

# Heavy Neutrino Searches: Current Status and Future Prospects

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PSBD, A. Pilaftsis and U.-k. Yang, arXiv:1308.2209 [hep-ph];  
C.-Y. Chen, PSBD and R. N. Mohapatra, Phys. Rev. D **88**, 033014 (2013) [arXiv:1306.2342];  
PSBD, C.-H. Lee and R. N. Mohapatra, Phys. Rev. D (2013) [arXiv:1309.0774]; and ongoing



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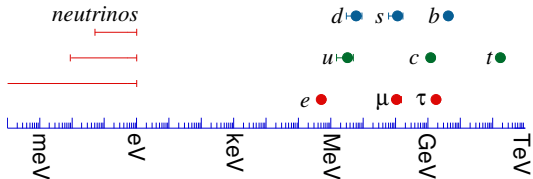


# Outline

- Introduction
- Type-I seesaw and its two aspects
- Experimental constraints
- Improving the LHC sensitivity
- Left-Right seesaw
- A predictive TeV-scale L-R seesaw model
- Conclusion

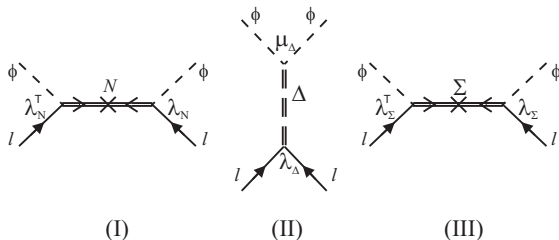
# Neutrino Oscillation $\Rightarrow$ Physics beyond the SM

- First conclusive *experimental* evidence of BSM Physics.
- Neutrinos massless in the SM because
  - No right-handed counterpart (no Dirac mass unlike charged fermions).
  - $\nu_L$  part of  $SU(2)_L$  doublet  $\Rightarrow$  No Majorana mass term  $\nu_L^T C^{-1} \nu_L$ .
  - SM has an **exact global  $(B - L)$ -symmetry**. Even non-perturbative effects cannot induce neutrino mass.
- Simply adding RH neutrinos ( $N$ ) requires **tiny Yukawa coupling  $y_\nu \lesssim 10^{-12}$**  in the Dirac mass term  $\mathcal{L}_{\nu, Y} = y_{\nu, ij} \bar{L}_i \Phi N_j + \text{h.c.}$
- (Unnaturally) small and has *no* experimentally observable effects.
- Large hierarchy between neutrino and charged fermion masses might be suggesting some new distinct mechanism behind neutrino masses.



# A Simple Paradigm

- A natural way to generate neutrino mass is by breaking  $(B - L)$ .
- Within the SM, can be parametrized through Weinberg's dimension-5 operator  $\lambda_{ij}(L_i^\top \Phi)(L_j^\top \Phi)/\Lambda$ . [S. Weinberg, PRL **43**, 1566 (1979)]
- Three tree-level realizations: Type I,II,III Seesaw mechanism.



- Majorana mass of the heavy particle ( $N, \Delta, \Sigma$ ) breaks  $L$  by two units.
- Other profound implications: Leptogenesis, Dark Matter, Electroweak Vacuum Stability, ...
- A pertinent question in the LHC era: Is LNV observable at the LHC and/or at low-energy?
- Other relevant question: Can it also lead to a large LFV?



# Type-I Seesaw

- Seesaw messenger: SM singlet fermions (RH neutrinos).
- Have a Majorana mass term  $M_N N^T C^{-1} N$ , in addition to the Dirac mass  $M_D = \nu y_\nu$ .
- In the flavor basis  $\{\nu_L^C, N\}$ , leads to the general structure

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & M_D \\ M_D^T & M_N \end{pmatrix}$$

[ Minkowski '77; Mohapatra, Senjanović '79; Yanagida '79; Gell-Mann, Ramond, Slansky '79; Glashow '79]

- In the seesaw approximation  $||\xi|| \ll 1$ , where  $\xi \equiv M_D M_N^{-1}$  and  $||\xi|| \equiv \sqrt{\text{Tr}(\xi^\dagger \xi)}$ ,
- $M_\nu^{\text{light}} \simeq -M_D M_N^{-1} M_D^T$  is the light neutrino mass matrix.
- $\xi \equiv M_D M_N^{-1}$  is the **heavy-light neutrino mixing**.
- From a bottom-up approach, we call this minimal scenario the 'SM seesaw'.
- No definite prediction for the seesaw scale: a wide range of possibilities over 20 orders of magnitude (keV -  $10^{14}$  GeV)!

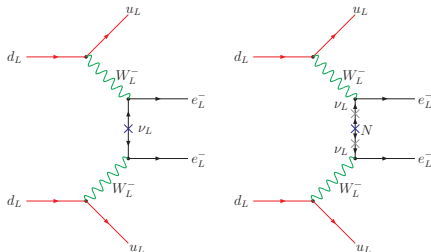


# Two Key Aspects of Seesaw

## Majorana Mass



LNV: Neutrinoless Double Beta Decay

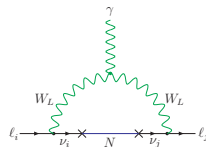


Does not probe the heavy-light mixing if the mixed diagram is sub-dominant.

## Heavy-light Mixing



● LFV ( $\mu \rightarrow e\gamma$ ,  $\mu \rightarrow 3e$ ,  $\mu - e$  conv,...)

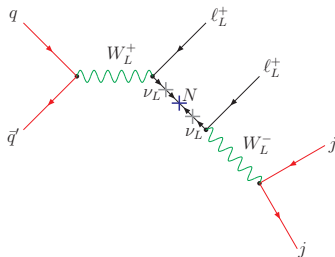


- Also non-unitarity of the PMNS matrix.
- Do not necessarily prove the Majorana nature since a Dirac neutrino can also give large LFV and non-unitarity effects.

Low-energy tests of Seesaw at the Intensity Frontier require a synergy between the two aspects.

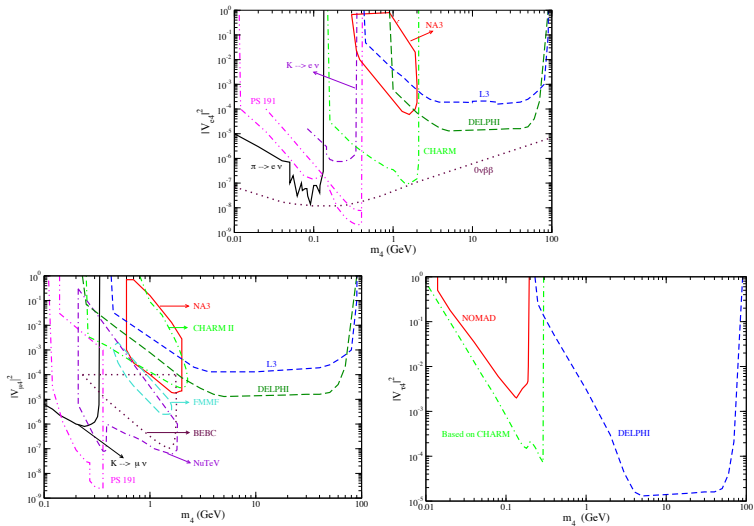
# Collider Signal

- A direct test of *both* aspects of type-I seesaw at the Energy Frontier.
- ‘Smoking gun’ signal:  $pp \rightarrow W^* \rightarrow \ell_\alpha^\pm N \rightarrow \ell_\alpha^\pm \ell_\beta^\pm jj$  with no  $\cancel{E}_T$ .



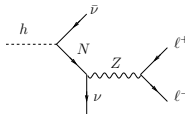
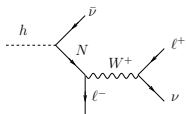
- Requires *both* the **Majorana nature** of  $N$  at (sub-)TeV scale and a ‘large’ **heavy-light mixing** to have an observable effect.
- A potential **direct** probe of both LNV and LFV (for  $\alpha \neq \beta$ ) if  $M_N = \mathcal{O}(100 \text{ GeV} - 1 \text{ TeV})$ .

# Pre-LHC Constraints



[A. Atre, T. Han, S. Pascoli and B. Zhang, JHEP **0905**, 030 (2009)]

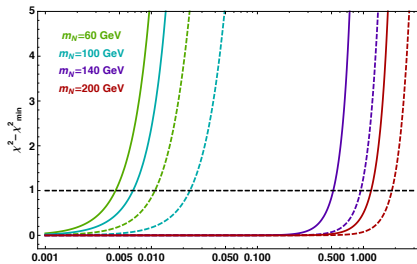
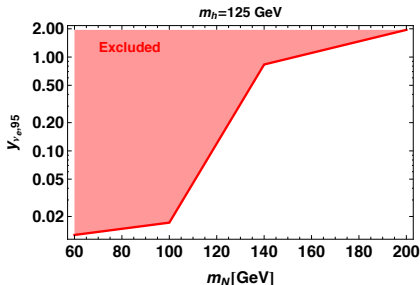
# Constraints from LHC Higgs Data



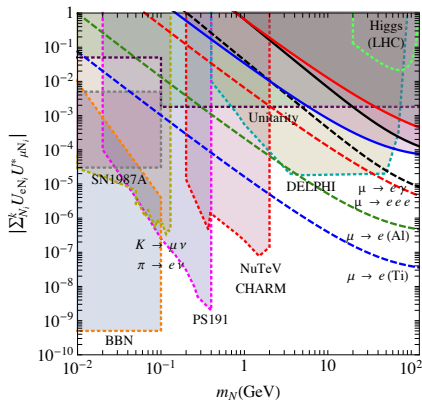
- Additional number of events expected in the  $h \rightarrow 2\ell 2\nu$  channel:

$$n(m_N, y) = \mathcal{L}\sigma_{\text{tot}}(pp \rightarrow h) \left[ \epsilon_{\text{SM}} \frac{\Gamma(h \rightarrow WW^* \rightarrow \ell\bar{\ell}\nu\bar{\nu})}{\Gamma_{\text{SM}} + \Gamma_N} + \sum_{j,k} \epsilon_{jk} \frac{\Gamma(h \rightarrow \bar{\nu}N + \text{c.c.} \rightarrow \ell_j\bar{\ell}_k\nu\bar{\nu})}{\Gamma_{\text{SM}} + \Gamma_N} \right]$$

- Require  $n(m_N, y) < 95\%$  CL upper limit from LHC Higgs data.



# LFV Constraints



[R. Alonso, M. Dhen, M. B. Gavela and T. Hambye, JHEP **1301**, 118 (2013)]

- Only constrains the product  $|V_{\ell N} V_{\ell' N}^*|$  (with  $\ell \neq \ell'$ ), and *not* the individual  $|V_{\ell N}|^2$ .

# Constraints from Non-unitarity

- The full seesaw matrix is diagonalized by the unitary matrix  $\mathcal{V} = \begin{pmatrix} U_L & \xi \\ \xi' & U_R \end{pmatrix}$ .
- For large  $\xi$ , the  $(3 \times 3)$  PMNS mixing matrix  $U_L$  is no longer unitary.
- Non-unitarity can be parametrized by  $\epsilon = U_L^\dagger U_L = I_3 - \eta$ .
- Off-diagonal entries of  $\epsilon$  are measures of the non-unitarity.

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- Several observable effects:
  - Modified neutrino oscillation probability, e.g.,

$$P_{\mu\tau} \simeq 4s_{23}^2 c_{23}^2 \sin^2 \left( \frac{\Delta m_{31}^2 L}{4E} \right) - 4|\eta_{\mu\tau}| \sin \delta_{\mu\tau} s_{23} c_{23} \sin \left( \frac{\Delta m_{31}^2 L}{4E} \right) + 4|\eta_{\mu\tau}|^2$$

Has a **zero-length effect**. [E. Fernandez-Martinez, M. B. Gavela, J. Lopez-Pavon, and O. Yasuda, *PLB* **649**, 427 (2007)]

- Suppression of  $W$  and  $Z$  coupling to light neutrinos.
- Contribution to EW precision observables.



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- Suppression of  $W$  and  $Z$  coupling to light neutrinos.
- Contribution to EW precision observables.
- Current limits (from a global fit of neutrino oscillation data, electroweak decays, lepton universality tests, and rare charged lepton decays): [Antusch, Biggio, Fernandez-Martinez, Gavela, Lopez-Pavon, *JHEP* **0610**, 084 (2006); Abada, Biggio, Bonnet, Gavela, Hambye, *JHEP* **0712**, 061 (2007)]

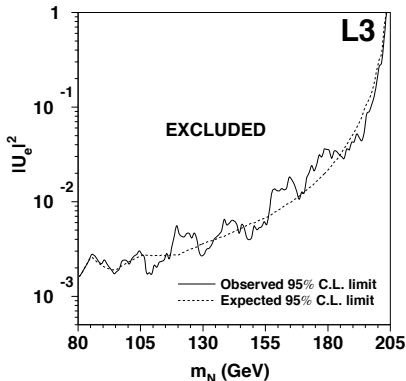
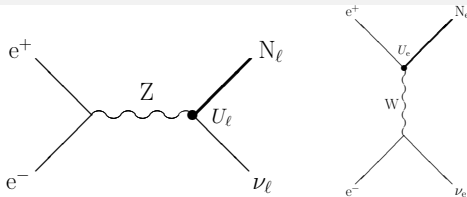
$$|\epsilon|_{\text{exp}} \approx \begin{pmatrix} 0.994 \pm 0.005 & < 7.0 \times 10^{-5} & < 1.6 \times 10^{-2} \\ < 7.0 \times 10^{-5} & 0.995 \pm 0.005 & < 1.0 \times 10^{-2} \\ < 1.6 \times 10^{-2} & < 1.0 \times 10^{-2} & 0.995 \pm 0.005 \end{pmatrix}.$$

# Constraints from EWPD

- Heavy neutrinos contribute to the  $S$ ,  $T$ ,  $U$  parameters. [Kniehl and Kohrs, PRD **48**, 225 (1993); Akhmedov, Kartavtsev, Lindner, Michaels, and Smirnov, JHEP **1305**, 081 (2013)]
- Tree-level non-unitarity effects and loop-level oblique corrections both affect the EWPD.
- Global fit gives an indirect limit on heavy-light mixing: [del Aguila, de Blas and Perez-Victoria, PRD **78**, 013010 (2008)]
- The current best limit for  $|V_{\mu N}|$  and  $|V_{\tau N}|$  for  $M_N > M_Z$ .

| Coupling         |                | $N$   |
|------------------|----------------|-------|
| Only with $e$    | $ V  <$        | 0.055 |
|                  | $ V_{\min}  =$ | 0.035 |
| Only with $\mu$  | $ V  <$        | 0.057 |
|                  | $ V_{\min}  =$ | 0.036 |
| Only with $\tau$ | $ V  <$        | 0.079 |
|                  | $ V_{\min}  =$ | 0.057 |
| Universal        | $ V  <$        | 0.038 |
|                  | $ V_{\min}  =$ | 0.025 |

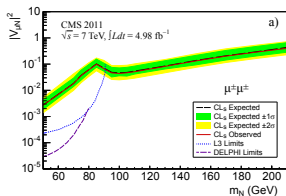
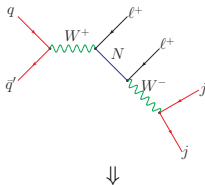
# Direct Search Limits from LEP



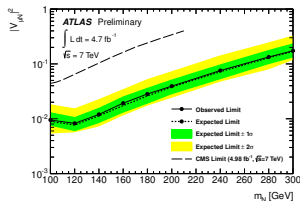
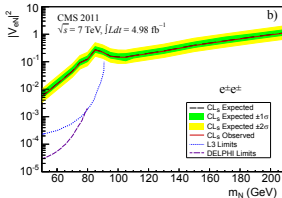
Looked for an isolated electron plus hadronic jets ( $N \rightarrow eW \rightarrow ejj$ ). [L3 Collaboration, PLB **517**, 67 (2001)]

# Direct Search Limits from LHC7

- Within SM seesaw framework, the only channel examined at the LHC so far:



[CMS Collaboration, PLB **717**, 109 (2012)]



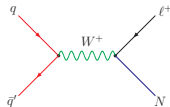
[ATLAS-CONF-2012-139]

- Signal strength depends on the largeness of  $V_{\ell N}$ .
- Can effectively probe heavy neutrinos only if  $M_N \lesssim 300$  GeV and  $|V_{\ell N}|^2 \gtrsim 10^{-3}$ .

[Datta, Guchait, Pilaftsis '93; Han, Zhang '06; del Aguila, Aguilar-Saavedra, Pittau '07;...]

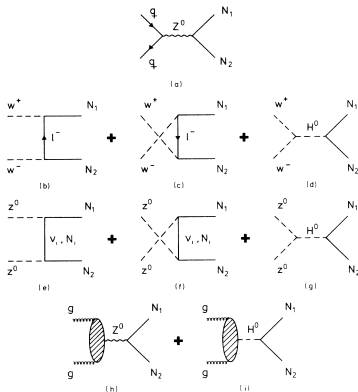
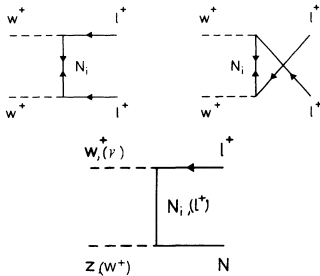
# Heavy Neutrino Production at the LHC

- LHC searches considered only



- Many other production modes, but most of them are negligible.

[A. Datta, M. Guchait and A. Pilaftsis, PRD **50**, 3195 (1994)]



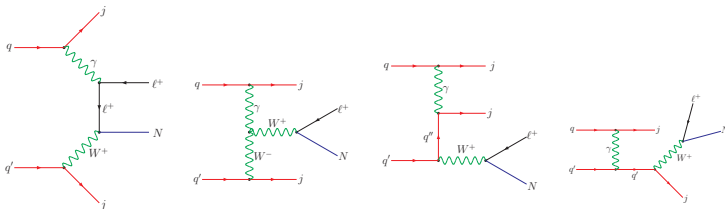
# A New *Dominant* Production Channel

[PSBD, A. Pilaftsis, U.-k. Yang, arXiv:1308.2209 [hep-ph]]

- Diagrams involving virtual photons in the  $t$ -channel give rise to *diffractive* processes, e.g.,

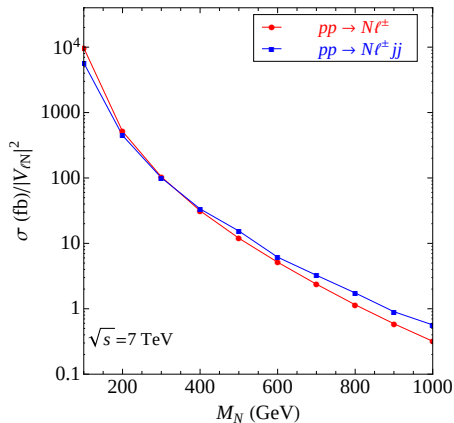
$$pp \rightarrow W^* \gamma^* jj \rightarrow \ell^\pm N jj ,$$

which are *not* negligible, but infrared enhanced.

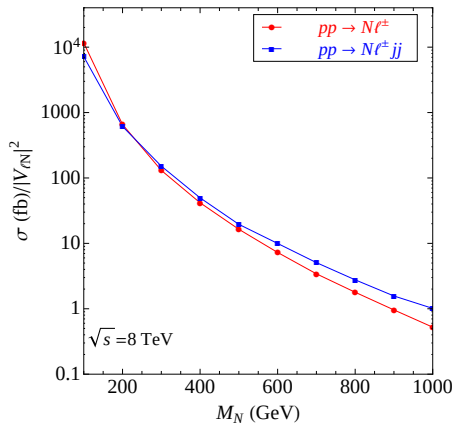


- Divergent inclusive cross section due to collinear singularity caused by the photon propagator.
- A minimum  $p_T^j$  cut required to make the cross section finite.
- Collinear divergence of the low- $p_T^j$  regime is absorbed into an effective photon structure function for the proton (analogous to the Weizsäcker-Williams equivalent photon approximation for electrons).

# Comparison of the Production Cross Sections

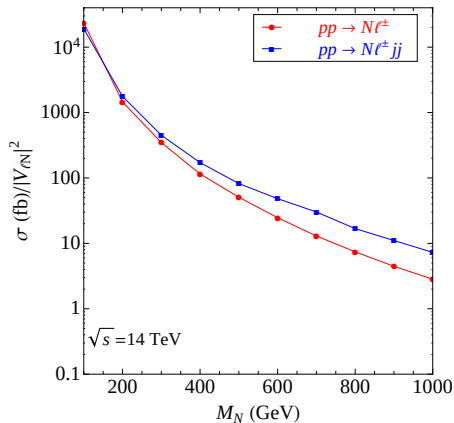


# Comparison of the Production Cross Sections





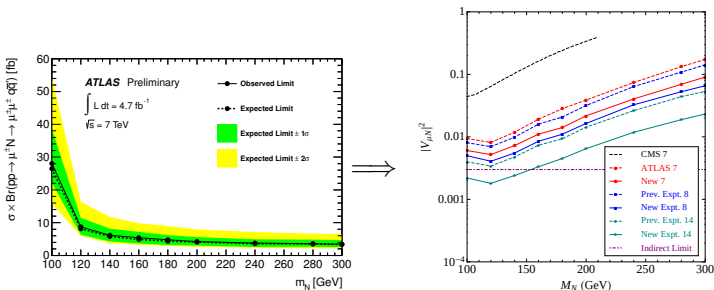
# Comparison of the Production Cross Sections



# Comparison of the Production Cross Sections

- The hadronic channels for  $pp \rightarrow N\ell^\pm jj$  mediated by virtual gluons and quarks give  $\mathcal{O}(\alpha_s)$  corrections and drop at the same rate as the  $pp \rightarrow N\ell^\pm$  cross section.
- The total electroweak ( $\gamma + Z$ ) contribution for  $pp \rightarrow N\ell^\pm jj$  drops at a rate slower than the  $pp \rightarrow N\ell^\pm$  cross section with increasing  $M_N$ .
- The production channel  $N\ell^\pm jj$  dominates over the earlier considered  $N\ell^\pm$  channel with increasing  $M_N$ .
- Similar behavior with increasing  $\sqrt{s}$  in the  $pp$  collisions.
- The crossover point shifts towards lower  $M_N$  with increasing  $\sqrt{s}$ .
- Thus, the  $N\ell^\pm jj$  process becomes increasingly important for  $M_N \gtrsim 200$  GeV.
- Must be taken into account in present and future analyses of the LHC data.

# Improved Upper Limit on Mixing



[PSBD, Pilaftsis, Yang, arXiv:1308.2209]

- Improved direct limits are rather conservative since we used only the  $\int L dt = 4.7 \text{ fb}^{-1}$  data at  $\sqrt{s} = 7 \text{ TeV}$  LHC ( $\sim 1\%$  of the total data expected).
- In practice, the direct limits from  $\sqrt{s} = 8$  and  $14 \text{ TeV}$  LHC data could be much more stringent (if no signal is observed!).

# Extension to Other Exotic Searches

- The infrared-enhanced mechanism can equally be extended to other exotic searches at the LHC.
- One example: In the context of type-II seesaw with singly and doubly-charged scalars, we have vertices of the form  $H^+ H^- A_\mu A_\nu$  and  $H^{++} H^{--} A_\mu A_\nu$ .
- Lead to diffractive processes such as

$$\begin{aligned} pp &\rightarrow \gamma^* \gamma^* jj \rightarrow H^{++} H^{--} jj \rightarrow \ell^+ \ell^+ \ell^- \ell^- jj \\ pp &\rightarrow \gamma^* \gamma^* jj \rightarrow H^+ H^- jj \rightarrow \ell^+ \nu \ell^- \bar{\nu} jj \end{aligned}$$

- Expected to dominate over the usually considered search channel

$$pp \rightarrow Z/\gamma^* \rightarrow H^{++} H^{--} \rightarrow \ell^+ \ell^+ \ell^- \ell^-$$

- LHC exclusion limits for  $M_{H^{\pm\pm}}$  can be improved significantly. [PSBD, T. Figy (work in progress)]

# Left-Right Seesaw

- L-R gauge group  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  provides a natural embedding of the heavy neutrinos and seesaw physics. [Pati, Salam '74; Mohapatra, Pati '75; Mohapatra, Senjanović '75]
  - $N$  is the parity partner of  $\nu_L$  and required by anomaly cancellation.
  - Scale of  $SU(2)_R$ -breaking sets the seesaw scale.

- Basic features:

- Fermions:  $Q_L \equiv \begin{pmatrix} u_L \\ d_L \end{pmatrix} \xrightarrow{P} \begin{pmatrix} u_R \\ d_R \end{pmatrix} \equiv Q_R, \quad \psi_L \equiv \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \xrightarrow{P} \begin{pmatrix} N \\ e_R \end{pmatrix} \equiv \psi_R.$

- Scalars:  $\Delta_R \equiv \begin{pmatrix} \Delta_R^{+}/\sqrt{2} & \Delta_R^{++} \\ \Delta_R^0 & -\Delta_R^{+}/\sqrt{2} \end{pmatrix}, \quad \phi \equiv \begin{pmatrix} \phi_1^0 & \phi_2^+ \\ \phi_1^- & \phi_2^0 \end{pmatrix}.$

- Yukawa Lagrangian:

$$\begin{aligned} \mathcal{L}_Y = & h_{ij}^{q,a} \bar{Q}_{L,i} \phi_a Q_{R,j} + \tilde{h}_{ij}^{q,a} \bar{Q}_{L,i} \tilde{\phi}_a Q_{R,j} + h_{ij}^{\ell,a} \bar{L}_i \phi_a R_j \\ & + \tilde{h}_{ij}^{\ell,a} \bar{L}_i \tilde{\phi}_a R_j + f_{ij} (R_i R_j \Delta_R + L_i L_j \Delta_L) + \text{h.c.} \end{aligned}$$

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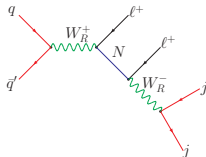
- $SU(2)_R \times U(1)_{B-L} \rightarrow U(1)_Y$  by  $\langle \Delta_R^0 \rangle = v_R$ . Leads to  $M_{W_R} = g_R v_R$ .
- $SU(2)_L \times U(1)_Y \rightarrow U(1)_{\text{em}}$  by  $\langle \phi \rangle = \text{diag}(\kappa', \kappa)$ .
- Leads to the fermion masses

$$\begin{aligned} M_U &= h^q \kappa' + \tilde{h}^q \kappa, \quad M_d = h^q \kappa + \tilde{h}^q \kappa', \quad M_\ell = h^\ell \kappa + \tilde{h}^\ell \kappa', \\ M_D &= h^\ell \kappa' + \tilde{h}^\ell \kappa, \quad M_N = f v_R \end{aligned}$$

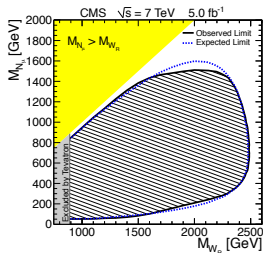
- Seesaw matrix fully determined.

# L-R Seesaw at the LHC

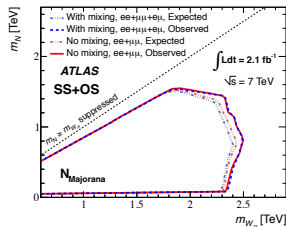
- New contribution via  $W_R$  exchange. [Keung and Senjanović, PRL **50**, 1427 (1983)]



- Independent of mixing effects. Could probe  $M_N$  up to 2-3 TeV, and  $M_{W_R}$  up to 5-6 TeV. [Ferrari *et al* '00; Nemevsek, Nesti, Senjanović, Zhang '11; Das, Deppisch, Kittel, Valle '12;...]
- Current LHC limits exclude  $M_{W_R}$  below about 2.5 TeV (depending on  $M_N$ ).

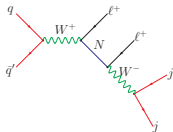


[CMS Collaboration, PRL **109**, 261802 (2012)]

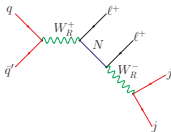


[ATLAS Collaboration, EPJC **72**, 2056 (2012)]

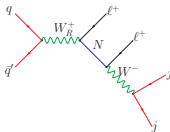
# New Diagram including Mixing Effects



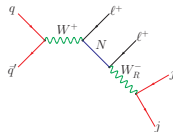
(a) LL



(b) RR

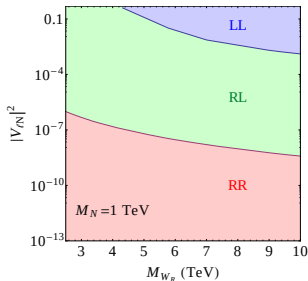
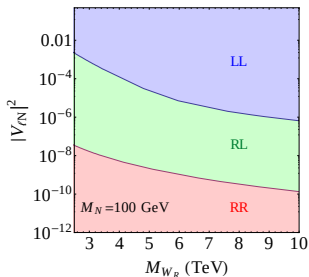


(c) RL



(d) LR

- RL diagram could dominate over LL and RR diagrams over a large range of L-R seesaw model parameter space.
- The L-R phase diagram for collider studies: [Chen, PSBD, and Mohapatra, PRD **88**, 033014 (2013)]





# A Unique Probe of $M_D$

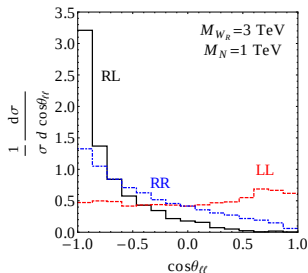
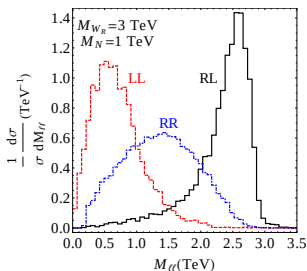
- The new RL mode is a unique probe of  $M_D$  in L-R seesaw at the LHC.
- Huge impact in low-energy searches of L-R seesaw:  $0\nu\beta\beta$ , LFV, electron EDM, neutrino transition moment, etc. [Nemevsek, Senjanović, and Tello, PRL **110**, 151802 (2013)]
- Immediate implication at high-energy: given an experimental limit on the  $\ell^\pm\ell^\pm jj$  cross section ( $\sigma_{\text{expt}}$ ),
  - $(M_N, M_{W_R})$  plane with  $\sigma_{\text{RL}} \geq \sigma_{\text{expt}}$  is ruled out. Complementary to that obtained from RR mode.
  - For  $\sigma < \tilde{\sigma}_{\text{LL}} < \sigma_{\text{expt}}$  (where  $\tilde{\sigma}_{\text{LL}}$  is  $\sigma_{\text{LL}}$  normalized to  $|V_{\ell N}|^2 = 1$ ), we can derive an improved limit on

$$|V_{\ell N}|^2 < \frac{\sigma_{\text{expt}} - \sigma_{\text{RL}}}{\tilde{\sigma}_{\text{LL}}}$$

- For LHC7, limits improve by about 10% at  $M_N = 300$  GeV.
- Better improvement for higher  $M_N$  and/or higher  $\sqrt{s}$ . Could be as high as 60%.
- Should be included in future LHC analyses to probe a bigger range of L-R seesaw parameter space.

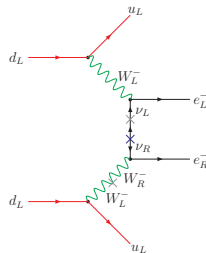
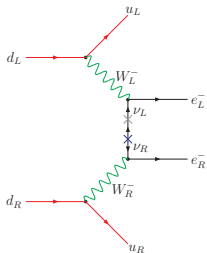
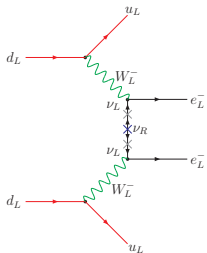
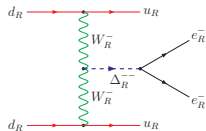
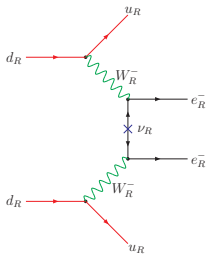
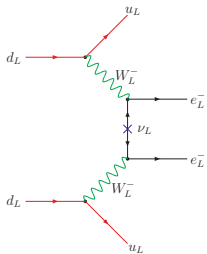
# Distinguishing RR from RL and LL

- Different helicity correlations lead to distinguishing features in the kinematic and angular distributions. [Han, Lewis, Ruiz, and Si, PRD **87**, 035011 (2013)]
- Can be used to pin down the dominant mode in L-R seesaw, if a signal is observed.



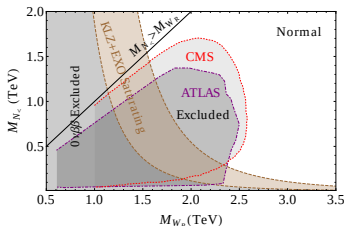
[Chen, PSBD, Mohapatra, PRD **88**, 033014 (2013)]

# Neutrinoless Double Beta Decay in L-R Seesaw

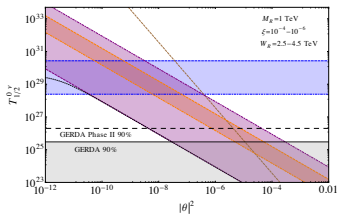
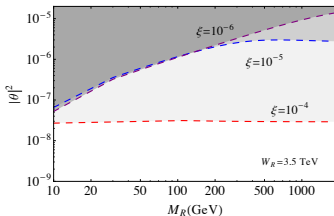


# Exclusion Limits from $0\nu\beta\beta$

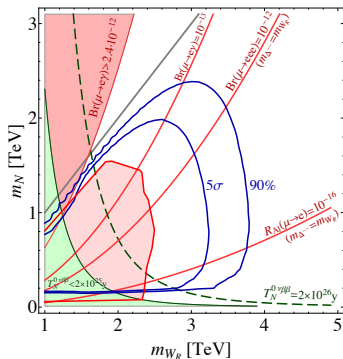
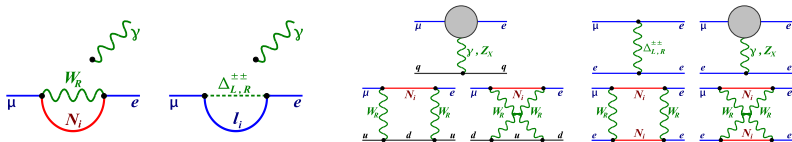
- Assuming dominance of purely RH-currents, can obtain exclusion regions complementary to those from the LHC. [PSBD, Goswami, Mitra, and Rodejohann, PRD (R) (2013)]



- For  $M_{W_R} \lesssim 10$  TeV, the  $\eta$ -diagram could provide the most stringent constraint on the electron-neutrino mixing parameter  $|V_{eN}|^2$ . [preliminary results]



# Charged Lepton Flavor Violation



[Das, Deppisch, Kittel and Valle, PRD **86**, 055006 (2012)]

# Large Heavy-Light Mixing with TeV-scale $M_N$

- In the 'vanilla' seesaw, for  $M_N \gtrsim \text{TeV}$ , we expect  $\xi \sim M_D M_N^{-1} \simeq (M_\nu M_N^{-1})^{1/2} \lesssim 10^{-6}$ .
- Suppresses all mixing effects to an unobservable level.
- Need special textures of  $M_D$  and  $M_N$  to have 'large' mixing effects even with TeV-scale  $M_N$ .  
[Pilaftsis '92; Kersten, Smirnov '07; Ibarra, Molinaro, Petcov '10; Mitra, Senjanović, Vissani '11; ...]
- One example: [Kersten, Smirnov '07]

$$M_D = \begin{pmatrix} m_1 & \delta_1 & \epsilon_1 \\ m_2 & \delta_2 & \epsilon_2 \\ m_3 & \delta_3 & \epsilon_3 \end{pmatrix} \text{ and } M_N = \begin{pmatrix} 0 & M_1 & 0 \\ M_1 & 0 & 0 \\ 0 & 0 & M_2 \end{pmatrix} \quad \text{with } \epsilon_i, \delta_i \ll m_i.$$

- In the limit  $\epsilon_i, \delta_i \rightarrow 0$ , the neutrino masses given by  $M_\nu \simeq -M_D M_N^{-1} M_D^T$  vanish, although the heavy-light mixing parameters given by  $\xi_{ij} \sim m_i/M_j$  can be large.

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- Can we have an L-R embedding of these textures?
- Nontrivial to find a phenomenologically viable scenario since  $M_D$  is related to  $M_\ell$  in L-R model.
- Also need to reproduce the observed neutrino masses and mixing.
- And all other experimental constraints.

# TeV-scale L-R Seesaw with Enhanced $V_{\ell N}$

- Supplement the L-R gauge group with a global discrete symmetry  $D = Z_4 \times Z_4 \times Z_4$ .  
[PSBD, Lee, and Mohapatra, PRD (2013)]
- The Yukawa Lagrangian invariant under this symmetry:

$$\mathcal{L}_{\ell,Y} = h_{\alpha 1} \bar{L}_\alpha \tilde{\phi}_1 R_1 + h_{\alpha 2} \bar{L}_\alpha \phi_2 R_2 + h_{\alpha 3} \bar{L}_\alpha \phi_3 R_3 + f_{12} R_1 R_2 \Delta_{R,1} + f_{33} R_3 R_3 \Delta_{R,2} + \text{h.c.}$$

| Field          | $Z_4 \times Z_4 \times Z_4$ Transformation |
|----------------|--------------------------------------------|
| $L_\alpha$     | (1, 1, 1)                                  |
| $R_1$          | (-i, 1, 1)                                 |
| $R_2$          | (1, -i, 1)                                 |
| $R_3$          | (1, 1, -i)                                 |
| $\phi_1$       | (-i, 1, 1)                                 |
| $\phi_2$       | (1, i, 1)                                  |
| $\phi_3$       | (1, 1, i)                                  |
| $\Delta_{R,1}$ | (i, i, 1)                                  |
| $\Delta_{R,2}$ | (1, 1, -1)                                 |



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- In the discrete symmetry limit,  $\langle \phi_a \rangle = \begin{pmatrix} 0 & 0 \\ 0 & \kappa_a \end{pmatrix}$  (with  $a = 1, 2, 3$ ).

$$M_\ell = \begin{pmatrix} 0 & h_{12} \kappa_2 & h_{13} \kappa_3 \\ 0 & h_{22} \kappa_2 & h_{23} \kappa_3 \\ 0 & h_{32} \kappa_2 & h_{33} \kappa_3 \end{pmatrix}, \quad M_D = \begin{pmatrix} h_{11} \kappa_1 & 0 & 0 \\ h_{21} \kappa_1 & 0 & 0 \\ h_{31} \kappa_1 & 0 & 0 \end{pmatrix}, \quad M_N = \begin{pmatrix} 0 & f_{12} v_{R1} & 0 \\ f_{12} v_{R1} & 0 & 0 \\ 0 & 0 & 2f_{33} v_{R2} \end{pmatrix}.$$

- In this limit,  $m_e = 0$  and  $m_{\nu,i} = 0$ .

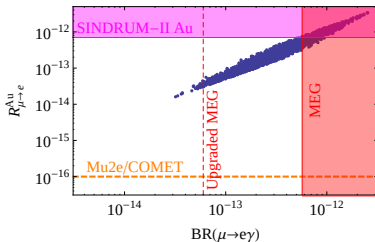
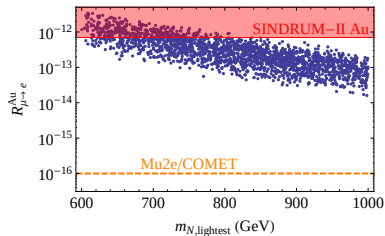
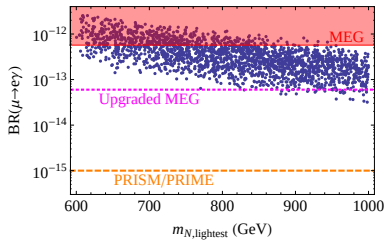
# A Predictive and Testable Model

- Discrete symmetry broken by  $\langle \phi_a \rangle = \begin{pmatrix} \delta\kappa_a & 0 \\ 0 & \kappa_a \end{pmatrix}$ , where  $\delta\kappa_a \ll \kappa_a$ .
- Can be generated naturally through loop-effects.
- $\delta\kappa$ 's responsible for nonzero electron mass as well as neutrino masses:

$$M_\ell = \begin{pmatrix} h_{11}\delta\kappa_1 & h_{12}\kappa_2 & h_{13}\kappa_3 \\ h_{21}\delta\kappa_1 & h_{22}\kappa_2 & h_{23}\kappa_3 \\ h_{31}\delta\kappa_1 & h_{32}\kappa_2 & h_{33}\kappa_3 \end{pmatrix}, \quad M_D = \begin{pmatrix} h_{11}\kappa_1 & h_{12}\delta\kappa_2 & h_{13}\delta\kappa_3 \\ h_{21}\kappa_1 & h_{22}\delta\kappa_2 & h_{23}\delta\kappa_3 \\ h_{31}\kappa_1 & h_{32}\delta\kappa_2 & h_{33}\delta\kappa_3 \end{pmatrix}.$$

- Can be written in an upper-triangular form: **only 11 free parameters**.
- Has to fit 3 charged lepton and 3 neutrino masses, 3 neutrino mixing angles, constraints on mixing  $V_{\ell_i N_j}$  (unitarity, LFV, etc), and on  $V_{R12}^\ell$  (from  $\mu \rightarrow 3e$ ).
- **Hence predictive and testable!!**
- Collider signal: LL mode absent. Only RL and RR modes observable.
- Only  $\mu^\pm e^\pm jj$  final states in the RL mode.
- Probes LNV and LFV simultaneously.

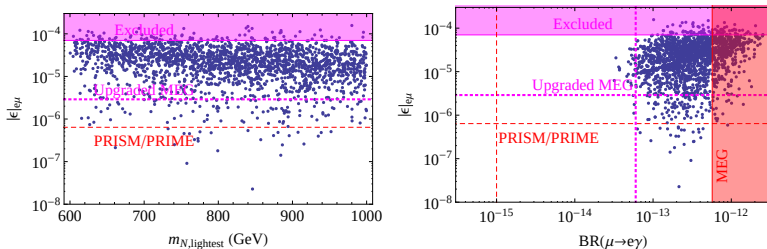
# LFV Predictions



[PSBD, Lee, and Mohapatra, PRD (2013)]

# Leptonic Non-unitarity Effects

- For large  $V_{\ell N}$ , the light neutrino mixing matrix could have large deviations from unitarity.



- Non-zero  $CP$ -phases can lead to observable leptonic  $CP$ -violation. [\[ongoing work\]](#)

# $0\nu\beta\beta$ Predictions

| Parameter           | Best-fit Value        | Current Limit<br>[Barry and Rodejohann, JHEP <b>1309</b> , 153 (2013)] |
|---------------------|-----------------------|------------------------------------------------------------------------|
| $ \eta_\nu^L $      | $8.1 \times 10^{-11}$ | $\lesssim 7.1 \times 10^{-7}$                                          |
| $ \eta_{\nu_R}^R $  | $4.4 \times 10^{-12}$ | $\lesssim 7.0 \times 10^{-9}$                                          |
| $ \eta_{\nu_R}^L $  | $1.2 \times 10^{-19}$ | $\lesssim 7.0 \times 10^{-9}$                                          |
| $ \eta_{\Delta_R} $ | $2.1 \times 10^{-10}$ | $\lesssim 7.0 \times 10^{-9}$                                          |
| $ \eta_\lambda $    | $1.5 \times 10^{-8}$  | $\lesssim 5.7 \times 10^{-7}$                                          |
| $ \eta_\eta $       | $1.5 \times 10^{-9}$  | $\lesssim 3.0 \times 10^{-9}$                                          |

$$\frac{1}{T_{1/2}^{0\nu}} = G_{01}^{0\nu} \left[ |\mathcal{M}_\nu^{0\nu}|^2 |\eta_\nu^L|^2 + |\mathcal{M}_{\nu_R}^{0\nu}|^2 (|\eta_{\nu_R}^L|^2 + |\eta_{\nu_R}^R + \eta_{\Delta_R}|^2) + |\mathcal{M}_\lambda^{0\nu}|^2 |\eta_\lambda|^2 + |\mathcal{M}_\eta^{0\nu}|^2 |\eta_\eta|^2 + \text{interference terms} \right]$$

| Nucleus           | Model Prediction for $T_{1/2}^{0\nu}$ (yr) | Current Limit (yr)                         | Future Limit (yr)                       |
|-------------------|--------------------------------------------|--------------------------------------------|-----------------------------------------|
| $^{76}\text{Ge}$  | $6.2 \times 10^{25} - 6.2 \times 10^{27}$  | $> 2.1 (3.0) \times 10^{25}$ (GERDA-I)     | $6 \times 10^{27}$ (GERDA-II, MAJORANA) |
| $^{136}\text{Xe}$ | $2.3 \times 10^{25} - 4.3 \times 10^{26}$  | $> 1.9 (3.1) \times 10^{25}$ (KamLand-Zen) | $8 \times 10^{26}$ (EXO-1000)           |

# Conclusion

- A simple paradigm for neutrino masses: Type-I Seesaw.
- Two key aspects: Majorana neutrino mass and Heavy-light neutrino mixing.
- Large mixing effects can be tested at the Intensity Frontier.
- Both aspects can be tested *directly* at the Energy Frontier.
- New heavy neutrino production mechanism gives improved LHC sensitivity due to infrared enhancement effects.

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**THANK YOU.**



# Selection Efficiency

- To compare with the old limits, we use the same selection criteria as used by ATLAS for  $pp \rightarrow \mu^\pm \mu^\pm jj$ :

$$p_T^j > 20 \text{ GeV}, p_T^\mu > 20 \text{ GeV}, p_T^{\mu, \text{leading}} > 25 \text{ GeV},$$

$$|\eta^j| < 2.8, |\eta^\mu| < 2.5, \Delta R^{jj} > 0.4, \Delta R^{\mu j} > 0.4,$$

$$m_{\mu\mu} > 15 \text{ GeV}, E_T^{\text{miss}} < 35 \text{ GeV}, m_{jj} \in [55, 120] \text{ GeV}.$$

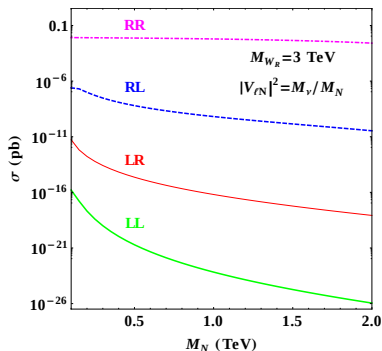
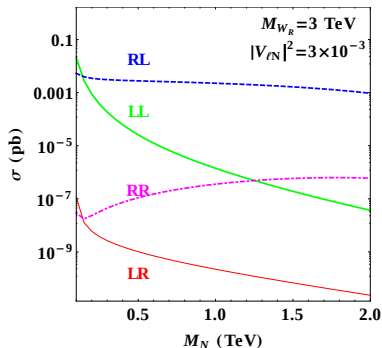
- Total selection efficiency for the  $\mu^\pm \mu^\pm$  signal remains almost the same as before.

| Signal $m_N$ [GeV]       | 100 | 120  | 140  | 160  | 180  | 200  | 240  | 280  | 300  |
|--------------------------|-----|------|------|------|------|------|------|------|------|
| Selection Efficiency [%] | 3.9 | 13.0 | 18.1 | 21.3 | 23.9 | 25.7 | 28.7 | 30.8 | 31.7 |

- SM background for di-muon+ $n$  jets (with  $n \geq 2$ ):

| Source                 | $\mu^\pm \mu^\pm$               |
|------------------------|---------------------------------|
| $WZ$                   | $1.0 \pm 0.2 \pm 0.3$           |
| $ZZ$                   | $0.22 \pm 0.05^{+0.07}_{-0.06}$ |
| $W^\pm W^\pm$          | $0.15 \pm 0.04 \pm 0.08$        |
| $t\bar{t} + V$         | $0.23 \pm 0.04 \pm 0.12$        |
| Charge mis-measurement | $< 0.03$                        |
| Non-prompt             | $1.1 \pm 0.5^{+0.6}_{-0.5}$     |
| Total background       | $2.7 \pm 0.5^{+0.7}_{-0.6}$     |
| Data                   | 3                               |

# Comparison between LL, RL and RR Cross Sections

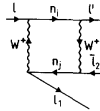


[Chen, PSBD, Mohapatra, PRD **88**, 033014 (2013)]

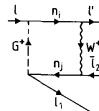
$$l_i \rightarrow \bar{l}_j l_k l_m$$



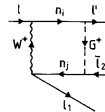
(a)



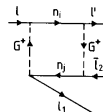
(b)



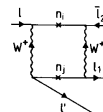
(c)



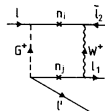
(d)



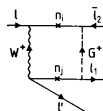
(e)



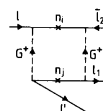
(f)



(g)



(h)

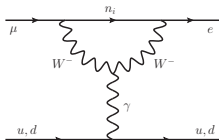


(i)

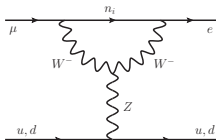
$$+ (l_1 \leftrightarrow l')$$

[Ilakovac, Pilaftsis, NPB **437**, 491 (1995)]

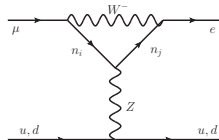
# $\mu - e$ Conversion



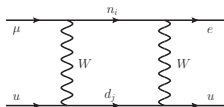
(a) Photon Penguin Diagram



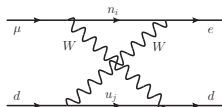
(b) Z Penguin Diagram



(c) Z Penguin Diagram



(d) Box Diagram



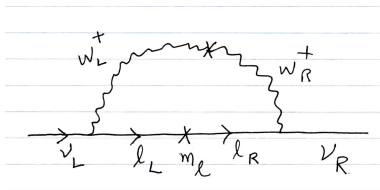
(e) Box Diagram

[Alonso, Dhen, Gavela, Hambye, JHEP **1301**, 118 (2013)]

# Why $Z_4 \times Z_4 \times Z_4$ ?

- Choice of the product of  $Z_4$  groups reduces possible multiple  $U(1)$  symmetries of the model associated with different bi-doublets.
- Other  $Z_n$ 's restrict the terms in the Higgs potential so much that the discrete group will get promoted to a continuous  $U(1)$  group, whose spontaneous breaking by non-zero vevs of  $\phi_a$  will lead to a massless Goldstone boson.
- With the  $Z_4$  group, terms like  $\lambda_a \text{Tr}[(\phi_a^\dagger \tilde{\phi}_a)^2]$  break the  $U(1)$  symmetry while keeping the  $Z_4$  subgroup of it intact (for  $\lambda_a \neq 0$ ).
- Gives mass of order  $\lambda_a \kappa_a^2$  (sub-TeV scale) to the leptophilic Higgses.
- Could also add soft  $D$ -breaking terms like  $\text{Tr}(\phi_a^\dagger \phi_b)$  without destabilizing the vacuum.

# Generating $\delta\kappa$ through Loops



$$(\delta m_D)_{\alpha i} \simeq \frac{g^2 h_{\alpha i \kappa}}{16\pi^2} \frac{g^2 \kappa_q \kappa'_q}{M_{W_R}^2} \simeq 10^{-6} h_{\alpha i \kappa}$$

# A Sample Fit

$$\begin{aligned}
 M_\ell &= \begin{pmatrix} 0.00153973 & -0.0511895 & -1.61367 \\ 0 & 0.0961545 & -0.366453 \\ 0 & 0 & -0.647105 \end{pmatrix} \text{ GeV}, \\
 M_D &= \begin{pmatrix} 14.0638 & -7.5 \times 10^{-10} & -1.8 \times 10^{-4} \\ 0 & 1.4 \times 10^{-9} & -4.1 \times 10^{-5} \\ 0 & 0 & -7.2 \times 10^{-5} \end{pmatrix} \text{ GeV}, \\
 M_N &= \begin{pmatrix} 0 & 814.118 & 0 \\ 814.118 & 0 & 0 \\ 0 & 0 & -2549.95 \end{pmatrix} \text{ GeV}. \\
 V_{\ell N} &= \begin{pmatrix} -0.004 & 0.004 & 7.7 \times 10^{-13} \\ 0.003 & -0.003 & 6.9 \times 10^{-11} \\ 0.011 & -0.011 & -7.7 \times 10^{-8} \end{pmatrix}.
 \end{aligned}$$

| Output Parameter  | Value                              |
|-------------------|------------------------------------|
| $m_e$             | 0.511 MeV                          |
| $m_\mu$           | 105.61 MeV                         |
| $m_\tau$          | 1.777 GeV                          |
| $\Delta m_{21}^2$ | $7.62 \times 10^{-5} \text{ eV}^2$ |
| $\Delta m_{31}^2$ | $2.41 \times 10^{-3} \text{ eV}^2$ |
| $\theta_{12}$     | $33.8^\circ$                       |
| $\theta_{23}$     | $39.1^\circ$                       |
| $\theta_{13}$     | $8.6^\circ$                        |
| $m_{N_1}$         | 814.24 GeV                         |
| $m_{N_2}$         | -814.24 GeV                        |
| $m_{N_3}$         | 2550 GeV                           |