

Results on $0\nu\beta\beta$ of ^{76}Ge from GERDA Phase I

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collaboration**

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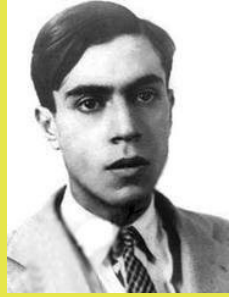


Warsaw, 23 June 2014

Outline

- **Neutrinos and Double Beta Decay**
- **The GERDA experiment**
- **GERDA Phase I data taking**
- **GERDA Phase I analysis**
- **Outlook on GERDA Phase II**

Unveil the nature of the neutrino



Majorana
 $\nu = \bar{\nu}$

or



Dirac
 $\nu \neq \bar{\nu}$

If $0\nu\beta\beta$ is observed:

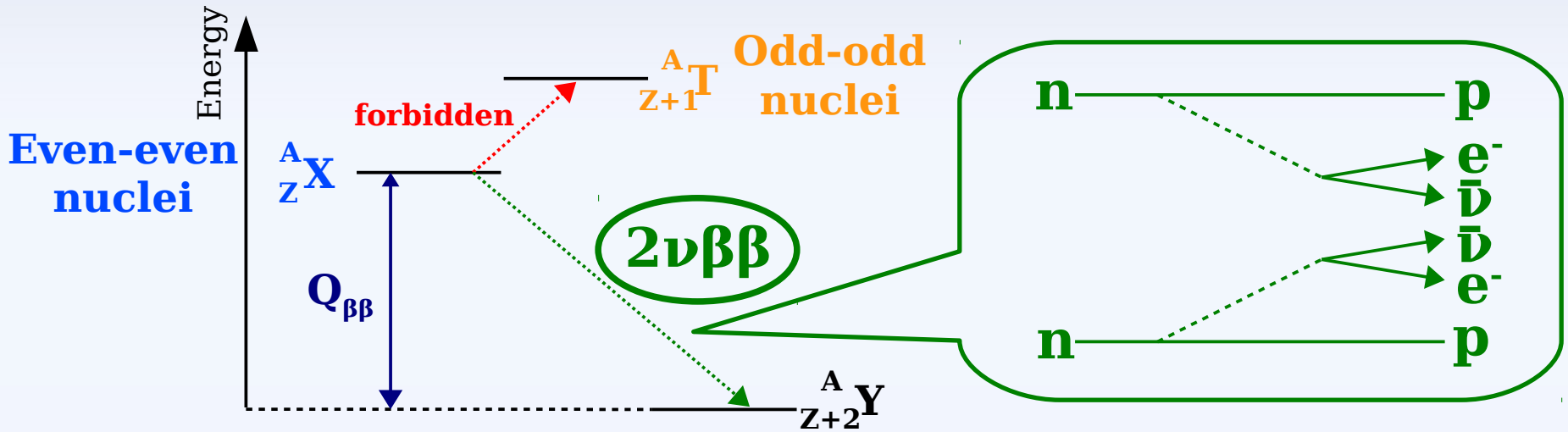
Lepton number violation $\Delta L=2$

Neutrino has a Majorana mass term

Sheds light on absolute neutrino mass scale

Sheds light on neutrino mass hierarchy

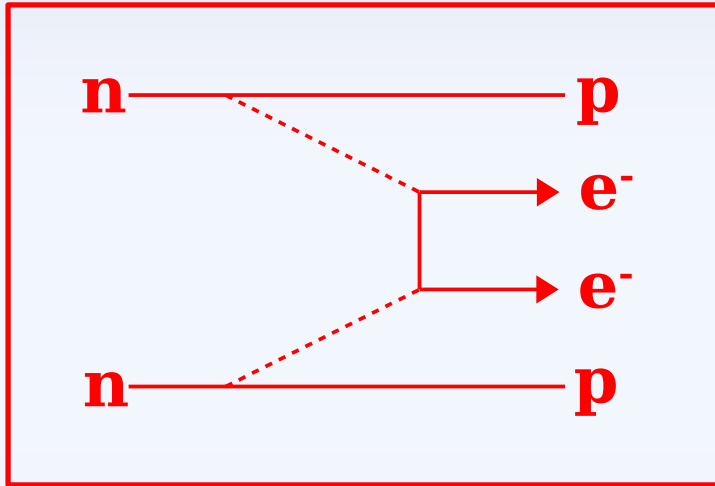
$2\nu\beta\beta$



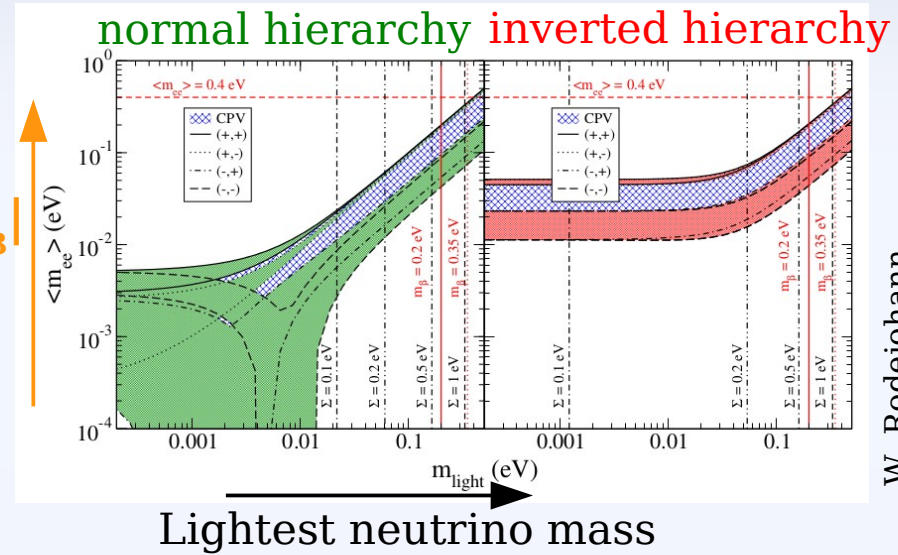
- allowed by SM
- $\Delta L=0$
- observed in many isotopes
- $T_{1/2}^{2\nu} \sim 10^{19} - 10^{21} \text{ yr}$
- $(T_{1/2}^{2\nu})^{-1} = G^{2\nu}(Q_{\beta\beta}, Z) \cdot |M^{2\nu}|^2$

\uparrow *Phase space* \uparrow *nuclear matrix element*

$0\nu\beta\beta$



$|m_{\beta\beta}|$



W. Rodejohann, J. Phys. G39 (2012), 124008

- forbidden process in SM, needs Majorana neutrino
- $\Delta L=2$
- $(T^{0\nu}_{1/2})^{-1} = G^{0\nu}(Q_{\beta\beta}, Z) \cdot |M^{0\nu}|^2 \cdot \langle m_{\beta\beta} \rangle^2 *$

Phase space ($\sim Q_{\beta\beta}^5$)

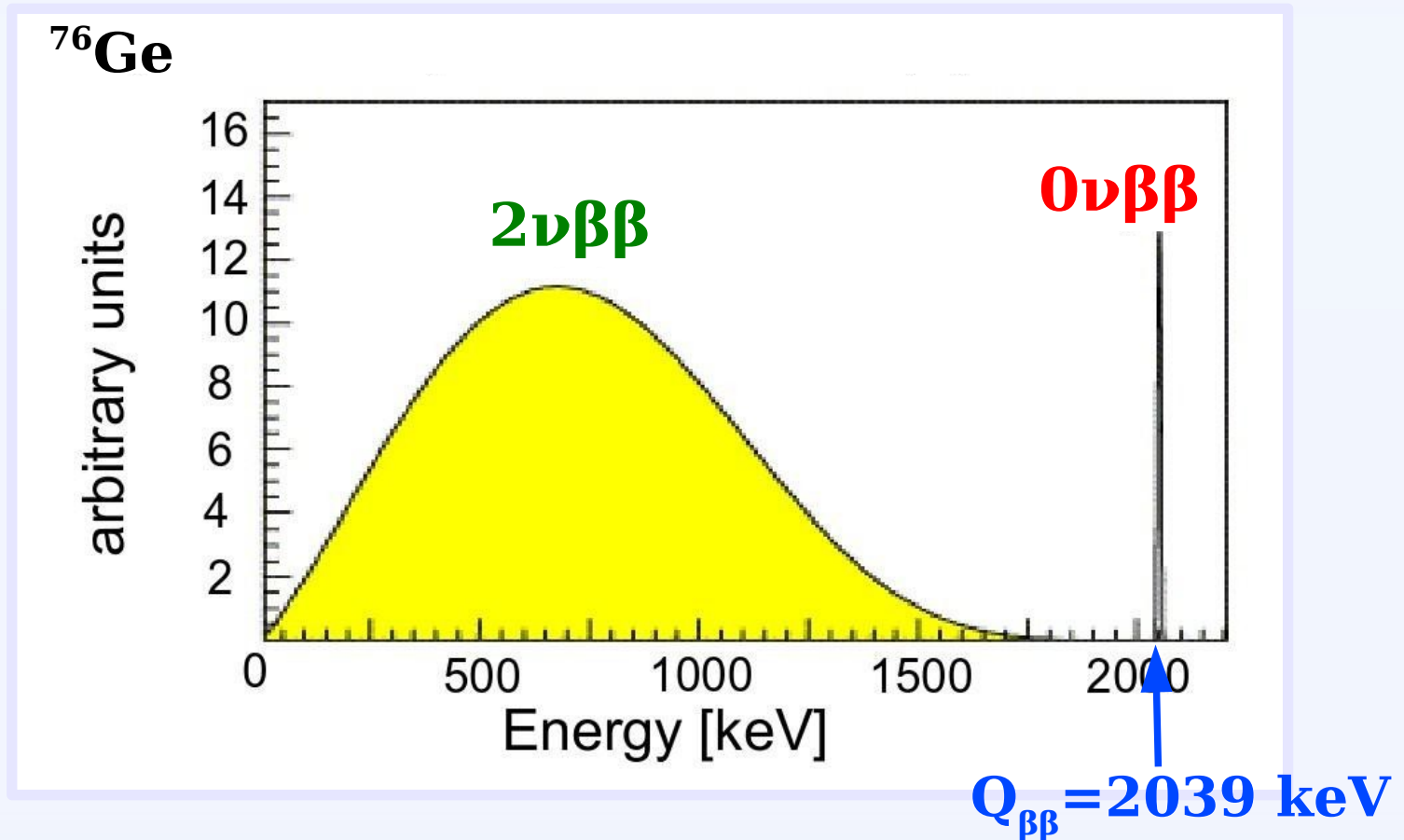
nuclear matrix element

$\langle m_{\beta\beta} \rangle^2 = |\sum_i U_{ei}^2 m_i|^2$
Majorana neutrino mass

* assuming exchange of light Majorana neutrino

Experimental signatures

➔ Measure summed **electron** energy spectrum **E**:



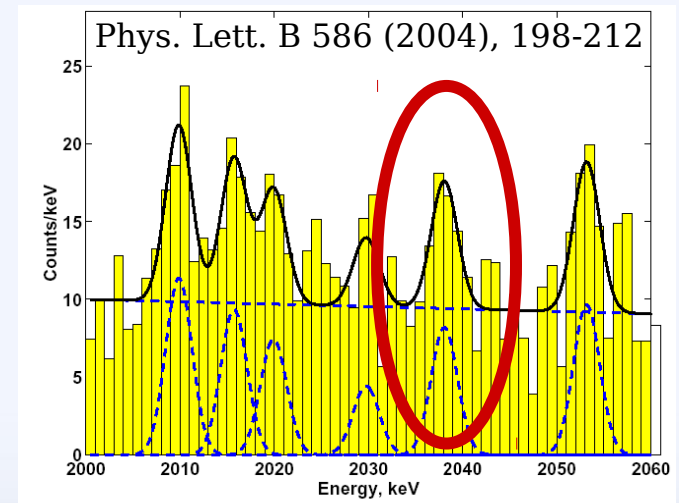
Most stringent limits on $0\nu\beta\beta$

Isotope	Experiment	$T_{1/2}^{0\nu}$ (yr) (90% C.L.)
^{76}Ge	HdM collaboration	$1.9 \cdot 10^{25}$ [1]
	IGEX collaboration	$1.6 \cdot 10^{25}$ [2]
^{136}Xe	EXO collaboration	$1.1 \cdot 10^{25}$ [3]
	KamLAND-Zen collaboration	$1.9 \cdot 10^{25}$ [4]

Claim of signal for $0\nu\beta\beta$:

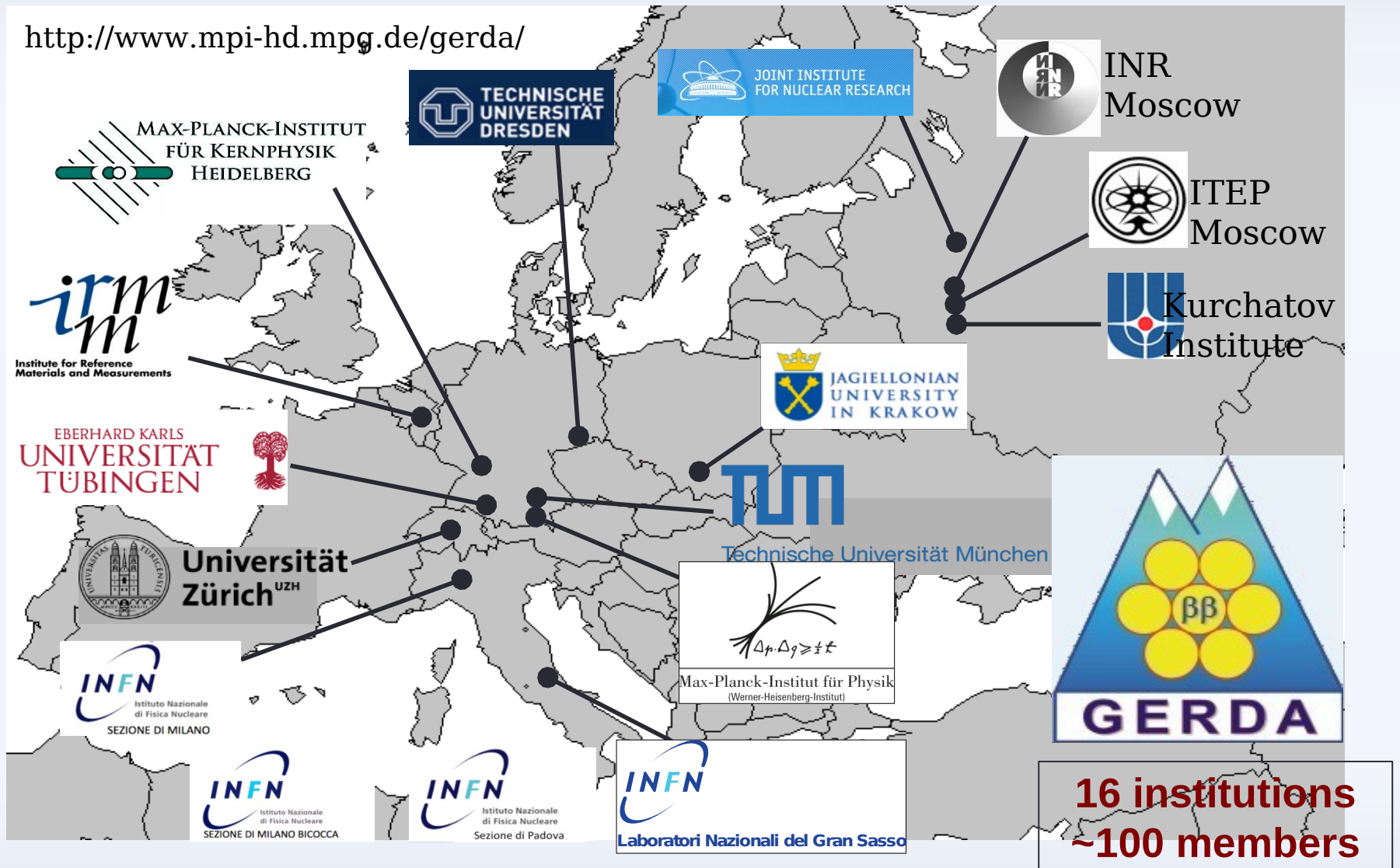
$$T_{1/2}^{0\nu} (^{76}\text{Ge}) = 1.19^{+0.37}_{-0.23} \cdot 10^{25} \text{ yr [5]}$$

- [1] Eur. Phys. J. A12 (2001), 147-154
- [2] Phys. Rev. D 65 (2002), 092007
- [3] Nature 510 (2014), 229-234
- [4] Phys. Rev. Lett. 110 (2013), 062502
- [5] Phys. Lett. B 586 (2004), 198-212



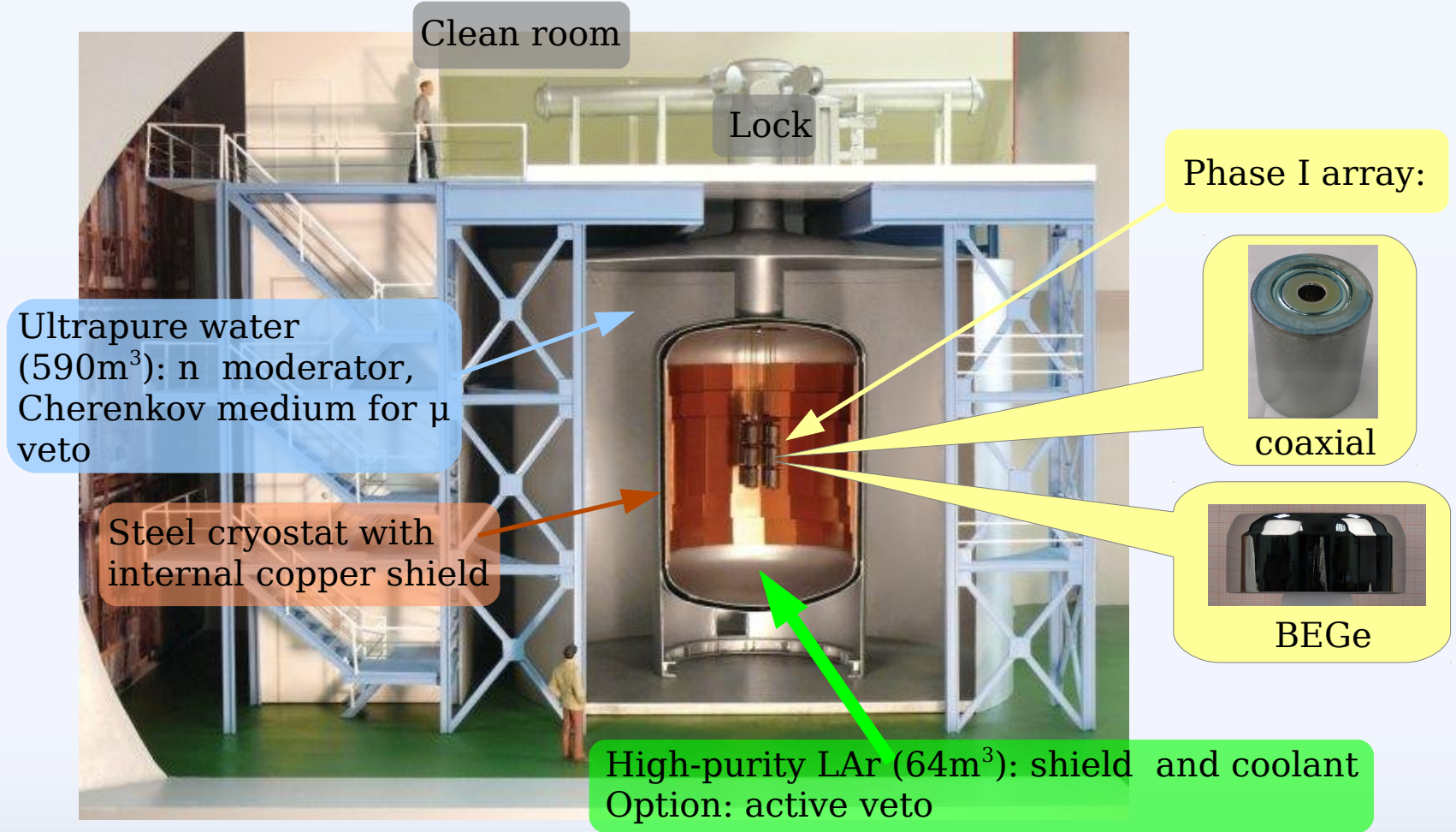
The GERDA experiment

<http://www.mpi-hd.mpg.de/gerda/>



Experimental setup

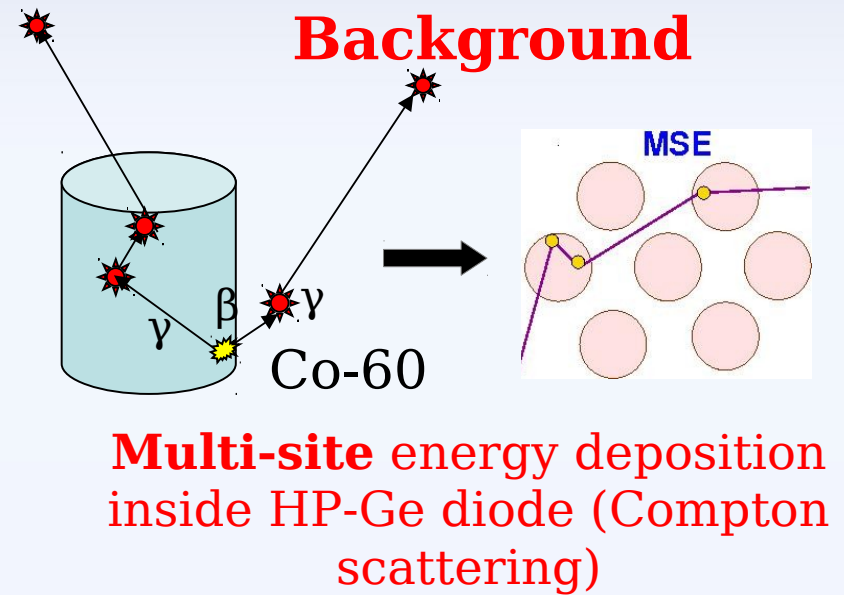
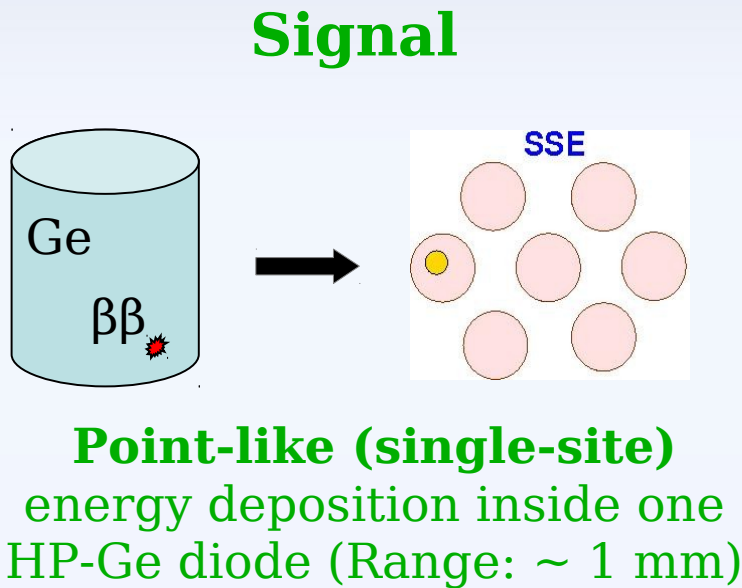
- situated in LNGS underground laboratories (3500 m w.e. shielding)
- graded shielding against ambient radiation
- rigorous material selection, avoid exposure above ground for detectors



Experimental setup



Additional background reduction



Signal analysis:

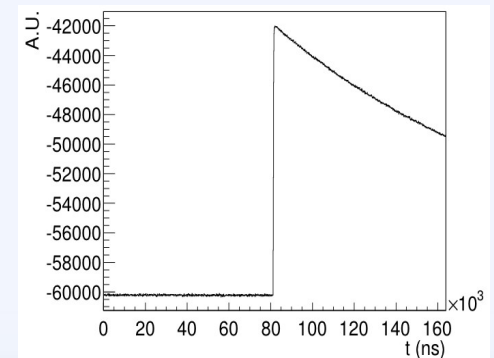
- anti-coincidence between detectors
- pulse shape analysis (PSA)
- time-coincidence (Bi-Po)

Ge diode with HV in blocking direction → leakage current very small

Energy deposition → e⁻h⁺-pair drift in E-field to electrodes

Readout with charge-sensitive preamplifier with R-feedback

Example of charge pulse



GERDA Phase I data



8 semi-coaxial p-type detectors
(reprocessed HdM and IGEX detectors)
(2 detectors not considered for analysis)
Enrichment fraction of ^{76}Ge : $\sim 86\%$
Data taking: November 2011 - May 2013



Total mass: 14.6 kg



5 p-type BEGe detectors
(newly processed Phase II detectors)
(1 detector not considered for analysis)
Enrichment fraction of ^{76}Ge : $\sim 88\%$
Data taking: July 2012 - May 2013



Total mass: 3.0 kg

GERDA Phase I data

Calibration and energy resolution

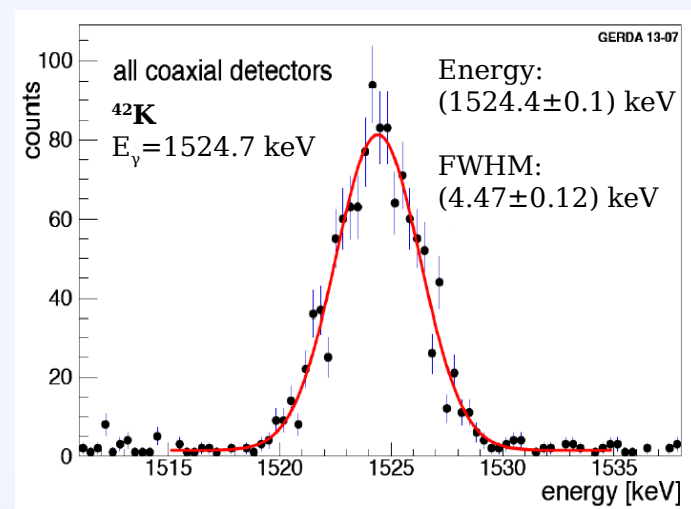
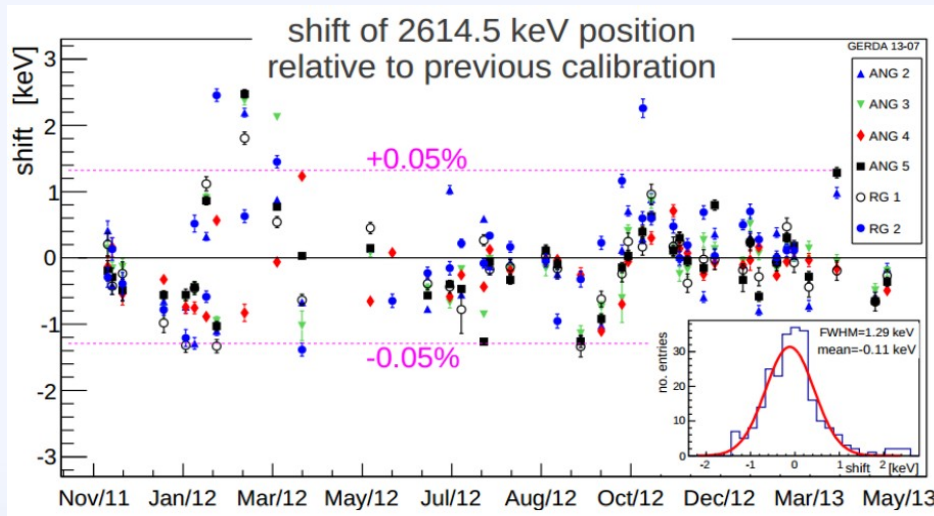
- (bi-) weekly calibration with ^{228}Th source
- offline energy reconstruction (semi-Gaussian filter)
- stability monitored with test pulses

Mean FWHM @ $Q_{\beta\beta}$:

Semi-coaxial detectors: (4.8 ± 0.2) keV

BEGe detectors: (3.2 ± 0.2) keV

Stable over the entire data taking period!

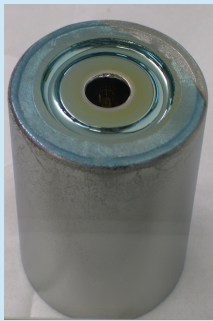
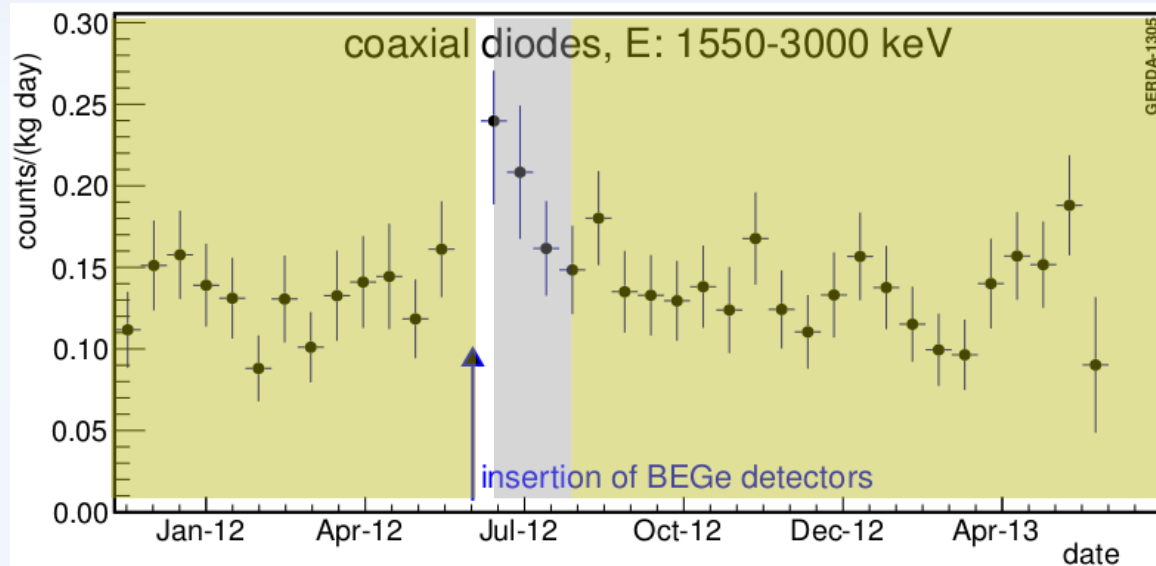


Shifts small compared to FWHM ($\sim 0.2\% Q_{\beta\beta}$)

Peak position within 0.3 keV of correct position

GERDA Phase I data

Group data according to energy resolution and background level:

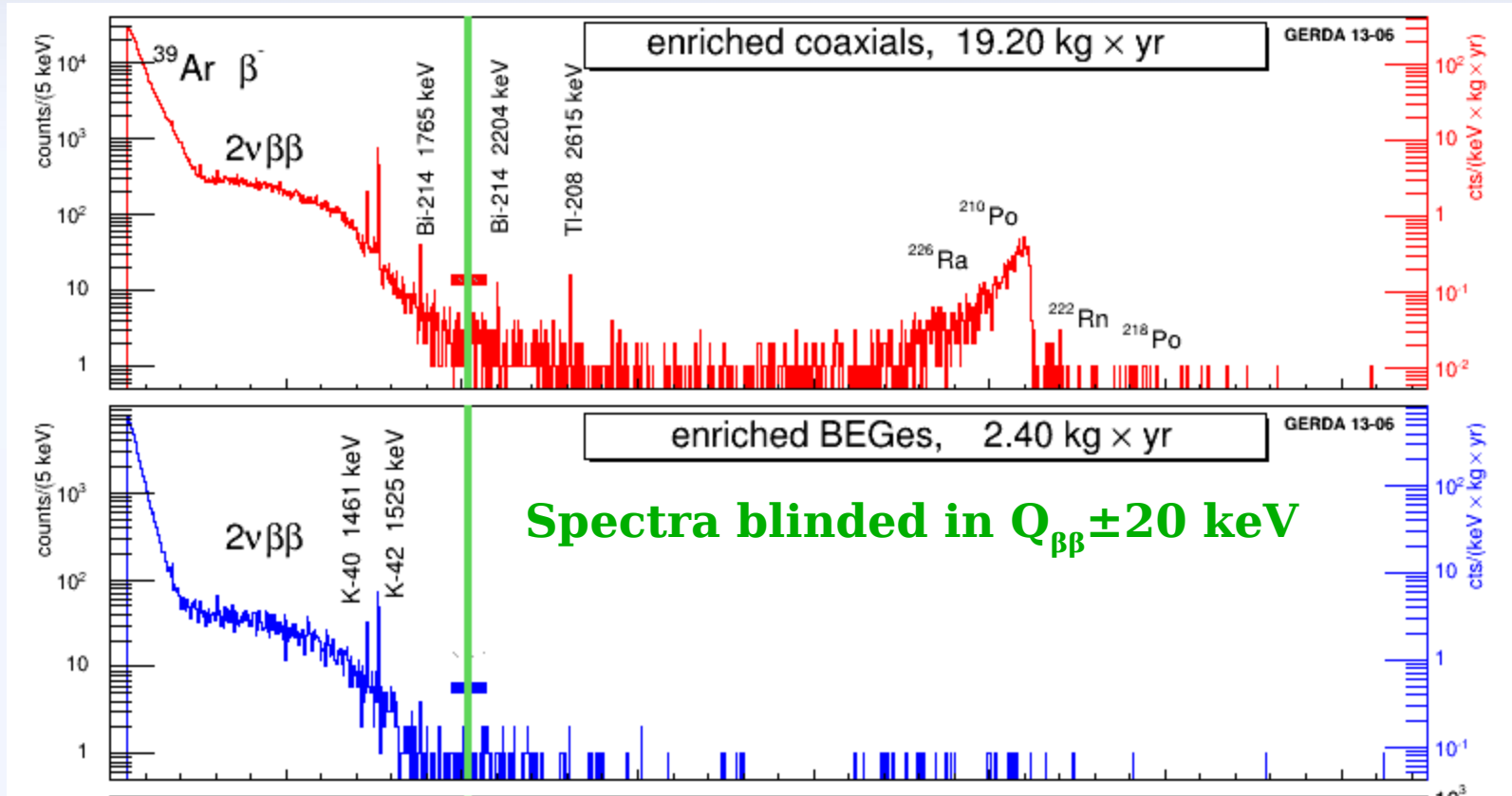


Golden data set: 17.9 kg·yr
Silver data set: 1.3 kg·yr



BEGe data set: 2.4 kg·yr

GERDA Phase I data

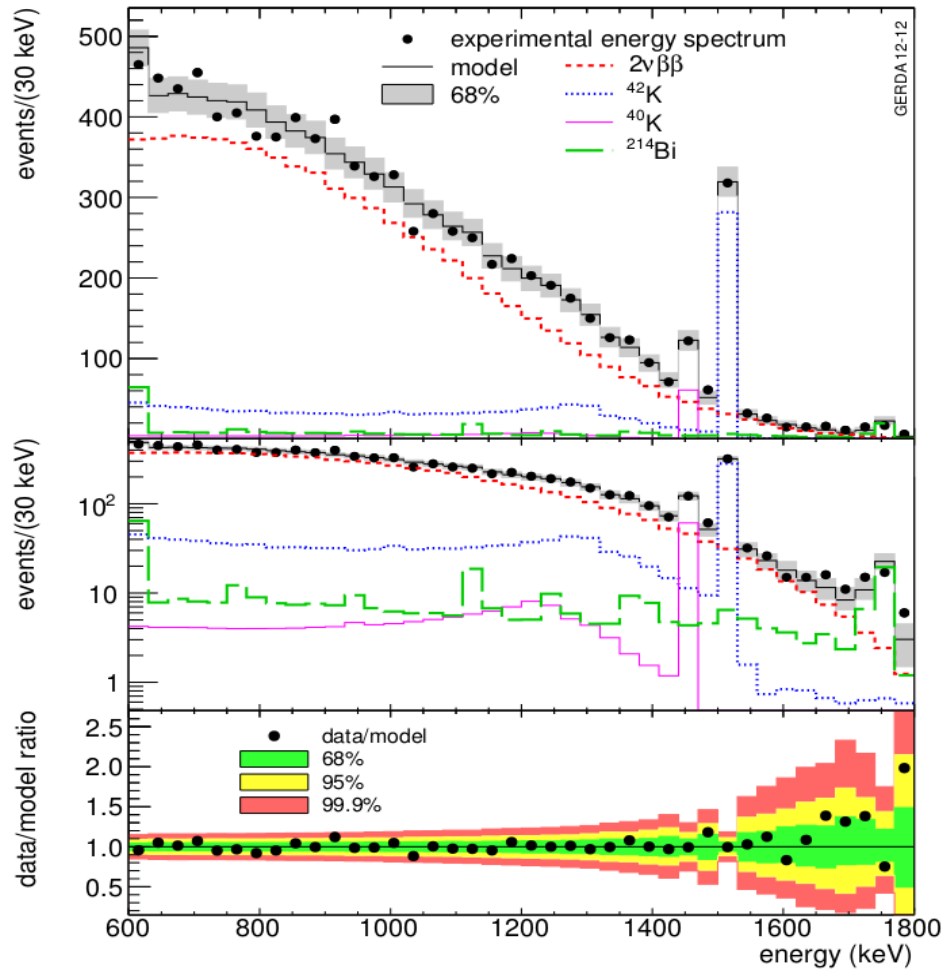


Dominating background sources:

- β -spectrum of ^{39}Ar ($Q=565$ keV)
- α -spectrum of ^{238}U chain (in coaxial detectors)
- γ -lines from ^{42}K , ^{40}K , $^{214}\text{Pb}/^{214}\text{Bi}$, ^{208}Tl , ^{228}Ac

Measurement of $T_{1/2}^{2\nu}$ of ^{76}Ge

Binned maximum likelihood approach

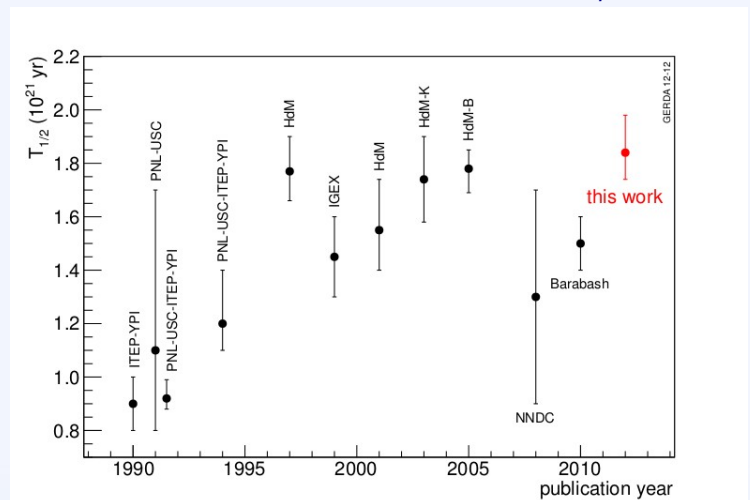


Data set: 5.04 kg·yr subset of golden data set

Fit window: [600;1800] keV

Model: Simulated spectra of $2\nu\beta\beta$, ^{42}K , ^{40}K , ^{214}Bi

Fit parameters: active det. masses, enrichment fractions, bkg contributions, common $T_{1/2}^{2\nu}$

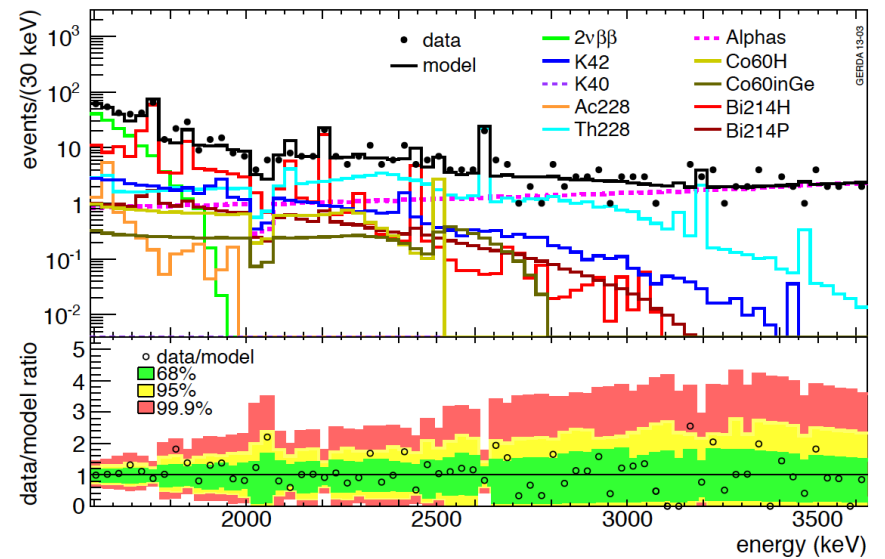
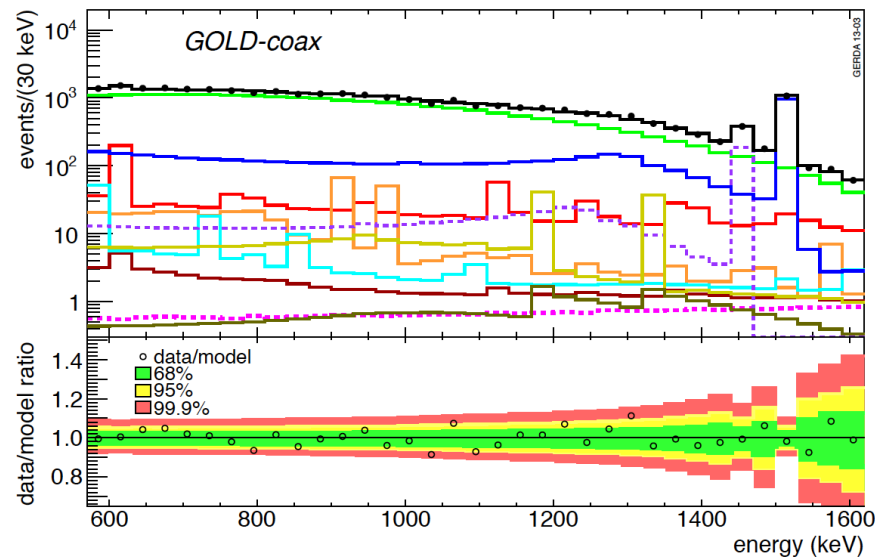
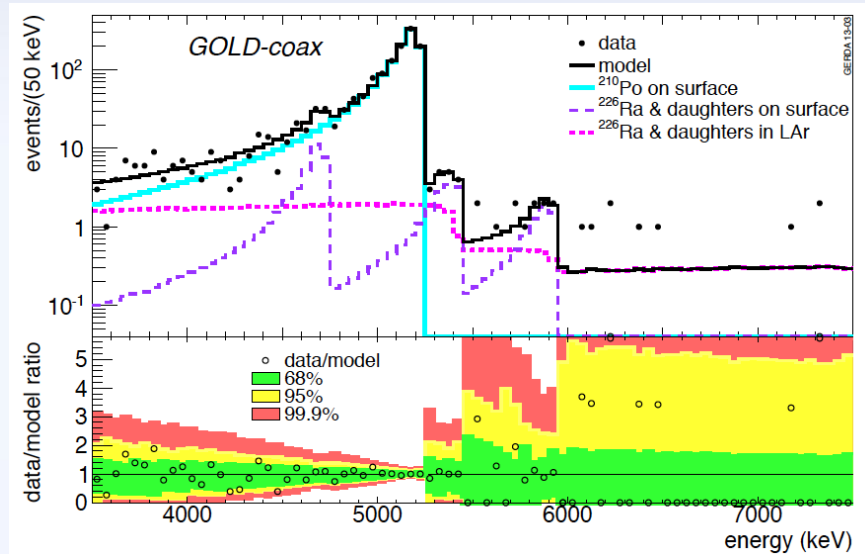


Final result: $(1.84^{+0.09}_{-0.08 \text{ fit}})^{+0.11}_{-0.06 \text{ syst}} \cdot 10^{21} \text{ yr} = (1.84^{+0.14}_{-0.10}) \cdot 10^{21} \text{ yr}$

Background model

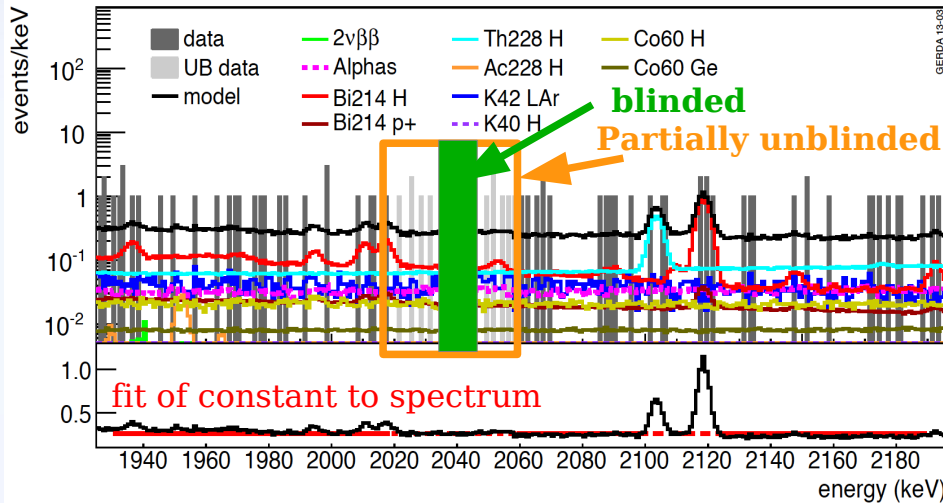
- simulate spectra of known and observed background sources
- spectral fit with combination of simulated spectra in [570;7500] keV (excluding blinded window)

EPJC 74 (2014) 2764



Background model

“Minimal” model (all known contributions)



Dominating contributions at $Q_{\beta\beta}$:

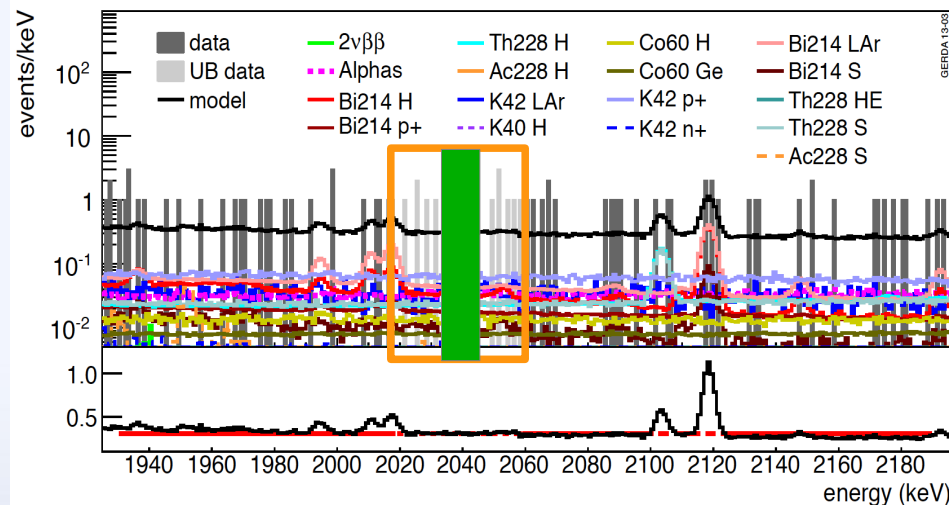
- β/γ events from ^{42}K , ^{60}Co , ^{214}Bi , ^{208}Tl
- α events from ^{238}U chain

No γ -line expected in the blinded window!

Flat background between 1930 and 2190 keV

excluding known γ -lines:
 (2104 \pm 5) keV (^{214}Bi)
 (2119 \pm 5) keV (^{208}Tl SEP)
(valid for all data sets)

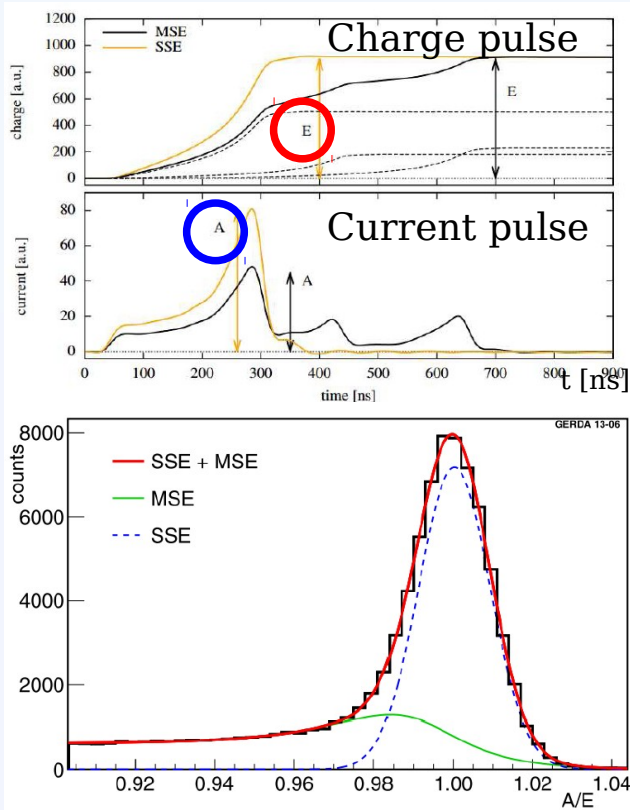
“Maximum” model (addit. contributions)



Partial unblinding after calibration & background model fixed:
 → no line observed
 → expected: 8.6-10.3 events
 observed: 13 events

Pulse shape analysis (PSA)

BEGe detectors



BEGe detectors:

- cut based on **A/E**
- tuned using double escape peak of ^{208}Tl , compton continuum and $2\nu\beta\beta$ events
- background acceptance at $Q_{\beta\beta} \leq 20\%$

$$\epsilon_{\text{PSA}} = 0.92 \pm 0.02 \text{ for SSE}$$

Semi-coaxial detectors:

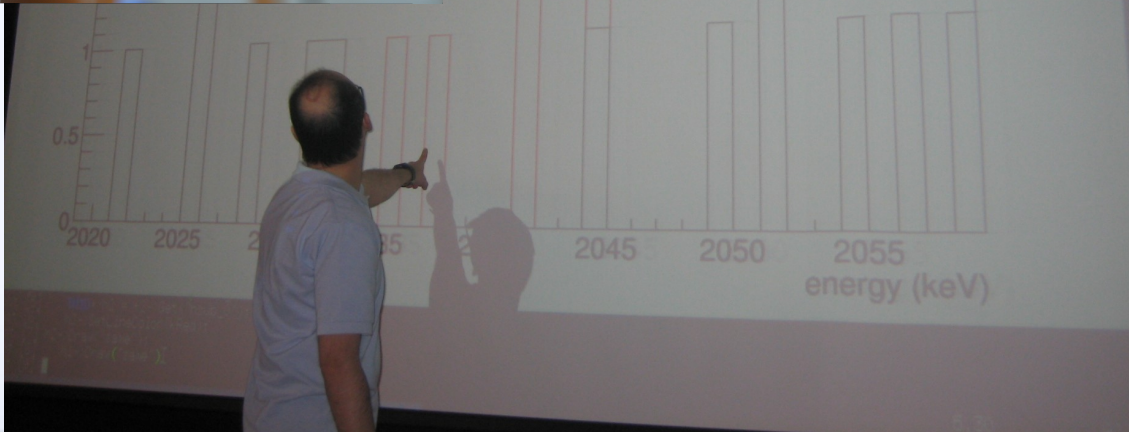
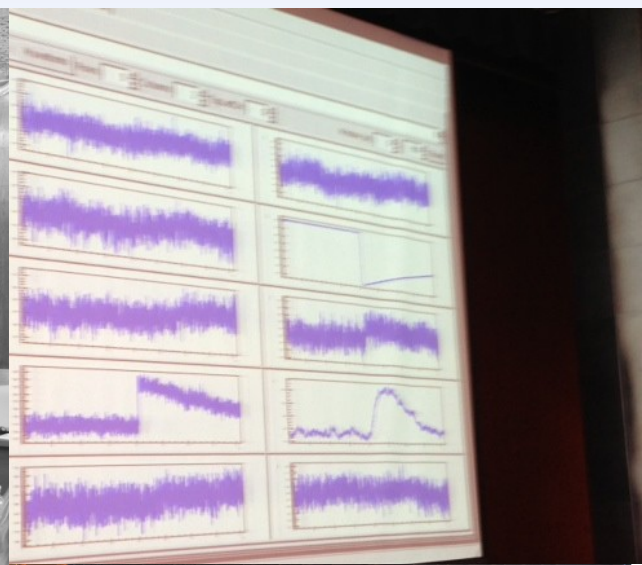
- cut based on ANN using rising part of charge pulse
- tuned using double escape peak of ^{208}Tl , $2\nu\beta\beta$, compton edge events
- background acceptance at $Q_{\beta\beta} \sim 45\%$

$$\epsilon_{\text{PSA}} = 0.90^{+0.05}_{-0.09} \text{ for SSE}$$

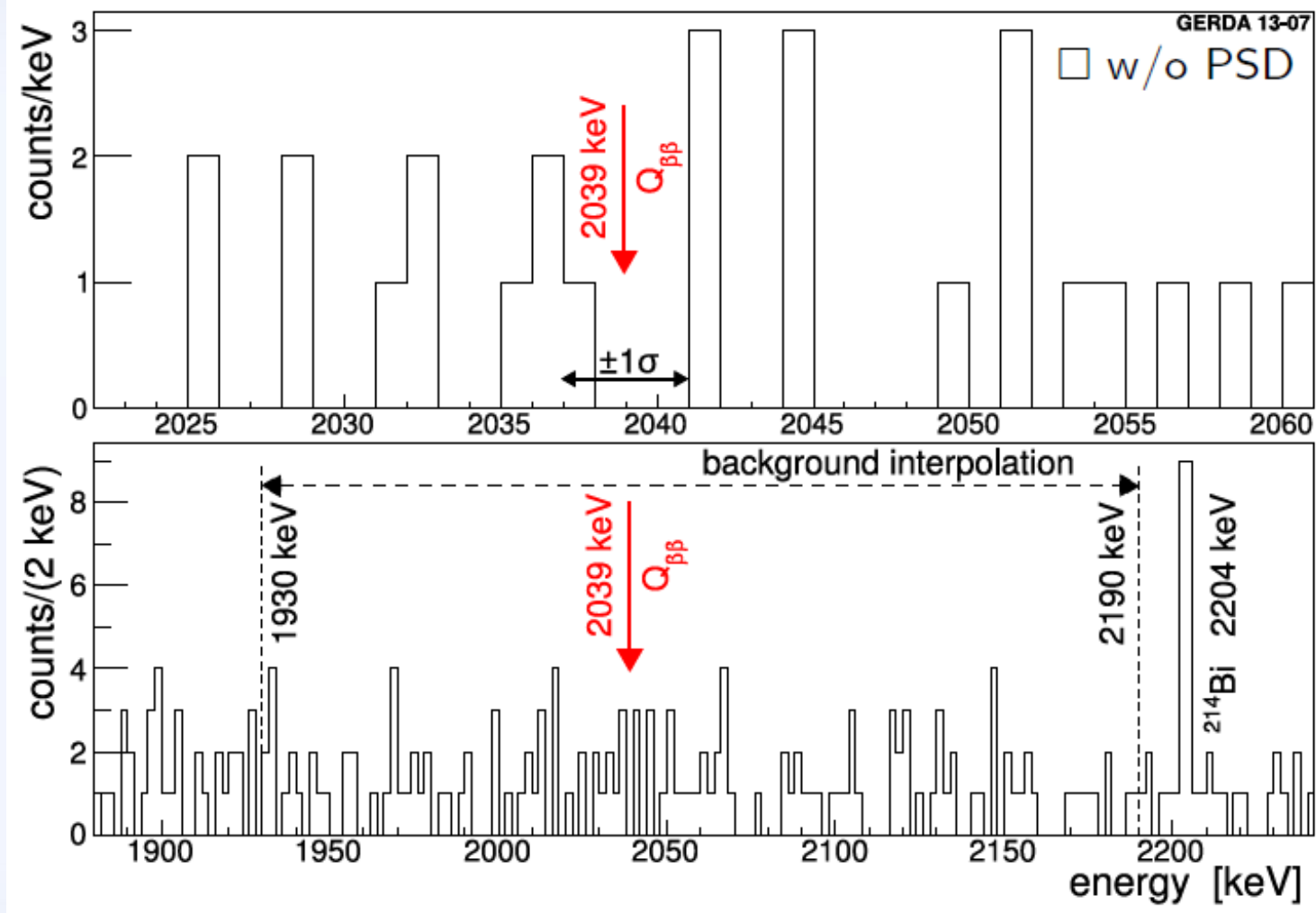
Eur.Phys.J C73 (2013) 2583

Unblinding Phase I data

At the GERDA collaboration meeting in Dubna, 12 June 2013

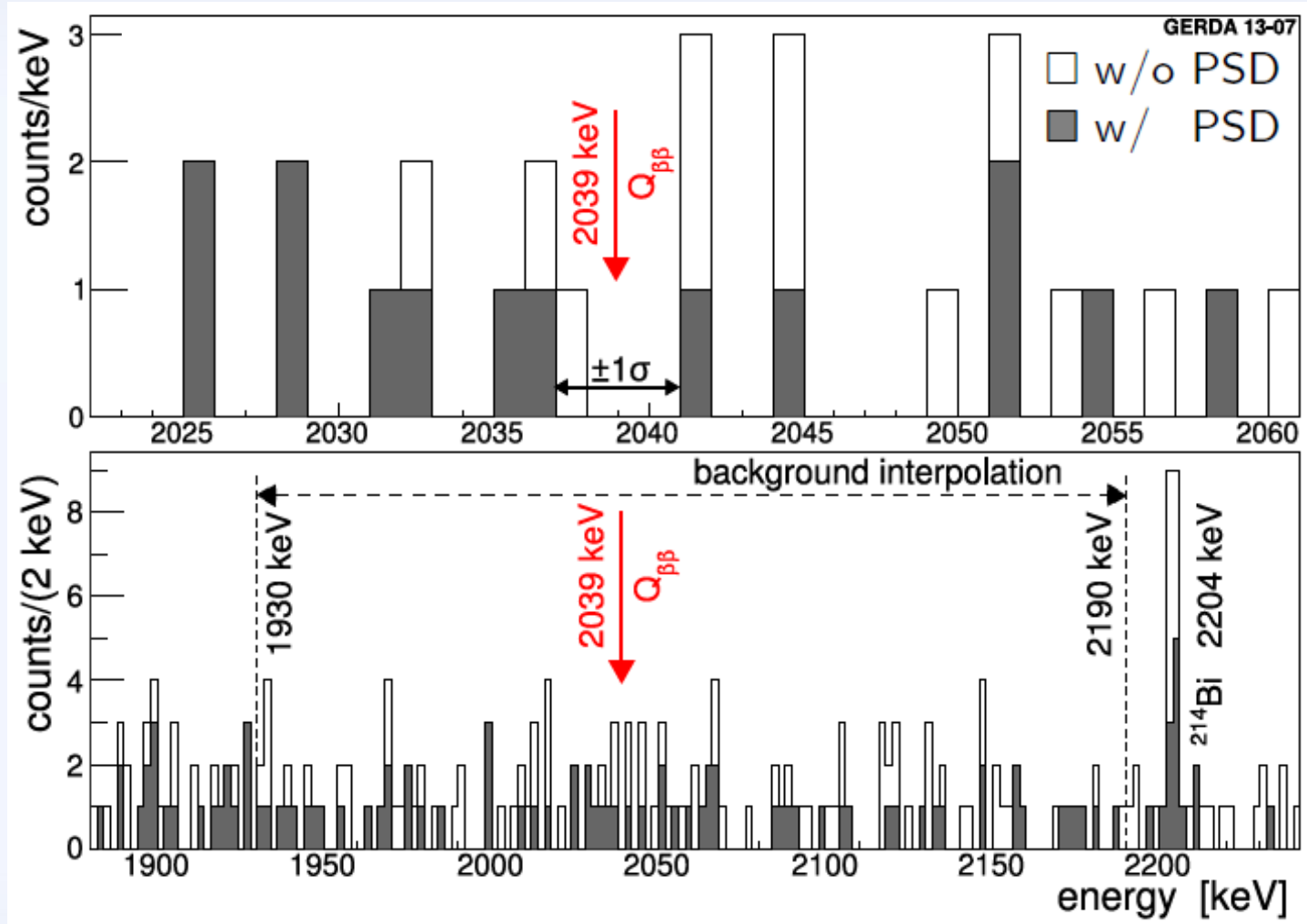


The unblinded energy spectrum



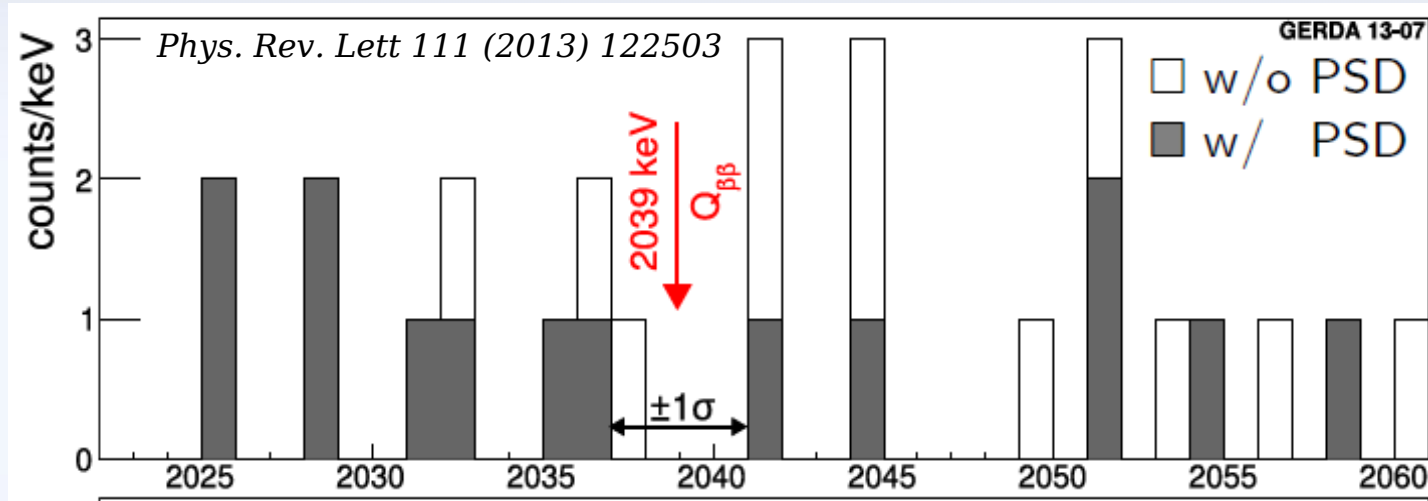
Phys. Rev. Lett 111 (2013) 122503

The unblinded energy spectrum



Phys. Rev. Lett 111 (2013) 122503

The unblinded energy spectrum

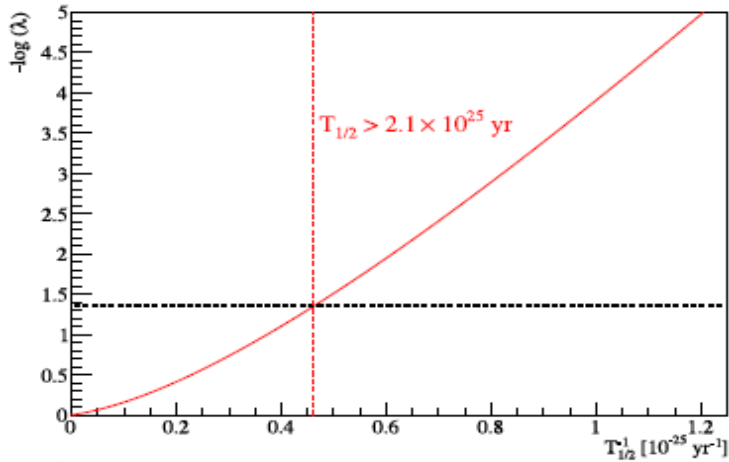


Data set	Exposure [kg·yr]	FWHM [keV]	Efficiency	BI [10^{-3} cts/(keV·kg·yr)]	Exp. counts in ($Q_{\beta\beta} \pm 5$ keV)	Obs. counts in ($Q_{\beta\beta} \pm 5$ keV)
Golden	17.3	4.8 ± 0.2	0.688 ± 0.031	18 ± 2	3.3	5
Silver	1.3	4.8 ± 0.2	0.688 ± 0.031	63^{+15}_{-14}	0.8	1
BEGe	2.4	3.2 ± 0.2	0.720 ± 0.018	42^{+10}_{-8}	1.0	1
Golden	17.3	4.8 ± 0.2	$0.619^{+0.044}_{-0.070}$	11 ± 2	2.0	2
Silver	1.3	4.8 ± 0.2	$0.619^{+0.044}_{-0.070}$	30^{+11}_{-9}	0.4	1
BEGe	2.4	3.2 ± 0.2	0.663 ± 0.022	5^{+4}_{-3}	0.1	0

Data analysis

Baseline analysis with frequentist approach (profile likelihood)

Phys. Rev. Lett 111 (2013) 122503



GERDA only

Best fit: $N^{0\nu} = 0$

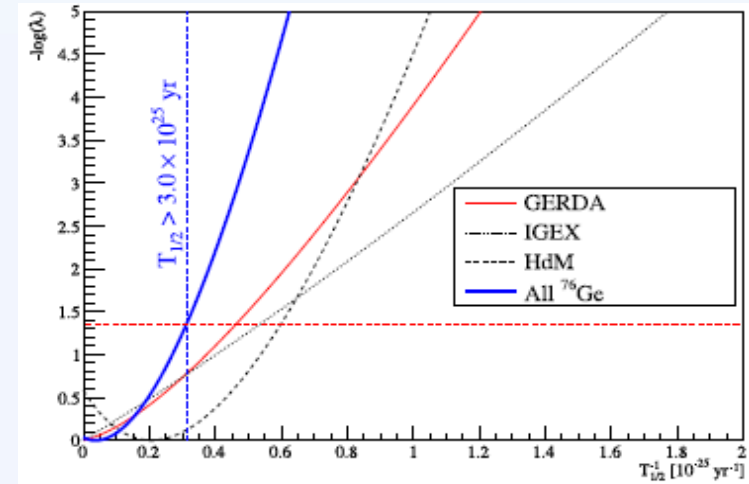
$N^{0\nu} < 3.5$ counts (90% C.L.)

$\rightarrow T_{1/2}^{0\nu} > 2.1 \cdot 10^{25}$ yr (90% C.L.)

MC Median sensitivity (for no signal):

$T_{1/2}^{0n} > 2.4 \cdot 10^{25}$ yr (90% C.L.)

- maximum likelihood spectral fit (constant+Gauss in [1930;2190] keV)
- 3 datasets
- 4 free parameters (3 constant background contributions, 1 common $T_{1/2}^{0\nu}$)
- systematic uncertainties in fit



GERDA+IGEX[1]+HdM[2]

Best fit: $N^{0\nu} = 0$

$T_{1/2}^{0\nu} > 3.0 \cdot 10^{25}$ yr (90% C.L.)

[1] *Eur. Phys. J. A* 12, 147 (2001)

[2] *Phys. Rev. D* 65, 092007 (2002)

Hypothesis test for claimed signal

Claim: $T_{1/2}^{0\nu} = 1.19^{+0.37}_{-0.23} \cdot 10^{25}$ yr [Phys. Lett. B 586 (2004) 198]

H₀: background only

Expected:

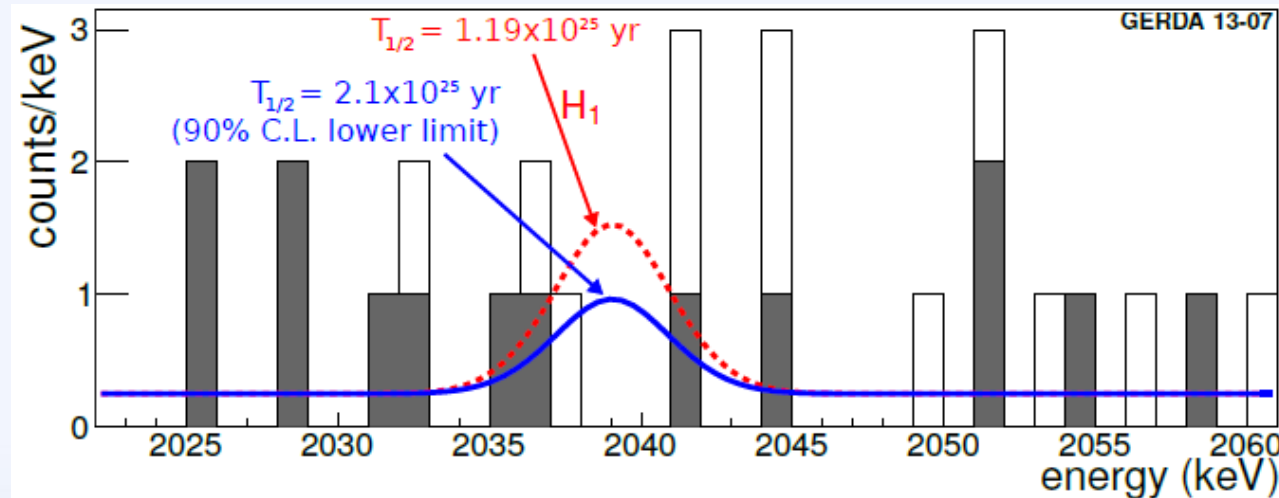
➔ 2.0 ± 0.3 background counts
in $Q_{\beta\beta} \pm 2\sigma_E$

H₁: background + signal (claim)

Expected:

➔ 2.0 ± 0.3 background counts
+ **5.9 ± 1.4 signal counts** in $Q_{\beta\beta} \pm 2\sigma_E$

Observed: 3 counts in $Q_{\beta\beta} \pm 2\sigma_E$



Phys. Rev. Lett 111 (2013) 122503

GERDA only
Profile likelihood:
 $P(N^{0\nu}=0|H_1)=0.01$
Bayes factor
 $P(H_1)/P(H_0)=0.024$

GERDA+IGEX+HdM
Bayes factor
 $P(H_1)/P(H_0)=0.0002$

Hypothesis test for claimed signal

Claim: $T_{1/2}^{0\nu} = 1.19^{+0.37}_{-0.23} \cdot 10^{25}$ yr [Phys. Lett. B 586 (2004) 198]

H₀: background only

Expected:

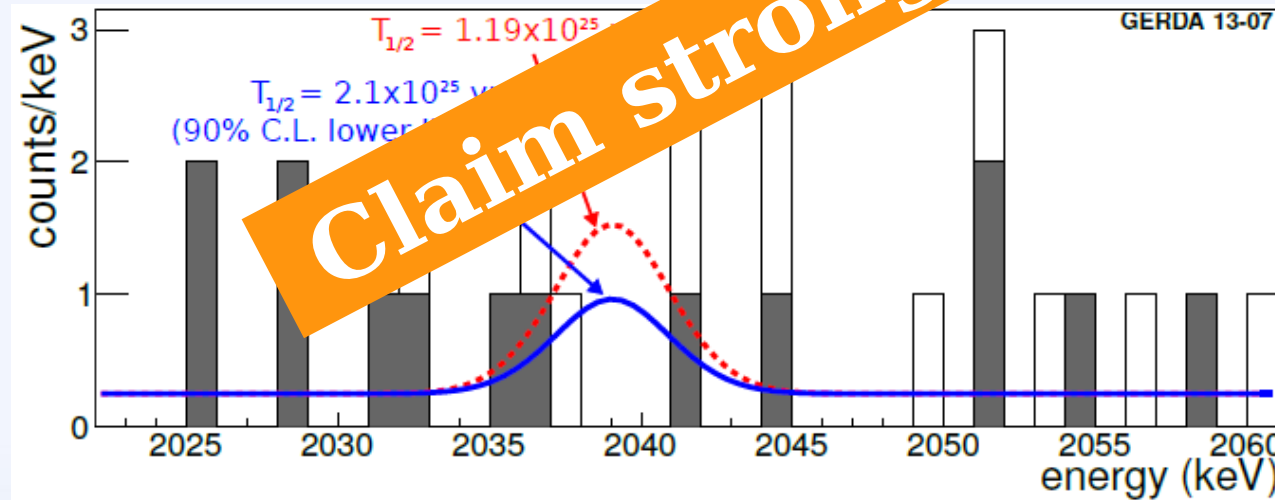
→ 2.0 ± 0.3 background counts
in $Q_{\beta\beta} \pm 2\sigma_E$

H₁: background + signal (claim)

Expected: 2.0 ± 0.3 background and counts
+ 1.0 ± 0.3 signal counts in $Q_{\beta\beta} \pm 2\sigma_E$

Observed: 3.0 ± 0.3 counts in $Q_{\beta\beta} \pm 2\sigma_E$

Claim strongly disfavoured!



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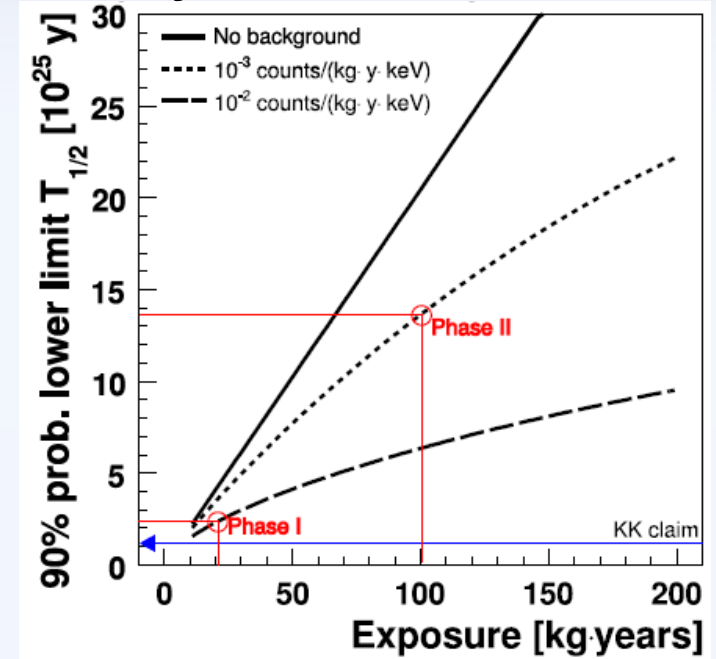
GERDA only
Profile likelihood:
 $P(N^{0\nu}=0|H_1)=0.01$
Bayes factor
 $P(H_1)/P(H_0)=0.024$

GERDA+IGEX+HdM
Bayes factor
 $P(H_1)/P(H_0)=0.0002$

Transition to Phase II

- new BEGe detectors
→ increase mass by 20 kg
- enhanced energy resolution
- enhanced background suppression
 - good PSA performance of BEGe detectors
 - detection of coincident LAr scintillation light

Phys.Rev.D75, 092003 (2006)



~35 kg of detector mass

BI $\leq 10^{-3}$ cts/(keV·kg·yr)

Improve sensitivity by one order of magnitude within 5 years

Conclusions

- GERDA Phase I collected 21.6 kg·yr of exposure
- Measurement of $2\nu\beta\beta$ with ~ 5 kg·yr: $T_{1/2}^{2\nu} = (1.84^{+0.14}_{-0.10}) \cdot 10^{21}$ yr
- Background at $Q_{\beta\beta}$ order of magnitude lower than previous experiments: 10^{-2} cts/(keV·kg·yr) after PSA
- Blind analysis results in **no positive $0\nu\beta\beta$ signal**:
 $T_{1/2}^{0\nu} > 2.1 \cdot 10^{25}$ yr (90% C.L.) with GERDA data
 $T_{1/2}^{0\nu} > 3.0 \cdot 10^{25}$ yr (90% C.L.) with GERDA+IGEX+HdM data
- **Claim from *Phys. Lett. B 586 (2004) 198* strongly disfavored**, in a model-independent way

Additional material

Previous measurements and claim

Previous $0\nu\beta\beta$ experiments

	HdM	IGEX
Location	LNGS	Homestake, Baksan, Canfranc
Exposure [kg·yr]	71.1	8.8
Bg [cts/(keV·kg·yr)]	≥ 0.11	0.17
$T_{1/2}$ limit (90% CL) [yr]	$1.9 \cdot 10^{25}$ [1]	$1.6 \cdot 10^{25}$ [2]

[1] *Eur. Phys. J. A12*, 147-154 (2001)

[2] *Phys. Rev. D 65*, 092007 (2002)

Claim of signal from part of HdM:

$$T_{1/2} (^{76}\text{Ge}) = 1.19^{+0.37}_{-0.23} \cdot 10^{25} \text{ yr} \quad \textit{Phys. Lett. B 586, 198-212 (2004)}$$

HdM claim

Data acquisition and analysis of the ^{76}Ge double beta experiment in Gran Sasso 1990-2003
 H.V. Klapdor-Kleingrothaus^{*1}, A. Dietz, I.V. Krivosheina², O. Chkvolets

Phys. Lett. B 586, 198-212 (2004)
 BI 0.11 cts / (keV·kg·yr)

28.75 ± 6.87 events (bgd: ~ 60)

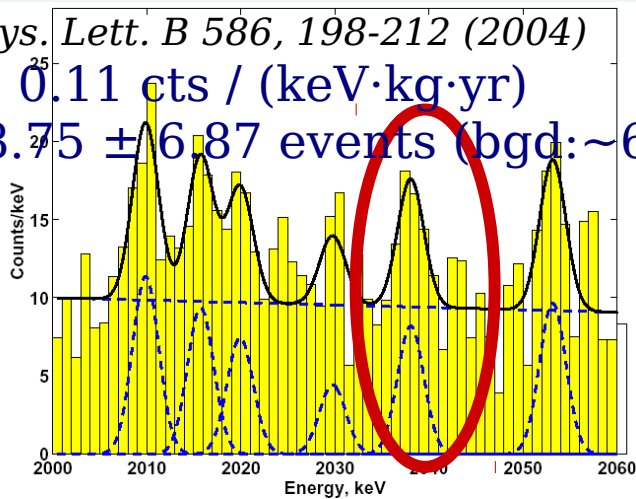


Fig. 17. The total sum spectrum of all five detectors (in total 10.96 kg enriched in ^{76}Ge), for the period November 1990–May 2003 (71.7 kg year) in the range 2000–2060 keV and its fit (see Section 3.2).

- Nov 1990 - May 2003
- 71.7 kg·yr
- $4.2\sigma/6\sigma$ evidence for $0\nu\beta\beta$

● $(0.69 - 4.18) \cdot 10^{25}$ yr (3σ)

Best fit: $1.19 \cdot 10^{25}$ yr

Phys. Lett. B 586, 198-212 (2004)

$2.23^{+0.44}_{-0.31} \cdot 10^{25}$ yr

Mod. Phys. Lett. A 21, 1547-1566 (2006)

Criticism in *Ann. Phys.* 525, 269-280 (2013):

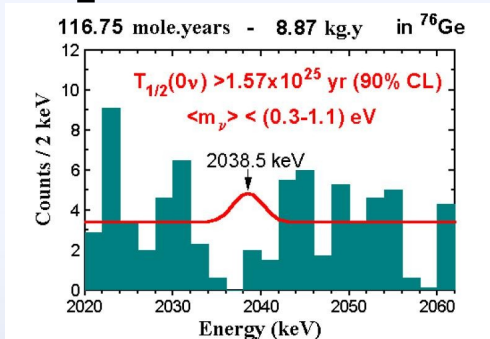
Mainly: missing efficiency correction, uncertainty on signal counts smaller than Poissonian

● $m_{\beta\beta} = (0.24-0.58)$ eV

(best fit 0.44 eV) /

0.32 ± 0.03 eV

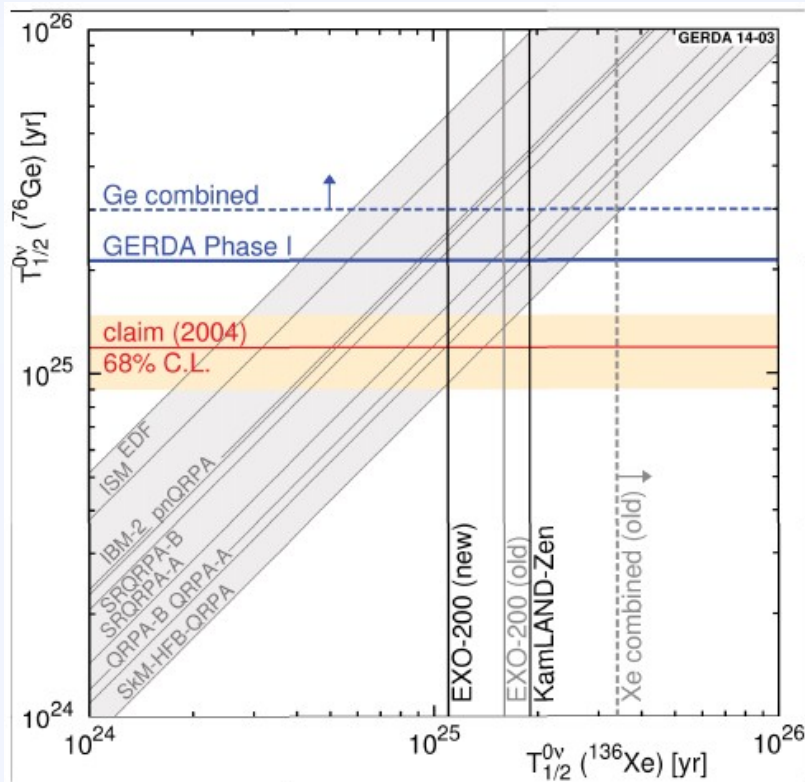
Comparison: IGEX



Note: statistical significance depends on background model!

Comparison with ^{136}Xe experiments

Phys. Rev. Lett 111 (2013) 122503



Premise: leading mechanism is exchange of light neutrino

NME calculations:

Phys. Rev. D 88 (2013) 091301

EXO-200 (new):

Nature 510 (2014) 229

KamLAND-Zen:

Phys. Rev. Lett. 110 (2013), 062502

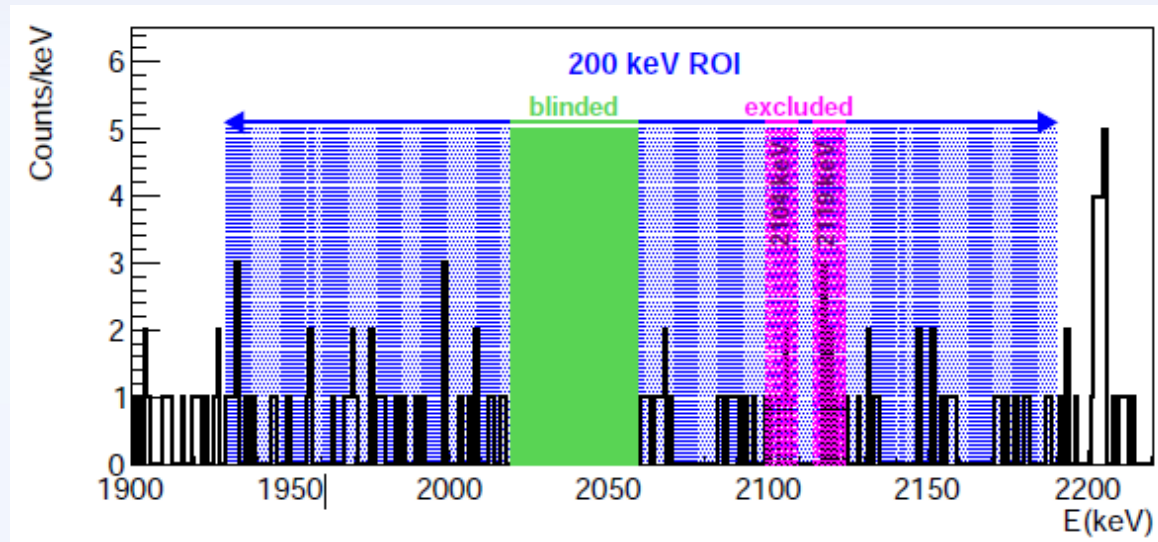
^{136}Xe combined using the latest results (not shown on the plot):

$T_{1/2}^{0\nu} > 2.2 \cdot 10^{25}$ yr (90% C.L.)

arXiv:1404.2616

BI definition

Definition of BI



BI (10^{-3} cts/(keV·kg·yr)) after partial unblinding:

	Before PSA	After PSA
Golden:	$18.5^{+2.3}_{-2.2}$	$10.9^{+1.9}_{-1.6}$
Silver:	$63.4^{+18.0}_{-14.3}$	$30.1^{+13.7}_{-9.8}$
BEGe sum:	$41.3^{+10.4}_{-8.4}$	$5.4^{+5.2}_{-2.9}$

Germanium for the search of $0\nu\beta\beta$

Searching in ^{76}Ge

$$S \sim \epsilon \cdot f \cdot \sqrt{\frac{M \cdot t_{\text{run}}}{\text{BI} \cdot \Delta E}}$$

S: sensitivity

ϵ : efficiency

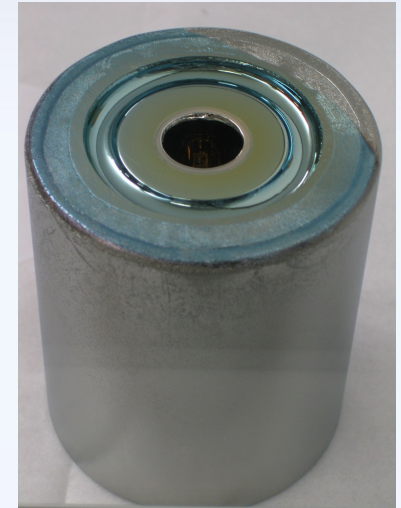
f: abundance of $0\nu\beta\beta$ isotope

M: detector mass

t_{run} : measurement time

BI: background index

ΔE : energy resolution at $Q_{\beta\beta}$



Germanium detector

Advantages of Germanium:

- **High ϵ** : Source = Detector
- **Small intrinsic BI**: High purity Ge
- **Excellent ΔE** : FWHM \sim (0.1-0.2)%
- Well-established technology

Disadvantages of Germanium:

- **High external BI**: $Q_{\beta\beta} = 2039\text{keV}$
- **Small f of ^{76}Ge** :
7.8% \rightarrow Enrichment needed!
- Limited sources of crystal & detector manufacturers
- Small $G^{0\nu}(Q_{\beta\beta}, Z)$

Pulse Shape Analysis

Pulse shape analysis in ROI

Data set	Detector	E (keV)	Date	Passed PSA
golden	ANG5	2041.8	Nov 18, 2011 22:52	–
silver	ANG5	2036.9	Jun 23, 2012 23:02	✓
golden	RG2	2041.3	Dec 16, 2012 00:09	✓
BEGe	GD32B	2036.6	Dec 28, 2012 09:50	–
golden	RG1	2035.5	Jan 29, 2013 03:35	✓
golden	ANG3	2037.4	Mar 2, 2013 08:08	–
golden	RG1	2041.7	Apr 27, 2013 22:21	–

Decays

Decay chains

^{238}U chain

Nuclide	mode	$T_{1/2}$	Q-value (keV)	decay product	E_γ (keV)
^{238}U	α	$4.5 \cdot 10^9$ yr	4270.0	^{234}Th	–
^{234}Th	β	24.1 d	273.0	$^{234\text{m}}\text{Pa}$	–
$^{234\text{m}}\text{Pa}$	β	1.2 min	2195.0	^{234}U	–
^{234}U	α	$2.5 \cdot 10^5$ yr	4858.5	^{230}Th	–
^{230}Th	α	$7.5 \cdot 10^4$ yr	2770.0	^{226}Ra	–
^{226}Ra	α	$1.6 \cdot 10^3$ yr	4870.6	^{222}Rn	–
^{222}Rn	α	3.8 d	5590.3	^{218}Po	–
^{218}Po	α	3.1 min	6114.7	^{214}Pb	–
^{214}Pb	β	26.8 min	1024.0	^{214}Bi	351.9
^{214}Bi	β	19.9 min	3272.0	^{214}Po	609.3
					768.4
					1120.3
					1238.1
					1764.5
					2204.2
^{214}Po	α	$164.3 \mu\text{s}$	7833.5	^{210}Pb	–
^{210}Pb	β	22.3 yr	63.5	^{210}Bi	–
^{210}Bi	β	5.0 d	1162.1	^{210}Po	–
^{210}Po	α	138.4 d	5407.5	^{206}Pb	–

^{232}Th chain

Nuclide	mode	$T_{1/2}$	Q-value (keV)	decay product	E_γ (keV)
^{232}Th	α	$1.4 \cdot 10^{10}$ yr	4082.8	^{228}Ra	–
^{228}Ra	β	5.8 yr	45.9	^{228}Ac	–
^{228}Ac	β	6.2 h	2127.0	^{228}Th	911.2
					969.0
^{228}Th	α	1.9 yr	5520.1	^{224}Ra	–
^{224}Ra	α	3.7 d	5788.9	^{220}Rn	–
^{220}Rn	α	55.6 s	6404.7	^{216}Po	–
^{216}Po	α	0.1 s	6906.5	^{212}Pb	–
^{212}Pb	β	10.6 h	573.8	^{212}Bi	–
^{212}Bi	$\beta /$	60.6 min	2254.0 /	$^{212}\text{Po} /$	727.3
	α		6207.1	^{208}Tl	
^{212}Po	α	$0.3 \mu\text{s}$	8954.1	^{208}Pb	–
^{208}Tl	β	3.1 min	5001.0	^{208}Pb	510.8
					583.2
					860.6
					2614.5

^{42}Ar : β (599 keV, 33 yr) \rightarrow ^{42}K : β (3525.4 keV, 1524.7 keV photon, 12 h)

^{40}K : $\beta/\beta^++\text{ec}$ (1311.1/1504.9 keV, 1460.8 keV photon, $1.3 \cdot 10^9$ yr)

^{60}Co : β (2823.9 keV, 1173.3 keV & 1332.5 keV photon, 5.3 yr)

^{68}Ge : ec (106.0 keV, 270 d) \rightarrow ^{68}Ga : $\text{ec}+\beta^+$ (2921.1 keV, 1077.4 keV photon, 67.6 min)

Neutrino properties

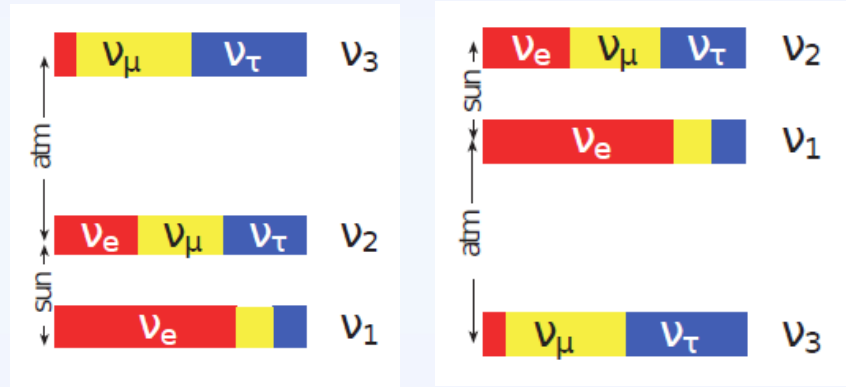
Neutrino properties

Neutrino Mixings

Weakly interacting and mass eigenstates are independent basis

$$\begin{bmatrix} |\nu_e\rangle \\ |\nu_\mu\rangle \\ |\nu_\tau\rangle \end{bmatrix} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{bmatrix} \begin{bmatrix} |m_1\rangle \\ |m_2\rangle \\ |m_3\rangle \end{bmatrix}$$

$$U_{\nu i} = \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{13}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{13}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{13}} & s_{23}c_{13} \\ s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{13}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{13}} & c_{23}c_{13} \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & e^{i\frac{\alpha_{21}}{2}} & 0 \\ 0 & 0 & e^{i\frac{\alpha_{31}}{2}} \end{bmatrix}$$



What we know:

- $m_2^2 - m_1^2 = \Delta m_{\text{sun}}^2$
- $m_2^2 - m_1^2 = \Delta m_{\text{atm}}^2$
- $\theta_{12} = \theta_{\text{sun}}$
- $\theta_{23} = \theta_{\text{atm}}$
- θ_{13}

What we do not know:

- Absolute mass scale
- Mass hierarchy
- Phases ($\delta_{13}, \alpha_{21}, \alpha_{31}$)
- Nature of the neutrino mass (Dirac or Majorana)
- CP violation in lepton sector?

parameter	best fit [1σ range]
$\Delta m_{21}^2 (10^{-5} \text{eV}^2)$	7.62 [7.43, 7.81]
$\Delta m_{31}^2 (10^{-3} \text{eV}^2)$	2.55 [2.46, 2.61]
	-2.43 [-2.37, -2.50]
$\sin^2 \theta_{12}$	0.320 [0.303, 0.336]
$\sin^2 \theta_{23}$	0.613 [0.573, 0.635]
	0.600 [0.569, 0.626]
$\sin^2 \theta_{13}$	0.0246 [0.0218, 0.0275]
	0.0250 [0.0223, 0.0276]