Discovery Reach for Non-Standard Interactions in a Neutrino Factory

hep-ph/0702269

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Introduction

References: P. Huber and J. W. F. Valle, Phys. Lett. **B523** (2001) 151. P. Huber, T. Schwetz, J. W. F. Valle, Phys. Rev. **D66** (2002) 013006. A. M. Gago, M. M. Guzzo, H. Nunokawa, W. J. C. Teves, and R. Zukanovich Funchal Phys. Rev. **D64** (2001) 073003. Y. Grossman, Phys. Lett. **B359** (1995) 141. M. C. Gonzalez-Garcia, Y. Grossman, A. Gusso, and Y. Nir, Phys. Rev. **D64** (2001) 096006. A. Bueno, M. Campanelli, M. Laveder, J. Rico, and A. Rubbia, JHEP **0106** (2001) 032. G. L. Fogli, E. Lisi, A. Mirizzi, and D. Montanino, Phys. Rev. **D66** (2002) 013009. TO, J. Sato, and N. Yamashita, Phys. Rev. **D65** (2002) 093015. S. Davidson, C. Peña-Garay, N. Rius, and A. Santamaria, JHEP **0303** (2003) 011. M. Blennow, T. Ohlsson, and W. Winter, Eur. Phys. J. **C49** (2007) 1023. M. Blennow, T. Ohlsson, and J. Skrotzki, hep-ph/0702059, M. Honda, N. Okamura, and T. Takeuchi, hep-ph/0603268. N. Kitazawa, H. Sugiyama, and O. Yasuda hep-ph/0606013. A. Friedland and C. Lunardini, Phys. Rev. **D74** (2006) 033012. etc. etc...

Introduction — Motivation

- The aim of future neutrino experiments is the precision measurement of the oscillation parameters such as θ_{13} and $\delta_{\rm CP}$
  - Osc. probabilities will be measured with $\mathcal{O}(1\text{-}0.1)\%$ or higher accuracy.
  - We have a good chance to observe not only the standard oscillation phenomena but also the sub-leading effects induced by non-standard interactions (NSIs).

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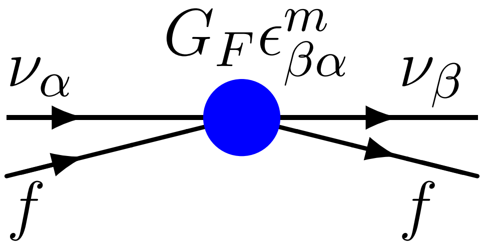
- NSIs — Flavour violating interactions with neutrinos such as $\nu_\alpha f \to \nu_\beta f$, $\ell_\alpha^- \to \nu_\beta e^- \bar{\nu}_e \ldots$
  - It can be written as eff. 4-Fermi int. as



$$-\mathcal{L}_{\mathrm{NSI}} = 2\sqrt{2} G_F \epsilon_{\beta\alpha}^m (\bar{\nu}_\beta \gamma^\rho P_L \nu_\alpha)(\bar{f} \gamma_\rho P_{L/R} f)$$

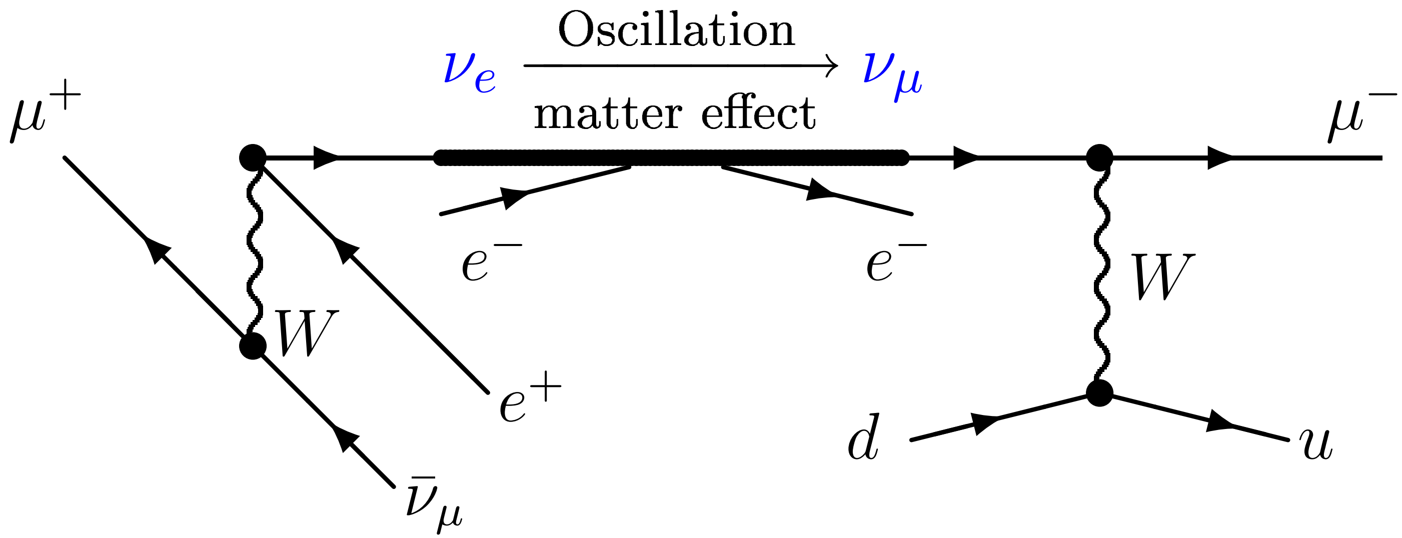
— We study the discovery reach of the NSIs in the osc. exp.

Introduction — Standard oscillation

- A long baseline exp. can be described diagrammatically as

$$\mathcal{A}(\nu_\mu N \to \mu^- X)\langle \nu_\mu | \mathrm{e}^{-\mathrm{i}HL} | \nu_e \rangle \mathcal{A}(\mu^+ \to e^+ \bar{\nu}_\mu \nu_e)$$

$$||$$



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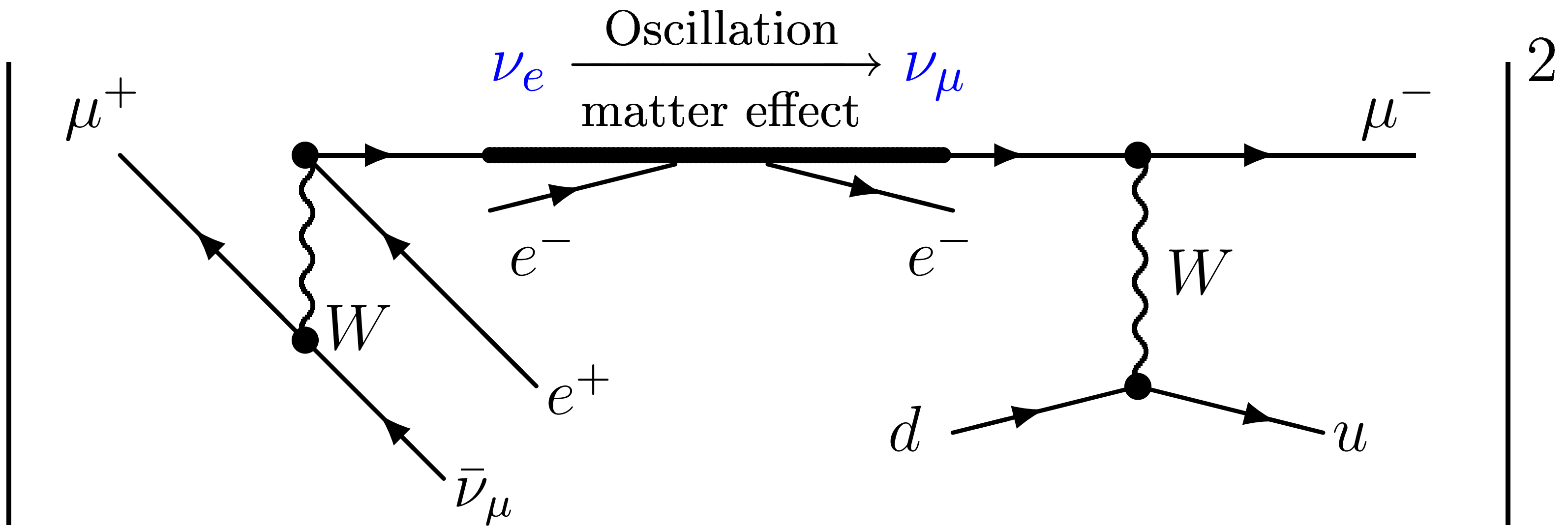
$$\parallel$$



Introduction — Standard oscillation

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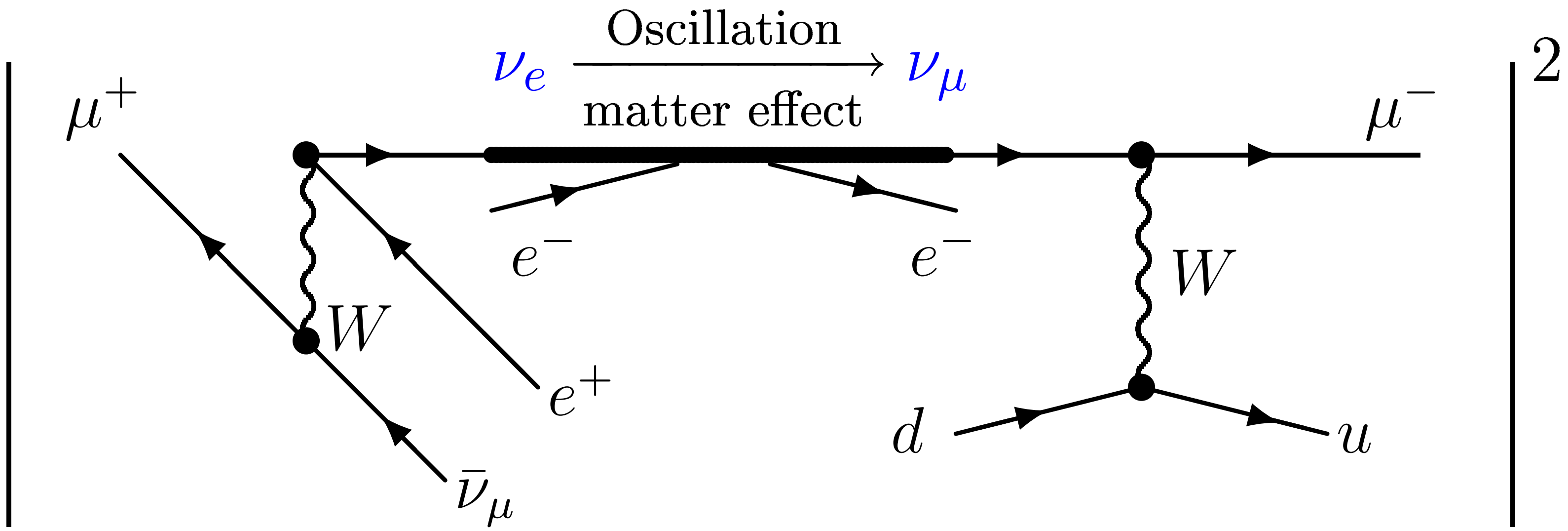
$$\sigma(\nu_\mu N \to \mu^- X) \times P_{\nu_e \to \nu_\mu} \times \Gamma(\mu^+ \to e^+ \bar{\nu}_\mu \nu_e)$$

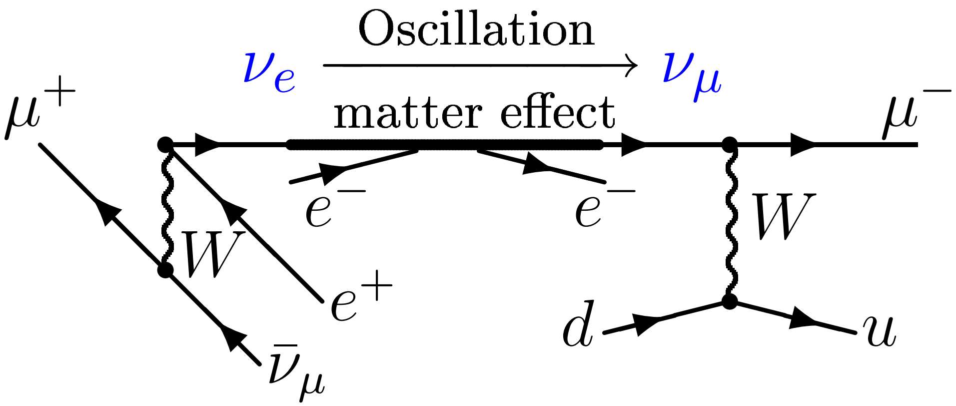
$$\Vert$$



Introduction — Oscillation enhanced search for NSIs

- ν osci. $=$ Flavour changing process

$$\ell_\alpha^- \xrightarrow{\text{CC}} \nu_\alpha \xrightarrow{\text{osc}} \nu_\beta \xrightarrow{\text{CC}} \ell_\beta^-$$



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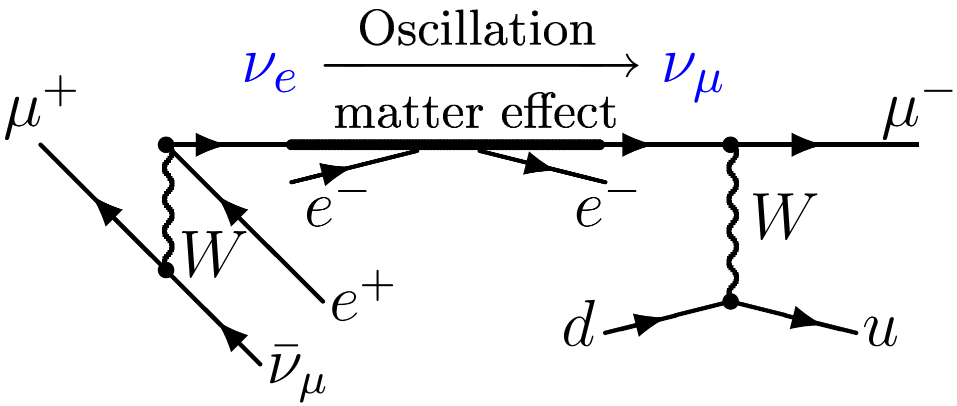

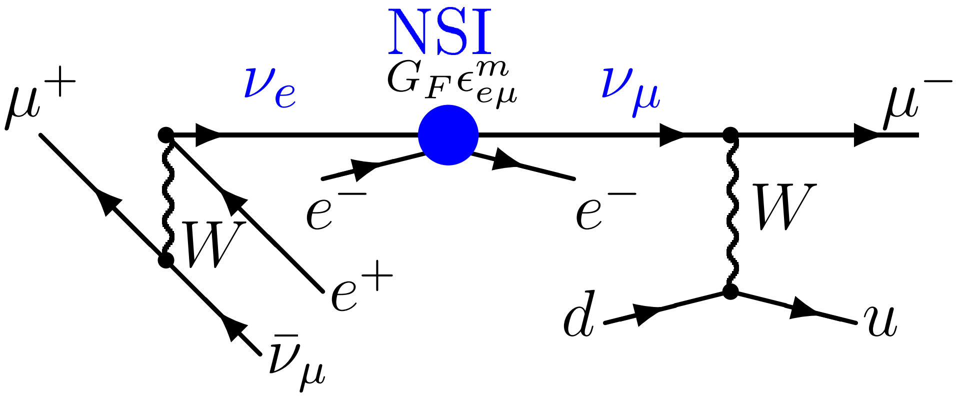

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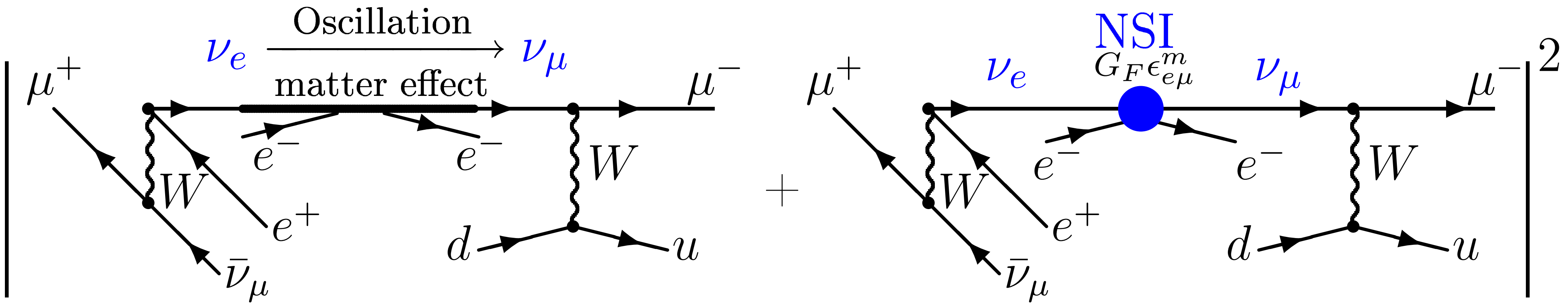
$$\ell_\alpha^- \xrightarrow{\text{CC}} \nu_\alpha \xrightarrow{\text{NSI}} \nu_\beta \xrightarrow{\text{CC}} \ell_\beta^-$$

— They interfere with each other.



- The signals of NSI appear in the osc. probability at $\mathcal{O}(\epsilon^m_{e\mu})$.
  — This is quite different from the charged lepton LFV process.
  e.g., $\mathrm{Br}(\mu \to 3e)$ is proportional to $|\epsilon^m_{e\mu}|^2$.

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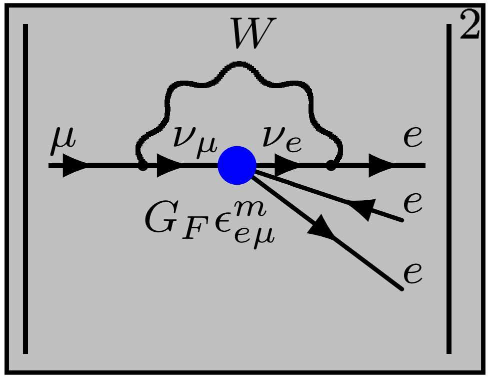
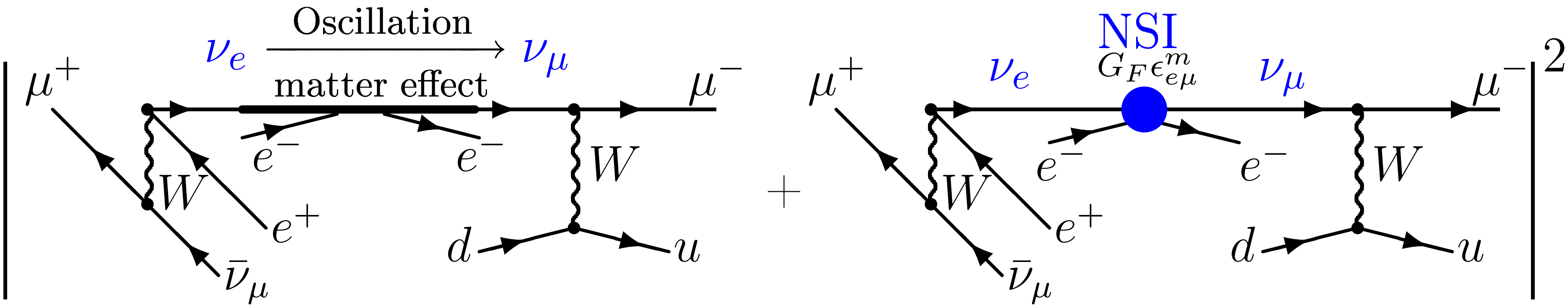


$|\epsilon^m_{e\mu}| < 5 \times 10^{-4}$ (90%CL)



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Introduction — NSIs in matter

- NSIs in matter can be described by extra potential terms — We parametrize them as

$$H_{\beta\alpha} = \frac{1}{2E_\nu}\left\{ U \begin{pmatrix} 0 & & \\ & \Delta m^2_{21} & \\ & & \Delta m^2_{31} \end{pmatrix} U^\dagger + \begin{pmatrix} a_{\rm CC} & & \\ & 0 & \\ & & 0 \end{pmatrix} + (V_{\rm NSI})_{\beta\alpha} \right\},$$

$$(V_{\rm NSI})_{\beta\alpha} = a_{\rm CC} \begin{pmatrix} \epsilon^m_{ee} & \epsilon^m_{e\mu} & \epsilon^m_{e\tau} \\ (\epsilon^m_{e\mu})^* & \epsilon^m_{\mu\mu} & \epsilon^m_{\mu\tau} \\ (\epsilon^m_{e\tau})^* & (\epsilon^m_{\mu\tau})^* & \epsilon^m_{\tau\tau}. \end{pmatrix}$$

- In general, each off-diagonal (flavour violating) element has a complex phase.

Discovery reach for NSIs in neutrino factory

Reference: P. Huber, M. Lindner, and W. Winter, Comput. Phys. Commun. **167** (2005) 195.

P. Huber, J. Kopp, M. Lindner, M. Rolinec, and W. Winter, hep-ph/0701187.

Discovery reach for NSIs in neutrino factory

- Discovery reach for $\epsilon^m_{e\mu}$ in neutrino factory
  — how small $|\epsilon^m_{e\mu}|$ can be found in the neutrino factory.
- We introduce a NSI as the complex parameter
  - There is no reason to consider it is a real parameter.
  - The discovery reach strongly depends on the phase.
- We turn off all NSIs other than the NSI which we study.
- Modified GLoBES software is used.
- The following values are adopted as the true value of the standard oscillation parameters

powered by
GLoBES

$$\sin^2 2\theta_{12}^{\text{true}} = 0.83, \quad \sin^2 2\theta_{13}^{\text{true}} = 0.01, \quad \sin^2 2\theta_{23}^{\text{true}} = 1.0,$$
$$(\Delta m^2_{21})^{\text{true}} = 8.2 \times 10^{-5}\ [\text{eV}^2], \quad (\Delta m^2_{31})^{\text{true}} = 2.5 \times 10^{-3}\ [\text{eV}^2].$$

Discovery reach for NSIs in neutrino factory

- Discovery reach for $|(\epsilon_{e\mu}^m)^{\text{true}}|$ is determined by[a]

  $$\chi^2 \equiv \min_{\lambda} \sum_i^{\text{bin}} \left| N_i\left(\lambda^{\text{true}}, (\epsilon_{e\mu}^m)^{\text{true}}\right) - N_i\left(\lambda, \epsilon_{e\mu}^m = 0\right) \right|^2 \Big/ V_i,$$

  where $\lambda \in \{\theta_{12}, \theta_{13}, \theta_{23}, \delta_{\text{CP}}, \Delta m_{21}^2, \Delta m_{31}^2, a_{\text{CC}}\}$.

- If $\chi^2 > \chi^2_{3\sigma}$, the effect induced by the NSI with the value of $|(\epsilon_{e\mu}^m)^{\text{true}}|$ will be discovered at the 3σ level.

- Undetermined parameters: $\delta_{\text{CP}}^{\text{true}}$ and $\arg[(\epsilon_{e\mu}^m)^{\text{true}}]$
  — We scan the value of χ^2 on the $\delta_{\text{CP}}^{\text{true}}$-$\arg[(\epsilon_{e\mu}^m)^{\text{true}}]$ plane for the fixed $|(\epsilon_{e\mu}^m)^{\text{true}}|$.

---

[a] In the numerical calculation, we use the χ^2 function for the Poisson distribution.

Discovery reach for $\epsilon^m_{e\mu}$ in neutrino factory

- In the case $|(\epsilon^m_{e\mu})^{\text{true}}| = 5 \times 10^{-4}$,
- $\boxed{|\epsilon^m_{e\mu}| \text{ is too small}}$

  ↓

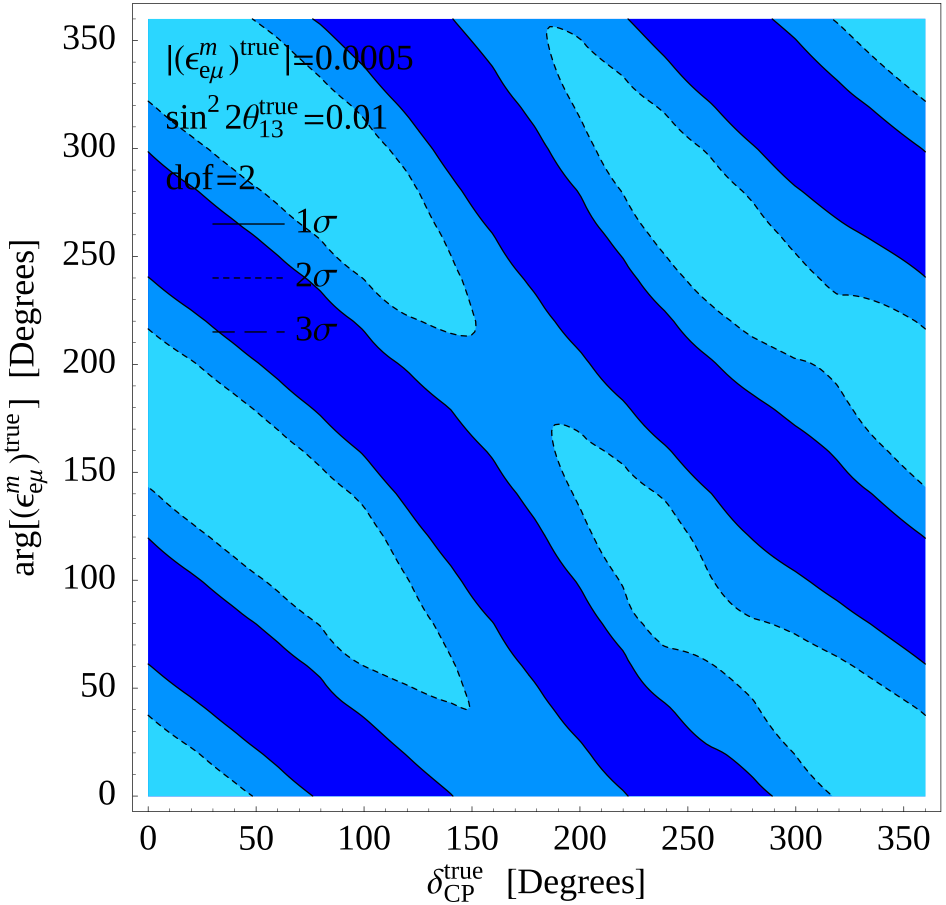
  χ^2 cannot exceed 3σ on the whole parameter plane. (Under the sea)

  ↓

  The deviation from the standard oscillation is not significant

  ↓

  No chance to discover!



Discovery reach for $\epsilon^{m}_{e\mu}$ in neutrino factory

- In the case $|(\epsilon^{m}_{e\mu})^{\rm true}| = 6 \times 10^{-4}$,
- $\boxed{|\epsilon^{m}_{e\mu}| \text{ becomes larger}}$

↓

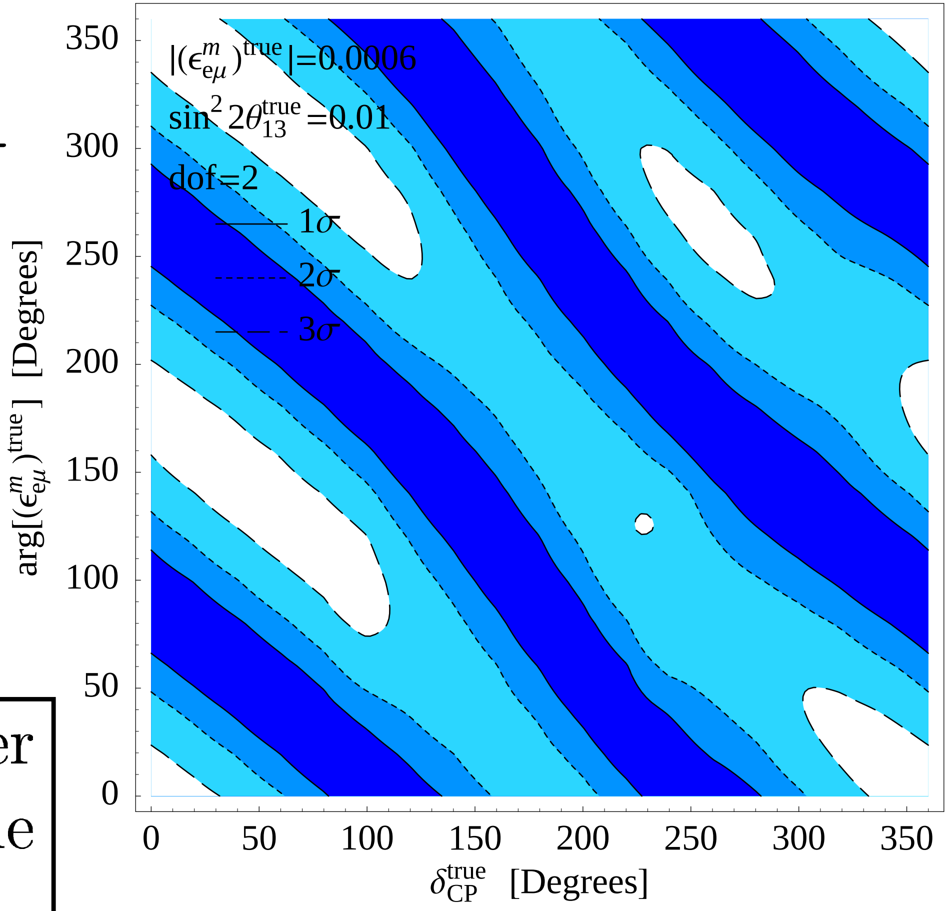
In some regions χ^2 exceeds 3σ (Islands appear)

↓

The deviation from the standard oscillation is significant at 3σ

↓

We have a chance to discover NSI effect depending on the phases



Discovery reach for $\epsilon^m_{e\mu}$ in neutrino factory

- In the case $|(\epsilon^m_{e\mu})^{\mathrm{true}}| = 1 \times 10^{-3}$,

- $\boxed{|\epsilon^m_{e\mu}| \text{ becomes larger}}$

  ↓

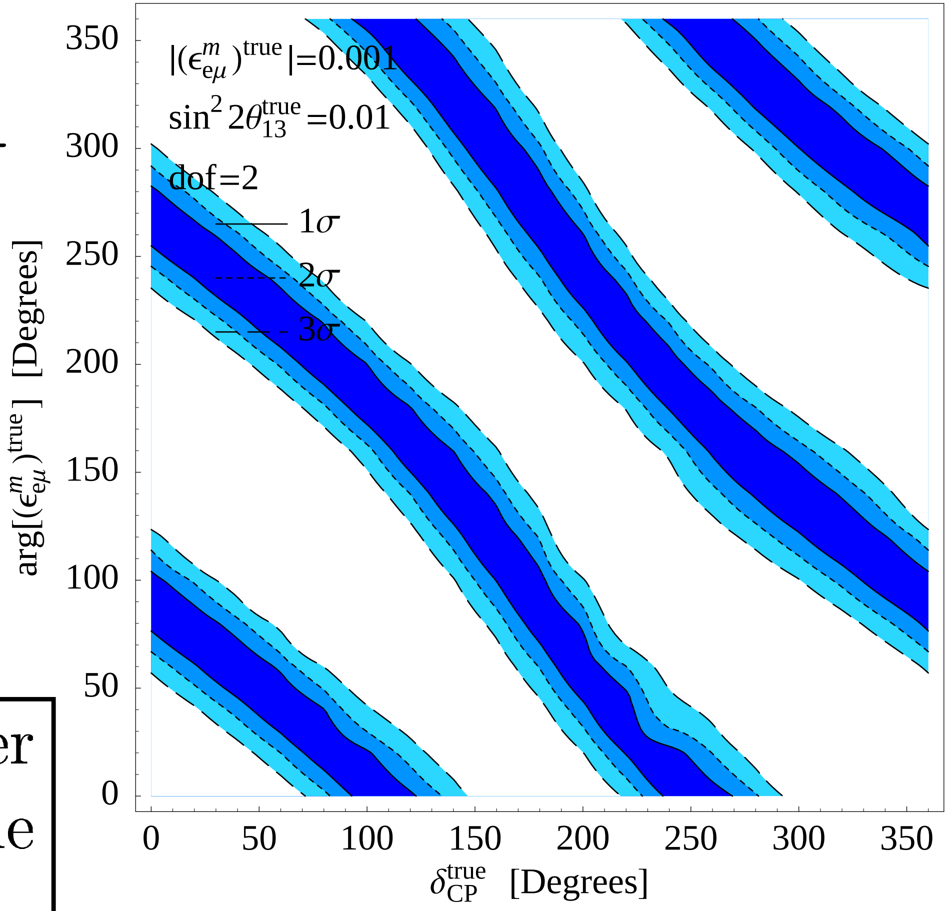
  In some regions χ^2 exceeds 3σ (Islands appear)

  ↓

  The deviation from the standard oscillation is significant at 3σ

  ↓

  We have a chance to discover NSI effect depending on the phases



Discovery reach for $\epsilon^m_{e\mu}$ in neutrino factory

- In the case $|(\epsilon^m_{e\mu})^{\text{true}}| = 2 \times 10^{-3}$,
- $\boxed{|\epsilon^m_{e\mu}| \text{ becomes larger}}$

  ↓

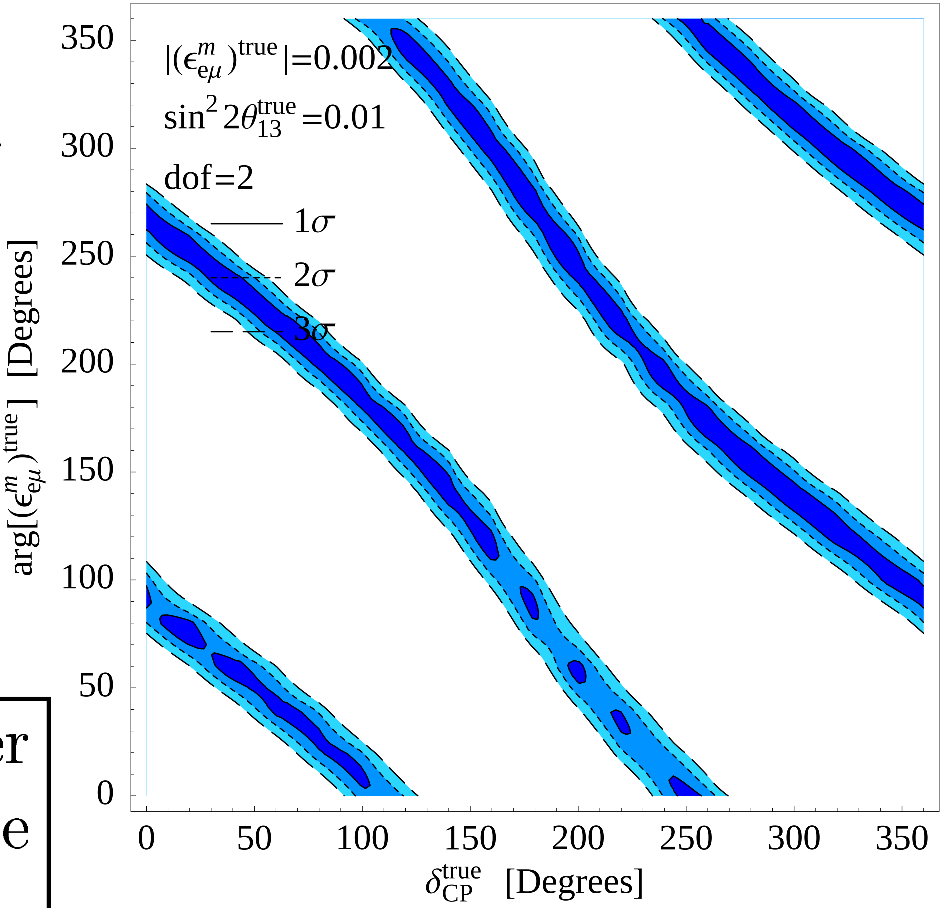
  In some regions χ^2 exceeds 3σ (Islands appear)

  ↓

  The deviation from the standard oscillation is significant at 3σ

  ↓

  We have a chance to discover NSI effect depending on the phases



Discovery reach for $\epsilon_{e\mu}^{m}$ in neutrino factory

- In the case $|(\epsilon_{e\mu}^{m})^{\mathrm{true}}| = 4 \times 10^{-3}$,

- $\boxed{|\epsilon_{e\mu}^{m}| \text{ becomes larger}}$

↓

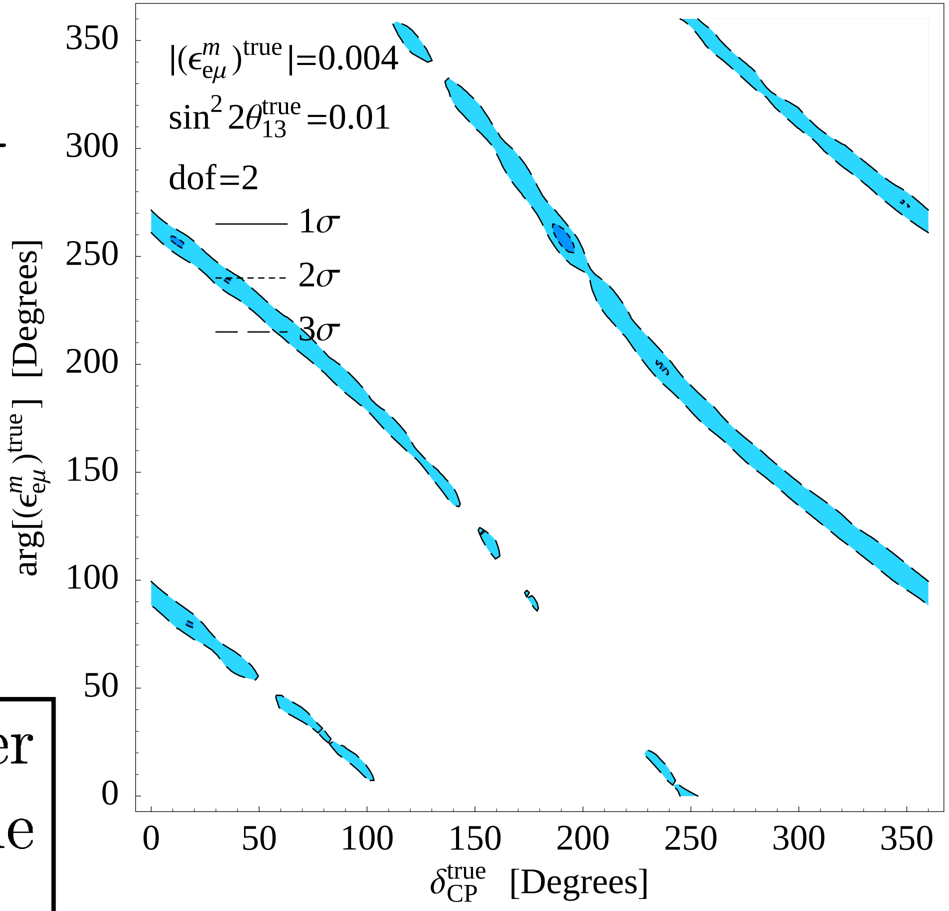
In some regions χ^2 exceeds 3σ (Islands appear)

↓

The deviation from the standard oscillation is significant at 3σ

↓

We have a chance to discover NSI effect depending on the phases



Discovery reach for $\epsilon^m_{e\mu}$ in neutrino factory

- In the case $|(\epsilon^m_{e\mu})^{\text{true}}| = 5 \times 10^{-3}$,

- $\boxed{|\epsilon^m_{e\mu}| \text{ is large enough}}$

  ↓

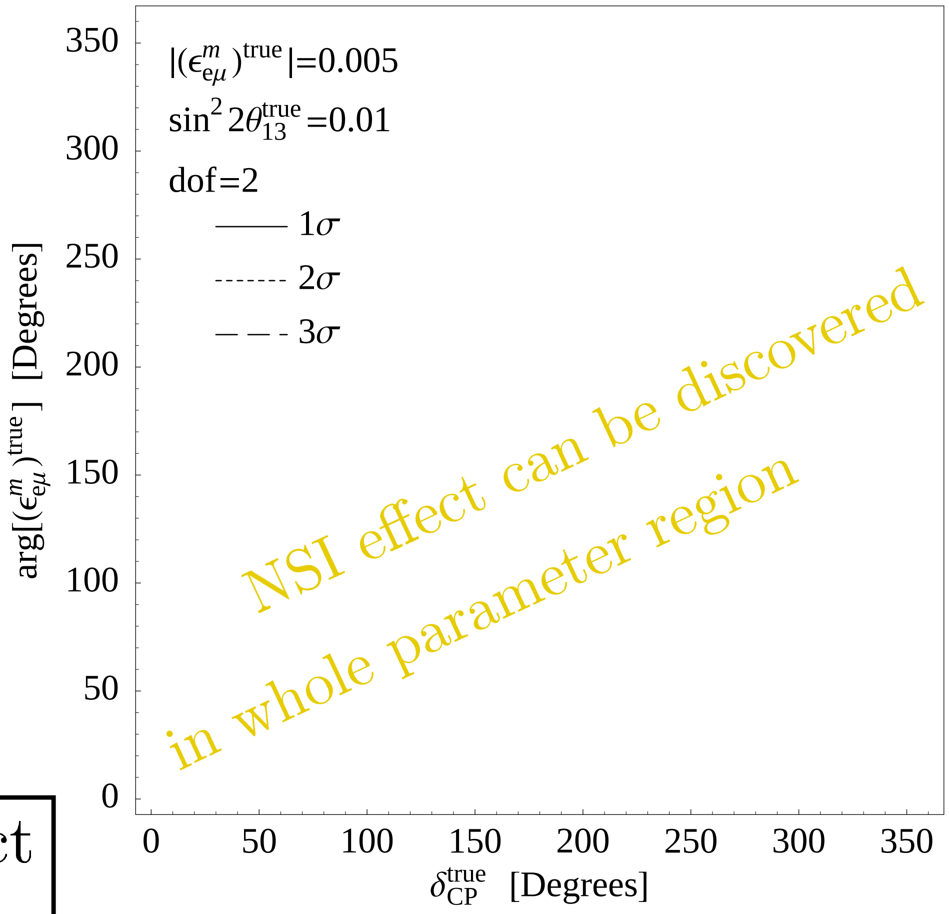
  χ^2 exceeds 3σ on the whole parameter plane (The sea disappears)

  ↓

  The deviation from the standard oscillation is significant at 3σ

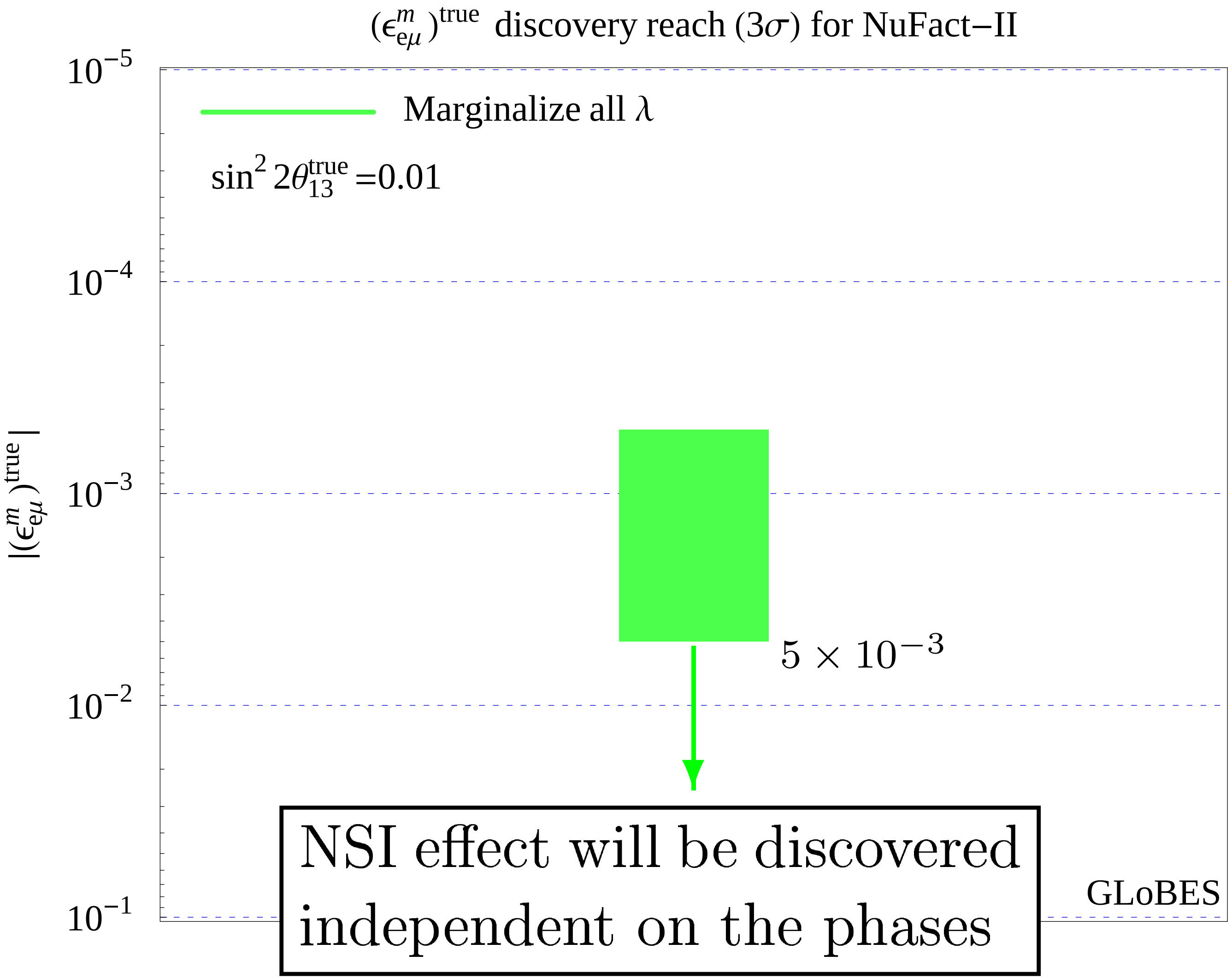
  ↓

  $\boxed{\text{We can observe the NSI effect with any values of phases.}}$



Discovery reach for NSIs in neutrino factory

- Summary plot for the discovery reach of $\epsilon_{e\mu}^{m}$



5×10^{-3}

NSI effect will be discovered independent on the phases

Discovery reach for NSIs in neutrino factory

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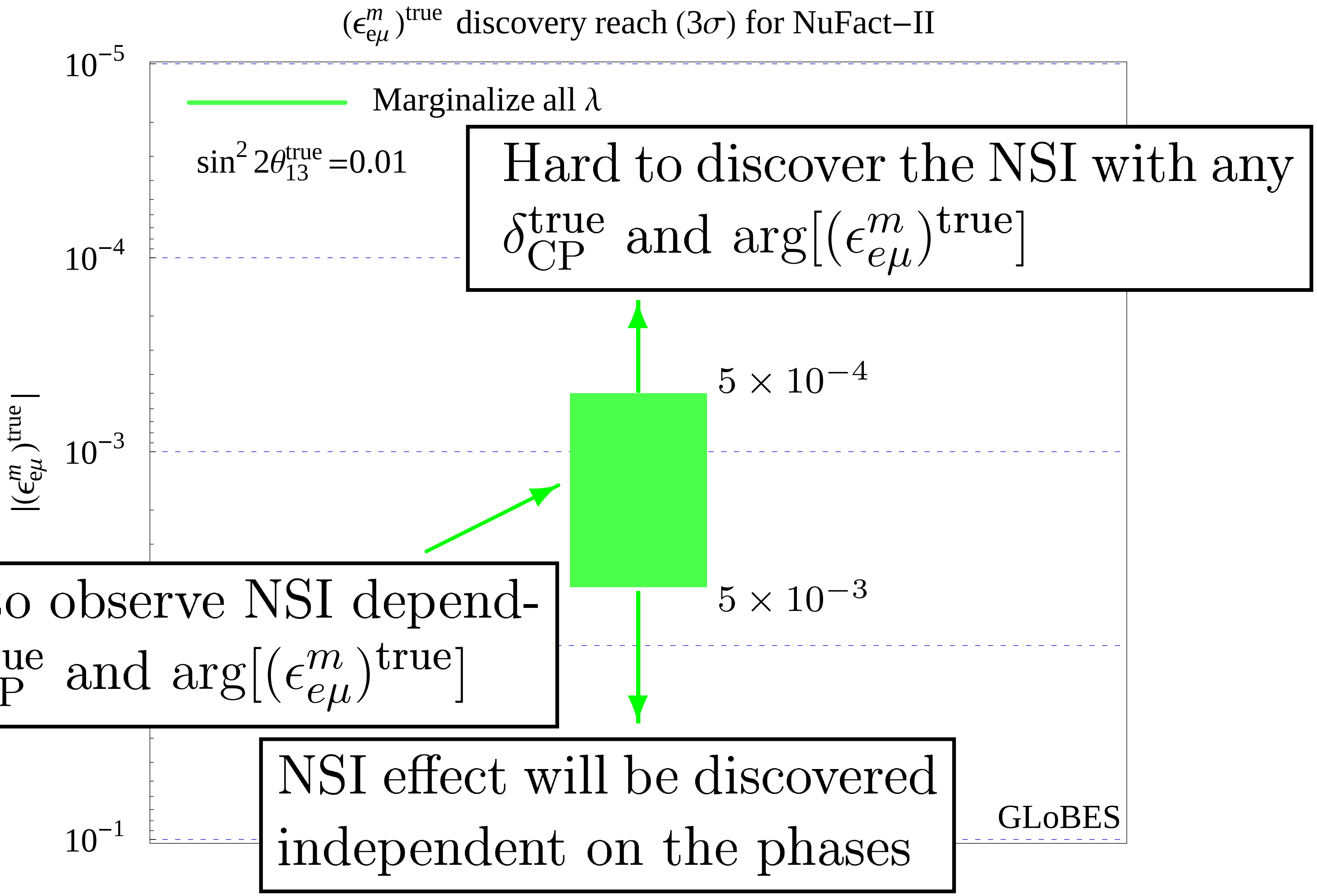


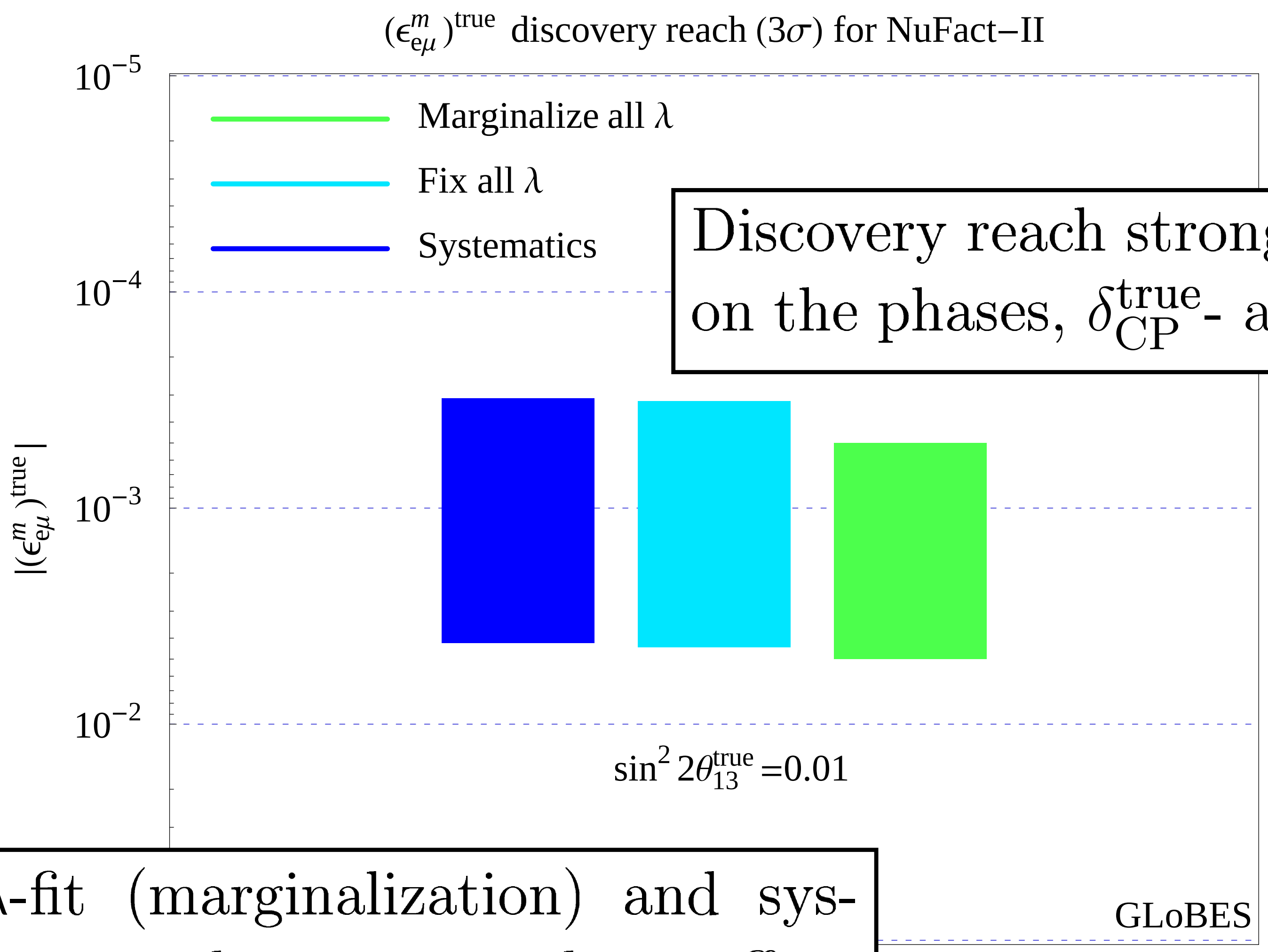
Hard to discover the NSI with any $\delta_{\rm CP}^{\rm true}$ and $\arg[(\epsilon_{e\mu}^{m})^{\rm true}]$

Possible to observe NSI depending on $\delta_{\rm CP}^{\rm true}$ and $\arg[(\epsilon_{e\mu}^{m})^{\rm true}]$

NSI effect will be discovered independent on the phases

Discovery reach for NSIs in neutrino factory

- Summary plot for the discovery reach of $\epsilon_{e\mu}^{m}$

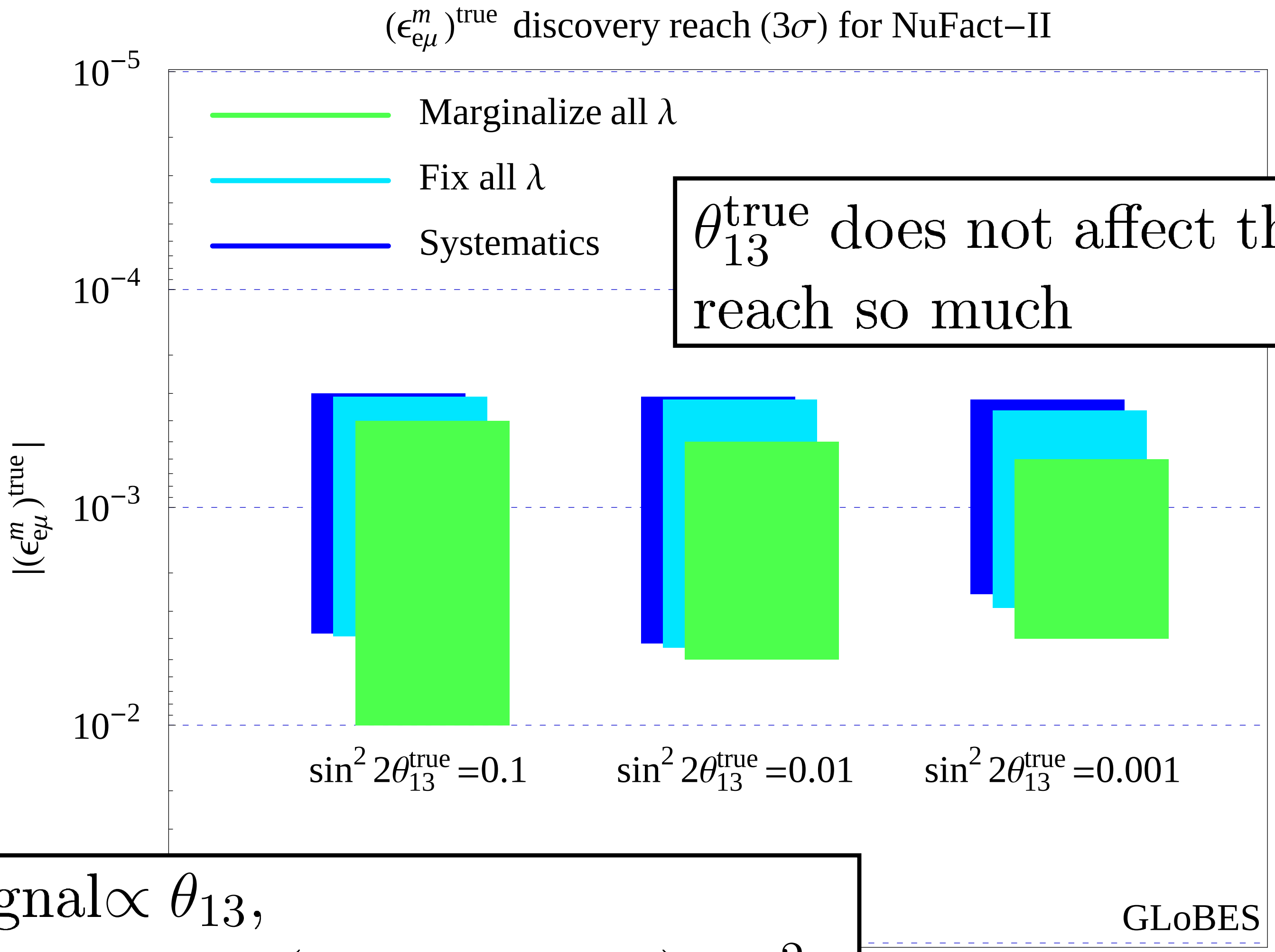


Discovery reach strongly depends on the phases, $\delta_{\text{CP}}^{\text{true}}$- $\arg[(\epsilon_{e\mu}^{m})^{\text{true}}]$

λ-fit (marginalization) and systematic do not give a large effect

Discovery reach for NSIs in neutrino factory

- Summary plot for the discovery reach of $\epsilon_{e\mu}^{m}$

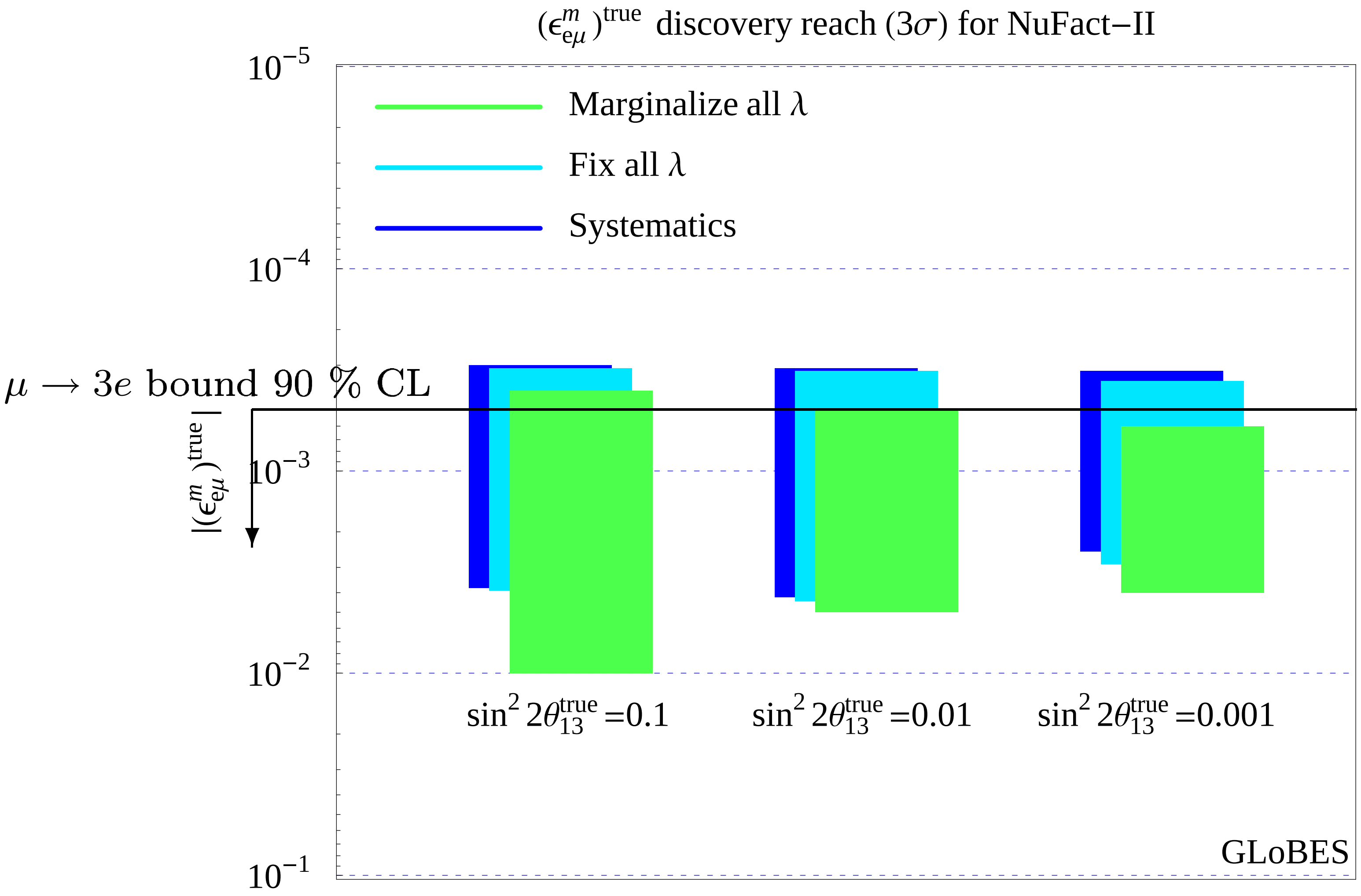


$\theta_{13}^{\text{true}}$ does not affect the discovery reach so much

signal $\propto \theta_{13}$,
background (standard osc.) $\propto \theta_{13}^2$

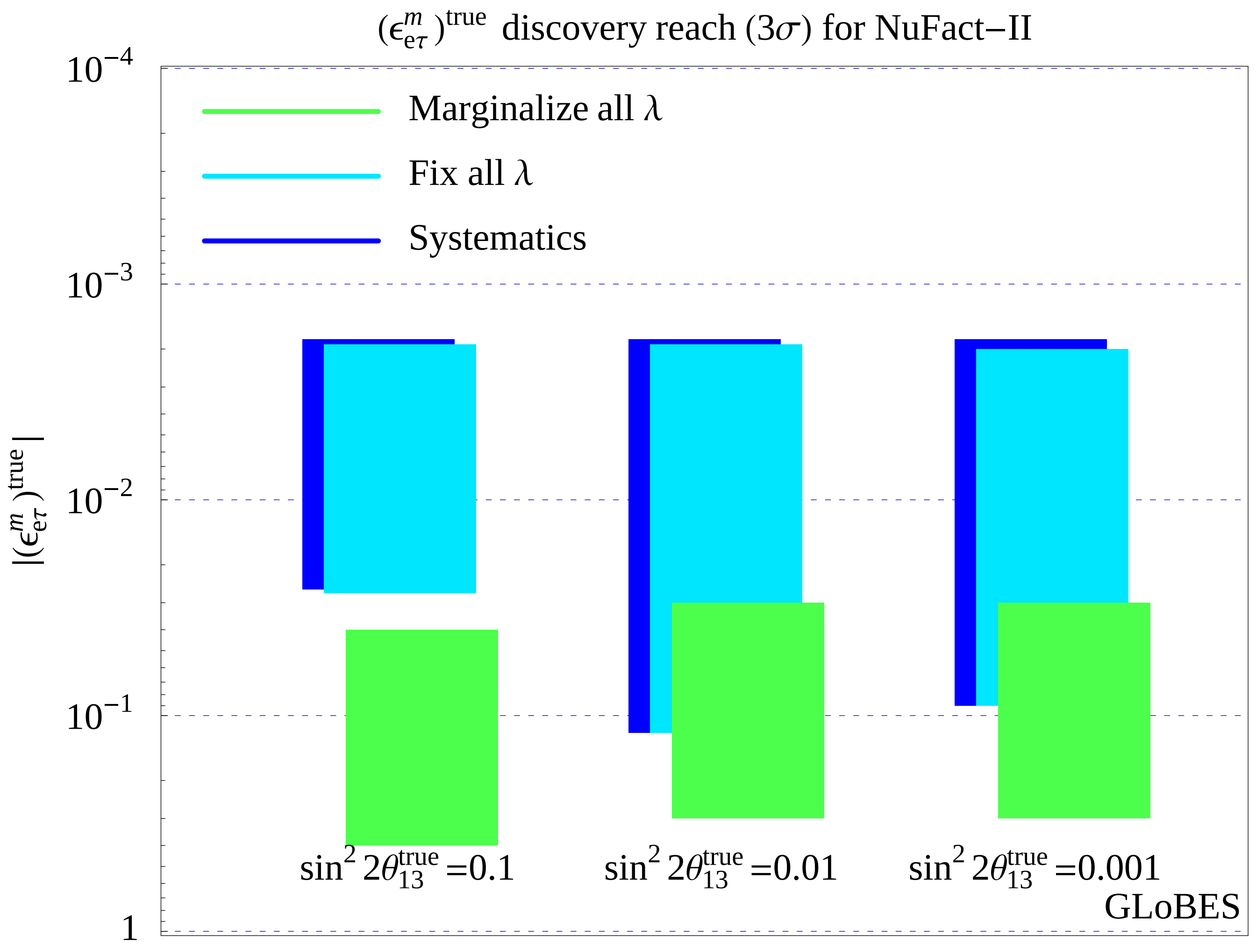
Discovery reach for NSIs in neutrino factory

- Summary plot for the discovery reach of $\epsilon^m_{e\mu}$



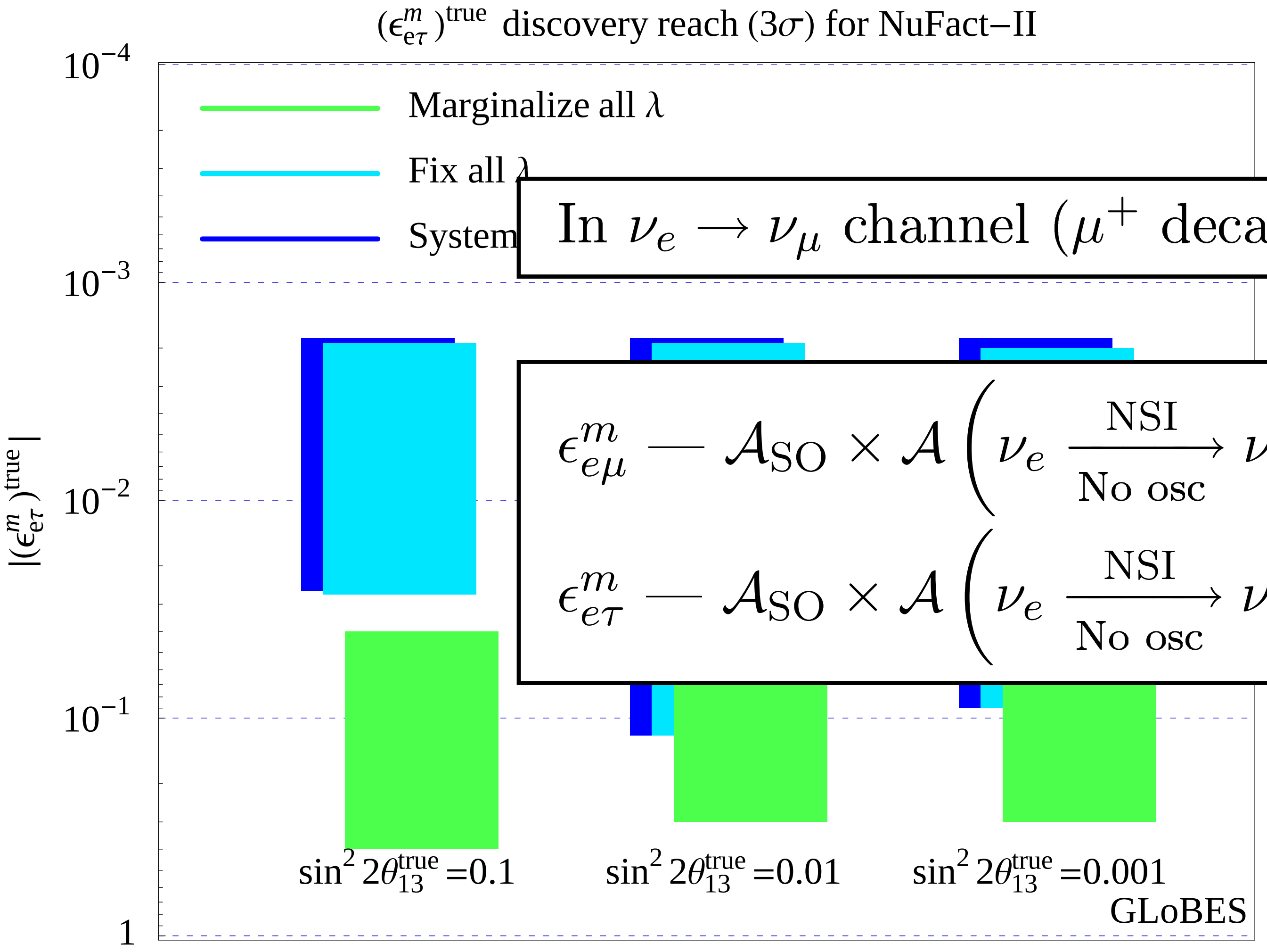
Discovery reach for NSIs in neutrino factory

- Similar plot for the discovery reach of $\epsilon^m_{e\tau}$



Discovery reach for NSIs in neutrino factory

- Similar plot for the discovery reach of $\epsilon^m_{e\tau}$



In $\nu_e \to \nu_\mu$ channel (μ^+ decay μ^- detection)

$$\epsilon^m_{e\mu} \;—\; \mathcal{A}_{\rm SO} \times \mathcal{A}\left(\nu_e \xrightarrow[\text{No osc}]{\text{NSI}} \nu_\mu\right)$$

$$\epsilon^m_{e\tau} \;—\; \mathcal{A}_{\rm SO} \times \mathcal{A}\left(\nu_e \xrightarrow[\text{No osc}]{\text{NSI}} \nu_\tau \xrightarrow[\text{Osc}]{} \nu_\mu\right)$$

Summary

Summary

- We have studied the discovery reach for the NSIs in a neutrino factory.
- The undetermined parameters $\delta_{\rm CP}^{\rm true}$ and $\arg[\epsilon^{\rm true}]$ are scanned.

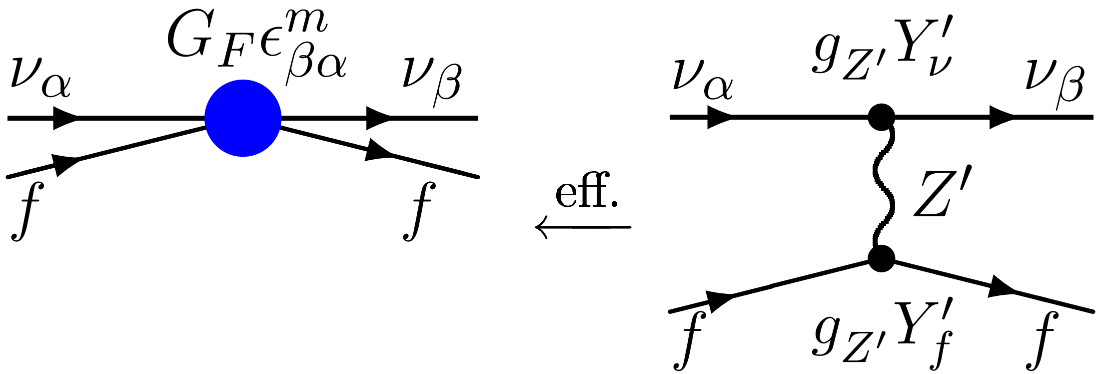
For $\epsilon_{e\mu}^{m}$, when $\sin^2 2\theta_{13}^{\rm true} = 0.01$

  - With $|\epsilon_{e\mu}^{m}| \geq 5 \times 10^{-4}$,
    we have a chance to discover the effect at the 3σ level, depending on the phases.
  - If $|\epsilon_{e\mu}^{m}| \geq 5 \times 10^{-3}$,
    it can be found in the ν factory regardless of the phases.

- Current bound from $\mu \to 3e$ is 5×10^{-4} at the 90% CL.
  — Comparable, depending on the phases

Summary

- The discovery reach for $\epsilon^m_{e\tau}$ and $\epsilon^s_{e\mu}$ has also studied.
  - $|\epsilon^s_{e\mu}| \sim \mathcal{O}(10^{-3,-4})$, $|\epsilon^m_{e\tau}| \sim \mathcal{O}(10^{-1,-2})$.
- The effective four-Fermi NSIs with $\epsilon \sim \mathcal{O}(10^{-2})$ may mean the TeV scale physics, i.e.,



  - If $g_{Z'}$ is the same as g_Z, $\epsilon^m_{\beta\alpha} = m^2_Z/m^2_{Z'}$.

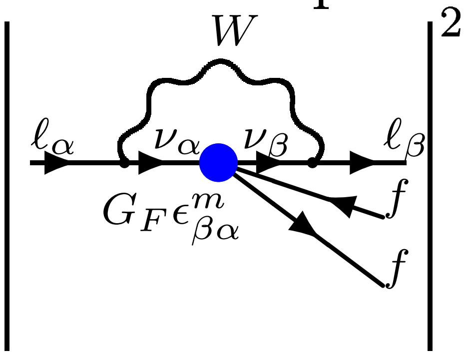
- NSIs are not good signals for MSSM
  — They are strongly supressed
  — NSIs may be the signals for something else than MSSM

Discussion: NSIs in models

References : T. O and J. Sato, Phys. Rev. **D71** (2005) 096004.

NSIs in models

- We dealt with NSIs as effective 4-Fermi interactions so far.
- Current experimental bounds coming from the LFV process



$\epsilon^m_{e\mu}$ $(f = e)$	5×10^{-4} (90% CL)
$\epsilon^m_{e\tau}$ $(f = e)$	2.9 (90% CL)

Comparable with discovery reach in ν fact.

NSIs in models

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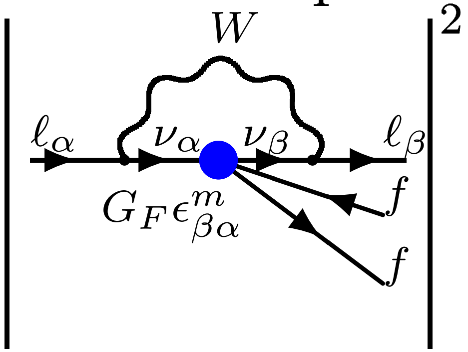
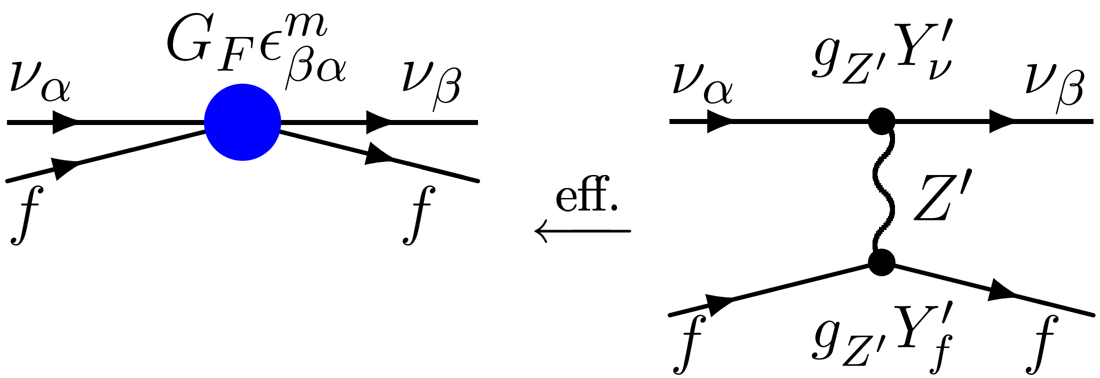


$\epsilon^m_{e\mu}$	$(f = e)$	5×10^{-4} (90% CL)
$\epsilon^m_{e\tau}$	$(f = e)$	2.9 (90% CL)

Comparable with discovery reach in ν fact.

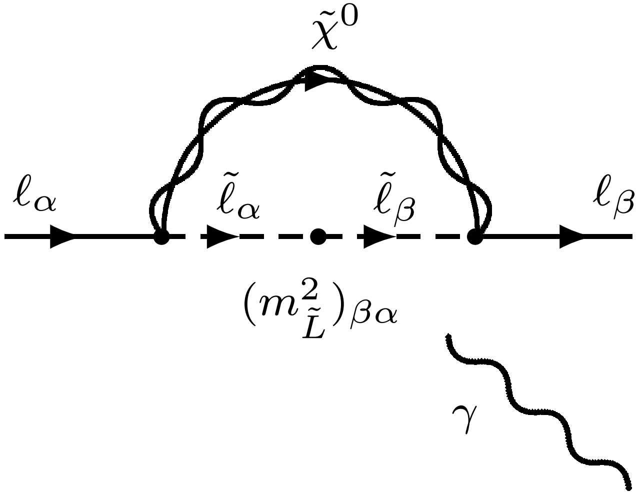
- These eff. int.s can be interpreted as *extra weak interactions*

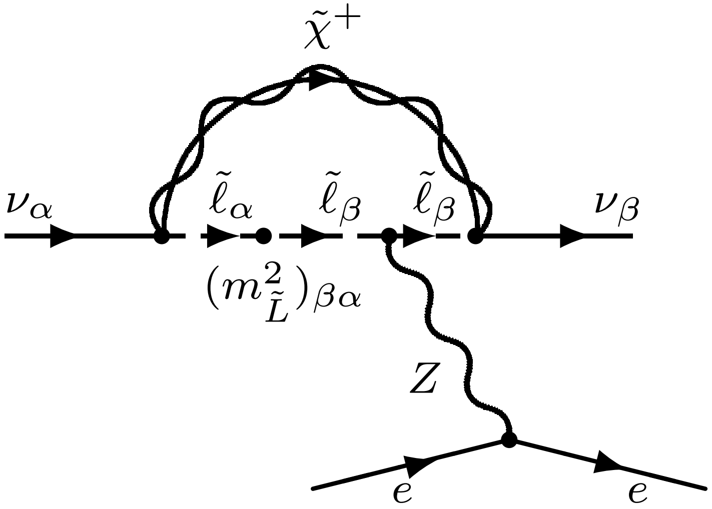


- If $g_{Z'}$ are the same as those of weak interaction, $\epsilon^m_{\beta\alpha} = m^2_Z/m^2_{Z'}$
- $\epsilon^m_{\alpha\beta} \sim \mathcal{O}(10^{-2})$ means *access to the TeV scale physics*

NSIs in models — MSSM with ν_R

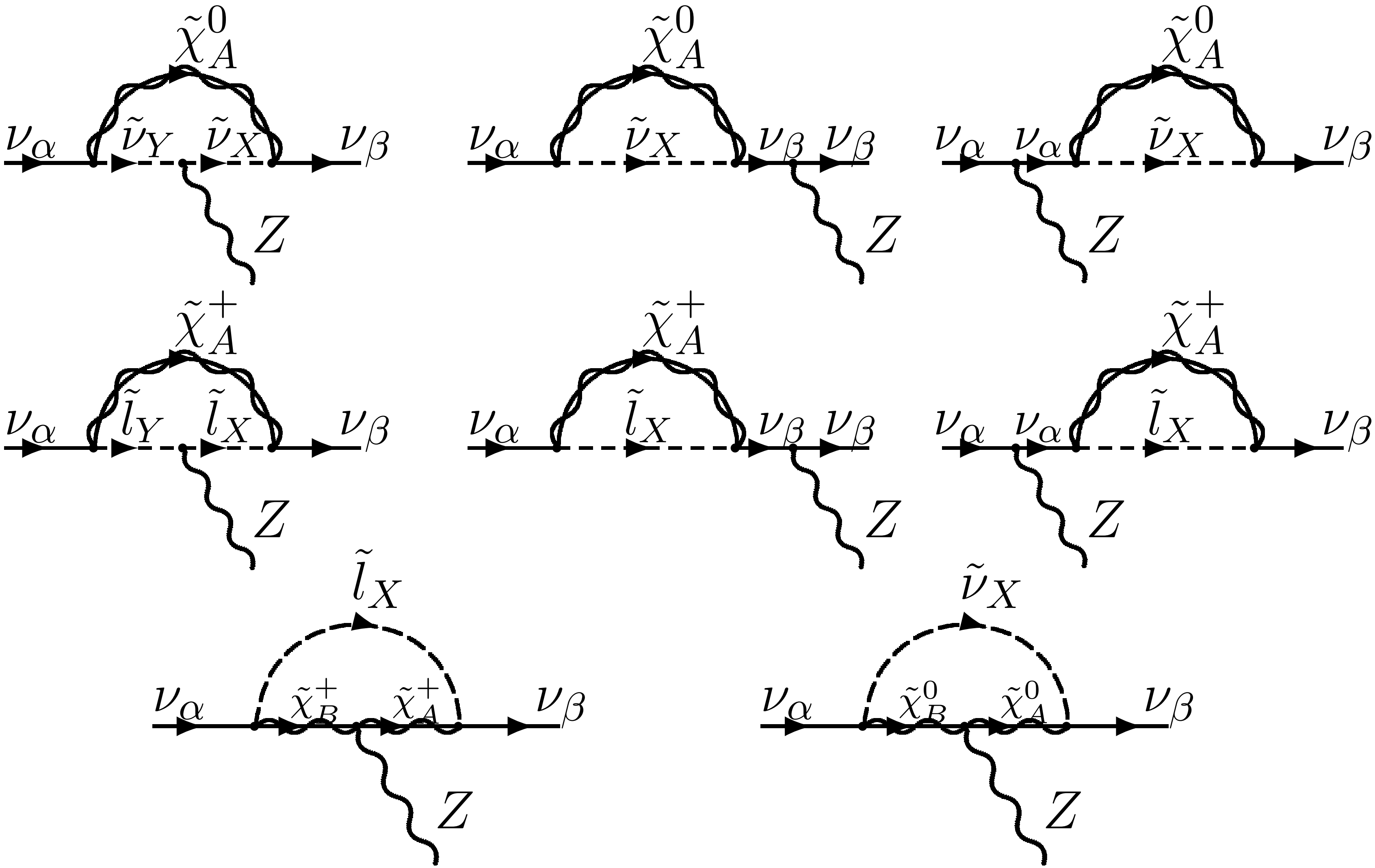
- In the MSSM, NSIs and $\ell_\beta \to \ell_\alpha \gamma$ are provided by similar one-loop diagrams with slepton mixings — they are correlated.





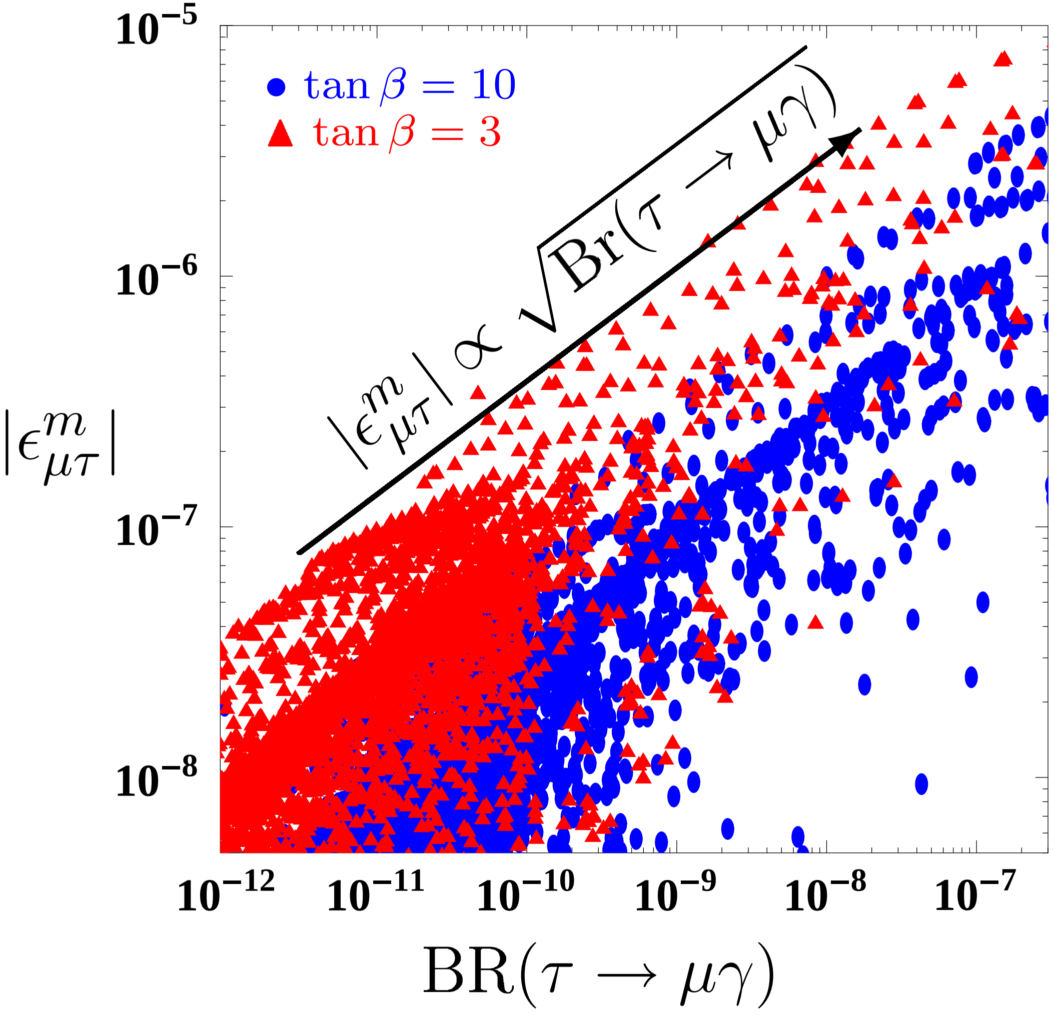
- Large slepton mixings are expected to be induced by the RGE effect associated with the neutrino Yukawa couplings.
- $\epsilon^{s,m}_{e\mu}$ is strongly suppressed, at least $\sqrt{\mathrm{Br}(\mu \to e\gamma)} = \mathcal{O}(10^{-5})$
- How about $\epsilon^m_{e\tau}$, $\epsilon^m_{\mu\tau}$?

NSIs in models — MSSM with ν_R



and box diagrams ...

NSIs in models — MSSM with ν_R



- Correlation between the NSI coupling $\epsilon^m_{\mu\tau}$ and LFV process $\tau \longrightarrow \mu\gamma$.
  - With some different Y_νs, we scan the m_0-$M_{1/2}$ space with $a_0 = 0$, $\tan\beta = 3, 10$, and $\mu > 0$.
- The parameter $\epsilon^m_{\mu\tau}$ is constrained at $\mathcal{O}(10^{-6})$ by the current bound of $\tau \longrightarrow \mu\gamma$.
- It is smaller than the naive estimation because of cancellation among diagrams.