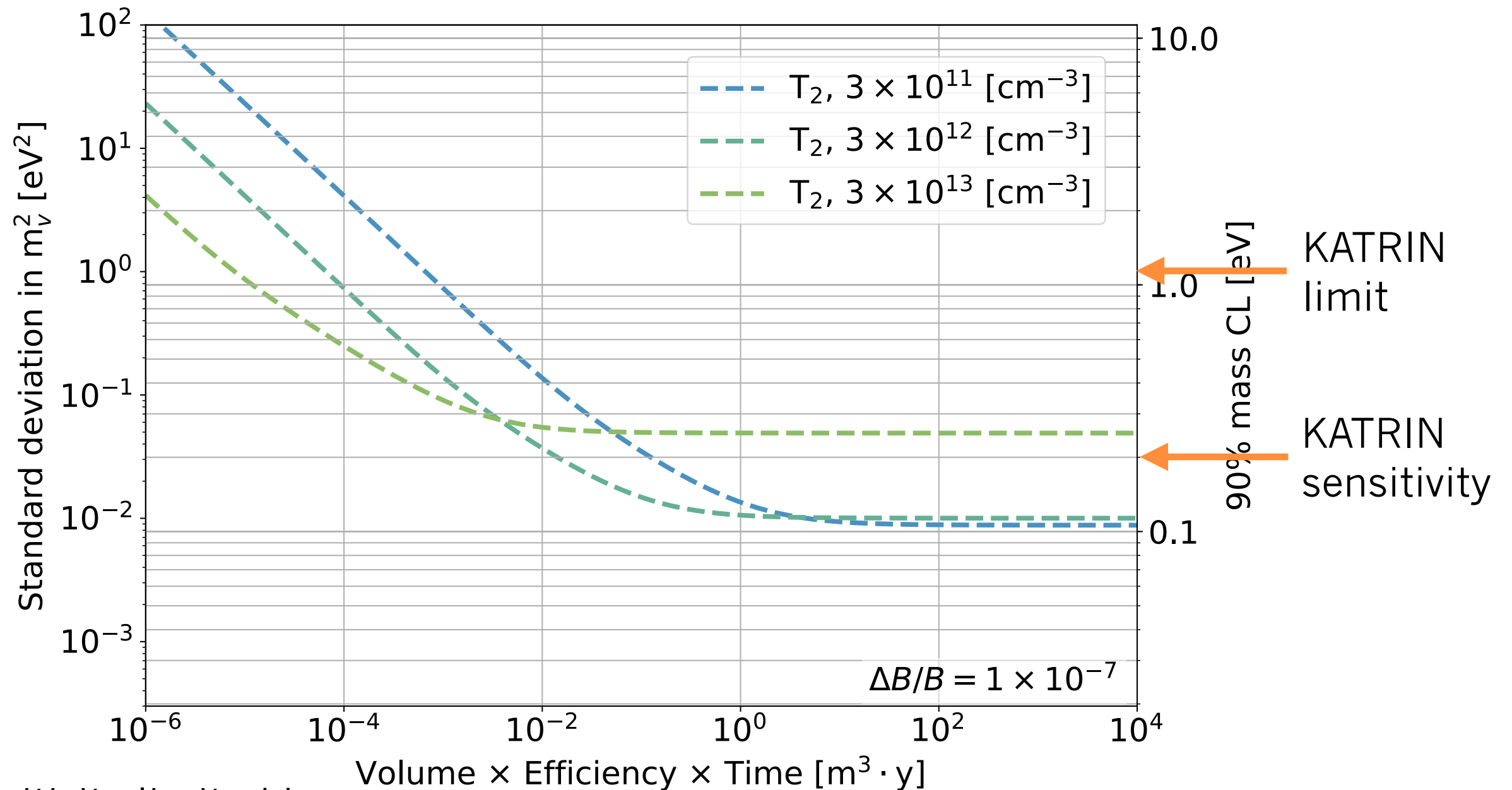
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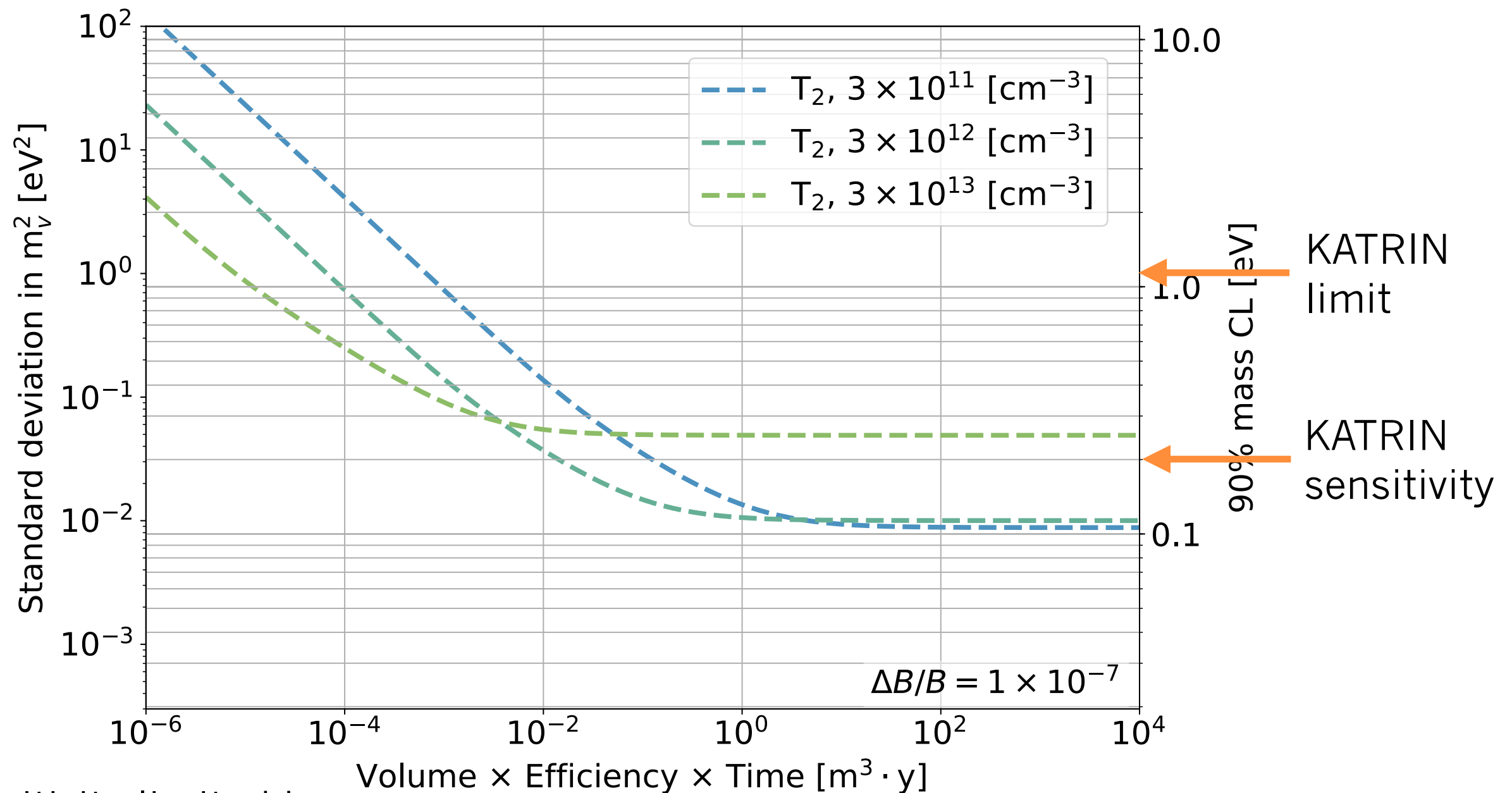
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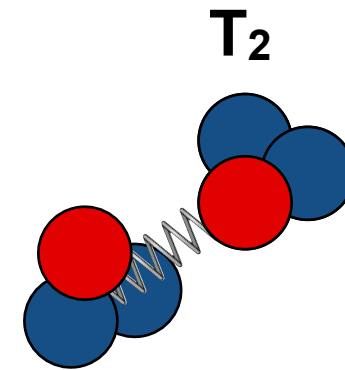
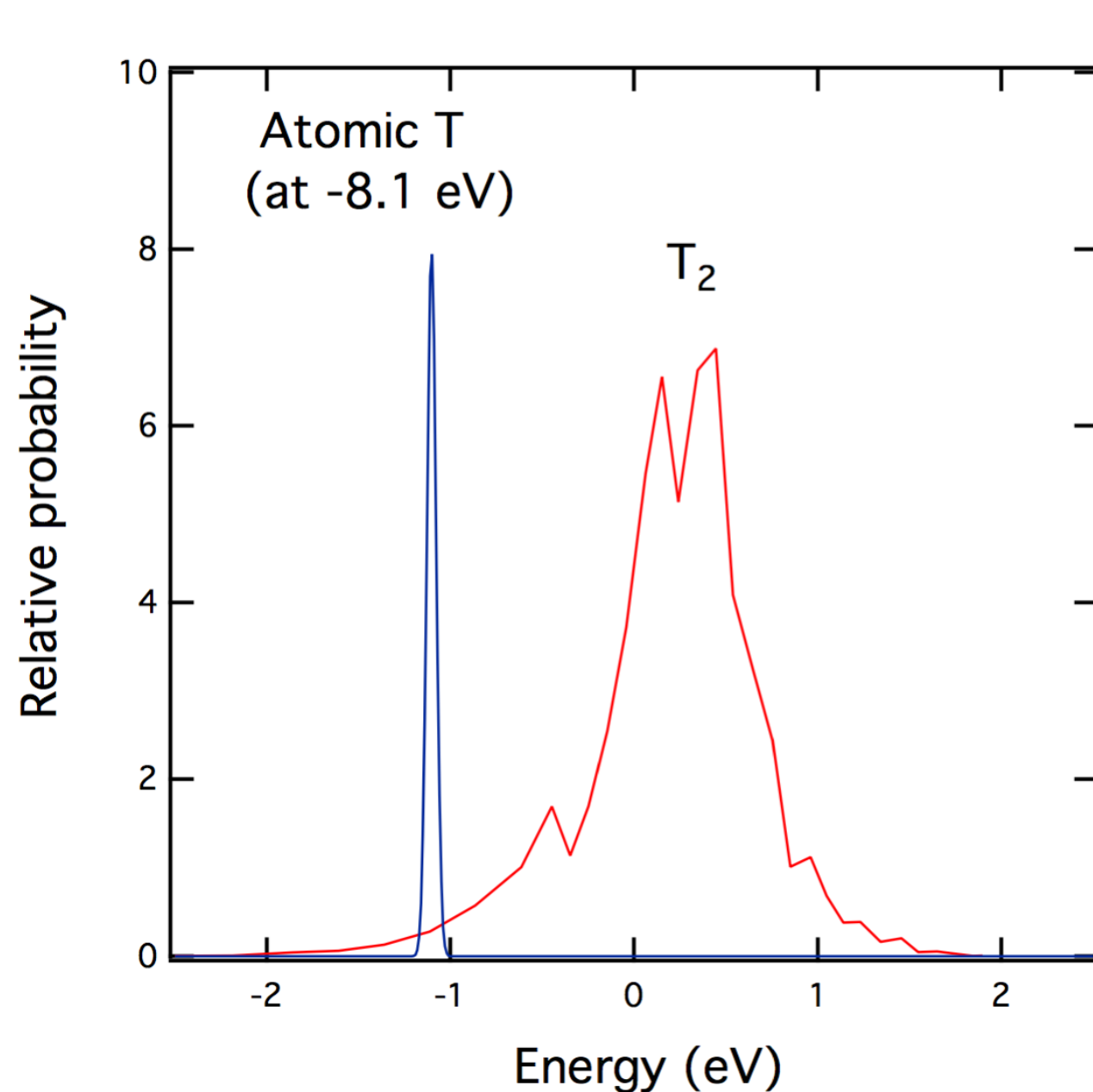
Potential for neutrino mass?



Sensitivity limited by

- density of tritium gas → rest gas interactions
- molecular excitations in T_2
 - need **atomic tritium**

Molecular tritium limitations

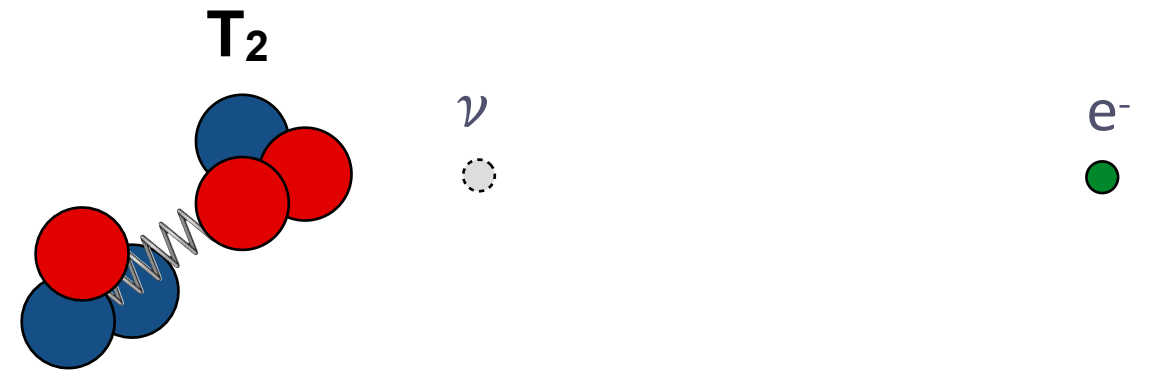
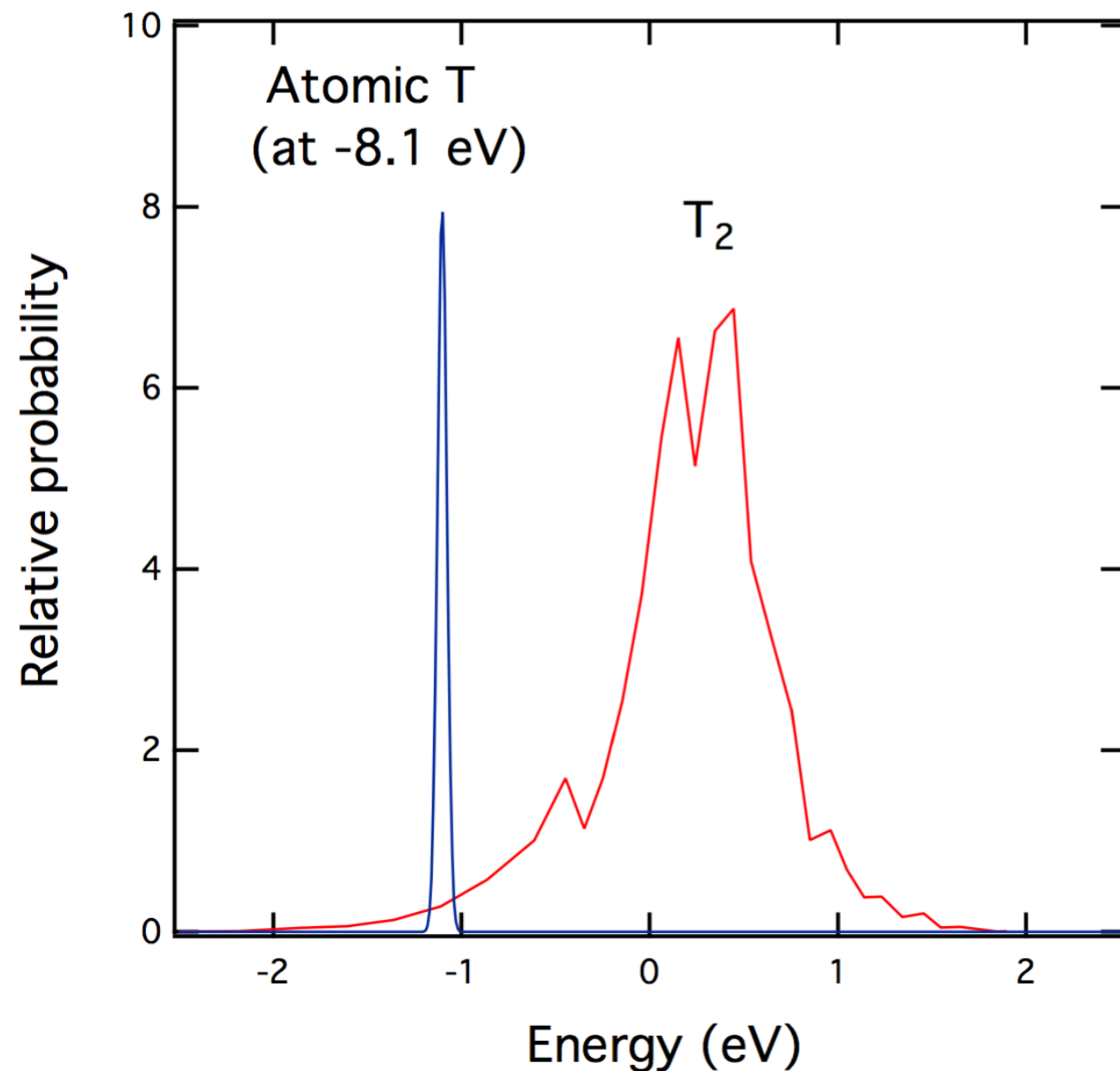


Molecular excitations
in ³HeT daughter molecule

- blur tritium endpoint
- fundamental limit to measurement of ν -mass

Need atomic tritium
for **ultimate** experiment!

Molecular tritium limitations

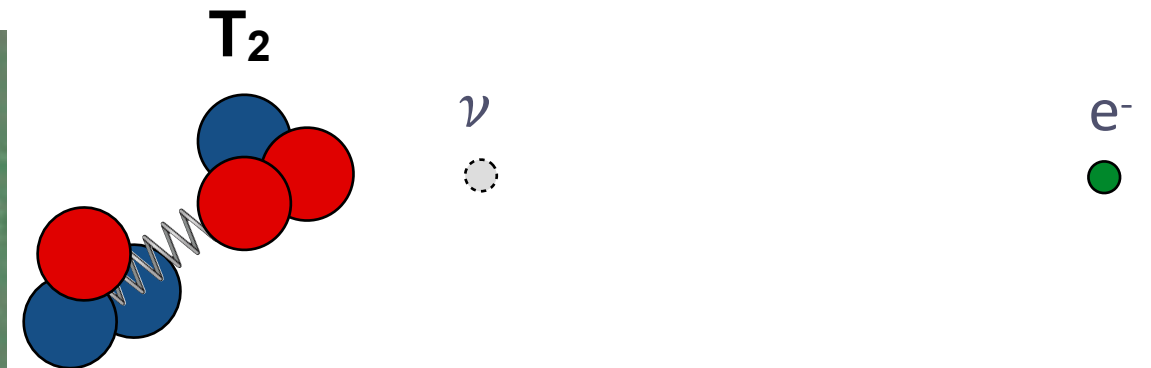
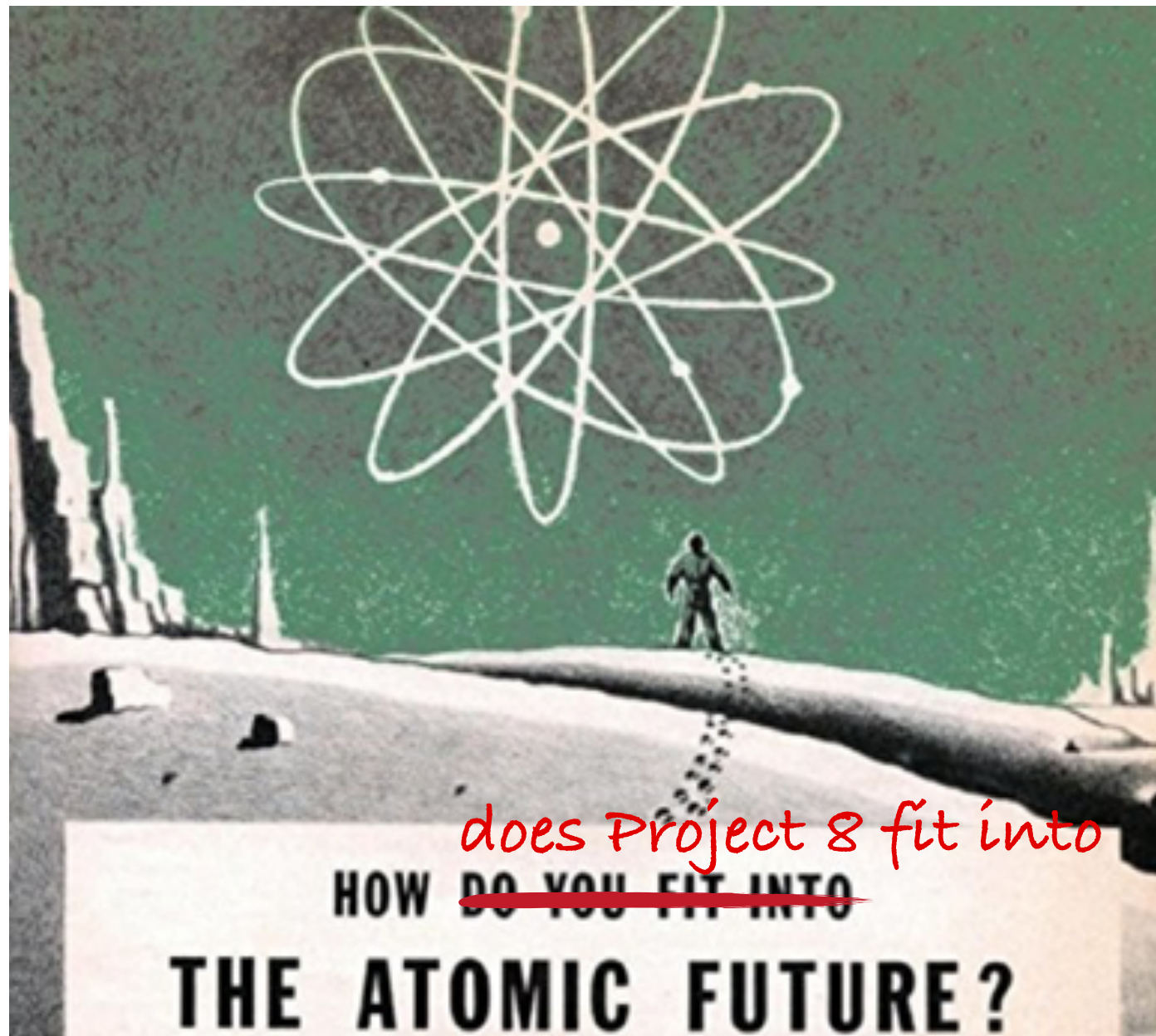


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Molecular tritium limitations



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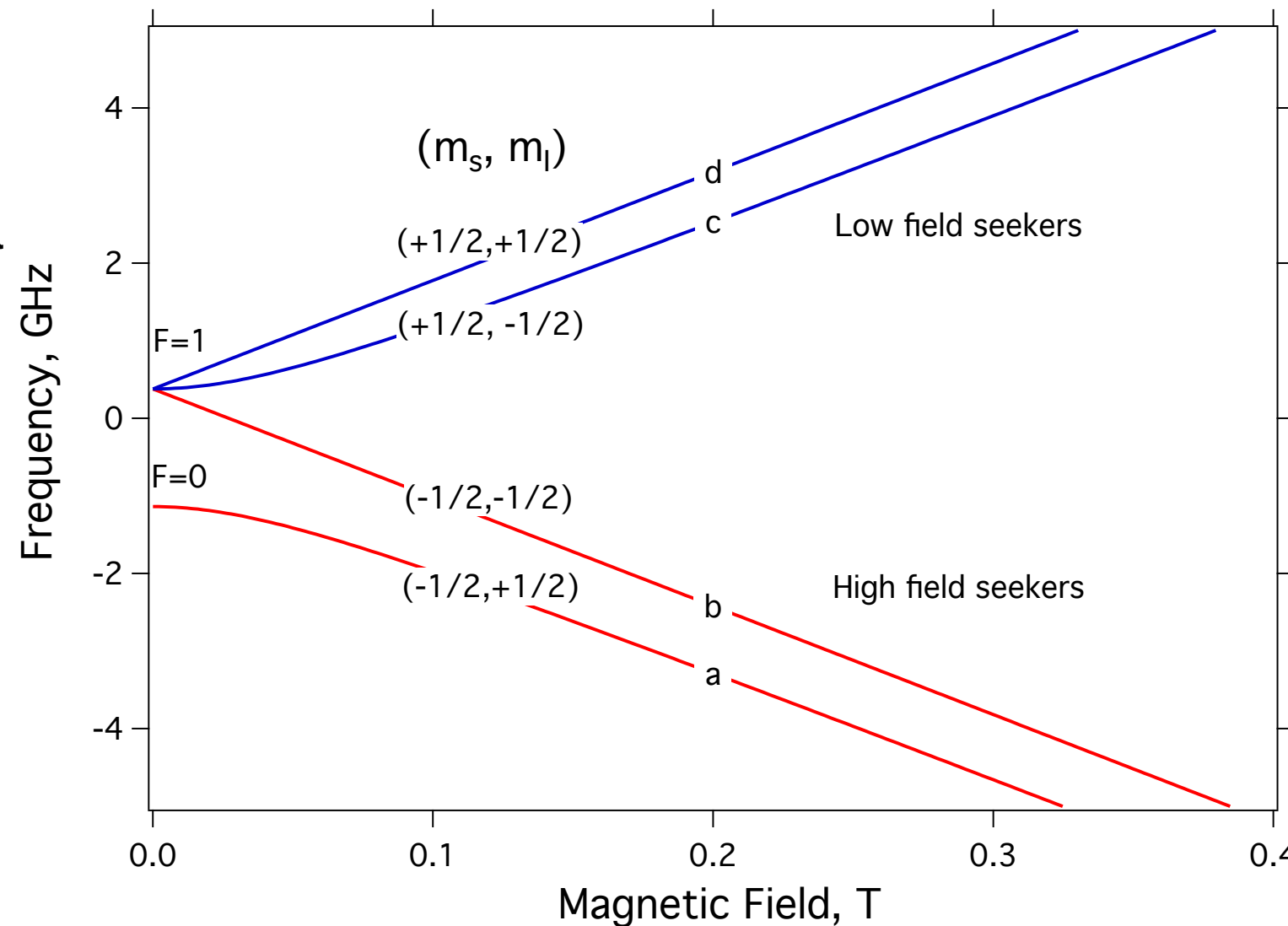
Magnetic storage of neutral atoms

Storage of atomic T

- recombination catalyzed by walls
→ difficult!
- H, D and T have unpaired e⁻
 - ▶ non-zero magnetic moment μ
 - ▶ tend to (anti-)align with B-field if change is adiabatic

Potential energy

- $\Delta E = -\vec{\mu} \cdot \vec{B}$
 - half of spin states seek field minimum



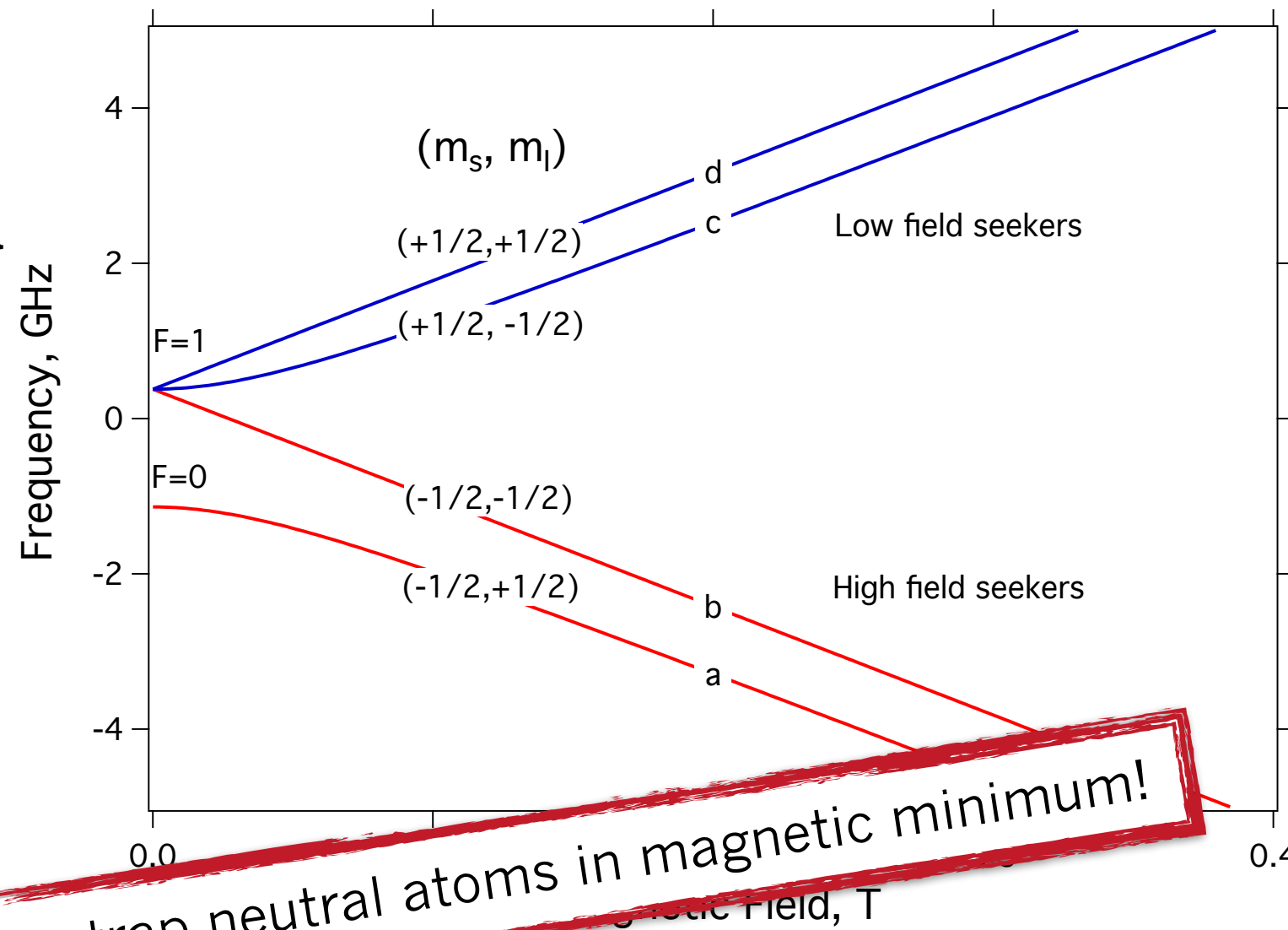
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Can trap neutral atoms in magnetic minimum!

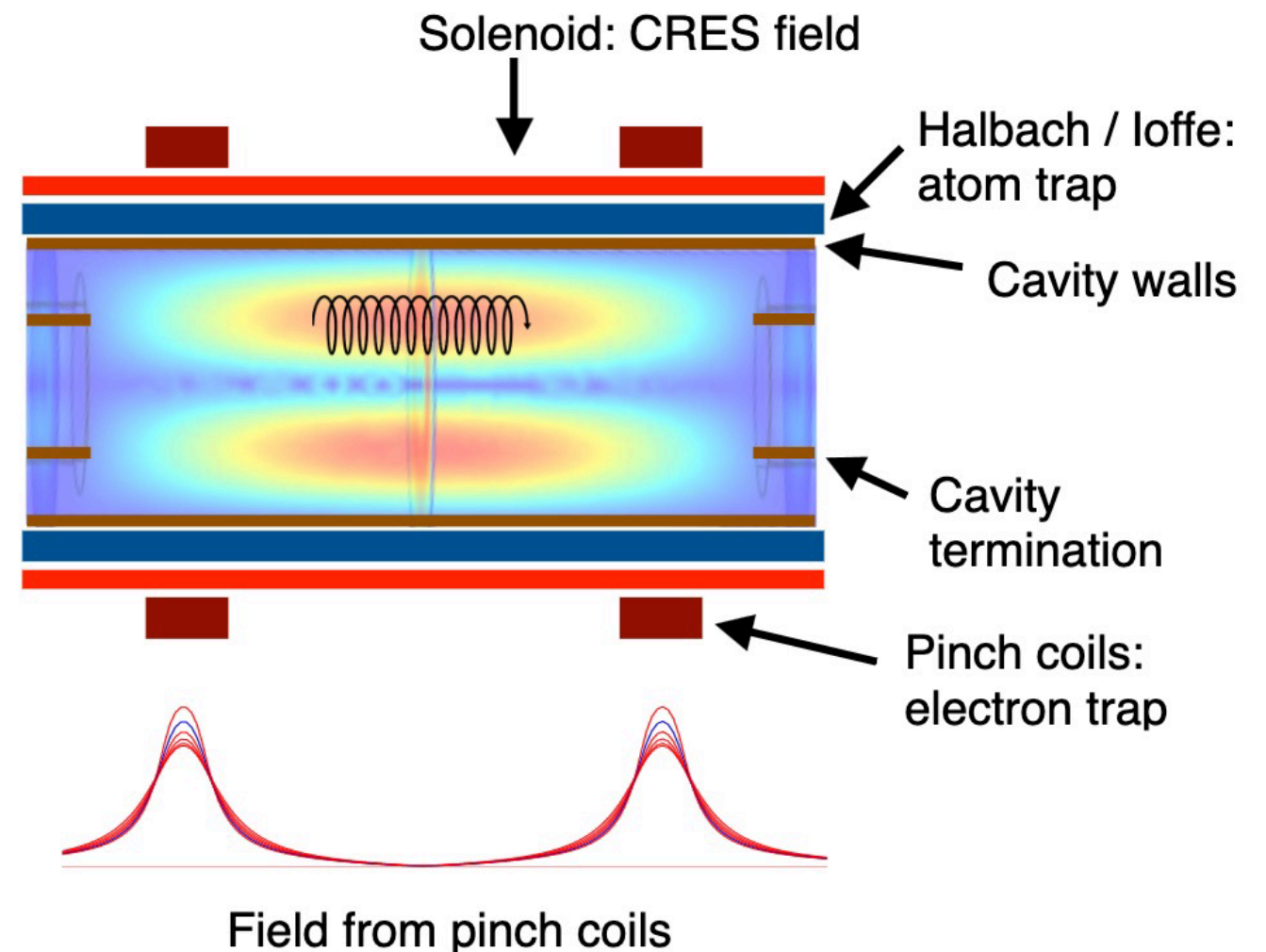
Scaling towards the future

Requirements

- high statistical power
 - ▶ large volume
 - ▶ high detection efficiency
- good energy resolution
 - ▶ atomic tritium
 - ▶ track reconstruction
- lower systematic uncertainties and easier calibration
 - ▶ cavity design with simple mode structure

Concept

- $\emptyset(\text{m}^3)$ **cavity** with **atom trap**
 - ▶ TE₀₁ mode at $\emptyset(100\text{MHz})$

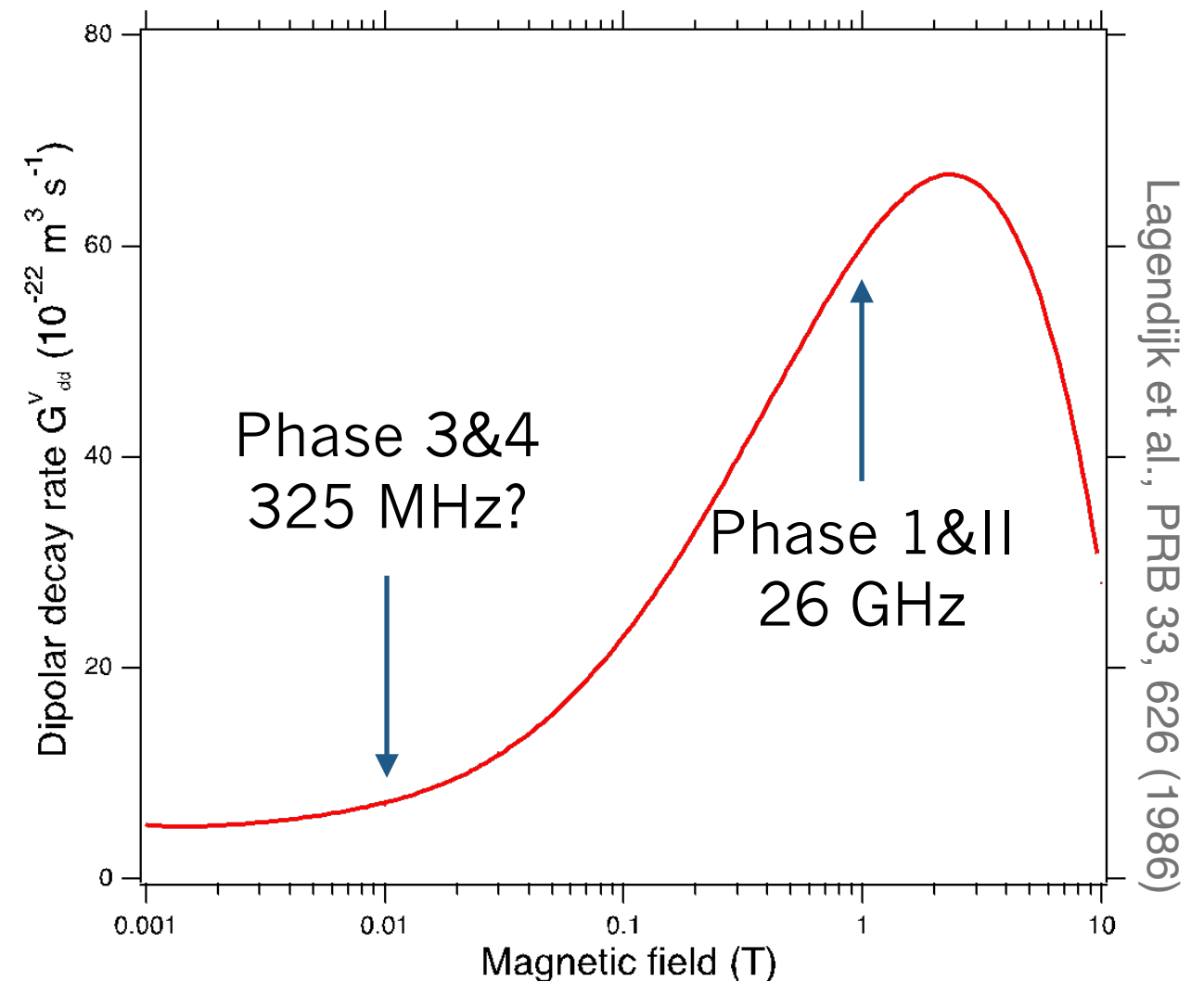


Low-frequency traps

Advantages

- lower magnetic field
 - ▶ lower dipolar spin-flip rate
 - ▶ lower atom loss rate
- larger cavity volume
 - ▶ scales with $1/f^3$
 - ▶ larger event rate

→ push to **larger, low-frequency cavities**



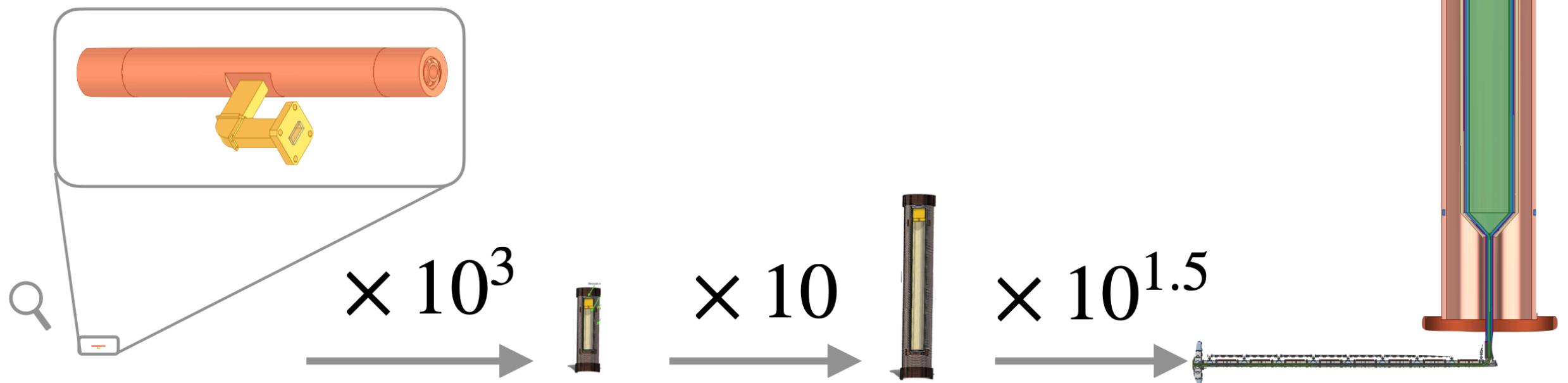
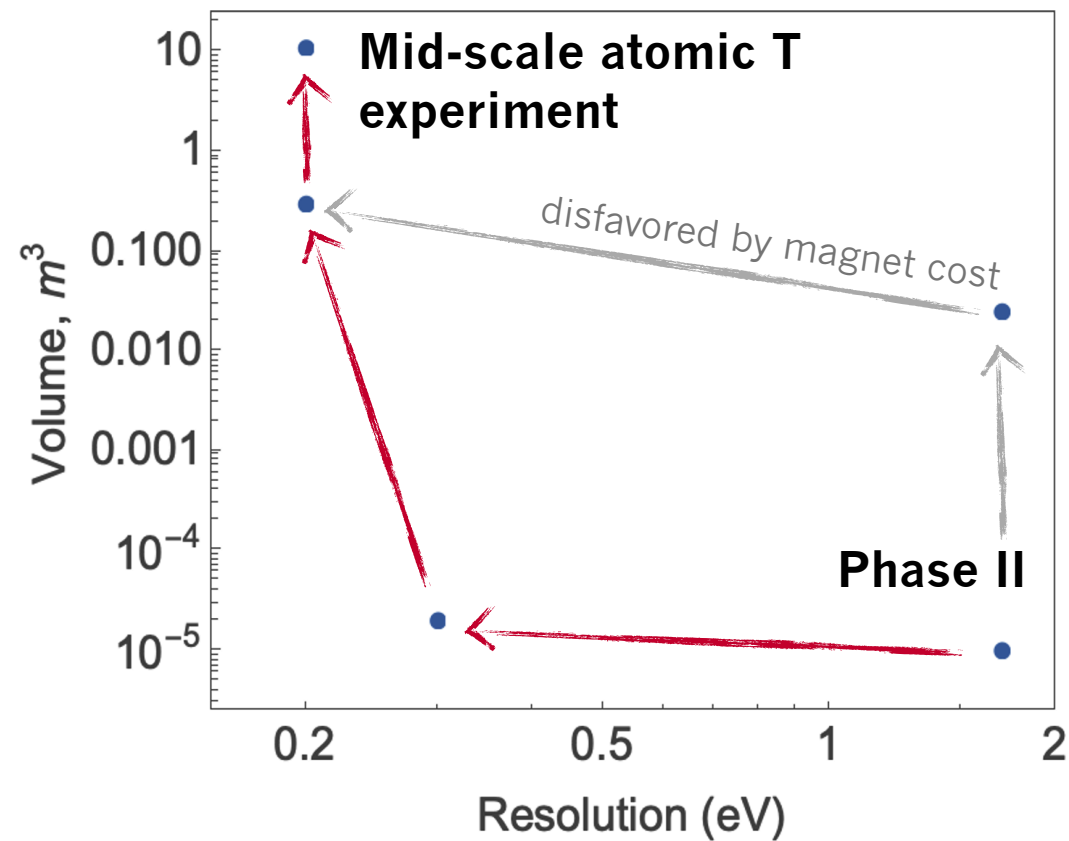
Phase III: Cavity design

Scaling approach

- Optimize cavity design
- Develop position-sensitive reconstruction
- Increased volume step by step!

Series of demonstrators

- partially parallelized



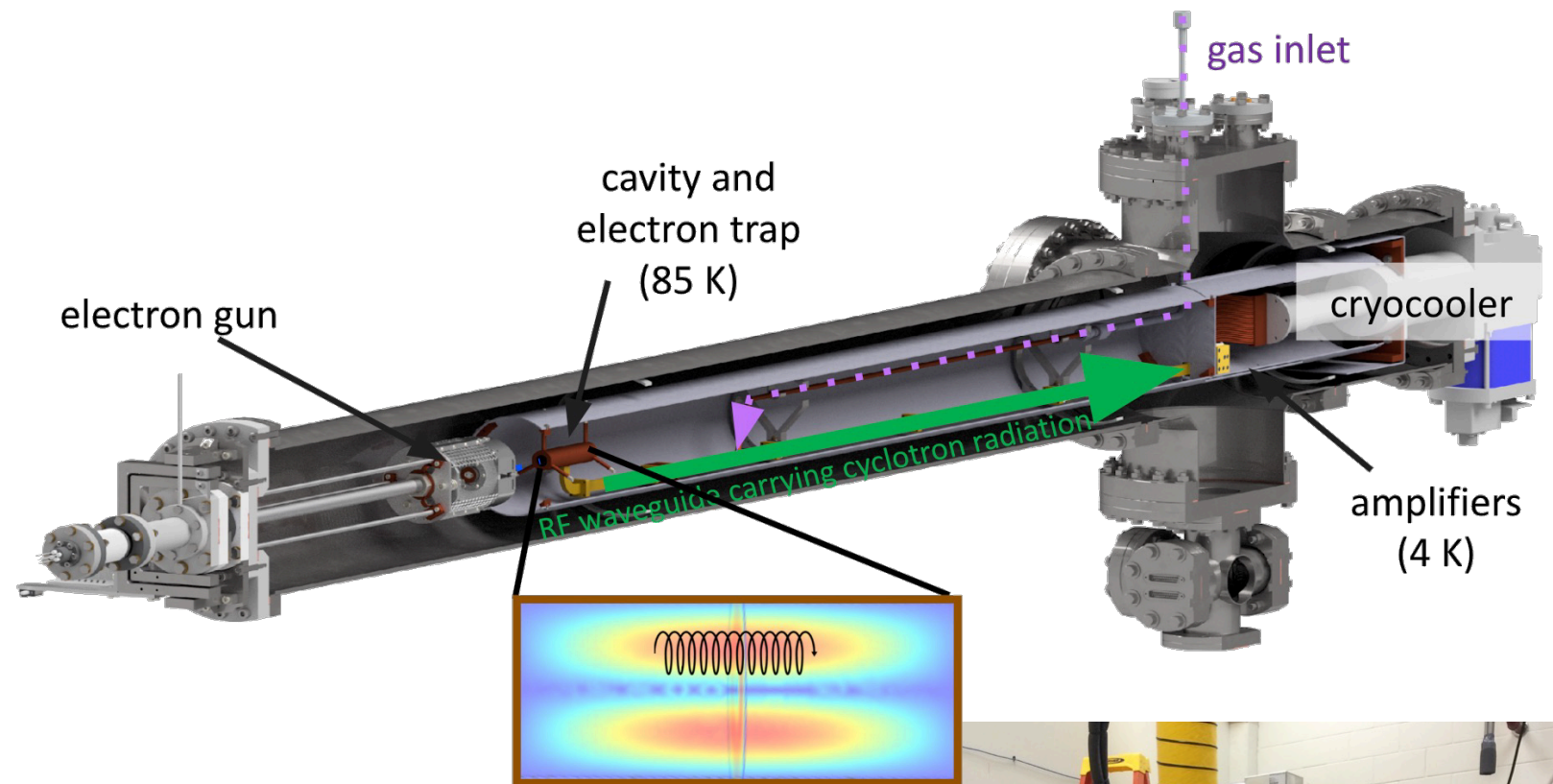
Cavity CRES Apparatus

Specifications

- cm³ cavity at 26 GHz
- Electron sources
 - ▶ 83mKr
 - ▶ electron gun
- insert in medical MRI magnet

Goals

- Demonstrate CRES in a cavity
- Improve detection efficiency
 - ▶ $\emptyset(1\%) \rightarrow \emptyset(10\%)$
 - ▶ maintaining very low background
- Demonstrate electron gun calibration
- Resolution $\sigma(E) < 300$ meV
 - ▶ axial frequency reconstruction



Pitch angle reconstruction

Magnetic field effects

- varies along axial motion

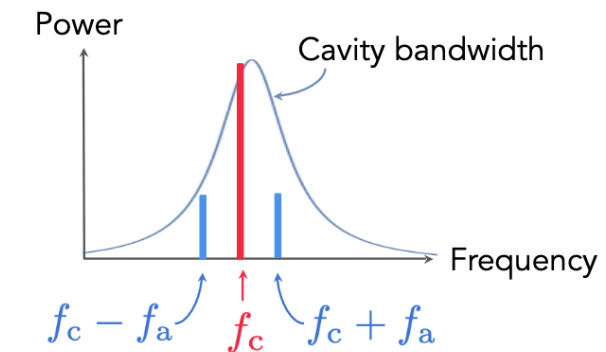
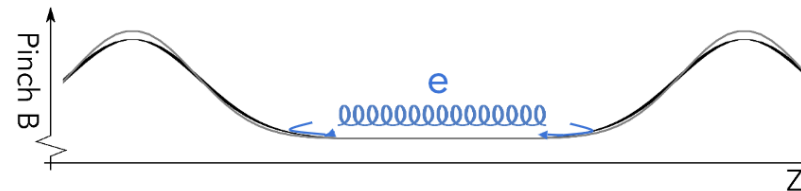
Electron signal is frequency modulated

- Main carrier
 - ▶ frequency proportional to average magnetic field
- Sidebands
 - ▶ spaced by axial frequency

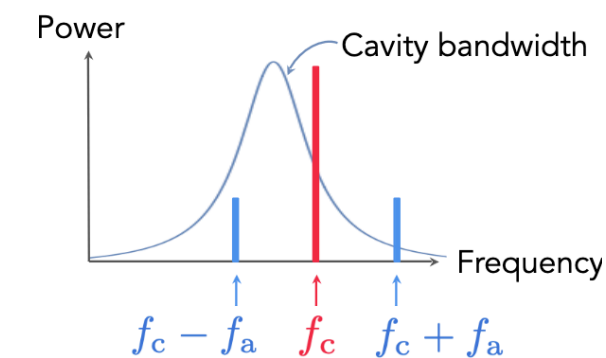
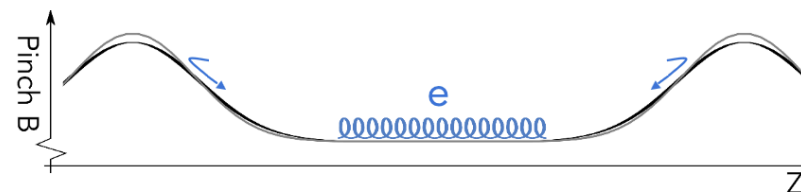
Approach

- Detect sidebands
 - ▶ correct for axial frequency effect
- limited by radial variation in trap shape!

Large pitch angle, $\theta \approx 90^\circ$:



"Small" pitch angle, $\theta \rightarrow \theta_{\min}$:



$$f_c = \frac{1}{2\pi} \frac{e\langle B \rangle}{m_e + E/c^2}$$

Optimization of trap design

Traps with more coils

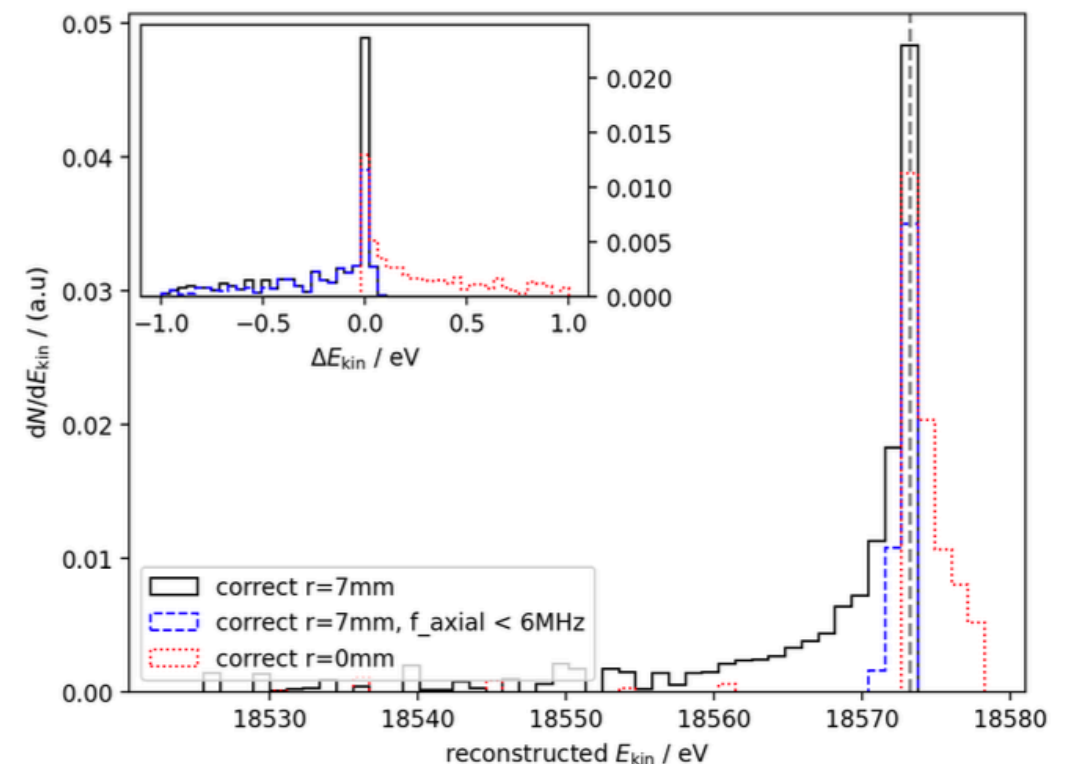
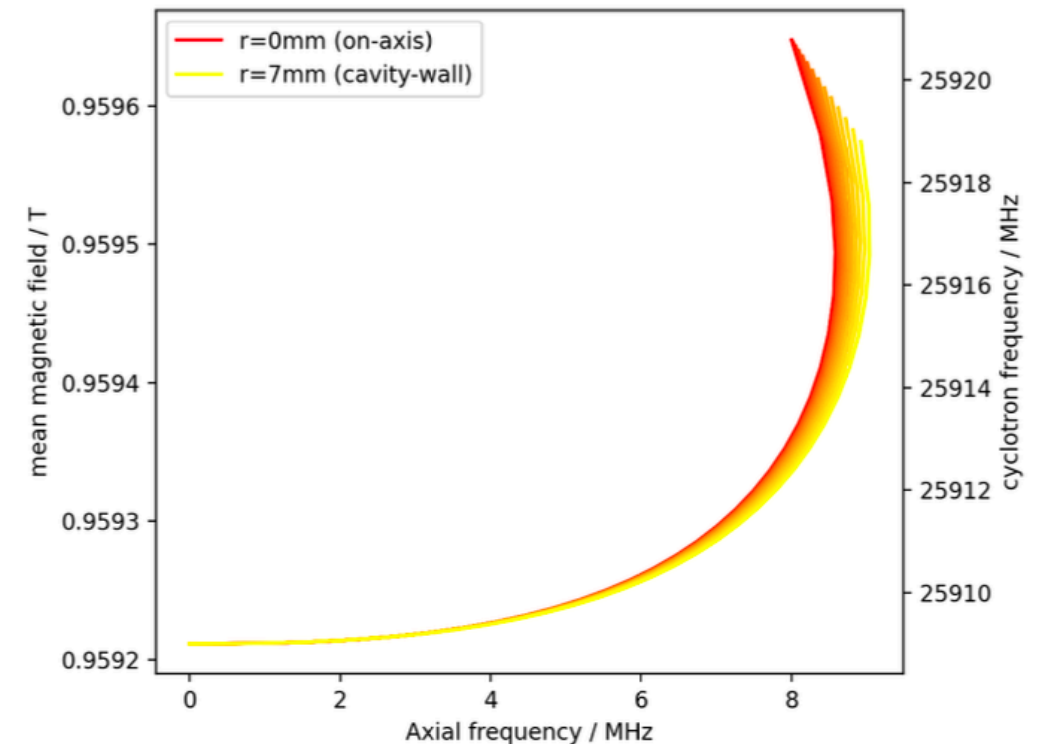
- steeper walls
 - ▶ less axial dependence
- less homogeneity in center

Optimization approach

- optimize many loops with individual currents
- reality constraints
 - ▶ geometry, power,...

Pitch angle correction

- limited by shape change at large radii
 - ▶ only probed at large pitch angles
- limit axial frequency for resolution goal



Optimization of trap design

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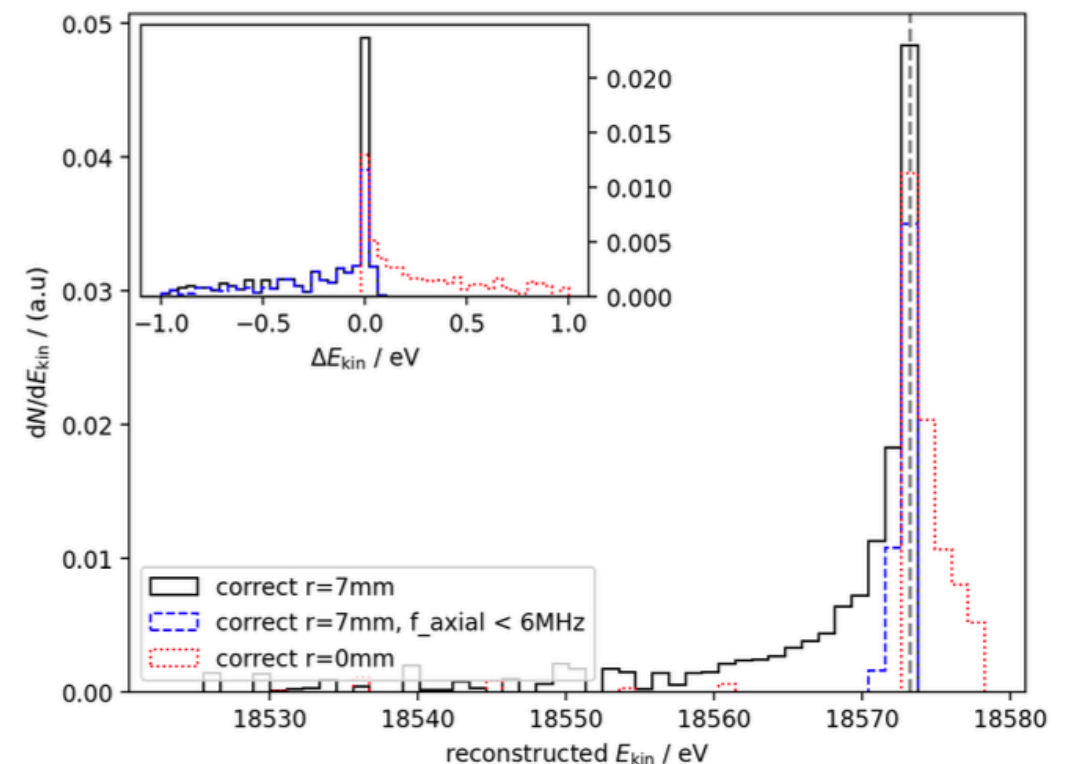
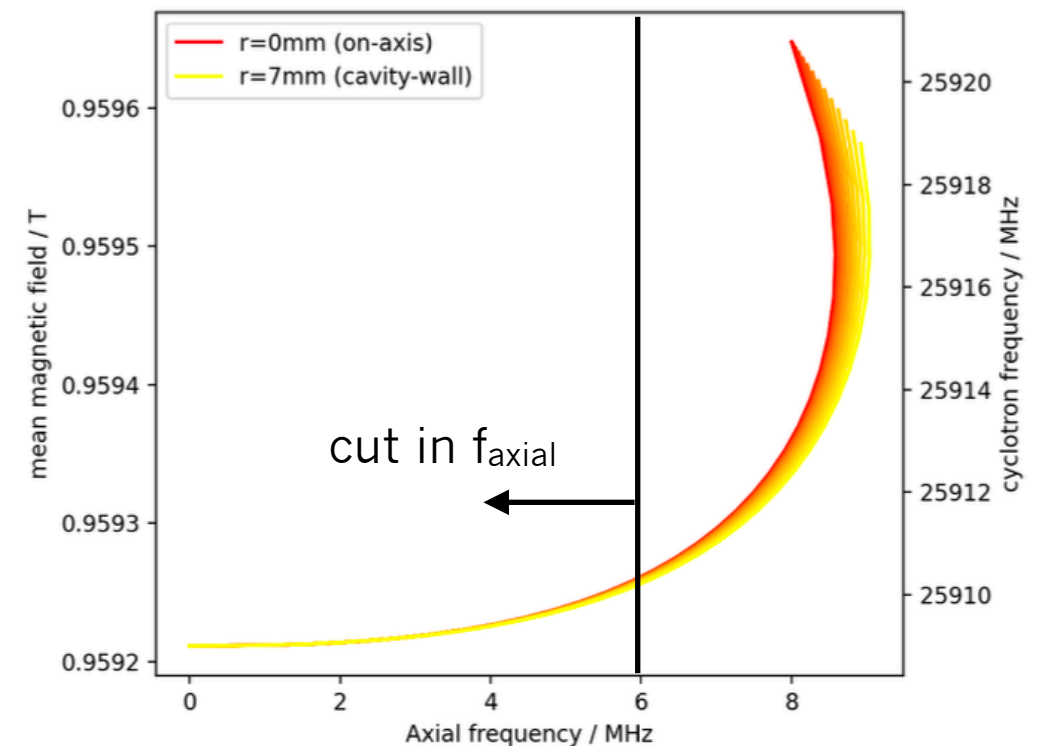
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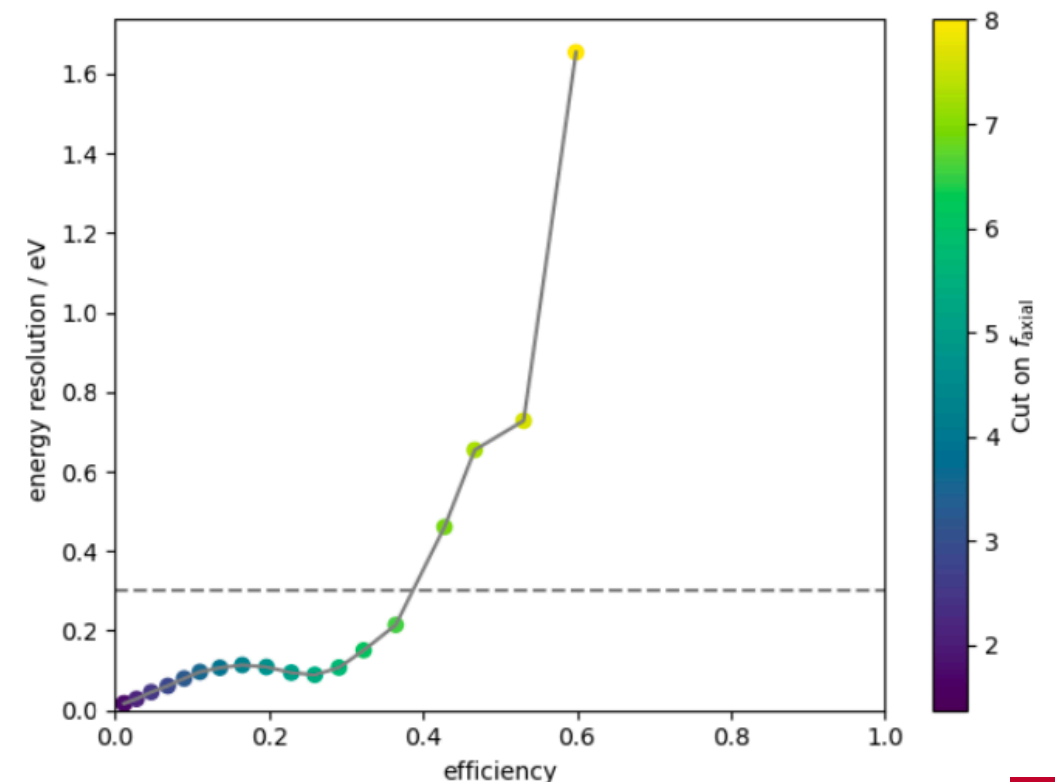
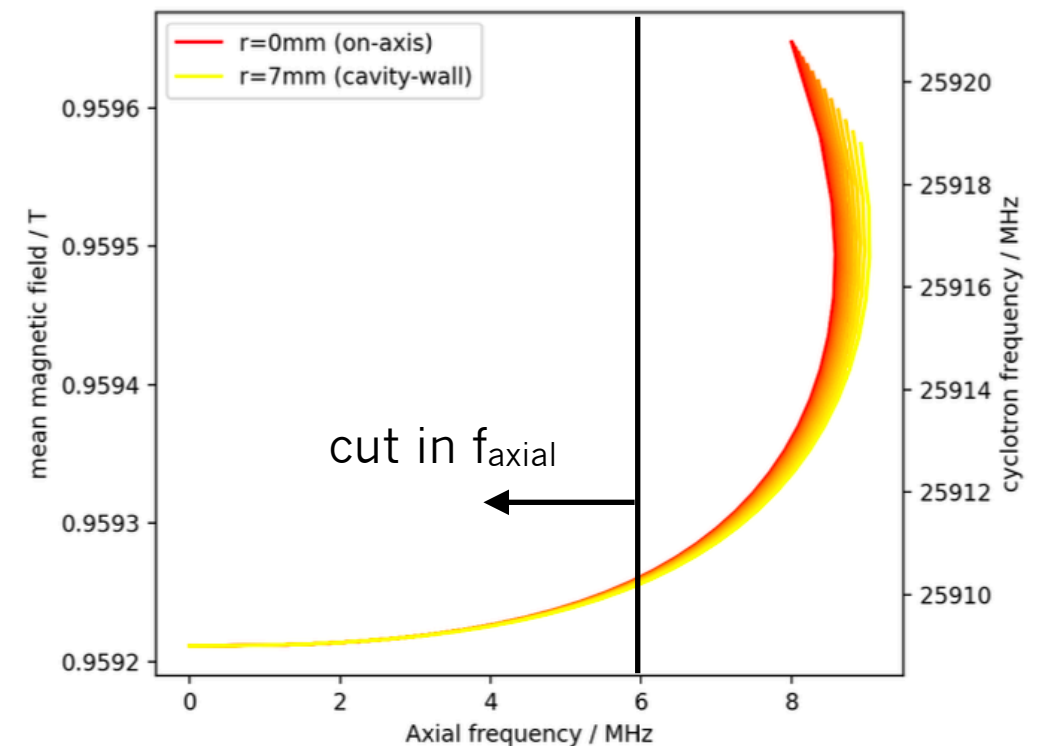
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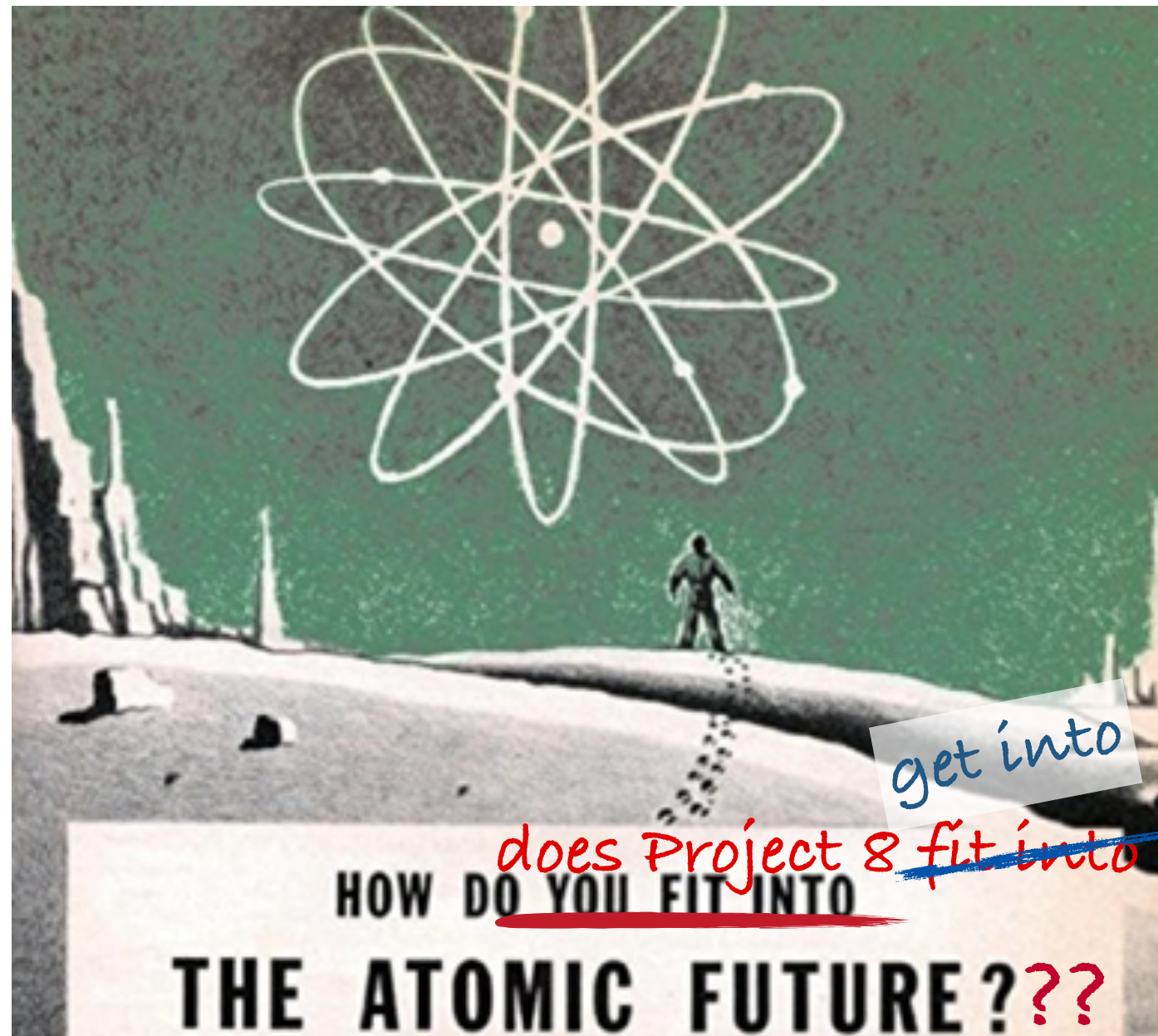
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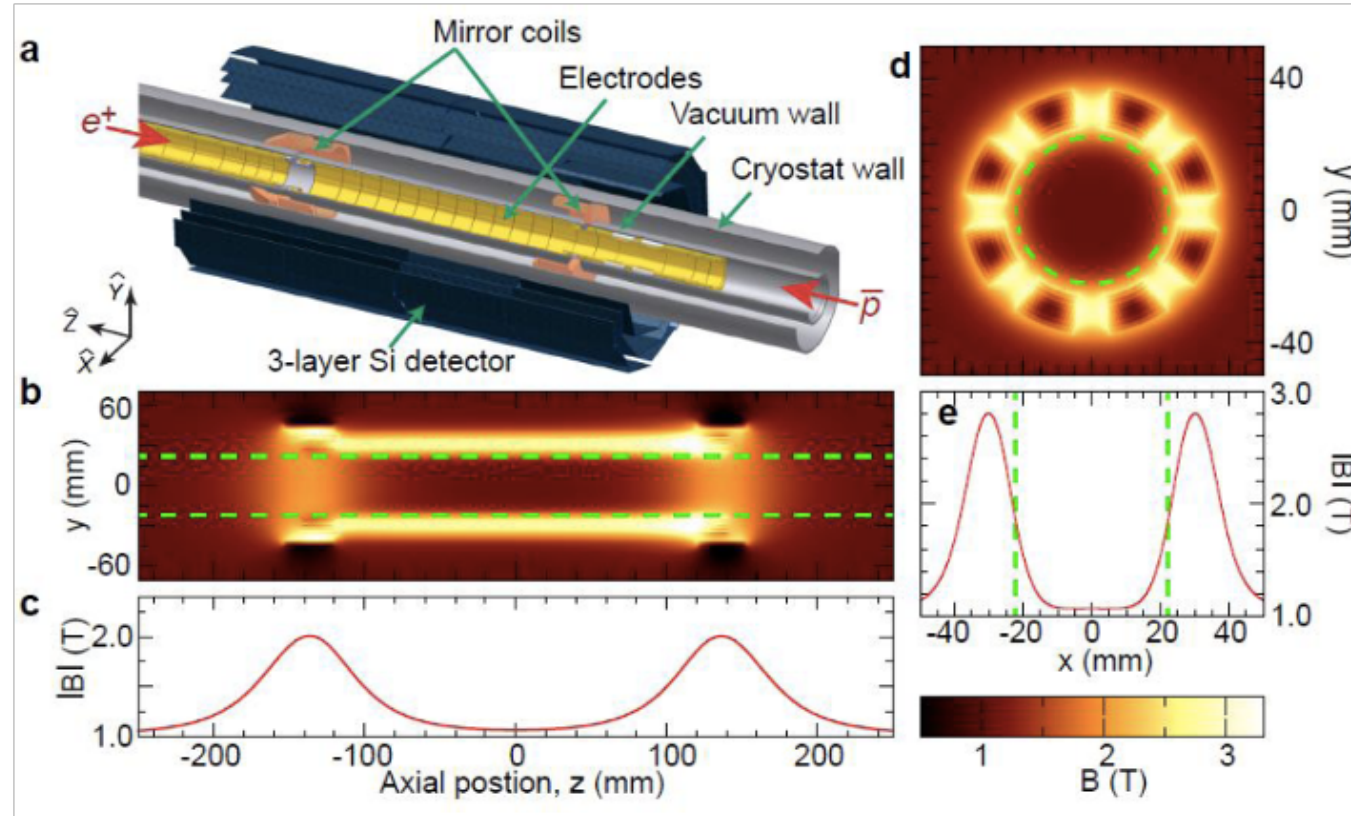
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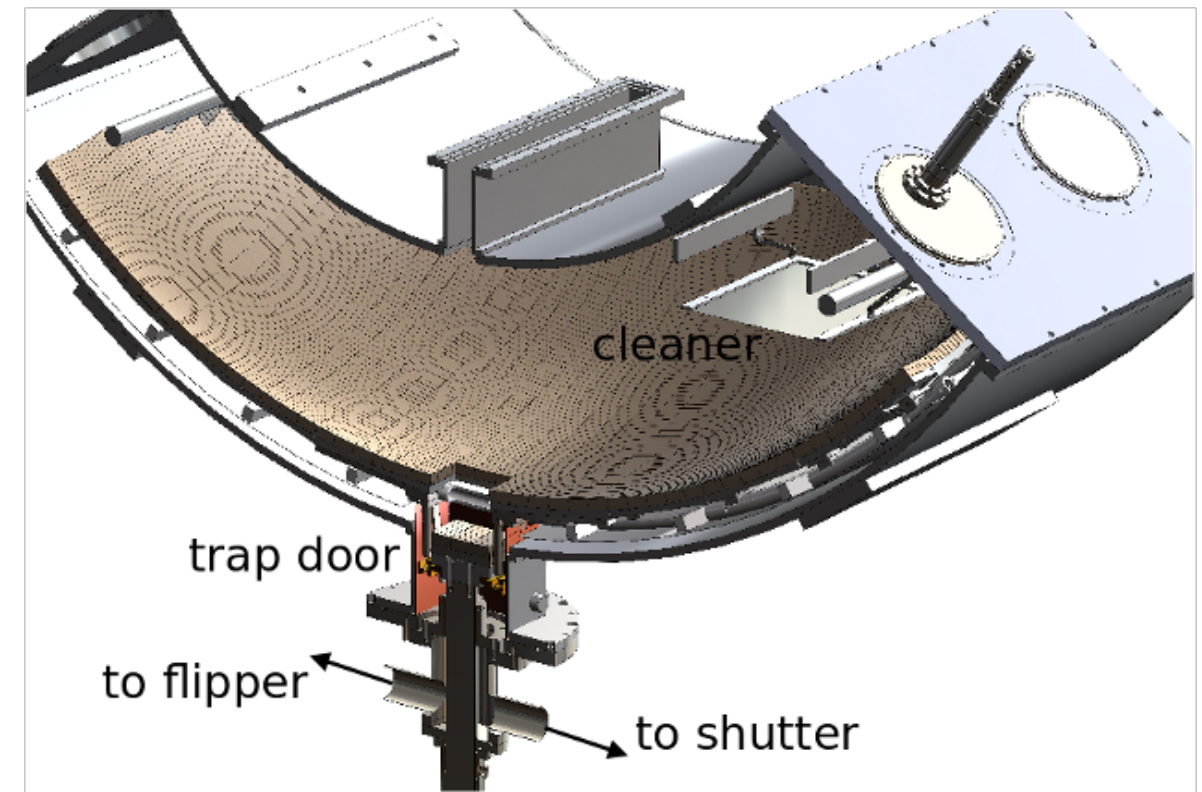
Phase III: Atomic source R&D



Neutral particle traps



ALPHA Collaboration: Nature Phys 7:558, 2011;
arXiv 1104.4982

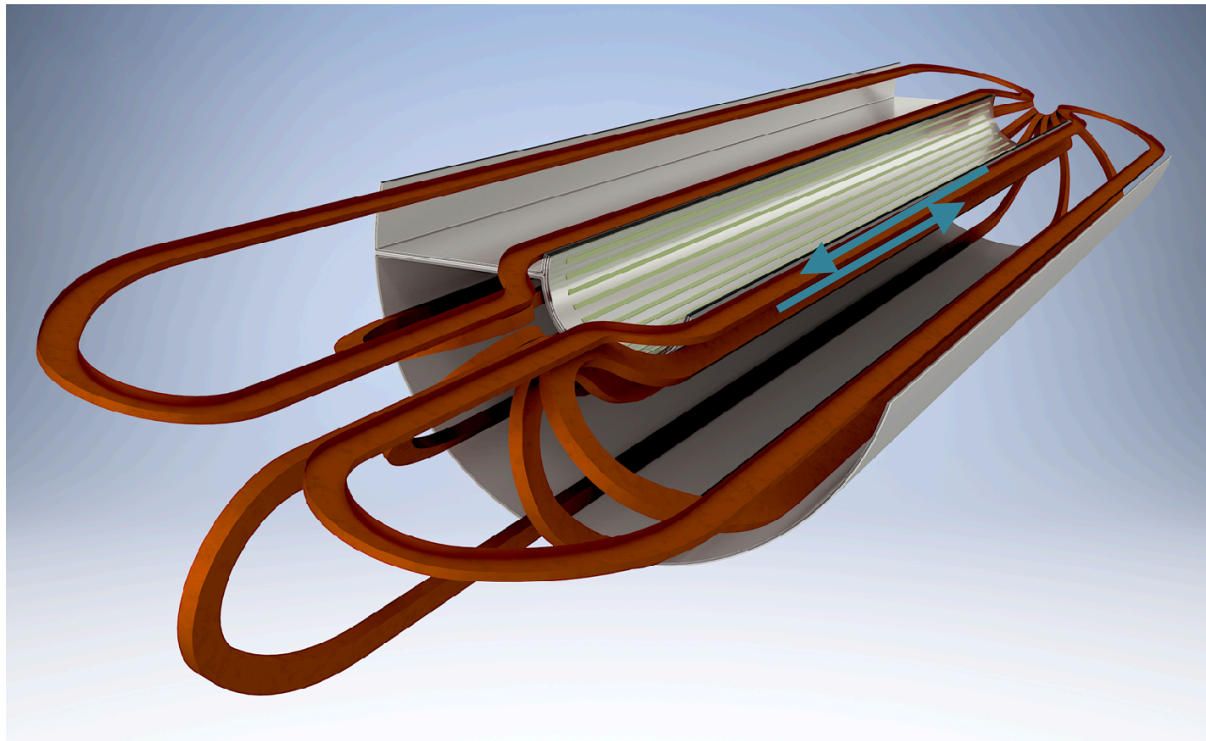


UCNtau Collaboration: Phys Rev C89, 052501, 2014;
arXiv 1310.5759v3

General design

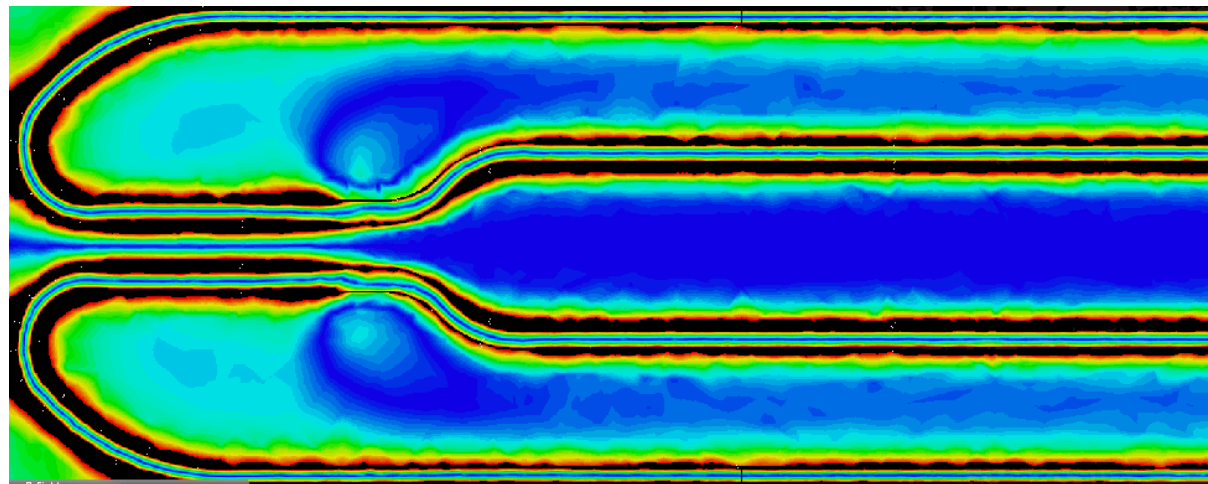
- high magnetic field at walls
- low magnetic fields in the center
 - ▶ near-field to far-field transition with opposing fields

Atom trapping



Ioffe-Pritchard trap

- plausible field step
 - ▶ $\Delta B = 2 \text{ T}$
- limit thermal loss fraction
 - ▶ $\epsilon_{\text{loss}} = 10^{-10}$
- maximum allowed temperature
 - ▶ $T_{\text{max}} = \mathbf{30 \text{ mK}}$



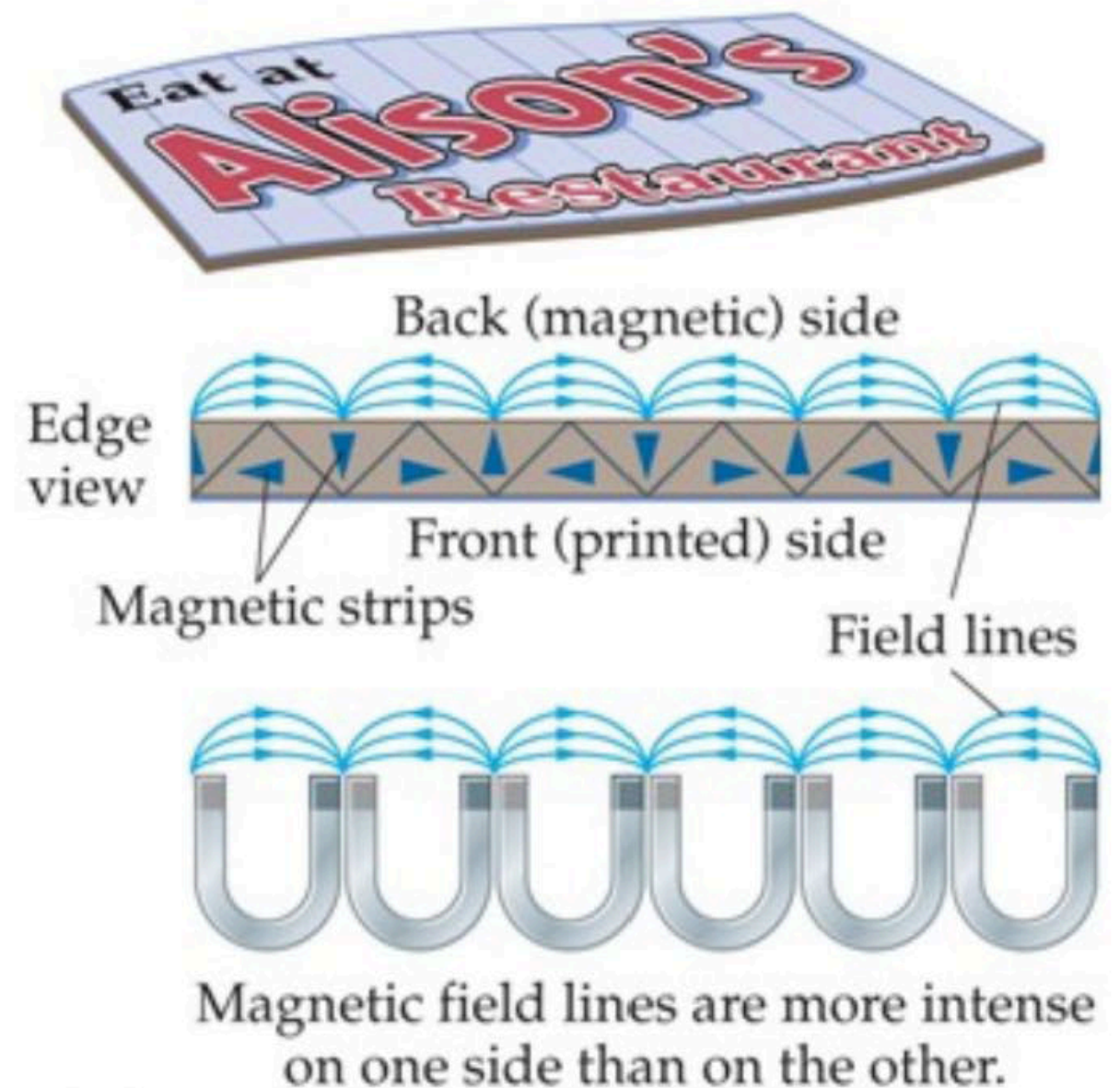
Challenges

- cooling to sub-Kelvin level
- keep high T/T_2 purity
 - ▶ molecular T_2 not trapped!
- field uniformity in central region

Halbach arrays

Permanent magnet configuration

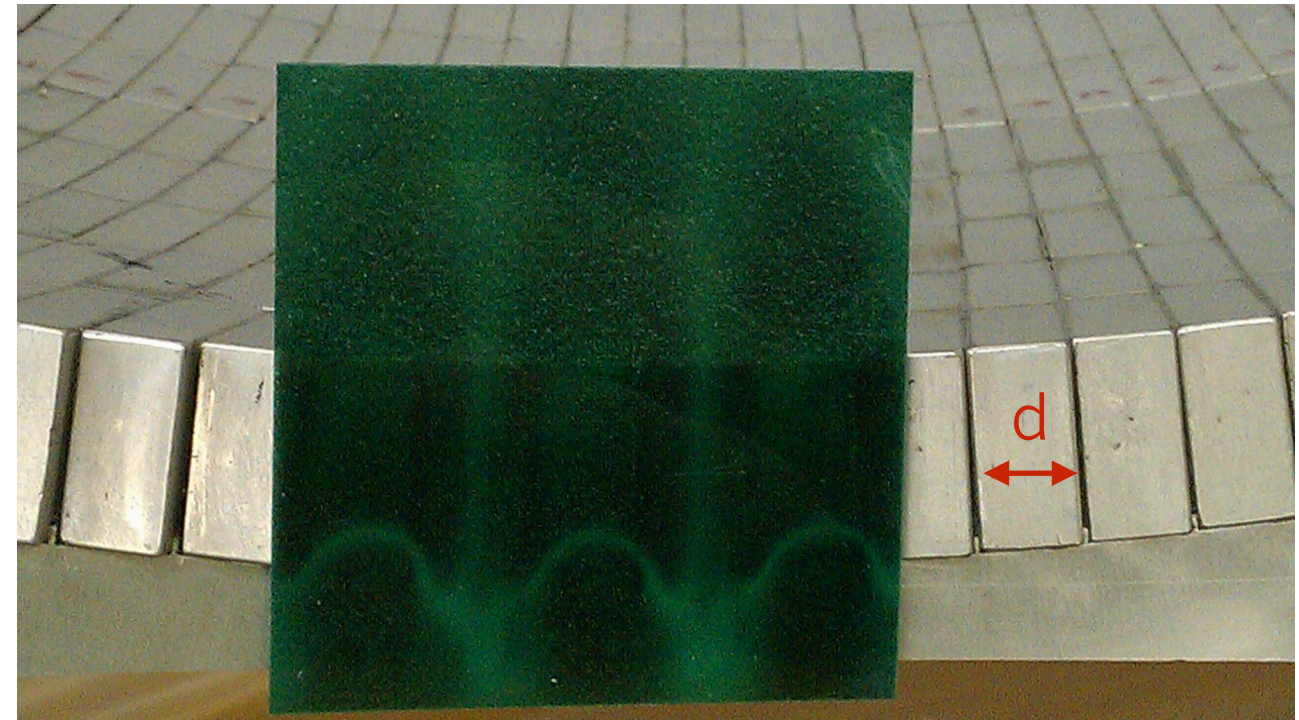
- alternate orientations
- circular flux configuration
 - ▶ one “*magnetic*” side
 - ▶ one “*non-magnetic*” side



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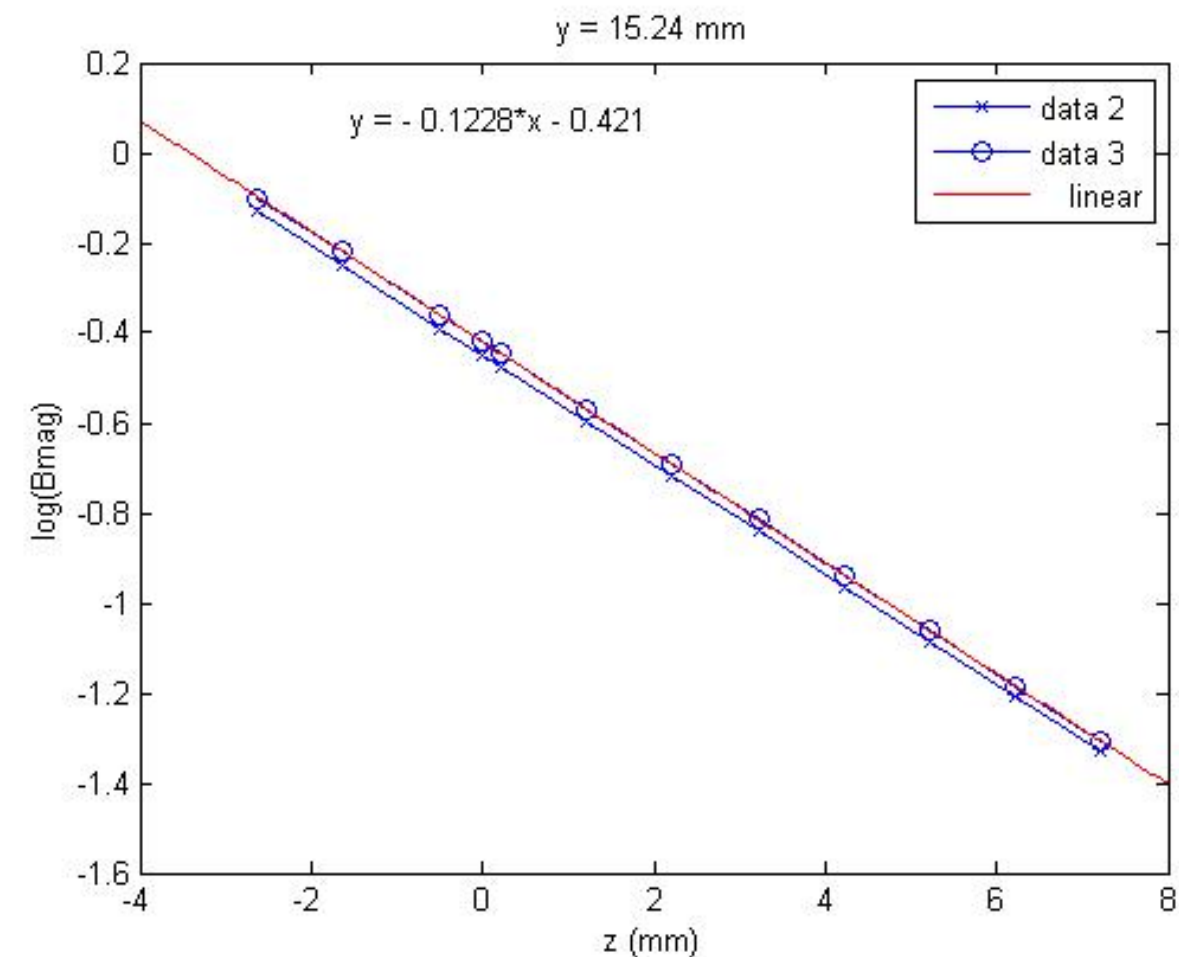
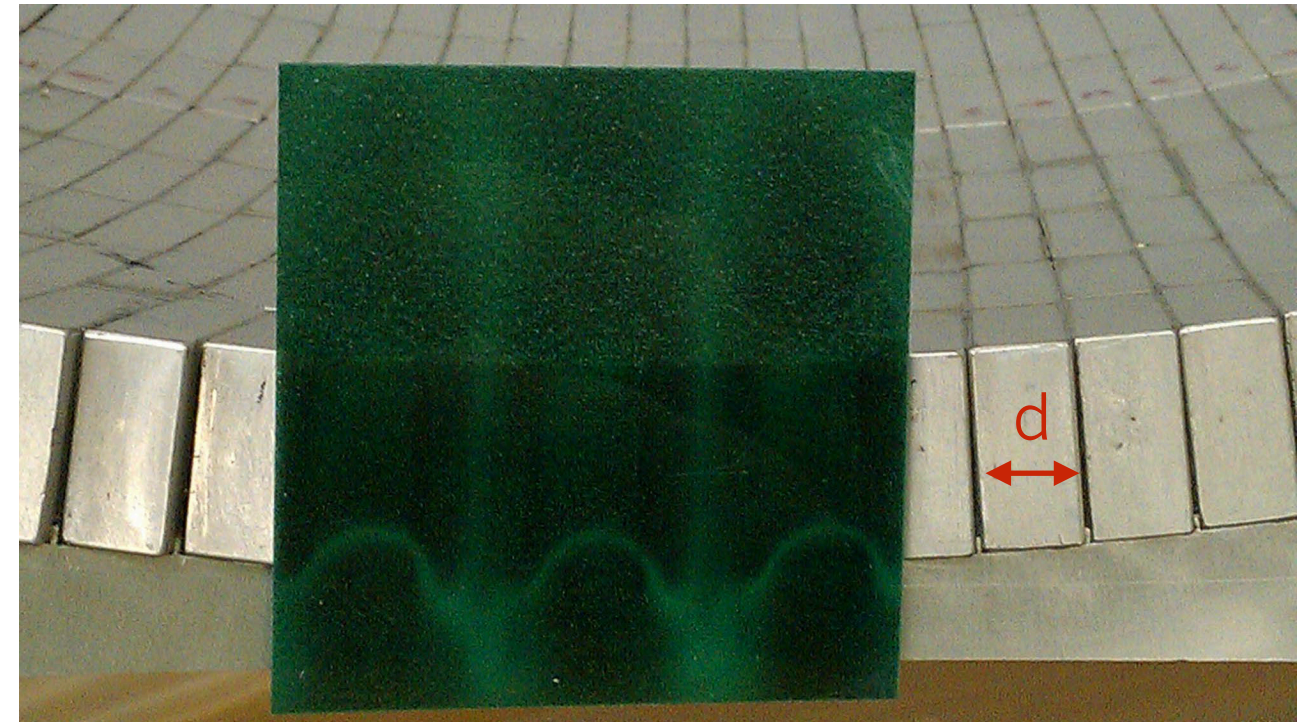
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Flat Halbach array

- field falls exponentially with characteristic length $l = \frac{2d}{\pi}$
 - ▶ weak far field

Challenges

- low temperatures
- overall field strength → evaporative loss



Magneto-gravitational trap

Magnetic trapping

- $E_m = \mu_B B = 58 \mu\text{eV/T}$

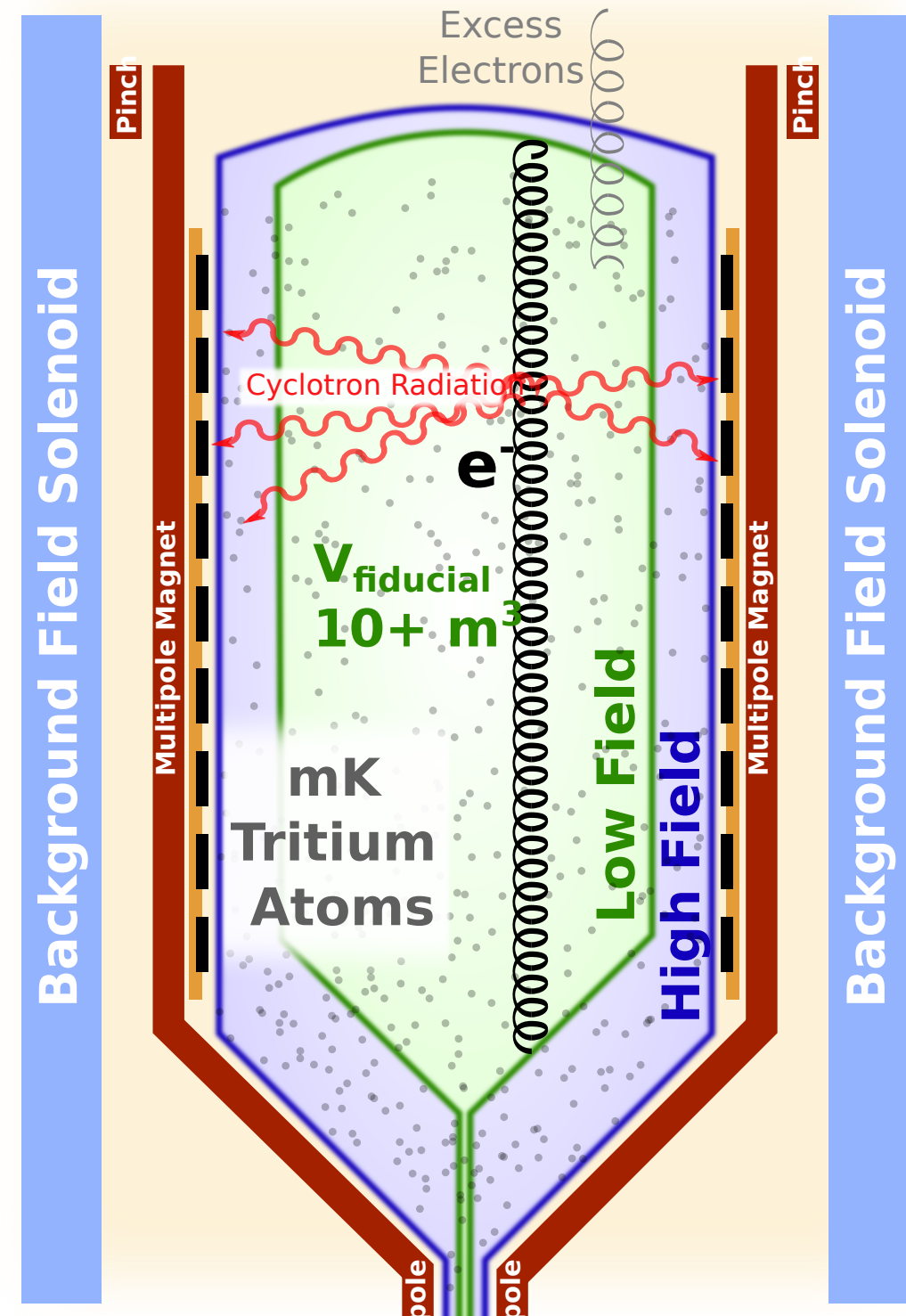
Energy of cold atomic beam

- $E_k = k_B T = 64 \mu\text{eV/K}$

Gravitational trapping

- $E_g = mgh = 0.3 \mu\text{eV/m}$

→ For 10mK cold beam, it takes 2.1 meters of gravity and 0.7T of B-field to trap.

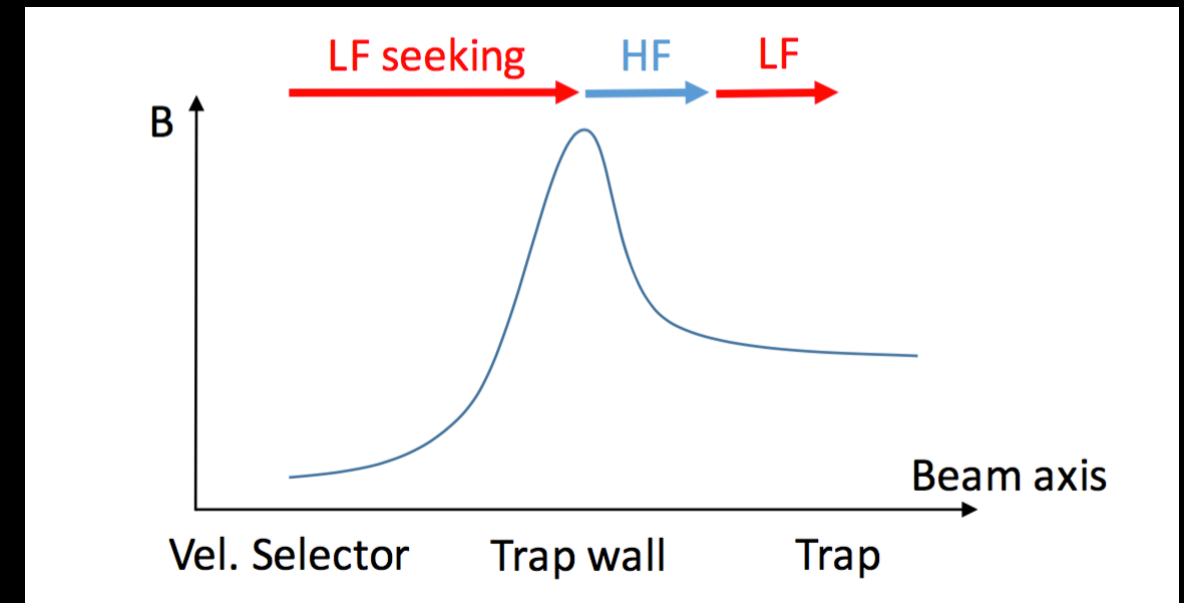


How to fill the trap?

How to fill the trap?

Spin-flip loading ?

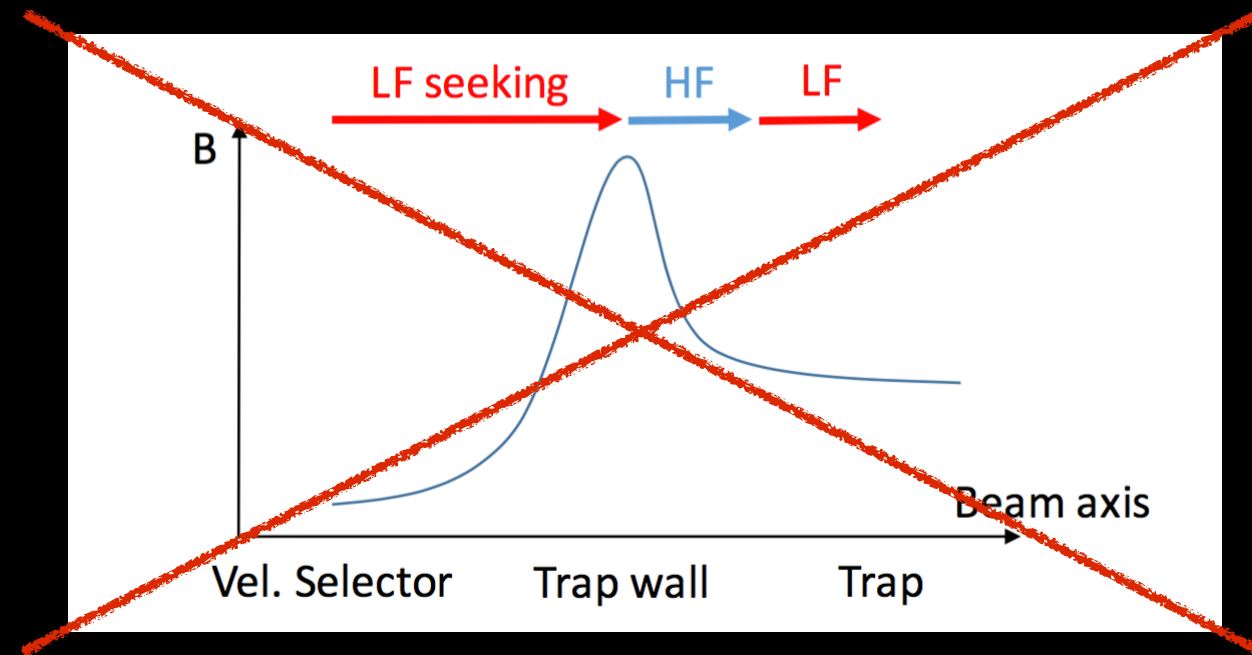
- Flip atom spin at trap edge
 - ▶ Carry atoms over potential wall (+ energy loss)
- But: stimulated emission
 - ▶ will lose trapped atoms



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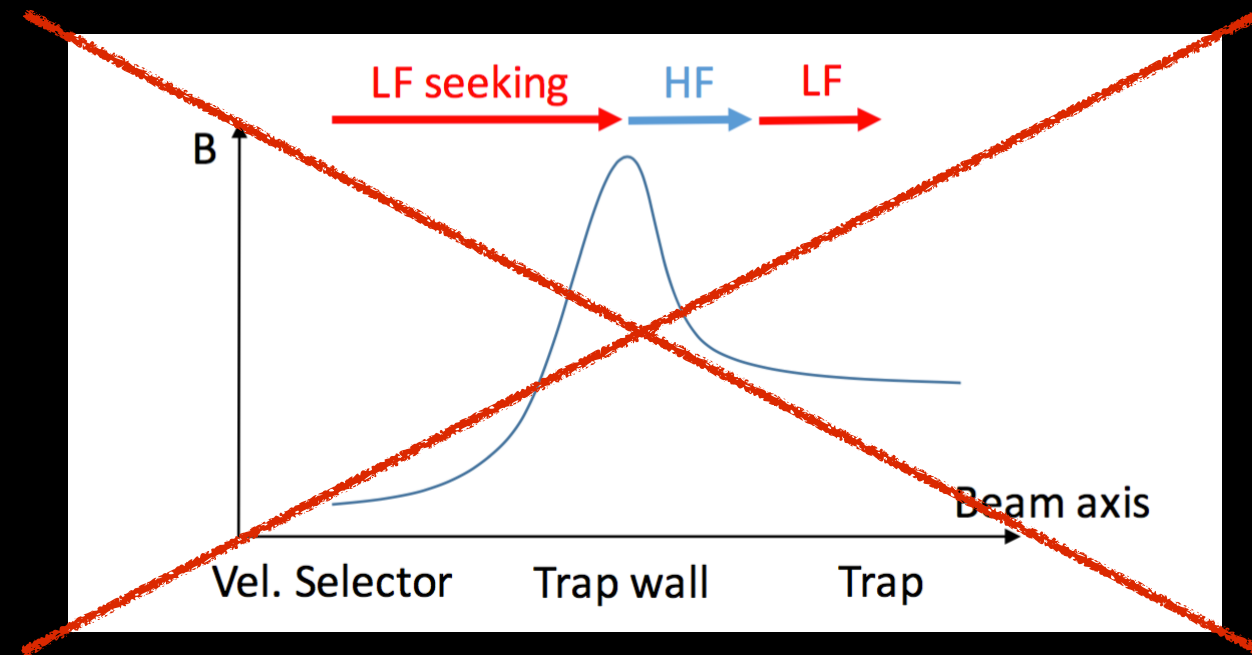
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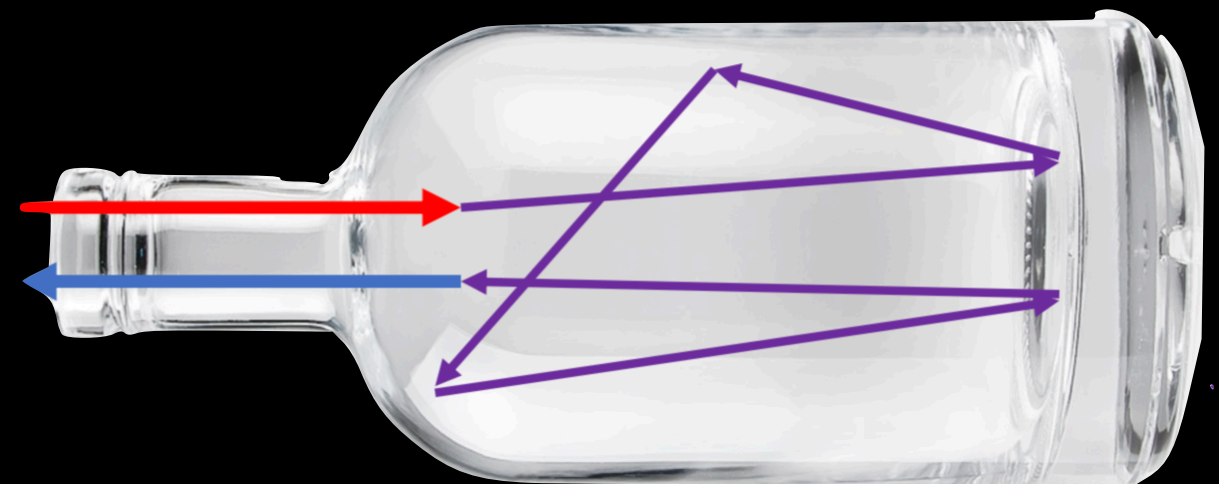
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Cornucopia* loading

- Blow cold atoms into trap
 - accept loss through entrance hole
- required input flux for 1cm hole @ 50mK
 - ▶ $5 \cdot 10^{12}$ atoms/sec

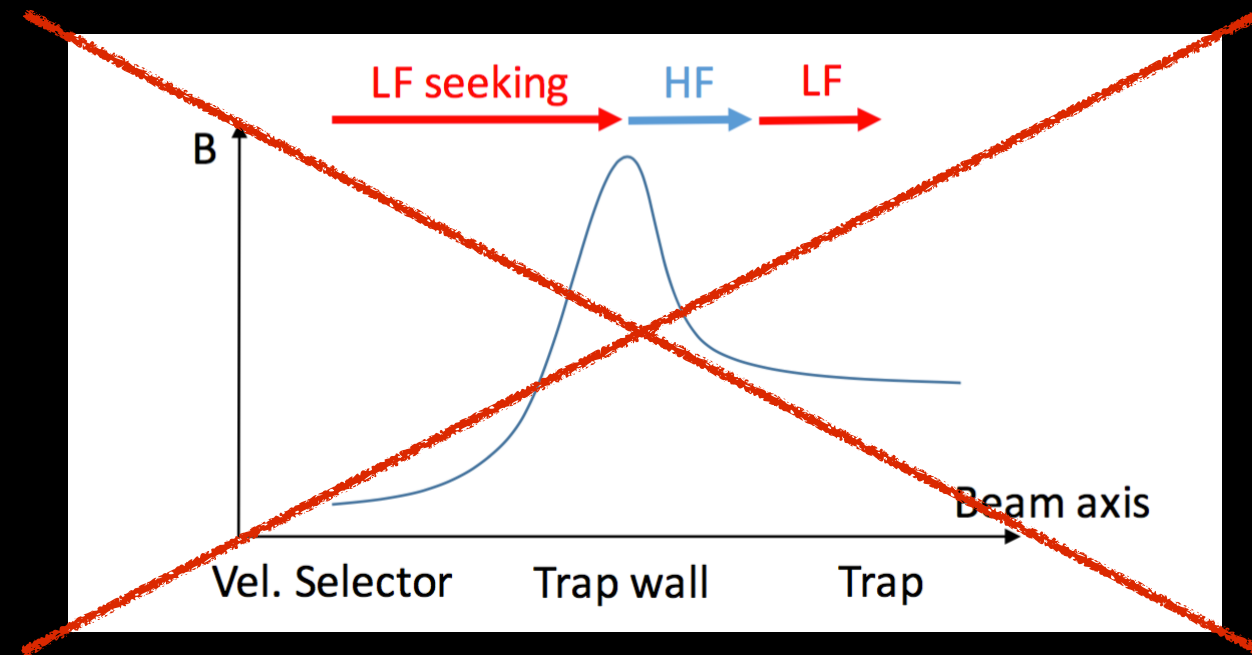


* horn of plenty

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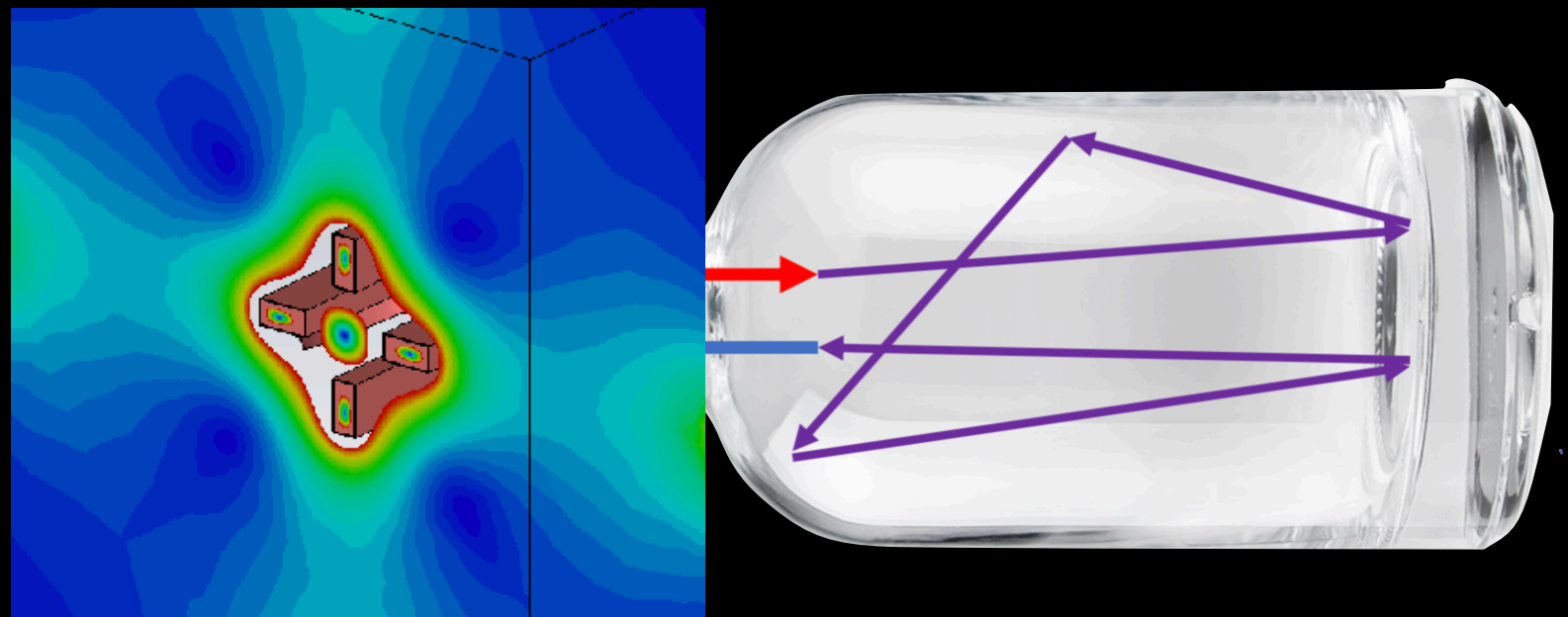
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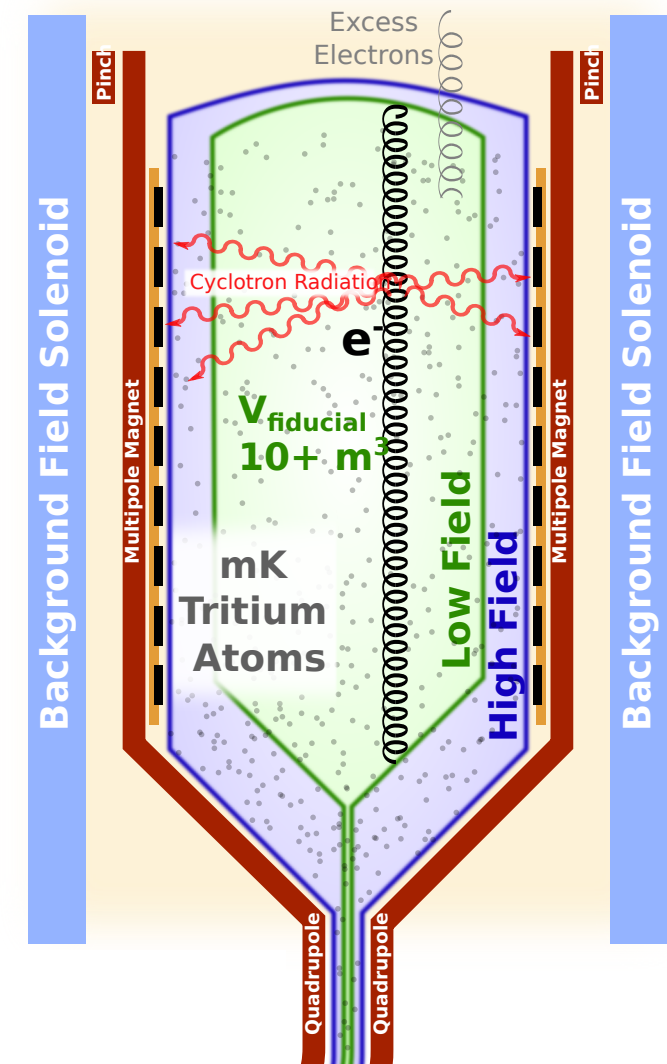
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Project 8: Designs concepts

Atomic T source

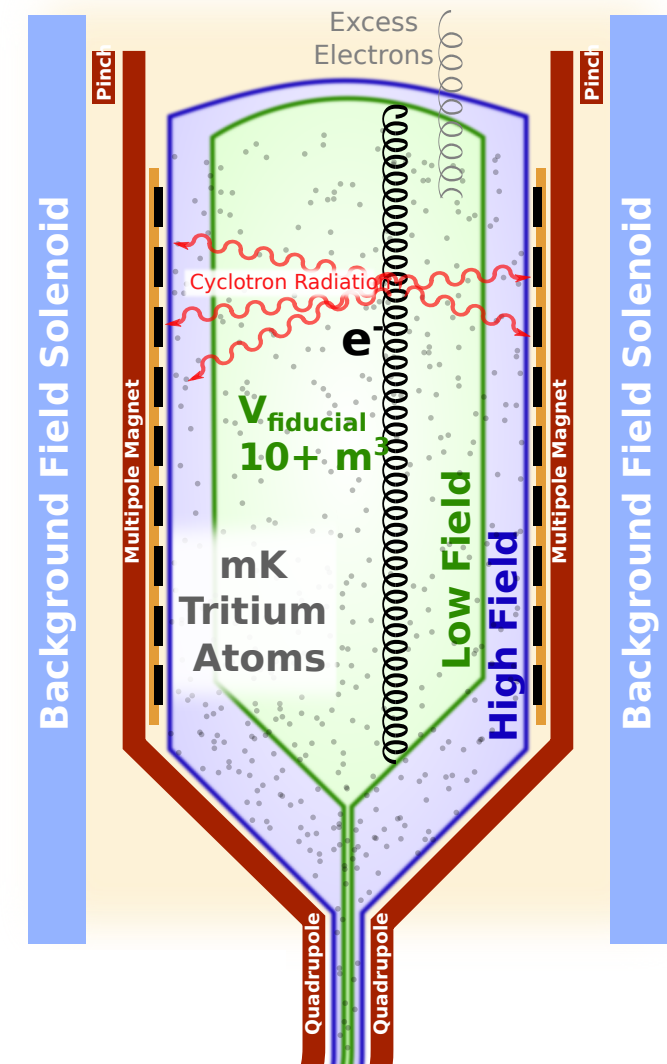
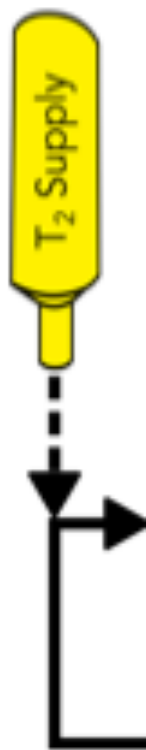
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Atomic T source



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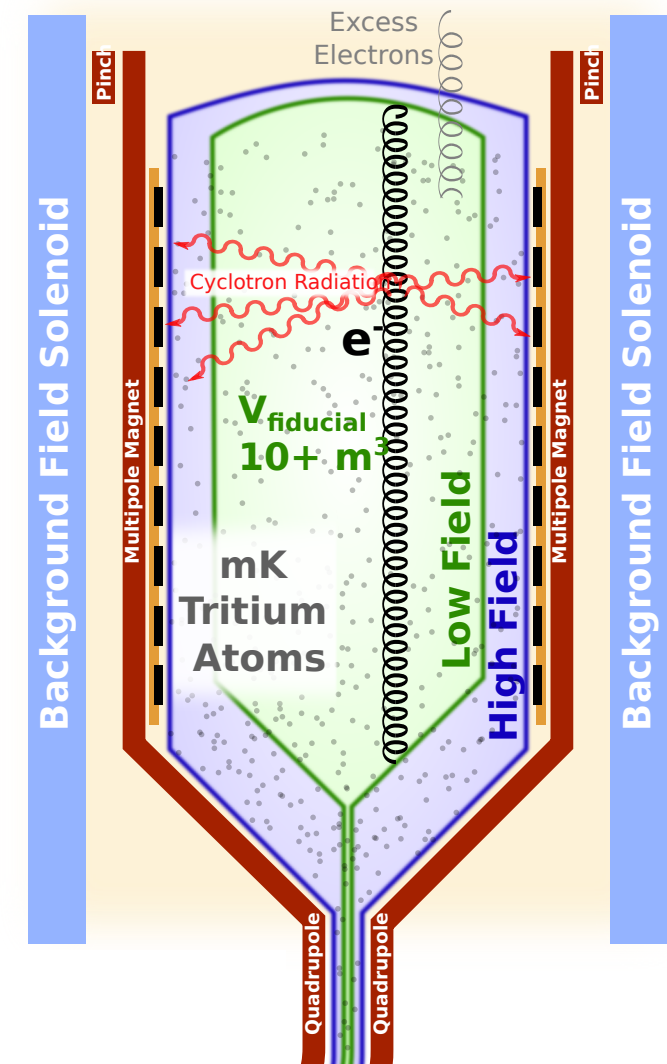
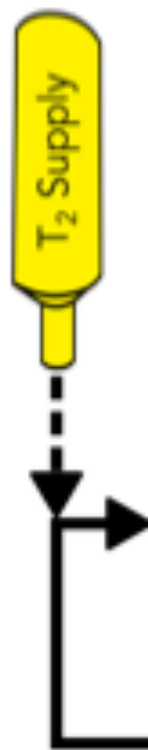
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Project 8: Designs concepts

Atomic T source

- Injection ✓
- Trapping ✓



Project 8: Designs concepts

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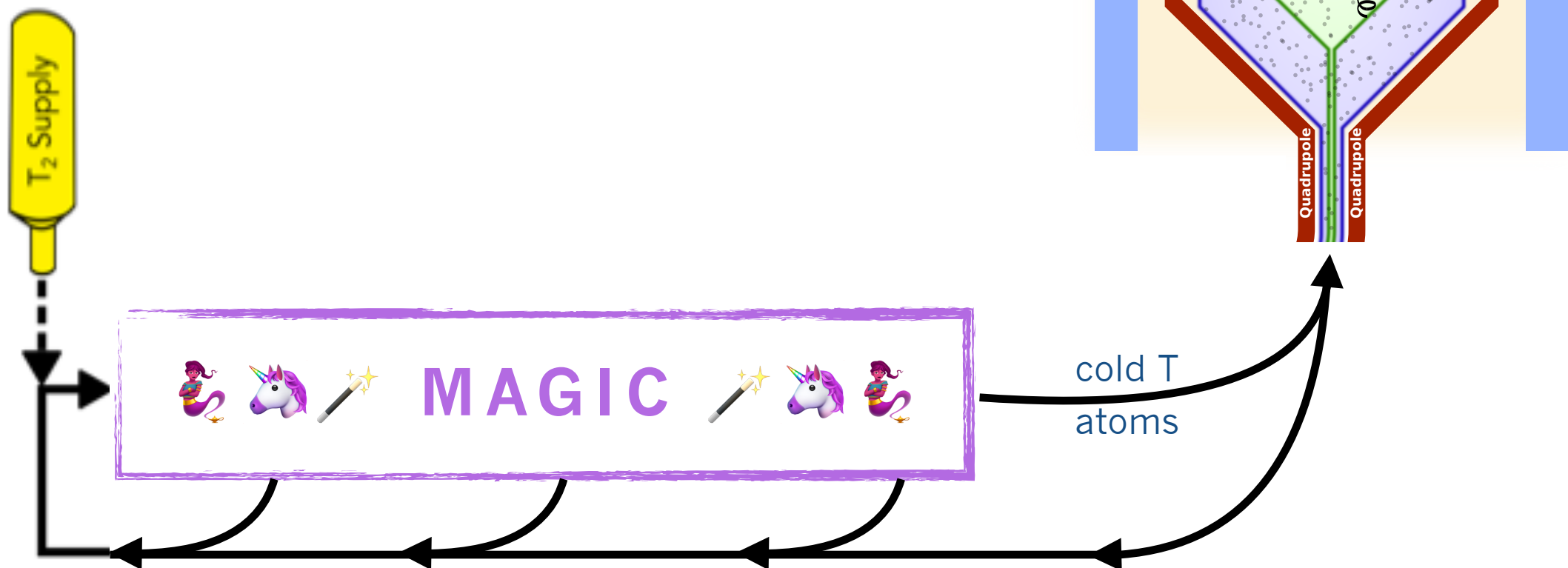
- Dissociation ???
- Cooling ???
- Injection ✓
- Trapping ✓



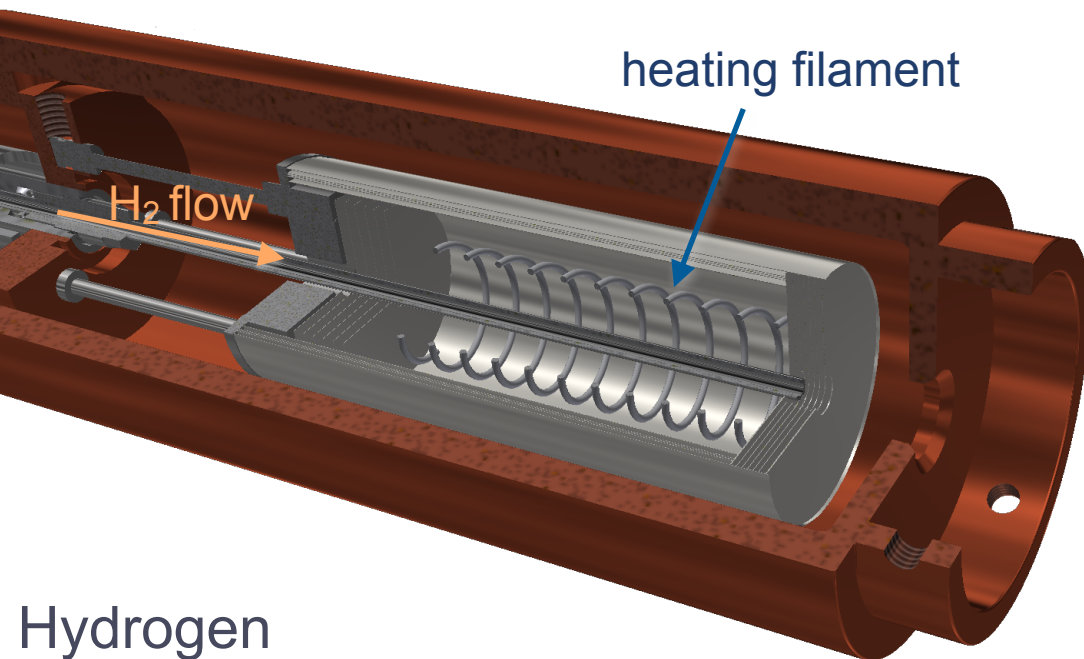
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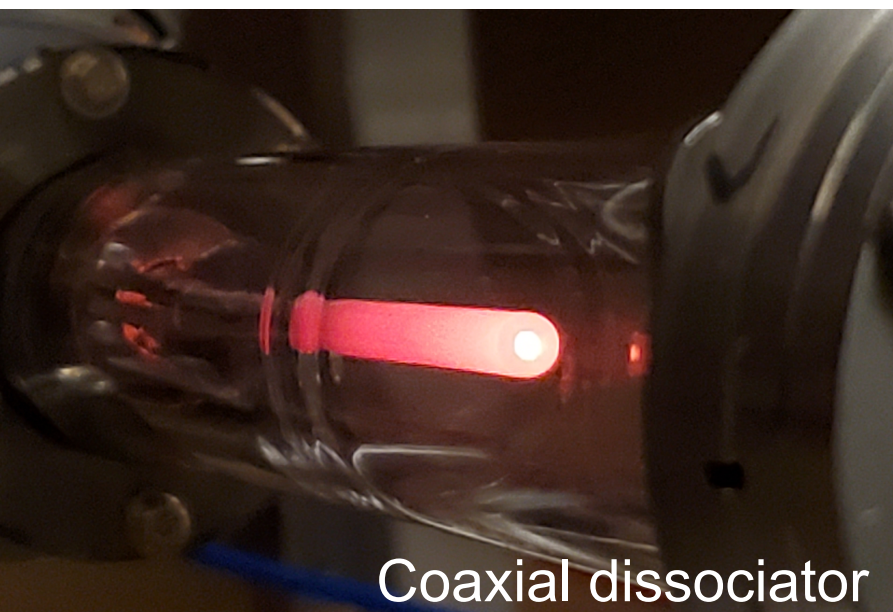
- Dissociation ???
- Cooling ???
- Injection ✓
- Trapping ✓
- Purification/Circulation (✓)



Thermal dissociation sources



Hydrogen
Atom Beam Source (HABS)



Coaxial dissociator

Working principle

- ▶ Dissociation on hot tungsten surface
- ▶ Temperatures 2200K - 2500K
- radiative or electron bombardment heating of capillary

Advantages

- ▶ Several models commercially available
- ▶ Partly well characterised
- MBE components “HABS”
 - Tschersich, K. G. et. al. J. Appl. Phys. 84 (1998), 8, 4065-4070
 - Tschersich, K. G. J. Appl. Phys. 87 (2000), 5, 2565-2573
 - Tschersich, K. G. et. al. J. Appl. Phys. 104 (2008), 034908
- ▶ Principle can be adapted for higher flows

→ Good starting point

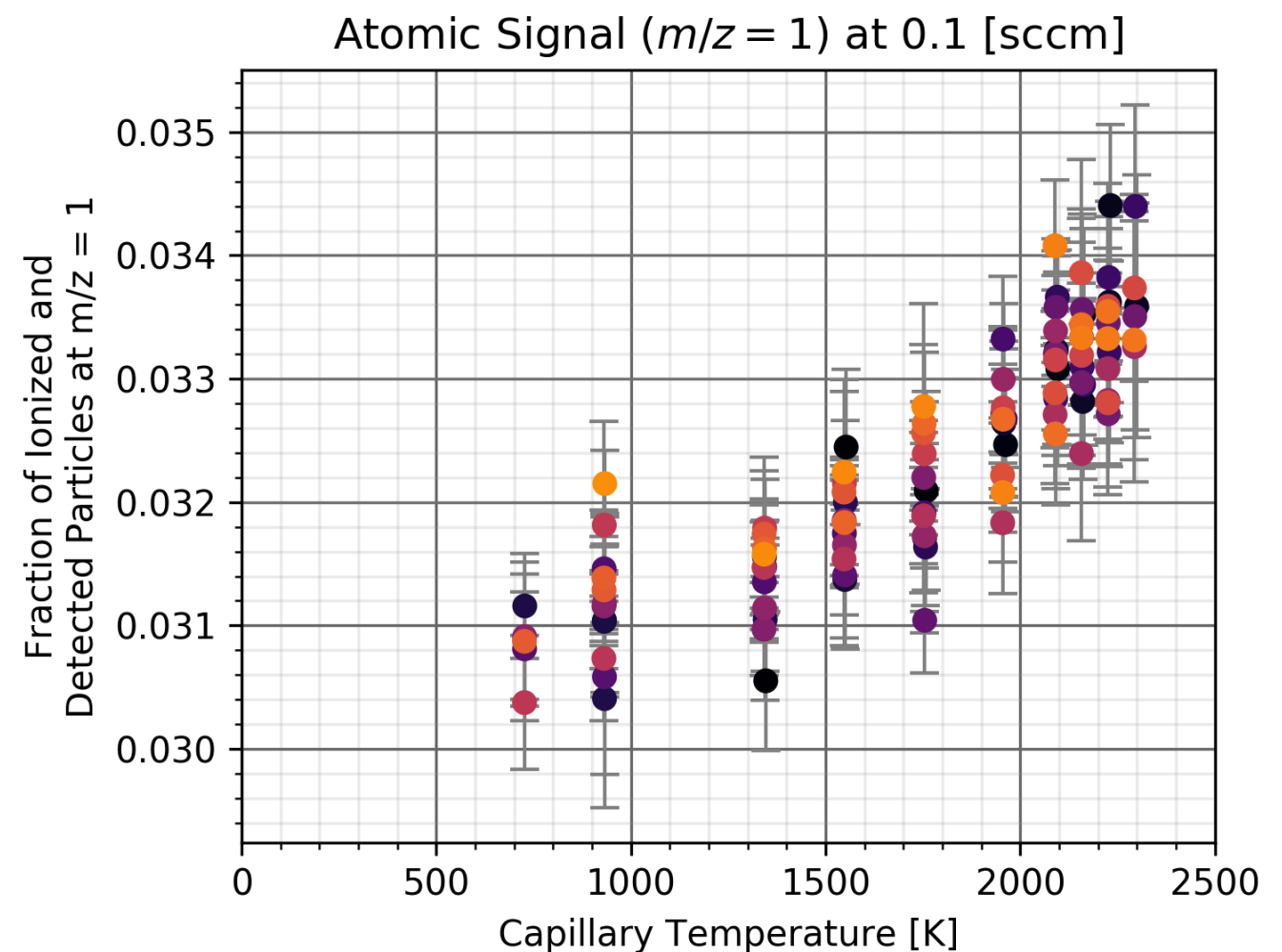
Source characterization

Measure dissociation efficiency

- Detect with ionizing mass spectrometer

Primary challenge

- Dissociative ionization background
 - ▶ $\text{H}_2 + \text{e}^- \rightarrow \text{H}^+ + \text{H} + 2\text{e}^-$
- require very good H_2 suppression
 - ▶ but $\text{H} \rightarrow \text{H}_2$ recombination with efficiency $\varepsilon \sim 1$!



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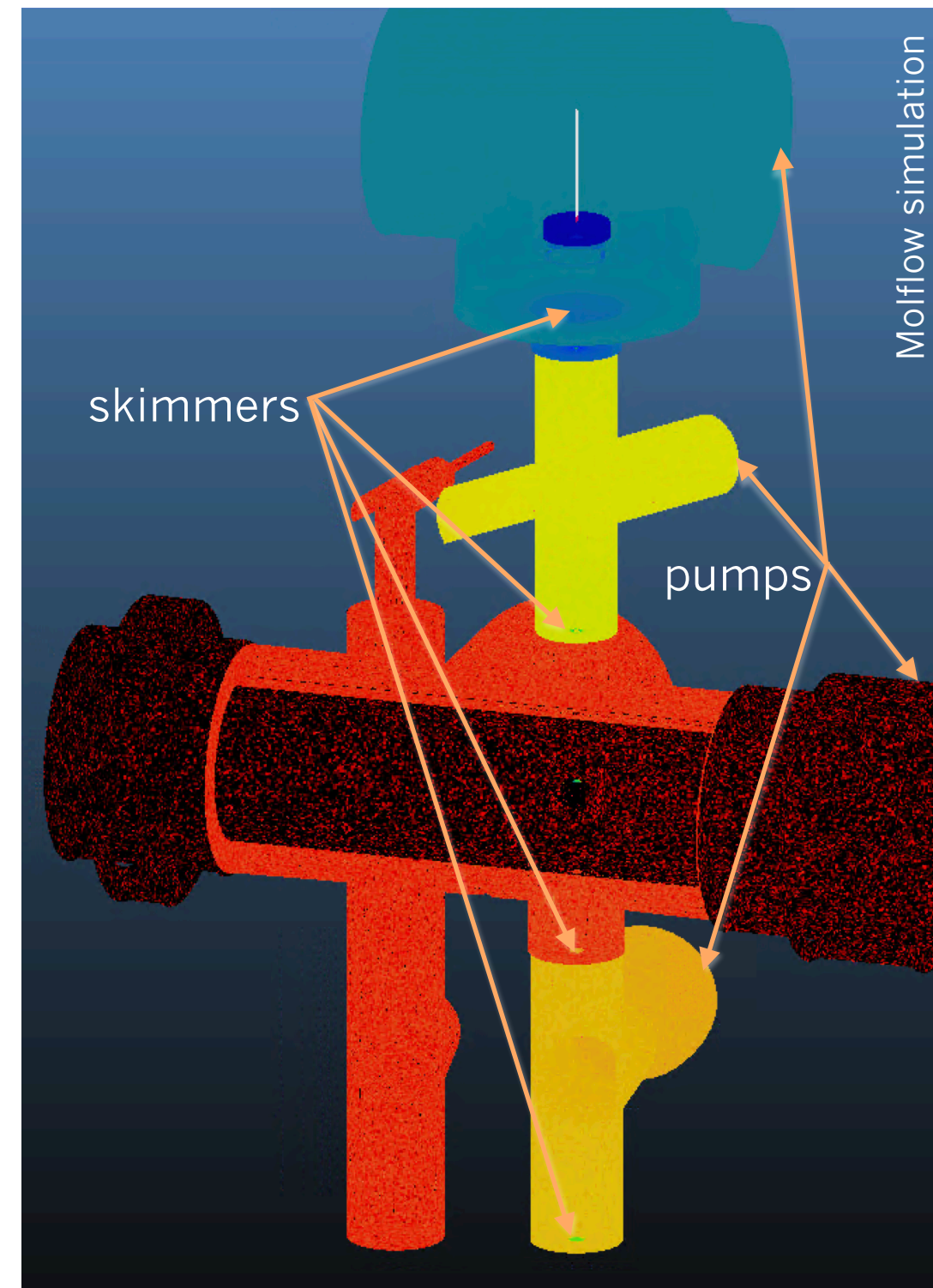
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Differential pumping

- optimized rejection of recombined H_2
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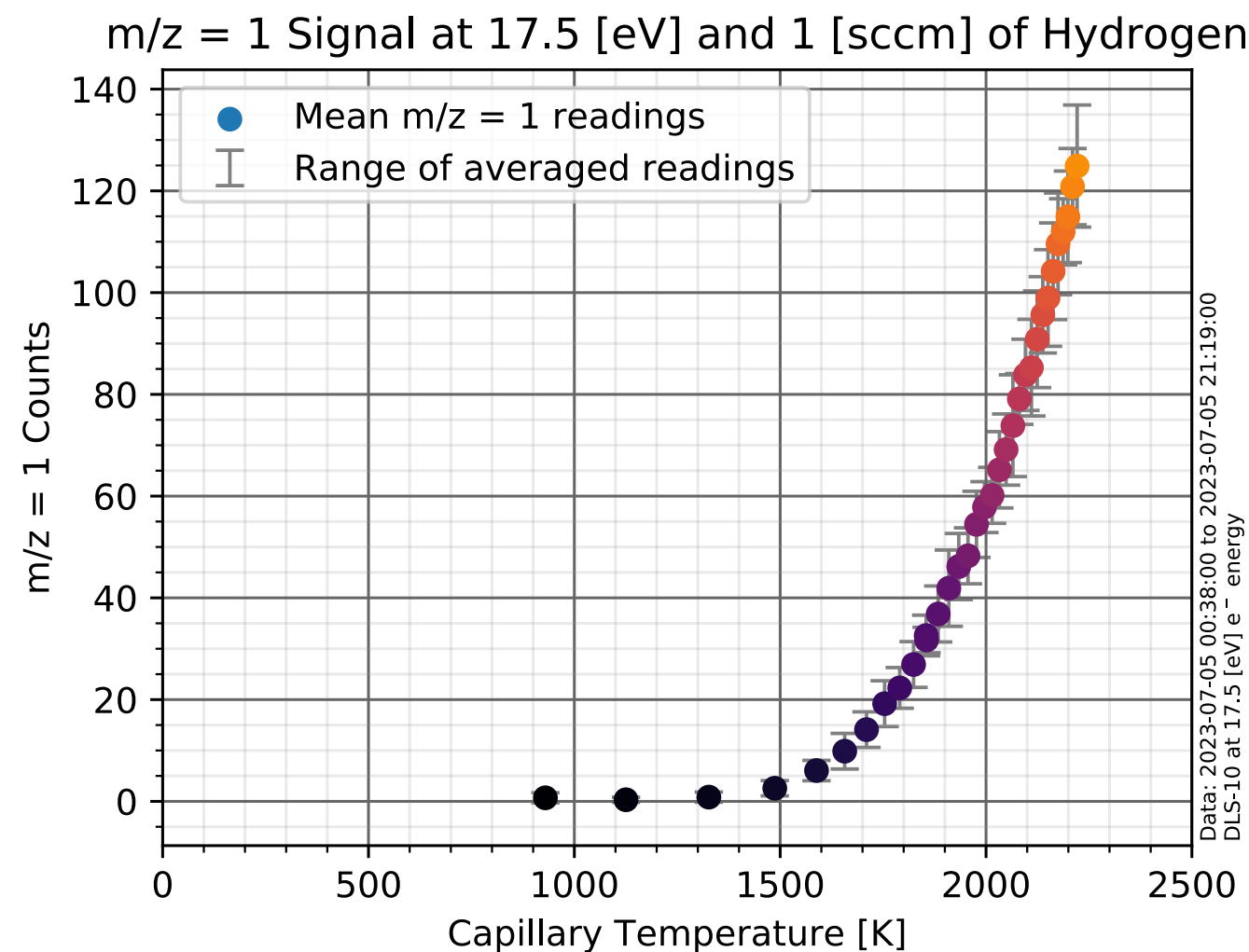
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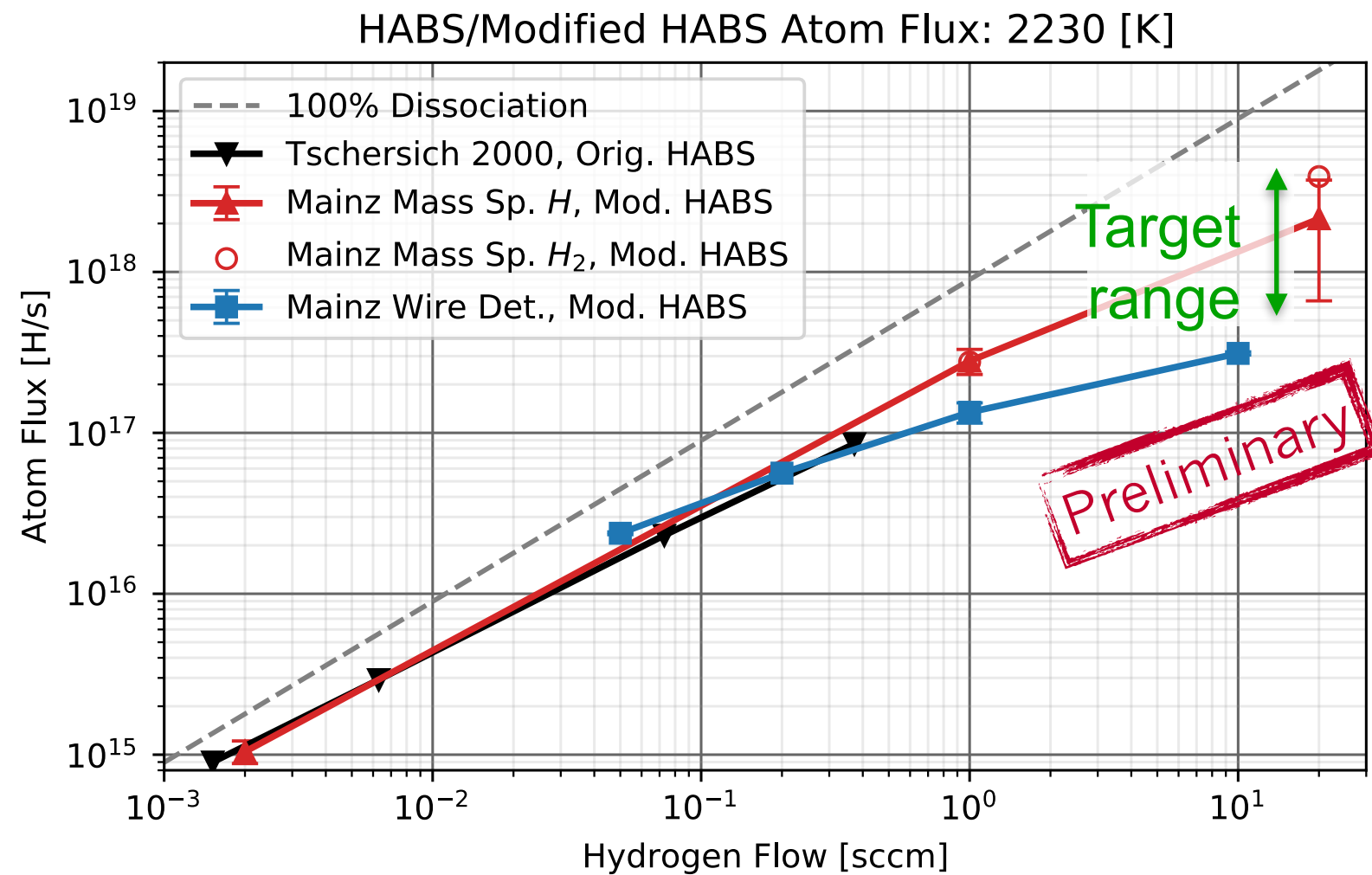
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Hydrogen isotopes

Hydrogen

- Mainz atomic test stand
- ▶ result so far



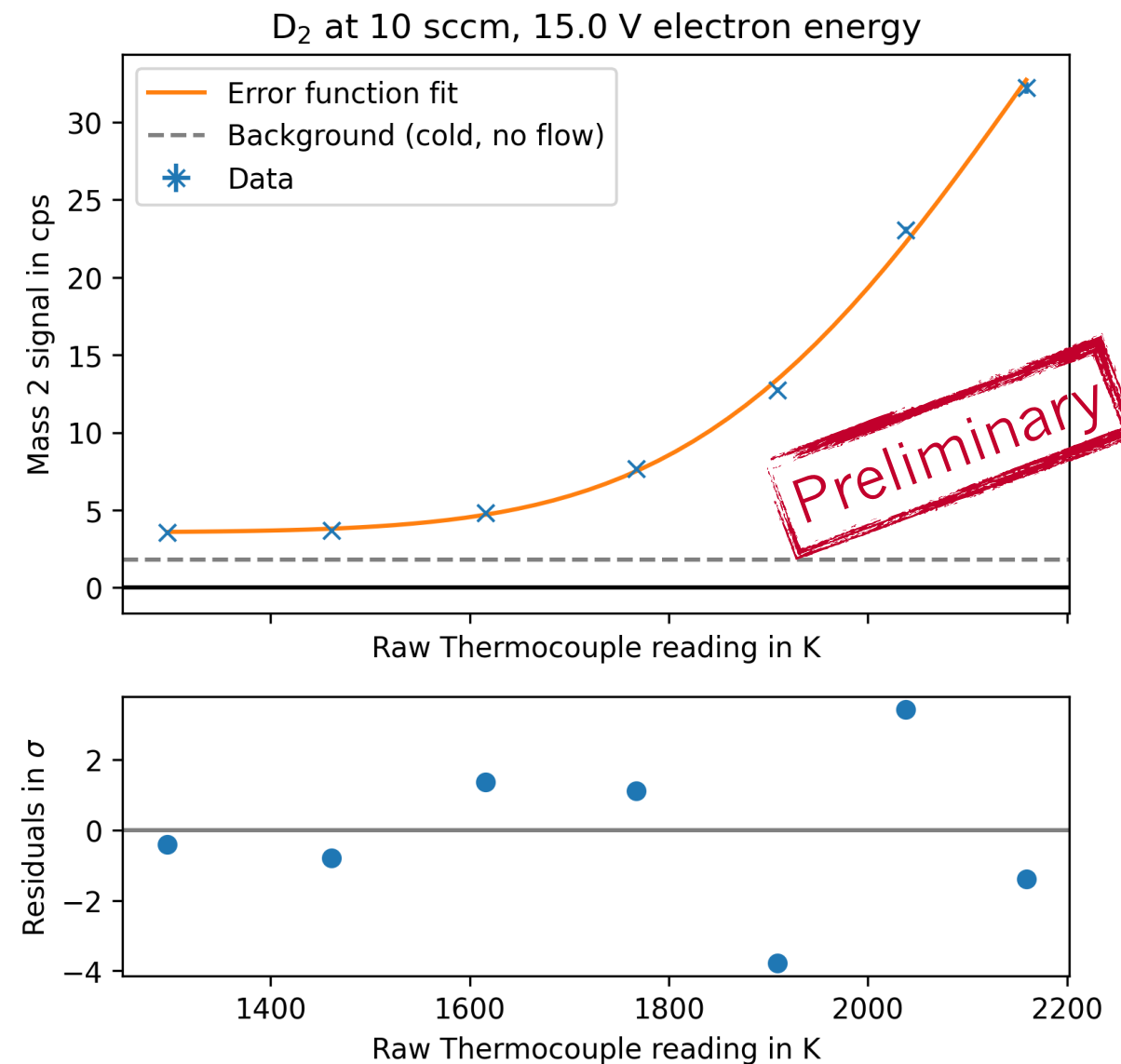
Hydrogen isotopes

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Deuterium

- UW atomic test stand
 - ▶ first dissociation signal



Hydrogen isotopes

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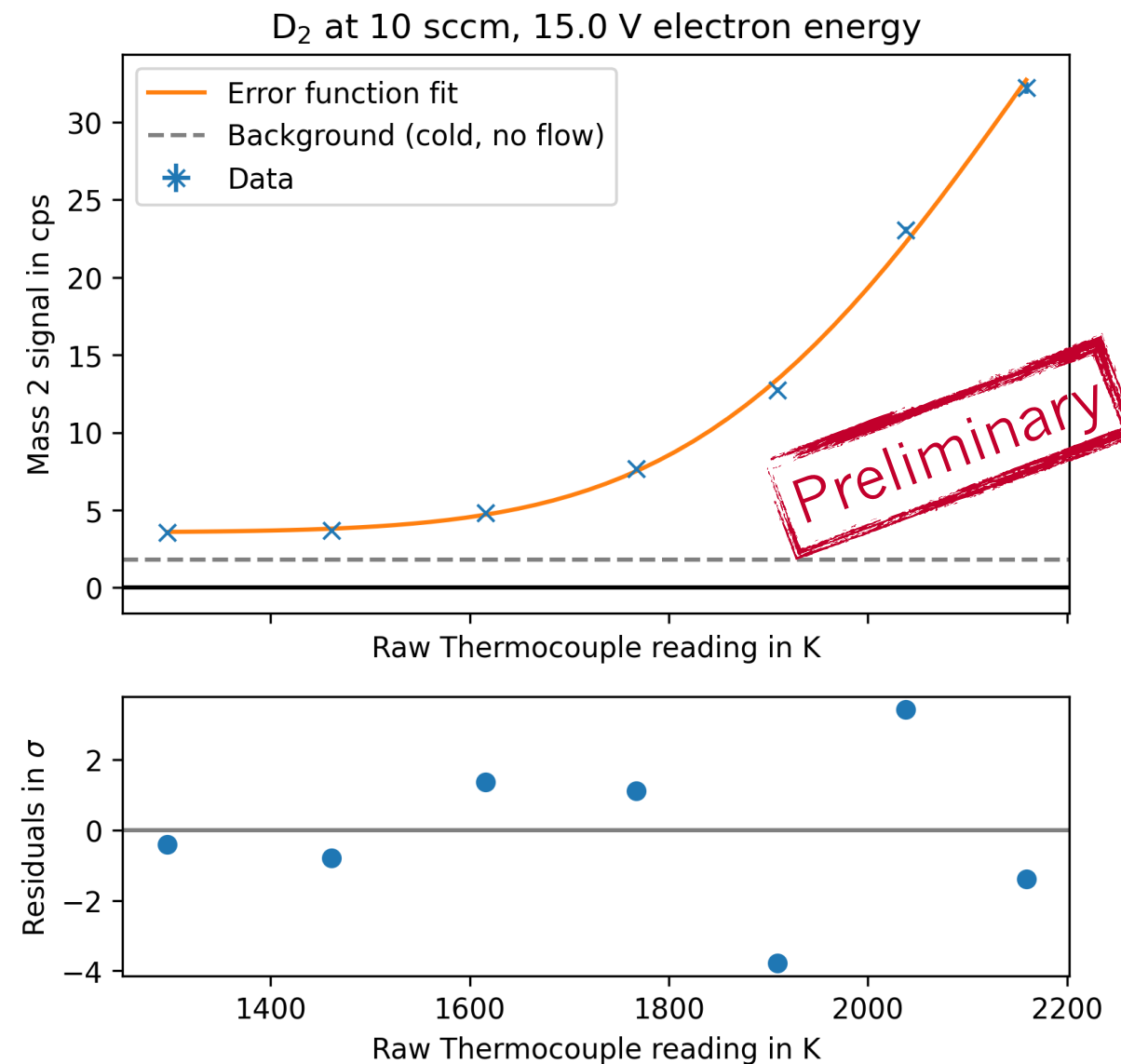
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Tritium

- requires tritium handling facility
 - ▶ joint effort with TLK
“KAMATE”



Cooling tritium atoms

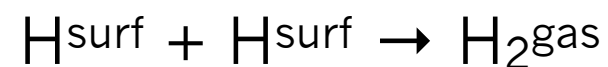
Recombination processes

- Eley– Rideal



- ▶ decreases with T and adsorbed H_{surf}

- Langmuir–Hinshelwood



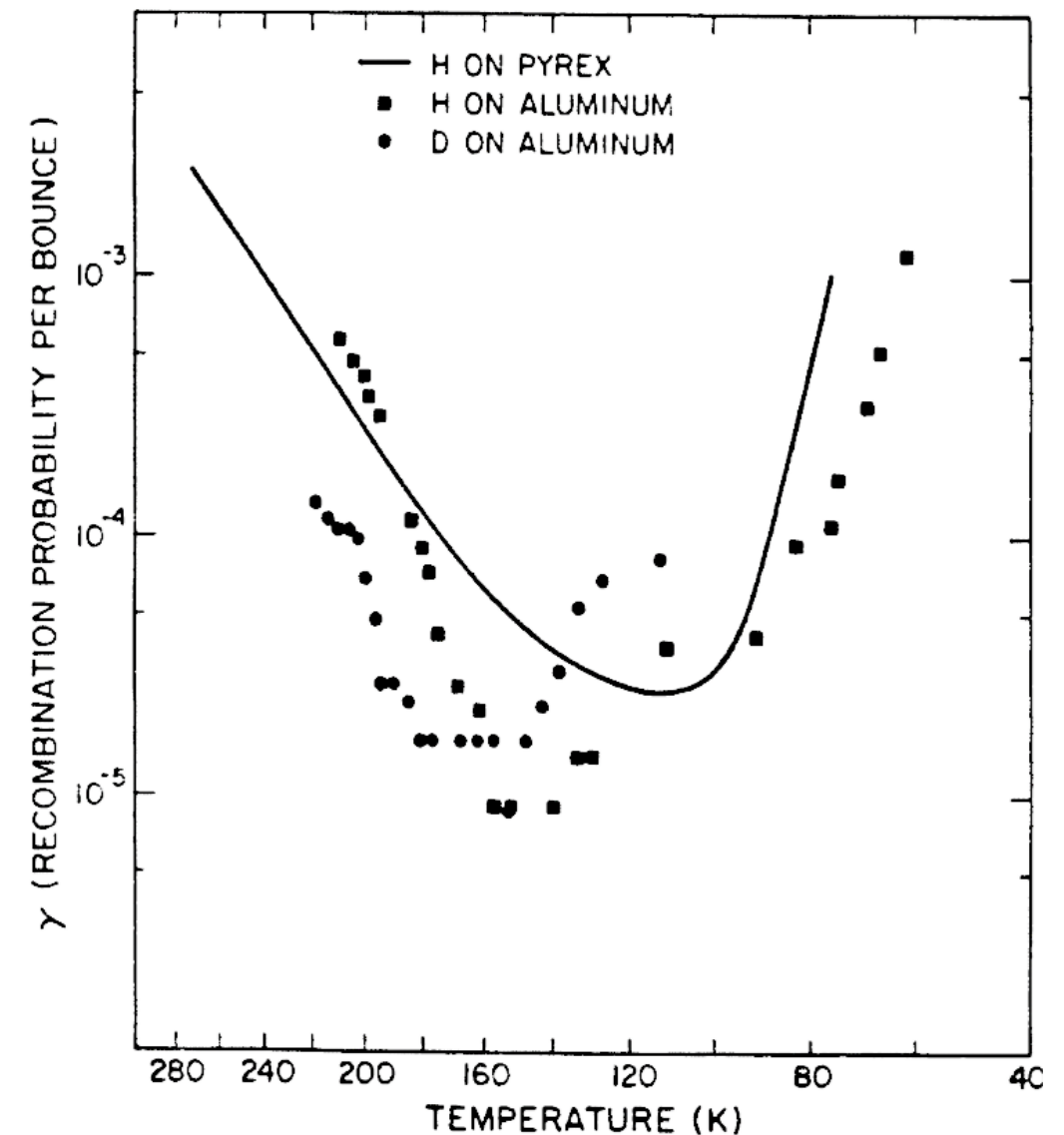
- ▶ increases with H_{surf} mobility

Surface cooling approach

- first step to recombination minimum (100-150 K) → *accomodator*
- second step to freeze-out (10K) with limited wall interactions → *nozzle*

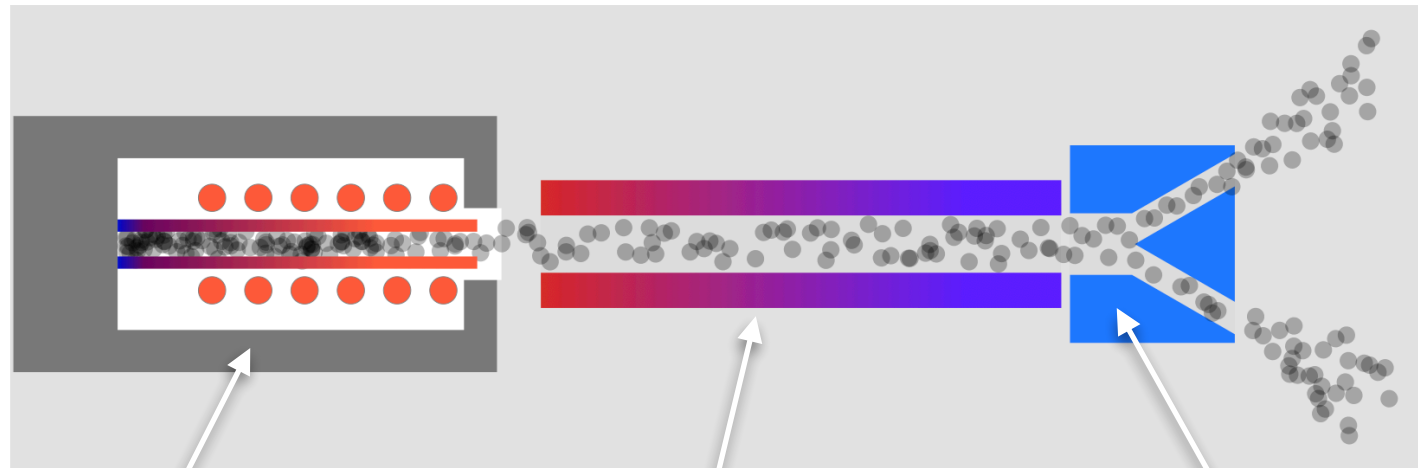
D. A. Knapp et al., AIP conference proceedings (1984)

Wood and H. Wise, J. Chem. Phys. 66, 1049, (1962)



Cooling tritium atoms

Cracker Accommodator Nozzle
2500 K 160 K ~10 K



Cracker

→ purity vs. flow

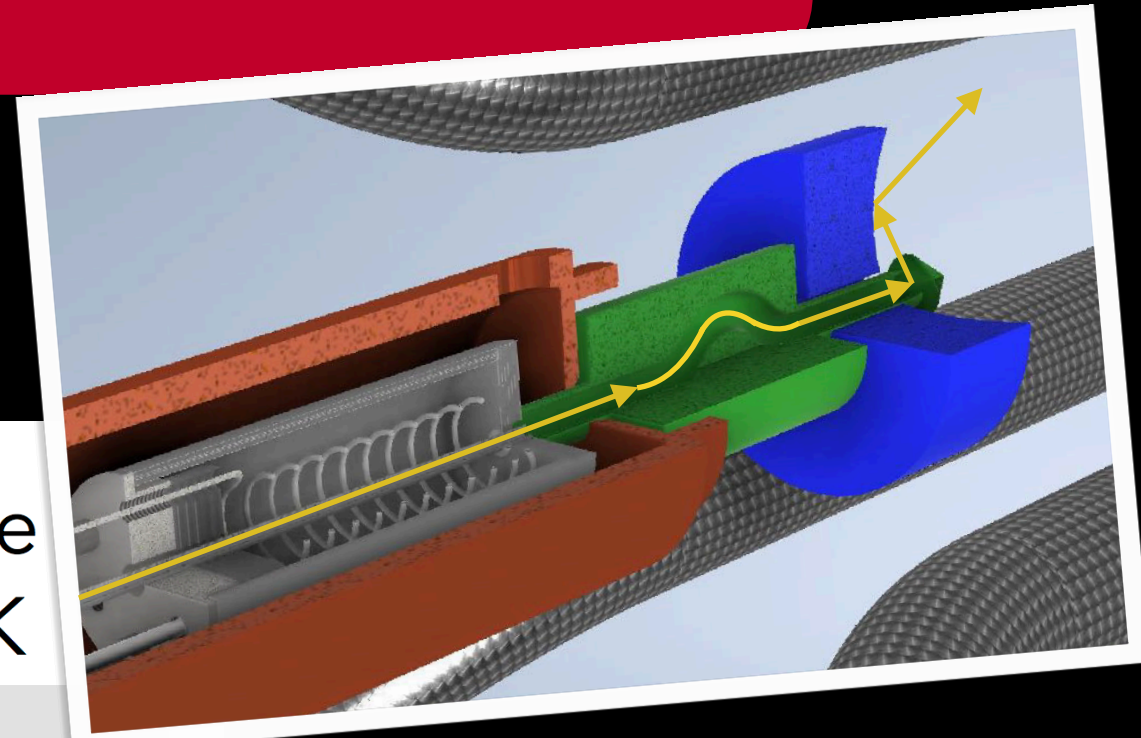
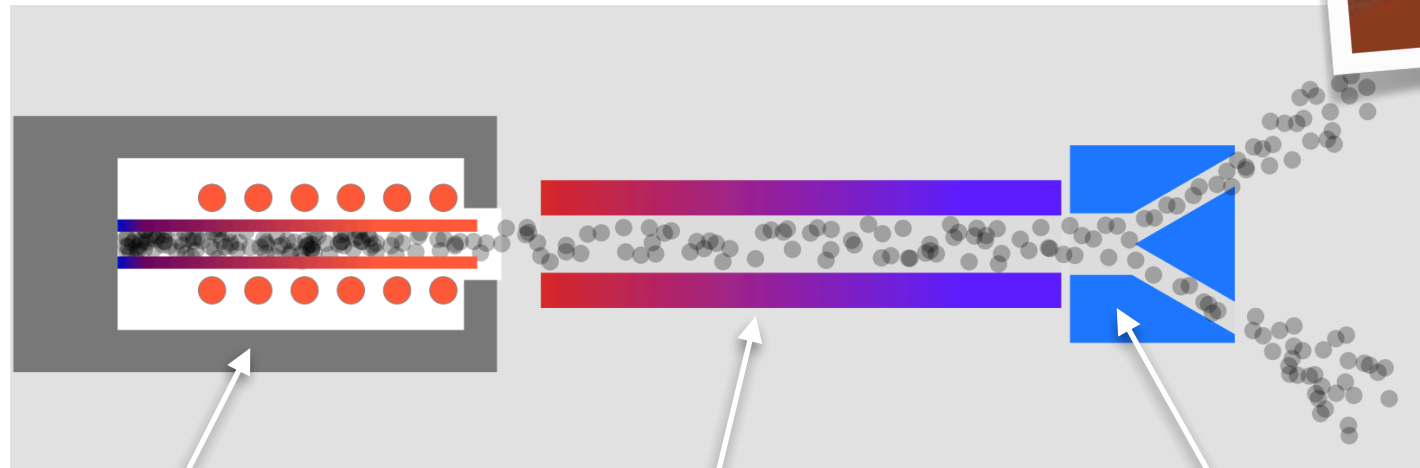
Accommodator
(liquid nitrogen)

Final nozzle

- design for few bounces
- freeze-out 30K
→ periodic purging

Cooling tritium atoms

Cracker 2500 K Accommodator 160 K Nozzle ~10 K



Cracker
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Accommodator
(liquid nitrogen)

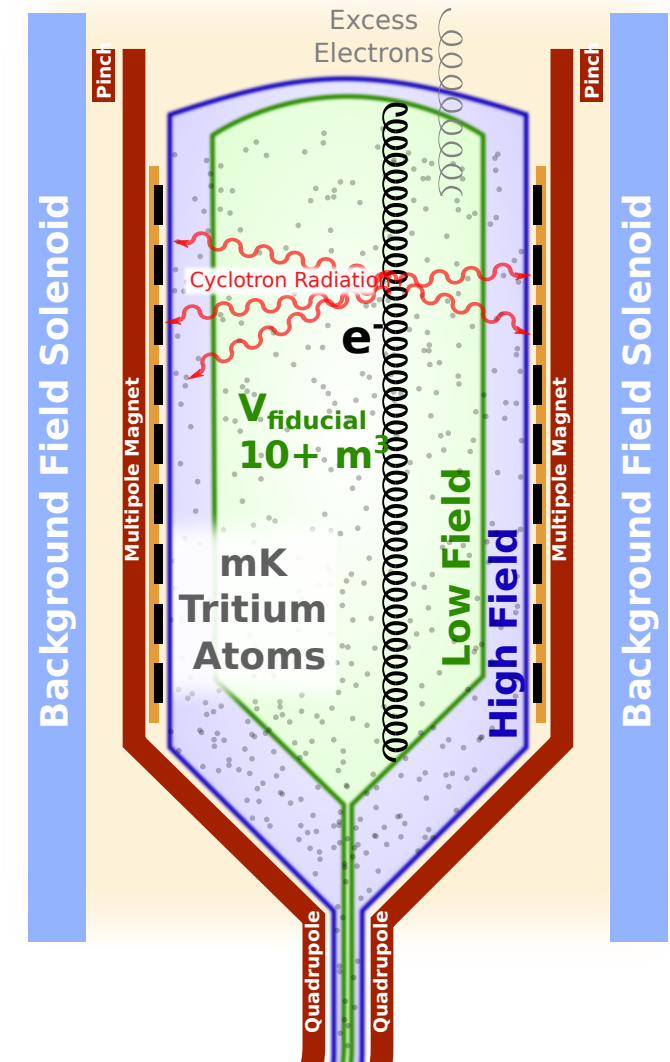
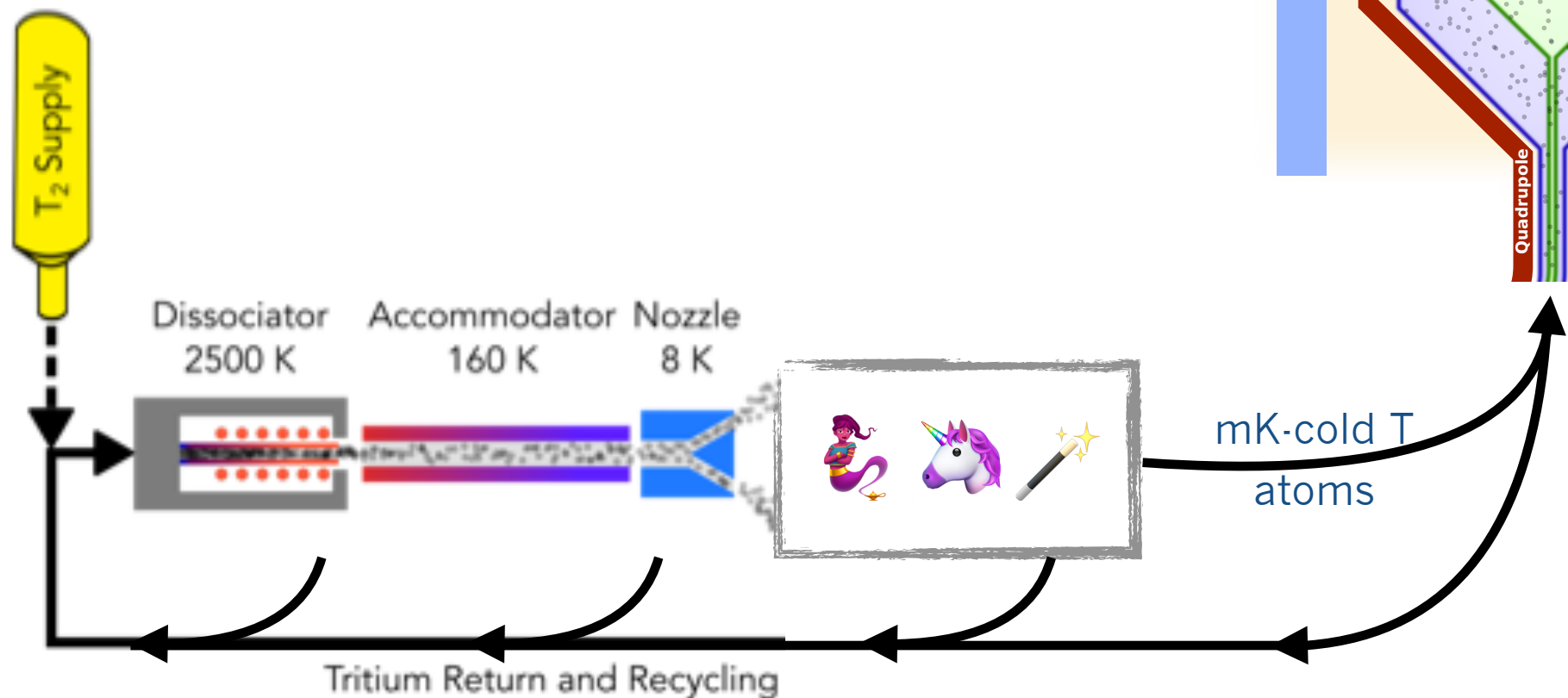
Final nozzle

- design for few bounces
- freeze-out 30K
→ periodic purging

Project 8: Design concepts

Atomic T source

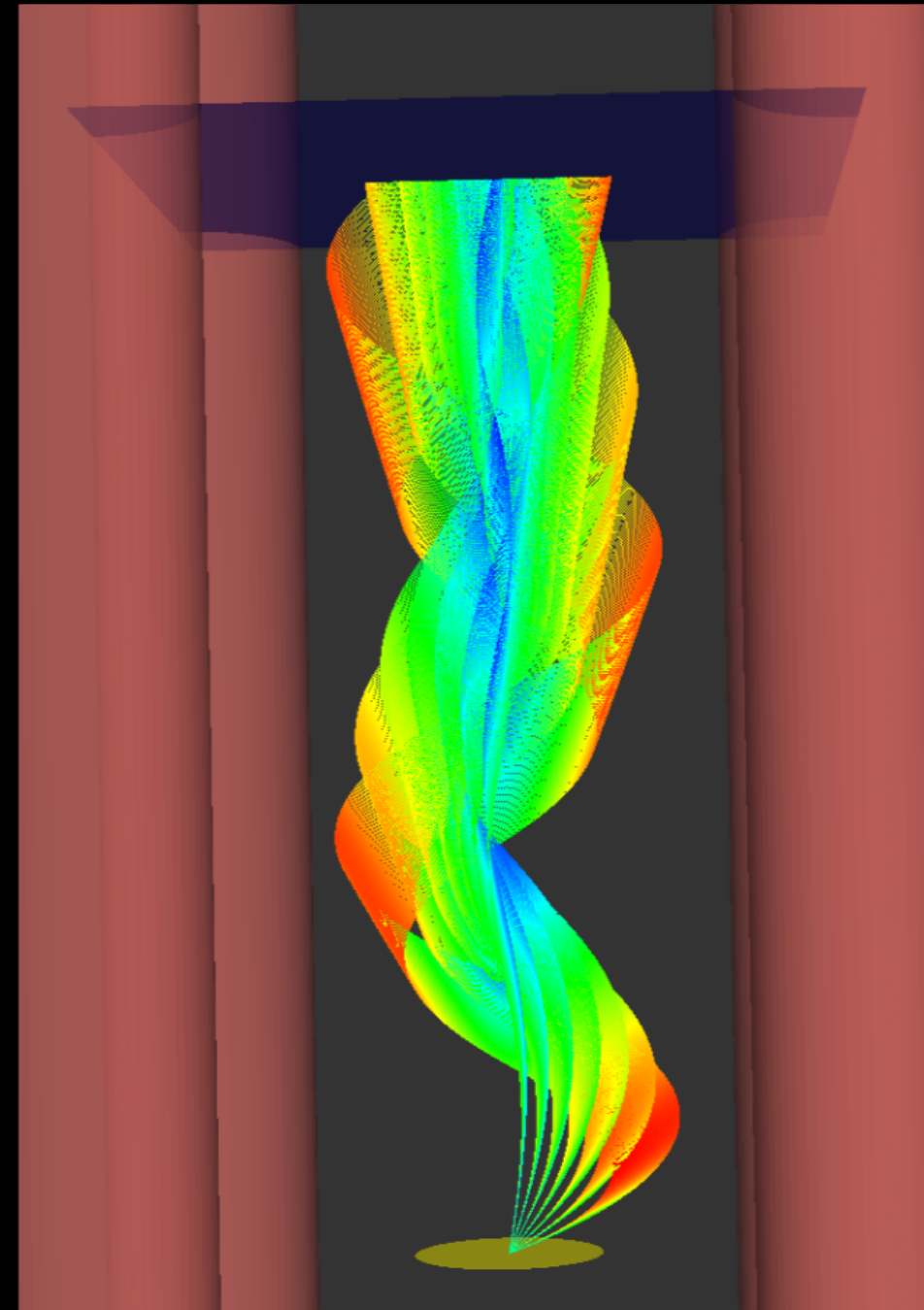
- Dissociation ✓
- Cooling ???
- Injection ✓
- Trapping ✓
- Purification/Circulation (✓)



Velocity and State Selectors

Only atomic T guided magnetically

- (bend) quadrupole with skimmers



Velocity and State Selectors

Only atomic T guided magnetically

- (bend) quadrupole with skimmers



—Associated Press
Workmen putting the finishing touches on Zig-zag turn, Mt Van Hoevenberg Olympic bobsled run

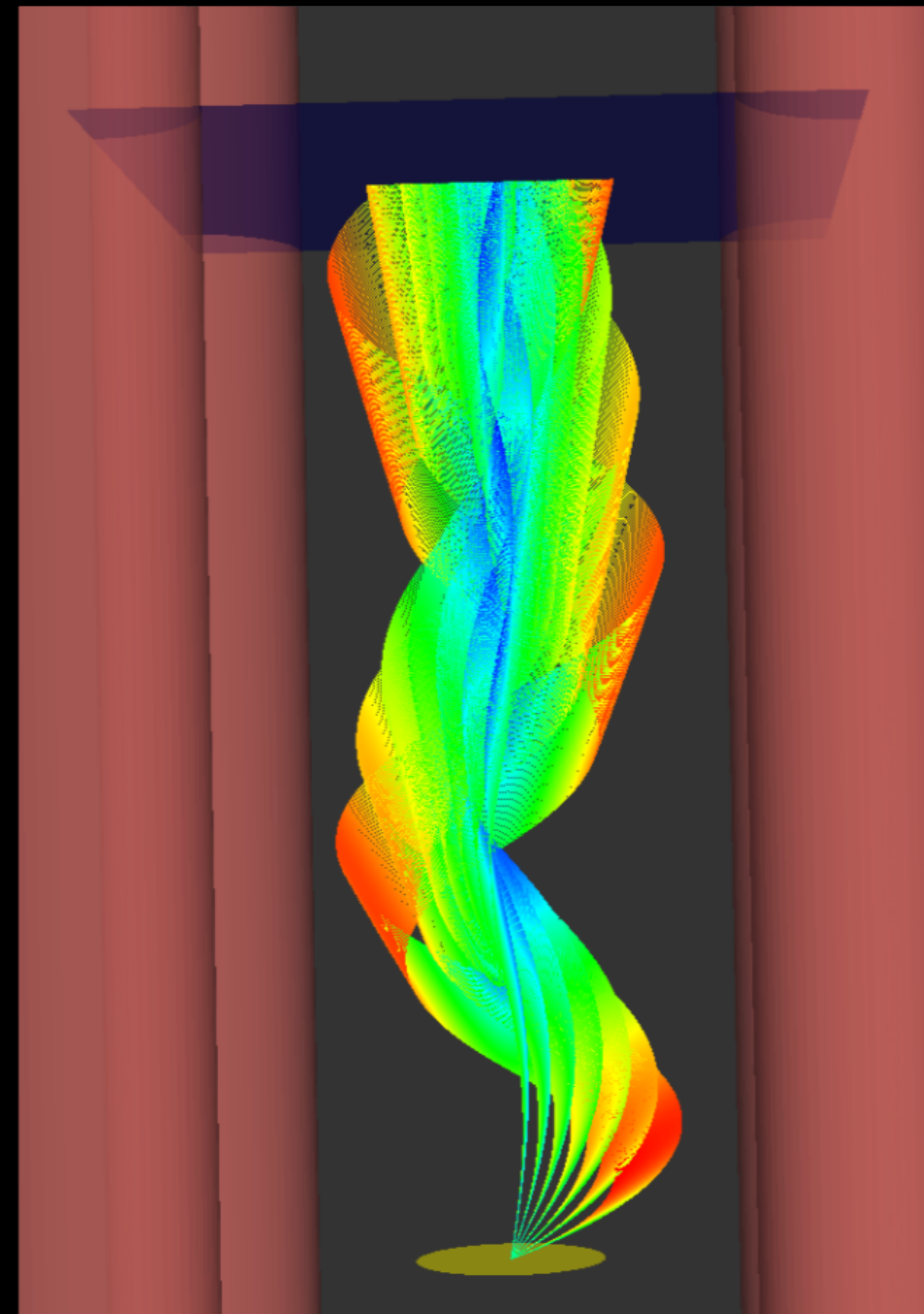
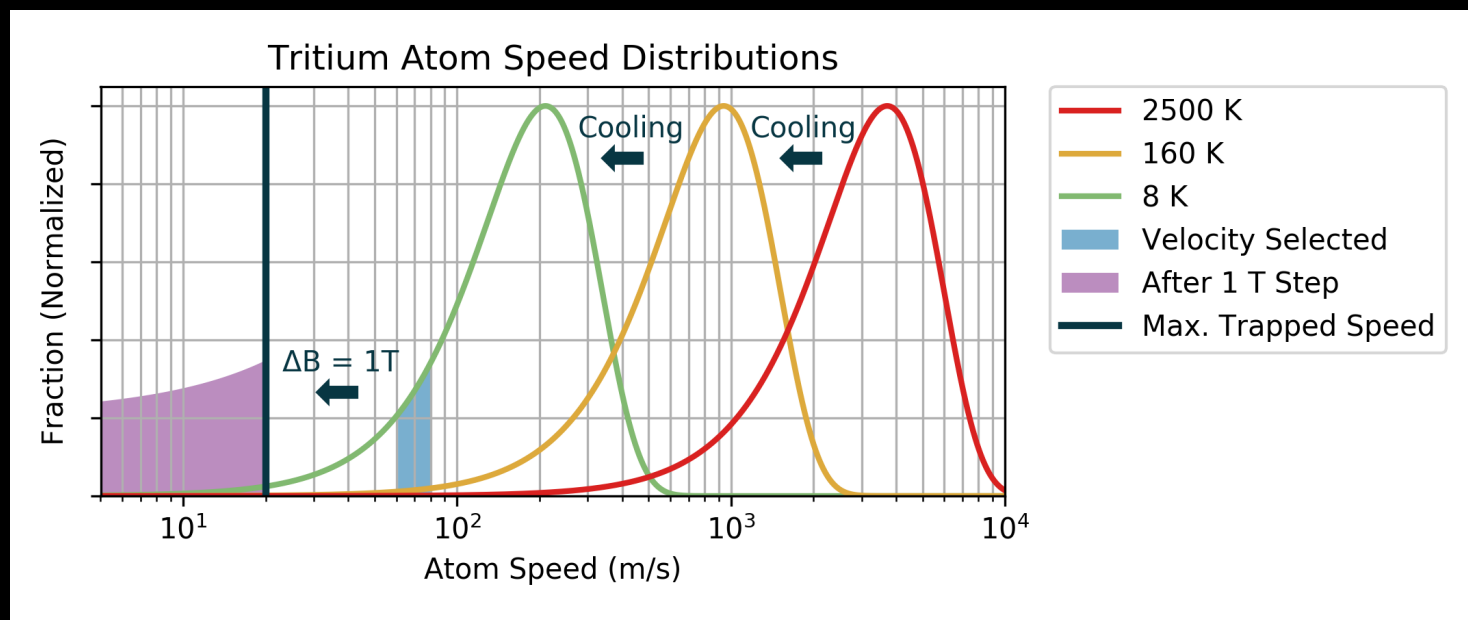
Velocity and State Selectors

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Tune acceptance for

- $T_{\text{out}} = \mathcal{O}(50\text{mK})$
- T_2 contamination $< 10^{-5}$
 - ▶ efficiency $\varepsilon_{\text{cold}} \sim 25\%-100\%$



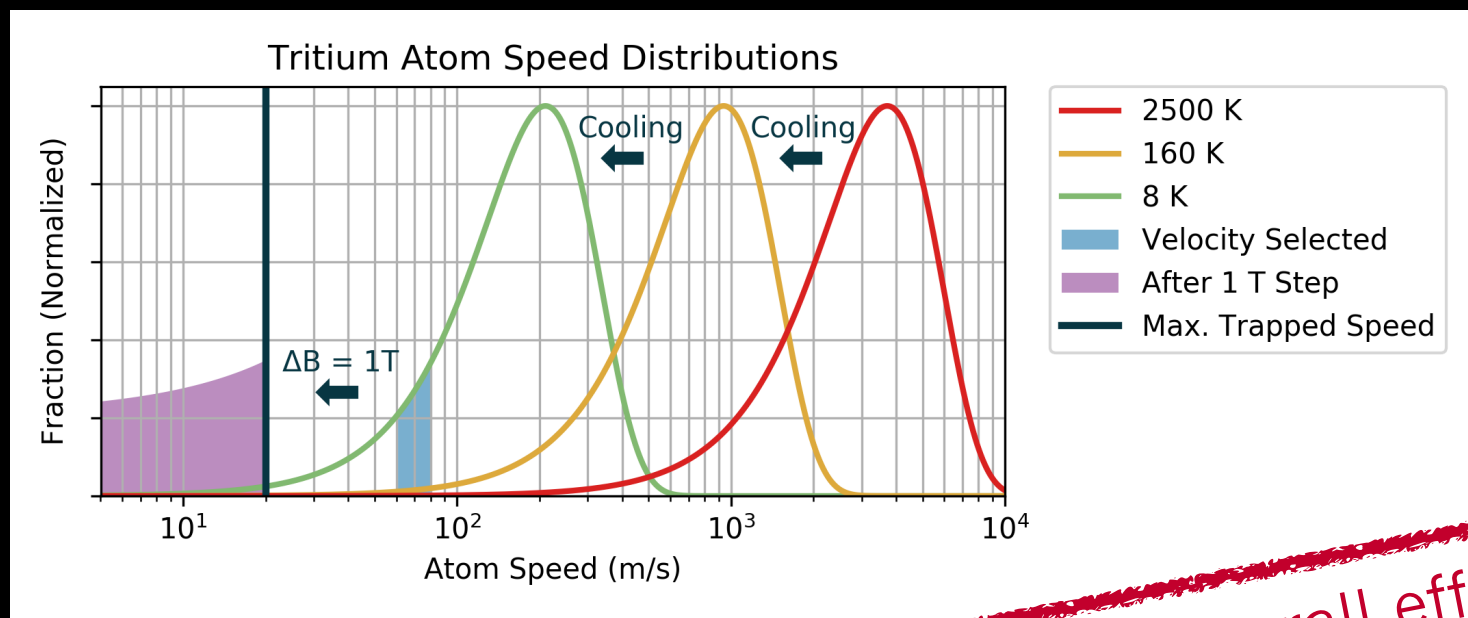
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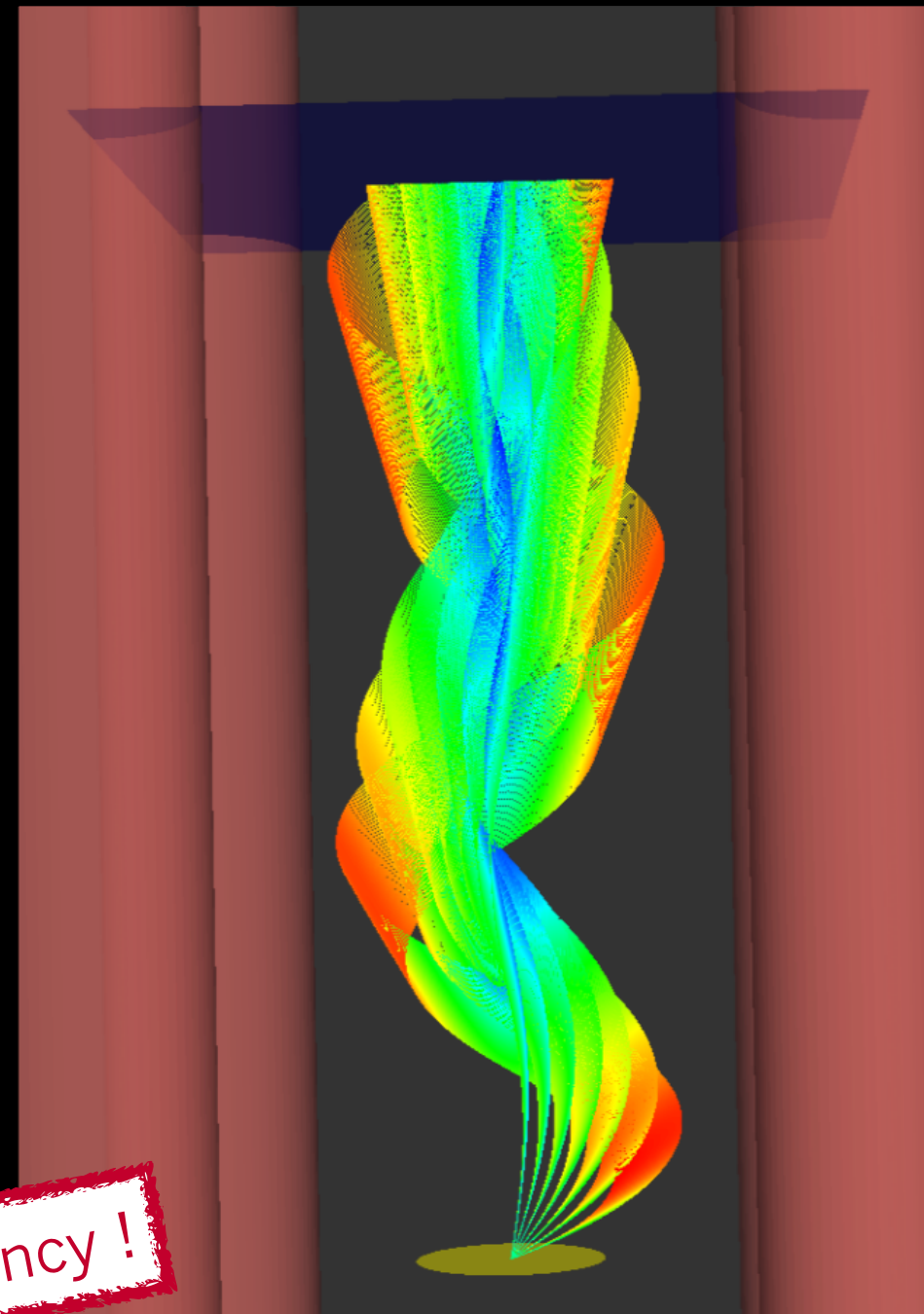
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Tune acceptance for

- $T_{\text{out}} = \mathcal{O}(50\text{mK})$
- T_2 contamination $< 10^{-5}$
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→ but poor overall efficiency !



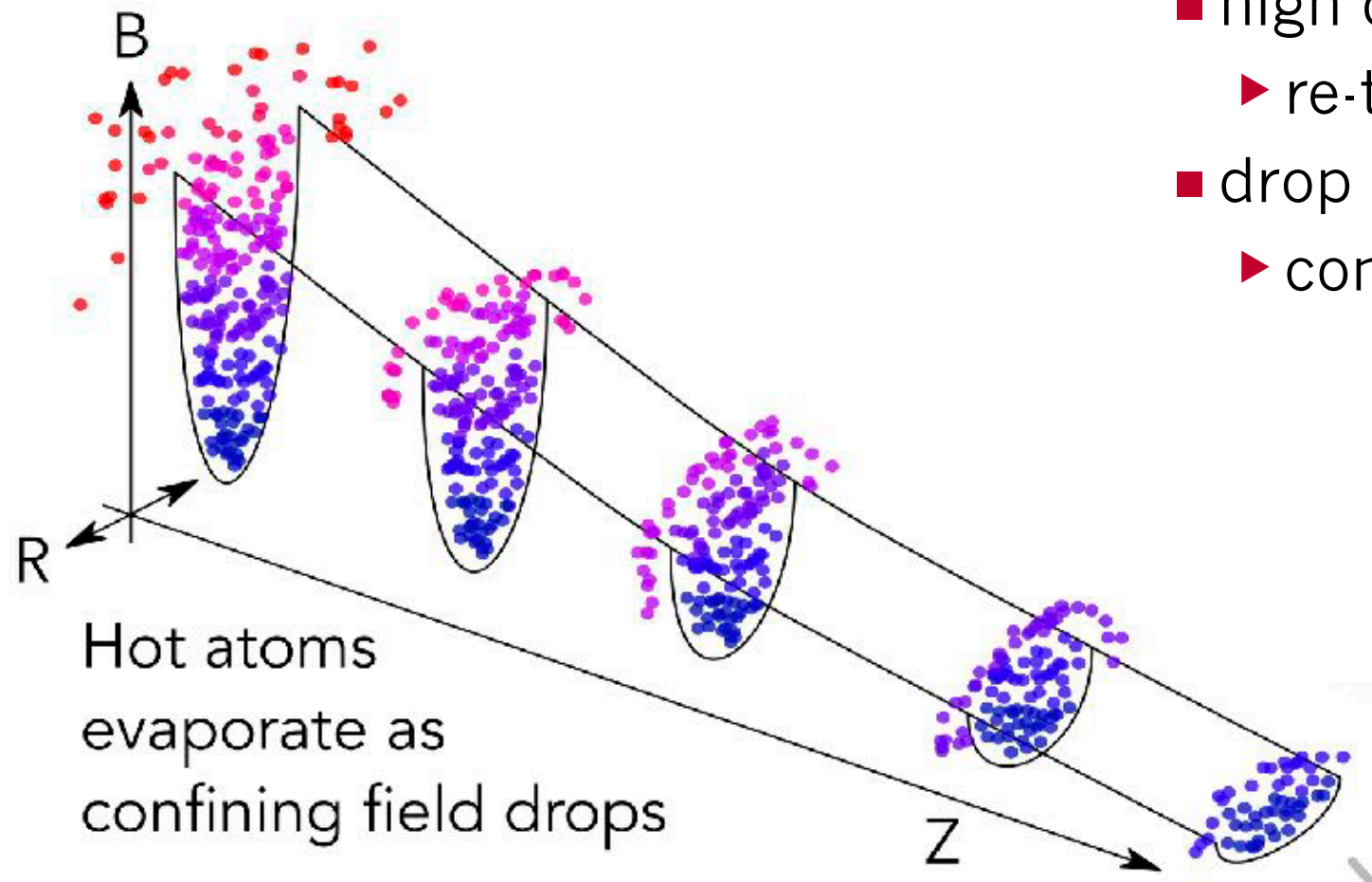
Evaporative cooling

Evaporative cooling of an atomic beam

E. Mandonnet¹, A. Minguzzi², R. Dum¹, I. Carusotto², Y. Castin¹, and J. Dalibard^{1,a}

¹ Laboratoire Kastler Brossel, 24 rue Lhomond, 75005 Paris, France

² INFM, Scuola Normale Superiore, Piazza dei Cavalieri 7, 56126 Pisa, Italy



Basic idea

- magnetic wall
 - ▶ loose *hot* atoms (high $p_{\perp}$)
- high density
 - ▶ re-thermalization
- drop magnetic field along beam
 - ▶ continuous cooling

Evaporative cooling: the math

Boltzman transport equation

$$\left(\frac{p}{m} \nabla_r - \nabla_r U \cdot \nabla_p + \frac{\partial}{\partial t} \right) f(r, p) = \frac{1}{\pi m^2} \int d^3 p_2 \int d^3 p_3 \int d^3 p_4 \frac{d\sigma}{d\Omega}(p_1, p_2, p_3, p_4) (f(r, p_3) f(r, p_4) - f(r, p) f(r, p_2))$$

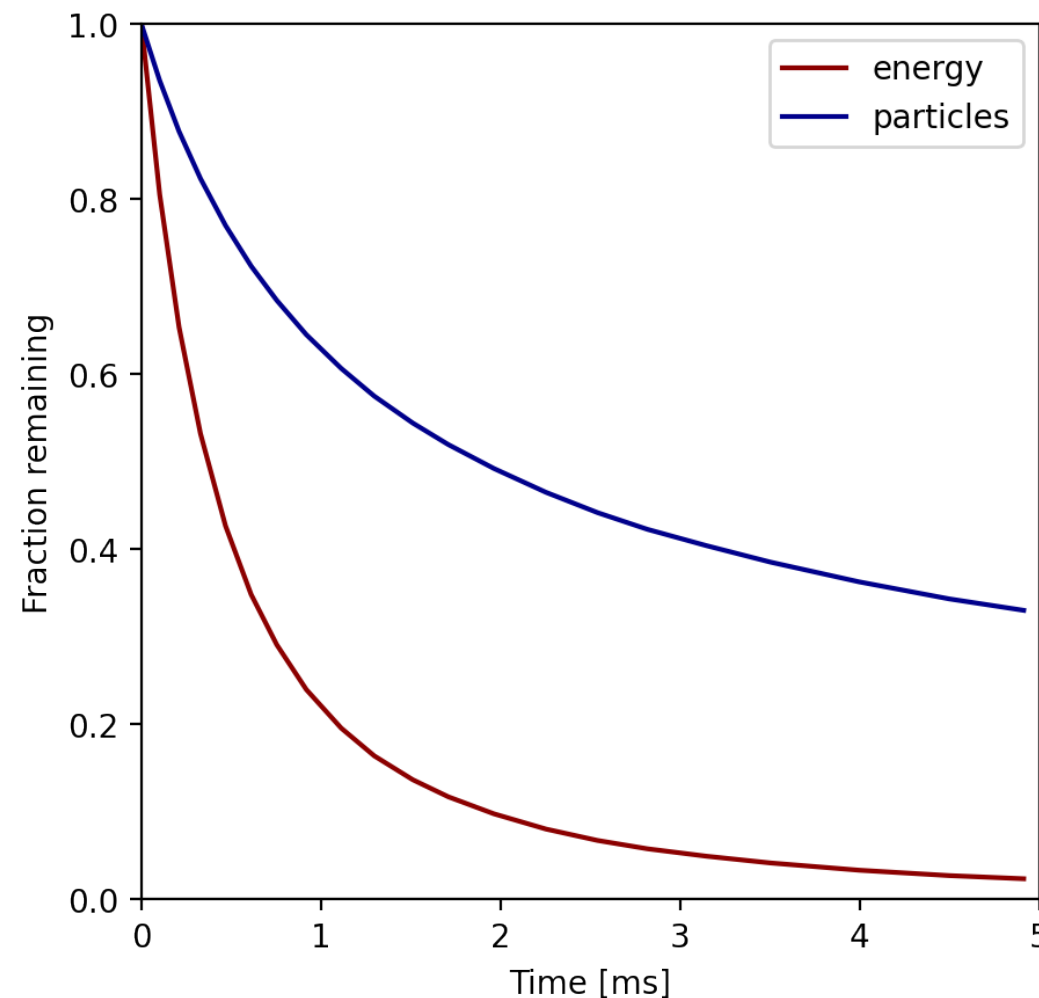
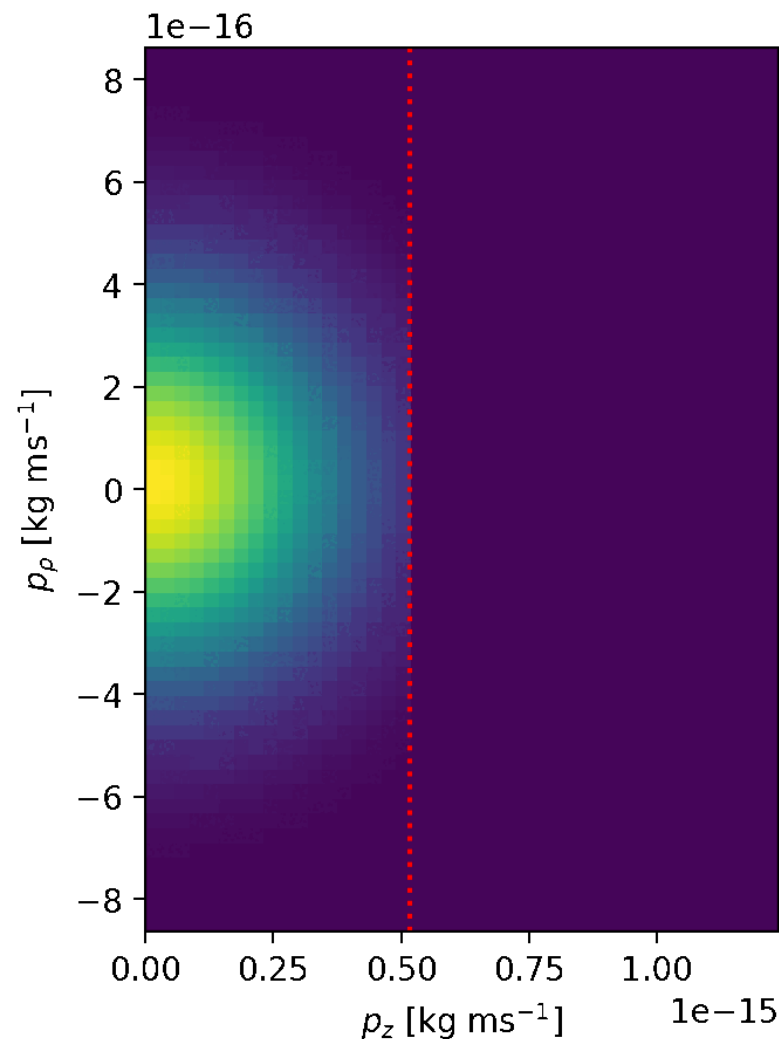


kinetic terms



collision integral

► solve numerically



- Losing energy faster than particles means cooling
- Radial cooling also cools longitudinal motion since collisions redistribute momentum

Evaporative cooling: the math

Boltzman transport equation

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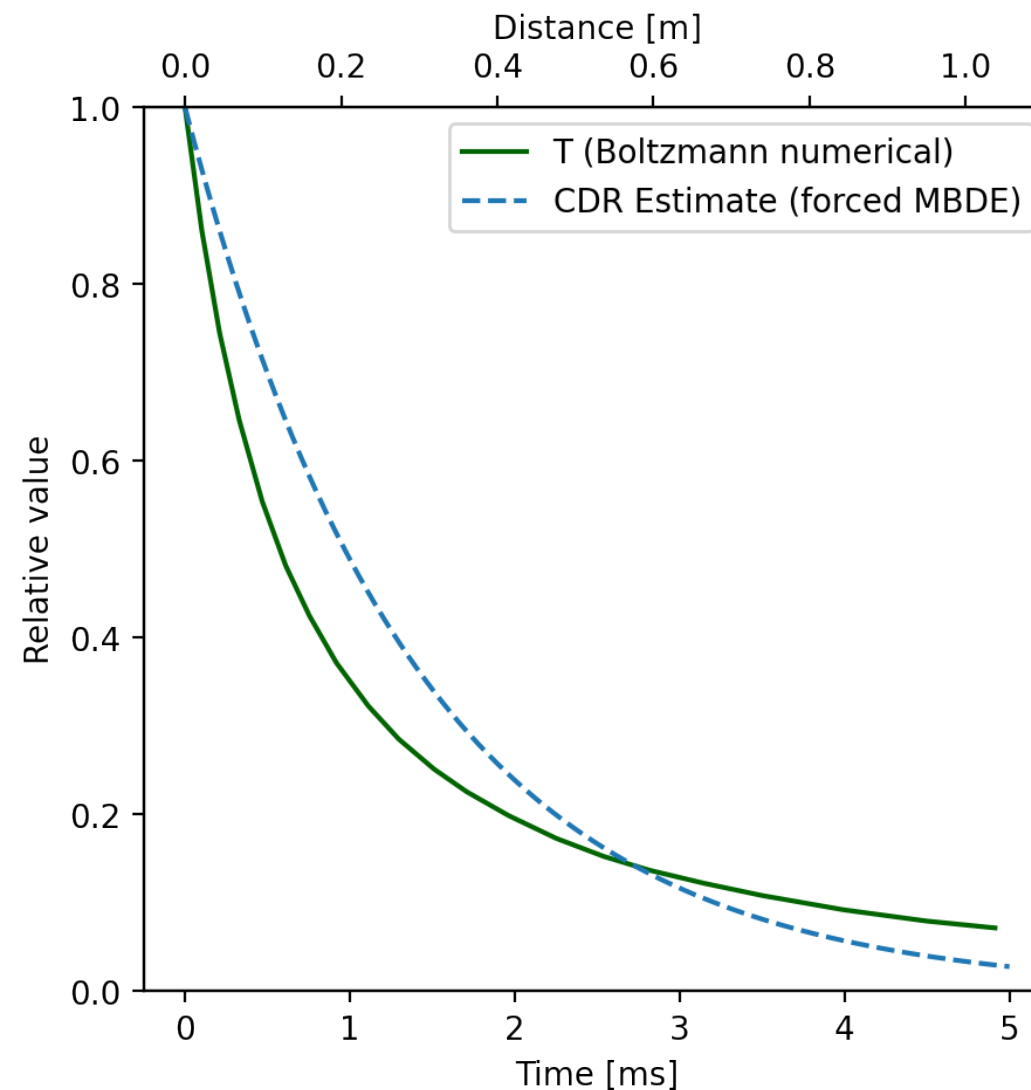
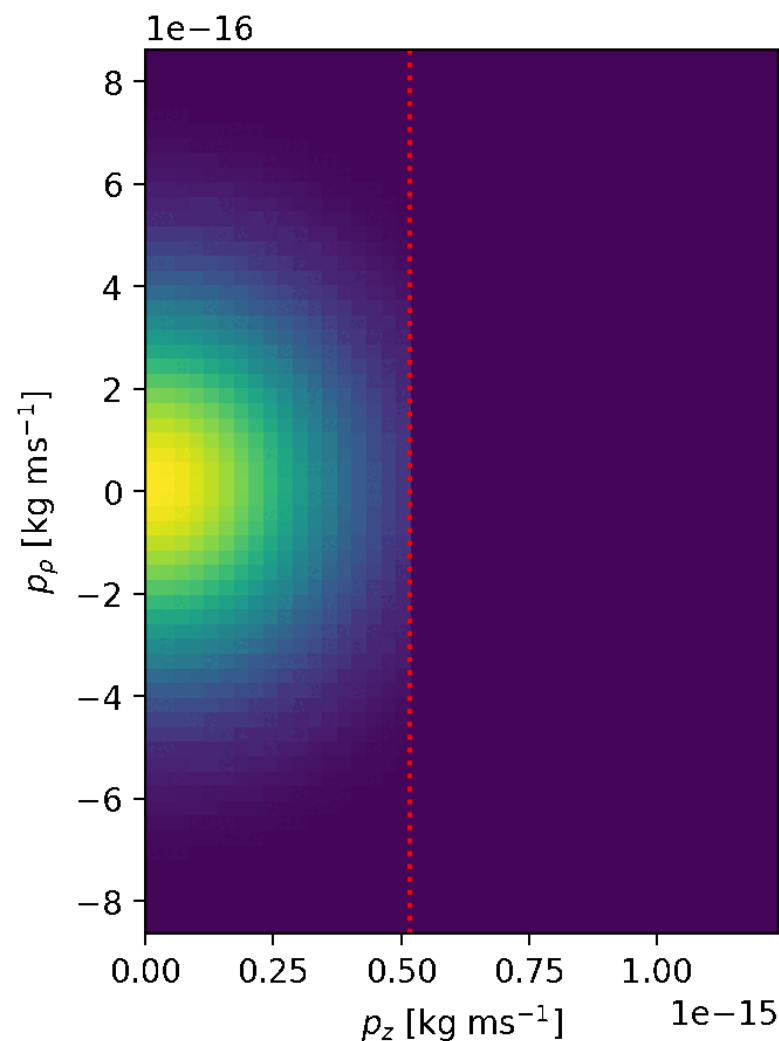


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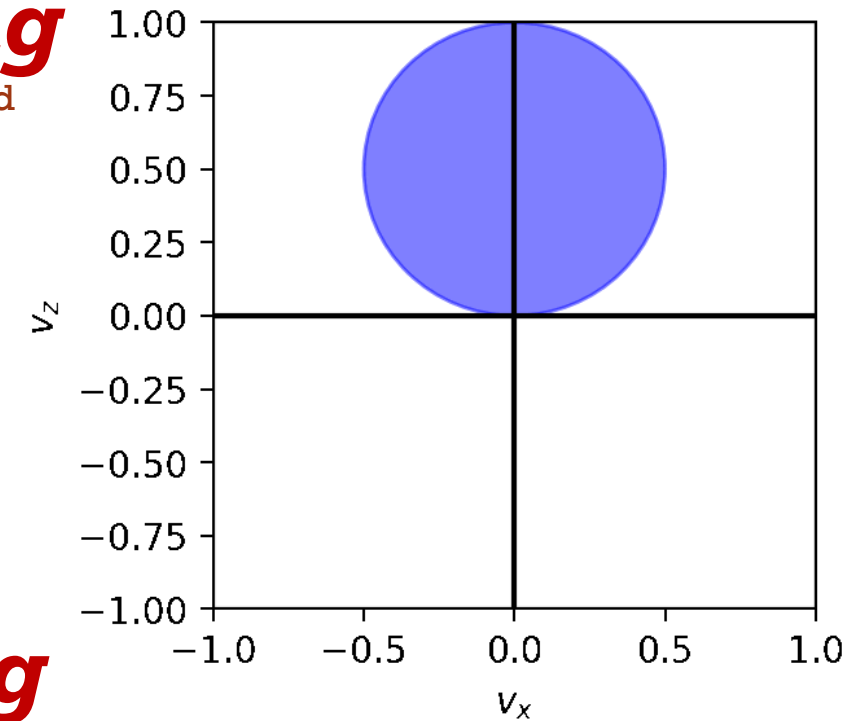
Cooling vs slowing

Initial atomic *beam*

- net forward momentum
 - ▶ need **cooling** and **slowing**

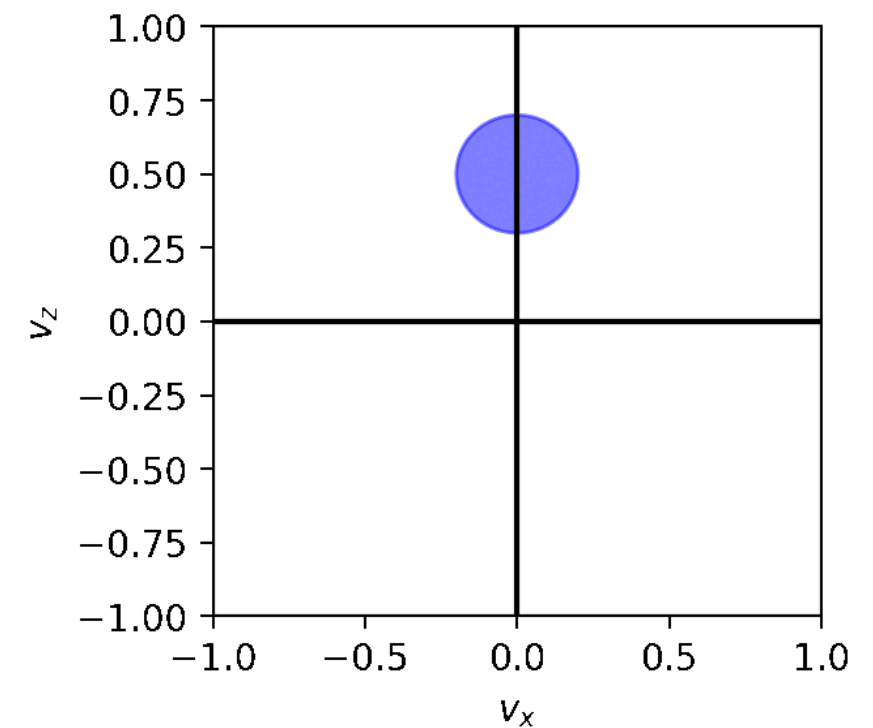
Cooling

Mean(p) conserved



Slowing

Mean(p) reduced



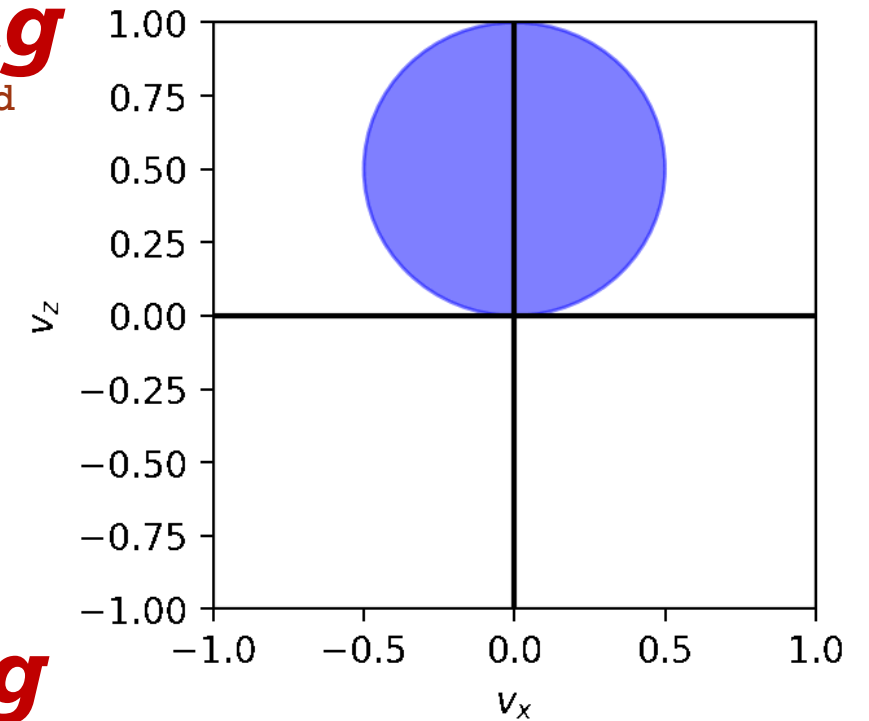
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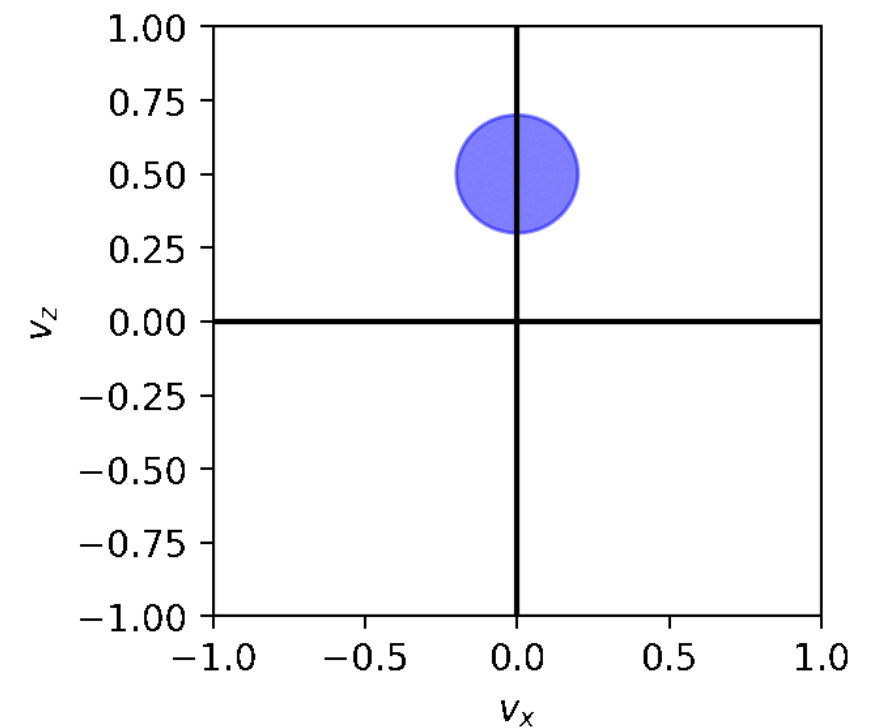
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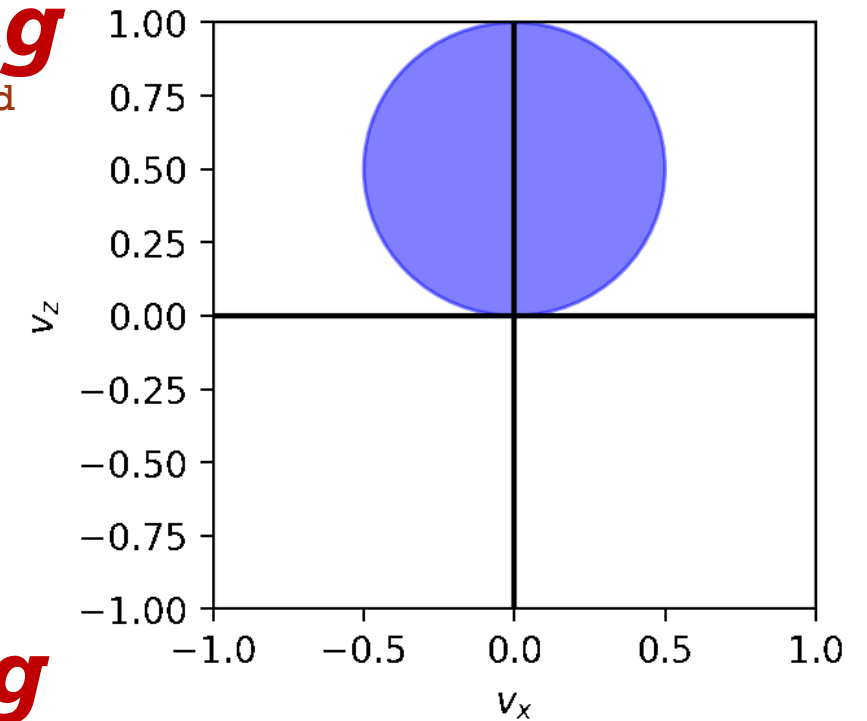
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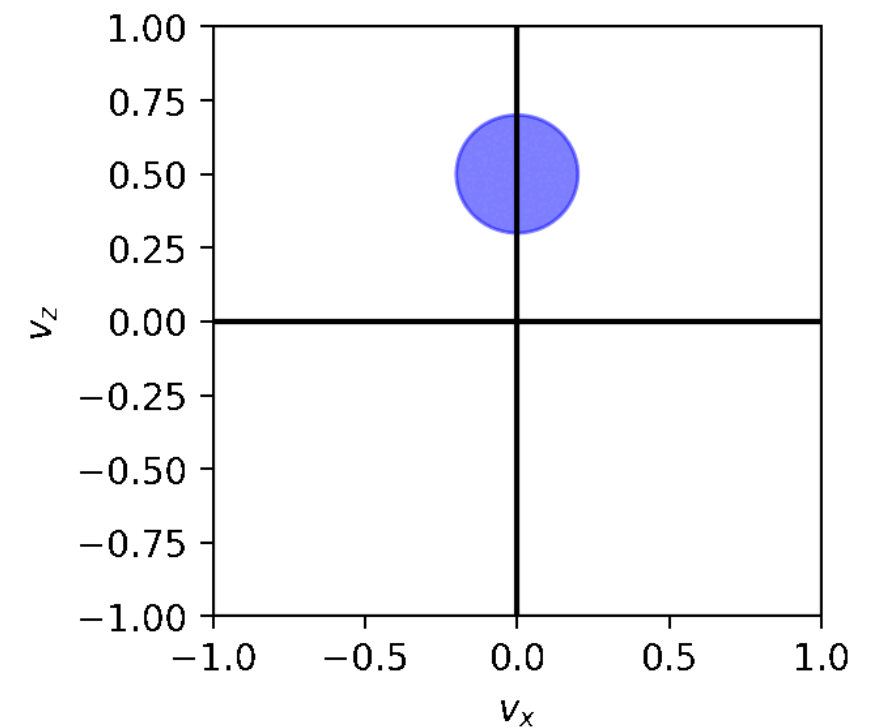
Cooling

Mean(p) conserved



Slowing

Mean(p) reduced



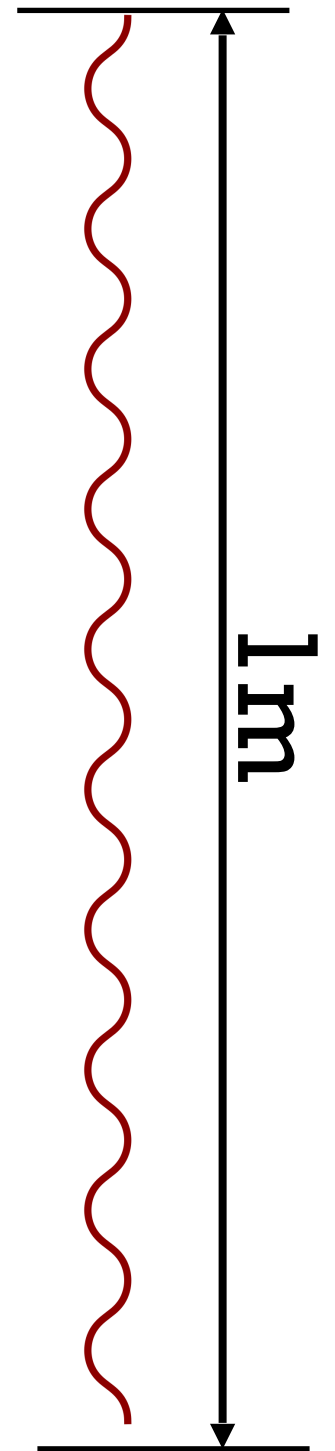
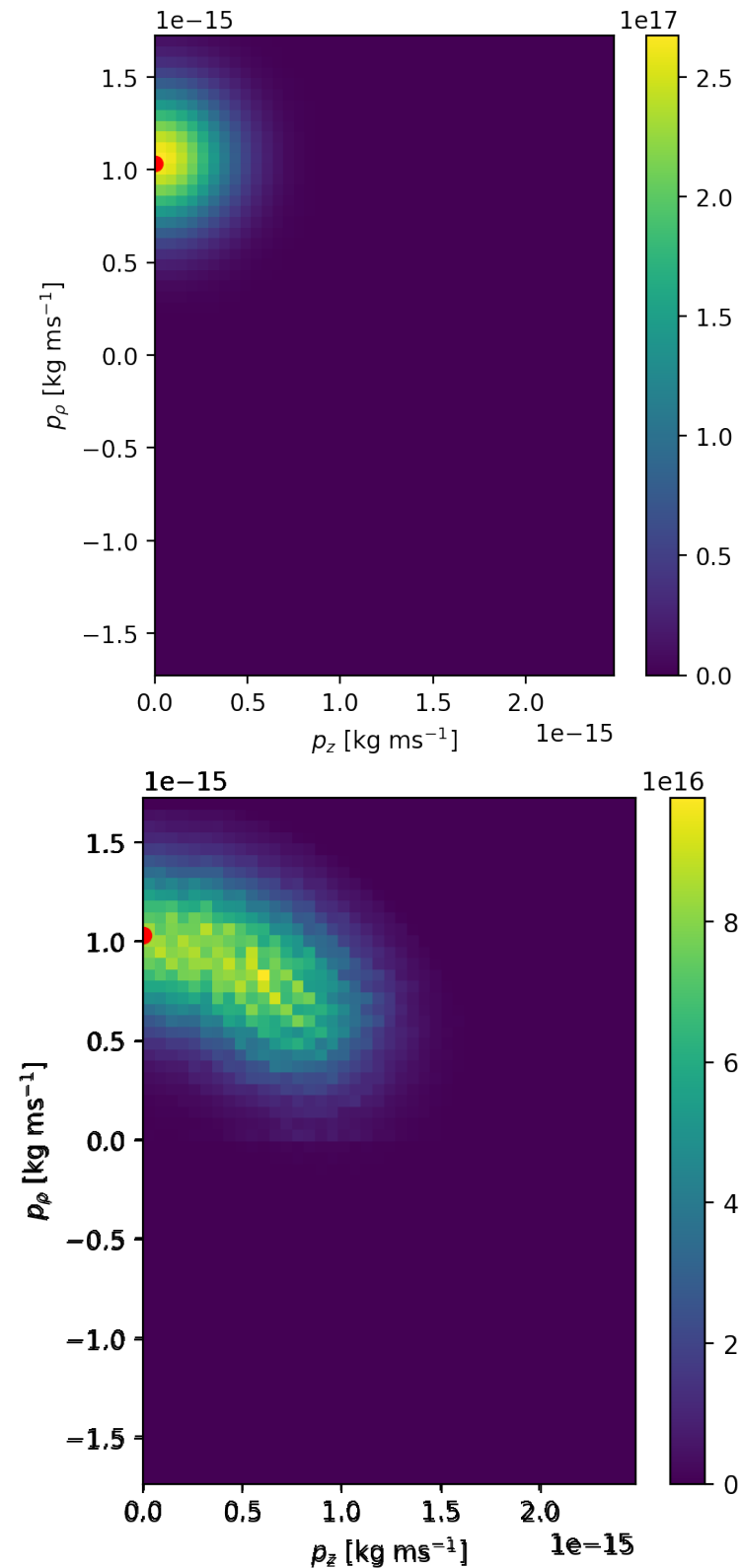
Cooling vs slowing

Initial atomic *beam*

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The *wiggler*

- several wiggles within mean free path
 - ▶ transfer longitudinal to perpendicular momentum
- re-thermalization
 - ▶ slows down beam



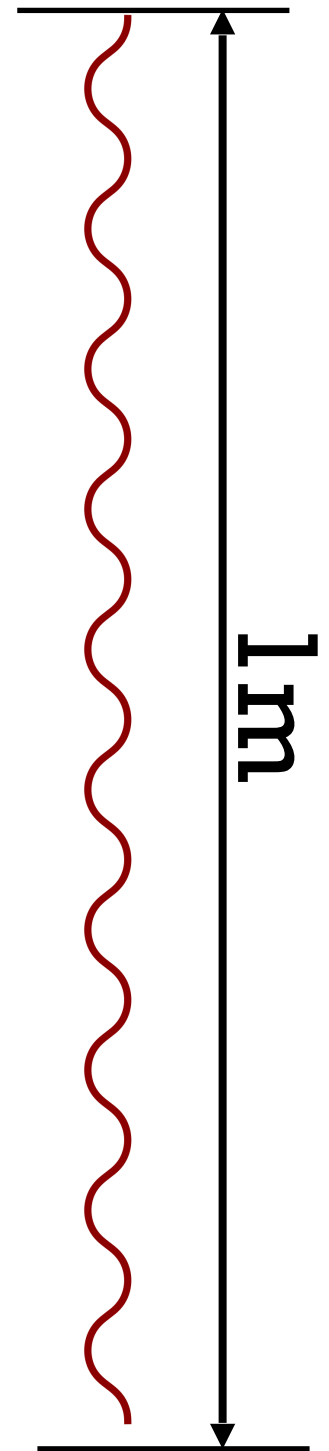
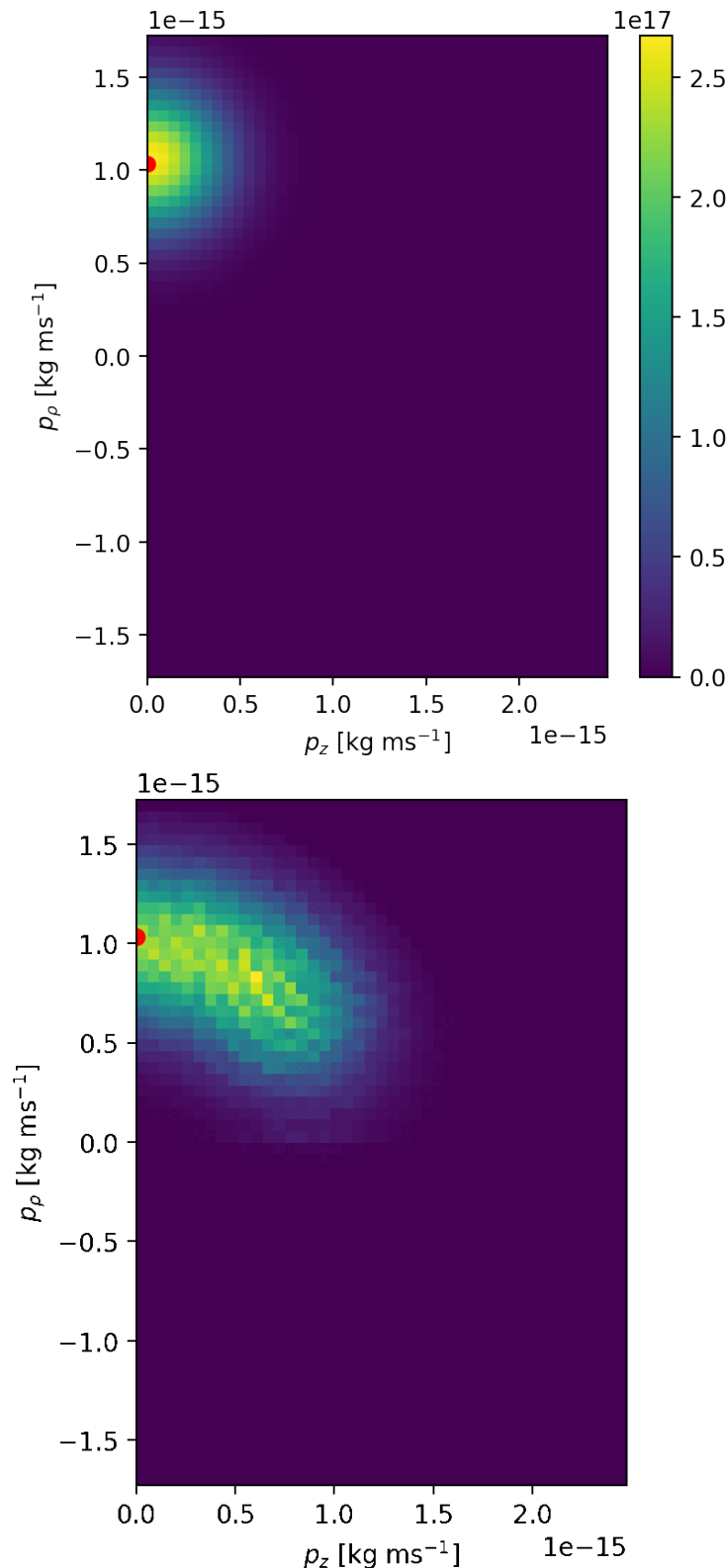
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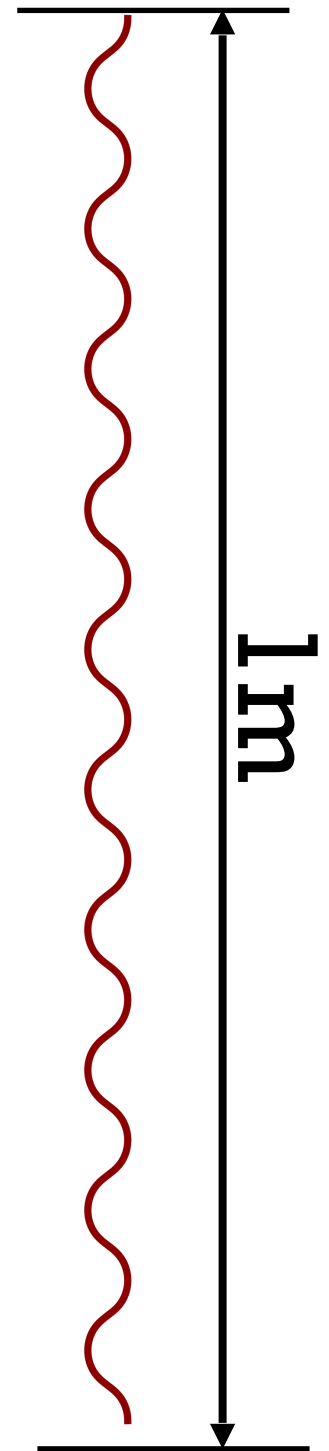
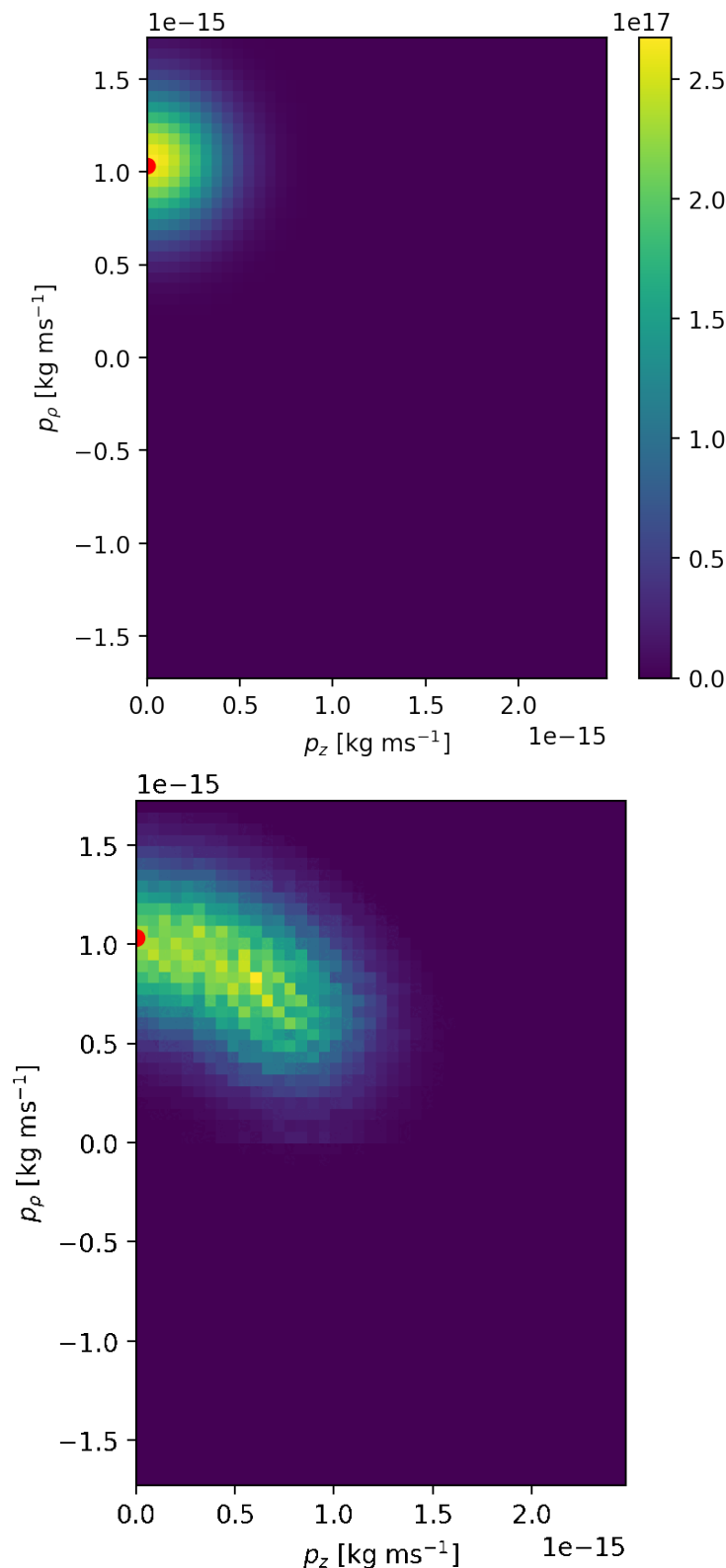
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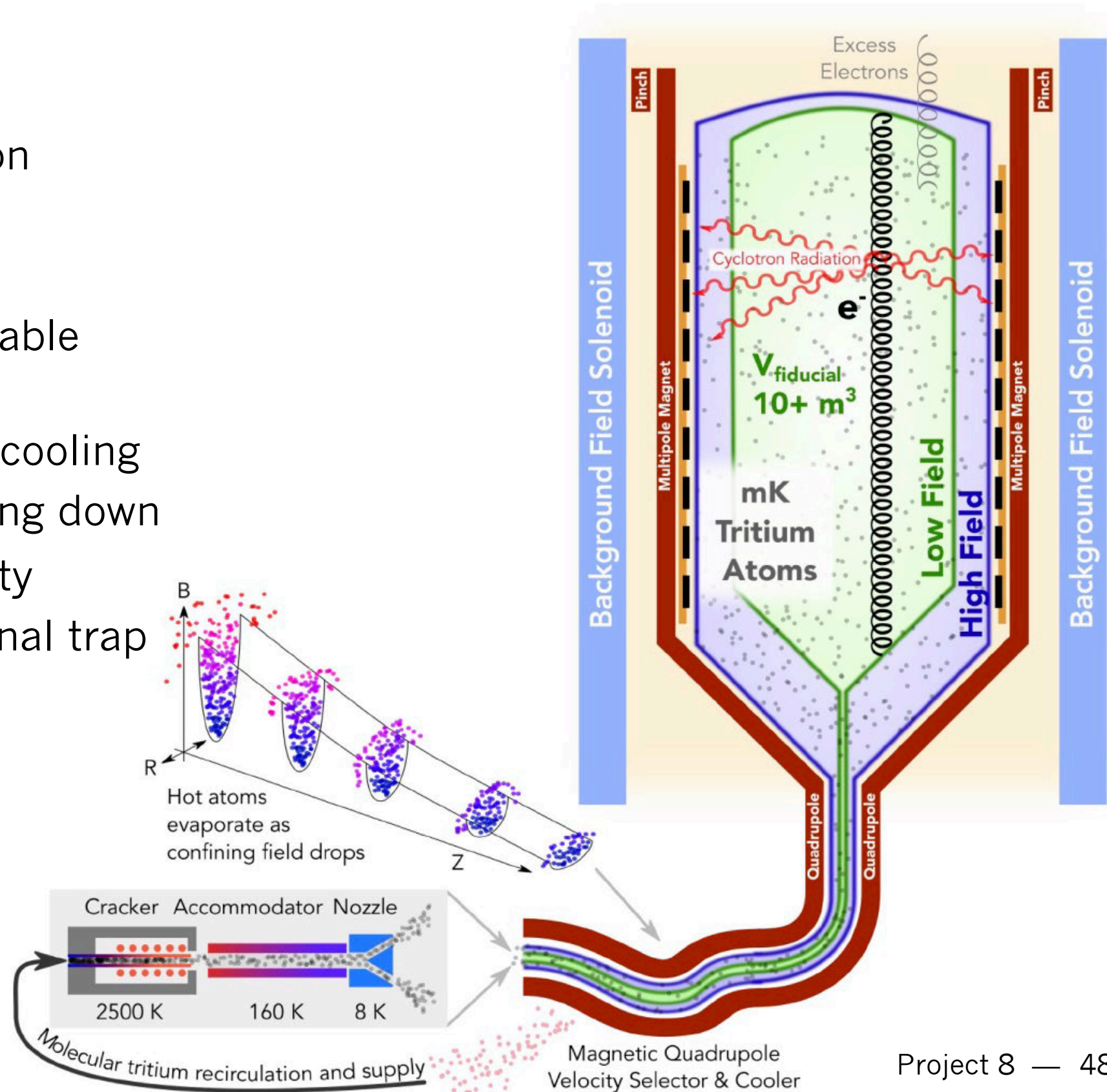


Atomic tritium experiment

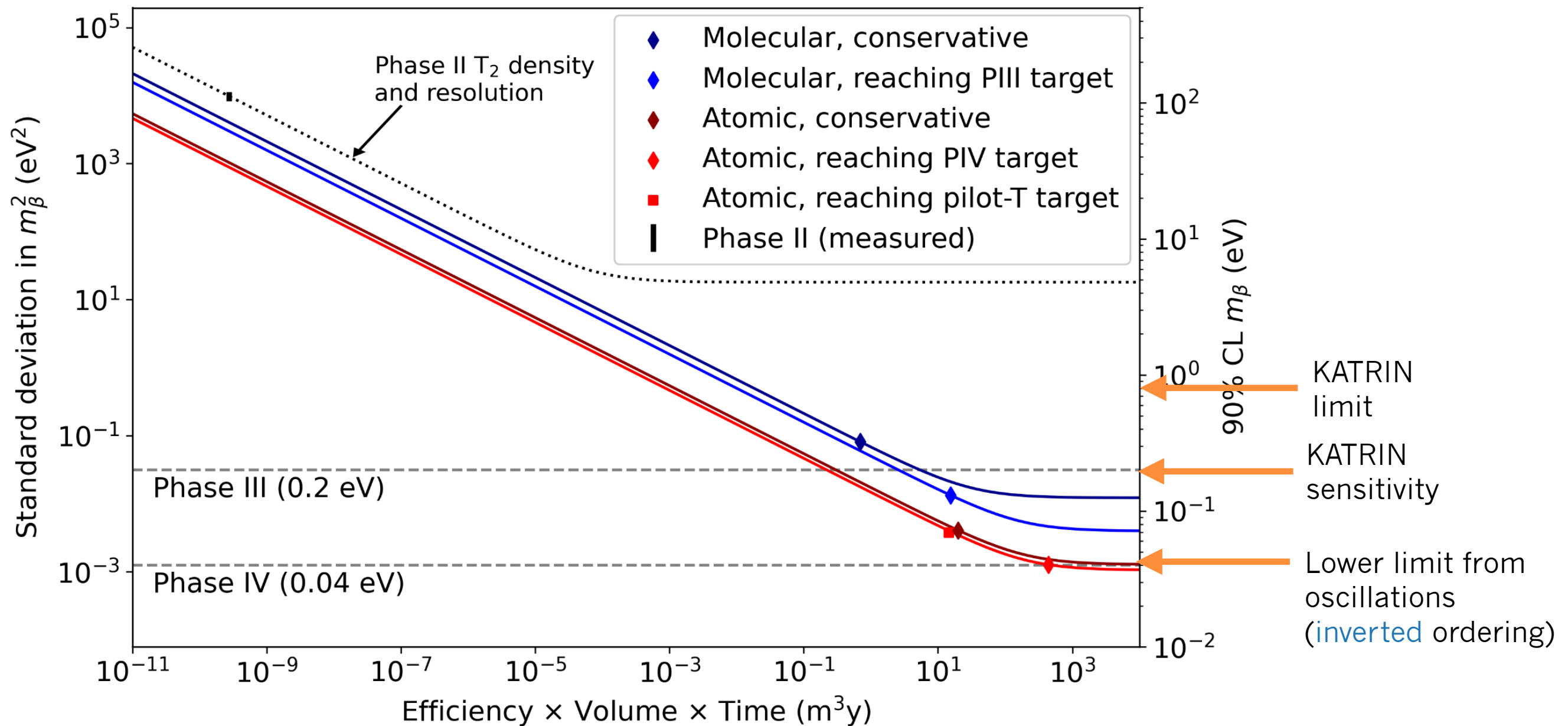
PROJECT 8

Conceptual design

- thermal dissociation
 - ▶ $T_2 \rightarrow T$
- accommodation
 - ▶ $\emptyset(K)$ with acceptable recombination
- evaporative wobble cooling
 - ▶ $\emptyset(mK)$ and slowing down
 - ▶ high atomic purity
- Magneto-gravitational trap
 - ▶ Halbach array



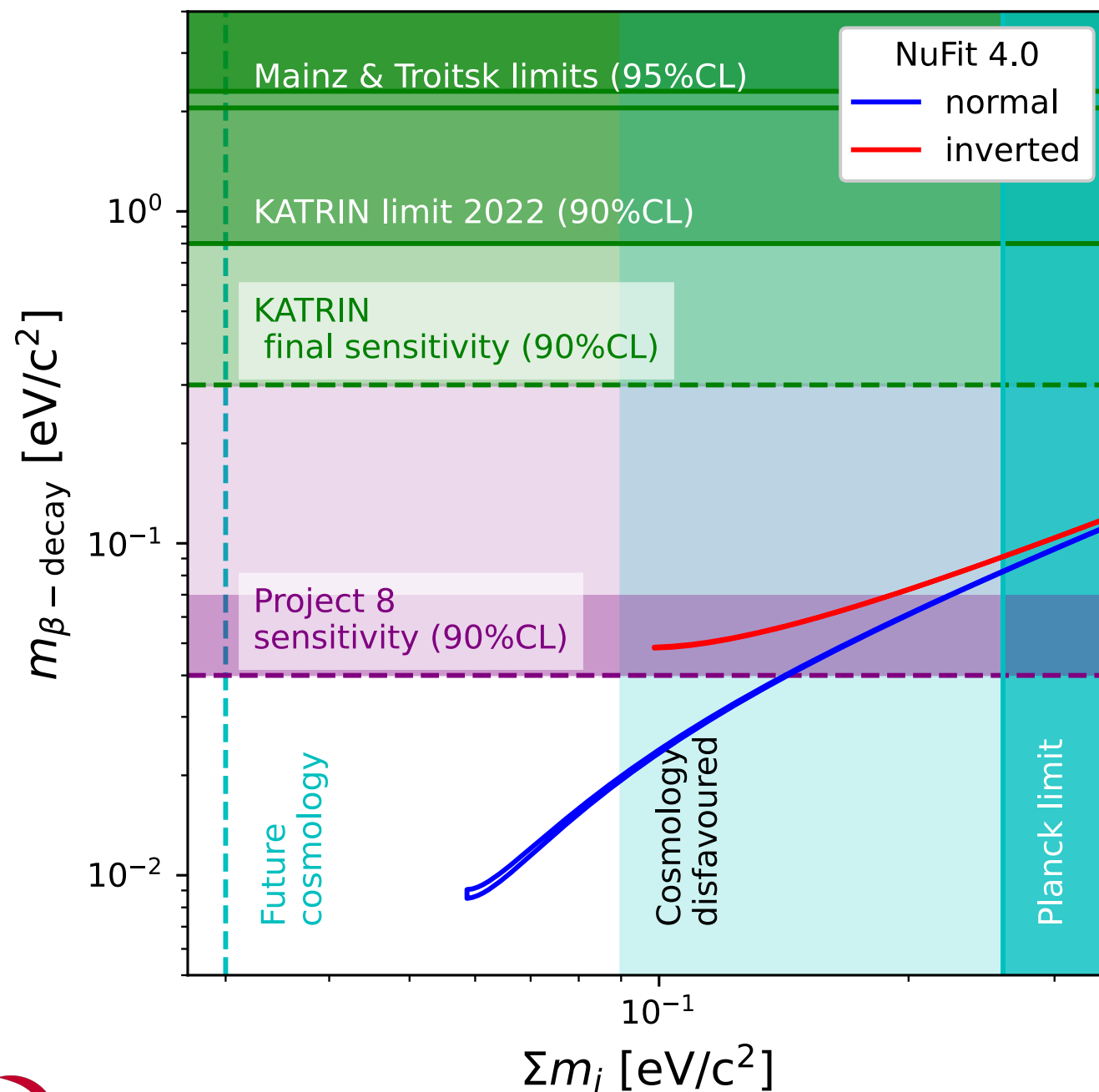
Potential for neutrino mass!



Comparison of methods

Measuring neutrino masses

- approaches are complementary



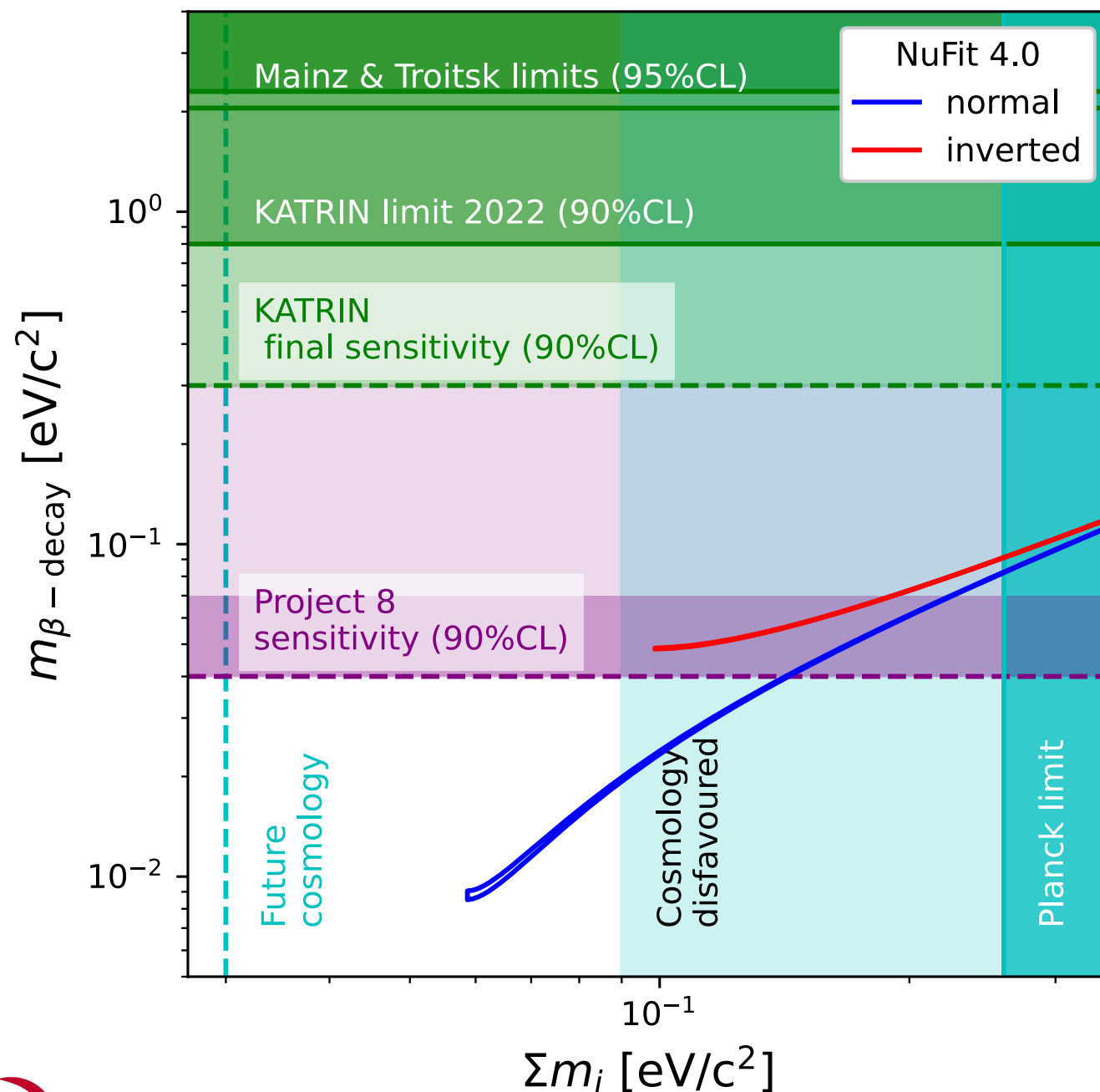
$$\Delta m^2 \equiv m_2^2 - m_1^2$$

Oscillation experiments

Comparison of methods

Measuring neutrino masses

- approaches are complementary



$$\Delta m^2 \equiv m_2^2 - m_1^2$$

Oscillation experiments

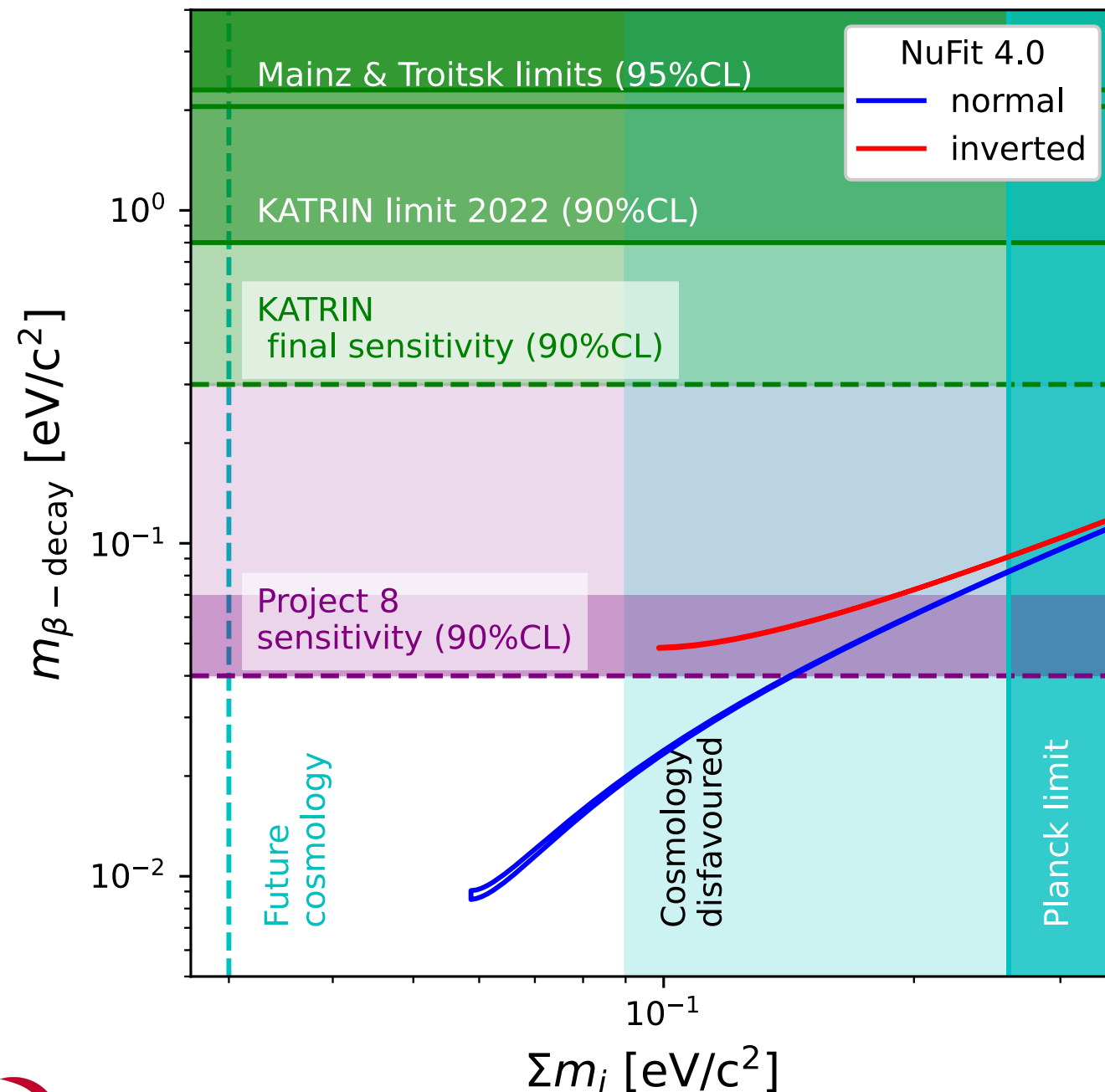
$$M = \sum_i^{n_\nu} m_i$$

Cosmological measurements

Comparison of methods

Measuring neutrino masses

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Oscillation experiments

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Cosmological measurements

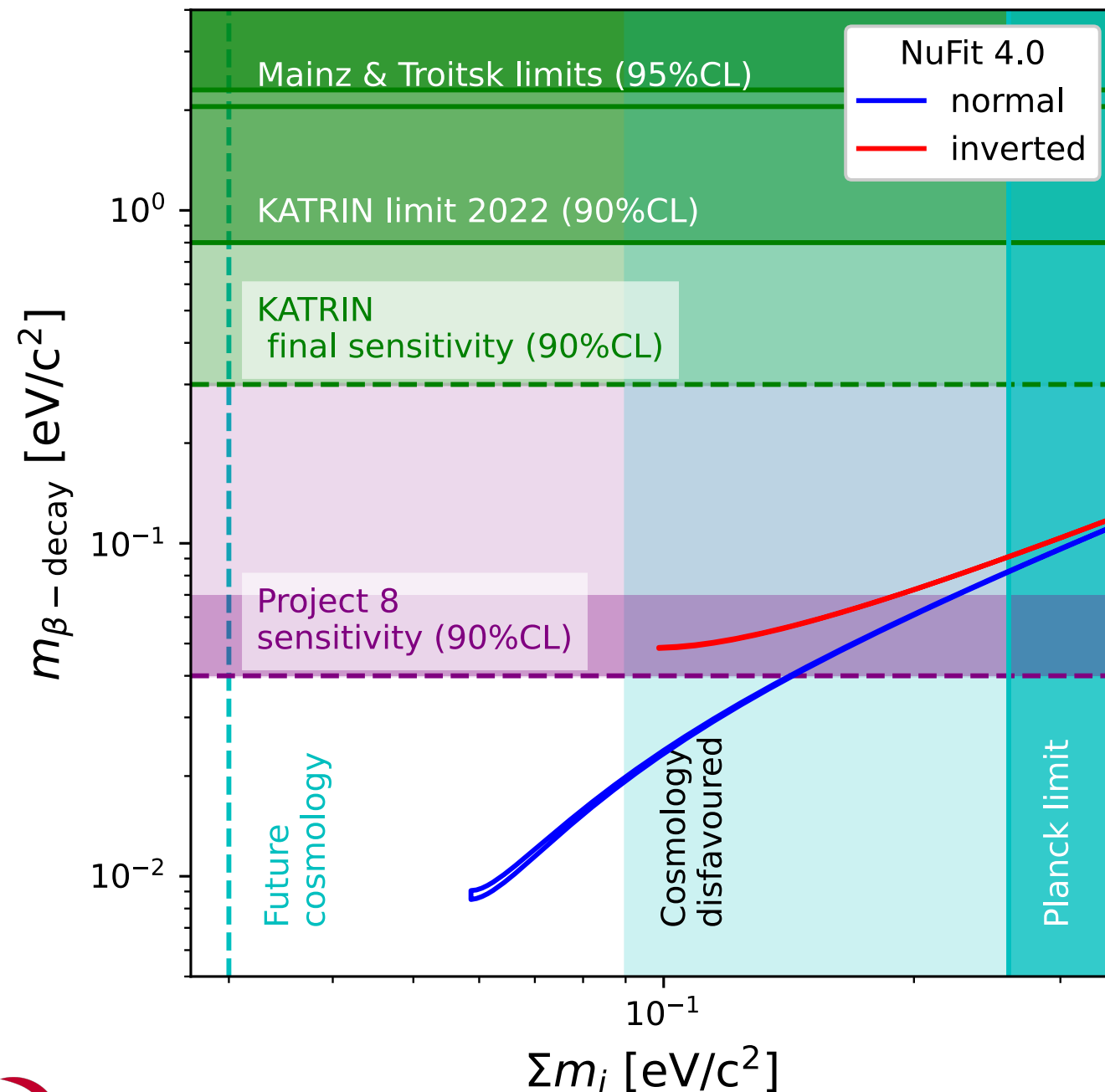
$$m_{\beta\beta}^2 = \left| \sum_i^{n_\nu} U_{ei}^2 m_i \right|^2$$

$0\nu\beta\beta$ decay experiments

Comparison of methods

Measuring neutrino masses

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Oscillation experiments

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$0\nu\beta\beta$ decay experiments

$$m_\beta^2 = \sum_i^{n_\nu} |U_{ei}^2| m_i^2$$

β -decay experiments

Project 8 collaboration



Thank you!

